svm

September 29, 2023

```
[1]: # This mounts your Google Drive to the Colab VM.
     from google.colab import drive
     drive.mount('/content/drive', force_remount=True)
     # Enter the foldername in your Drive where you have saved the unzipped
     # assignment folder, e.g. 'cs231n/assignments/assignment1/'
     FOLDERNAME = 'cs231n/assignments/assignment1/'
     assert FOLDERNAME is not None, "[!] Enter the foldername."
     # Now that we've mounted your Drive, this ensures that
     # the Python interpreter of the Colab VM can load
     # python files from within it.
     import sys
     sys.path.append('/content/drive/My Drive/{}'.format(FOLDERNAME))
     # This downloads the CIFAR-10 dataset to your Drive
     # if it doesn't already exist.
     %cd drive/My\ Drive/$FOLDERNAME/cs231n/datasets/
     !bash get datasets.sh
     %cd /content/drive/My\ Drive/$FOLDERNAME
```

Mounted at /content/drive /content/drive/My Drive/cs231n/assignments/assignment1/cs231n/datasets /content/drive/My Drive/cs231n/assignments/assignment1

1 Multiclass Support Vector Machine exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

In this exercise you will:

- implement a fully-vectorized **loss function** for the SVM
- implement the fully-vectorized expression for its analytic gradient
- check your implementation using numerical gradient
- use a validation set to tune the learning rate and regularization strength
- optimize the loss function with SGD
- visualize the final learned weights

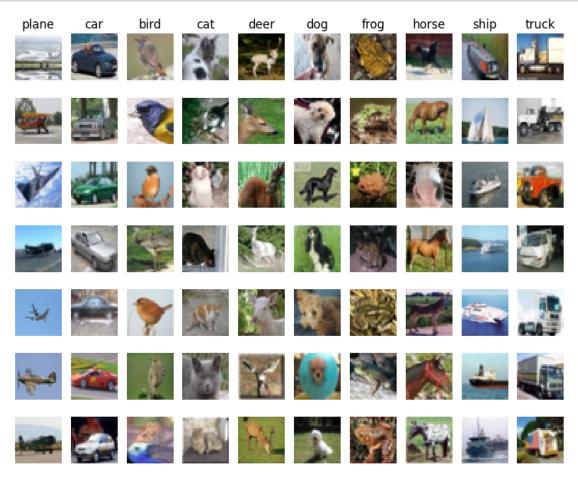
```
[2]: # Run some setup code for this notebook.
     import random
     import numpy as np
     from cs231n.data_utils import load_CIFAR10
     import matplotlib.pyplot as plt
     # This is a bit of magic to make matplotlib figures appear inline in the
     # notebook rather than in a new window.
     %matplotlib inline
     plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
     plt.rcParams['image.interpolation'] = 'nearest'
     plt.rcParams['image.cmap'] = 'gray'
     # Some more magic so that the notebook will reload external python modules;
     # see http://stackoverflow.com/questions/1907993/
      \rightarrow autoreload-of-modules-in-ipython
     %load ext autoreload
     %autoreload 2
```

1.1 CIFAR-10 Data Loading and Preprocessing

```
[3]: # Load the raw CIFAR-10 data.
     cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
     # Cleaning up variables to prevent loading data multiple times (which may cause_
      →memory issue)
     try:
       del X_train, y_train
       del X_test, y_test
       print('Clear previously loaded data.')
     except:
       pass
     X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
     # As a sanity check, we print out the size of the training and test data.
     print('Training data shape: ', X_train.shape)
     print('Training labels shape: ', y_train.shape)
     print('Test data shape: ', X_test.shape)
     print('Test labels shape: ', y_test.shape)
```

Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)

```
[4]: # Visualize some examples from the dataset.
     # We show a few examples of training images from each class.
     classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', _
     ⇔'ship', 'truck']
     num_classes = len(classes)
     samples_per_class = 7
     for y, cls in enumerate(classes):
         idxs = np.flatnonzero(y_train == y)
         idxs = np.random.choice(idxs, samples_per_class, replace=False)
         for i, idx in enumerate(idxs):
             plt_idx = i * num_classes + y + 1
             plt.subplot(samples_per_class, num_classes, plt_idx)
             plt.imshow(X_train[idx].astype('uint8'))
             plt.axis('off')
             if i == 0:
                 plt.title(cls)
     plt.show()
```



```
[5]: # Split the data into train, val, and test sets. In addition we will
     # create a small development set as a subset of the training data;
     # we can use this for development so our code runs faster.
     num_training = 49000
     num validation = 1000
     num_test = 1000
     num_dev = 500
     # Our validation set will be num validation points from the original
     # training set.
     mask = range(num training, num training + num validation)
     X_val = X_train[mask]
     y_val = y_train[mask]
     # Our training set will be the first num train points from the original
     # training set.
     mask = range(num_training)
     X_train = X_train[mask]
     y_train = y_train[mask]
     # We will also make a development set, which is a small subset of
     # the training set.
     mask = np.random.choice(num_training, num_dev, replace=False)
     X dev = X train[mask]
     y_dev = y_train[mask]
     # We use the first num_test points of the original test set as our
     # test set.
     mask = range(num_test)
     X_test = X_test[mask]
     y_test = y_test[mask]
     print('Train data shape: ', X_train.shape)
     print('Train labels shape: ', y_train.shape)
     print('Validation data shape: ', X_val.shape)
     print('Validation labels shape: ', y_val.shape)
     print('Test data shape: ', X_test.shape)
     print('Test labels shape: ', y_test.shape)
    Train data shape: (49000, 32, 32, 3)
    Train labels shape: (49000,)
    Validation data shape: (1000, 32, 32, 3)
    Validation labels shape: (1000,)
    Test data shape: (1000, 32, 32, 3)
    Test labels shape: (1000,)
```

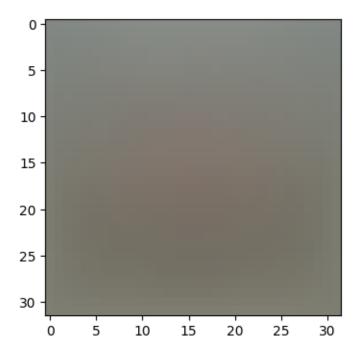
```
[6]: # Preprocessing: reshape the image data into rows
   X_train = np.reshape(X_train, (X_train.shape[0], -1))
   X_val = np.reshape(X_val, (X_val.shape[0], -1))
   X_test = np.reshape(X_test, (X_test.shape[0], -1))
   X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))

# As a sanity check, print out the shapes of the data
   print('Training data shape: ', X_train.shape)
   print('Validation data shape: ', X_val.shape)
   print('Test data shape: ', X_test.shape)
   print('dev data shape: ', X_dev.shape)

Training data shape: (49000, 3072)
   Validation data shape: (1000, 3072)
   Test data shape: (1000, 3072)
   dev data shape: (500, 3072)
```

```
[7]: # Preprocessing: subtract the mean image
     # first: compute the image mean based on the training data
     mean_image = np.mean(X_train, axis=0)
     print(mean_image[:10]) # print a few of the elements
     plt.figure(figsize=(4,4))
     plt.imshow(mean_image.reshape((32,32,3)).astype('uint8')) # visualize the mean_i
      \hookrightarrow image
     plt.show()
     # second: subtract the mean image from train and test data
     X_train -= mean_image
     X_val -= mean_image
     X_test -= mean_image
     X_dev -= mean_image
     # third: append the bias dimension of ones (i.e. bias trick) so that our SVM
     # only has to worry about optimizing a single weight matrix W.
     X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
     X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
     X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
     X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
     print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
```

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)

1.2 SVM Classifier

Your code for this section will all be written inside cs231n/classifiers/linear_svm.py.

As you can see, we have prefilled the function svm_loss_naive which uses for loops to evaluate the multiclass SVM loss function.

```
[8]: # Evaluate the naive implementation of the loss we provided for you:
from cs231n.classifiers.linear_svm import svm_loss_naive
import time

# generate a random SVM weight matrix of small numbers
W = np.random.randn(3073, 10) * 0.0001

loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.000005)
print('loss: %f' % (loss, ))
```

loss: 8.967418

The grad returned from the function above is right now all zero. Derive and implement the gradient for the SVM cost function and implement it inline inside the function svm_loss_naive. You will find it helpful to interleave your new code inside the existing function.

To check that you have correctly implemented the gradient correctly, you can numerically estimate the gradient of the loss function and compare the numeric estimate to the gradient that you computed. We have provided code that does this for you:

```
[9]: # Once you've implemented the gradient, recompute it with the code below
     # and gradient check it with the function we provided for you
     # Compute the loss and its gradient at W.
     loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.0)
     # Numerically compute the gradient along several randomly chosen dimensions, and
     \# compare them with your analytically computed gradient. The numbers should
      \rightarrow match
     # almost exactly along all dimensions.
     from cs231n.gradient_check import grad_check_sparse
     f = lambda w: svm_loss_naive(w, X_dev, y_dev, 0.0)[0]
     grad_numerical = grad_check_sparse(f, W, grad)
     # do the gradient check once again with regularization turned on
     # you didn't forget the regularization gradient did you?
     loss, grad = svm loss naive(W, X dev, y dev, 5e1)
     f = lambda w: svm_loss_naive(w, X_dev, y_dev, 5e1)[0]
     grad_numerical = grad_check_sparse(f, W, grad)
```

```
numerical: 11.042283 analytic: 0.000000, relative error: 1.000000e+00
numerical: 1.699520 analytic: 0.000000, relative error: 1.000000e+00
numerical: 6.855507 analytic: 0.000000, relative error: 1.000000e+00
numerical: -0.912618 analytic: 0.000000, relative error: 1.000000e+00
numerical: 9.911521 analytic: 0.000000, relative error: 1.000000e+00
numerical: 3.268000 analytic: 0.000000, relative error: 1.000000e+00
numerical: -10.220423 analytic: 0.000000, relative error: 1.000000e+00
numerical: -2.412000 analytic: 0.000000, relative error: 1.000000e+00
numerical: -6.367687 analytic: 0.000000, relative error: 1.000000e+00
numerical: -4.606000 analytic: 0.000000, relative error: 1.000000e+00
numerical: -14.004909 analytic: -0.001762, relative error: 9.997484e-01
numerical: -11.582655 analytic: 0.006174, relative error: 1.000000e+00
numerical: 8.354130 analytic: 0.002433, relative error: 9.994178e-01
numerical: -20.889944 analytic: 0.007170, relative error: 1.000000e+00
numerical: 16.217820 analytic: -0.000159, relative error: 1.000000e+00
numerical: -1.190195 analytic: 0.005412, relative error: 1.000000e+00
numerical: 1.330341 analytic: 0.011780, relative error: 9.824464e-01
numerical: 15.946821 analytic: -0.003691, relative error: 1.000000e+00
numerical: -8.981715 analytic: -0.004985, relative error: 9.988905e-01
numerical: -6.708374 analytic: -0.010764, relative error: 9.967959e-01
```

Inline Question 1

It is possible that once in a while a dimension in the gradcheck will not match exactly. What could such a discrepancy be caused by? Is it a reason for concern? What is a simple example in one dimension where a gradient check could fail? How would change the margin affect of the frequency of this happening? Hint: the SVM loss function is not strictly speaking differentiable

Your Answer: The SVM loss function is defined as the maximum between 0 and the score value

subtracted from the margin, and it is not differentiable precisely at hinge point where margin equals 1. During gradient checks, it is expected that the analytical gradient and numerically approximated gradient may not match exactly.

To check if differentiation fails at the hinge point, both analytical and numerical methods can be used. The error between the two gradients is typically very small but not exactly zero.

Increasing the safety margin to avoid the exact hinge point (e.g., using margin of 1.01 instead of 1) could potentially mitigate the issue, but it comes at the cost of allowing more margin violations, which might lead to lower classification accuracy. Thus, there is a trade-off between achieving a smoother loss surface and maintaining the classification performance.

Naive loss: 8.967418e+00 computed in 0.018630s Vectorized loss: 8.967418e+00 computed in 0.013200s difference: -0.000000

```
[11]: # Complete the implementation of sum_loss_vectorized, and compute the gradient
# of the loss function in a vectorized way.

# The naive implementation and the vectorized implementation should match, but
# the vectorized version should still be much faster.
tic = time.time()
_, grad_naive = svm_loss_naive(W, X_dev, y_dev, 0.000005)
toc = time.time()
print('Naive loss and gradient: computed in %fs' % (toc - tic))

tic = time.time()
_, grad_vectorized = svm_loss_vectorized(W, X_dev, y_dev, 0.000005)
toc = time.time()
print('Vectorized loss and gradient: computed in %fs' % (toc - tic))
```

```
# The loss is a single number, so it is easy to compare the values computed
# by the two implementations. The gradient on the other hand is a matrix, so
# we use the Frobenius norm to compare them.
difference = np.linalg.norm(grad_naive - grad_vectorized, ord='fro')
print('difference: %f' % difference)
```

Naive loss and gradient: computed in 0.029247s Vectorized loss and gradient: computed in 0.012363s difference: 3040.613243

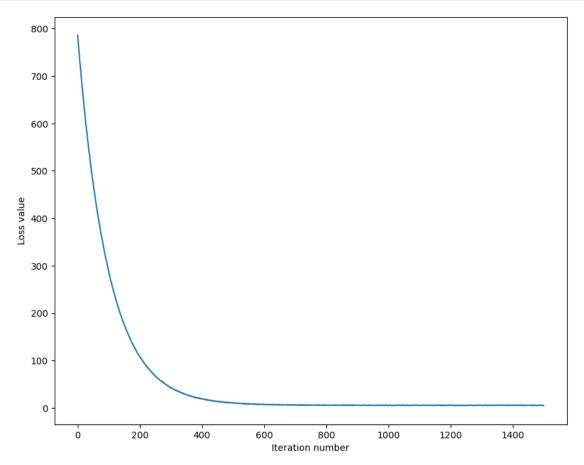
1.2.1 Stochastic Gradient Descent

We now have vectorized and efficient expressions for the loss, the gradient and our gradient matches the numerical gradient. We are therefore ready to do SGD to minimize the loss. Your code for this part will be written inside cs231n/classifiers/linear_classifier.py.

```
iteration 0 / 1500: loss 785.672391
iteration 100 / 1500: loss 287.056242
iteration 200 / 1500: loss 107.367213
iteration 300 / 1500: loss 42.321357
iteration 400 / 1500: loss 19.346025
iteration 500 / 1500: loss 10.252051
iteration 600 / 1500: loss 6.860802
iteration 700 / 1500: loss 5.715234
iteration 800 / 1500: loss 5.439343
iteration 900 / 1500: loss 5.836427
iteration 1000 / 1500: loss 5.087377
iteration 1100 / 1500: loss 5.760094
iteration 1200 / 1500: loss 5.525966
iteration 1300 / 1500: loss 5.303209
iteration 1400 / 1500: loss 5.129233
That took 11.860566s
```

```
[13]: # A useful debugging strategy is to plot the loss as a function of
    # iteration number:
    plt.plot(loss_hist)
    plt.xlabel('Iteration number')
```

```
plt.ylabel('Loss value')
plt.show()
```



```
[14]: # Write the LinearSVM.predict function and evaluate the performance on both the
# training and validation set
y_train_pred = svm.predict(X_train)
print('training accuracy: %f' % (np.mean(y_train == y_train_pred), ))
y_val_pred = svm.predict(X_val)
print('validation accuracy: %f' % (np.mean(y_val == y_val_pred), ))
```

training accuracy: 0.367184 validation accuracy: 0.372000

```
[15]: # Use the validation set to tune hyperparameters (regularization strength and # learning rate). You should experiment with different ranges for the learning # rates and regularization strengths; if you are careful you should be able to # get a classification accuracy of about 0.39 on the validation set.

# Note: you may see runtime/overflow warnings during hyper-parameter search.
```

```
# This may be caused by extreme values, and is not a buq.
# results is dictionary mapping tuples of the form
# (learning_rate, regularization_strength) to tuples of the form
# (training_accuracy, validation_accuracy). The accuracy is simply the fraction
# of data points that are correctly classified.
results = {}
best_val = -1  # The highest validation accuracy that we have seen so far.
best_svm = None # The LinearSVM object that achieved the highest validation
# TODO:
# Write code that chooses the best hyperparameters by tuning on the validation #
# set. For each combination of hyperparameters, train a linear SVM on the
# training set, compute its accuracy on the training and validation sets, and
# store these numbers in the results dictionary. In addition, store the best
# validation accuracy in best_val and the LinearSVM object that achieves this
# accuracy in best sum.
# Hint: You should use a small value for num iters as you develop your
# validation code so that the SVMs don't take much time to train; once you are #
# confident that your validation code works, you should rerun the validation
# code with a larger value for num_iters.
# Provided as a reference. You may or may not want to change these_
→hyperparameters
learning_rates = [1e-7, 2e-7, 5e-8]
regularization_strengths = [2e4, 5e4]
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# To find the optimal Ir and reg strength we have to create 2 loops to figure,
out the best hyperparameters to find the best softmax classifier.
best_learning_rate = 0
best_reg_strength = 0
# Looping over all combinations of hyperparameters
for lr in learning_rates:
   for reg in regularization_strengths:
       # Create a LinearSVM classifier object with the current hyperparameters
       svm = LinearSVM()
       # Training the classifier on the training data with 1200 iterations
       svm.train(X_train, y_train, learning_rate=lr, reg=reg,
                num_iters=1200, verbose=True)
```

```
# Prediction on the training and validation sets
        y_train_pred = svm.predict(X_train)
       y_val_pred = svm.predict(X_val)
        # Computing accuracy on training and validation sets
       train_accuracy = np.mean(y_train == y_train_pred)
        val_accuracy = np.mean(y_val == y_val_pred)
        # Storing the accuracy values in the results dictionary
        results[(lr, reg)] = (train_accuracy, val_accuracy)
        # Checking if this is the best validation accuracy so far and adding to
        if val_accuracy > best_val:
            best_val = val_accuracy
            best svm = svm
            best_learning_rate = lr
            best_reg_strength = reg
print(f"Best Pair of lr and reg is (lr,reg):
 →{(best_learning_rate,best_reg_strength)}")
pass
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# Print out results.
for lr, reg in sorted(results):
   train_accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
                lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' %⊔
 ⇒best val)
```

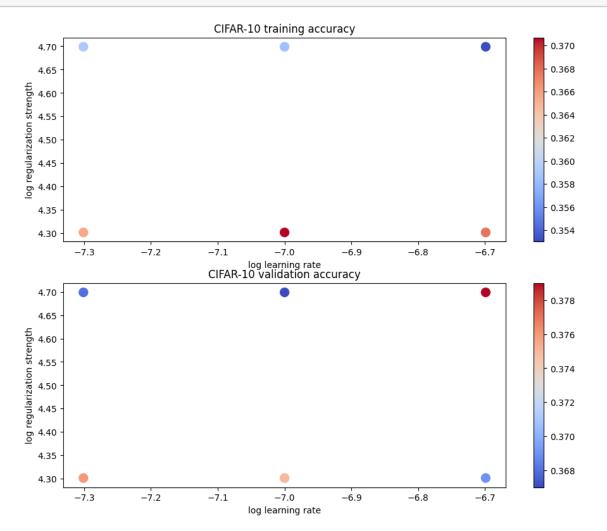
```
iteration 0 / 1200: loss 636.392334 iteration 100 / 1200: loss 282.463443 iteration 200 / 1200: loss 128.486229 iteration 300 / 1200: loss 60.529248 iteration 400 / 1200: loss 29.589954 iteration 500 / 1200: loss 15.707261 iteration 600 / 1200: loss 10.195858 iteration 700 / 1200: loss 7.366290 iteration 800 / 1200: loss 6.459745 iteration 900 / 1200: loss 5.428998 iteration 1000 / 1200: loss 5.239562 iteration 1100 / 1200: loss 5.415083 iteration 0 / 1200: loss 1552.683104 iteration 100 / 1200: loss 209.470476
```

```
iteration 200 / 1200: loss 32.854935
iteration 300 / 1200: loss 9.208821
iteration 400 / 1200: loss 6.303889
iteration 500 / 1200: loss 5.818498
iteration 600 / 1200: loss 5.472783
iteration 700 / 1200: loss 6.092746
iteration 800 / 1200: loss 5.401369
iteration 900 / 1200: loss 5.370357
iteration 1000 / 1200: loss 5.777847
iteration 1100 / 1200: loss 5.929584
iteration 0 / 1200: loss 635.229452
iteration 100 / 1200: loss 127.916151
iteration 200 / 1200: loss 30.352040
iteration 300 / 1200: loss 9.911900
iteration 400 / 1200: loss 6.132874
iteration 500 / 1200: loss 5.532101
iteration 600 / 1200: loss 5.743142
iteration 700 / 1200: loss 5.538841
iteration 800 / 1200: loss 4.813722
iteration 900 / 1200: loss 5.588044
iteration 1000 / 1200: loss 4.998336
iteration 1100 / 1200: loss 5.170718
iteration 0 / 1200: loss 1564.782100
iteration 100 / 1200: loss 32.586659
iteration 200 / 1200: loss 6.038992
iteration 300 / 1200: loss 5.853585
iteration 400 / 1200: loss 6.455551
iteration 500 / 1200: loss 5.598117
iteration 600 / 1200: loss 5.722990
iteration 700 / 1200: loss 5.473484
iteration 800 / 1200: loss 6.258077
iteration 900 / 1200: loss 6.151456
iteration 1000 / 1200: loss 5.568236
iteration 1100 / 1200: loss 5.370822
iteration 0 / 1200: loss 627.550705
iteration 100 / 1200: loss 417.789850
iteration 200 / 1200: loss 279.135987
iteration 300 / 1200: loss 188.053498
iteration 400 / 1200: loss 127.587273
iteration 500 / 1200: loss 87.013248
iteration 600 / 1200: loss 60.033360
iteration 700 / 1200: loss 41.272632
iteration 800 / 1200: loss 29.480405
iteration 900 / 1200: loss 21.738501
iteration 1000 / 1200: loss 15.624555
iteration 1100 / 1200: loss 12.226743
iteration 0 / 1200: loss 1546.822016
iteration 100 / 1200: loss 565.487708
```

```
iteration 200 / 1200: loss 209.495753
     iteration 300 / 1200: loss 79.311019
     iteration 400 / 1200: loss 32.432737
     iteration 500 / 1200: loss 15.301361
     iteration 600 / 1200: loss 8.676943
     iteration 700 / 1200: loss 7.023456
     iteration 800 / 1200: loss 5.886734
     iteration 900 / 1200: loss 5.687791
     iteration 1000 / 1200: loss 5.454899
     iteration 1100 / 1200: loss 5.642962
     Best Pair of 1r and reg is (1r,reg):(2e-07, 50000.0)
     lr 5.000000e-08 reg 2.000000e+04 train accuracy: 0.365633 val accuracy: 0.376000
     lr 5.000000e-08 reg 5.000000e+04 train accuracy: 0.359061 val accuracy: 0.368000
     lr 1.000000e-07 reg 2.000000e+04 train accuracy: 0.370694 val accuracy: 0.375000
     lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.358408 val accuracy: 0.367000
     1r 2.000000e-07 reg 2.000000e+04 train accuracy: 0.367755 val accuracy: 0.369000
     1r 2.000000e-07 reg 5.000000e+04 train accuracy: 0.353000 val accuracy: 0.379000
     best validation accuracy achieved during cross-validation: 0.379000
[16]: # Visualize the cross-validation results
      import math
      import pdb
      # pdb.set trace()
      x_scatter = [math.log10(x[0]) for x in results]
      y_scatter = [math.log10(x[1]) for x in results]
      # plot training accuracy
      marker size = 100
      colors = [results[x][0] for x in results]
      plt.subplot(2, 1, 1)
      plt.tight_layout(pad=3)
      plt.scatter(x_scatter, y_scatter, marker_size, c=colors, cmap=plt.cm.coolwarm)
      plt.colorbar()
      plt.xlabel('log learning rate')
      plt.ylabel('log regularization strength')
      plt.title('CIFAR-10 training accuracy')
      # plot validation accuracy
      colors = [results[x][1] for x in results] # default size of markers is 20
      plt.subplot(2, 1, 2)
      plt.scatter(x_scatter, y_scatter, marker_size, c=colors, cmap=plt.cm.coolwarm)
      plt.colorbar()
      plt.xlabel('log learning rate')
      plt.ylabel('log regularization strength')
```

plt.title('CIFAR-10 validation accuracy')





```
[17]: # Evaluate the best sum on test set
    y_test_pred = best_svm.predict(X_test)
    test_accuracy = np.mean(y_test == y_test_pred)
    print('linear SVM on raw pixels final test set accuracy: %f' % test_accuracy)
```

linear SVM on raw pixels final test set accuracy: 0.365000





Inline question 2

Describe what your visualized SVM weights look like, and offer a brief explanation for why they look they way that they do.

Your Answer: The visualization of SVM weights typically resembles a set of color maps or images, where each pixel corresponds to a feature in the input space. The color or intensity of each pixel represents the weight associated with that feature. These weights capture the importance of each feature in making classification decisions.

For exampkle, if we're using an SVM to classify images of objects, such as cars, the SVM weights for the "car" class might exhibit patterns resembling a car's front view. This is because the SVM has learned that specific features, like the shape of the car's headlights or grille, are significant for identifying cars in the dataset.

In essence, SVM weights visually show the distinctive characteristics and patterns in the training data that are crucial for distinguishing between different classes. They reflect what the SVM has learned about the important features that contribute to its classification decisions.