

Module 1: Basics of Information Theory

(6 Hrs)

(6 hrs → around 5–6 MCQs.)

1.

The unit of information is:

- a) Bit
- b) Byte
- c) Nibble
- d) Word

Answer: a) Bit

2.

If the probability of an event is $\frac{1}{4}$, what is the information content (in bits)?

- a) 2
- b) 4
- c) 1
- d) 0.5

Answer: a) 2

Reason: $\text{Information} = -\log_2(P) = -\log_2(1/4) = 2$

3.

The entropy $H(X)H(X)H(X)$ of a random variable XXX is maximum when:

- a) All outcomes are equally likely
- b) One outcome is certain
- c) Probabilities are different
- d) None of these

Answer: a) All outcomes are equally likely

4.

Mutual Information $I(X;Y)$ is zero if and only if:

- a) XXX and YYY are dependent
- b) XXX and YYY are independent
- c) Entropy is zero
- d) Information rate is zero

Answer: b) XXX and YYY are independent

5.

Which channel model assumes no memory and independent errors?

- a) AWGN channel
- b) Binary Symmetric Channel
- c) Fading Channel
- d) Erasure Channel

Answer: b) Binary Symmetric Channel

6.

Channel capacity is defined as:

- a) Minimum achievable data rate
- b) Maximum achievable data rate
- c) Average achievable data rate
- d) Zero achievable data rate

Answer: b) Maximum achievable data rate

Set 1

Match the following:

Left Side

Entropy

Right Side

Average information per symbol

Information Rate	Information per second
Mutual Information	Shared information between two variables

Answer Set 1:

- Entropy → Average information per symbol (Definition)
 - Information Rate → Information per second (Rate = bits/sec)
 - Mutual Information → Shared information between two variables (Common part)
-

Set 2

Match the following:

Left Side	Right Side
Joint Entropy	Entropy of combined variables
Conditional Entropy	Uncertainty of one variable given another
Shannon's Theorem	Limit for reliable communication

Answer Set 2:

- Joint Entropy → Entropy of combined variables ($H(X, Y)$)
- Conditional Entropy → Uncertainty of one variable given another ($H(Y|X)$)
- Shannon's Theorem → Limit for reliable communication (Defines channel capacity)

Set 3

Match the following:

Left Side	Right Side
Noiseless Channel	No error
Channel Capacity	Maximum possible data rate
Channel Model	Represents channel behavior

Answer Set 3:

- Noiseless Channel → No error (Ideal case)
- Channel Capacity → Maximum possible data rate (Upper bound)
- Channel Model → Represents channel behavior (Includes noise, distortion, etc.)

Module 2: Data Compression (14 Hrs)

1.

Which of the following is a variable-length, prefix-free code?

- a) Shannon-Fano code
- b) Huffman code
- c) Arithmetic code
- d) Both a and b

Answer: d) Both a and b

2.

In Huffman coding, the two symbols combined at each step have:

- a) Highest probabilities
- b) Lowest probabilities
- c) Equal probabilities
- d) Random probabilities

Answer: b) Lowest probabilities

3.

The source coding theorem states that the average codeword length is:

- a) Equal to entropy
- b) Always greater than entropy
- c) Always less than entropy
- d) Close to entropy but not less

Answer: d) Close to entropy but not less

4.

Which coding technique achieves compression by grouping similar adjacent pixel values?

- a) Run Length Encoding (RLE)
- b) Huffman Coding

- c) Arithmetic Coding
- d) LZW Coding

Answer: a) Run Length Encoding (RLE)

5.

In arithmetic coding, a message is represented as:

- a) A binary tree
- b) A sequence of fixed codes
- c) A fractional interval
- d) A vector of codewords

Answer: c) A fractional interval

6.

LZW coding is best suited for:

- a) Random data
- b) Highly redundant data
- c) Encrypted data
- d) Compressed data

Answer: b) Highly redundant data

7.

Which of the following is NOT a type of Quantization?

- a) Scalar Quantization
- b) Vector Quantization
- c) Differential Quantization
- d) Arithmetic Quantization

Answer: d) Arithmetic Quantization

8.

Transform coding is based on the idea of:

- a) Encoding frequently occurring patterns
- b) Reducing signal energy

- c) Representing signals in another domain
- d) Replicating the signal

Answer: c) Representing signals in another domain

9.

Which transform is most commonly used in JPEG image compression?

- a) Fourier Transform
- b) Hadamard Transform
- c) Discrete Cosine Transform
- d) Wavelet Transform

Answer: c) Discrete Cosine Transform

10.

Sub-band coding divides a signal into:

- a) Time intervals
- b) Frequency bands
- c) Amplitude levels
- d) Signal energy parts

Answer: b) Frequency bands

11.

Which compression method is generally used for audio signals?

- a) Run Length Encoding
- b) Huffman Coding
- c) Sub-band coding
- d) Arithmetic Coding

Answer: c) Sub-band coding

12.

Video compression primarily exploits:

- a) Frequency redundancy
- b) Spatial and temporal redundancy

- c) Signal distortion
d) Quantization error

Answer: b) Spatial and temporal redundancy

Set 1

Match the following:

Left Side	Right Side
Shannon-Fano Coding	Based on symbol probability
Huffman Coding	Optimal prefix code
Arithmetic Coding	Represents entire message as one number

Answer Set 1:

- Shannon-Fano Coding → Based on symbol probability (Builds tree based on probability)
- Huffman Coding → Optimal prefix code (Greedy algorithm)
- Arithmetic Coding → Represents entire message as one number (Interval coding)

Set 2

Match the following:

Left Side **Right Side**

Run Length Encoding	Good for repetitive data
Scalar Quantization	Single value mapping
Sub-band Coding	Divides signal into frequency bands

Answer Set 2:

- Run Length Encoding → Good for repetitive data (e.g., images, black/white areas)
 - Scalar Quantization → Single value mapping (One symbol quantization)
 - Sub-band Coding → Divides signal into frequency bands (Compression technique)
-

Set 3

Match the following:

Left Side	Right Side
Differential Coding	Stores difference between values
Vector Quantization	Group-based quantization
Transform Coding	Converts signal to another domain

Answer Set 3:

- Differential Coding → Stores difference between values (Delta coding)

- Vector Quantization → Group-based quantization (Block coding)
 - Transform Coding → Converts signal to another domain (e.g., DCT)
-

Set 4

Match the following:

Left Side	Right Side
Audio Coding	Compression based on human hearing
Video Compression	Exploits spatial and temporal redundancy

Answer Set 4:

- Audio Coding → Compression based on human hearing (e.g., MP3)
- Video Compression → Exploits spatial and temporal redundancy (e.g., MPEG)

Module 3: Linear Block Codes (6 Hrs)

1.

Error control coding is needed primarily to:

- a) Increase transmission speed
- b) Reduce bandwidth
- c) Detect and correct errors
- d) Encrypt the data

Answer: c) Detect and correct errors

2.

In linear block codes, the set of valid codewords forms a:

- a) Vector space
- b) Matrix space
- c) Affine space
- d) Random set

Answer: a) Vector space

3.

Which of the following matrices is used for detecting errors?

- a) Generator matrix
- b) Parity check matrix
- c) Syndrome matrix
- d) Transformation matrix

Answer: b) Parity check matrix

4.

The syndrome vector in error detection is computed as:

a) $S = H \times C^T$

b) $S = H \times R^T$

c) $S = G \times C^T$

d) $S = G \times R^T$

Answer: b) $S = H \times R^T$

Reason: H = parity matrix, R = received word.

5.

A linear block code with minimum distance d_{min} can detect up to:

a) d_{min} errors

b) $d_{min} - 1$ errors

c) $d_{min}/2$ errors

d) $d_{min} + 1$ errors

Answer: b) $d_{min} - 1$ errors

6.

If a code can correct up to t errors, then its minimum distance must be at least:

a) $2t+1$

b) $2t+1$

c) t

d) $t+1$

Answer: b) $2t+1$

Set 1

Match the following:

Left Side	Right Side
Single-bit Error	Only one bit flipped
Burst Error	Multiple consecutive bits flipped
Parity Bit	Simple error detection

Answer Set 1:

- Single-bit Error → Only one bit flipped (Common error)
 - Burst Error → Multiple consecutive bits flipped (Typical in noisy channels)
 - Parity Bit → Simple error detection (Even/odd parity)
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Set 2

Match the following:

Left Side	Right Side
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Linear Block Codes	Satisfy linearity property
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Generator Matrix	Used to encode data
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Parity Check Matrix	Used to detect errors
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Answer Set 2:

- Linear Block Codes → Satisfy linearity property (Addition of codewords = codeword)
- Generator Matrix → Used to encode data (G matrix)
- Parity Check Matrix → Used to detect errors (H matrix)

Set 3

Match the following:

Left Side

Right Side

Syndrome
Decoding

Uses parity check matrix

Error Syndrome Non-zero when error exists

Minimum Distance Minimum number of differing bits

Answer Set 3:

- Syndrome Decoding → Uses parity check matrix (Checks for errors)
- Error Syndrome → Non-zero when error exists (If syndrome = 0 → No error)
- Minimum Distance → Minimum number of differing bits (Important for error correction)

Module 4: Cyclic Code and Convolution Code (9 Hrs)

1.

Cyclic codes are a subset of:

- a) Linear block codes
- b) Convolution codes
- c) Source codes
- d) Prefix codes

Answer: a) Linear block codes

2.

The generator polynomial $g(x)$ of a cyclic code must:

- a) Divide $x^n - 1$ exactly
- b) Be irreducible
- c) Have degree 1
- d) Always be primitive

Answer: a) Divide $x^n - 1$ exactly

3.

In cyclic redundancy check (CRC), the remainder obtained is known as:

- a) Syndrome
- b) Parity
- c) Check bits
- d) Redundancy bits

Answer: a) Syndrome

4.

The primary advantage of cyclic codes is:

- a) Ease of encoding and decoding
- b) Less hardware required
- c) No need for error detection
- d) Low memory usage

Answer: a) Ease of encoding and decoding

5.

BCH codes are a type of:

- a) Block codes
- b) Convolutional codes
- c) Cyclic codes
- d) Source codes

Answer: c) Cyclic codes

6.

Convolutional codes process:

- a) Blocks of data at a time
- b) Continuous data streams
- c) Only error-free data
- d) Random blocks

Answer: b) Continuous data streams

7.

In convolutional encoding, the constraint length refers to:

- a) Length of input sequence
- b) Memory of the encoder
- c) Number of parity bits
- d) Decoding delay

Answer: b) Memory of the encoder

8.

Which decoding technique is commonly used for convolutional codes?

- a) Hamming decoding
- b) Viterbi algorithm
- c) Syndrome decoding
- d) Turbo decoding

Answer: b) Viterbi algorithm

9.

Tree and trellis diagrams are used in convolutional coding mainly for:

- a) Compression
- b) Encryption
- c) Error detection
- d) Decoding paths

Answer: d) Decoding paths

Set 1

Match the following:

Left Side

Cyclic Codes

BCH Codes

Right Side

Codewords are cyclic shifts

Correct multiple errors

Generator Polynomial	Used to generate cyclic codes
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Answer Set 1:

- Cyclic Codes → Codewords are cyclic shifts (Circular property)
- BCH Codes → Correct multiple errors (Designed for powerful correction)
- Generator Polynomial → Used to generate cyclic codes ($G(x)$ defines the code)

Set 2

Match the following:

Left Side

Right Side

Syndrome Computation

Used for error detection in cyclic codes

Convolutional Encoder

Uses shift registers

Trellis Diagram

Visual representation of code sequences

Answer Set 2:

- Syndrome Computation → Used for error detection in cyclic codes (Calculates remainder)
 - Convolutional Encoder → Uses shift registers (Sequential encoding)
 - Trellis Diagram → Visual representation of code sequences (Paths and states)
-

Set 3

Match the following:

Left Side	Right Side
Convolution Codes	Encodes with memory
Tree Diagram	Shows all possible code paths
Viterbi Algorithm	Optimal decoding for convolution codes

Answer Set 3:

- Convolution Codes → Encodes with memory (Depends on previous bits)
- Tree Diagram → Shows all possible code paths (Branching structure)

- Viterbi Algorithm → Optimal decoding for convolution codes (Dynamic programming approach)

Module 5: Basics of Number Theory and Cryptography (10 Hrs)

1.

A prime number is a number that:

- a) Has exactly two distinct positive divisors
- b) Has only one divisor
- c) Is divisible by all numbers
- d) Has no divisors

Answer: a) Has exactly two distinct positive divisors

2.

Random number generation is important in cryptography for:

- a) Faster encryption
- b) Reducing errors
- c) Increasing security
- d) Data compression

Answer: c) Increasing security

3.

The solution to $ax+by=d$ exists if and only if:

- a) d divides a
- b) d divides b
- c) d divides $\gcd(a,b)$
- d) a and b are coprime

Answer: c) d divides $\gcd(a,b)$

4.

The Chinese Remainder Theorem is applicable when moduli are:

- a) Coprime
- b) Equal
- c) Prime numbers only
- d) Divisible by each other

Answer: a) Coprime

5.

Which of the following statements is TRUE according to Fermat's Little Theorem?

- a) $a^p \equiv 1 \pmod{p}$ for any prime p and integer a
- b) $p^a \equiv 1 \pmod{a}$
- c) $a^p \equiv p \pmod{a}$
- d) $p^a \equiv a \pmod{p}$

Answer: a) $a^p \equiv 1 \pmod{p}$

6.

Euler's Theorem is a generalization of:

- a) Fermat's Little Theorem
- b) Chinese Remainder Theorem
- c) Modular Inverse Theorem
- d) Lagrange's Theorem

Answer: a) Fermat's Little Theorem

7.

According to Shannon, a good cipher should exhibit:

- a) High confusion and low diffusion
- b) High diffusion and low confusion
- c) High confusion and high diffusion
- d) Low confusion and low diffusion

Answer: c) High confusion and high diffusion

8.

Which cipher rearranges the order of characters without changing them?

- a) Substitution cipher
- b) Transposition cipher
- c) Affine cipher
- d) Vigenere cipher

Answer: b) Transposition cipher

9.

The Caesar cipher is an example of:

- a) Substitution cipher
- b) Transposition cipher
- c) Block cipher
- d) Stream cipher

Answer: a) Substitution cipher

10.

The Affine cipher uses which two mathematical operations?

- a) Addition and Division
- b) Multiplication and Division
- c) Multiplication and Addition
- d) Addition and Subtraction

Answer: c) Multiplication and Addition

11.

In the Vigenère cipher, the keyword is:

- a) Numeric
- b) Alphabetic
- c) Alphanumeric
- d) Random

Answer: b) Alphabetic

Set 1

Match the following:

Left Side	Right Side
Prime Number Generation	Fundamental for cryptography
Random Number Generation	Needed for keys and nonces
Linear Congruences	Equations in modular arithmetic

Answer Set 1:

- Prime Number Generation → Fundamental for cryptography (Used in RSA, etc.)
 - Random Number Generation → Needed for keys and nonces (Secure randomness)
 - Linear Congruences → Equations in modular arithmetic (e.g., $ax \equiv b \pmod{n}$)
-

Set 2

Match the following:

Left Side	Right Side
Chinese Remainder Theorem	Solves multiple congruences simultaneously
Fermat's Little Theorem	Basis for primality testing
Euler's Theorem	Generalizes Fermat's Little Theorem

Answer Set 2:

- Chinese Remainder Theorem → Solves multiple congruences simultaneously (CRT technique)
 - Fermat's Little Theorem → Basis for primality testing (If p is prime, then $a^{(p-1)} \equiv 1 \pmod{p}$)
 - Euler's Theorem → Generalizes Fermat's Little Theorem (Uses Euler's totient function)
-

Set 3

Match the following:

Left Side	Right Side
Encryption	Converting plaintext to ciphertext
Decryption	Recovering original message
Confusion and Diffusion	Concepts for strong cipher design

Answer Set 3:

- Encryption → Converting plaintext to ciphertext (Scrambling information)
 - Decryption → Recovering original message (Reverse process)
 - Confusion and Diffusion → Concepts for strong cipher design (Confusion hides relation to key, diffusion spreads plaintext influence)
-

Set 4

Match the following:

Left Side	Right Side
Caesar Cipher	Simple additive cipher
Affine Cipher	Uses both multiplication and addition
Vigenère Cipher	Polyalphabetic cipher

Answer Set 4:

- Caesar Cipher → Simple additive cipher (Shift letters)
- Affine Cipher → Uses both multiplication and addition ($ax + b \bmod 26$)
- Vigenère Cipher → Polyalphabetic cipher (Keyword-based shifting)