

ARRAYS : CARRY FORWARD

"Believe you can and you're halfway there."

~ Theodore Roosevelt



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Today's content

01. Count pairs "ag"
02. Leaders in an array
03. Subarray basics
04. Subarray containing min & max

01. Count pairs "ag"

Given a `char[] s`. Calculate no. of pairs ^{indices} (i, j) such that $i < j$ & $s[i] = 'a'$ & $s[j] = 'g'$.

Note:- All characters are in lower case.

Constraints : $1 \leq N \leq 10^5$ $N = \text{len of array}$

$'a' \leq s[i] \leq 'z'$

Eg:- $s[8] : \{ b \ a \ a \ g \ d \ c \ a \ g \}$
 0 1 2 3 4 5 6 7

Pairs

(1, 3) (1, 7)

(2, 3) (2, 7)

(6, 7)

ans = 5

Eg:- $\{ b \ c \ a \ g \ g \ a \ a \ g \}$
 0 1 2 3 4 5 6 7

Pairs $\{ (2, 3) \ (2, 4) \ (2, 7) \}$
 $(5, 7) \ (6, 7)$

Ans = 5

Eg:- { a c g d g a g }

Pairs - (0, 2) (5, 6)
(0, 4)
(0, 6)

Ans = 4

Brute force Approach

↘
Check for all the pairs & count the no. of "ag" pairs

count = 0;

for (i = 0 ; i < N ; i++)

TC: $O(n^2)$

SC: $O(1)$

for (j = i+1 ; j < N ; j++) {

if (s[i] == 'a' && s[j] == 'g')

count++;

{ b c a g g a a g }

↑
j

Idea 2 → Consider only correct pairs

count = 0

```
for (i=0; i<N; i++)
```

TC : $O(n^2)$

SC : $O(1)$

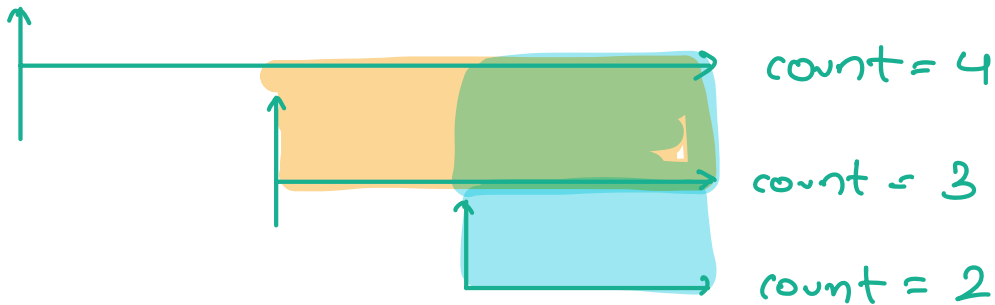
```
    if (s[i] == 'a')
```

```
        for (j=i+1; j<N; j++) {
```

```
            if (s[j] == 'g') count = count + 1;
```

```
}
```

Ex: a d g a g a g f g



count = 9

Optimised Approach



Count the no. of 'g' from right hand side & update the answer as soon as you have 'a'

↖ overall ans
ans = 0

↖ count of g
count = 0

a	d	g	a	g	a	g	f	g
ans += c ans = 5 + 4 = 9	×	c = c + 1 c = 4	ans = ans + c ans = 2 + 3 = 5	c = c + 1 c = 3	ans = ans + c ans = 2	c = c + 1 c = 2		c = c + 1 c = 1

Ans = 9

⇒

c = 0 , ans = 0

for (i = n - 1 ; i ≥ 0 ; i --)

if (s[i] == 'g') { c = c + 1 ; }

if (s[i] == 'a') { ans = ans + c ; }

}

return ans ;

TC = O(n)

SC = O(1)

TODO → Figure out the way to build our answer by counting no. of 'a's & update the answer at j .

Leaders in Array

Given an array $arr[N]$, count the no. of leaders.

An ele is a leader if it is strictly greater than all the ele on right hand side

Note :- $arr[N-1]$ is always a leader

Eg:- { 15 -1 7 4 2 5 2 3 } Ans = 4

Eg :- { 10 7 9 3 2 4 }
 0 1 2 3 4 5 Ans = 3

Eg:- { 8 8 8 } Ans = 1

Brute force → For every element, iterate on to RHS & find max if ($arr[i] > \max$) leader ++;

TC = $O(n^2)$

SC = $O(1)$

Optimised Idea \rightarrow Carry forward the max of elements of RHS

\Rightarrow

count = 1

max = arr[n-1]:

for (i = n-2; i \geq 0; i--) {

if (arr[i] > max) {

count = count + 1;

max = arr[i]

3

3

7 9 8
max = 8

TC: $O(n)$

SC: $O(1)$

Subarray \rightarrow Continuous part of the array

Note:- {
01. A single ele
02. A complete array is also a subarray
03. [] \rightarrow No

Eg:- { 1, 2, 3, 4, 10, 7, 6 }
0 1 2 3 4 5 6

indices \rightarrow (1, 4) \longrightarrow { 2, 3, 4, 10 }

indices \rightarrow (2, 5) \longrightarrow { 3, 4, 10, 7 }

indices \rightarrow (6, 6) \longrightarrow { 6 }

indices $\rightarrow (s \ e) \longrightarrow \text{len of subarr} = e - s + 1$

03. Closest Min - Max

Given an array, find the length of smallest subarray which contains both min & max of array.

Eg:-

1	2	3	1	3	4	6	4	6	3
0	1	2	3	4	5	6	7	8	9

Min = 1

max = 6

subarray $[0 \ 6] \rightarrow \text{len} = 6$

subarray $[3 \ 6] \rightarrow \text{len} = 6 - 3 + 1 = 4$

Eg:- { 2 2 6 4 5 1 5 2 6 4 1 }

0	1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	---	----

min = 1

max = 6

subarr = $[2 \ 5] \rightarrow \text{len} = 4$

subarr = $[8 \ 10] \rightarrow \text{len} = 10 - 8 + 1 = 3$

Eg:- { 8, 8, 8, 8, 8 }

min = 8

max = 8

subarray $\rightarrow [0 \ 0] \rightarrow \text{len} = 1$

Observations

01. If min & max are same, ans = 1

02. Can you have more than one min or max in subarr

$\{1, 6, 1, 6\}$

$1, 2, 5, 1, 6$

$1, 2, 3, 1, 3, 4, 6$

$1, 2, 5, 5, 6, 6$

↓
To get the smallest subarr, we only need one min & one max

03. Position of min max → should be at the corners of subarray

subarr → $\{ \dots \text{min} \dots \text{max} \dots \}$

subarr → $\{ \dots \text{max} \dots \text{min} \}$

04. subarr $[i \dots j] \Rightarrow \text{len} = j - i + 1$

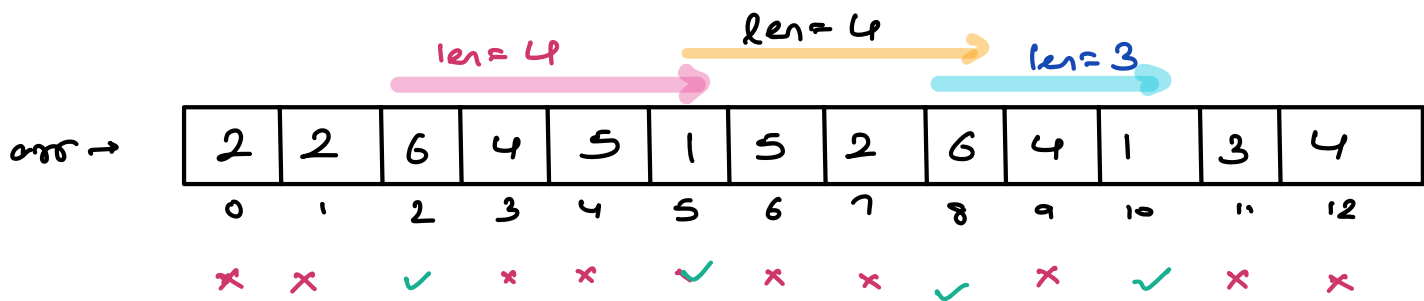
05. Case I $\rightarrow \{ \text{min} \quad \text{max} \}$ if $(\text{arr}[i] == \text{min})$

\downarrow
Need to look for
closest max on
RHS

Case II $\rightarrow \{ \text{max} \quad \text{min} \}$ if $(\text{arr}[i] == \text{max})$

\downarrow
closest min on RHS

$\text{Min} = 1$
 $\text{Max} = 6$



Ans = 3

01. Iterate & find the min & max of the array.

if $(\text{min} == \text{max})$ return 1

ans = n ;

```
for (i=0; i<n; i++)
```

```
    if (arr[i] == min) // look for first max
```

```
        for (j=i+1; j<n; j++) {
```

```
            if (arr[j] == max) {
```

```
                ans = min(ans, j-i+1);  
                break;
```

```
        }
```

```
    if (arr[i] == max)
```

```
        for (j=i+1; j<n; j++)
```

```
            if (arr[j] == min)
```

```
                ans = min(ans, j-i+1);  
                break;
```

```
    }
```

```
}
```

```
return ans;
```

TC = $O(n^2)$

SC = $O(1)$

Idea → Carry forward the mini & maxi

$$\text{Min} = 1$$

$$\text{mini} = -1$$

$$\text{ans} = 17$$

$$\text{max} = 6$$

$$\text{maxi} = -1$$



Eg.:

1	6	4	6	5	1	5	2	6	4	4	2	1	2	
---	---	---	---	---	---	---	---	---	---	---	---	---	---	--

0

1

2

3

4

5

6

7

8

9

10

11

12

12

$$\text{mini} = 0$$

$$\text{mini} = 5$$

$$\text{mini} = 5$$

$$\text{mini} = 5$$

$$\text{mini} = 12$$

$$\text{mini} = 12$$

$$\text{maxi} = 1$$

$$\text{maxi} = 1$$

$$\text{maxi} = 3$$

$$\text{maxi} = 8$$

$$\text{maxi} = 8$$

$$\text{maxi} = -1$$

$$\text{as} = 3 \text{ vs } 2$$

$$\text{as} = 3 \text{ vs } 5$$

$$\text{as} = 4 \text{ vs } 3$$

$$\text{as} = 5 \text{ vs } 4$$

$$\text{as} = 14 \text{ vs } 5$$

2

3

3

as = 4

= 5

$$\text{Min} = 1$$

$$\text{mini} = -1$$

$$\text{ans} = 5$$

$$\text{Max} = 6$$

$$\text{maxi} = -1$$



1	2	<u>6</u>	1	3
---	---	----------	---	---

0

1

2

3

4

$$\text{mini} = 0$$

$$\text{mini} = 0$$

$$\text{mini} = 3$$

$$\text{maxi} = -1$$

$$\text{maxi} = 2$$

$$\text{maxi} = 2$$

$$\text{as} = 5 \text{ vs } 3$$

$$\text{as} = 3 \text{ vs } 2$$

3

2

01. Iterate & find min & max

if (min == max) return 1;

ans = n, mini = -1, maxi = -1

for (i = n - 1 ; i ≥ 0 ; i--) {

if (arr[i] == min)

mini = i ;

if (maxi != -1) {

ans = minimum (ans , maxi - mini + 1)

}

}

if (arr[i] == max)

maxi = i

if (mini != -1)

ans = minimum (ans , mini - maxi + 1)

}

}

TC: $O(n)$

SC: $O(1)$

}

return ans;

Doubt session

$${}^nC_r = \frac{n!}{(n-r)! * r!}$$

$${}^3C_2 = \frac{3!}{(3-2)! * 2!} = \frac{3 * \cancel{2} * 1}{1 * \cancel{2} * 1} = 3$$

Product Array puzzle

1	6	5	4	3	2
0	1	2	3	4	5

pmul =

1	6	30	120	360	720
0	1	2	3	4	5

smul =

720	720	120	24	6	2
0	1	2	3	4	5

For a particular ar[i]

$$as = pmul[i-1] * smul[i+1]$$