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Name of student:

Examiners Report

Use the following codes for evaluation:

A : All Good

B : Silly Mistake

C : Conceptual Error

D : Hard question

E : Not Applicable

Question Number	Marks	Remark									
1	A	4	E	7	E						
2	B	5	A	8	E						
3	A	6	D								

Math

Name: Maanya

① Start : 08:06
End : 09:00

② Start : 19:38
End : 20:00

Q1) a) $\tan x = \frac{\sin x}{\cos x}$

$$\frac{dy}{dx} = \frac{\cos^2 x + \sin^2 x}{\cos^2 x} \xrightarrow{=} \frac{1}{\cos^2 x} \xrightarrow{\text{M1A1}} \sec^2 x \xrightarrow{\text{AG}}$$

b) $y = \arctan x$

$$x = \tan y \xrightarrow{\text{M1}} \frac{dx}{dy} = \sec^2 y \xrightarrow{\text{A1}}$$

$$\frac{dy}{dx} = \frac{1}{\frac{dx}{dy}} \xrightarrow{\text{from part (a)}} \frac{1}{\sec^2 y} \xrightarrow{\text{A1}}$$

$$\frac{1}{\sec^2 y} = \frac{1}{1 + x^2} \xrightarrow{\text{AG}}$$

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Q2)

a) $f(0) = \frac{100}{51} = 1.96 \quad (3 \text{ s.f.}) \xrightarrow{\text{A1}}$

b) $f(x) = 95 = \frac{100}{1 + 50e^{-0.2x}} \xrightarrow{\text{M1}}$

$$95 = \frac{100}{1 + 50e^{-0.2x}} \quad (3 \text{ s.f.}) \xrightarrow{\text{A1}}$$

c) $0 < y < 100 \xrightarrow{\text{A1A1A1}}$

d)
$$\frac{(1 + 50e^{-0.2x})(0) - 100(50e^{-0.2x} \cdot -0.2)}{(1 + 50e^{-0.2x})^2} \xrightarrow{\text{M1A1A1}}$$

$$\frac{-100(-10e^{-0.2x})}{(1 + 50e^{-0.2x})^2} \xrightarrow{\text{A1}}$$

$$f'(x) = \frac{1000e^{-0.2x}}{(1 + 50e^{-0.2x})^2} \xrightarrow{\text{AG}}$$

e) N/A

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$$Q3) \frac{dy}{dx} = 8x^3 + 18x^2 + 7x - 5 \rightarrow 0 \quad A1$$

$$\begin{aligned} 8x^3 + 18x^2 + 7x - 5 &= -2 \\ x = -2 \end{aligned} \quad A1M1$$

$$-8 + 18 - 7 - 5 = -2$$

$$8x^3 + 18x^2 + 7x - 5 \geq 0$$

$$= (x+1)(4x-1)(2x+3) \geq 0 \quad A1M1$$

$$x = -1, x = 0.25, x = -1.5 \quad M1A1$$

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Q4) N/A

Q5)

$$y = x^3 - 6x^2 + kx - 4$$

$$\frac{dy}{dx} = 3x^2 - 12x + k \quad M1A1$$

$$3x^2 - 12x + k = 0 \quad (\text{only one solution})$$

$$b^2 - 4ac = 0$$

$$144 - 4(3)(k) = 0 \quad A1$$

$$\cancel{k = 12} \quad A1$$

5/5

$$Q6) a) x^3 + 1 = \frac{1}{x^3 + 1}$$

$$\text{Using GDC} \quad z \rightarrow (-1, 2, -1) \quad A1$$

b) N/A

1/1

Q7) & Q8) N/A