

No matter the chosen element we can have the leftover elements of form ([a,b] - row , [c,d] - column and [e,f,g,h] as box)

We iterate (grover) the algorithm thrice to find the positions of a type of element, say 1. Now no of solutions for this if all 8 are empty are four so we run grovers algo pi/4*sqrt(2**8/4) == 6 times and it changes with the number of filled squares in leftover 8.

Input [a,b,c...h] -> 8 bit string with ones representing the positions of that value

Ex: Image 1 - find 2

We give the conditions and for every filled box we give that value as $0 \rightarrow a=0$ and c=0 is added to condition

 (a^b) and (c^d) and (c^e^f) and (d^g^h) and (a^e^g) and (b^f^h) and $(e^f+g^h)=1$

We run this thrice (say get for 1,2,3) to obtain all the values

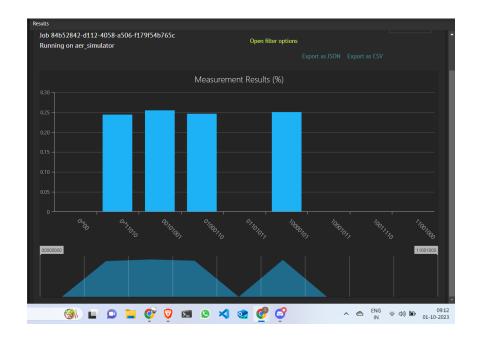
We have included model and files in the repo as well

Stats after Execution:

Depth: 4679 Width: 21

Gate count U : 3926 CX : 3786

IBM Quantum, aer_simulator, simulator



All the four results are valid.