

# ae-2017-1 to 13

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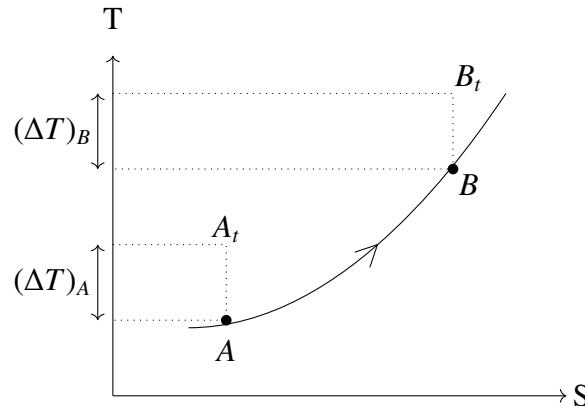
- 1) Given the vectors  $\mathbf{v}_1 = \hat{i} + 3\hat{j}$ ;  $\mathbf{v}_2 = 2\hat{i} - 4\hat{j} + 3\hat{k}$ , the vector  $\mathbf{v}_3$  that is perpendicular to both  $\mathbf{v}_1$  and  $\mathbf{v}_2$  is given by:
  - a)  $\mathbf{v}_3 = \mathbf{v}_1 - (\mathbf{v}_1 \cdot \mathbf{v}_2) \frac{\mathbf{v}_2}{\|\mathbf{v}_2\|}$
  - b)  $\mathbf{v}_3 = \hat{k}$
  - c)  $\mathbf{v}_3 = \mathbf{v}_2 - (\mathbf{v}_1 \cdot \mathbf{v}_2) \frac{\mathbf{v}_1}{\|\mathbf{v}_1\|}$
  - d)  $\mathbf{v}_3 = \frac{\mathbf{v}_1 \times \mathbf{v}_2}{\|\mathbf{v}_1 \times \mathbf{v}_2\|}$
- 2) The value of the integral  $I = \int_C ((x-y)dx + x^2dy)$ , with  $C$  the boundary of the square  $0 \leq x \leq 2$ ;  $0 \leq y \leq 2$ , is \_\_\_\_\_
- 3) Let  $\mathbf{v}(t)$  be a unit vector that is a function of the parameter  $t$ . Then  $\mathbf{v} \cdot \frac{d\mathbf{v}}{dt} =$  \_\_\_\_\_
- 4) The eigenvalues  $\lambda_n$  and eigenfunctions  $u_n(x)$  of the Sturm-Liouville problem

$$\frac{d^2y}{dx^2} + k^2\lambda y = 0, 0 < x < 1; y(0) = 0, y(1) = 0$$

are given by:

- a)  $\lambda_n = n^2\pi^2$ ;  $u_n(x) = \sin \lambda_n x, n = 0, \pm 1, \pm 2, \dots, \infty$
  - b)  $\lambda_n = \frac{n^2\pi^2}{k^2}$ ;  $u_n(x) = \sin kn\pi x, n = 0, \pm 1, \pm 2, \dots, \infty$
  - c)  $\lambda_n = \frac{n^2\pi^2}{k^2}$ ;  $u_n(x) = \sin n\pi x, n = 0, \pm 1, \pm 2, \dots, \infty$
  - d)  $\lambda_n = n^2\pi^2$ ;  $u_n(x) = \sin n\pi x, n = 0, \pm 1, \pm 2, \dots, \infty$
- 5) 3-point Gaussian integration formula is given by:  $\int_{-1}^1 f(x) dx \approx \sum_{j=1}^3 A_j f(x_j)$  with  $x_1 = 0, x_2 = -x_3 = -\sqrt{\frac{3}{5}}$ ;  $A_1 = \frac{8}{9}, A_2 = A_3 = \frac{5}{9}$ . This formula exactly integrates
    - a)  $f(x) = 5 - x^7$
    - b)  $f(x) = 2 + 3x + 6x^4$
    - c)  $f(x) = 13 + 6x^3 + x^6$
    - d)  $f(x) = e^{-x^2}$
  - 6) Which one of the following statements is NOT true
    - a) The pitching moment of any airfoil at any angle of attack is always zero at the center of pressure
    - b) The pitching moment of any airfoil at any angle of attack is always zero at the aerodynamic center
    - c) The center of pressure and aerodynamic center coincide for a symmetric airfoil
    - d) The pitching moment about the aerodynamic center, for any airfoil, does not vary with angle of attack
  - 7) Which one of the following statements is NOT true
    - a) Compared to a laminar boundary layer, a turbulent boundary layer is more desirable on a wing operating at large angle of attack
    - b) The skin friction drag for a turbulent boundary layer is larger than that for a laminar boundary layer
    - c) The location of transition from laminar to turbulent boundary layer depends only on the operating Reynolds number
    - d) A separated flow does not necessarily lead to a turbulent boundary layer

- 8) A De Laval nozzle is to be designed for an exit Mach number of 1.5. The reservoir conditions are given as  $P_o = 1 \text{ atm (gage)}$ ,  $T_o = 20^\circ \text{C}$ ,  $\gamma = 1.4$ . Assuming shock free flow in the nozzle, the exit absolute pressure (in atm) is \_\_\_\_\_ (in three decimal places)
- 9) Consider a steady one dimensional flow of a perfect gas with heat transfer in a duct. The T-s diagram (shown below) shows both the static and the stagnation conditions at two locations, A and B, in the duct.  $A_t$  and  $B_t$  denote stagnation conditions for states A and B, respectively. It is known that  $(\Delta T)_A = (\Delta T)_B$ .  $M_A$  and  $M_B$  are the Mach numbers of the flow at locations A and B.



Which of the following statements is true about the flow.

- Flow is subsonic and  $M_A < M_B$
  - Flow is supersonic and  $M_A > M_B$
  - Flow is subsonic and  $M_A > M_B$
  - Flow is supersonic and  $M_A < M_B$
- 10) To ensure only the longitudinal static stability (and not the condition for equilibrium) of a low speed aircraft, the aircraft components must be designed to satisfy which one of the following conditions:
- $\frac{\partial C_m}{\partial \alpha} < 0$  and  $C_{m_0} > 0$
  - $\frac{\partial C_m}{\partial \alpha} < 0$
  - $\frac{\partial C_m}{\partial C_L} < 0$  and  $C_{m_0} < 0$
  - $\frac{\partial C_m}{\partial C_L} = 0.0$
- 11) Which of the following statement(s) is/are true about the shear centre of a cross-section:
- P: It is that point in the cross-section through which shear loads produce no twisting.  
 Q: This point is also the centre of twist of sections subjected to pure torsion.  
 R: The normal stress at this point is always zero.
- P, Q and R
  - P only
  - P and Q only
  - P and R only
- 12) Let  $\bar{N}_m$  and  $\bar{N}_0$  be respectively the non-dimensional locations of the stick-fixed maneuver point and stick-fixed neutral point of a low speed convectional aircraft. These distances are measured with respect to the nose of the fuselage. The numerical value of  $\bar{N}_m - \bar{N}_0$
- will always be negative
  - will always be positive
  - will always be zero
  - can have any value depending on the location of the center of gravity of the aircraft
- 13) The phenomenon of rudder lock in conventional low speed aircraft is primarily due to

- a) large value of directional derivative,  $C_{n\beta}$
- b) the sidewash due to fuselage on the vertical stabilizer
- c) the tendency of rudder to float rapidly at high angles of side-slip the sidewash due to wing on the vertical stabilizer