

# **CSE/ECE 848 Introduction to Evolutionary Computation**

**Module 4 - Lecture 20 - Part 4**

## **Dynamic Problems in EC: Performance Measures and Benchmark Problems**

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# Performance Measures for DO

- Performance measures for stationary problems
  - Best so far
  - Average best so far (offline)
  - Average of all evaluations (online)
- Performance measures for dynamic problems

- Adaptation performance I
- Average distance to the optimum
- Best of generation average
- Accuracy Acc

$$I = 1/T \sum f_{\text{best}}(t)/f_{\text{opt}}(t)$$

$T$ : number of generation  
 $f_{\text{best}}(t)$ : best fitness in the population at time  $t$   
 $f_{\text{opt}}(t)$ : global optimum at time  $t$

$$\text{Acc} = 1/K \sum \text{err}_i$$

$\text{err}_i$ :

difference between the current best in the population just before change and the optimum value averaged over the entire run

$K$ :

Number of changes of the fitness landscape

# Knowledge for Performance Measures

- Knowledge on the position of the optimum is available
  - Distance to optimum can be calculated
- Knowledge on the best fitness value is available
  - Accuracy can be calculated
- No global knowledge is available
  - Only the current best can be known

# Benchmark Problems

- Change a constant problem into a time-dependent problem
- Real space
  - Switch between different functions
  - Move/reshape peaks in fitness landscape
- Binary space
  - Switch between states of a problem (eg knapsack)
  - Use binary masks (eg XOR DOP generator)
- Permutation space
  - Change decision variables (eg item weights/profits in knapsack)
  - Add/delete decision variables (new jobs/nodes etc)

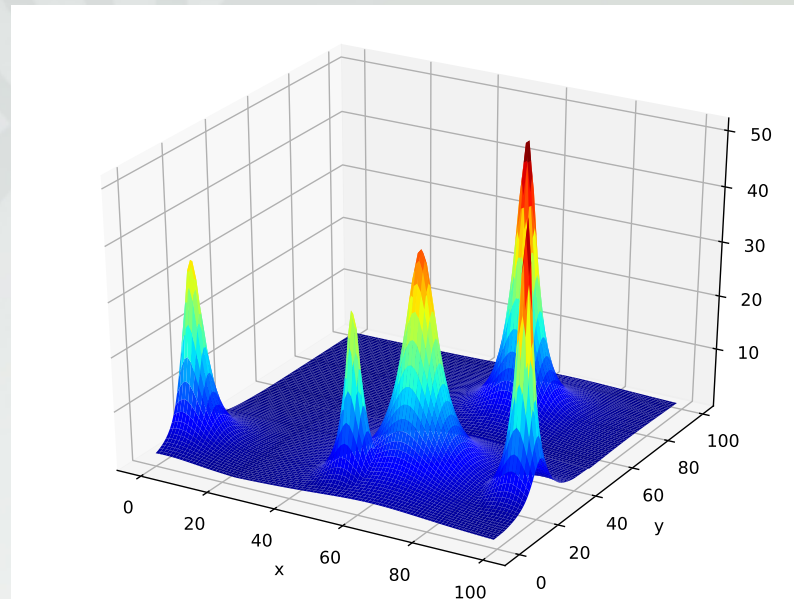
# Benchmark Problems - Real Space

- Moving Peaks Benchmark (MBP) (Branke 1999)

$$f(\mathbf{x}) = \frac{h}{1+w\sqrt{\sum_{i=1}^N (x_i - p_i)^2}}$$

$h(t)$ : Height;  $w(t)$  width;  
 $p_i(t)$  location of peak

with appropriate dynamics



DEAP Benchmarks

# Benchmark Problems - Binary Space

- XOR DOP generator (Yang 2003)
- Can create DOPs from any binary fitness function  $f(x)$
- Create a mask  $M(k)$  where  $k$  is the period  $k=t/\tau$  with  $\tau$  being the number of generations things are constant

$$\vec{M}(0) = \vec{0} \text{ (the initial state)}$$

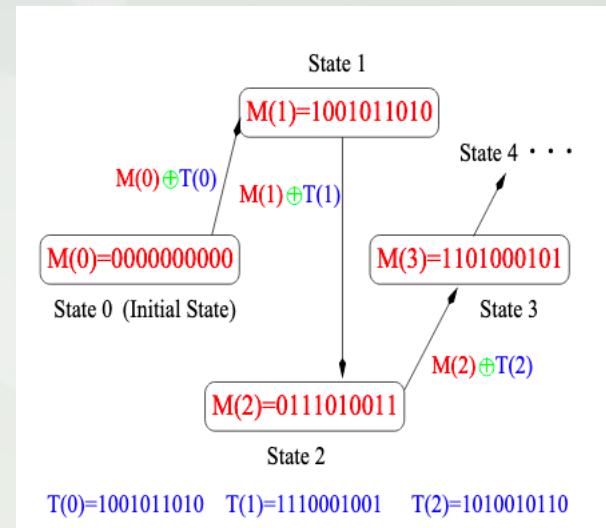
$$\vec{M}(k+1) = \vec{M}(k) \oplus \vec{T}(k)$$

- with  $T(k)$  a template with  $p$  randomly distributed ones

- Then

$$f(\vec{x}, t) = f(\vec{x} \oplus \vec{M}(k))$$

- $\tau, p$  control the speed/severity of change



# Benchmark Problems - Combinatorial Space

- Dynamic Traveling Salesperson (DTSP)
- Minimize tour length or cost  $D(t)$
- Given a set of cities  $i$ , visit each city once and return to your starting place
- Distance/cost between cities  $d_{ij}(t)$  is time dependent

$$f(x, t) = \text{Min}(\sum_{i=1}^n d_{x_i, x_{i+1}}(t))$$

where  $i = \{1, \dots, n\}$ ;  $x_{n+1} = x_1$