

IF a sum of money becomes N_1 Times in T_1 yrs and N_2 times in T_2 years then

$$(N_1)^{T_2} = (N_2)^{T_1} \text{ OR } N_2 = (N_1)^{T_2/T_1}$$

A sum of money get doubled in 4 years. IN how much time it will become 8 times?

Solution:- I (FORMULA)

$$N_1 = 2, T_1 \rightarrow 4$$

$$N_2 \rightarrow 8, T_2 = ?$$

$$N_2 = (N_1)^{T_2/T_1} \Rightarrow 8 = (2)^{T_2/4}$$

$$\text{OR } 2^3 = (2)^{T_2/4} \Rightarrow T_2/4 = 3$$

$$\Rightarrow T_2 = 12 \text{ yrs.}$$

II (TRICKY)

$$2^1 \text{ गुणा} \rightarrow 4 \text{]} +4$$

$$2^2 \text{ times} \rightarrow 8 \text{]} +4$$

$$2^3 \text{ times} \rightarrow 12 \text{]} +4$$

$$\hookrightarrow 8 \text{ times} \rightarrow 12 \text{ yrs}$$

कोई राशि चक्रवृद्धि व्याज की दर से 3 साल में 3 गुणा हो जाती है। कितने समय में यह राशि 81 गुणा हो जाएगी?

Solution:- I (FORMULA)

$$N_1 \rightarrow 3, T_1 \rightarrow 3$$

$$N_2 \rightarrow 81, T_2 \rightarrow ?$$

$$N_2 = (N_1)^{T_2/T_1}$$

$$\Rightarrow 81 = (3)^{T_2/3} \Rightarrow 3^4 = 3^{T_2/3}$$

$$\Rightarrow T_2/3 = 4 \Rightarrow 12 \text{ yrs}$$

II (TRICKY)

$$3^1 \text{ times} \rightarrow 3 \text{]} +3$$

$$3^2 \text{ times} \rightarrow 6 \text{]} +3$$

$$3^3 \text{ times} \rightarrow 9 \text{]} +3$$

$$3^4 = 81 \text{ times} \rightarrow 12 \text{]} +3$$

$$12 \text{ years Ans.}$$

A sum of money becomes 81 times in 4 years. in how much time it will become 27 times?

Solution:- I (FORMULA)

$$N_1 \rightarrow 81, T_1 \rightarrow 4$$

$$N_2 \rightarrow 27, T_2 \rightarrow ?$$

$$27 = (81)^{T_2/4}$$

$$\text{OR } \Rightarrow 27 = (3^4)^{T_2/4}$$

$$3^3 = 3^{T_2} \Rightarrow T_2 = 3 \text{ yrs.}$$

II (TRICKY)

$$A : P$$

$$T=4 \rightarrow 81 : 1$$

$$T=1 \rightarrow \sqrt[4]{81} : \sqrt[4]{1}$$

$$3 : 1$$

$$\therefore 3^1 \text{ --- } 1 \text{ साल}$$

$$3^2 \text{ --- } 2 \text{ साल}$$

$$27 = 3^3 \text{ --- } 3 \text{ साल}$$

ANS 3

$P = 625 \text{ ₹}$ $R = 4\%$ $T = 2 \text{ yrs}$, $CI = ?$

$4\% = \frac{1 - I}{25 - P} \Rightarrow A = 26$

$\downarrow 25 : 26 : 26 \downarrow$
 $\downarrow 25 : 25 : 26 \downarrow$

$625 : 650 : 676$
 मूलधन \leftarrow \downarrow \rightarrow 2 साल के बाद मिश्रधन
 1 साल के बाद मिश्रधन

$I = A - P$

$= 676 - 625 = 51$

$\downarrow 25 \text{ ₹} \quad \downarrow 26 \text{ ₹}$
 पहले साल का व्याज \downarrow दूसरे साल का व्याज
 $\downarrow 1 \text{ ₹}$
 दो साल के व्याज का अंतर

$1000 = P$, $R = 10\%$, $T = 3 \text{ yrs}$
 CI

$10\% = \frac{1}{10}$

$\downarrow 10 : 11 : 11 : 11 \downarrow$
 $\downarrow 10 : 10 : 11 : 11 \downarrow$
 $\downarrow 10 \quad 10 : 10 : 11$

$\overline{1000 \quad 1331}$
 $\swarrow \quad \searrow$
 331
 \downarrow ANS.

$P = 3000$, $R = 20\%$
 $T = 2 \text{ yrs}$, $A = ?$

$20\% = \frac{1}{5}$

$\downarrow 5 : 6 : 6 \downarrow$
 $\downarrow 5 : 5 : 6 \downarrow$

$(P) \quad 25 : 30 : 36 (A)$
 $\downarrow \times 120 \quad \downarrow \times 120$
 $3000 \quad 4320$ ANS.

A sum of money becomes ₹ 4800 after 4 years and ₹ 6000 after 8 years. Find the Principal?

Solution:- I (TRICKY)

$$\begin{cases} A_8 \rightarrow 6000 \\ A_4 \rightarrow 4800 \end{cases}$$

4 yr change $\frac{A_8}{A_4} = \frac{6000}{4800} = \frac{5}{4}$

[Every 4 yrs it will change by $\frac{5}{4}$]

$$\therefore \frac{A_4}{P} = \frac{5}{4} \Rightarrow \frac{4800}{P} = \frac{5}{4} \Rightarrow P = 3840$$

OR $P \times \frac{5}{4} = 4800$ OR $P \times \frac{5}{4} \times \frac{5}{4} = 6000$

$P = 3840$ ANS.

कोई धनराशि 8 साल के बाद 1600 ₹ हो जाती है और 12 साल के बाद 2000 ₹ हो जाती है तो 16 साल बाद मिलनी हो जाएगी?

Solution:- I

$$\begin{cases} A_{12} \rightarrow 2000 \\ A_8 \rightarrow 1600 \end{cases}$$

4 साल में $= \frac{2000}{1600} = \frac{5}{4}$ गुनी

[हर 4 साल बाद $\frac{5}{4}$ गुनी हो जाएगी]

$$A_{12} \times \frac{5}{4} = A_{16}$$

$2000 \times \frac{5}{4} = 2500$ ₹ ANS.

II (SUPER TRICKY)

$$\begin{matrix} & 4 & & 4 & \\ P & \swarrow & & \swarrow & \\ & A_4 & & A_8 & \end{matrix}$$

4800 : 6000

4 : 5 : 5

4 : 5 : 5

16 : 20 : 25

$\downarrow \times 240$ $\downarrow \times 240$

3840

4800

$$\begin{matrix} & 4 \text{ YR} & & 4 \text{ YR} & \\ A_8 & \swarrow & & \swarrow & \\ & A_{12} & & A_{16} & \end{matrix}$$

1600 : 2000

4 : 5 : 5

4 : 4 : 5

16 : 20 : 25

$\downarrow \times 100$
2000

$\downarrow \times 100$
2500 ANS.

CI For 2 years and 3 years for a certain sum is 156 and 254 respectively. Find the Rate of compound interest? a) $14\frac{2}{7}\%$. b) $16\frac{2}{3}\%$. c) 10%. d) 9%.

Solution:- $CI_3 = P \left[\left(1 + \frac{R}{100} \right)^3 - 1 \right] = \frac{254}{156} = \frac{127}{78}$ — (1)

$CI_2 = P \left[\left(1 + \frac{R}{100} \right)^2 - 1 \right]$

Let $1 + \frac{R}{100} = x \Rightarrow \frac{x^3 - 1}{x^2 - 1} = \frac{127}{78} \Rightarrow \frac{(x-1)(x^2+1+x)}{(x-1)(x+1)} = \frac{127}{78}$

$\Rightarrow 78x^2 + 78 + 78x = 127x + 127$

$\Rightarrow 78x^2 - 127x + 78x + 78 - 127 = 0 \Rightarrow 78x^2 - 49x - 49 = 0$

$78x^2 - 91x + 42x - 49 = 0$

OR $13x[6x-7] + 7[6x-7] = 0 \Rightarrow x = \frac{7}{6} \therefore 1 + \frac{R}{100} = \frac{7}{6}$

$\Rightarrow R = 16\frac{2}{3}\% \text{ Ans.}$

OR Check by option in (1)
option b will satisfy.

Find the compound interest on Rs 15625 for 9 months at 16% p.a. compounded quarterly?

Solution:- $R = \frac{16}{4} = 4\%$. and $T = 9 \times 4 = 36 \text{ months} = 3 \text{ yrs}$

$4\% = \frac{1}{25}$

P	A
25	26
25	26
25	26

15625 — 17576

CI = A - P = 1951

OR PASCAL 3 3 1

$3A + 3B + C$

$3 \times \frac{15625 \times 4}{100} + 3 \times \frac{625 \times 4}{100} + 1$

$= 625 \times 3 + 25 \times 3 + 1$

$= 1951 \text{ Ans.}$



INSTALLMENT (1624) IN COMPOUND INTEREST

$$P = \frac{X}{\left[1 + \frac{R}{100}\right]^1} + \frac{X}{\left[1 + \frac{R}{100}\right]^2} + \dots + \frac{X}{\left[1 + \frac{R}{100}\right]^T}$$

where $P = \text{प्रधान / Principal}$, $X = \text{1624 (INSTALLMENT)}$

$T \rightarrow \text{समय (Time) OR No. of Installments}$

A man borrows Rs 21000 at 10% compound interest. How much he has to pay equally at the end of year to settle his loan in two years.

Solution:- I (FORMULA)

$$21000 = \frac{X}{\left[1 + \frac{10}{100}\right]} + \frac{X}{\left[1 + \frac{10}{100}\right]^2}$$

$$\text{OR } 21000 = \frac{10X}{11} + \frac{100X}{121}$$

$$\text{OR } 21000 = \frac{110X + 100X}{121}$$

$$\text{OR } X = 12100 \text{ Ans.}$$

II (TRICKY)

$$R = 10\% = \frac{1}{10} \rightarrow I \Rightarrow \text{Installment} = 11$$

[make each installment equal]

1st year $\frac{P}{10 \times 11}$ Installment

2nd year $\frac{(10)^2}{(11)^2}$

110 121
100 121

$$21000 = 100 \times \frac{210}{100} + \frac{121 \times 100}{100} = 12100$$

A man buys a scooter on making a cash down payment of ₹ 16224 and promise to pay two more yearly installment of equivalent amount in next two years. If the Rate of Interest is 4% p.a.C.I. Find the cash value of scooter?

Solution:- I (BASIC)

$$P = \frac{16224}{\left[1 + \frac{4}{100}\right]^1} + \frac{16224}{\left[1 + \frac{4}{100}\right]^2}$$

$$= 16224 \left[\frac{25}{26} + \frac{625}{676} \right]$$

$$= 30600$$

$$\text{cash value} = 30600 + 16224$$

$$= 46824 \text{ Ans.}$$

II (TRICKY) $R = 4\% = \frac{1}{25}$

Principal Installment

I 25×26 26×26

II $+ 625$ 676

1275 676

1×24 1×24

30600 16224

$$\text{CASH VALUE} = 30600 + 16224 = 46824$$

A man borrows Rs 4200 and undertakes to pay back with CI @ 10% p.a in two equal yearly installments at the end of 1st and 2nd year. what is the amount of each installment?

Solution :- $R = 10\% = \frac{10}{100}$

[but installment must be equal]

	P	Inst.
1st Yr	10×11	11×11
2nd Yr	$\frac{10}{100}$	$\frac{11}{121}$
	<hr/>	<hr/>
	210	121

OR by FORMULA

$$4200 = \frac{x}{\left[1 + \frac{10}{100}\right]} + \frac{x}{\left[1 + \frac{10}{100}\right]^2}$$

$$\begin{array}{r} 210 \\ | \times 20 \end{array} \quad \begin{array}{r} 121 \\ | \times 20 \end{array}$$

$$\Rightarrow 4200 = x \left[\frac{10}{11} + \frac{100}{121} \right]$$

$$4200 \quad 2420 \text{ Ans.} \Rightarrow 4200 = \frac{210x}{121} \Rightarrow x = 2420 \text{ Ans.}$$

A man borrows Rs 1820 and undertakes to pay back with compound interest @ 20% p.a in 3 equal yearly installment at the end of 1st, 2nd and 3rd year. what is the amount of each installment?

Solution :- $R = 20\% = \frac{20}{100} \Rightarrow \text{Installment} = 5+1=6$

1st	5×36	$6 \times 36 = 216$	} Installment must be equal
2nd	25×6	$36 \times 6 = 216$	
3rd	125	$216 = 216$	
	<hr/>	<hr/>	
	455	216	
	$ \times 4$	$ \times 4$	
	1820	864	

864 Ans.

A man borrows a certain sum of money and pays it back in two equal installments, if CI is reckoned at 5% per annum and he pays back annually Rs 882. what sum did he borrow?

Solution :- $R = 5\% = \frac{5}{100}$

	P	I	} [Installment must be equal]
1st	20×21	21×21	
2nd	$\frac{400}{100}$	$\frac{441}{100}$	
	<hr/>	<hr/>	
	820	441	
	$ \times 2$	$ \times 2$	
Ans	1640	882	

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