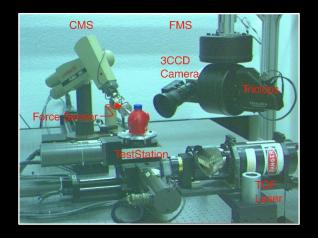
Scanning Physical Interaction Behavior of 3D Objects

Dinesh K. Pai, Kees van den Doel, Doug L. James, Jochen Lang, John E. Lloyd, Joshua L. Richmond, Som H. Yau

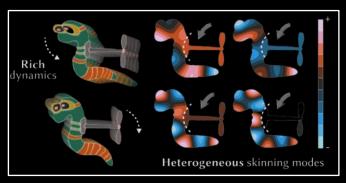
Presented by Rishit Dagli

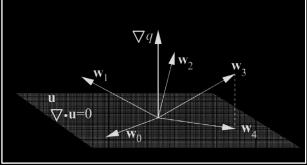


some content taken from the paper

what did we do up until now?

- start with physical laws
- develop some numerical methods to solve these equations
- make sure you have good accuracy and stability in your simulation
- predict behavior from the first laws





[BZCGZJ 2023]

[S 1999]

let us introduce a new problem

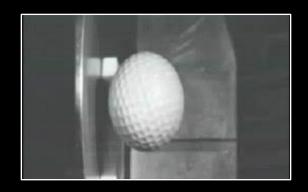
- start with physical laws
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 $\nabla q \Lambda$ \mathbf{w}_1 \mathbf{w}_2 \mathbf{w}_3 $\nabla \cdot \mathbf{u} = 0$

[BZCGZJ 2023]

[S 1999]

- observe the behavior of a real object
- reproduce the observed phenomena
- make sure you can well capture or measure the phenomena



let us introduce a new problem

- start with physical laws
- no longer need models of complex phenomena
- can easily capture certain behaviors which are hard to simulate
- often very efficient for real-time (producing behaviors in real-time)

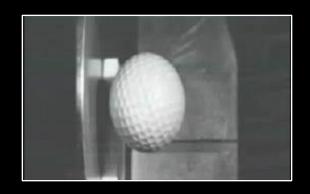




[BZCGZJ 2023]

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- observe the behavior of a real object
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what will we talk about today?

To appear in SIGGRAPH 2001 Conference Proceedings

Scanning Physical Interaction Behavior of 3D Objects

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Department of Computer Science, University of British Columbia, Vancouver, Canada {pai,kvdoel,djames,jlang,lloyd,jlrichmo,shvau}@cs.ubc.ca



(a) Real toy tiger. By design, it is soft to touch and exhibits significant deformation behavior.



(b) Deformable model of tiger scanned by our system, with haptic interaction.



(c) Real clay pot, with glazed regions. The pot exhibits a variety of contact textures and sounds.

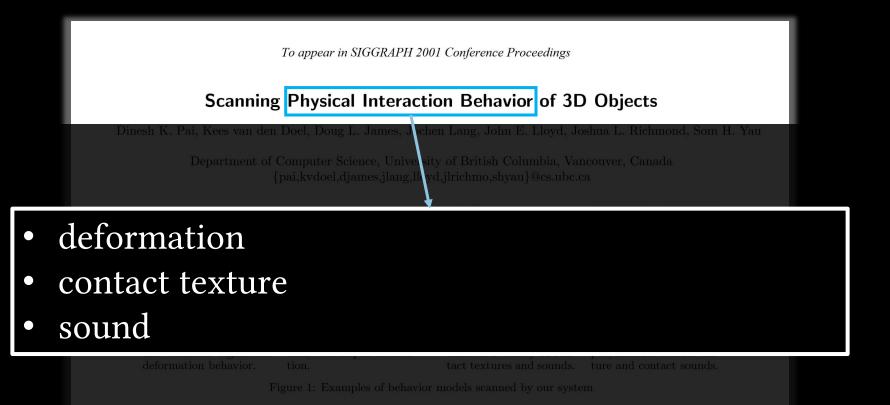


(d) Virtual interaction with scanned model of pot; includes contact texture and contact sounds.

Figure 1: Examples of behavior models scanned by our system

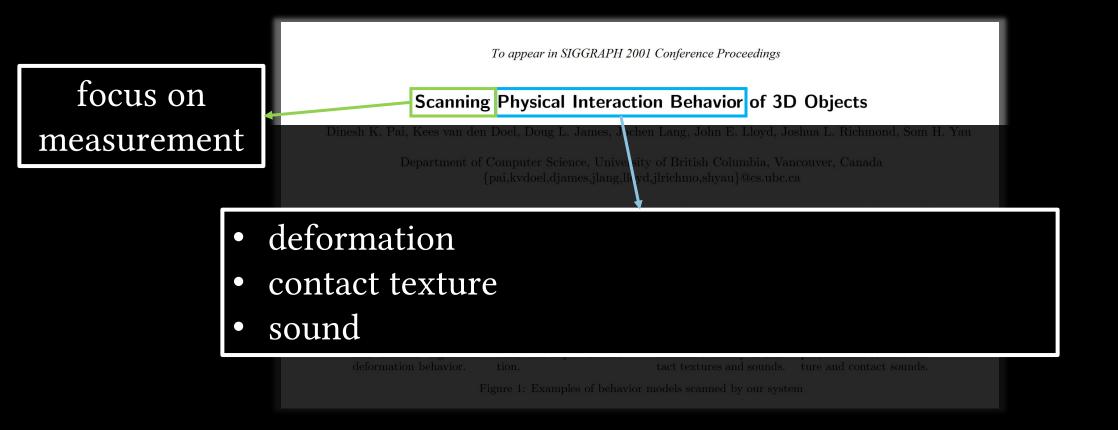
from 2001 **%**

what will we talk about today?



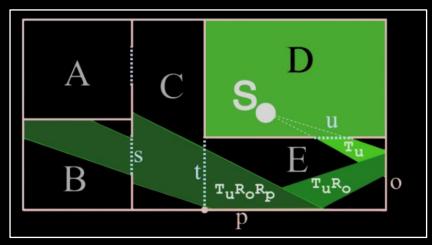


what will we talk about today?

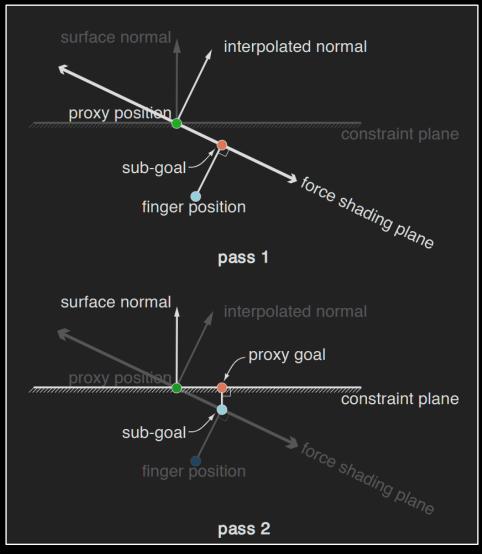


from 2001 **%**

- there were some deformation models back then that kind of worked
- there did exist haptic simulations
- and acoustic modelling techniques or more accurately spatialization techniques



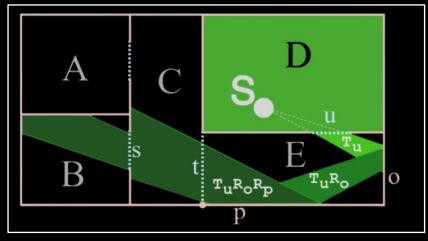
[FCEPSW 1999]



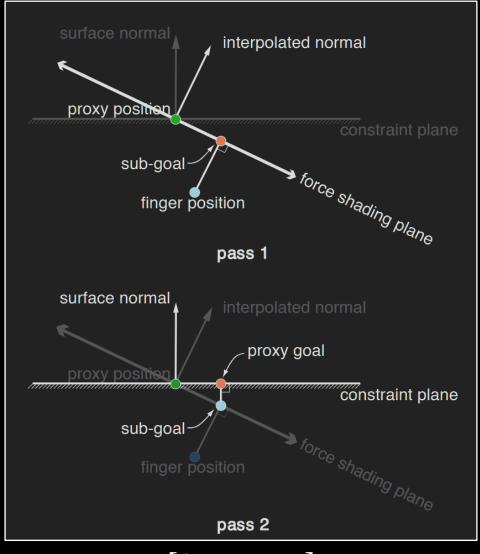
[RKK 1997]

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- and acoustic modelling techniques or more accurately spatialization techniques

often require completely different frameworks



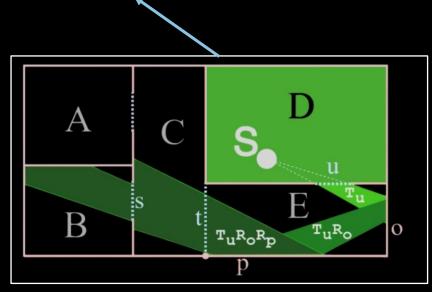
[FCEPSW 1999]



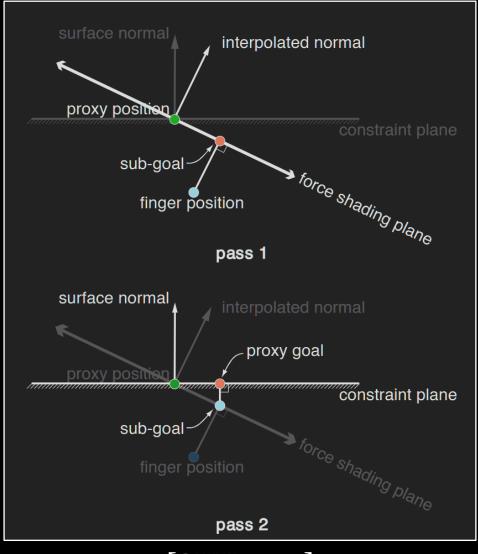
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very far from simulating all the relevant information



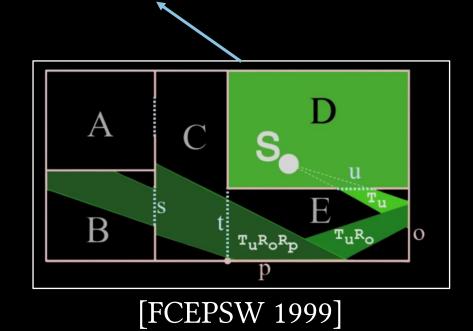
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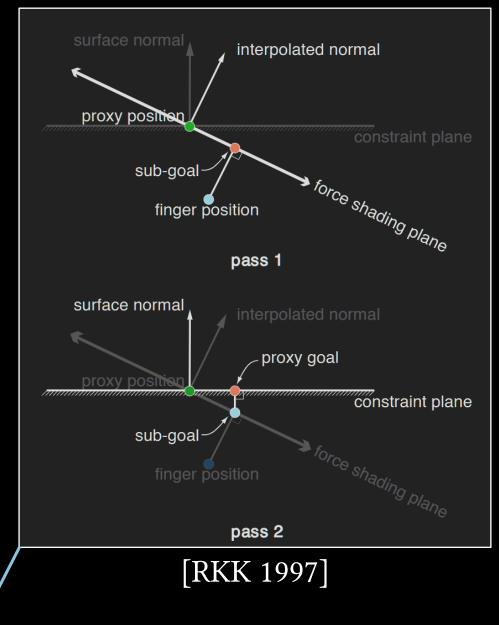


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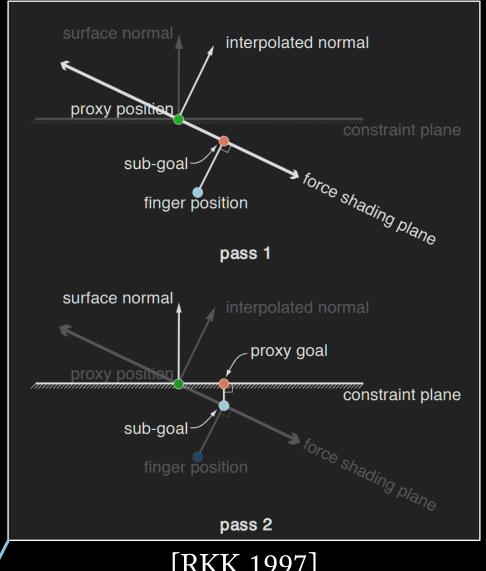
very far from simulating all the relevant information





very hard to make this work to mimic a real object

make models which have such parameters such that they can all be efficiently (automatically) captured just through a real object

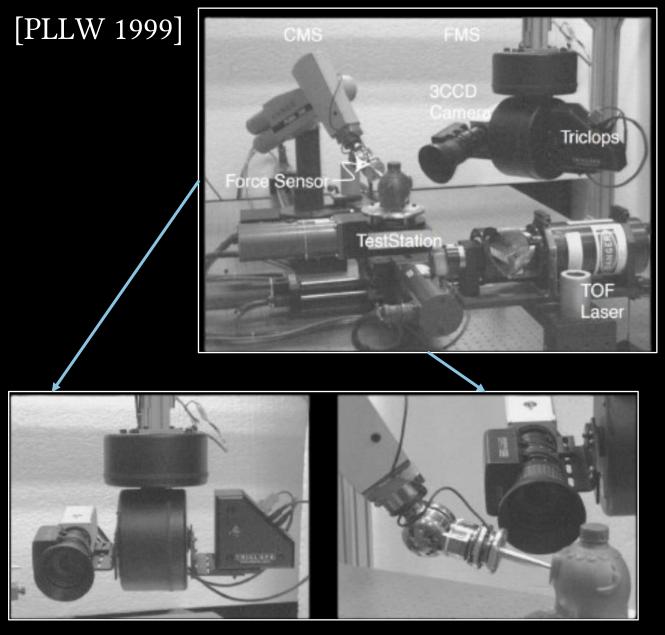


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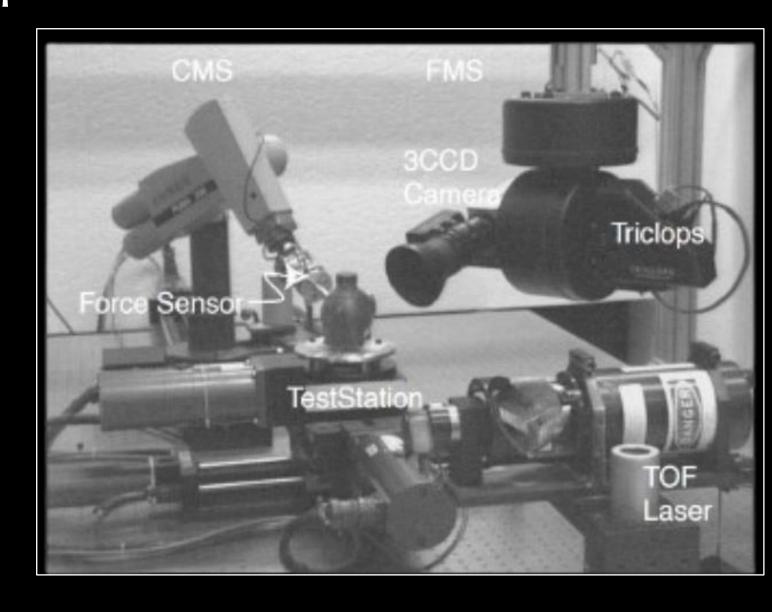


what to measure and how to measure?

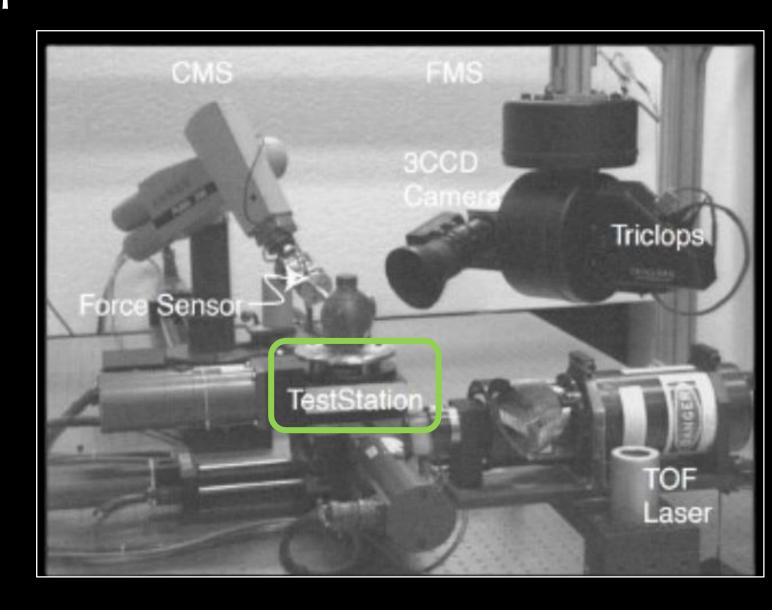


field measurement system

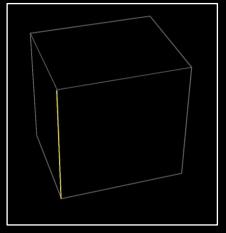
force/position measurement system

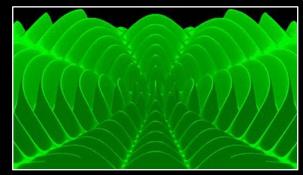


3 DOF placement



field measurement system (stereo vision + rgb camera + mic) on a 5 DOF positioning robot

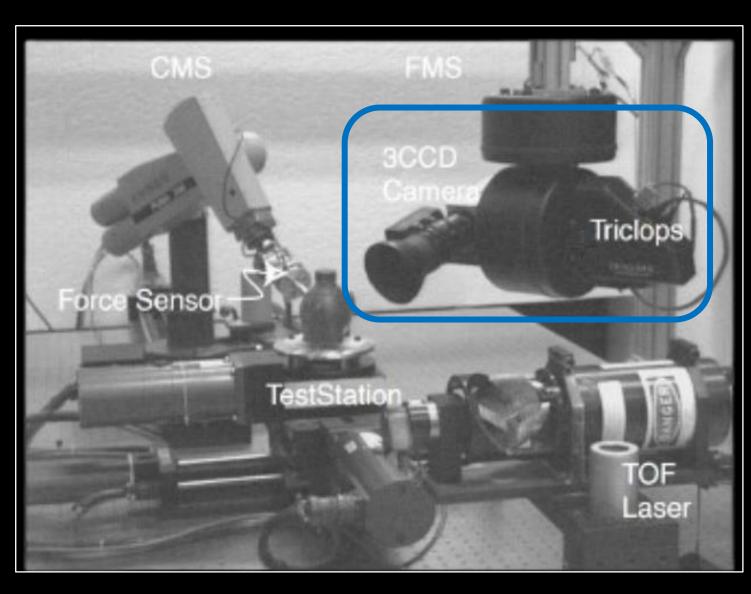




light field

sound field





[MID 2002]



stereo range data is highly noisy we need some kind of filtering to decide what stereo range data we need

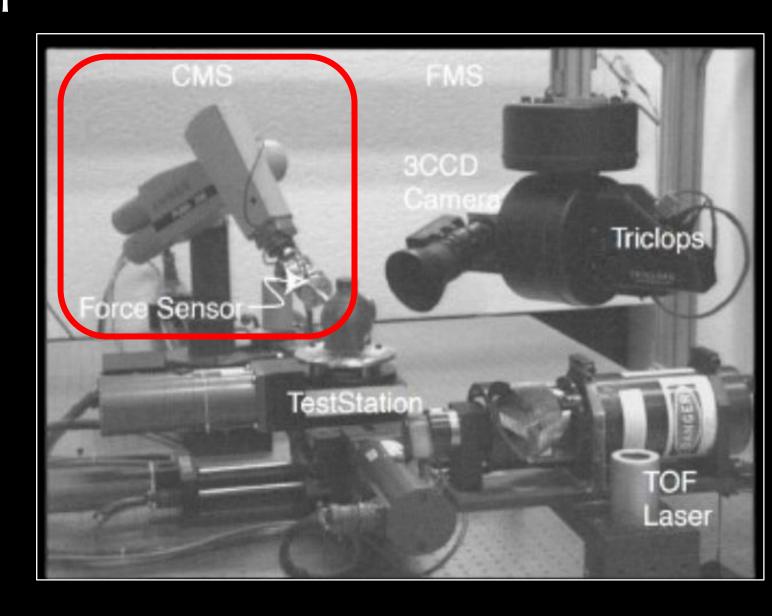
[MID 2002]

some classical techniques:

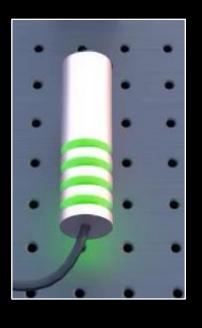
- variable mask size voting
- estimate (local) surface normal
- decide some handcrafted ways of choosing what to keep

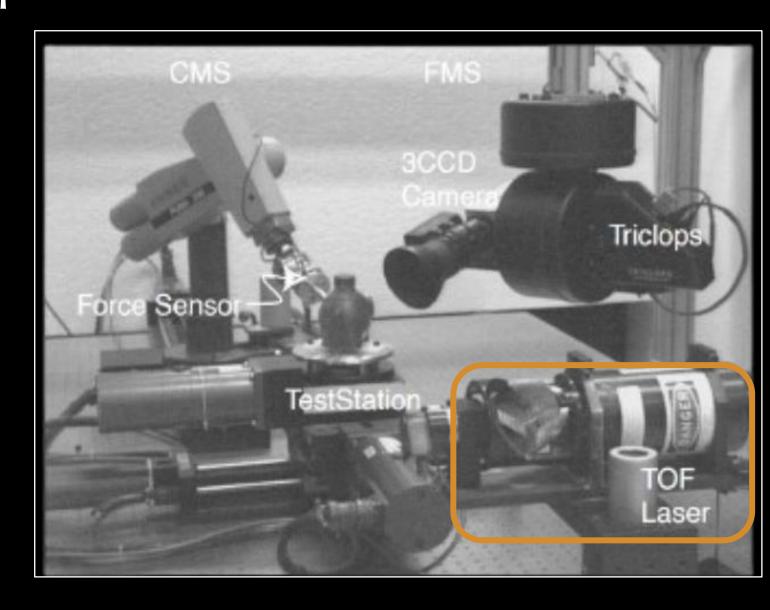
force/position measurement system (force/torque sensor) on a linear stage





time-of-flight laser range finder



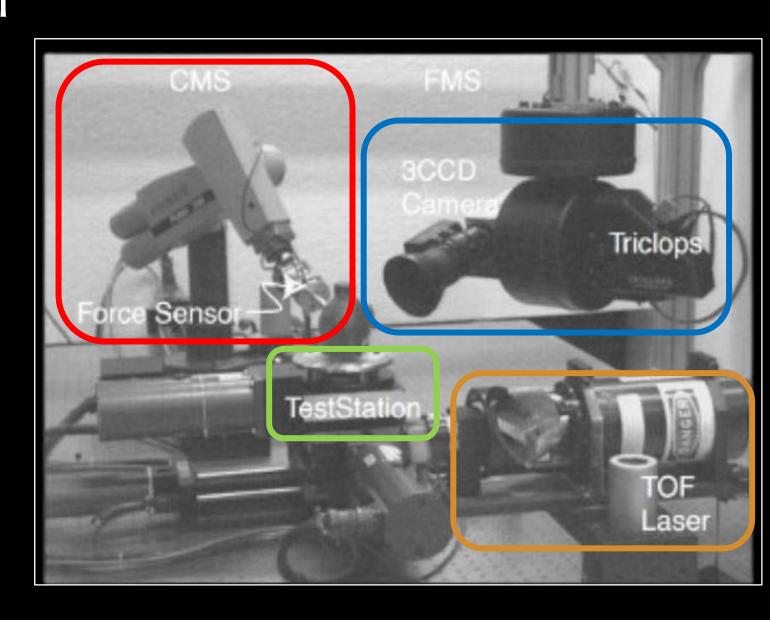


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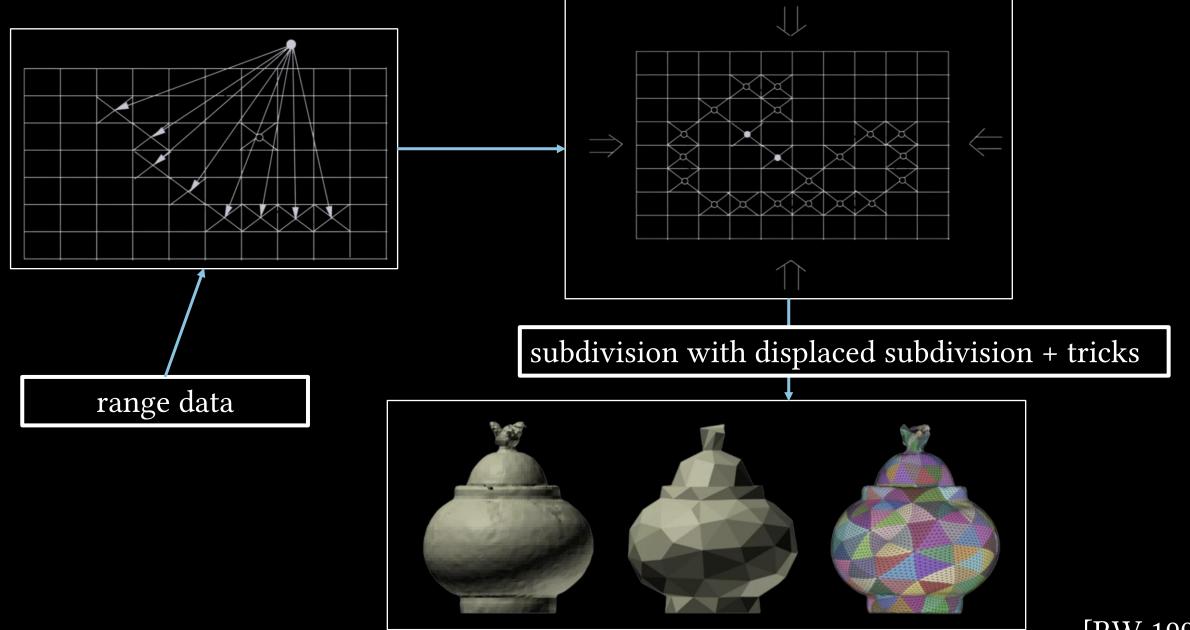
force/position measurement system (force/torque sensor) on a linear stage

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mesh reconstruction

multiresolution mesh



multiresolution mesh subdivision with displaced subdivision + tricks [RW 1997]

multiresolution textured mesh

multiview color images

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let us focus on this now



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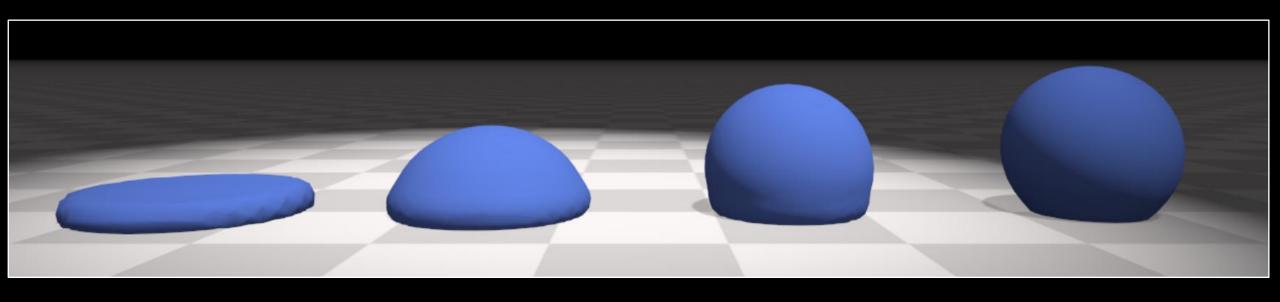


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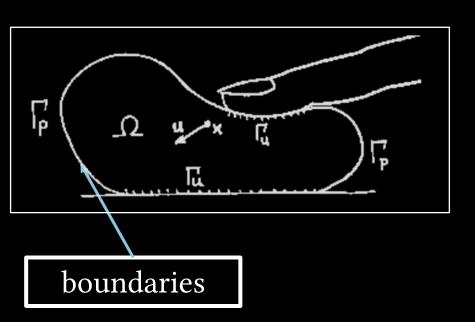
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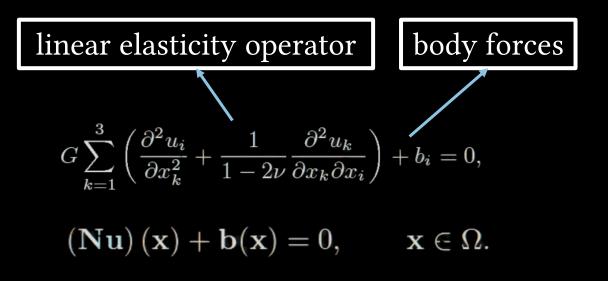
Figure 1: Examples of behavior models scanned by our system



deformation

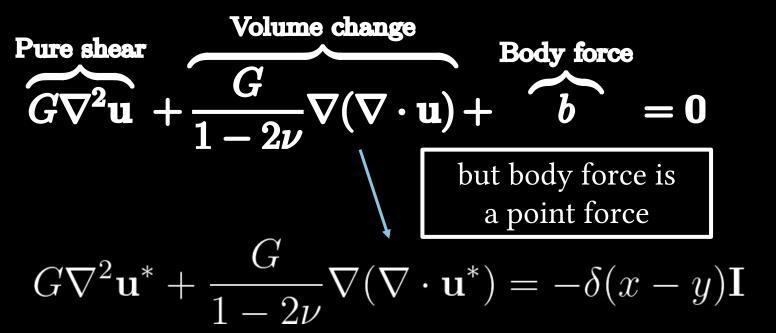
what model do we use?





Pure shear
$$G = \frac{G}{1 - 2\nu} \nabla (\nabla \cdot \mathbf{u}) + \frac{G}{b} = 0$$

$$\mathbf{u} = \bar{\mathbf{u}} \quad \text{on} \quad \Gamma_u$$
 $\mathbf{p} = \bar{\mathbf{p}} \quad \text{on} \quad \Gamma_p$

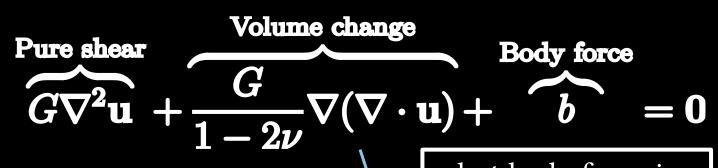




$$G\nabla^2 \mathbf{u}^* + \frac{G}{1 - 2\nu} \nabla(\nabla \cdot \mathbf{u}^*) = -\delta(x - y) \mathbf{I} \cdot \mathbf{u}^*$$

exploit linearity

$$G\nabla^{2}u_{ij}^{*} + \frac{G}{1 - 2\nu} \frac{\partial}{\partial x_{i}} \left(\sum_{k=1}^{3} \frac{\partial u_{kj}^{*}}{\partial x_{k}} \right) = - \underbrace{\delta(x - y)\delta_{ij}}^{\text{point force in direction j}}$$



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fourier transform

$$G(-|\xi|^2)\hat{u}_{ij}^* + \frac{G}{1-2\nu}(-\xi_i\xi_j\hat{u}_{ij}^*) = -e^{-i\xi\cdot y}\delta_{ij}$$

 $G(-|\xi|^2)\hat{u}_{ij}^* + \frac{G}{1-2\nu}(-\xi_i\xi_j\hat{u}_{ij}^*) = -e^{-i\xi\cdot y}\delta_{ij}$ aside: make greens functions

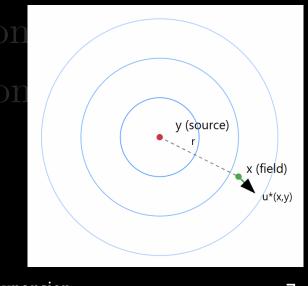
$$G(-|\xi|^2)\hat{u}_{ij}^* + \frac{G}{1-2\nu}(-\xi_i\xi_j\hat{u}_{ij}^*) = -e^{-i\xi\cdot y}\delta_{ij}$$

solve this in fourier space

risotropic expansion

$$u_{ij}^*(x,y) = \frac{1}{16\pi G(1-\nu)} \begin{bmatrix} \overbrace{(3-4\nu)\delta_{ij}} \\ r \end{bmatrix} + \underbrace{\frac{r_i r_j}{r^3}}_{\text{directional deformation}}$$

Pure shear
$$G \nabla^2 \mathbf{u} + \frac{G}{1 - 2\nu} \nabla (\nabla \cdot \mathbf{u}) + \frac{Body \text{ force}}{b} = \mathbf{0}$$



Elastic operator

$$\sqrt[4]{\mathbf{N}\mathbf{u}^*(x,y)} + \underbrace{\delta(x-y)\mathbf{I}}_{\text{Point force}} = \mathbf{0} \qquad u_{ij}^*(x,y) = \frac{1}{16\pi G(1-\nu)} \begin{bmatrix} \frac{1}{(3-4\nu)\delta_{ij}} \\ \frac{1}{r} \end{bmatrix} + \underbrace{\frac{r_i r_j}{r^3}}_{\text{Directional deformation}}$$

green function

$$p_{ij}^*(x,y) = -\frac{1}{8\pi(1-\nu)r^2} \left[\underbrace{\frac{\partial r}{\partial n}((1-2\nu)\delta_{ij} + 3\frac{r_i r_j}{r^2})}_{\text{Normal traction}} + \underbrace{(1-2\nu)(n_i r_j - n_j r_i)}_{\text{Shear traction}} \right]$$

weighted residual

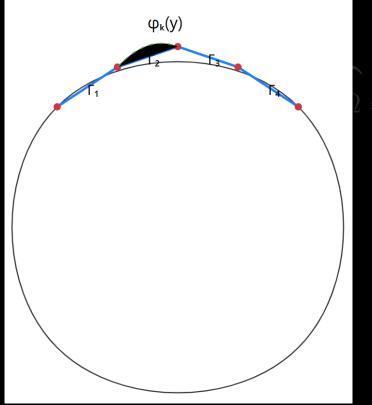
Volume work
$$\int_{\Omega} \mathbf{u}^* \cdot \mathcal{N} \mathbf{u} d\Omega = \oint_{\Gamma} \mathbf{u}^* \cdot \mathbf{p} d\Gamma - \int_{\Omega} \nabla \mathbf{u}^* : \boldsymbol{\sigma}(\mathbf{u}) d\Omega$$
Boundary work

reciprocal theorem and by parts

Difference of virtual works in volume

$$\int_{\Omega} (\mathbf{u}^* \cdot \mathcal{N} \mathbf{u} - \mathbf{u} \cdot \mathcal{N} \mathbf{u}^*) d\Omega = \oint_{\Gamma} (\mathbf{u}^* \cdot \mathbf{p} - \mathbf{u} \cdot \mathbf{p}^*) d\Gamma$$

Difference of virtual works on boundary



$$= \underbrace{\int_{\Gamma} \mathbf{u}^* \cdot \mathbf{p} d\Gamma}_{\text{Boundary, work}} - \underbrace{\int_{\Omega} \nabla \mathbf{u}^* : \boldsymbol{\sigma}(\mathbf{u}) d\Omega}_{\text{Boundary, work}}$$

reciprocal theorem and by parts

Difference of virtual works in volume

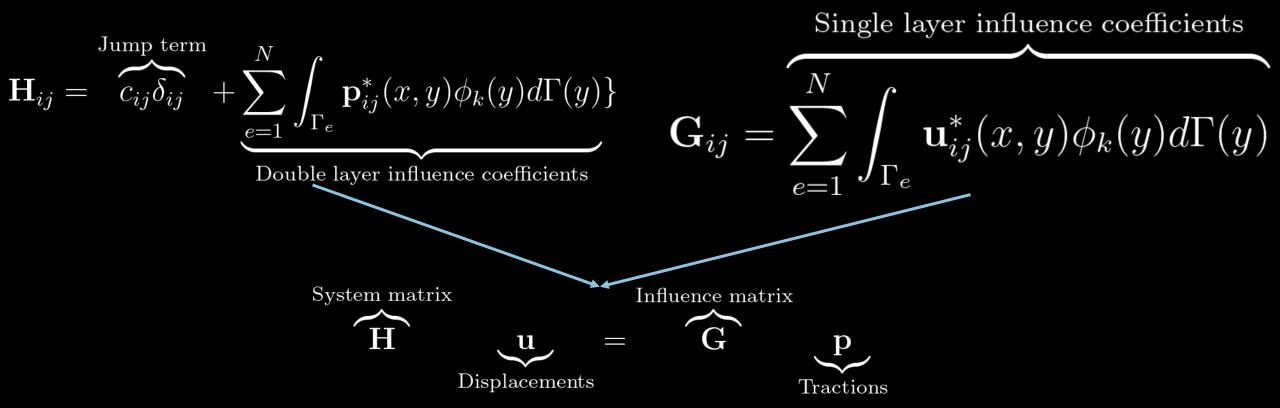
$$\int_{\Omega} (\mathbf{u}^* \cdot \mathcal{N}\mathbf{u} - \mathbf{u} \cdot \mathcal{N}\mathbf{u}^*) d\Omega = \underbrace{\int_{\Gamma} (\mathbf{u}^* \cdot \mathbf{p} - \mathbf{u} \cdot \mathbf{p}^*)}_{\text{Difference of virtual works on boundary}} d\Gamma$$

discretize the boundary into non-overlapping pieces do field approximations for u and p

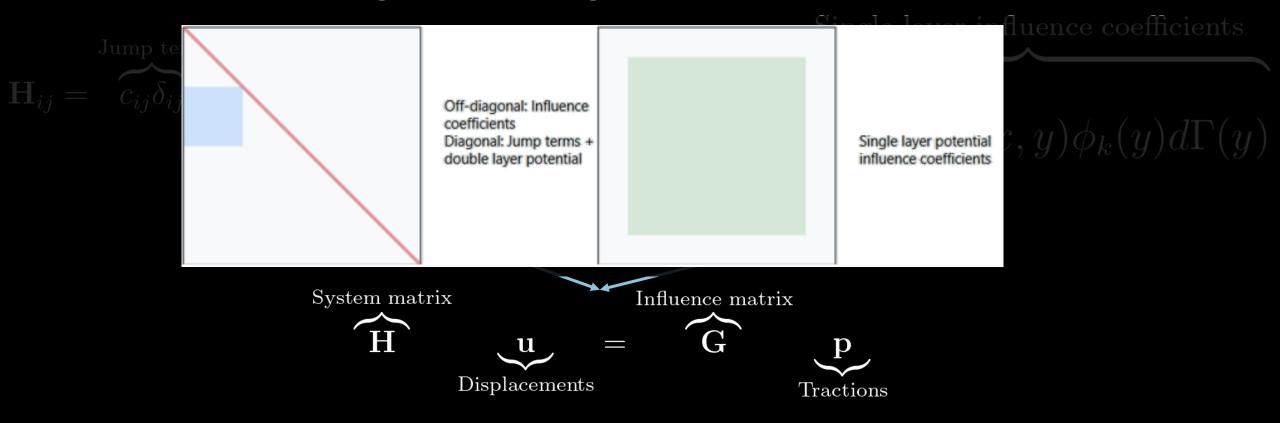
Point displacement $\underbrace{c_{ij}(x^m)\mathbf{u}_j(x^m)}^{\text{Point displacement}} + \underbrace{\sum_{e=1}^{N} \int_{\Gamma_e} \mathbf{p}_{ij}^*(x^m, y) \phi_k(y) d\Gamma(y) \mathbf{u}_j^k}_{\text{Influence of all displacements}} = \underbrace{\sum_{e=1}^{N} \int_{\Gamma_e} \mathbf{u}_{ij}^*(x^m, y) \phi_k(y) d\Gamma(y) \mathbf{p}_j^k}_{\text{Influence of all displacements}}$

[JP 1999]

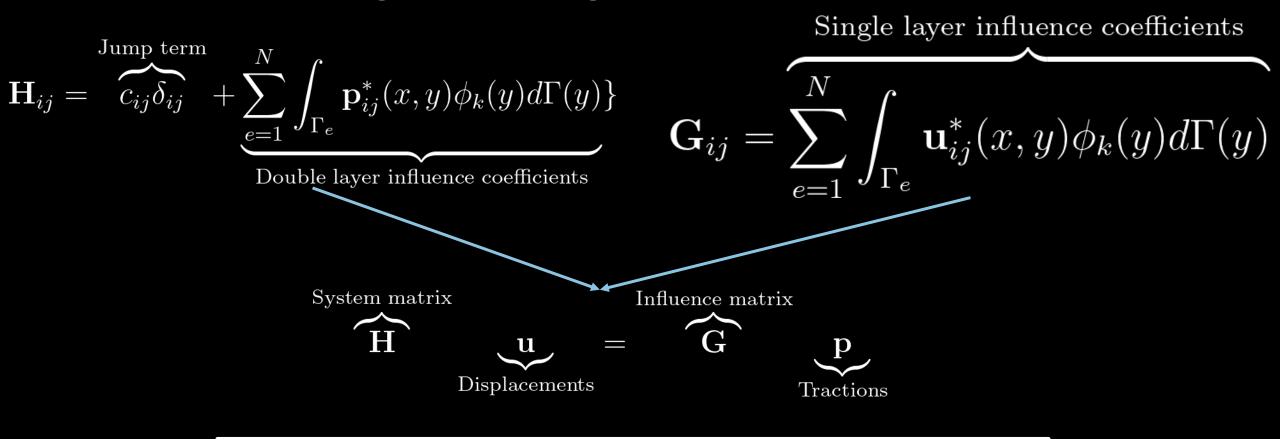
now let us bring it all together



now let us bring it all together

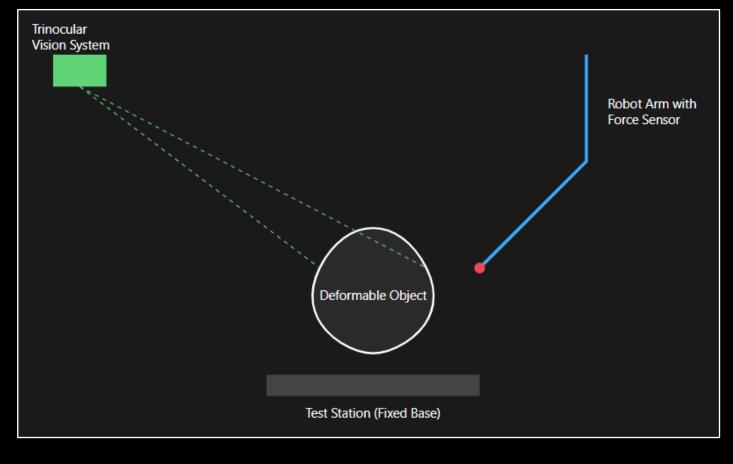


now let us bring it all together



does this look familiar?

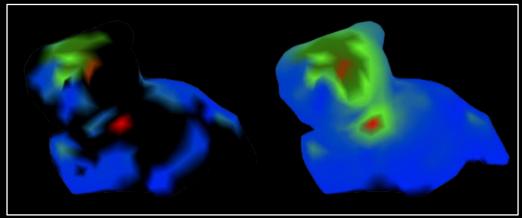
getting back to capturing



- apply a controlled force
- records 6D force/torque data at 1000Hz
- trinocular vision system captures the surface deformation at 30Hz
- repeat

use vision system:

- track visual features from optical flow
- reconstructing 3D motion field
- map the deformation onto the mesh vertices



get model parameters

we already have displacement field and force for vertices of mesh

$$[\mathbf{p}_j^1 \mathbf{p}_j^2 \cdots \mathbf{p}_j^M]^T \mathbf{U}_{ij}^T = [\mathbf{u}_i^1 \mathbf{u}_i^2 \cdots \mathbf{u}_i^M]^T$$

does this look familiar? tsvd + least trimmed squares

get model parameters

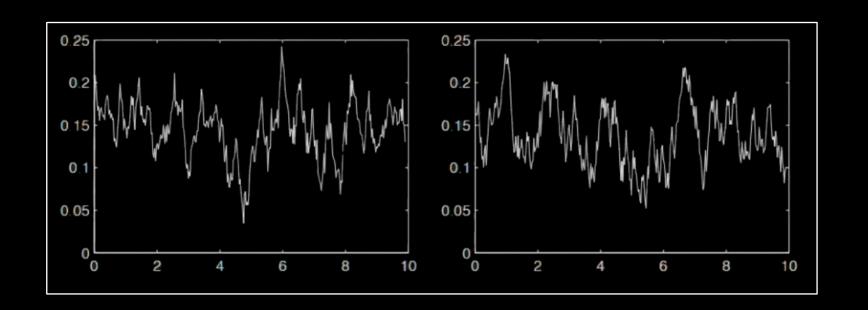
make this system

we already have displacement field and force for vertices of mesh

$$[\mathbf{p}_j^1 \mathbf{p}_j^2 \cdots \mathbf{p}_j^M]^T \mathbf{U}_{ij}^T = [\mathbf{u}_i^1 \mathbf{u}_i^2 \cdots \mathbf{u}_i^M]^T$$

does this look familiar?

tsvd + least trimmed squares also interpolate missing values also interpolate across resolutions



contact texture

in general: model, measurement, rendering

model friction
surface roughness

$$\mathbf{f}_f = -\mu \|\mathbf{f}_n\|\mathbf{u}_m$$
 $\mu_e(x) = \mu + \tilde{\mu}(x)$ non-typical

$$\mathbf{f}_f = -\mu \|\mathbf{f}_n\|\mathbf{u}_m$$

$$\mu_e(x) = \mu + \tilde{\mu}(x) \quad \text{non-typical}$$

model all these variations as an auto-regressive process

$$\tilde{\mu}(x) = \tilde{\mu}(\underline{k}\Delta) \equiv \tilde{\mu}(k) = \sum_{i=1}^{r} a_i \tilde{\mu}(k-i) + \sigma \epsilon(k)$$

index

how many times do you do this

ar coefficients

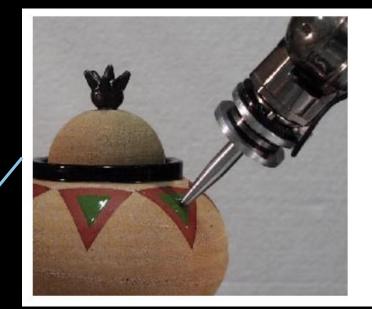
std dev of noise

zero mean and std. dev 1 noise

$$\mathbf{f}_f = -\mu \|\mathbf{f}_n\|\mathbf{u}_m$$
 $\mu_e(x) = \mu + \tilde{\mu}(x)$ non-typical

model all these variations as an auto-regressive process

$$\begin{bmatrix} \mu(x) = \tilde{\mu}(k\Delta) \\ \mu(x) \end{bmatrix} = \begin{bmatrix} \tilde{\mu}(k) = \lambda & \tilde{\mu}(k) \\ a_1 & a_2 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \mu(x-\Delta) \\ \mu(x-2\Delta) \end{bmatrix} + \begin{bmatrix} \sigma \\ 0 \end{bmatrix} \epsilon(x)$$
do you do this



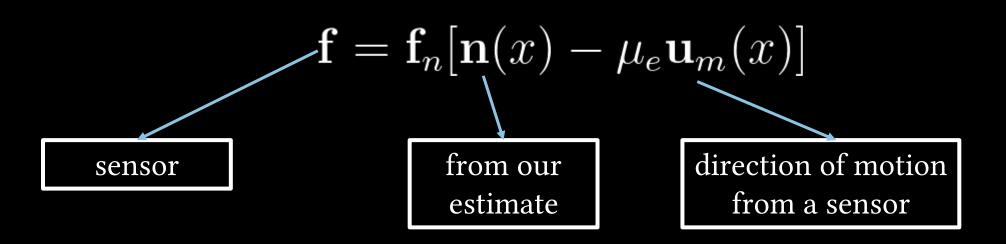


use multi resolution mesh

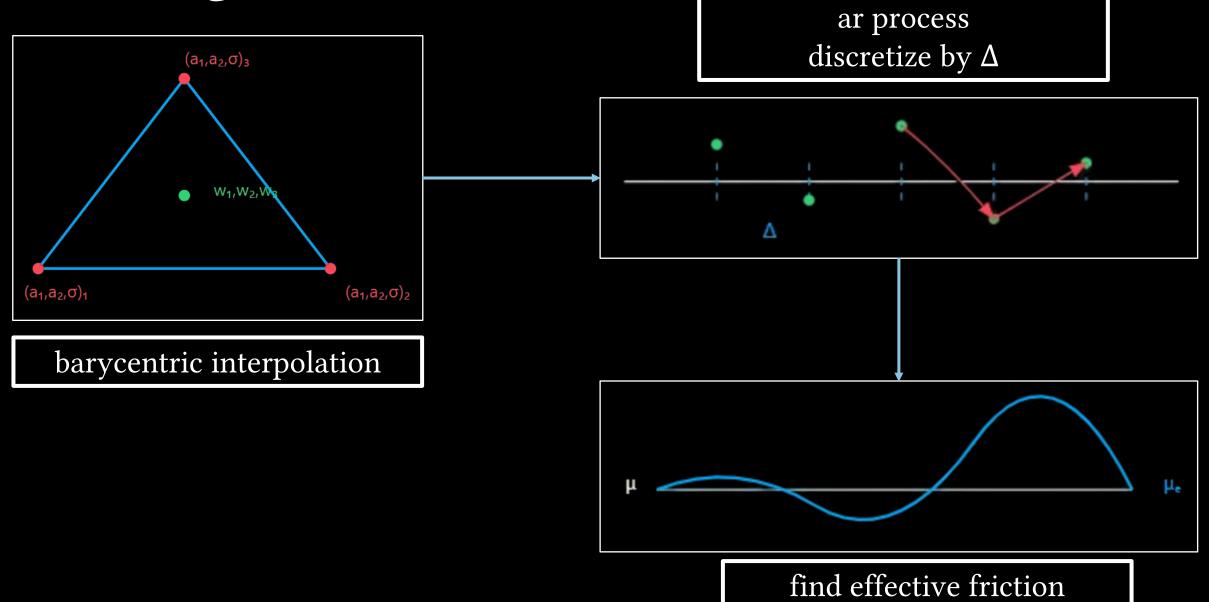
$$\mu = \tan(\theta/2)$$

$$\mathbf{n}(x) = \frac{\mathbf{f}_f^+ + \mathbf{f}_f^-}{\|\mathbf{f}_f^+ + \mathbf{f}_f^-\|}$$

$$\mathbf{n}(x) = \frac{\mathbf{f}_f^+ + \mathbf{f}_f^-}{\|\mathbf{f}_f^+ + \mathbf{f}_f^-\|}$$



rendering





sound

model

frequencies decay rates

$$M = \{ \widehat{\mathbf{f}} , \widehat{\mathbf{d}} , \underbrace{\mathbf{A}}_{\text{mode gains}} \}$$

$$y_k(t) = \sum_{n=1}^{N \text{ mode amplitude}} \underbrace{a_{nk}}^{\text{oscillation}} \underbrace{e^{-d_n t}}^{\text{oscillation}} \underbrace{\sin(2\pi f_n t)}^{\text{oscillation}}$$

model

$$M = \{ \begin{array}{c} \mathbf{f} \end{array}, \begin{array}{c} \mathbf{d} \end{array}, \underbrace{\mathbf{A}}_{\mathrm{mode\ gains}} \}$$

$$y_k(t) = \sum_{n=1}^{N \text{ mode amplitude}} \underbrace{a_{nk}}^{\text{oscillation}} \underbrace{e^{-d_n t}}^{\text{oscillation}} \underbrace{\sin(2\pi f_n t)}^{\text{oscillation}}$$

$$F_{audio}(t) = \overbrace{F_N}^{\text{normal force}} \cdot \underbrace{\mu_e(v \cdot t)}_{\text{friction variation}} \cdot \underbrace{v(t)}_{\text{sliding velocity}}$$

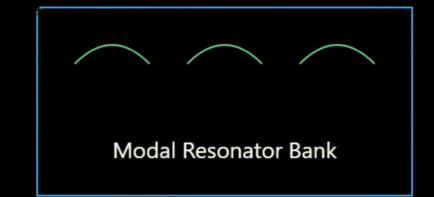
measure impulse repsonse

$$h(t) = \sum_{n=1}^{N} \underbrace{A_n e^{-d_n t}}_{\text{oscillation}} \cdot \underbrace{\cos(2\pi f_n t + \phi_n)}_{\text{oscillation}}$$



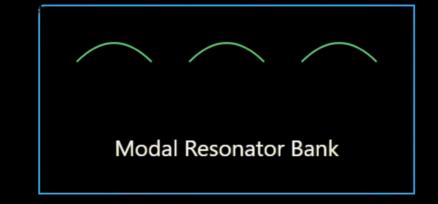
rendering

resonator dynamics
$$\overline{\ddot{x}_n + 2d_n\dot{x}_n + \omega_n^2 x_n} = F_{audio}(t)$$
input force



rendering

resonator dynamics
$$\widetilde{\ddot{x}_n + 2d_n\dot{x}_n + \omega_n^2 x_n} = F_{audio}(t)$$
input force



$$\begin{bmatrix} x_n(t + \Delta t) \\ \dot{x}_n(t + \Delta t) \end{bmatrix} = \underbrace{e^{A\Delta t}}_{t} \begin{bmatrix} x_n(t) \\ \dot{x}_n(t) \end{bmatrix} + \underbrace{\int_{t}^{t + \Delta t} e^{A(t + \Delta t - \tau)} bF_{audio}(\tau) d\tau}_{t}$$

$$A = \begin{bmatrix} 0 & 1 \\ -\omega_n^2 & -2d_n \end{bmatrix}, \quad b = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

summary





Synthesized or Real?

2

references

[PDJLLRY 2001] D. K. Pai, K. van den Doel, D. L. James, J. Lang, J. E. Lloyd, J. L. Richmond, S. H. Yau, "Scanning Physical Interaction Behavior of 3D Objects," in Computer Graphics (ACM SIGGRAPH 2001 Conference Proceedings), August

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