

Matrix Theory Assignment 8

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Abstract—This problem demonstrate a method to find weather given transformation is linear or not.

All the codes for the figure in this document can be found at

https://github.com/Ritesh622/Assignment_EE5609/tree/master/Assignment_8

1 PROBLEM

Find weather given functions \mathbf{T} from \mathbb{R}^2 into \mathbb{R}^2 are linear transformations or not

$$\mathbf{T}(x_1, x_2) = (x_1^2, x_2) \quad (1.0.1)$$

2 SOLUTION

Let

$$\mathbf{A} = (x_1, x_2) \mathbf{P} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad (2.0.1)$$

and

$$\mathbf{Q} = \begin{pmatrix} x_1 & 0 \\ 0 & 1 \end{pmatrix} \quad (2.0.2)$$

We know that if we have \mathbf{P} as a fixed matrix with entries in the field \mathbb{F} and \mathbf{Q} be a fixed matrix over \mathbb{F} . then we can define a function \mathbf{T} from the space $\mathbb{F}^{m \times n}$ into itself by $\mathbf{T}(\mathbf{A}) = \mathbf{PAQ}$. Then \mathbf{T} is a linear transformation from \mathbb{F} into \mathbb{F} .

Now given transformation can be written as :

$$\mathbf{T}(x_1, x_2) = \mathbf{PAQ} \quad (2.0.3)$$

$$\Rightarrow \mathbf{T}(x_1, x_2) = \begin{pmatrix} 1 \\ 1 \end{pmatrix} (x_1 \ x_2) \begin{pmatrix} x_1 & 0 \\ 0 & 1 \end{pmatrix} \quad (2.0.4)$$

We can observe that matrix \mathbf{Q} is not a fixed matrix. Hence we can conclude that given transformation is not linear.