

↗ filter = (3x3)

STRIDE

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

↘ image = (6x6), stride = 1

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

stride = 2 → window

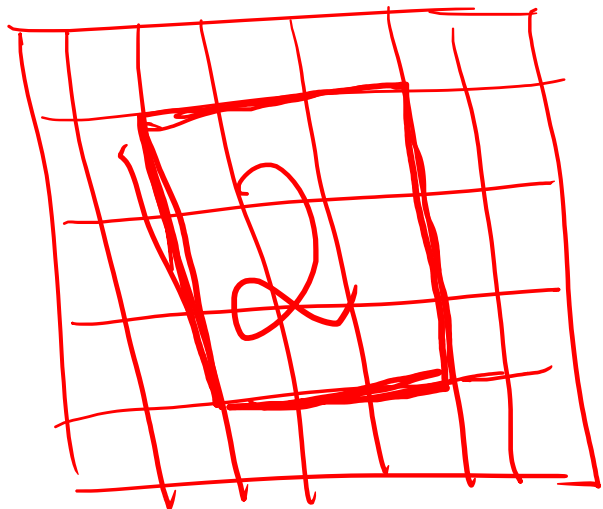
1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

This type of convolution is called as strided convolution.



0	0	0	0	0	0	0	0
0	4	5	8	9	2	2	0
0	6	5	1	3	6	5	0
0	1	7	1	0	4	1	0
0	4	2	8	9	2	8	0
0	4	6	1	4	9	7	0
0	1	3	5	6	7	6	0
0	0	0	0	0	0	0	0

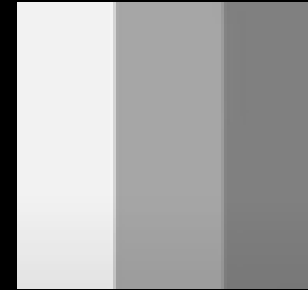
# Max-pooling (layer)

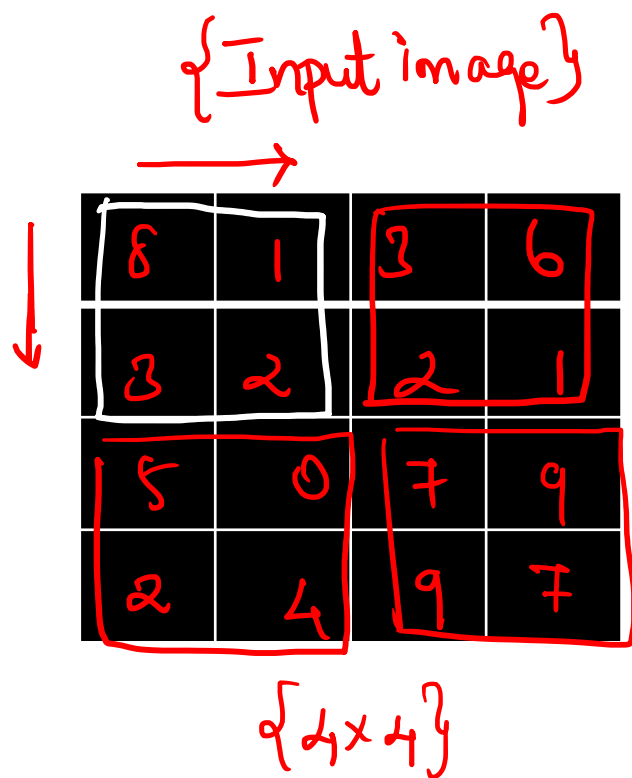
Input Image



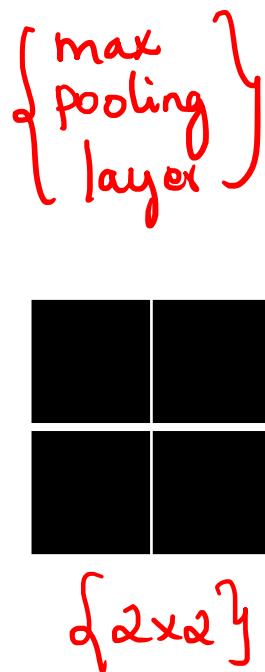
pooling

Output Image

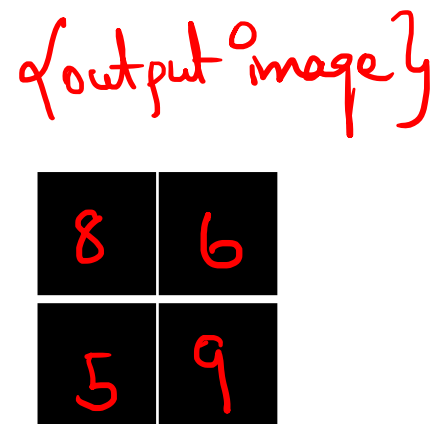




(\*)



stride=2  
⇒



$$(n \times n) \times (f \times f) = \underset{\substack{\downarrow \\ \text{stride}}}{f} \left\lfloor \frac{n-f}{f} + 1 \right\rfloor \times \left\lfloor \frac{n-f}{f} + 1 \right\rfloor \Rightarrow f \left\lfloor \frac{4-2}{2} + 1 \right\rfloor \Rightarrow f \left\lfloor \frac{2}{2} + \frac{2}{2} \right\rfloor$$

$$\Rightarrow f \left\lfloor 4/2 \right\rfloor \Rightarrow (2 \times 2)$$

8	1	3	6
3	2	2	1
5	0	7	1
2	4	9	7

or


stride=1  
⇒

8	3	6
5	7	7
5	9	9

⇓  
[ Create duplicate  
pixel ]

$$\text{floor} \left[ \frac{n-f}{s} + 1 \right] \Rightarrow \left[ \frac{4-2}{1} + 1 \right] \Rightarrow 2/1 + 1/1 \Rightarrow 3/1 \Rightarrow (3 \times 3)$$

(Input Image)

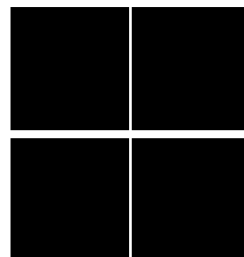
{6x6}

0	0.1	0.2	0.3	0.4	0.5
0	0.1	0.2	0.3	0.4	0.5
0	0.1	0.2	0.3	0.4	0.5
0	0.1	0.2	0.3	0.4	0.5
0	0.1	0.2	0.3	0.4	0.5
0	0.1	0.2	0.3	0.4	0.5

(\*)

{max pooling}  
filter

{2x2}

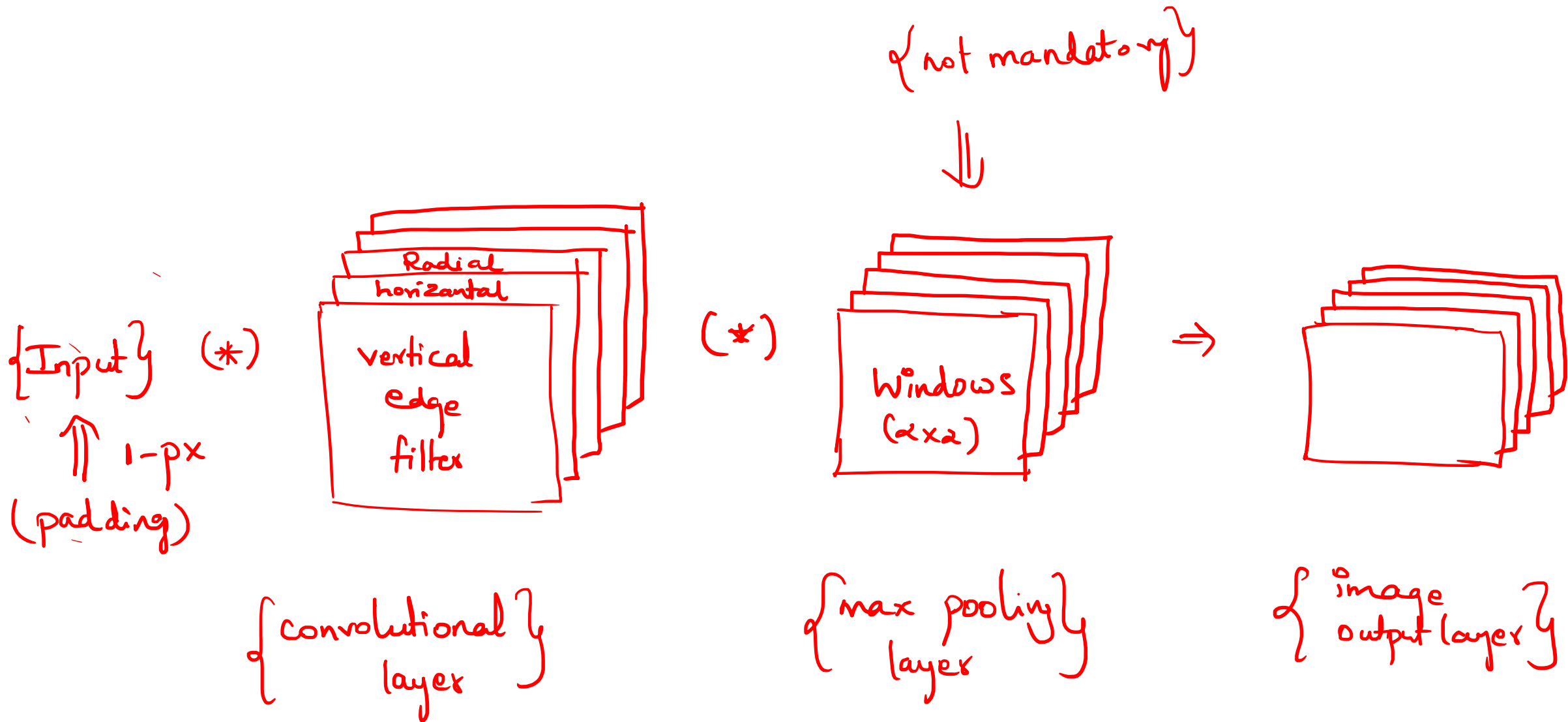


stride=2

Output  
image

0.1	0.3	0.5
0.1	0.3	0.5
0.1	0.3	0.5

$$\text{floor} \left[ \frac{n-f}{s} + 1 \right] \Rightarrow f \left[ \frac{6-2}{2} + 1 \right] \Rightarrow f \left[ \frac{4}{2} + \frac{2}{2} \right] \Rightarrow (3 \times 3)$$





# { Average - pooling }

Input

8	1	3	6
3	2	2	1
5	0	7	1
2	4	9	7

(\*)

Average  
Pooling  
layer




output  
image

3.5	3
2.8	6

Why pooling?

- Reduce image size to reduce the computational cost
- Enhance the pixel by maxing it.

Where pooling?

- after convolutional layer
- No parameters involved, no training needed.