

LBC error detection and correction

Error detection and correction Capability of Linear Block Code

Step-1 - Identify d_{\min} [minimum Hamming distance]

Error detection Capability of Linear block code

$$\Rightarrow d_{\min} \geq s + 1$$

→ where, s = error detection capacity

Error Correction Capability of Linear block code

$$\Rightarrow d_{\min} \geq 2t + 1$$

→ where, t = error correction capacity

- If minimum hamming dist.ⁿ of Linear block code is 3.
Find LBC code ~~dist~~ detection & correction capability.

→ $d_{\min} = 3$

→ for error detection

$$\Rightarrow d_{\min} \geq s + 1$$

$$\Rightarrow 3 \geq s + 1$$

$$\Rightarrow 2 \geq s$$

$$\Rightarrow s \leq 2$$

→

- If minimum hamming dist.ⁿ of Linear block code is 3.

Find LBC code ~~dist.~~ detection & correction capability.

→ $d_{\min} = 3$

→ for error detection

$$\Rightarrow d_{\min} \geq s + 1$$

$$\Rightarrow 3 \geq s + 1$$

$$\Rightarrow 2 \geq s$$

$$\Rightarrow s \leq 2$$

→ this code can detect 2 bit error.

→ For error correction

- If min hamming dist. of 2 errors
Find the code detection & correction capability.

$$\rightarrow d_{\min} = 3$$

\rightarrow for error detection

$$\Rightarrow d_{\min} \geq s + 1$$

$$\Rightarrow 3 \geq s + 1$$

$$\Rightarrow 2 \geq s$$

$$\Rightarrow s \leq 2$$

\rightarrow this code can detect 2 bit errors.

\rightarrow for error correction

$$\Rightarrow d_{\min} \geq 2t + 1$$

$$\Rightarrow 3 \geq 2t + 1$$

$$\Rightarrow 2 \geq 2t$$

$$\Rightarrow t \leq 1$$

\rightarrow this code can correct 1 bit error

Error syndromes and Error correction

Error Syndromes in Linear block Codes with Example.

- If Received Codeword is $[Y]$
- then error syndromes

$$[S] = [Y][H^T]$$

- Here, Received Codeword $[Y]$

$$[Y] = [C] + [e]$$

where, $[C]$ = Codeword

$[e]$ = error

- If error $[e] = 0$, $[Y] = [C]$

Error Syndromes in Linear block Codes with Example.

- If Received Codeword is $[Y]$
- then error syndromes

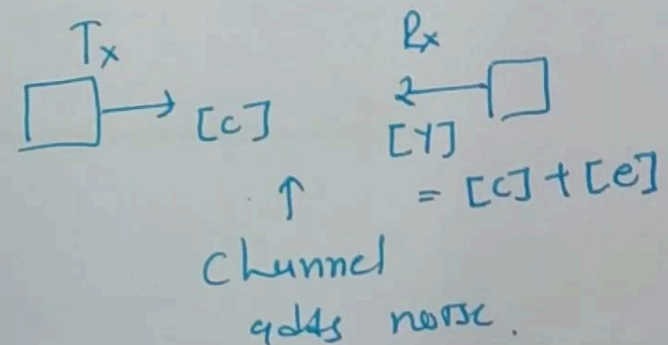
$$[S] = [Y][H^T]$$

- If Received Codeword $[Y]$

$$[Y] = [C] + [e]$$

where $[C]$ is Codeword

and $[e]$ is error



Find the error syndromes of $V_1 = (1101101)$, for

$$H^T = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

, where V is received codeword.
also calculate the error bit

→ Rec

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\rightarrow [S] = [V_1][H^T]$$

$$= \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$

Input A	Input B	Output
0	0	0
0	1	1
1	0	1
1	1	0

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\rightarrow [S] = [V_1][H^T]$$

$$= \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\rightarrow [S] = [V_1][H^T]$$

$$= \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$y = [1101101]$$

$$e_2 [0000100]$$

$$X = \gamma + e$$

$$2 \quad [1 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1]$$

$$\rightarrow [S] = [V_1][H^T]$$

$$= [1 \ 1 \ 0 \ 1 \ 0 \ 1]$$

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$$= [1 \ 0 \ 0]$$

$$\begin{bmatrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$