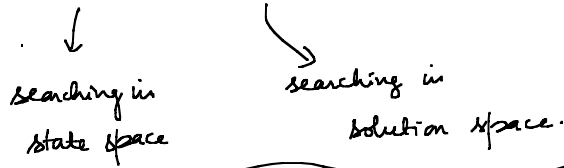


04/02/2022

Local Search

Path V/S State optimization.



Satisfaction

V/S

Optimization.

Goal satisfaction

Reach the goal node.

Constraint satisfaction.

Optimize. (function cost)

Constraint optimization.

Goal states:

Constraints:

$$\begin{cases} \text{for } i: f(n_i) \geq C^* \\ C_1, C_2, \dots, C_n \end{cases}$$

8-Queens problem

8x8 chessboard

Place 8 queens

such that no two queens can attack each other.

Convert

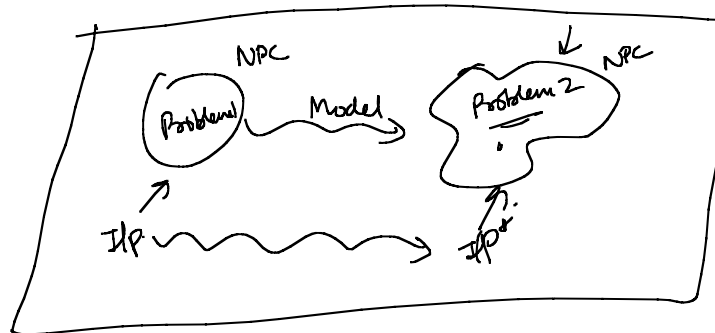
Minimize
Objective funcⁿ = # constraints not satisfied.

Constraints:

C_1, C_2, \dots, C_n

↓
 $f(n)$ reaches 0

Max $f(n)$
s.t. C_1
 C_2
 C_n



Local Search

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 18 | 12 | 14 | 13 | 13 | 12 | 14 | 14 |
| 14 | 16 | 13 | 15 | 12 | 14 | 12 | 16 |
| 14 | 12 | 18 | 13 | 15 | 12 | 14 | 14 |
| 15 | 14 | 14 | 14 | 13 | 16 | 13 | 16 |
| 14 | 17 | 15 | 14 | 16 | 16 | 16 | 16 |
| 17 | 16 | 18 | 15 | 15 | 15 | 15 | 15 |
| 18 | 14 | 15 | 15 | 14 | 16 | 16 | 16 |
| 14 | 14 | 13 | 17 | 12 | 14 | 12 | 18 |

$f = 17$

- ↳ keep track of single current state.
- ↳ move only to neighboring state
- ↳ Ignore paths.

Adv:- use very little memory.
= can often find reasonable solⁿ in even large or infinite state space.

Constraints:- Exactly one queen in each column.

Objective funcⁿ:- Number of pairs of queens that are attacking each other. $\Rightarrow f$.
(minimize)

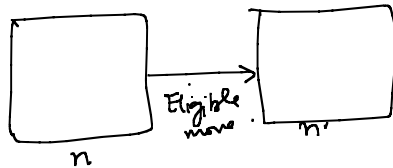
Search Space

State:- All 8 queens on the board in some configuration.

of possible states = 8^8

Min. $f(n)$: # pairs of queens in attacking position.

Neighborhood / Successor funcⁿ :- Move a single queen to any



neighbors
= 56
(7×8)

other position in the same column.

all move queens one position in

neighbors
8 to 16

same column.

Goal.



balance

A good neighbor funcⁿ.

Hill Climbing