

Глубокое обучение и вообще

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1 февраля 2023 г.

Графовые нейронные сети

Графы

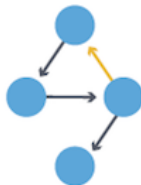
Undirected



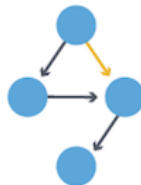
Directed



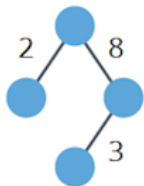
Cyclic



Acyclic



Weighted



Unweighted



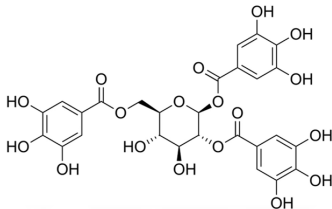
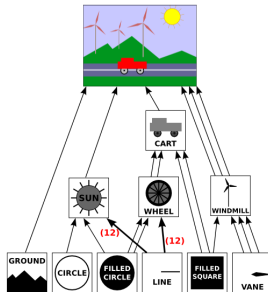
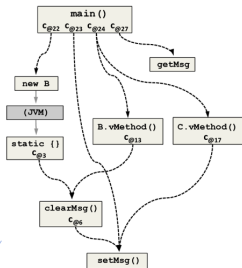
Sparse



Dense



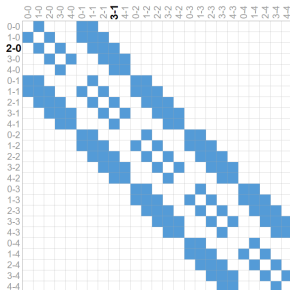
Графы в жизни



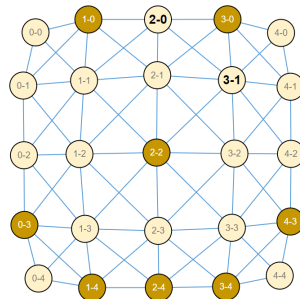
Картинки как графы

0-0	1-0	2-0	3-0	4-0
0-1	1-1	2-1	3-1	4-1
0-2	1-2	2-2	3-2	4-2
0-3	1-3	2-3	3-3	4-3
0-4	1-4	2-4	3-4	4-4

Image Pixels

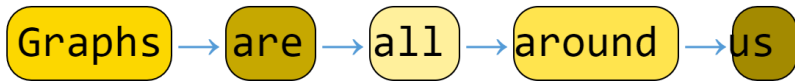


Adjacency Matrix



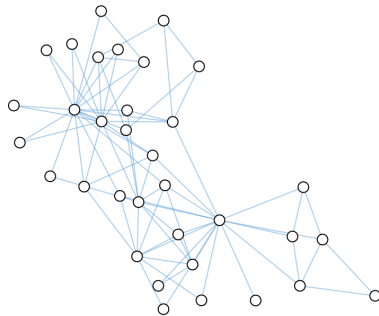
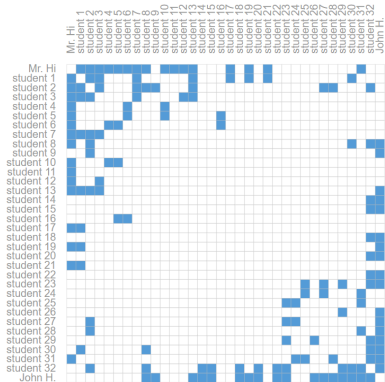
Graph

Текст как графы

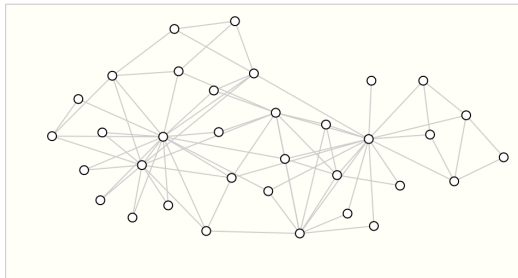


	Graphs	are	all	around	us
Graphs		■			
are			■		
all				■	
around					■
us					

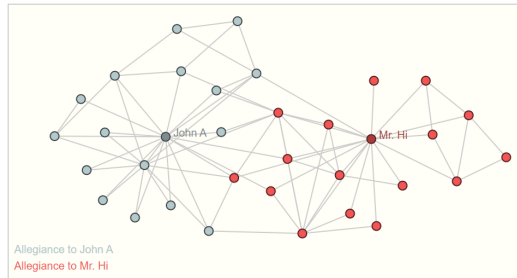
Пример графа



Задачи на графах: вершины

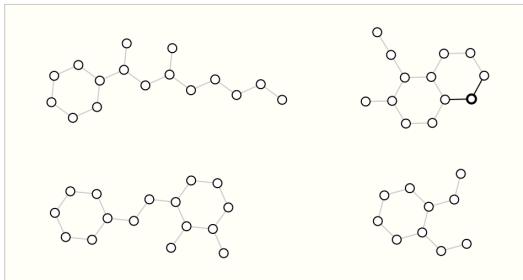


Input: graph with unlabeled nodes

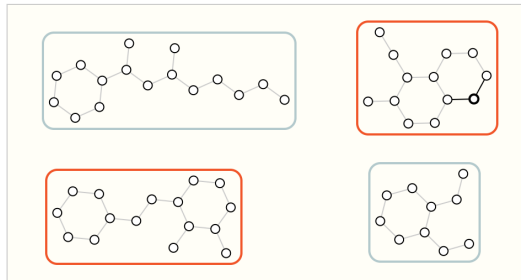


Output: graph node labels

Задачи на графах: целый граф

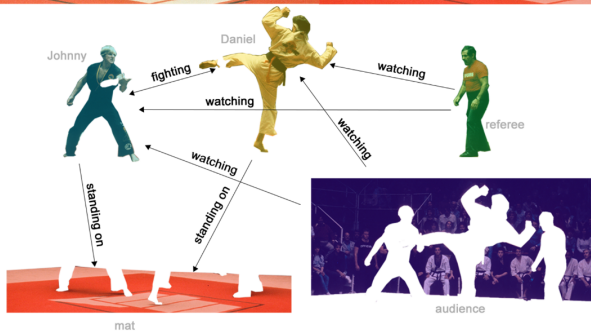


Input: graphs

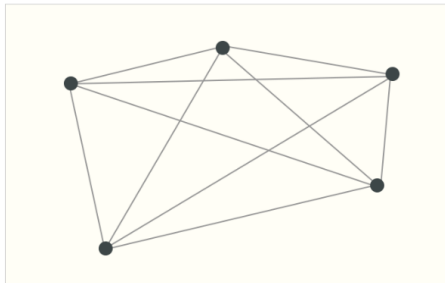


Output: labels for each graph, (e.g., "does the graph contain two rings?")

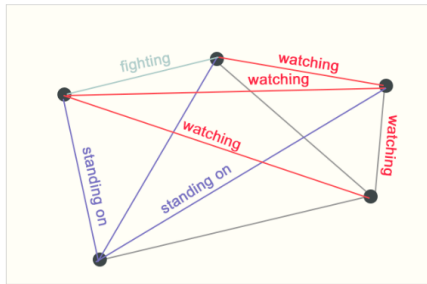
Задачи на графах: ребра



Задачи на графах: ребра



Input: fully connected graph, unlabeled edges

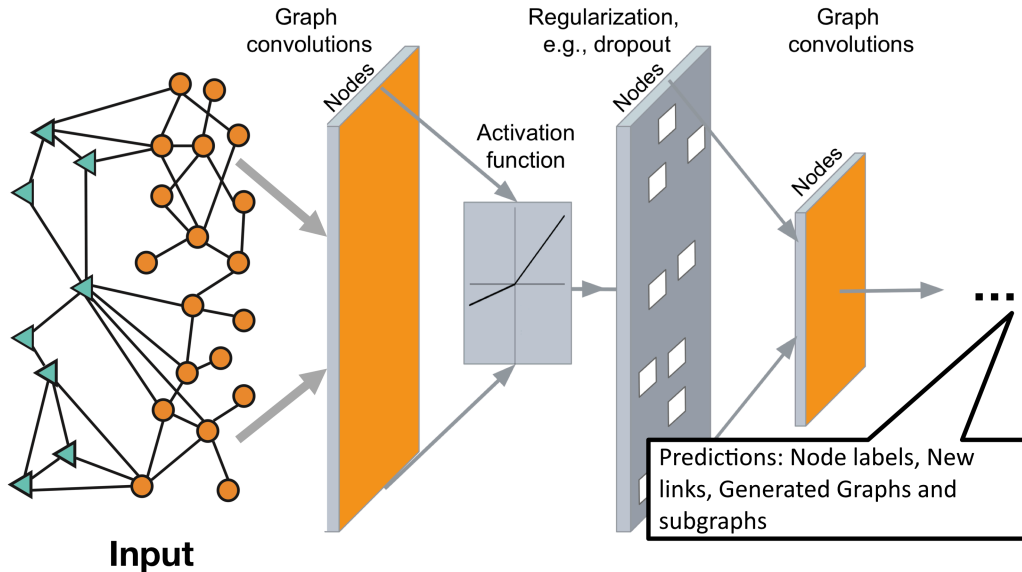


Output: labels for edges

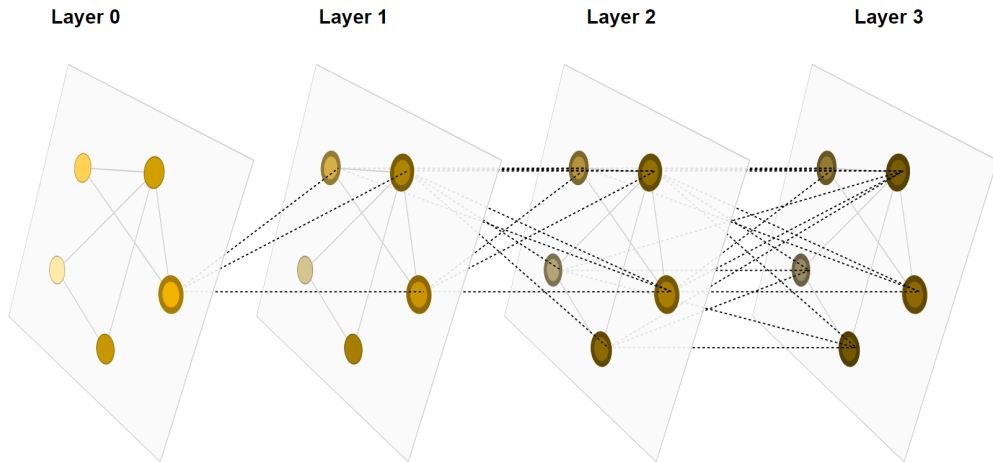
Проблемы при работе с графами

- Размеры
- Часто имеют динамическую структуру
- Нет порядка вершин

Графы



Message Passing



GraphSAGE

Algorithm 1: GraphSAGE embedding generation (i.e., forward propagation) algorithm

Input : Graph $\mathcal{G}(\mathcal{V}, \mathcal{E})$; input features $\{\mathbf{x}_v, \forall v \in \mathcal{V}\}$; depth K ; weight matrices $\mathbf{W}^k, \forall k \in \{1, \dots, K\}$; non-linearity σ ; differentiable aggregator functions $\text{AGGREGATE}_k, \forall k \in \{1, \dots, K\}$; neighborhood function $\mathcal{N} : v \rightarrow 2^{\mathcal{V}}$

Output : Vector representations \mathbf{z}_v for all $v \in \mathcal{V}$

```
1  $\mathbf{h}_v^0 \leftarrow \mathbf{x}_v, \forall v \in \mathcal{V};$ 
2 for  $k = 1 \dots K$  do
3   for  $v \in \mathcal{V}$  do
4      $\mathbf{h}_{\mathcal{N}(v)}^k \leftarrow \text{AGGREGATE}_k(\{\mathbf{h}_u^{k-1}, \forall u \in \mathcal{N}(v)\});$ 
5      $\mathbf{h}_v^k \leftarrow \sigma \left( \mathbf{W}^k \cdot \text{CONCAT}(\mathbf{h}_v^{k-1}, \mathbf{h}_{\mathcal{N}(v)}^k) \right)$ 
6   end
7    $\mathbf{h}_v^k \leftarrow \mathbf{h}_v^k / \|\mathbf{h}_v^k\|_2, \forall v \in \mathcal{V}$ 
8 end
9  $\mathbf{z}_v \leftarrow \mathbf{h}_v^K, \forall v \in \mathcal{V}$ 
```

Почитать

- Graph Convolution Network: <https://arxiv.org/pdf/1609.02907.pdf>
- GraphSAGE: <https://arxiv.org/pdf/1706.02216.pdf>
- Graph Attention Network: <https://arxiv.org/pdf/1710.10903.pdf>
- Overview: <https://arxiv.org/pdf/1810.00826.pdf>