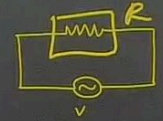


Fundamental AC circuit:

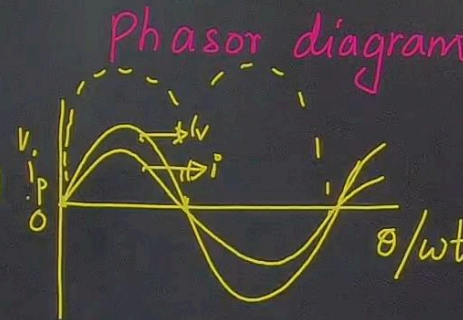
- ① AC through pure resistance
- ② AC through pure inductance
- ③ AC through pure capacitance

AC Circuit Containing resistance only.



Voltage $V = V_m \sin(\omega t + \phi)$

Current $i = I_m \sin(\omega t + \phi)$



Scale $1\text{cm} = 3\text{V}$.

24V
 $\xrightarrow{8\text{cm}} V$

$\xrightarrow{I} V$

power $P = V \times I$.

$V = \frac{V_m}{\sqrt{2}} \quad I = \frac{I_m}{\sqrt{2}}$

Impedance $(Z) = \frac{V}{I} = R$

$Z = R$

Phase Angle

$\phi = 0$

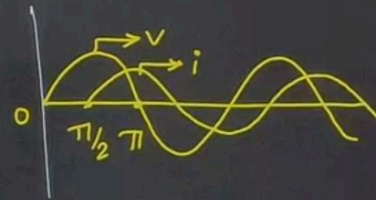
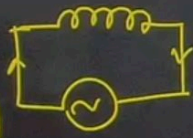
$p.f = \cos \phi = \cos 0 = 1 \text{ (Unity)}.$

Thus V & I are in phase.

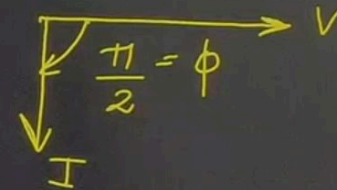
AC Circuit containing pure Inductance only (Unit Henry H)

Voltage $v = V_m \sin \omega t$

$$i = I_m \sin(\omega t - \frac{\pi}{2})$$



Phasor Diagram



Impedance (Z)

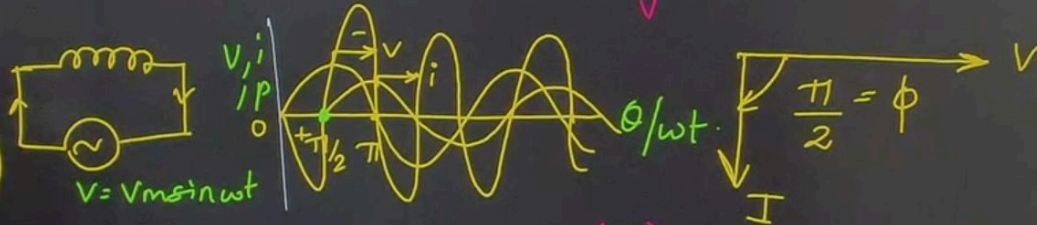
angle

AC Circuit containing pure Inductance only (Unit Henry H)

Voltage $V = V_m \sin \omega t$

Phasor Diagram

Current $i = I_m \sin(\omega t - \frac{\pi}{2})$



Power $P = 0$

Impedance (Z) $= \frac{V}{I} = \omega L$

In Inductive circuit current lags Voltage by $\pi/2$.

Phase angle $\phi = -\frac{\pi}{2}$

$p.f = \cos \phi = \cos \pi/2 = 0$

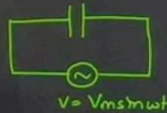
$Z = \omega L \Omega$

$X_L = \omega L \Omega$

$X_L = 2\pi f L \Omega$

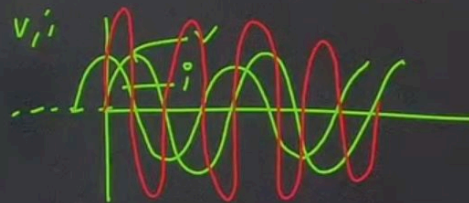
AC Circuit containing pure Capacitance (Unit farad F)

Voltage $V = V_m \sin \omega t$



Current $i = I_m \sin(\omega t + \frac{\pi}{2})$

Phasor diagram



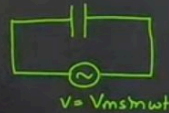
Impedance (Z)

Power $P = 0$

Phase angle

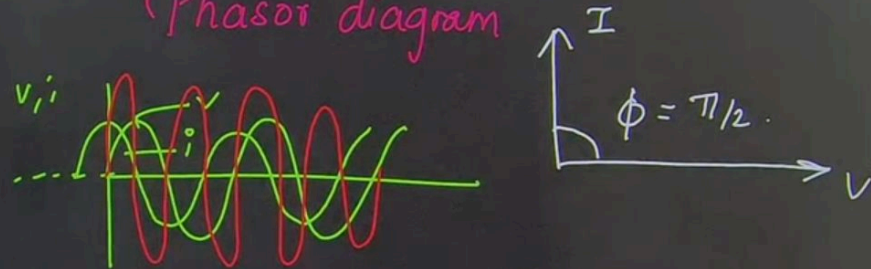
AC Circuit containing pure Capacitance (Unit farad F)

Voltage $V = V_m \sin \omega t$



Current $i = I_m \sin(\omega t + \frac{\pi}{2})$

Phasor diagram



Power $P = 0$

In capacitive circuit I leads V by $\pi/2$.

Phase angle $\phi = \pi/2$

$$P_f = \cos \phi = 0$$

$$\text{Impedance (Z)} = \frac{V}{I} = \frac{1}{\omega C}$$

$$Z = \frac{1}{\omega C}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

Q. A $318 \mu\text{F}$ capacitor is connected across a 230V , 50Hz system.

① Determine capacitive reactance ② RMS value of current & equation of V & I

$$C = 318 \mu\text{F} = 318 \times 10^{-6} \text{ F.}$$

$$V = 230\text{V}$$

$$f = 50\text{Hz.}$$

$$X_c$$

$$I_m, V_m.$$

$$V =$$

$$i =$$

$$\textcircled{1} X_c = \frac{1}{2\pi f \cdot C} = \frac{1}{2 \times \pi \times 50 \times 318 \times 10^{-6}} \\ = \underline{10 \Omega}.$$

②

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$$\text{② } \frac{V}{I} = Z = \frac{1}{\omega C} = X_c \\ \frac{V}{I} = X_c$$



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① Determine capacitive reactance ② RMS value of current & equation of V & I .

$$C = 318 \mu\text{F} = 318 \times 10^{-6} \text{ F.}$$

$$V = 230\text{V}$$

$$f = 50\text{ Hz.}$$

$$\textcircled{1} X_c = \frac{1}{2\pi f \cdot C} = \frac{1}{2 \times \pi \times 50 \times 318 \times 10^{-6}}$$

$$= 10 \Omega$$

$$\omega = 2\pi f$$

$$= 2 \times \pi \times 50$$

$$= 314 \text{ rad/s}$$

$$X_c$$

$$I_m, V_m$$

$$V =$$

$$i =$$

$$\textcircled{II} \frac{V}{I} = X_c$$

$$I = \frac{230}{10} = 23\text{ A.}$$

$$I_m = I \times \sqrt{2} = 32.53\text{ A.}$$

$$V_m = \sqrt{2} \times V$$

$$= \sqrt{2} \times 230$$

$$= 325.27\text{ V.}$$

$$V = V_m \sin \omega t$$

$$V = 325.27 \sin 314t$$

$$i = I_m \sin \omega t + \frac{\pi}{2}$$

$$i = 32.53 \sin 314t + \frac{\pi}{2}$$

A 10 mH inductor has a current of $i = 5 \cos(2000)t$ A. Obtain the voltage V_L across it.

$$L = 10 \text{ mH} = 10 \times 10^{-3} \text{ H.}$$

$$i = 5 \cos(2000t)$$

$$= 5 \sin\left(2000t + \frac{\pi}{2}\right)$$

$$i = I_m \sin\left(\omega t + \frac{\pi}{2}\right)$$

$$\omega = 2000$$

$$I_m = 5$$

$$I = \frac{I_m}{\sqrt{2}} = \frac{5}{\sqrt{2}} = 3.54 \text{ A.}$$

$$\frac{V}{I} = X_L$$

$$V = I \cdot X_L$$

$$= I \cdot \omega L$$

$$= 3.54 \times 2000 \times 10 \times 10^{-3}$$

$$\boxed{V = 70.8 \text{ V.}}$$

A 10 mH inductor has a current of $i = 5 \cos(2000)t$ A. Obtain the voltage V_L across it.

$$L = 10 \text{ mH} = 10 \times 10^{-3} \text{ H}$$

$$i = 5 \cos(2000t)$$

$$= 5 \sin\left(2000t + \frac{\pi}{2}\right)$$

$$i = I_m \sin\left(\omega t + \frac{\pi}{2}\right)$$

$$\omega = 2000$$

$$I_m = 5$$

$$I = \frac{I_m}{\sqrt{2}} = \frac{5}{\sqrt{2}} = 3.54 \text{ A}$$

$$\frac{V}{I} = X_L$$

$$V = I \cdot X_L$$

$$= I \cdot \omega L$$

$$= 3.54 \times 2000 \times 10 \times 10^{-3}$$

$$V = 70.8 \text{ V}$$

$$V_m = V \times \sqrt{2}$$

$$= 70.8 \times \sqrt{2}$$

$$V = 70.8 \times \sqrt{2} \cdot \sin\left(2000t + \frac{\pi}{2}\right)$$

$$L = 10 \text{ sec}$$