

Standard form of alternating quantity

$$\text{Angular velocity} = \frac{\theta}{T}$$

$$\omega = \frac{2\pi}{T}$$

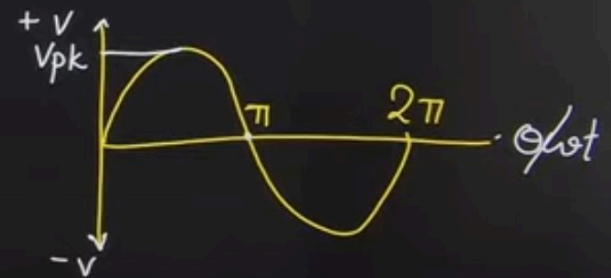
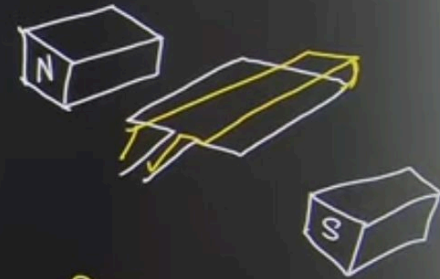
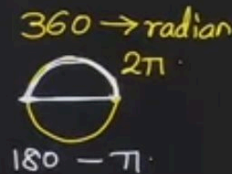
Put $1/T = f$ $\omega = 2\pi f$

$$v(\theta) = V_{pk} \sin \theta$$

$$v = V_m \sin \theta$$

$$v = V_m \sin \omega t \quad \theta = \omega t$$

$$v = V_m \sin 2\pi f t \quad \omega = 2\pi f$$



Angular velocity 026 624

$$\omega = \frac{2\pi}{T}$$

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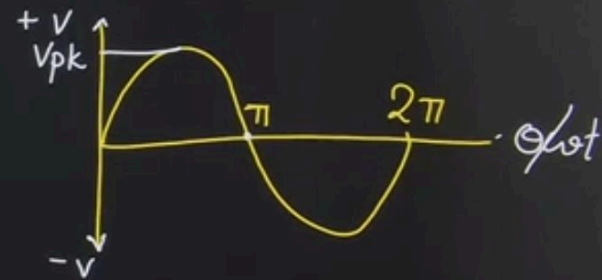
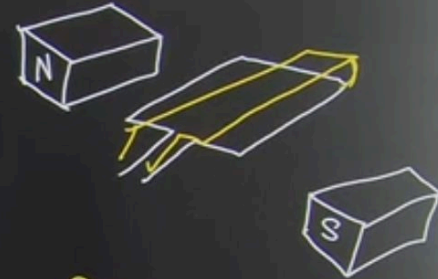
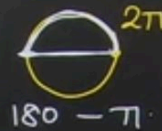
$$v = V_m \sin \theta$$

$$v = V_m \sin \omega t \quad \theta = \omega t$$

$$v = V_m \sin 2\pi f \cdot t \quad \omega = 2\pi f$$

$$v = V_m \sin \frac{2\pi}{T} \cdot t$$

360 \rightarrow radian



Standard form of alternating voltage.

$$v(\theta) = V_{pk} \sin \theta$$

$$v = V_m \sin \theta$$

$$v = V_m \sin \omega t \quad \theta = \omega t$$

$$v = V_m \sin 2\pi f \cdot t \quad \omega = 2\pi f$$

$$v = V_m \sin \frac{2\pi}{T} \cdot t$$

Standard form of alternating current.

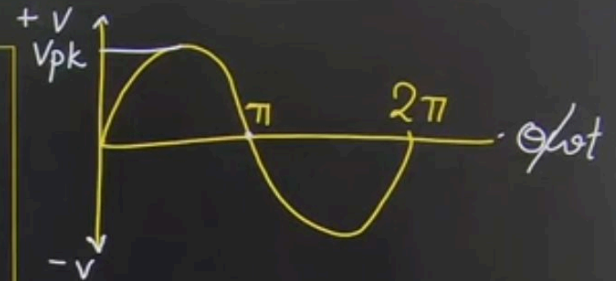
$$i(\theta) = I_{pk} \sin \theta$$

$$i = I_m \sin \theta$$

$$i = I_m \sin \omega t \quad \theta = \omega t$$

$$i = I_m \sin 2\pi f \cdot t \quad \omega = 2\pi f$$

$$i = I_m \sin \frac{2\pi}{T} \cdot t \quad f = \frac{1}{T}$$



Standard form of alternating voltage.

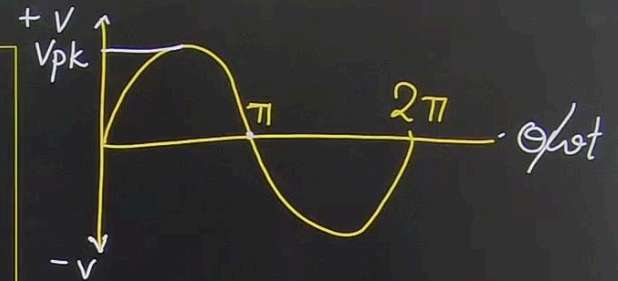
$$v(\theta) = V_{pk} \sin \theta$$

$$v = V_m \sin \theta$$

$$v = V_m \sin \omega t \quad \theta = \omega t$$

$$v = V_m \sin 2\pi f \cdot t \quad \omega = 2\pi f$$

$$v = V_m \sin \frac{2\pi}{T} \cdot t$$



Standard form of alternating current.

$$i(\theta) = I_{pk} \sin \theta$$

$$i = I_m \sin \theta \quad \text{degree}$$

$$i = I_m \sin \omega t \quad \theta = \omega t \text{ [radian]}$$

$$i = I_m \sin 2\pi f \cdot t \quad \omega = 2\pi f$$

$$i = I_m \sin \frac{2\pi}{T} \cdot t \quad f = \frac{1}{T}$$

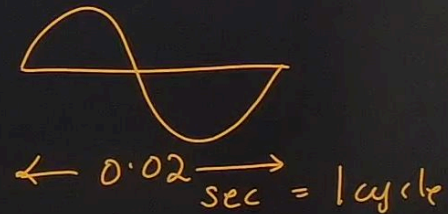
An alternating current i is given by $i = 141.4 \sin 314t$. Find
 i) the maximum value ii) the frequency iii) The time period
 iv) The instantaneous value when time is 3 msec.

Compare $i = 141.4 \sin 314t$ with standard form
 $i = I_m \sin \omega t$

The maximum value is $(I_m) = 141.4 \text{ A}$.

$$\text{Frequency} = \frac{\omega}{2\pi} = \frac{314}{2 \times \pi} = 49.97 = 50 \text{ Hz}$$

$$\text{Time period (T)} = \frac{1}{f} = \frac{1}{50} = 0.02 \text{ sec}$$



1 sec = 50 cycles

- i) the maximum value 550.912 ii) the frequency iii) The time period
iv) The instantaneous value when time is 3 msec.

Compare $i = 141.4 \sin 314t$ with standard form
 $i = I_m \sin \omega t$

The maximum value is $(I_m) = 141.4 \text{ A}$.

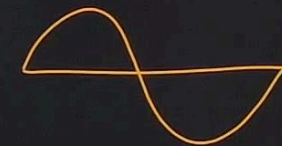
$$\text{Frequency} = \frac{\omega}{2\pi} = \frac{314}{2 \times \pi} = 49.97 = 50 \text{ Hz}$$

$$\text{Time period (T)} = \frac{1}{f} = \frac{1}{50} = 0.02 \text{ sec}$$

Instantaneous value at $t = 3 \times 10^{-3} \text{ sec}$.

$$i = 141.4 \sin \left[314 \times 3 \times 10^{-3} \times \frac{180}{\pi} \right]$$

$$\boxed{i = 114.35 \text{ A}}$$



$\leftarrow 0.02 \text{ sec} = 1 \text{ cycle}$

1 sec = 50 cycles

degree $= x \frac{\pi}{180}$ radian

radian $= x \frac{180}{\pi}$ degree

$$0.02 = \frac{1}{x}$$

$$x = \frac{1}{0.02}$$

$$= 50$$

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An alternating current of frequency 60 Hz has a maximum value of 12 A.
 i) Write down the equation of the instantaneous value,
 ii) find the ^{value} of current after $\frac{1}{360}$ sec. and $i = I_m \sin \omega t$.
 iii) find the time taken to reach 9.6 A for the first time

Given: $f = 60 \text{ Hz}$, $I_m = 12 \text{ A}$, $i = 9.6 \text{ A}$ in III case.

i) Instantaneous value: $i = I_m \sin \omega t$

$$\omega = 2\pi f = 2 \times \pi \times 60 = 376.99 = 377 \text{ rad/sec.}$$

$$i = 12 \sin 377 t$$

ii) Value of current (i) at $t = \frac{1}{360}$ sec.

$$i = 12 \sin \left[377 \times \frac{1}{360} \times \frac{180}{\pi} \right]^\circ$$

$$i = 10.39 \text{ A}$$

iii) $i = 9.6 \text{ A}$ t.

$$i = I_m \sin \omega t$$

$$9.6 = 12 \sin 377 t$$

$$\frac{9.6}{12} = \sin 377 t$$

$$0.8 = \sin 377 t$$

$$0.8 = \sin \left(377 \times t \times \frac{180}{\pi} \right)^\circ$$

$$\sin^{-1}(0.8) = 377 t \times \frac{180}{\pi}$$

$$53.13 = \frac{377 \times 180}{\pi} t$$

$$53.13 = 21600.5 t$$

$$t = \frac{53.13}{21600.5}$$

$$t = 2.45 \times 10^{-3}$$

$$t = 2.45 \text{ msec.}$$