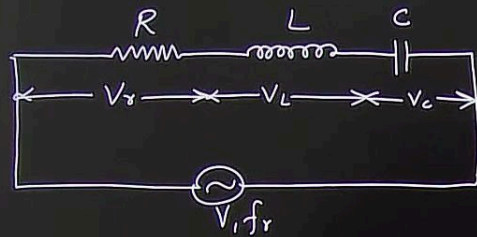
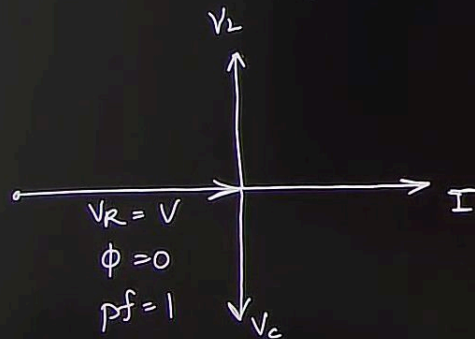


Series Resonance



Circuit diagram



Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi f L \Omega$$

$$X_C = \frac{1}{2\pi f C} \Omega$$

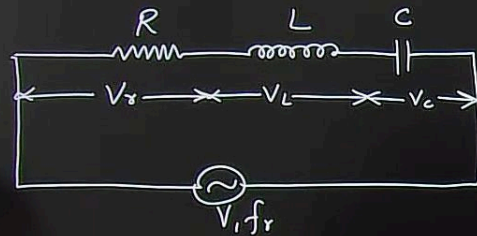
$$pf = 1, \phi = 0$$

$$X_L - X_C = 0$$

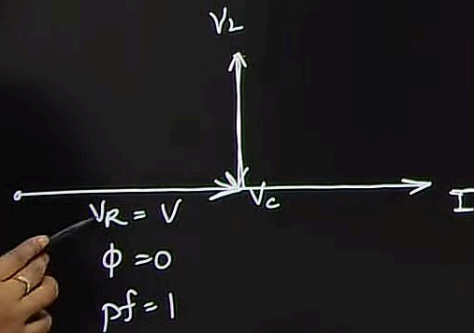
$$X_L = X_C$$

Here the frequency is
termed as resonance frequency

Series Resonance



Circuit diagram



Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi f L \Omega$$

$$X_C = \frac{1}{2\pi f C} \Omega$$

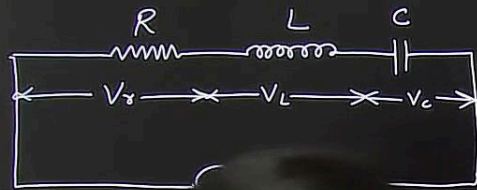
$$pf = 1, \phi = 0$$

$$X_L - X_C = 0$$

$$X_L = X_C$$

Here the frequency is
termed as resonance frequency

Series Resonance



$$Z = R + X_j$$

$$X_L = X_C$$

$$2\pi f_r L = \frac{1}{2\pi f_r C}$$

$$f_r \cdot f_r = \frac{1}{(2\pi)^2 \cdot L \cdot C}$$

$$f_r^2 = \frac{1}{2\pi^2 \cdot L \cdot C}$$

$$\sqrt{f_r^2} = \sqrt{\frac{1}{(2\pi)^2 \cdot L \cdot C}}$$

$$f_r = \frac{1}{2\pi \sqrt{LC}}$$

Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi f L \Omega$$

$$X_C = \frac{1}{2\pi f C} \Omega$$

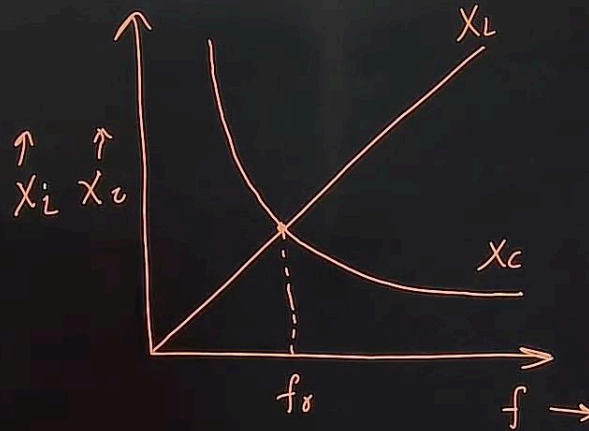
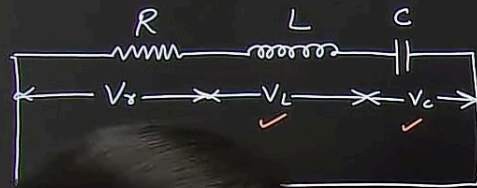
$$pf = 1, \phi = 0$$

$$X_L - X_C = 0$$

$$\underline{X_L = X_C}$$

Here the frequency is termed as resonance frequency

Series Resonance



$$Z = R$$

Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi fL \Omega$$

$$X_C = \frac{1}{2\pi fC} \Omega$$

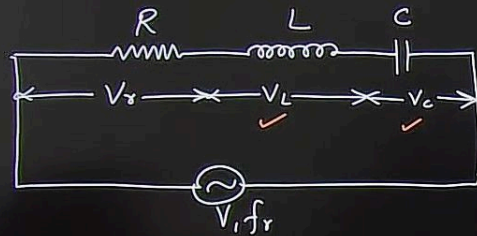
$$pf = 1, \phi = 0$$

$$X_L - X_C = 0$$

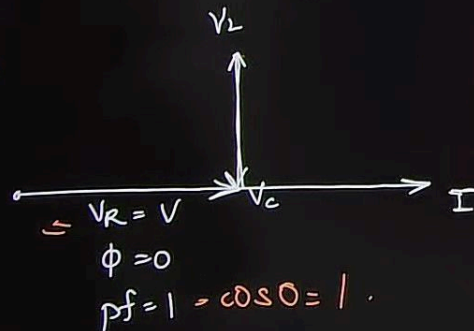
$$\frac{X_L = X_C}{f_r = \frac{1}{2\pi\sqrt{LC}}}$$

Here the frequency is
termed as resonance frequency

Series Resonance



Circuit diagram



Q-factor

$$Q = \frac{V_L \text{ or } V_C}{V}$$

$$= \frac{I \cdot X_L}{I R}$$

$$Q = \frac{\omega L}{R}$$

$$Q = \frac{2\pi f_r \cdot L}{R}$$

$$Q = \frac{2\pi L}{R} \cdot \frac{1}{2\pi\sqrt{LC}}$$

$$Q = \frac{L}{R} \cdot \frac{1}{\sqrt{LC}} = \frac{\cancel{\sqrt{L}} \times \sqrt{L}}{R \cdot \cancel{\sqrt{L}} \cdot \sqrt{C}}$$

$$Q = \frac{1}{R} \cdot \frac{\sqrt{L}}{\sqrt{C}}$$

Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi f L \Omega$$

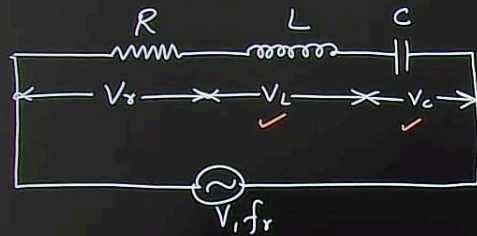
$$X_C = \frac{1}{2\pi f C} \Omega$$

$$pf = 1, \phi = 0$$

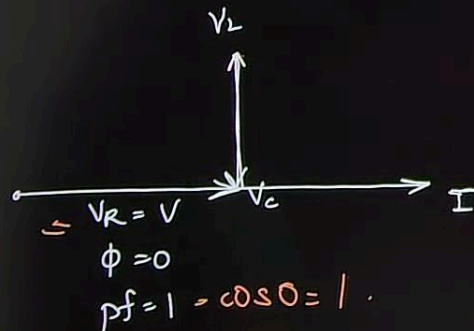
$$\begin{matrix} X_L - X_C = 0 \\ X_L = X_C \end{matrix} \left| \begin{matrix} f_r = \frac{1}{2\pi \sqrt{LC}} \end{matrix} \right.$$

Here the frequency is termed as resonance frequency

Series Resonance



Circuit diagram



To find Voltage drop.

$$V_L = I_r \cdot X_L \xrightarrow{\omega L} 2\pi f L$$

$$= \frac{V}{R} \cdot 2\pi \cdot \frac{1}{2\pi\sqrt{LC}} \cdot L$$

$$V_L = \frac{V}{R} \cdot \frac{\sqrt{L}}{\sqrt{C}}$$

$$V_L = \frac{V}{R} \cdot \sqrt{\frac{L}{C}}$$

$$\frac{\sqrt{L} \cdot \sqrt{L}}{\sqrt{L} \cdot \sqrt{C}} = \frac{\sqrt{L}}{\sqrt{C}}$$

Imp points

$$X = (X_L - X_C) \Omega$$

$$X_L = 2\pi f L \Omega$$

$$X_C = \frac{1}{2\pi f C} \Omega$$

$$pf = 1, \phi = 0$$

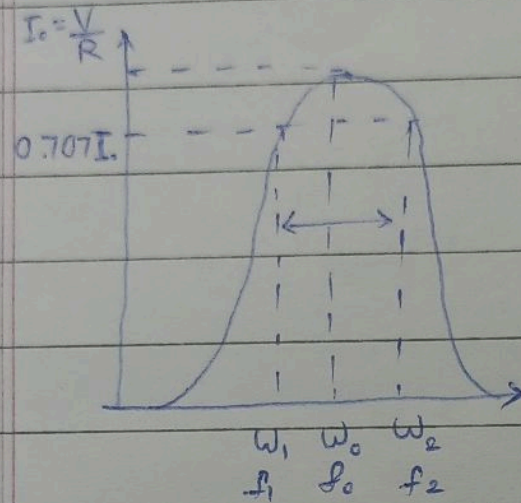
$$X_L - X_C = 0 \quad \left| \begin{array}{l} f_r = \frac{1}{2\pi\sqrt{LC}} \\ X_L = X_C \end{array} \right.$$

Here the frequency is termed as resonance frequency



$$f_r = \underline{Q_{factor} \times Bandwidth}.$$

* Bandwidth



$$\text{Bandwidth} = \omega_2 - \omega_1$$

$I_0 \rightarrow$ Max current at Resonance

$$I = I_0 / \sqrt{2} \quad \text{or} \quad 0.707 I_0$$

$$P = VI \cos \phi$$

At Resonance

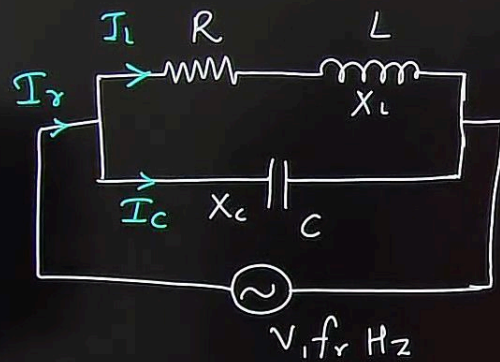
$$P_0 = I_0^2 R$$

$$\text{for } I_0 / \sqrt{2} = I,$$

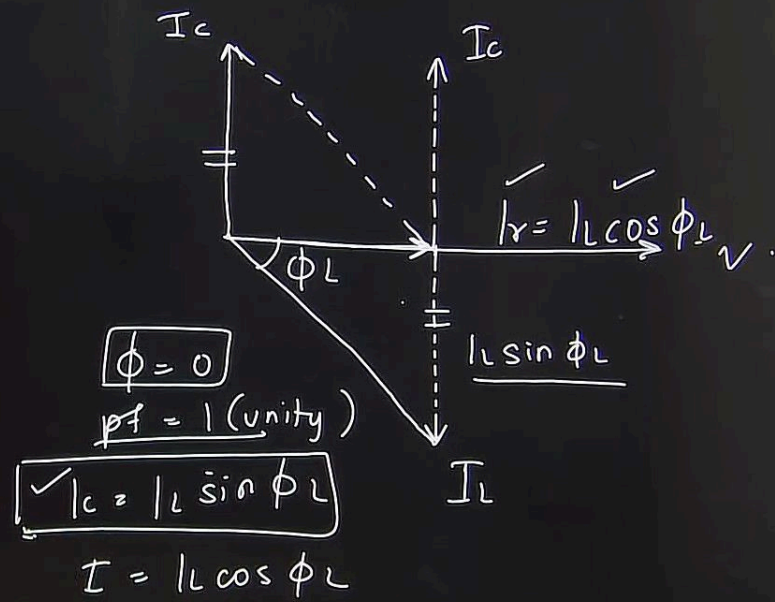
$$P_0 = \frac{I_0^2 R}{2} = \frac{P_0}{2}$$

f_1 & $f_2 \rightarrow$ also called Half Power points.

Parallel Resonance

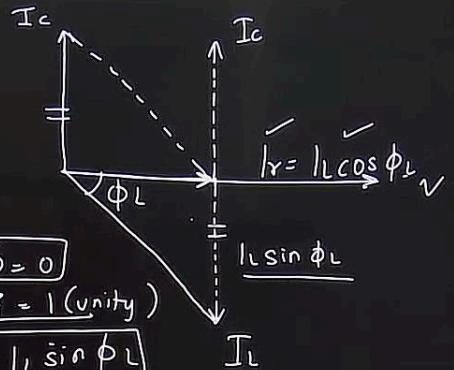
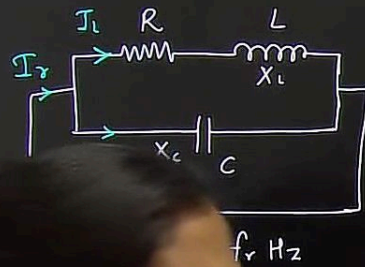


a) Circuit diagram



b) Phasor diagram

Parallel Resonance



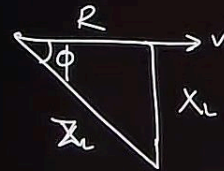
$$\phi = 0$$

$$pf = 1 \text{ (unity)}$$

$$I_C = I_L \sin \phi_L$$

$$I = I_L \cos \phi_L$$

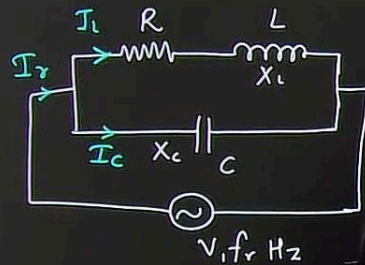
b) Phasor diagram



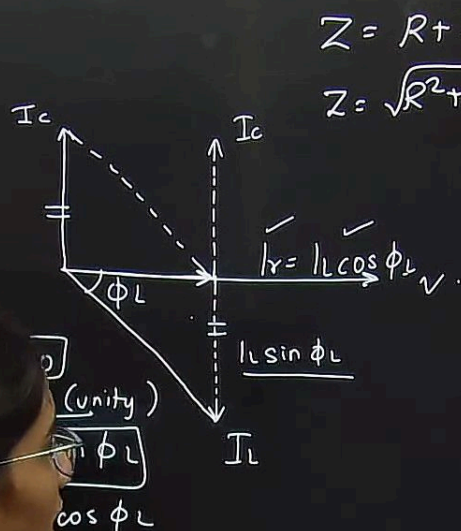
$$I_C = I_L \sin \phi_L$$

$$\frac{V}{X_C} = \frac{V}{Z_L} \cdot \frac{X_L}{Z_L}$$

Parallel Resonance



a) Circuit diagram



b) Phasor diagram

$$Z = R + jX_L$$

$$Z = \sqrt{R^2 + X_L^2}$$

$$I_C = I_L \sin \phi_L$$

$$\frac{V}{X_C} = \frac{V}{Z_L} \cdot \frac{X_L}{Z_L}$$

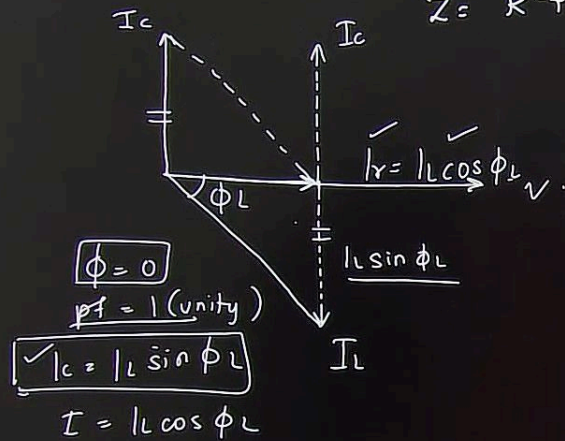
$$Z_L^2 = X_L \cdot X_C$$

$$Z_L^2 = \omega L \cdot \frac{1}{\omega C}$$

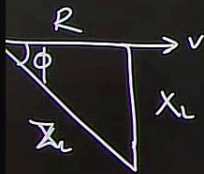
$$Z_L^2 = \frac{L}{C}$$

$$Z = R + Xj$$

$$Z^2 = R^2 + X^2$$



b) Phasor diagram



$$I_C = I_L \sin \phi_L$$

$$\frac{V}{X_C} = \frac{V}{Z_L} \cdot \frac{X_L}{Z_L}$$

$$Z_L^2 = X_L \cdot X_C$$

$$Z_L^2 = \cancel{\omega L} \cdot \frac{1}{\cancel{\omega C}}$$

$$Z_L^2 = \frac{L}{C}$$

$$R^2 + X_L^2 = \frac{L}{C}$$

$$R^2 + (2\pi f_r L)^2 = \frac{L}{C}$$

$$(2\pi f_r L)^2 = \frac{L}{C} - R^2$$

Square root.

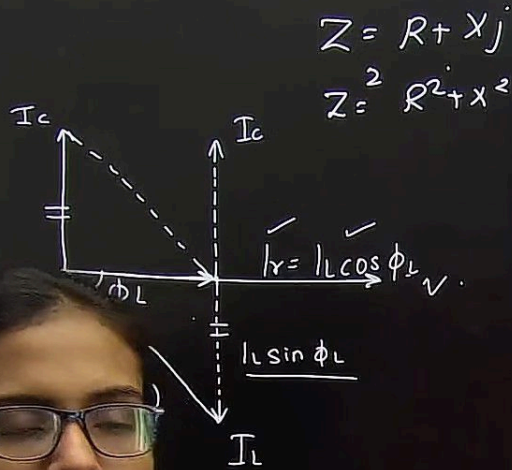
$$2\pi f_r L = \sqrt{\frac{L}{C} - R^2}$$

$$f_r = \frac{1}{2\pi L} \sqrt{\frac{L}{C} - R^2}$$

$$= \frac{1}{2\pi} \sqrt{\frac{L}{L^2 C} - \frac{R^2}{L^2}}$$

$$f_r = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$$





$$I = I_c \cos \phi_L$$

$$\frac{V}{Z_r} = \frac{V}{Z_L} \cdot \frac{R}{Z_L}$$

$$\frac{1}{Z_r} = \frac{R}{Z_L^2}$$

$$Z_L^2 = \frac{L}{C}$$

$$Z_r = \frac{Z_L^2}{R}$$

$$Z_r = \frac{L}{R C} \Omega$$

$$Q = \frac{I_L \text{ or } I_c}{I} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$(2\pi f_r L)^2 = \frac{L}{C} - R^2$$

Square root.

$$2\pi f_r L = \sqrt{\frac{L}{C} - R^2}$$

$$f_r = \frac{1}{2\pi L} \sqrt{\frac{L}{C} - R^2}$$

$$= \frac{1}{2\pi} \sqrt{\frac{L}{L^2 C} - \frac{R^2}{L^2}}$$

$$f_r = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$$

Comparison between series and parallel resonance

550 912

Particular

Series circuit

Parallel Circuit

1. Impedance at resonance

Minimum ($Z_r = R$) $X = 0$
Voltage drop

Maximum $Z_r = \frac{L}{CR}$

2. Current at resonance

Maximum ($I_r = \frac{V}{R}$) $\frac{V}{R} \sqrt{\frac{L}{C}}$

Minimum $I_r = \frac{V}{Z_r}$

3. Resonant frequency

$$f_r = \frac{1}{2\pi\sqrt{LC}} \text{ Hz}$$

$$f_r = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}}$$

4. Q-Factor

$$Q = \frac{V_L \text{ or } V_C}{V} = \frac{1}{R} \sqrt{\frac{L}{C}}$$

$$Q = \frac{I_L \text{ or } I_C}{I}$$

5. It magnifies

Voltage

Current

6. When $f < f_r$

Circuit is capacitive

Circuit is inductive

7. When $f > f_r$

Circuit is Inductive

Circuit is capacitive

Q. A parallel circuit consists of a $2.5 \mu\text{F}$ capacitor and a coil whose resistance and inductance are 15Ω & 260 mH . Determine the resonant frequency, Q factor of the circuit at resonance & dynamic impedance.

Given data: $C = 2.5 \times 10^{-6} \text{ F}$
 $R = 15 \Omega$
 $L = 260 \times 10^{-3} \text{ H}$

$$\text{Resonant frequency} = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{L^2}} = \frac{1}{2\pi} \sqrt{\frac{1}{260 \times 10^{-3} \times 2.5 \times 10^{-6}} - \frac{(15)^2}{(260 \times 10^{-3})^2}}$$

$$\text{Q factor} = \frac{1}{R} \sqrt{\frac{L}{C}} = \frac{1}{15} \sqrt{\frac{260 \times 10^{-3}}{2.5 \times 10^{-6}}} = 21.49$$

$$\text{Dynamic Impedance } Z = \frac{L}{CR} = \frac{260 \times 10^{-3}}{2.5 \times 10^{-6} \times 15} = 6933.33 \Omega$$