

Artificial Intelligence Lab Report



Submitted by

Rushi Hundiwala(1BM21CS224)

Course: Artificial Intelligence

Course Code: 24CS5PCAIN

Sem & Section: 5D

**BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING**



**B. M. S. COLLEGE OF ENGINEERING
(Autonomous Institution under
VTU) BENGALURU-560019
2023-2024**

Table of contents

Program Number	Program Title	Page Number
1	Tic-Tac-Toe Game	1-9
2	8 Puzzle BFS and DFS	10-23
3	Iterative Deepening Search	24-28
4	Vacuum Cleaner Agent	29-35
5	A* Search Algorithm Hill Climbing Algorithm	36-61
6	Simulated Annealing	62-68
7	Knowledge Base using prepositional logic	69-70
8	Unification in FOL	79-84
9	Forward Reasoning	88-92
10	Alpha Beta Pruning	93-96

Program 1 - Tic Tac toe

Algorithm

LAB-1

TIC TAC TOE vs computer.

Algorithm

step-1 → create a 3×3 matrix with which will give 9 empty boxes.

step-2 → Assign X or O to the user depending on the symbol he chooses if then assign the other to the computer

step-3 → If the user starts the next turn will be given to the computer, this will happen till one of them wins or till all the null spaces are filled which results in a tie.

step-4 :- Now if the user starts, the computer should place 'O' in such a way that it should not let the user make a row of a column or a diagonal.

with X's. (basically should not let the user win).

step-5: If the user or the computer creates a row or column or a diagonal with their respective symbol, will be the ~~winner~~ winner of that particular round in the tic-tac-toe game.

{
if $a[0][0] == a[1][0] == a[2][0] == \text{player}$
if $a[0][1] == a[1][1] == a[2][1] == \text{player}$
if $a[0][2] == a[1][2] == a[2][2] == \text{player}$

if $a[0][0] == a[0][1] == a[0][2] == \text{player}$
if $a[1][0] == a[1][1] == a[1][2] == \text{player}$
if $a[2][0] == a[2][1] == a[2][2] == \text{player}$ }

if name == "main":

play game()

Output

X	X	X

enter row (1-3) = 2
enter row (1-3) = 2

```
code:  
import random  
import math  
  
def print_board(board):  
    for row in board:  
        print(" | ".join(row))  
    print("-" * 9)  
  
def check_winner(board,  
                 mark):  
    # Check rows  
    for row in board:  
        if all(cell == mark for  
               cell in row):  
            return True  
  
    # Check columns  
    for col in range(3):  
        if all(board[row][col] ==  
               mark for row in range(3)):  
            return True  
  
    # Check diagonals  
    if all(board[i][i] == mark  
          for i in range(3)) or  
        all(board[i][2 - i] == mark  
             for i in range(3)):  
        return True  
  
    return False  
  
def  
    get_available_moves(boa  
rd):  
    return [(r, c) for r in  
            range(3) for c in range(3)  
            if board[r][c] == " "  
  
def minimax(board, depth,
```

```

is_maximizing):
if check_winner(board,
"O"):
    return 10 - depth
if check_winner(board,
"X"):
    return depth - 10
if not
get_available_moves(boa
rd):
    return 0

if is_maximizing:
    best_score = -math.inf
    for (row, col) in
get_available_moves(boa
rd):
        board[row][col] =
    "O"
        score =
minimax(board, depth +
1, False)
        board[row][col] = " "
        best_score =
max(best_score, score)
    return best_score
else:
    best_score = math.inf
    for (row, col) in
get_available_moves(boa
rd):
        board[row][col] =
    "X"
        score =
minimax(board, depth +
1, True)
        board[row][col] = " "
        best_score =
min(best_score, score)
    return best_score

```

```

def computer_move(board):
best_score = -math.inf

```

```

best_move = None
for (row, col) in
get_available_moves(boa
rd):
    board[row][col] = "O"
    score =
minimax(board, 0, False)
    board[row][col] = " "
    if score > best_score:
        best_score = score
        best_move = (row,
col)
return best_move

```

```

def main():
    print("Yashraj Sinha
(1BM22CS335)")
    print("Welcome to Tic
Tac Toe!")
    board = [[" " for _ in
range(3)] for _ in range(3)]

print_board(board)

```

```

for turn in range(9):
    if turn % 2 == 0:
        # Player's turn
        while True:
            try:
                row =
int(input("Enter the row
(0, 1, 2): "))
                col =
int(input("Enter the
column (0, 1, 2): "))
                if (row, col) not
in
get_available_moves(boa
rd):
                    print("This
spot is already taken or
invalid. Try again.")
                else:

```

```
board[row][col] = "X"
        break
    except
ValueError:
    print("Invalid
input. Please enter
numbers 0, 1, or 2.")
else:
    # Computer's turn
    row, col =
computer_move(board)
    board[row][col] =
"O"
    print(f"Computer
chose: ({row}, {col})")

print_board(board)

# Check for a winner
if check_winner(board,
"X"):

print("Congratulations!
You win!")
    return
elif
check_winner(board,
"O"):
    print("Computer
wins! Better luck next
time.")
    return

print("It's a tie!")

if __name__ == "__main__":
main()
```

Output

```
Yashraj Sinha (1EM22CS335)
Welcome to Tic Tac Toe!
| |
-----
| |
-----
| |
-----
Enter the row (0, 1, 2): 0
Enter the column (0, 1, 2): 0
X | |
-----
| |
-----
| |
-----
Computer chose: (1, 1)
X | |
-----
| O |
-----
| |
-----
Enter the row (0, 1, 2): 2
Enter the column (0, 1, 2): 1
X | |
-----
| O |
-----
| X |
-----
Computer chose: (1, 0)
X | |
-----
O | O |
-----
| X |
-----
Enter the row (0, 1, 2): 1
Enter the column (0, 1, 2): 2
X | |
-----
O | O | X
-----
| X |
-----
Computer chose: (0, 2)
X | | O
-----
O | O | X
-----
| X |
-----
Enter the row (0, 1, 2): 2
```

```
Enter the row (0, 1, 2): 2
Enter the column (0, 1, 2): 0
X |   | O
-----
O | O | X
-----
X | X |
-----
Computer chose: (2, 2)
X |   | O
-----
O | O | X
-----
X | X | O
-----
Enter the row (0, 1, 2): 0
Enter the column (0, 1, 2): 1
X | X | O
-----
O | O | X
-----
X | X | O
-----
It's a tie!
```

Program 2 - 8 Puzzle BFS and DFS

Algorithm

Lab - 3

8 word puzzle using D.F.S & Manhattan distance.

1	2	3		1	2	3	
7	6	5		4	5	6	
8	4			7	8		

In an 8 word puzzle who have 9 boxes with 8 with 1 movable puzzle. $m\text{-dist}^n = g\text{oal} - s\text{tart}$

D.F.S

start-state = [- - -]
goal-state = [- - -]

stack = push (start-state)
visited-set = {}
moves = 0

~~f(i,j) { visited-set add (currnt-state)~~
~~if (currnt-state == goal-state)~~
~~return moves.~~

if (not in visited set) {
left = f(i,j-1)
right = f(i,j+1)
up = f(i-1,j)
down = f(i+1,j)}

Manhattan distance.

- > start at initial list of the given matrix (3×3) .
- > compare each element in the index to the final state & see how far it is from the final state.

~~manhattan (current-state, final-state)~~
~~if the file is not blank~~
~~tile (current X, current Y)~~
~~= position of the current tile.~~
 ~~$(\text{current } X - \text{goal } X) + (\text{current } Y - \text{goal } Y)$~~
~~return total distance.~~

Code (BFS)

```
from collections import
deque
def is_solvable(state):
    inversions = 0
    flattened = [num for row
in state for num in row if
num != 0]
    for i in
range(len(flattened)):
        for j in range(i + 1,
len(flattened)):
            if flattened[i] >
flattened[j]:
                inversions += 1

    return inversions % 2
== 0
```

```
def print_state(state,
label=None):
    if label:
        print(label)
    for row in state:
        print(" ".join(str(num)
if num != 0 else " " for num
in row))
    print()
```

```
def get_neighbors(state):
    rows, cols = len(state),
len(state[0])
    zero_pos = None
    for r in range(rows):
        for c in range(cols):
            if state[r][c] == 0:
                zero_pos = (r, c)
                break
        if zero_pos:
            break

    directions = [(-1, 0), (1,
0), (0, -1), (0, 1)]
    neighbors = []
```

```

for dr, dc in directions:
    nr, nc = zero_pos[0] +
dr, zero_pos[1] + dc
    if 0 <= nr < rows and
0 <= nc < cols:
        new_state = [row[:] for row in state]
new_state[zero_pos[0]][zero_pos[1]],
new_state[nr][nc] = (
    new_state[nr][nc],
    new_state[zero_pos[0]][zero_pos[1]],
)
neighbors.append(new_state)
return neighbors

```

```

def bfs(initial, goal):
    queue = deque([(initial, [])])
    visited = set()
    visited.add(tuple(tuple(row) for row in initial))

    while queue:
        current, path =
queue.popleft()
        if current == goal:
            return path +
[current]

        for neighbor in
get_neighbors(current):
            neighbor_tuple =
tuple(tuple(row) for row in
neighbor)
            if neighbor_tuple
not in visited:
                visited.add(neighbor_tuple)

```

```
queue.append((neighbor,
path + [current]))
return None
```

```
def main():
    print("Yashraj Sinha
(1BM22CS335)")
    print("8-Puzzle Solver
Using BFS")
    initial_state = [[1, 2, 3],
[4, 0, 5], [7, 8, 6]] #
Example initial state
    goal_state = [[1, 2, 3], [4,
5, 6], [7, 8, 0]] # Goal state

    print_state(initial_state,
label="Initial State:")
    print_state(goal_state,
label="Goal State:")
```

```
if not
is_solvable(initial_state):
    print("This puzzle is
not solvable.")
    return

solution =
bfs(initial_state, goal_state)
if solution:
    print("Solution found
in {}"
steps:\n".format(len(solution) - 1))
    for i, step in
enumerate(solution):
        if i == 0:
            print_state(step,
label="Initial State:")
        elif i ==
len(solution) - 1:
            print_state(step,
label="Final State:")
        else:
            print_state(step,
label=f"Step {i}:")
    else:
```

```
    print("No solution  
exists.")
```

```
if __name__ ==  
 "__main__":  
     main()
```

Code (DFS)

```
def is_solvable(state):
    inversions = 0
    flattened = [num for row in state for num in row if num != 0]
    for i in range(len(flattened)):
        for j in range(i + 1, len(flattened)):
            if flattened[i] > flattened[j]:
                inversions += 1

    return inversions % 2 == 0

def print_state(state, label=None):
    if label:
        print(label)
    for row in state:
        print(" ".join(str(num) if num != 0 else " " for num in row))
    print()

def get_neighbors(state):
    rows, cols = len(state), len(state[0])
    zero_pos = None
    for r in range(rows):
        for c in range(cols):
            if state[r][c] == 0:
                zero_pos = (r, c)
                break
        if zero_pos:
            break

    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]
    neighbors = []

    for dr, dc in directions:
        nr, nc = zero_pos[0] + dr, zero_pos[1] + dc
        if 0 <= nr < rows and 0 <= nc < cols:
            new_state = [row[:] for row in state]
            new_state[zero_pos[0]][zero_pos[1]], new_state[nr][nc] = (
                new_state[nr][nc],
                new_state[zero_pos[0]][zero_pos[1]],
            )
            neighbors.append(new_state)

    return neighbors
```

```

def dfs(initial, goal):
    stack = [(initial, [])]
    visited = set()
    visited.add(tuple(tuple(row) for row in initial))

    while stack:
        current, path = stack.pop()
        if current == goal:
            return path + [current]

        for neighbor in get_neighbors(current):
            neighbor_tuple = tuple(tuple(row) for row in neighbor)
            if neighbor_tuple not in visited:
                visited.add(neighbor_tuple)
                stack.append((neighbor, path + [current]))
    return None

def main():
    print("Yashraj Sinha (1BM22CS335)")
    print("8-Puzzle Solver Using DFS")
    initial_state = [[1, 2, 3], [4, 0, 5], [7, 8, 6]] # Example initial state
    goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]] # Goal state

    print_state(initial_state, label="Initial State:")
    print_state(goal_state, label="Goal State:")

    if not is_solvable(initial_state):
        print("This puzzle is not solvable.")
        return

    solution = dfs(initial_state, goal_state)
    if solution:
        print("Solution found in {} steps:\n".format(len(solution) - 1))
        for i, step in enumerate(solution):
            if i == 0:
                print_state(step, label="Initial State:")
            elif i == len(solution) - 1:
                print_state(step, label="Final State:")
            else:
                print_state(step, label=f"Step {i}:")
    else:
        print("No solution exists.")

if __name__ == "__main__":
    main()

```

Output (BFS)

```
Yashraj Sinha (1BM22CS335)
8-Puzzle Solver Using BFS
Initial State:
1 2 3
4   5
7 8 6

Goal State:
1 2 3
4 5 6
7 8

Solution found in 2 steps:

Initial State:
1 2 3
4   5
7 8 6

Step 1:
1 2 3
4 5
7 8 6

Final State:
1 2 3
4 5 6
7 8
```

Output (DFS)

```
Yashraj Sinha (1BM22CS335)
8-Puzzle Solver Using DFS
Initial State:
1 2 3
4   5
7 8 6

Goal State:
1 2 3
4 5 6
7 8

Solution found in 2 steps:

Initial State:
1 2 3
4   5
7 8 6

Step 1:
1 2 3
4 5
7 8 6
<
Final State:
1 2 3
4 5 6
7 8
```

Program 3 - Iterative Deepening Search

Algorithm

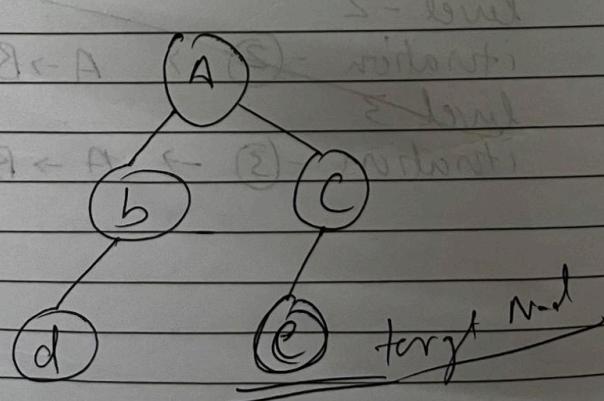
bool IDDFS (src, target, max-depth) 2)
for limit from 0 to max-depth
if DLS (src, target, limit) == true
return true
return false.

bool DLS (src, target, limit)
~~if (src == target) {~~
~~return true;~~

~~if (limit <= 0)~~
~~return false;~~

~~for each adjacent i of SRC~~
~~if DLS (i, target, limit-1)~~
~~return true;~~

~~return false~~ ○ - level
① - visitant
S - level
② - visitant
→ level
S - level



Code

```
print("Yashraj Sinha (1BM22CS335)")
def is_solvable(state):
    inversions = 0
    flattened = [num for row in state for num in row if num != 0] for i in range(len(flattened)):
        for j in range(i + 1, len(flattened)):
            if flattened[i] > flattened[j]:
                inversions += 1
    return inversions % 2 == 0

def print_state(state, label=None):
    if label:
        print(label)
    for row in state:
        print(" ".join(str(num) if num != 0 else " " for num in row)) print()

def get_neighbors(state):
    rows, cols = len(state), len(state[0])
    for r in range(rows):
        for c in range(cols):
            if state[r][c] == 0:
                zero_pos = (r, c)
                break
    directions = [(-1, 0), (1, 0), (0, -1), (0, 1)]
    neighbors = []
    for dr, dc in directions:
        nr, nc = zero_pos[0] + dr, zero_pos[1] + dc
        if 0 <= nr < rows and 0 <= nc < cols:
            new_state = [row[:] for row in state]
            new_state[zero_pos[0]][zero_pos[1]], new_state[nr][nc] = new_state[nr][nc], new_state[zero_pos[0]][zero_pos[1]]
            neighbors.append(new_state)
    return neighbors
```

```
def ids(initial, goal, depth_limit):  
    def dls(state, path, depth):  
        if state == goal:
```

```

        return path + [state]
    if depth == 0:
        return None
    for neighbor in get_neighbors(state):
        if tuple(tuple(row) for row in neighbor) not in visited:
            visited.add(tuple(tuple(row) for row in neighbor))
            result = dls(neighbor, path + [state], depth - 1)
            if result:
                return result
    return None

for depth in range(depth_limit):
    visited = set()
    visited.add(tuple(tuple(row) for row in initial))
    result = dls(initial, [], depth)
    if result:
        return result
return None

def main():
    print("8-Puzzle Solver Using Iterative Deepening Search")
    initial_state = [[1, 2, 3], [4, 0, 5], [7, 8, 6]] # Example initial state
    goal_state = [[1, 2, 3], [4, 5, 6], [7, 8, 0]] # Goal state

    print_state(initial_state, label="Initial State:")
    print_state(goal_state, label="Goal State:")

    if not is_solvable(initial_state):
        print("This puzzle is not solvable.")
        return

    depth_limit = 20
    solution = ids(initial_state, goal_state, depth_limit)
    if solution:
        print("Solution found in {} steps:\n{}".format(len(solution) - 1))
        for i, step in enumerate(solution):
            if i == 0:
                print_state(step, label="Initial State:")

```

```
elif i == len(solution) - 1:  
    print_state(step, label="Final State:")  
else:
```

```
    print_state(step, label=f"Step {i}:")
else:
    print("No solution exists within depth limit {}.".format(depth_limit))

if __name__ == "__main__":
    main()
```

Output

```
Yashraj Sinha (1BM22CS335)
8-Puzzle Solver Using Iterative Deepening Search
Initial State:
1 2 3
4   5
7 8 6

Goal State:
1 2 3
4 5 6
7 8

Solution found in 2 steps:

Initial State:
1 2 3
4   5
7 8 6

Step 1:
1 2 3
4 5
7 8 6

Final State:
1 2 3
4 5 6
7 8
```

Program 4 - Vacuum Cleaner Agent

Algorithm

LAB-2

Vacuum Cleaner.

X Algorithm.

1) Create 2 rooms using classes.

```
class room:  
    def __init__(self, a):  
        self.state = a.  
    def suck(self):  
        self.state = "clean"
```

2) Instantiate the class & take user input.

```
a = str(input("Room A state:"))  
b = str(input("Room B state:"))  
  
room_list = []  
room_list.append(room(a))  
room_list.append(room(b))
```

3) Perception Sequence:

```
for i in room_list:  
    if (i.state == "dirty"):  
        i.suck()
```

Lab-2 (code continued)

```
else if (i == 0 & j == 0) {  
    bust-score = float('inf')  
    for m in range(3):  
        for n in range(3):  
            if board[m][n] == "":  
                (m + N) < m + bust-score; board[m][n] = '0'  
            bust-score = min(bust-score,  
                               board[m][n])  
    board[i][j] = ""
```

d "Position too many") try

lab (3)- vacuum cleaner
code.

```
class VacuumCleaner:  
    def __init__(self, room):  
        self.room = room  
        self.position = (0, 0)  
        self.cleaned = 0
```

```
def isdirty(self, position):  
    x, y = position  
    return self.room[x][y] == 1.
```

```
def clean(self, position):  
    x, y = position  
    if self.isdirty(position):  
        self.room[x][y] = 0  
        self.cleaned += 1  
    print("cleaned position?")
```

Page _____

```

def move(self, direction):
    n, y = self.position
    if direction == "up" & n > 0:
        self.position = (n - 1, y)
    elif direction == "down" & n <
        len(self.room) - 1:
        self.position = (n + 1, y)
    elif direction == "left" & y > 0:
        self.position = (n, y - 1)
    else:
        print("Move not possible!")

```

Output

```

cleaned position (0,0)
Move not possible!
Cleaned position (2,0)
Move not possible!
Move not possible!
Total cleaned spots: 2

```

Code

```
print("Yashraj Sinha (1BM22CS335)")
```

```
def vacuum_cleaner(initial_state):
```

```
# Initial states of rooms A and
# B room_A, room_B =
initial_state

# Trace of actions
actions = []

# Start in Room A
actions.append("Starting in Room
A.")

# Check room A
if room_A == 1:
    actions.append("Room A is dirty. Cleaning Room A.")
    room_A = 0
else:
    actions.append("Room A is already clean.")
```

```
# Move to Room B
```

```
actions.append("Moving to Room  
B.")
```

```
# Check room B
```

```
if room_B == 1:
```

```
    actions.append("Room B is dirty. Cleaning Room B.")
```

```
    room_B = 0
```

```
else:
```

```
    actions.append("Room B is already clean.")
```

```
# Move back to Room A
```

```
actions.append("Returning to Room A.")
```

```
# Final state
```

```
final_state = (room_A, room_B)
```

```
actions.append("Both rooms are now clean.")
```

```
return final_state, actions
```

```
def main():

    print("Vacuum Cleaner AI")

    # Input initial states of Room A and Room B

    room_A = int(input("Enter the state of Room A (0 for clean, 1 for dirty): "))

    room_B = int(input("Enter the state of Room B (0 for clean, 1 for dirty): "))

    # Validate input

    if room_A not in (0, 1) or room_B not in (0, 1):

        print("Invalid input. Please enter 0 or 1.")

    return

# Solve using vacuum cleaner AI

final_state, actions = vacuum_cleaner((room_A, room_B))

# Output actions and final state

print("\nActions:")
```

for action in actions:

```
print(action)

print("\nFinal State:")

print(f"Room A: {'Clean' if final_state[0] == 0 else 'Dirty'}")

print(f"Room B: {'Clean' if final_state[1] == 0 else 'Dirty'}")

if __name__ == "__main__":
    main()
```

Output

```
Yashraj Sinha (1BM22CS335)
Vacuum Cleaner AI
Enter the state of Room A (0 for clean, 1 for dirty): 1
Enter the state of Room B (0 for clean, 1 for dirty): 1

Actions:
Starting in Room A.
Room A is dirty. Cleaning Room A.
Moving to Room B.
Room B is dirty. Cleaning Room B.
Returning to Room A.
Both rooms are now clean.

Final State:
Room A: Clean
Room B: Clean
```

Program 5 - A* Search Algorithm and Hill Climbing Algorithm

Algorithm

4) Implementing A* algorithm using python.

→ A^*

```
function A*search (problem) return a
    solution or failure
    node ← a node n with n.state =
        problem.initial_state, n.g = 0
    frontier ← a priority queue ordered
        by ascending g+h, only
        element n.
    loop do
        if empty? (frontier) then return
            failure
        n ← pop (frontier)
        if problem.goalTest (n.state) then
            return solution(n)
        for each action a in problem.
            actions (n.state) do
                n' ← ChildNode (problem, n, a)
                insert (n', g(n') + h(n'),
                    frontier)
```

- (i) Using no. of misplaced tiles as heuristic function

$$f(n) = g(n) + h(n)$$

1	2	3
4	5	6
0	7	8

Initial State

1	2	3
4	5	6
7	3	0

Final state

Output

1	2	3
4	0	6 5
6	7	8

Initial state

$$\begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 0 \\ 6 & 7 & 8 \end{array} \rightarrow \begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 8 \\ 6 & 7 & 0 \end{array} \rightarrow \begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 8 \\ 6 & 0 & 7 \end{array}$$

↓

$$\begin{array}{ccc} (12\ 13) & 1 & 2 & 3 \\ 5 & 0 & 8 \\ 4 & 6 & 7 \end{array} \leftarrow \begin{array}{ccc} 0 & 5 & 8 \\ 4 & 6 & 7 \end{array} \leftarrow \begin{array}{ccc} 4 & 5 & 8 \\ 6 & 0 & 7 \end{array}$$

↓

$$\begin{array}{ccc} 1 & 2 & 3 \\ 5 & 6 & 8 \\ 4 & 0 & 7 \end{array} \rightarrow \begin{array}{ccc} 1 & 2 & 3 \\ 5 & 6 & 8 \\ 4 & 7 & 0 \end{array} \rightarrow \begin{array}{ccc} 1 & 2 & 3 \\ 5 & 6 & 0 \\ 4 & 7 & 3 \end{array}$$

↓

$$\begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 0 & 7 & 3 \end{array} \leftarrow \begin{array}{ccc} 0 & 4 & 5 \\ 4 & 7 & 3 \end{array} \leftarrow \begin{array}{ccc} 5 & 0 & 6 \\ 4 & 7 & 3 \end{array}$$

↓

$$\begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 0 & 8 \end{array} \rightarrow \begin{array}{ccc} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 3 & 0 \end{array}$$

8
ans 10

i) Using Manhattan distance

→ Initial state

1	2	3
4	0	5
7	8	6

Goal state

1	2	3
4	5	6
7	8	0

Tile 1 : Manhattan distance (MD) = 0

Tile 2 : MD = 0

Tile 4 : MD = 0

Tile 2 : MD = 1

Tile 7 : MD = 1

Tile 8 : MD = 0

Tile 6 : MD = 1

$f(n) = \text{Total MD} = 3$

} 1st iteration

Tile 1 : Total MD = 20

Tile 2 : Total MD = 20

Tile 3 : Total MD = 0

Tile 4 : Total MD = 20

Tile 5 : Total MD = 22

Tile 6 : Total MD = 21

Tile 7 : Total MD = 20

Tile 8 : Total MD = 20

$f(n) = \text{Total MD} = 3$

$f(n) = \text{Total MD} = 0$

} 2nd iteration

→ Solution in 3rd iteration

1	2	3
4	0	5
7	8	6

 \rightarrow

1	2	3
4	5	0
7	8	6

 \rightarrow

1	2	3
4	5	6
7	8	0

5) Implementing Hill Climbing search algorithm to solve N-Queens problem.

→ function Hill-Climbing (problem) returns a state that is local maximum

current \leftarrow Make-Node (problem, Initial-State)

loop do

neighbour \leftarrow a highest value successor of current

if neighbour.value \leq current.value

then return current.state

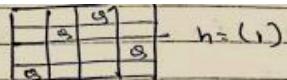
execute
current \leftarrow neighbour.

8) Show how the cost calculation of current state and neighbour nodes. And continue until you reach goal configuration of 4-Queens board.

			Q ₃	
				Q ₂
		Q ₁		

<u>State</u>	<u>n(score)</u>
3, 1, 2, 0	2
1, 3, 2, 0	1
2, 1, 3, 0	1
0, 1, 2, 3	6
3, 2, 1, 0	6
3, 0, 2, 1	1
3, 1, 0, 2	1

state	shape:	$h = (2)$	$h = (1)$
3, 1, 2, 0			
2, 1, 3, 0			
0, 1, 2, 3			
3, 2, 1, 0			
3, 0, 2, 1			
3, 1, 0, 2			

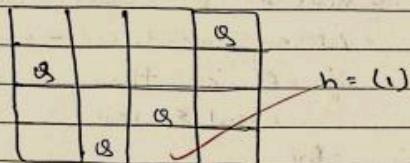


3, 1, 0, 2

$h = (1)$

• Next step

1, 3, 2, 0



$h = (1)$

state

h (score)

1, 2, 2, 0

1

3, 1, 2, 0

2

2, 3, 1, 0

2

0, 3, 2, 1

3

1, 2, 3, 0

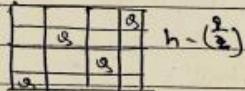
3

1, 3, 0, 2

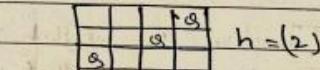
0

← return solution

state
choice:

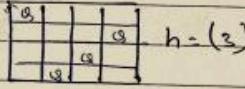


3, 1, 2, 0

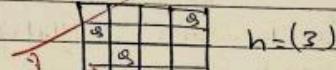


2, 3, 1, 0

$h = (2)$

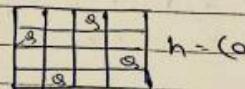


0, 3, 2, 1

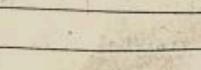


1, 2, 3, 0

$h = (3)$



1, 3, 0, 2



$h = (0)$

Code (A* algorithm using N – displaced Tiles)

```
import heapq

# Goal state

goal_state = (
    (1, 2, 3),
    (4, 5, 6),
    (7, 8, 0)
)

# Function to compute the heuristic (misplaced
# tiles) def misplaced_tiles(state):
    misplaced = 0

    for i in range(3):
        for j in range(3):
            if state[i][j] != goal_state[i][j] and state[i][j] != 0:
                misplaced += 1

    return misplaced
```

```
# Function to get possible moves (neighbors)
```

```

def get_neighbors(state):

    neighbors = []

    zero_pos = [(i, j) for i in range(3) for j in range(3) if state[i][j] == 0][0]

    i, j = zero_pos

    # Possible moves: up, down, left, right

    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]

    for move in moves:

        new_i, new_j = i + move[0], j + move[1]

        if 0 <= new_i < 3 and 0 <= new_j < 3:

            new_state = list(list(row) for row in state) # Create a copy of the state

            new_state[i][j], new_state[new_i][new_j] = new_state[new_i][new_j], new_state[i][j]

            neighbors.append(tuple(tuple(row) for row in new_state)) # Convert back to tuple

    return neighbors

# Function to count the number of inversions in the

puzzle def count_inversions(state):

    one_d_state = [tile for row in state for tile in row if tile != 0]

```

inversions = 0

```
for i in range(len(one_d_state)):

    for j in range(i + 1, len(one_d_state)):

        if one_d_state[i] > one_d_state[j]:

            inversions += 1

return inversions

# Check if the puzzle is solvable

def is_solvable(state):

    inversions = count_inversions(state)

    return inversions % 2 == 0

# A* Algorithm

def a_star(initial_state):

    if not is_solvable(initial_state):

        print("This puzzle is not solvable.")

    return None

open_list = []
```

```
heapq.heappush(open_list, (0 + misplaced_tiles(initial_state), 0, initial_state, [])) # (f(n), g(n),  
state, path)
```

```
closed_list = set()

while open_list:

    f, g, current_state, path =

        heapq.heappop(open_list)

    closed_list.add(current_state)

    # If goal state is reached

    if current_state == goal_state:

        return path + [current_state]

    # Generate neighbors

    for neighbor in get_neighbors(current_state):

        if neighbor not in closed_list:

            heapq.heappush(open_list, (

                g + 1 + misplaced_tiles(neighbor), # f(n) = g(n) + h(n)

                g + 1, # Increment g(n) by 1 for each move

                neighbor,
```

path + [current_state]

)

```
return None # No solution found

# Function to display the puzzle state

def display_state(state, label):

    print(f"{label}

state:") for row in

state:

    print(" ".join(str(x) for x in row))

print()

# Example initial state (this one is solvable)

initial_state = (

(1, 2, 3),

(5, 6, 4),

(7, 8, 0)

)
```

```
# Solving the puzzle
```

```
solution = a_star(initial_state)
```

```
# Displaying the result

if solution:

    # Print Yashraj's information

    print("Yashraj Sinha (1BM22CS335)\n")

    # Print the initial state

    display_state(initial_state, "Initial")

    # Print the final state

    display_state(goal_state, "Goal")

    # Displaying the solution path

    print("Solution path:")

    for step in solution:

        display_state(step,
                      "Step")

else:
```

```
print("No solution found.")
```

Code (A* algorithm using Manhattan distance)

```
import
heapq

# Goal state

goal_state = (
    (1, 2, 3),
    (4, 5, 6),
    (7, 8, 0)
)

# Function to compute the Manhattan distance heuristic

def manhattan_distance(state):
    distance = 0

    for i in range(3):
        for j in range(3):
            tile = state[i][j]

            if tile != 0:
                goal_i, goal_j = divmod(tile - 1, 3)
```

```
distance += abs(goal_i - i) + abs(goal_j - j)
```

```

return distance

# Function to get possible moves (neighbors)

def get_neighbors(state):

    neighbors = []

    zero_pos = [(i, j) for i in range(3) for j in range(3) if state[i][j] == 0][0]

    i, j = zero_pos

    # Possible moves: up, down, left, right

    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]

    for move in moves:

        new_i, new_j = i + move[0], j + move[1]

        if 0 <= new_i < 3 and 0 <= new_j < 3:

            new_state = list(list(row) for row in state) # Create a copy of the state

            new_state[i][j], new_state[new_i][new_j] = new_state[new_i][new_j], new_state[i][j]

            neighbors.append(tuple(tuple(row) for row in new_state)) # Convert back to tuple

    return neighbors

```

```
# Function to count the number of inversions in the puzzle
```

```
def count_inversions(state):

    one_d_state = [tile for row in state for tile in row if tile != 0]

    inversions = 0

    for i in range(len(one_d_state)):

        for j in range(i + 1, len(one_d_state)):

            if one_d_state[i] > one_d_state[j]:

                inversions += 1

    return inversions
```

```
# Check if the puzzle is solvable
```

```
def is_solvable(state):

    inversions = count_inversions(state)

    return inversions % 2 == 0
```

```
# A* Algorithm
```

```
def a_star(initial_state):

    if not is_solvable(initial_state):

        print("This puzzle is not solvable.")
```

```
return None
```

```
open_list = []

heapq.heappush(open_list, (0 + manhattan_distance(initial_state), 0, initial_state, [])) # (f(n), g(n),
state, path)

closed_list = set()

while open_list:

    f, g, current_state, path =

        heapq.heappop(open_list)

    closed_list.add(current_state)

    # Print the current state and its f(n) value

    print(f"State: {current_state}")

    print(f"f(n) = g(n) + h(n) = {g} + {manhattan_distance(current_state)} = {f}")

    print()

# If goal state is reached

if current_state == goal_state:

    return path + [current_state]
```

```
# Generate neighbors
```

```
for neighbor in get_neighbors(current_state):

    if neighbor not in closed_list:

        heapq.heappush(open_list, (

            g + 1 + manhattan_distance(neighbor), # f(n) = g(n) + h(n)
            g
            + 1, # Increment g(n) by 1 for each move

            neighbor,
            path + [current_state]

        ))

return None # No solution found

# Function to display the puzzle state

def display_state(state, label):

    print(f"{label}

state:") for row in

    state:

        print(" ".join(str(x) for x in row))

    print()
```

Example initial state (this one is solvable)

```
initial_state = (  
    (1, 2, 3),  
    (5, 6, 4),  
    (7, 8, 0)  
)
```

```
# Solving the puzzle
```

```
solution = a_star(initial_state)
```

```
# Displaying the result
```

```
if solution:
```

```
    # Print Yashraj's information
```

```
    print("Yashraj Sinha (1BM22CS335)\n")
```

```
    # Print the initial state
```

```
    display_state(initial_state, "Initial")
```

```
    # Print the final state
```

```
display_state(goal_state, "Goal")
```

```
# Displaying the solution path

print("Solution path:")

for step in solution:

    display_state(step,
                  "Step")

else:

    print("No solution found.")
```

Code (Hill Climbing algorithm)

```
import random

print("Yashraj Sinha (1BM22CS335)")

# Function to calculate the number of attacking pairs of
queens def calculate_attacks(board):

    attacks = 0

    n = len(board)

    for i in range(n):
```

```
for j in range(i + 1, n):
```

```
    if board[i] == board[j] or abs(board[i] - board[j]) == j - i:
```

```
    attacks +=

1 return attacks

# Function to generate a random initial state

def generate_initial_state(n):

    return [random.randint(0, n - 1) for _ in range(n)]


# Function to generate neighbors by moving one queen to a different row

def generate_neighbors(board):

    neighbors = []

    n = len(board)

    for col in range(n): for

        row in range(n):

            if row != board[col]: # Make sure we are not moving the queen to its current row

                neighbor = board[:]

                neighbor[col] = row

                neighbors.append(neighbor)

    return neighbors
```

```
# Hill Climbing algorithm with random restarts

def hill_climbing(n, max_restarts=100):

    for restart in range(max_restarts):

        current_state = generate_initial_state(n)

        current_attacks = calculate_attacks(current_state)

        while True:

            # Generate all neighbors

            neighbors = generate_neighbors(current_state)

            # Find the neighbor with the minimum number of attacks

            next_state = None

            next_attacks = current_attacks

            for neighbor in neighbors:

                attacks = calculate_attacks(neighbor)

                if attacks < next_attacks:

                    next_state = neighbor
```

```
next_attacks = attacks
```

```
# If no improvement, return the solution or  
terminate if next_attacks == current_attacks:  
break
```

```
current_state = next_state
```

```
current_attacks = next_attacks
```

```
# If a solution is found, return the current  
state if current_attacks == 0:  
return current_state
```

```
# If no solution found after max_restarts, return None  
return None
```

```
# Function to display the board
```

```
def display_board(board):
```

```
n = len(board)
```

```
for i in range(n):
```

```
row = ['Q' if i == board[col] else '.' for col in
       range(n)] print(' '.join(row))

print()

# Set the size of the board (N)

N = 8

# Solve the N-Queens problem with random restarts

solution = hill_climbing(N)

# Display the result

if solution:

    print(f"Solution for {N}-Queens:")

    display_board(solution)

else:

    print(f"No solution found for {N}-Queens.")
```

```
Yashraj Sinha (IBM22CS335)
```

```
Initial state:
```

```
1 2 3  
5 6 4  
7 8 0
```

```
Goal state:
```

```
1 2 3  
4 5 6  
7 8 0
```

```
Solution path:
```

```
Step state:
```

```
1 2 3  
5 6 4  
7 8 0
```

```
Step state:
```

```
1 2 3  
5 6 0  
7 8 4
```

```
Step state:
```

```
1 2 3  
5 0 6  
7 8 4
```

```
Step state:
```

```
1 2 3  
0 5 6  
7 8 4
```

```
Step state:
```

```
1 2 3  
7 5 6  
0 8 4
```

```
Step state:
```

```
1 2 3  
7 5 6  
8 0 4
```

```
Step state:  
1 2 3  
7 5 0  
8 4 6
```

```
Step state:  
1 2 3  
7 0 5  
8 4 6
```

```
Step state:  
1 2 3  
7 4 5  
8 0 6
```

```
Step state:  
1 2 3  
7 4 5  
0 8 6
```

```
Step state:  
1 2 3  
0 4 5  
7 8 6
```

```
Step state:  
1 2 3  
4 0 5  
7 8 6
```

Output (Manhattan Distance)

```
Yashraj Sinha (1BM22CS335)

Initial state:
1 2 3
5 6 4
7 8 0

Goal state:
1 2 3
4 5 6
7 8 0

Solution path:
Step state:
1 2 3
5 6 4
7 8 0

Step state:
1 2 3
5 6 0
7 8 4

Step state:
1 2 3
5 0 6
7 8 4

Step state:
1 2 3
0 5 6
7 8 4

Step state:
1 2 3
7 5 6
0 8 4
```

```
Step state:
```

```
1 2 3
```

```
7 4 5
```

```
0 8 6
```

```
Step state:
```

```
1 2 3
```

```
0 4 5
```

```
7 8 6
```

```
Step state:
```

```
1 2 3
```

```
4 0 5
```

```
7 8 6
```

```
Step state:
```

```
1 2 3
```

```
4 5 0
```

```
7 8 6
```

```
Step state:
```

```
1 2 3
```

```
4 5 6
```

```
7 8 0
```

Output (Hill Climbing)

```
Yashraj Sinha (1BM22CS335)
Solution for 8-Queens:
. . . . Q . .
. . Q . . . .
Q . . . . . .
. . . . . . Q .
. . . . Q . . .
. Q . . . . .
. . . Q . . . .
. . . . . . Q .
```

Program 6 - Simulated Annealing

Algorithm

Lab-5

Simulated Annealing Algorithm

→ used to approximate global maxima

→ \Rightarrow

1) start with initial soln (s)
- current solution

• Define initial temperature "T",
a cooling schedule, & a
stopping condition

2) Iteration loop

3) Objective function :- $f(s)$ to be
minimised or maximised.

3) Iteration

- Iteration

max

min

- Generate a new solⁿ
- perturb $s \rightarrow s'$
- evaluate $\Delta E = f(s') - f(s)$
- Acceptance:

if $\Delta E < 0$, accept s' as better
 if $\Delta E > 0$

accept s' with prob.
 $P = e^{-\Delta E / T}$

(this allows accepting
 worse solⁿ to escape
 local maxima)

3) Update
~~(if $s' \neq s$) set $s = s'$ if s' is accepted.~~
~~Update T according to cooling~~
~~schedule~~

4) Keep track of best solⁿ & return it.

↓ proceed

Code

```
import random  
  
import math  
  
print("Yashraj Sinha (1BM22CS335)")  
  
# Objective function: count the number of attacking pairs of queen
```

```
def calculate_attacks(board):

    attacks = 0

    n = len(board)

    for i in range(n):

        for j in range(i + 1, n):

            # Check if two queens are in the same row, column, or
            # diagonal if board[i] == board[j] or abs(board[i] - board[j]) == j - i:

            attacks += 1

    return attacks

# Function to generate a random initial state (random queen positions in each column)

def generate_initial_state(n):

    return [random.randint(0, n - 1) for _ in range(n)]

# Function to generate a neighboring solution by moving one queen in a column

def generate_neighbor(board):

    neighbor = board[:]

    column = random.randint(0, len(board) - 1)
```

```
# Randomly select a new row for the queen in the chosen column
```

```
neighbor[column] = random.randint(0, len(board) - 1)

return neighbor

# Simulated Annealing algorithm to solve the N-Queens problem

def simulated_annealing(n, max_iterations, initial_temperature, cooling_rate):

    current_state = generate_initial_state(n)

    current_attacks = calculate_attacks(current_state)

    temperature = initial_temperature

    best_state = current_state

    best_attacks = current_attacks

    for iteration in range(max_iterations):

        # Generate a neighbor solution

        neighbor = generate_neighbor(current_state)

        neighbor_attacks = calculate_attacks(neighbor)

        # Calculate the energy difference (how much worse the new state is)
```

```
delta_attacks = neighbor_attacks - current_attacks
```

```
# Accept the neighbor if it has fewer attacks or with a probability if it's worse

if delta_attacks < 0 or random.random() < math.exp(-delta_attacks / temperature):

    current_state = neighbor

    current_attacks = neighbor_attacks

# Update the best solution if

necessary if current_attacks <

best_attacks:

    best_state = current_state

    best_attacks = current_attacks

# Cool down the temperature

temperature *= cooling_rate

# If no attacks, we found the

solution if best_attacks == 0:

    break
```

```
return best_state, best_attacks
```

```
# Function to display the board (where 'Q' is a queen and '.' is an empty space)

def display_board(board):

    n = len(board)

    for i in range(n):

        row = ['Q' if i == board[col] else '.' for col in
               range(n)] print(' '.join(row))

    print()

# Parameters for Simulated Annealing

N = 8 # Set the size of the board (N x N)

max_iterations = 10000 # Higher number of iterations for better convergence

initial_temperature = 1000 # High initial temperature

cooling_rate = 0.995 # Cooling rate (temperature decreases by 0.5% every iteration)

# Solve the N-Queens problem using Simulated Annealing

solution, attacks = simulated_annealing(N, max_iterations, initial_temperature, cooling_rate)
```

```
# Output the result
```

```
print(f"Solution for {N}-Queens found:")
```

```
display_board(solution)
```

```
print(f"Total number of attacks: {attacks}")
```

Output

```
Yashraj Sinha (1BM22CS335)
Solution for 8-Queens found:
```

```
. . . . . . . Q
. . Q . . . .
Q . . . . . .
. . . . . Q . .
. Q . . . .
. . . . Q . .
. . . . . . Q .
. . . Q . . .
```

```
Total number of attacks: 0
```

Program 7 - Knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm

#	Knowledge - Base:
1.	Alice is the mother of Bob M (Alice, Bob)
2.	Bob is the father of Charlie f(Bob, Charlie)
3.	A father is a parent.
4.	A mother is a parent.
5.	All parents have children.
6.	If someone is a parent, their children are siblings.
7.	Alice is married to David.
	$\Rightarrow \{ \exists n \forall y (\text{father}(n,y) \rightarrow \text{parent}(n,y)) \} \quad \{ \forall n (\text{parent}(n,y) \wedge \text{parent}(n,z) \rightarrow \text{child}(y,z)) \}$
#	Hypothesis
	• Charlie is a sibling of Bob.
=>	Solution
	* On applying scientific method.
1.	Is bob a parent?
	\Rightarrow Yes, bob's a parent, he is charlie's father.
2.	Does Bob and Charlie share a parent?
	\Rightarrow No because Bob & is the father of Charlie.

Code

```
from sympy.logic.boolalg import Or, And,  
Not from sympy.abc import A, B, C, D, E, F  
57from sympy import simplify_logic  
def is_entailment(kb, query):  
    # Negate the query  
    negated_query = Not(query)  
    # Add negated query to the knowledge base  
    kb_with_negated_query = And(*kb, negated_query)  
    # Simplify the combined KB to CNF  
    simplified_kb = simplify_logic(kb_with_negated_query,  
form="cnf") # If the simplified KB evaluates to False, the query is  
entailed return simplified_kb == False  
    # Define a larger Knowledge Base  
    kb = [  
        Or(A, B),  
        # A v B  
        Or(Not(A), C), # ¬A v C  
        Or(Not(B), D), # ¬B v D  
        Or(Not(D), E), # ¬D v E  
        Or(Not(E), F), # ¬E v F  
        F  
        # F  
    ]  
    # Query to check  
    query = Or(C, F) # C v F  
    # Check entailment  
    result = is_entailment(kb, query)  
    print(f"Is the query '{query}' entailed by the knowledge base? {'Yes' if result else 'No'}")
```

OUTPUT:

Is the query 'C | F' entailed by the knowledge base? Yes

Code

```
Keep track of all unique
clauses in the knowledge
base
print(f"Initial Knowledge
Base + negation of query:
{kb}")
```

```
while True:
    added_new_clause =
    False

    # Try to resolve every
    pair of clauses
    clauses =
    list(new_clauses)
    for i in
    range(len(clauses)):
        for j in range(i + 1,
        len(clauses)):
            clause1 = clauses[i]
            clause2 = clauses[j]
```

```
            # Try to resolve
            these two clauses
            resolvent =
            resolve(clause1, clause2)
```

```
            if resolvent is not
            None:
                print(f"Resolving
                clauses: {clause1} and
                {clause2}")
                print(f"Resolved
                to: {resolvent}")
```

```
            # If resolvent is
            empty, we found a
            contradiction
            if not resolvent:
```

```

        return True #
Found a contradiction, so
the query is provable

        # Add the new
clause if it's not already in
the set
        if resolvent not in
new_clauses:

    new_clauses.add(resolvent)

    added_new_clause = True

        # If no new clause was
added, resolution has
terminated without a
contradiction
        if not
added_new_clause:
            break

    return False # No
contradiction found, so the
query is not provable

```

```

def resolve(clause1, clause2):
    """Resolve two clauses if
possible and return the
resolvent."""
    # Split clauses into literals
    literals1 =
    set(clause1.split(" v "))
    literals2 =
    set(clause2.split(" v "))

    # Try to find
    complementary literals
    for literal in literals1:
        neg_literal =
        negation(literal)

```

```

if neg_literal in literals2:
    # Resolve the two
    clauses by removing
    complementary literals
    new_clause =
    literals1.union(literals2) -
    {literal, neg_literal}
    return " v
    ".join(sorted(new_clause))
# Return the resolved
clause as a string

return None # No resolvent
found

```

```

# Example knowledge base
and query (where T is
provable)
kb = [
    "P v Q",    # P or Q
    "~P v R",   # Not P or R
    "Q v ~R",   # Q or Not R
    "R v T"     # R or T
]

```

```

query = "T" # Query to prove
(e.g., prove T)

```

```

# Perform resolution to prove
the query
result = resolution(kb, query)

```

```

if result:
    print(f"\nQuery '{query}' is
provable from the
knowledge base.")
else:
    print(f"\nQuery '{query}' is

```

not provable from the knowledge base.")

```
def negation(p):
    """Negate a literal."""
    if p.startswith("~"):
        return p[1:] # Remove
        the '~' from negated literals
    return f"~{p}"\n\n\n\n\n\ndef resolution(kb, query):
    """Perform resolution on
    the knowledge base to
    prove the query."""
    \n    # Add the negation of the
    # query to the knowledge
    # base (for proof by
    # contradiction)
    kb.append(negation(query))\n\n    # Apply the resolution rule
    # until we reach an empty
    # clause (which means
    # contradiction)
    new_clauses = set(kb) #
```

Program 8- Unification

Algorithm:

Date 19/11/24
Page _____

* Unification in first order logic

Expressions : $A ::= \text{Love}(n, y)$
 $B ::= \text{Love}(\text{John}, \text{Mary})$

Unification Steps = Substitution

1) Compare $\text{Love}(n, y)$ & $\text{Love}(\text{John}, \text{Mary})$
- predicate symbol 'Love' matches
[] Args, [] Arg in = both expression.

2. first() Argument : A prn
• In A : n (a variable)
• In B : John (a const)
• Unify n with John
Substitution : $n = \text{John}$.

3. Second Argument
• In A : y (a variable)
• In B : Mary (a const)
• Unify 'y' with Mary : Substitution
: $y = \text{Mary}$.

Result : Unified expression :
 $\text{Love}(\text{John}, \text{Mary})$

CODE:

```
def is_variable(term):
    """Check if a term is a variable (starts with an uppercase letter)."""
    return isinstance(term, str) and term[0].isupper()

def unify(x, y, subst):
    """
    Perform unification of two terms x and y under a given substitution subst.
    """
    if subst is None: # If unification fails, return None
        return None
    elif x == y: # If terms are identical, return the current substitution
        return subst
    elif is_variable(x): # If x is a variable, unify it with y
        return unify_variable(x, y, subst)
    elif is_variable(y): # If y is a variable, unify it with x
        return unify_variable(y, x, subst)
    elif isinstance(x, tuple) and isinstance(y, tuple): # If both are compound terms
        if len(x) != len(y):
            return None
        for xi, yi in zip(x, y):
            subst = unify(xi, yi, subst)
        return subst
    else:
        return None

def unify_variable(var, term, subst):
    """
    Unify a variable with a term under a substitution subst.
    """
    if var in subst:
        return unify(subst[var], term, subst)
    elif term in subst:
        return unify(var, subst[term], subst)
    elif occurs_check(var, term, subst):
        return None
    else:
        subst[var] = term
    return subst

def occurs_check(var, term, subst):
    """
    Check for circular references in unification (occurs check).
    """

```

```
if var == term:  
    return True  
elif isinstance(term, tuple):  
    return any(occurs_check(var, t, subst) for t in term)  
elif term in subst:  
    return occurs_check(var, subst[term], subst)  
return False
```

```
def unify_terms(term1, term2):  
    """  
    Top-level function for unification.  
    Returns the substitution if unification succeeds, else None.  
    """  
    return unify(term1, term2, {})
```

```
# Example usage  
if __name__ == "__main__":  
    # Terms are represented as tuples  
    term1 = ("f", "X", "a") # f(X, a)  
    term2 = ("f", "b", "a") # f(b, a)  
  
    result = unify_terms(term1, term2)  
  
    if result:  
        print("Unification succeeded!")  
        print("Substitution:", result)  
    else:  
        print("Unification failed.")
```

Program 9 - Knowledge base consisting of first order logic statements and prove the given query using forward reasoning..

Algorithm

forward chaining Algorithm

1. Initialize Knowledge Base

Representation in FOL

— It is a crime for an American to sell weapons to hostile nations

Let's say p, q, r are variables

$\text{American}(p) \wedge \text{weapon}(q) \wedge \text{sells}(p, q, r) \wedge \text{Hostile}(r) \Rightarrow \text{Criminal}(p)$

— Country A has some missiles

$\exists x \text{ Owns}(A, x) \wedge \text{Missile}(x)$

Existential Instantiation, introducing a new constant T_1 :

~~Own(A, T₁)~~
~~Missile(T₁)~~

— All of the missiles were sold to country A by Robert

$\forall x \text{ Missiles}(x) \wedge \text{Owns}(A, x) \Rightarrow \text{Sells}(\text{Robert}, A, x)$

→ Missiles are weapons

$$\text{Missile}(x) \Rightarrow \text{Weapon}(x)$$

→ Enemy of America is known as hostile

$$\nexists \text{Enemy}(x, \text{America}) \Rightarrow \text{Hostile}(x)$$

→ Robert is an American

American(Robert)

→ The country A, an enemy of America.

enemy(A, America)

To Prove:

Robert is Criminal

Criminal(Robert)

P-dad

Date 3/12/24

Page _____

forward Chaining Proof

American(Robert) | Missile(T1) | Owns(A, T1)

Enemy(A, American)

Weapons(T1)

Sells(Robert, T1, A)

Hostile(A)

Robert(Criminal)

American(p) \wedge weapon(q) \wedge sells(p, q, r)

\wedge Hostile(r) \Rightarrow Criminal(p)

Code

```
knowledge_base = {
    "facts": {
        "American(Robert)": True,
        "Enemy(A, America)": True,
        "Owns(A, T1)": True,
        "Missile(T1)": True,
    },
    "rules": [
        {"if": ["Missile(x)", "then": ["Weapon(x)"]]},
        {"if": ["Enemy(x, America)", "then": ["Hostile(x)"]]},
        {"if": ["Missile(x)", "Owns(A, x)", "then": ["Sells(Robert, x, A)"]]},
        {
            "if": ["American(p)", "Weapon(q)", "Sells(p, q, r)", "Hostile(r)", "then": ["Criminal(p)"]],
        },
    ],
}
def forward_chaining(kb):
    facts =
    kb["facts"].copy()
    rules =
    kb["rules"]
    inferred =
    set()
    while True:
        new_inferences = set()
        for rule in rules:
            if_conditions = rule["if"]
            then_conditions = rule["then"]
            substitutions = {}
            all_conditions_met = True
            for condition in if_conditions:
                predicate, args =
                condition.split("(")
                args =
                args[:-1].split(",")
                matched = False
                for fact in facts:
                    fact_predicate, fact_args = fact.split("(")
                    fact_args =
                    fact_args[:-1].split(",")
                    if predicate == fact_predicate and len(args) == len(fact_args):
```

```
temp_subs = {}
for var, val in zip(args, fact_args):
if var.islower():
if var in temp_subs and temp_subs[var] != val:
break
```

```

temp_subs[var] = val
elif var != val:
    break
else:
    matched = True
    substitutions.update(temp_subs)
    break
if not matched:
    all_conditions_met = False
    break
44if all_conditions_met:
    for condition in then_conditions:
        predicate, args = condition.split("(")
        args = args[:-1].split(",")
        new_fact = predicate + "(" + ",".join(substitutions.get(arg, arg) for arg in args)
        + ")"
        new_inferences.add(new_fact)
    if new_inferences - inferred:
        inferred.update(new_inferences) facts.update({fact:
            True for fact in new_inferences}) else:
        break
    return inferred
result = forward_chaining(knowledge_base)
print('Yashraj Sinha (1BM22CS335):')
if "Criminal(Robert)" in result:
    print("Proved: Robert is a criminal.")
else:
    print("Could not prove that Robert is a criminal.")

```

OUTPUT:

Yashraj Sinha (1BM22CS335):
Proved: Robert is a criminal.

Program 10 - Implement Alpha-Beta Pruning.

Algorithm

★ Pseudocode : 8 Queens with α - β pruning.

```
function ALPHA-BETA-SEARCH(state, row, α, β) returns a list of soln
    if row > 8 then return [state]
    solutions ← []
    for col in 1 to 8 do
        if IS-SAFE(state, row, col) then
            newState ← state + [col]
            result ← ALPHA-BETA-SEARCH(newState, row+1, α, β)
            solutions . extend (result)
            α ← max (α, ln(solutions))
        if α ≥ β then break.
    return solutions

function IS-SAFE(state, row, col) returns boolean
    for r in 1 to row-1 do
        c ← state(r-1)
```

Date _____
Page _____

if $c == \text{col}$ or $\text{abs}(c - \text{col}) == \text{abs}(r - \text{row})$

Thru

return false

return true; } (q, x)

function SOLVE-8-GUENNS() returns
a list of solutions.

$\alpha \leftarrow -\infty$

$\beta \leftarrow +\infty$

return ALPHA-BETA-SEARCH([], 1, &, β)

→ Output :-

Code

```
import math

def alpha_beta_pruning(depth, node_index, is_maximizing_player, values, alpha, beta,
max_depth):
    # Base case: when the maximum depth is
    reached if depth == max_depth:
        return values[node_index]
    if is_maximizing_player:
        best = -math.inf
        # Recur for left and right children
        for i in range(2):
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, False, values, alpha, beta,
max_depth)
            best = max(best, val)
            alpha = max(alpha, best)
        # Prune the remaining nodes
        if beta <= alpha:
            break
        return best
    else:
        best = math.inf
        # Recur for left and right children
        for i in range(2):
            val = alpha_beta_pruning(depth + 1, node_index * 2 + i, True, values, alpha, beta,
max_depth)
            best = min(best, val)
            beta = min(beta, best)
    # Prune the remaining nodes
    if beta <= alpha:
        break
    return best

print("Yashraj Sinha (1BM22CS335):")

# Example usage
if __name__ == "__main__":
    # Example tree represented as a list of leaf node values
    values = [3, 5, 6, 9, 1, 2, 0, -1]
    max_depth = 3 # Height of the tree
    result = alpha_beta_pruning(0, 0, True, values, -math.inf, math.inf, max_depth)
    print("The optimal value is:", result)
```

OUTPUT:

Yashraj Sinha (1BM22CS335):

The optimal value is: 5