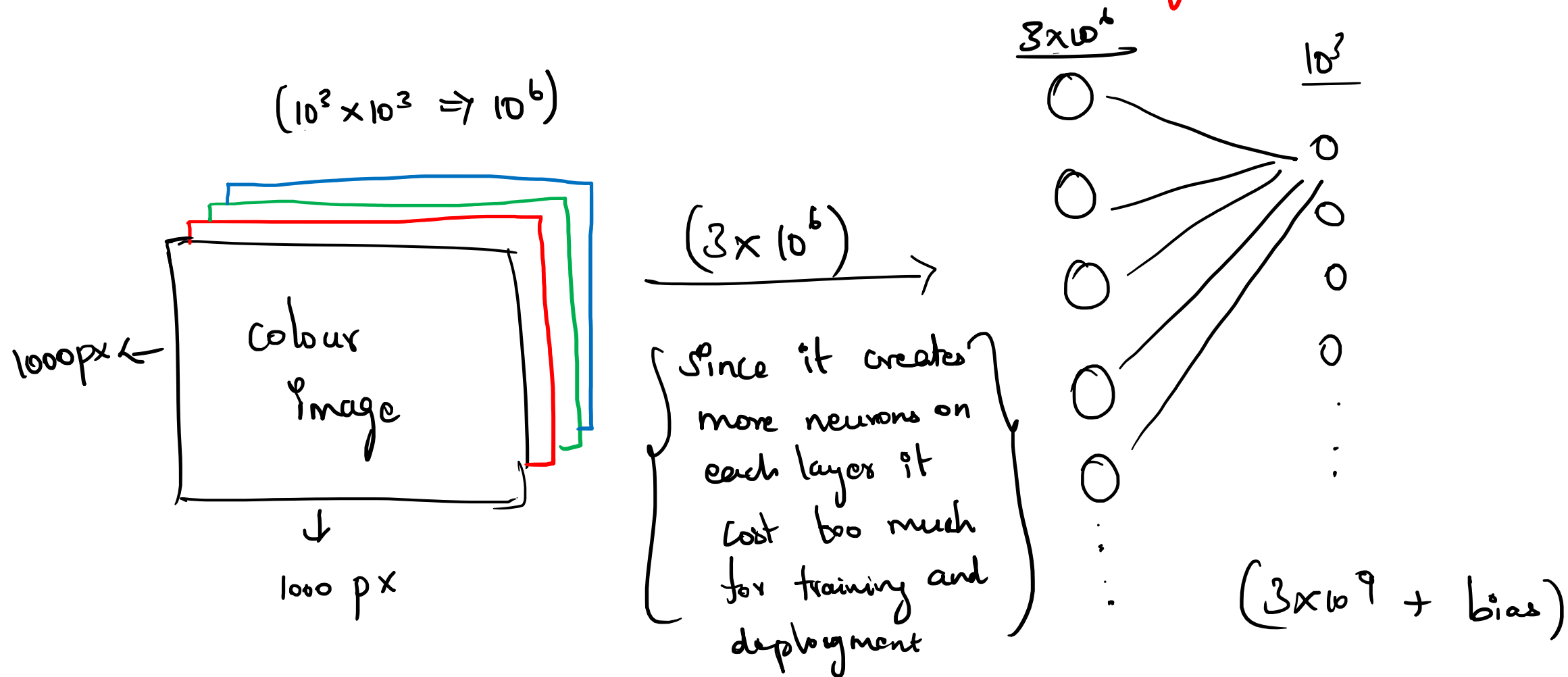


Convolutional Neural Network: (CNN) \Rightarrow images, videos

The architecture of CNN is completely different from ANN.



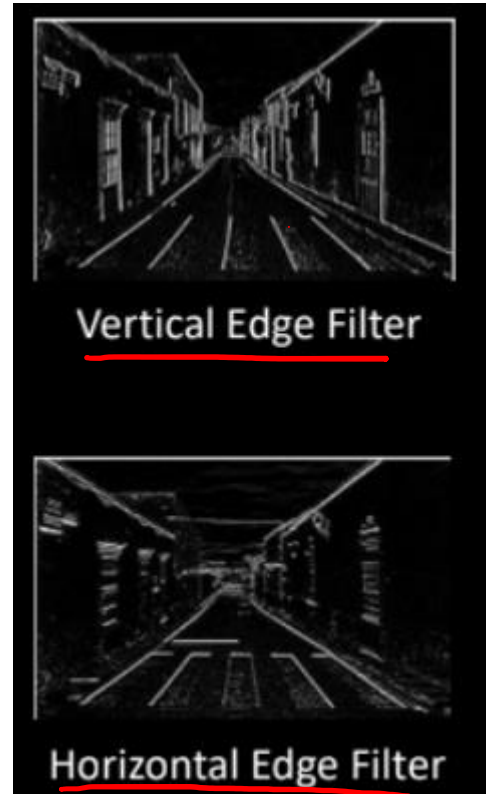
⇒ Images are made up of pixels:

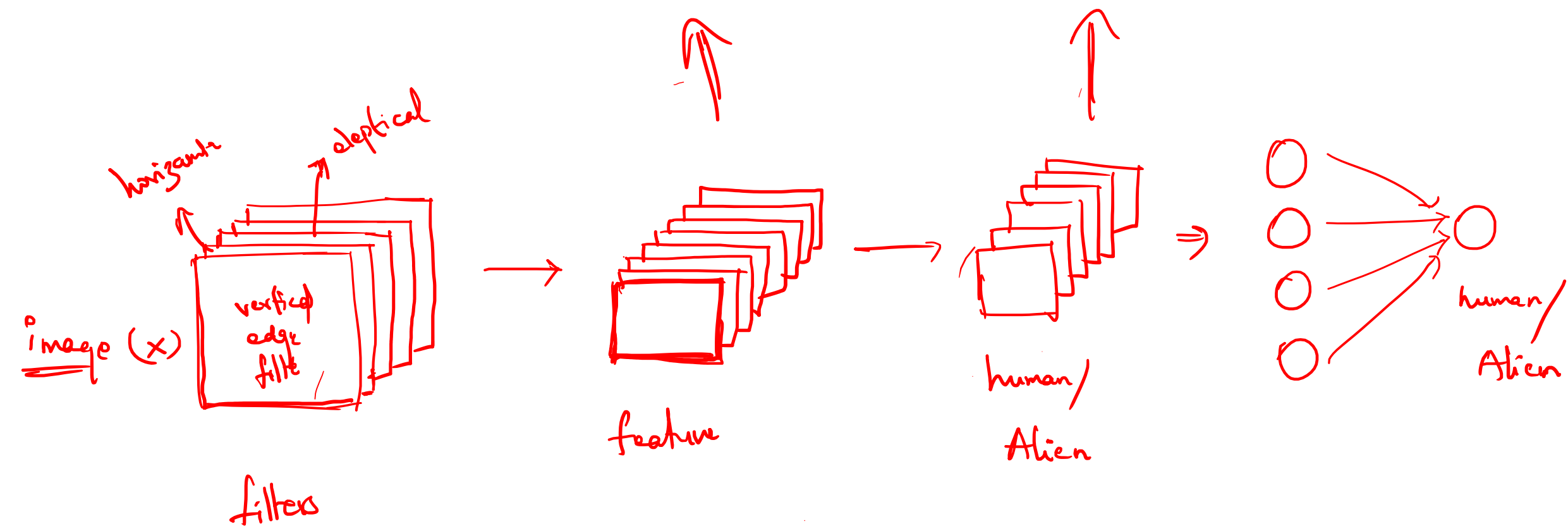
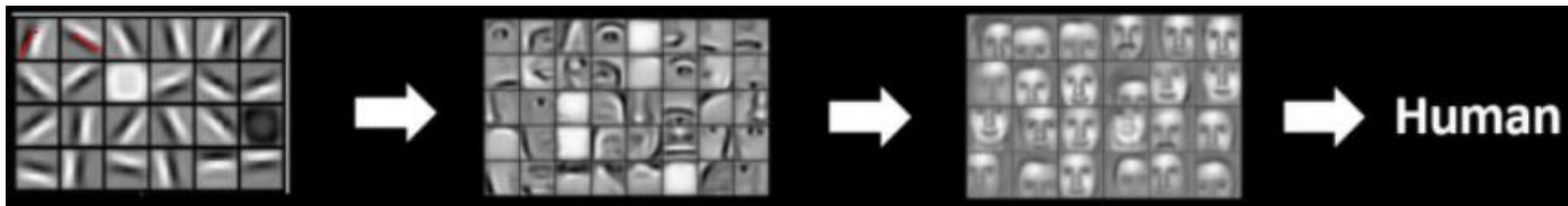
⇒ pixels are the input for CNN

Filters:



image





Grey
Scale

$(n \times n)$

1	6	9	10	2	8
2	5	1	8	4	2
3	7	4	9	10	3
9	8	3	6	7	9
8	0	9	4	7	2
9	10	12	6	9	8

$\{6 \times 6 \text{ pixel}\}$

$(f \times f)$
 $\{ \text{vertical edge} \}$
filter
↑

(x)

1	0	-1
1	0	-1
1	0	-1

$\{2 \times 3 \text{ pixel}\}$
(window)

\Rightarrow

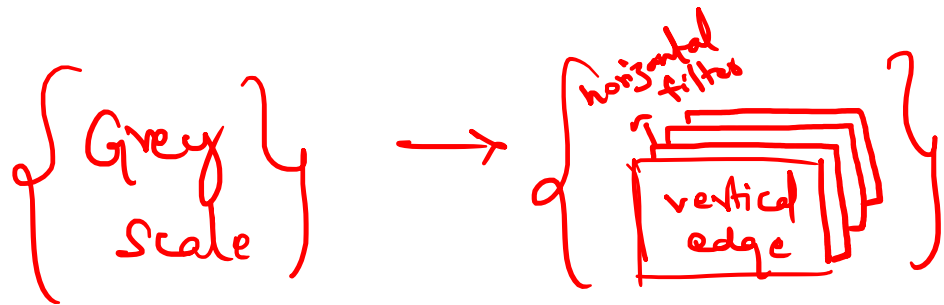
-8	-9	-2	14
6	-3	-13	9
4	-4	-8	5
2	2	1	-3

$\{4 \times 4 \text{ pixel}\}$

$$\begin{aligned} (n \times n) \times (f \times f) &= (n - f + 1) \times (n - f + 1) \\ (6 \times 6) \times (3 \times 3) &= (6 - 3 + 1) \times (6 - 3 + 1) \Rightarrow (4 \times 4) \end{aligned}$$

↗

Input image (x) filters



\Rightarrow

$\{ \text{output image with layers} \}$
 and filters

\downarrow

$$(n-f+1) \times (n-f+1) \times \textcircled{C}$$

\Downarrow

$\{ \# \text{ filters} \}$

\downarrow

$$(n \times n) \times \textcircled{1}$$

\Downarrow

1-layer

\downarrow

$$(f \times f) \times \textcircled{C}$$

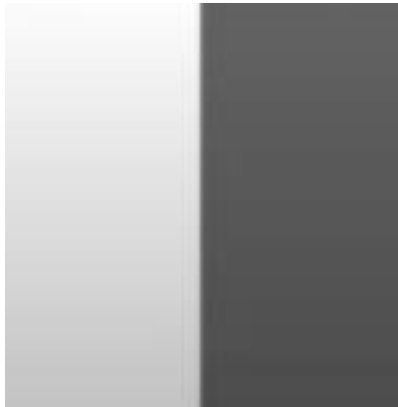
\Downarrow

$\{ \# \text{ of filters} \}$

Grey scale image \rightarrow 1 layer
Colour image \rightarrow 3 layer (RGB)

(6x6 px)

1	1	1	0	0	0
1	1	1	0	0	0
1	1	1	0	0	0
1	1	1	0	0	0
1	1	1	0	0	0
1	1	1	0	0	0



x

(3x3 px)

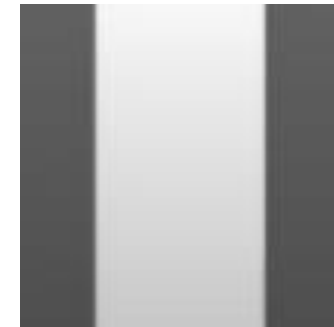
1	0	-1
1	0	-1
1	0	-1

vertical
edge
filter

⇒

(4x4 px)

0	3	3	0
0	3	3	0
0	3	3	0
0	3	3	0





*

{ vertical
edge }

1	0	-1
1	0	-1
1	0	-1

=



*

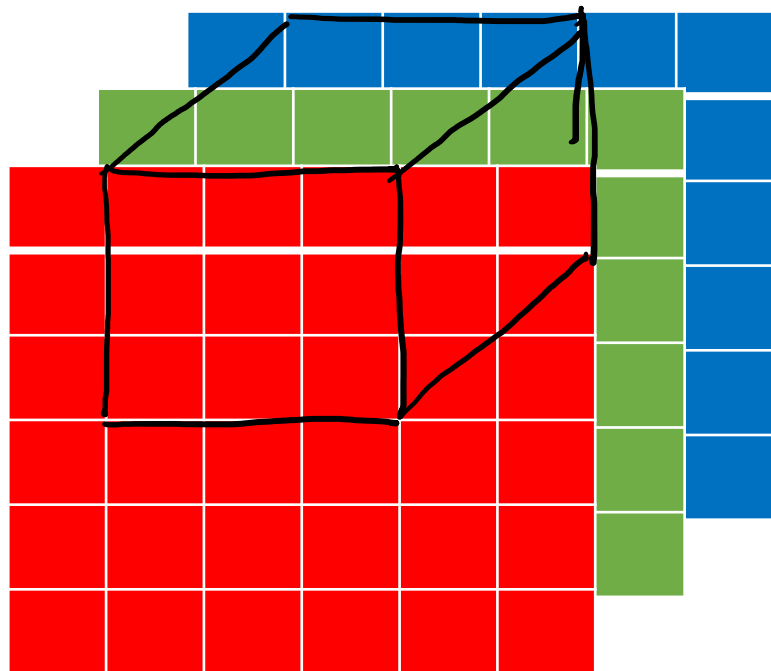
{ horizontal
edge }

1	1	1
0	0	0
-1	-1	-1

=



(Colour image)

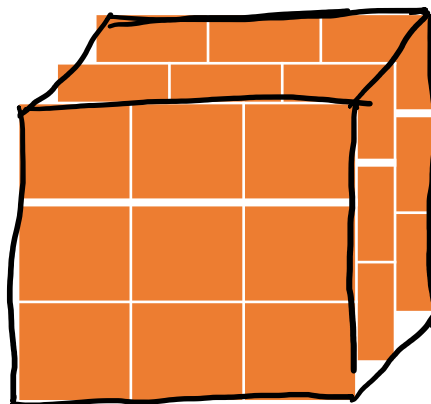


$n \times n \times 3$

$$\Rightarrow (\text{layer}-1) + (\text{layer}-2) + (\text{layer}-3) = 1$$

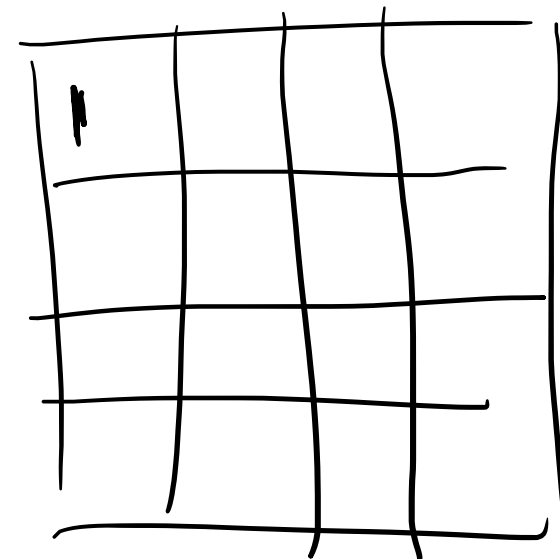
{ vertical
edge
filter }

(x)



$f \times f \times 3$

\Rightarrow



$(n-f+1) \times (n-f+1) \times 1$

$(n \times n \times 3)$



*



$f \times f \times 3$



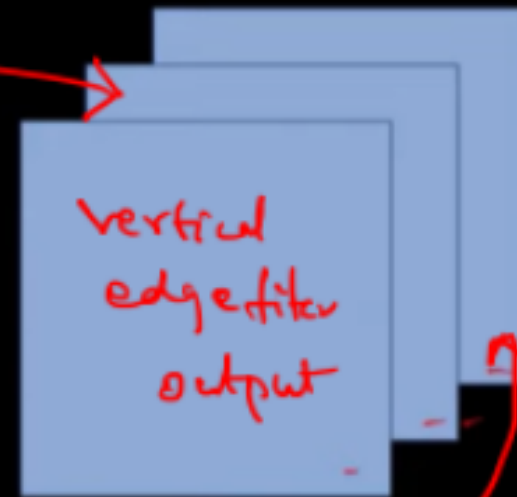
$f \times f \times 3$

=

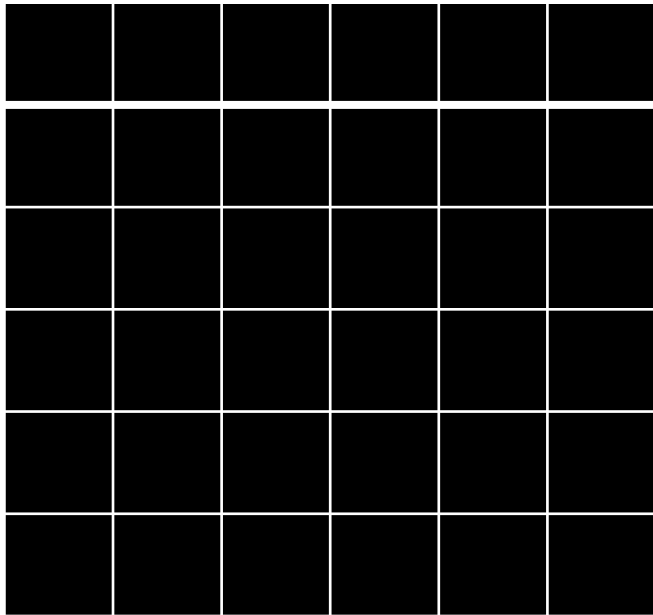


$f \times f \times 3$

$(h-f+1)(n-f+1) \times 3$



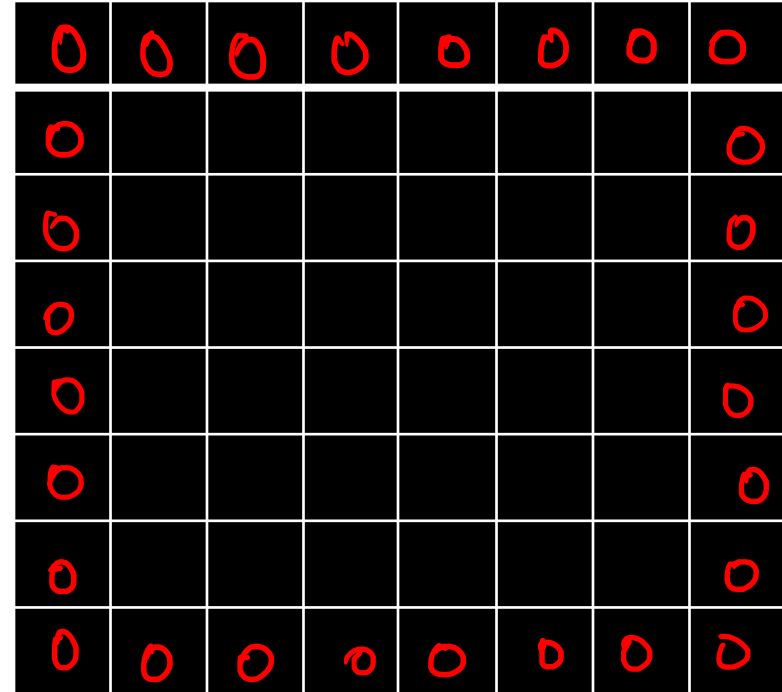
Padding: \Rightarrow padding is used to retain the output px w.r.t input px



{6x6 px}



{1-px
padding}



{8x8 px}

padded
image

*

vertical
filter

\Rightarrow

output

$\{8 \times 8\}$

*

$\{3 \times 3\}$

\Rightarrow

$\{6 \times 6\}$

$(n \times n)$

*

$(f \times f)$

$= (n - f + 1) (n - f + 1)$

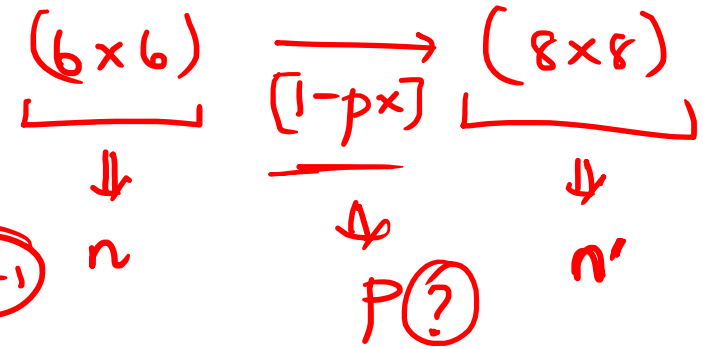
$= (8 - 3 + 1) (8 - 3 + 1)$

$= (6 \times 6) \Rightarrow \text{original image size}$

Types:

1. valid convolution \Rightarrow No padding

2. Same convolution $\Rightarrow \underline{n' = n + 2p} \Rightarrow \text{equ-1}$



$$\Rightarrow \underline{(n' - f + 1)} = n$$

$$(n' \times n') (f \times f) = \underline{(n' - f + 1)} (n' - f + 1)$$

Apply equ-1 on above

$$\Rightarrow (n + 2p - f + 1) = n$$

$$\Rightarrow 2p = n - n + f - 1$$

$$\Rightarrow 2p = f - 1 \Rightarrow p = \left\{ \frac{(f-1)}{2} \right\} \Rightarrow \text{padding size formula}$$

$$\{6 \times 6\} \times \{3 \times 3\} \Rightarrow \{n \times n\} \times \{f \times f\}$$

$$\Rightarrow \{n' - f + 1\} = n$$

$$\Rightarrow \{n + 2p - f + 1\} = n$$

$$\Rightarrow \{6 + 2p - 3 + 1\} = 6$$

$$\Rightarrow 2p = 6 - 6 + 3 - 1$$

$$\Rightarrow 2p = 2$$

$$\Rightarrow p = 1$$

$$\{6 \times 6\} \rightarrow 1\text{-px padding} \rightarrow ?$$

$$\Rightarrow n' \times n' = (n + 2p) (n + 2p)$$

$$\Rightarrow n' \times n' = (6 + 2(1)) (6 + 2(1))$$

$$\Rightarrow n' \times n' = 8 \times 8$$

python: $\Rightarrow \text{keras.conv2d}(x, w, \text{padding} = \text{"valid"} \text{ or "same"})$