Supplementary Material

for

"A practical approach to designing partial-profile choice experiments with two alternatives for estimating main effects and interactions of many two-level attributes" by Heiko Großmann

The supplementary material presents for Example 3 of the paper the position arrays \mathcal{B}_1 and \mathcal{B}_2 which are derived from the annotated position array \mathcal{B}_2^* in Section 3 of the paper. Furthermore, the design that can be constructed by using these position arrays and which was not shown in Section 4 of the paper is given in this document.

In Example 3, there are K = 11 two-level attributes. The profile strength is S = 4 and the comparison depth is d = 2. The position arrays \mathcal{B}_1 and \mathcal{B}_2 that are obtained from the annotated position array \mathcal{B}_2^* in equation (9) of the paper are

and

Example 3 was revisited in Section 4. There it was mentioned that by using the position arrays \mathcal{B}_1 and \mathcal{B}_2 given above and the matrices

$$\mathbf{A} = \mathbf{H}_2 = \begin{pmatrix} +1 & +1 \\ +1 & -1 \end{pmatrix}$$
 and $\mathbf{F} = \begin{pmatrix} -1 & -1 \\ -1 & +1 \\ +1 & -1 \\ +1 & +1 \end{pmatrix}$

a partial-profile design with N=120 pairs and a D-efficiency of ${\rm eff}_D=97.77$ can be generated. This design is shown in the following Table 1.

Table 1: Partial-profile design in Example 3 for K=11 two-level attributes, profile strength S=4, comparison depth d=2 with N=120 pairs

	I		Al	terna	tive 1	(s =	$(s_1,$	\dots, s_1	1))					Al	terna	tive 2	(t =	$(t_1,$	\ldots, t_1	1))		
Pair	s_1	s_2	s_3	s_4	s_5	s_6	s_7	s_8	s_9	s_{10}	s_{11}	t_1	t_2	t_3	t_4	t_5	t_6	t_7	t_8	t_9	t_{10}	t_{11}
1	1	1	-1	-1	0	0	0	0	0	0	0	-1	-1	-1	-1	0	0	0	0	0	0	0
2	1	-1	-1	-1	0	0	0	0	0	0	0	-1	1	-1	-1	0	0	0	0	0	0	0
3	1	1	-1	1	0	0	0	0	0	0	0	-1	-1	-1	1	0	0	0	0	0	0	0
4 5	1 1	$-1 \\ 1$	$-1 \\ 1$	-1	0	0	0	0	0	0	0 0	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	-1	$-1 \\ 1$	-1	0	0	0	0	0	0	0
6	1	-1	1	-1	0	0	0	0	0	0	0	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	1	1	-1	0	0	0	0	0	0	0
7	1	1	1	1	0	0	0	0	0	0	0	-1	-1	1	1	0	0	0	0	0	0	0
8	1	-1	1	1	0	0	0	0	0	0	0	-1	1	1	1	0	0	0	0	0	0	0
9	1	-1	0	0	1	-1	0	0	0	0	0	-1	-1	0	0	-1	-1	0	0	0	0	0
10	1	-1	0	0	-1	-1	0	0	0	0	0	-1	-1	0	0	1	-1	0	0	0	0	0
11	1	-1	0	0	1	1	0	0	0	0	0	-1	-1	0	0	-1	1	0	0	0	0	0
12 13	1 1	$-1 \\ 1$	0	0	$-1 \\ 1$	-1	0	0	0	0	0	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	$-1 \\ 1$	0	0	-1	$1 \\ -1$	0	0	0	0	0
14	1	1	0	0	-1	-1	0	0	0	0	0	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	1	0	0	1	-1	0	0	0	0	0
15	1	1	0	0	1	1	0	0	0	0	0	-1	1	0	0	-1	1	0	0	0	0	0
16	1	1	0	0	-1	1	0	0	0	0	0	-1	1	0	0	1	1	0	0	0	0	0
17	-1	0	0	0	1	0	1	-1	0	0	0	-1	0	0	0	-1	0	-1	-1	0	0	0
18	-1	0	0	0	1	0	-1	-1	0	0	0	-1	0	0	0	-1	0	1	-1	0	0	0
19	-1	0	0	0	1	0	1	1	0	0	0	-1	0	0	0	-1	0	-1	1	0	0	0
$\frac{20}{21}$	$\begin{vmatrix} -1 \\ 1 \end{vmatrix}$	0	0	0	1 1	0	$-1 \\ 1$	-1	0	0	0	$\begin{vmatrix} -1 \\ 1 \end{vmatrix}$	0	0	0	$-1 \\ -1$	0	-1	-1	0	0	0 0
22	1	0	0	0	1	0	-1	-1	0	0	0	1	0	0	0	-1	0	1	$-1 \\ -1$	0	0	0
23	1	0	0	0	1	0	1	1	0	0	0	1	0	0	0	-1	0	-1	1	0	0	0
24	1	0	0	0	1	0	-1	1	0	0	0	1	0	0	0	-1	0	1	1	0	0	0
25	-1	-1	0	0	0	0	0	1	1	0	0	-1	-1	0	0	0	0	0	-1	-1	0	0
26	-1	-1	0	0	0	0	0	1	-1	0	0	-1	-1	0	0	0	0	0	-1	1	0	0
27	-1	1	0	0	0	0	0	1	1	0	0	-1	1	0	0	0	0	0	-1	-1	0	0
28	$\begin{vmatrix} -1 \\ 1 \end{vmatrix}$	1	0	0	0	0	0	1	-1	0	0	-1	1	0	0	0	0	0	-1	1	0	0
29 30	1 1	$-1 \\ -1$	0	0	0	0	0	1 1	$\begin{array}{c} 1 \\ -1 \end{array}$	0	0 0	$\begin{vmatrix} 1 \\ 1 \end{vmatrix}$	$-1 \\ -1$	0	0	0	0	0	$-1 \\ -1$	$-1 \\ 1$	0	0
31	1	1	0	0	0	0	0	1	1	0	0	1	1	0	0	0	0	0	-1	-1	0	0
32	1	1	0	0	0	0	0	1	-1	0	0	1	1	0	0	0	0	0	-1	1	0	0
33	1	1	0	0	0	0	0	0	0	-1	-1	-1	-1	0	0	0	0	0	0	0	-1	-1
34	1	-1	0	0	0	0	0	0	0	-1	-1	-1	1	0	0	0	0	0	0	0	-1	-1
35	1	1	0	0	0	0	0	0	0	-1	1	-1	-1	0	0	0	0	0	0	0	-1	1
$\frac{36}{37}$	1 1	$-1 \\ 1$	0	0	0	0	0	0	0	$-1 \\ 1$	$\begin{array}{c} 1 \\ -1 \end{array}$	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	-1	0	0	0	0	0	0	0	$-1 \\ 1$	$\begin{array}{c} 1 \\ -1 \end{array}$
38	1	-1	0	0	0	0	0	0	0	1	-1	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	1	0	0	0	0	0	0	0	1	-1
39	1	1	0	0	0	0	0	0	0	1	1	-1	-1	0	0	0	0	0	0	0	1	1
40	1	-1	0	0	0	0	0	0	0	1	1	-1	1	0	0	0	0	0	0	0	1	1
41	0	1	0	0	0	-1	-1	0	1	0	0	0	-1	0	0	0	-1	-1	0	-1	0	0
42	0	1	0	0	0	-1	-1	0	-1	0	0	0	-1	0	0	0	-1	-1	0	1	0	0
43	0	1	0	0	0	-1	1	0	1	0	0	0	-1	0	0	0	-1	1	0	-1	0	0
$\frac{44}{45}$	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	1 1	0	0	0	$-1 \\ 1$	$\begin{array}{c} 1 \\ -1 \end{array}$	0	$-1 \\ 1$	0	0 0	0	$-1 \\ -1$	0	0	0	$-1 \\ 1$	-1	0	$\begin{array}{c} 1 \\ -1 \end{array}$	0	0
46	0	1	0	0	0	1	-1	0	-1	0	0	0	-1	0	0	0	1	-1	0	1	0	0
47	0	1	0	0	0	1	1	0	1	0	0	0	-1	0	0	0	1	1	0	-1	0	0
48	0	1	0	0	0	1	1	0	-1	0	0	0	-1	0	0	0	1	1	0	1	0	0
49	0	0	1	1	-1	-1	0	0	0	0	0	0	0	-1	-1	-1	-1	0	0	0	0	0
50	0	0	1	-1	-1	-1	0	0	0	0	0	0	0	-1	1	-1	-1	0	0	0	0	0
51	0	0	1	1	-1	1	0	0	0	0	0	0	0	-1	-1	-1	1	0	0	0	0	0
52 53	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	1	$-1 \\ 1$	$-1 \\ 1$	-1	0	0	0	0	0 0	0	0	$-1 \\ -1$	-1	$-1 \\ 1$	$\frac{1}{-1}$	0	0	0	0	0
54	0	0	1	-1	1	-1	0	0	0	0	0	0	0	-1	1	1	-1	0	0	0	0	0
55	0	0	1	1	1	1	0	0	0	0	0	0	0	-1	-1	1	1	0	0	0	0	0
56	0	0	1	-1	1	1	0	0	0	0	0	0	0	-1	1	1	1	0	0	0	0	0
57	0	0	1	-1	0	0	-1	0	0	1	0	0	0	-1	-1	0	0	-1	0	0	-1	0
58	0	0	1	-1	0	0	-1	0	0	-1	0	0	0	-1	-1	0	0	-1	0	0	1	0
59	0	0	1	-1	0	0	1	0	0	1	0	0	0	-1	-1	0	0	1	0	0	-1	0
60	0	0	1	-1	0	0	1	0	0	-1	0	0	0	-1	-1	0	0	1	0	0	1	0

Table 1: Partial-profile design in Example 3 for K=11 two-level attributes, profile strength S=4, comparison depth d=2 with N=120 pairs (continued)

	Alternative 1 ($\mathbf{s} = (s_1, \dots, s_{11})$)									Alternative 2 ($\mathbf{t} = (t_1, \dots, t_{11})$)												
Pair	s_1	s_2	s_3	s_4	s_5	s_6	87	s_8	s ₉	s_{10}	s_{11}	t_1	t_2	t_3	t_4	t_5	t_6	t_7	t_8	t_9	t_{10}	t_{11}
61	0	0	1	1	0	0	-1	0	0	1	0	0	0	-1	1	0	0	-1	0	0	-1	0
62	0	0	1	1	0	0	-1	0	0	-1	0	0	0	-1	1	0	0	-1	0	0	1	0
63 64	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	1 1	$\frac{1}{1}$	0	0	1 1	0 0	0	$\begin{array}{c} 1 \\ -1 \end{array}$	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	$-1 \\ -1$	1 1	0	0	1 1	0	0	$-1 \\ 1$	0
65	0	0	1	0	0	0	0	-1	-1	1	0	0	0	$-1 \\ -1$	0	0	0	0	-1	-1	-1	0
66	0	0	1	0	0	0	0	-1	-1	-1	0	0	0	-1	0	0	0	0	-1	-1	1	0
67	0	0	1	0	0	0	0	-1	1	1	0	0	0	-1	0	0	0	0	-1	1	-1	0
68	0	0	1	0	0	0	0	-1	1	-1	0	0	0	-1	0	0	0	0	-1	1	1	0
69	0	0	1	0	0	0	0	1	-1	1	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	-1	0	0	0	0	1	-1	-1	0
70 71	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	1 1	0	0	0	0	1 1	$-1 \\ 1$	$-1 \\ 1$	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	$-1 \\ -1$	0	0	0	0	1 1	$-1 \\ 1$	$\begin{array}{c} 1 \\ -1 \end{array}$	0
72	0	0	1	0	0	0	0	1	1	-1	0	0	0	-1	0	0	0	0	1	1	1	0
73	0	0	-1	0	-1	0	0	0	0	1	1	0	0	-1	0	-1	0	0	0	0	-1	-1
74	0	0	-1	0	-1	0	0	0	0	1	-1	0	0	-1	0	-1	0	0	0	0	-1	1
75	0	0	-1	0	1	0	0	0	0	1	1	0	0	-1	0	1	0	0	0	0	-1	-1
76	0	0	-1	0	1	0	0	0	0	1	-1	0	0	-1	0	1	0	0	0	0	-1	1
77 78	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	1 1	0	$-1 \\ -1$	0	0	0	0	1 1	$\begin{array}{c} 1 \\ -1 \end{array}$	0	0	1 1	0	$-1 \\ -1$	0	0	0	0	$-1 \\ -1$	$-1 \\ 1$
79	0	0	1	0	-1 1	0	0	0	0	1	-1 1	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	1	0	-1 1	0	0	0	0	-1	-1
80	0	0	1	0	1	0	0	0	0	1	-1	0	0	1	0	1	0	0	0	0	-1	1
81	0	0	0	1	0	1	0	-1	0	0	-1	0	0	0	-1	0	-1	0	-1	0	0	-1
82	0	0	0	1	0	-1	0	-1	0	0	-1	0	0	0	-1	0	1	0	-1	0	0	-1
83	0	0	0	1	0	1	0	-1	0	0	1	0	0	0	-1	0	-1	0	-1	0	0	1
84	0	0	0	1	0	-1	0	-1	0	0	1	0	0	0	-1	0	1	0	-1	0	0	1
85 86	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	0	$\frac{1}{1}$	0	-1	0	1 1	0	0	$-1 \\ -1$	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	$-1 \\ -1$	0	$-1 \\ 1$	0	1 1	0	0	$-1 \\ -1$
87	0	0	0	1	0	1	0	1	0	0	-1 1	0	0	0	-1	0	-1	0	1	0	0	1
88	0	0	0	1	0	-1	0	1	0	0	1	0	0	0	-1	0	1	0	1	0	0	1
89	0	0	0	1	1	0	-1	0	-1	0	0	0	0	0	-1	-1	0	-1	0	-1	0	0
90	0	0	0	1	-1	0	-1	0	-1	0	0	0	0	0	-1	1	0	-1	0	-1	0	0
91	0	0	0	1	1	0	-1	0	1	0	0	0	0	0	-1	-1	0	-1	0	1	0	0
92 93	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	0	$\frac{1}{1}$	$-1 \\ 1$	0	$-1 \\ 1$	0	$\begin{array}{c} 1 \\ -1 \end{array}$	0	0	0	0	0	$-1 \\ -1$	-1	0	$-1 \\ 1$	0	$-1 \\ -1$	0	0
93 94	0	0	0	1	-1	0	1	0	$-1 \\ -1$	0	0	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	-1	-1 1	0	1	0	-1	0	0
95	0	0	0	1	1	0	1	0	1	0	0	0	0	0	-1	-1	0	1	0	1	0	0
96	0	0	0	1	-1	0	1	0	1	0	0	0	0	0	-1	1	0	1	0	1	0	0
97	0	0	0	0	0	1	-1	0	0	-1	1	0	0	0	0	0	-1	-1	0	0	-1	-1
98	0	0	0	0	0	1	-1	0	0	-1	-1	0	0	0	0	0	-1	-1	0	0	-1	1
99	0	0	0	0	0	1	-1	0	0	1	1	0	0	0	0	0	-1	-1	0	0	1	-1
100 101	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	0	0	0	1 1	$-1 \\ 1$	0	0	$\begin{array}{c} 1 \\ -1 \end{array}$	$-1 \\ 1$	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	0	0	$-1 \\ -1$	$-1 \\ 1$	0	0	$-1 \\ -1$	$\begin{array}{c} 1 \\ -1 \end{array}$
102	0	0	0	0	0	1	1	0	0	-1	-1	0	0	0	0	0	-1	1	0	0	-1	1
103	0	0	0	0	0	1	1	0	0	1	1	0	0	0	0	0	-1	1	0	0	1	-1
104	0	0	0	0	0	1	1	0	0	1	-1	0	0	0	0	0	-1	1	0	0	1	1
105	0	0	0	0	0	1	0	1	-1	0	-1	0	0	0	0	0	-1	0	-1	-1	0	-1
106	0	0	0	0	0	1	0	-1	-1	0	-1	0	0	0	0	0	-1	0	1	-1	0	-1
$\frac{107}{108}$	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	0	0	0 0	1 1	0 0	$\begin{array}{c} 1 \\ -1 \end{array}$	$-1 \\ -1$	0	1 1	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	0	0	$-1 \\ -1$	0	$-1 \\ 1$	$-1 \\ -1$	0	1 1
109	0	0	0	0	0	1	0	1	1	0	-1	0	0	0	0	0	$-1 \\ -1$	0	-1	1	0	-1
110	0	0	0	0	0	1	0	-1	1	0	-1	0	0	0	0	0	-1	0	1	1	0	-1
111	0	0	0	0	0	1	0	1	1	0	1	0	0	0	0	0	-1	0	-1	1	0	1
112	0	0	0	0	0	1	0	-1	1	0	1	0	0	0	0	0	-1	0	1	1	0	1
113	0	0	0	0	0	0	1	0	1	-1	-1	0	0	0	0	0	0	-1	0	-1	-1	-1
114	0	0	0	0	0	0	1	0	-1	-1	-1	0	0	0	0	0	0	-1	0	1	-1	-1
$\frac{115}{116}$	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	0	0	0	0 0	0	1 1	0	$-1 \\ -1$	$-1 \\ -1$	1 1	$\begin{bmatrix} 0 \\ 0 \end{bmatrix}$	0	0	0	0	0	$-1 \\ -1$	0	$-1 \\ 1$	$-1 \\ -1$	1 1
117	0	0	0	0	0	0	1	0	-1 1	-1 1	-1	0	0	0	0	0	0	$-1 \\ -1$	0	-1	1	-1
118	0	0	0	0	0	0	1	0	-1	1	-1	0	0	0	0	0	0	-1	0	1	1	-1
119	0	0	0	0	0	0	1	0	1	1	1	0	0	0	0	0	0	-1	0	-1	1	1
120	0	0	0	0	0	0	1	0	-1	1	1	0	0	0	0	0	0	-1	0	1	1	1