

4-4.4-13

AI24BTECH11020 - RISHIKA KOTHA

Question: Equation of the circle with centre on the Y axis and passing through the origin and the point (2, 3) is

a) $3x^2 + 3y^2 - 13y = 0$

b) $3x^2 + 3y^2 + 13x + 3 = 0$

c) $6x^2 + 6y^2 - 13x = 0$

d) $x^2 + y^2 + 13x + 3 = 0$

Solution: from the given information, the following equations can be formulated

$$\|P\|^2 + 2u^T P + f = 0 \quad (0.1)$$

$$u = ke_2 \quad (0.2)$$

$$\|u\|^2 - f = r^2 \quad (0.3)$$

$$P = \begin{pmatrix} 2 \\ 3 \end{pmatrix} \text{ and } r = 13/6 \quad (0.4)$$

$$\|P\|^2 + 2ke_2^T P + \|u\|^2 = r^2 \quad (0.5)$$

$$k^2 + 2ke_2^T P + \|P\|^2 - r^2 = 0 \quad (0.6)$$

$$k = -e_2^T P \pm \sqrt{(e_2^T P)^2 + r^2 - \|P\|^2} \quad (0.7)$$

Substituting numerical values,

$$k = 13/6, -13/6 \quad (0.8)$$

since $k < 0$, $k = -13/6$

∴ the equation of the circle is $3x^2 + 3y^2 - 13y = 0$.

parameter	value
centre(C)	$\begin{pmatrix} 0 \\ 13/6 \end{pmatrix}$
Origin(O)	$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$
point(P)	$\begin{pmatrix} 2 \\ 3 \end{pmatrix}$
radius(r)	13/6

