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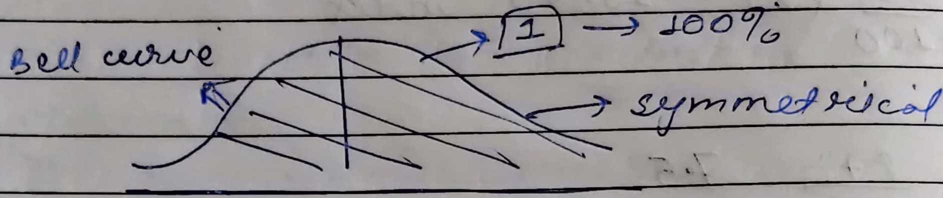
Topics

1. Normal Distribution/Gaussian Dist.
2. Standard Normal distribution
3. Z score
4.

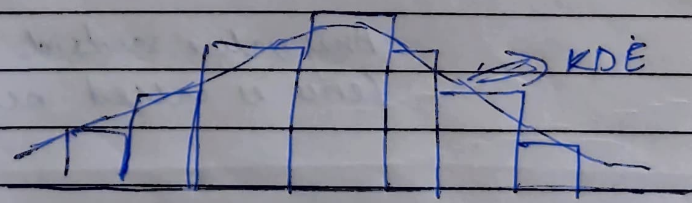
Gaussian / Normal Distribution



As per domain expertise Age, weight, height data were having ~~Guassian~~ Gaussian distribution

IRIS DATASET

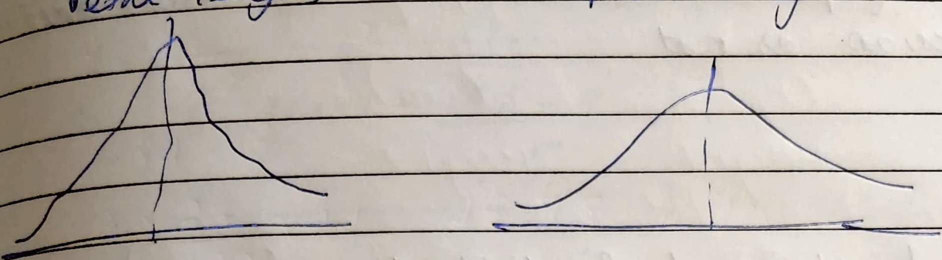
→ When histogram is smoothen using Kernel density estimator (KDE) then we get Guassian Distribution



→ IRIS Dataset was first where ML was applied

IRIS Dataset

Petal length   Sepal length



* Emperical Rule of Normal / Guassian distribution

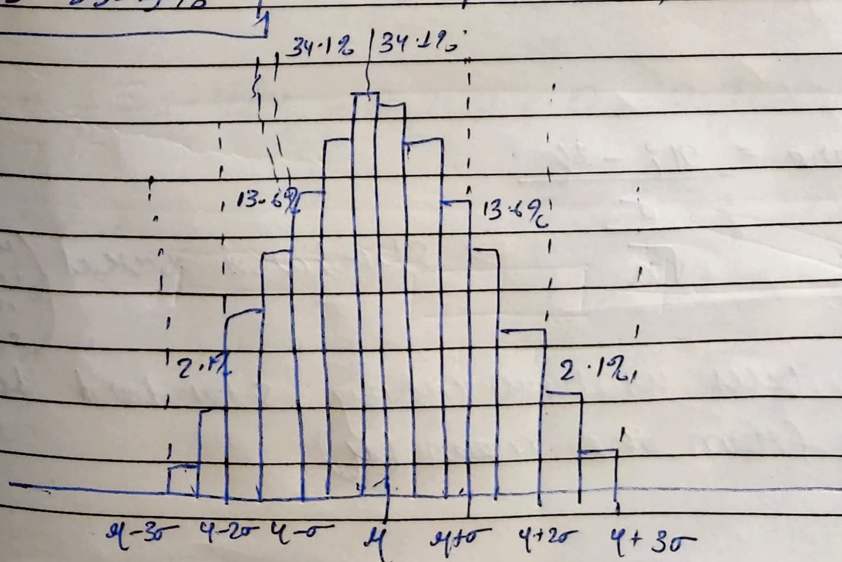
* Assumptions of the data

→ Around ~~to~~ 68% of ~~data~~ the entire distribution falls under first standard deviation to the ~~ft~~ left and right

→ Around 95% of the entire distribution falls under second standard deviation to the left and right

→ ~~Arou~~ Around 99.7% of the entire distribution falls under three standard deviation to the ~~te~~ left and right

$\boxed{68-95-99.7\%}$ → Emperical ~~formula~~ rule



→ using Q-Q plot we can find whether distribution is Gaussian or not

Standard Normal distribution (SND)

~~Let~~ x is a random variable with Gaussian Distribution

$$x \approx \text{Gaussian Distribution}(\mu, \sigma)$$
$$\Downarrow$$
$$y \approx SND(\mu = 0, \sigma = 1)$$

→ using Z score formula we ~~get SND~~ can convert Gaussian to SND

$x = \{1, 2, 3, 4, 5\}$

$\mu = 3$
$\sigma = 1.41$

$$Z\ \text{score} = \frac{x_i - \mu}{\boxed{\frac{\sigma}{\sqrt{n}}}}$$

$\Rightarrow$ Standard error (will be used in inferential stats)

⇒ Z score tells us how many standard deviation (σ) away from the mean (μ)

here $\boxed{n=1}$, since $n=1$ will be applied to all value of dataset x

$$\therefore \boxed{Z\text{-score} = \frac{x_i - \mu}{\sigma}}$$

$x = \{1, 2, 3, 4, 5\}$

$\mu = 3$

$\sigma = 1.414$

$= \frac{1-3}{1.414} = \cancel{-1.14}\ -1.414$

$= \frac{2-3}{1.414} = -0.707$

$= \frac{3-3}{1.414} = 0$

$= \frac{4-3}{1.414} = 0.707$

$= \frac{5-3}{1.414} = +1.414$

$\therefore y = \{-1.414, -0.707, 0, 0.707, 1.414\}$

mean (μ) has become 0

Q) Why we are converting Gaussian to SND

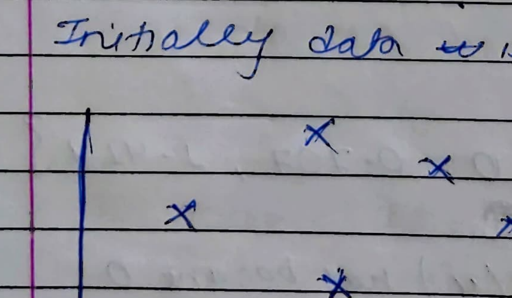
(years) Age	(Kg) Weight	(cm) Height
24	72	150
26	78	160
32	84	165
33	92	170
34	87	150
28	83	180
29	80	175

This above dataset has different units and data is having high difference values

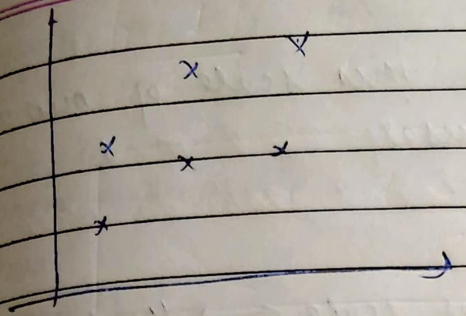
24 → 72 → 150

72	150
:	:
80	175

Initially data is



By using standardization, we are trying to bring the data closer



v.v. imp

* standardisation is used to achieve this scaling down of values, where

$\mu = 0$

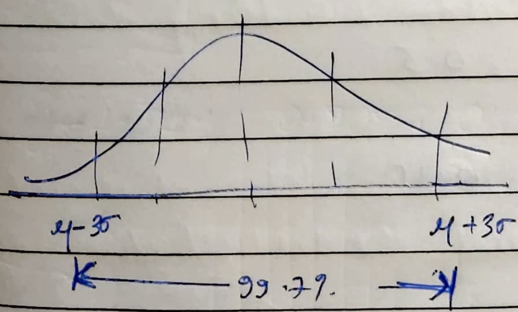
$\sigma = 1$

using Z score formula we can achieve this

standardisation {Z-score}

$\boxed{\mu = 0, \sigma = 1}$

[$-3 \longleftrightarrow +3$] values are converted in this range automatically



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→ But in Normalization this scale of min and max is defined by user

Normalization [Lower scale ⟶ Higher scale]

① Min Max Scaler [0-1]

$$\boxed{x_{scaled} = \frac{x - x_{min}}{x_{max} - x_{min}}}$$

using above formula

x ⇒	y
1	0
2	0.25
3	0.5
4	0.75
5	1

$\Rightarrow \frac{1-1}{5-1} = 0$

$\Rightarrow \frac{2-1}{5-1} = \frac{1}{4} = 0.25$

$\Rightarrow \frac{3-1}{5-1} = \frac{2}{4} = 0.5$

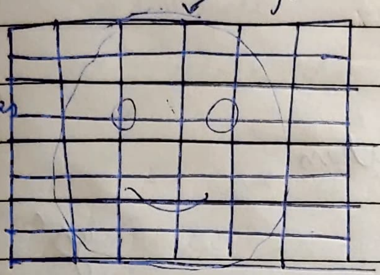
$\Rightarrow \frac{4-1}{5-1} = \frac{3}{4} = 0.75$

$\Rightarrow \frac{5-1}{5-1} = 1$

Application of Normalization

- Deep learning
- where ~~pix~~ pixels are involved
- where Guassian distribution is not required

Image



In an image the ~~pix~~ ~~pix~~ pixels will range between (0-255)

It can be scaled down to 0-1 using Normalization

Imp

* Feature scaling
  - Standardization (In ML)
  - Normalization (In DL)

{ In most cases. }

RECAP

Standardization

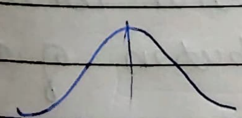
$x \rightarrow$ Normal distribution (μ, σ)

$\Downarrow$ Z score

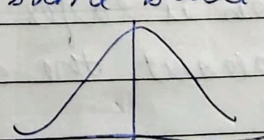
$y \rightarrow$ SND $(\mu = 0, \sigma = 1)$

$$\boxed{Z \text{ score} = \frac{x_i - \mu}{\sigma}}$$

Why we are doing $\rightarrow$ Bring the features in the same scale



100



0

B.

Normalization

→ Here we are not doing $\mu = 0$, & $\sigma = 1$
→ we are using Min Max scalar to bring it in a range

Normalization | | Standardization |
--- | --- | --- | ---

x →	y	x'	y'
~~0~~	~~0~~	~~-1.414~~	
1	0	-0.707	-1.414
2	0.25	0	-0.707
3	0.5	+0.707	0
4	0.75	-	+0.707
5	1		+1.414

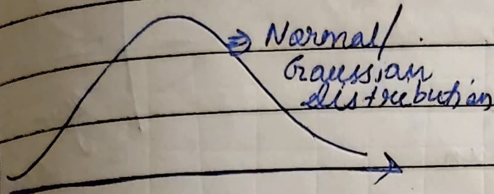
Here GD is not maintained

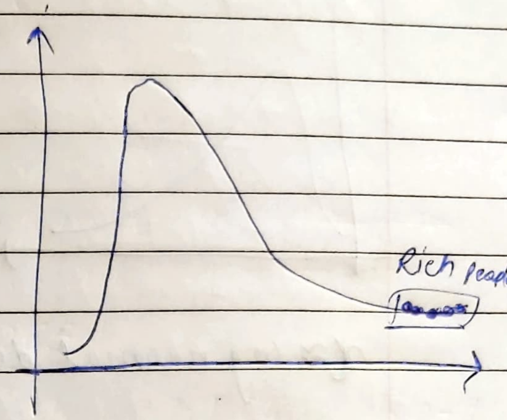
Here Gaussian Distribution is maintained

→ Standardization is ideal for data that gets a normal / gaussian distribution
→ It's superior when handling data with outliers

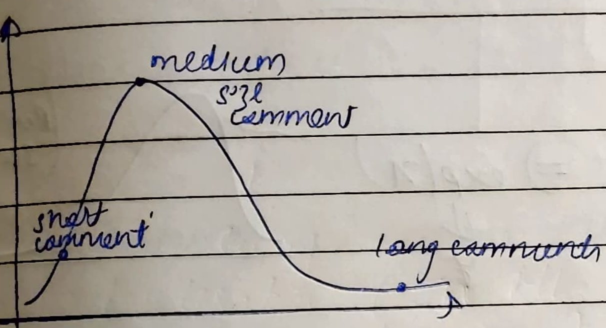
→ Normalization is safer alternative when we are unsure about the distribution of data

Log Normal Distribution





Wealth
Distribution

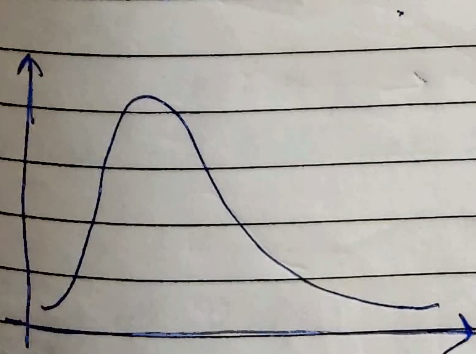


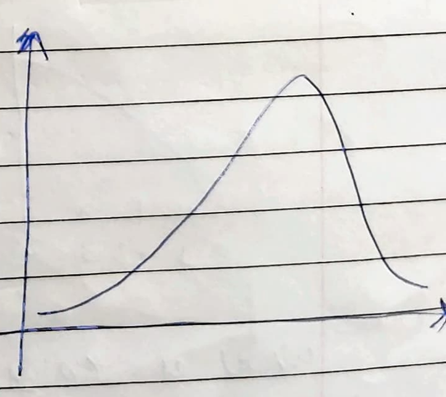
length of
comments

~~Assignment~~

Assignment

From ascending order give the relation of mean, median and mode?





$\ln(x)$ ⇒ $\log_e(x)$ (natural log)
$\log(x)$ ⇒ $\log_{10}(x)$

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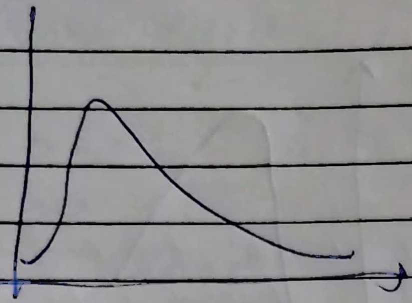
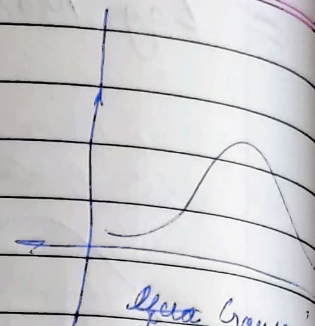
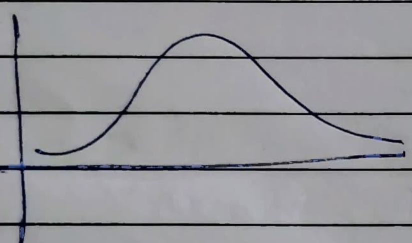


⇒ ~~log(x)~~ $y = \ln(x)$ →

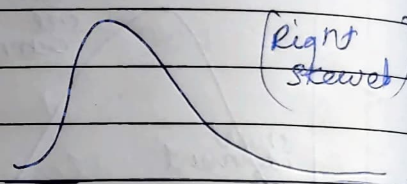


Gaussian distribution

$x \approx$ log normal distribution



⇒ $\exp(x)$ ⇓ y



(Right skewed)

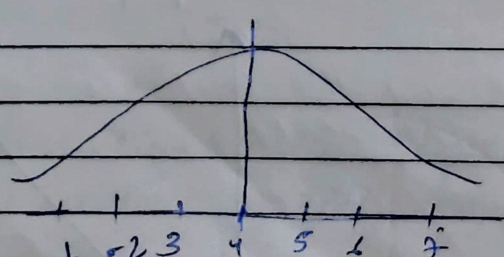
$x \approx$ Normal Distribution

$y \approx$ log normal distribution

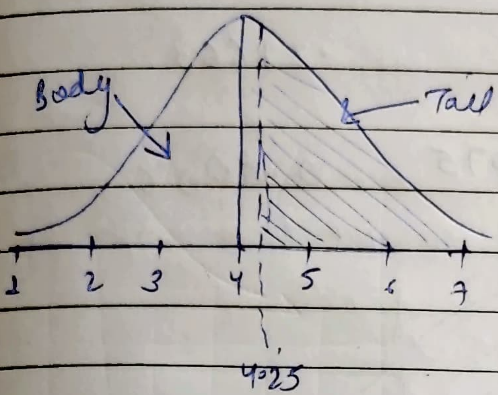
→ only right skewed is log normally distributed

Q

$x = \{1, 2, 3, 4, 5, 6, 7\}$ $\left.\begin{matrix}\mu = 4 \\ \sigma = 1\end{matrix}\right\}$ let

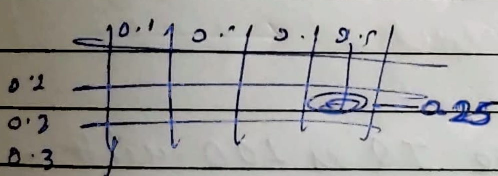


What is the ~~perc~~ percentage of score that fall above 4.25?



Z score = $\frac{x_i - \mu}{\sigma} = \frac{4.25 - 4}{1} = 0.25$

V.V. Imp
Using Z table we can get the area



You can get values of Z score from google search

0.59 ⇒ 59%

-0.25

1 - 0.59% = 0.41%

For 3.75

Z score = $\frac{3.75 - 4}{1} = -0.25$

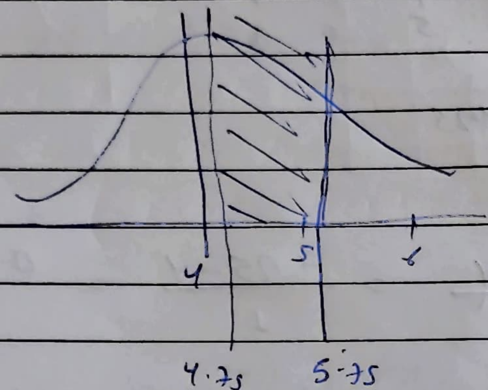
using Z table: 0.4052 ⇒

∴ %age = 40%

4.75 & ~~4.5757~~ 5.75

$\frac{4-4.75}{1} = -0.75$ .22663

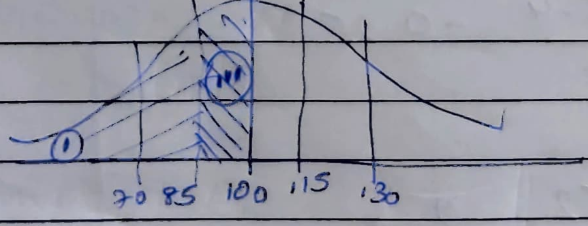
$\frac{48-5.75}{1} = -1.75$ 0.4006



40 - 22 = 18%

(Q) In India the average IQ is 100 with a standard deviation of 15. What is the percentage of population would you expect do have an IQ

(i) Lower than 85
(ii) Higher than 85
(iii) Between 85 and 100



(i) Z score $= \frac{85-100}{15} = -1$ $= .1587$
$= 15.87$ (Ans)

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(iii) $1 - 15.87$

$= 84.13$

(iii) $0.5 - 0.1587$

$= 0.3413$