Assignment 4

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As given in question we will be given a input string w where each alphabet is either 0 or 1 and we have to design a turing machine which will transform given string to swap ith and (i+1)th alphabet if i is odd and less than n.

Here we will reformat the input and swap alphabets if needed. Here we can have 4 cases for ith and (i+1)th characters. So here are 4 cases -

If both are 00 then if we swap there is no change so we just move 2 steps forward from ith position.

If both are 11 then if we swap there is no change so we just move 2 steps forward from ith postion.

If both are 01 then we have swap it to 10 and then move 2 steps forward from ith position.

If both are 10 then we have swap it to 01 and then move 2 steps forward from ith position.

Here Turing Machine M is defined as follows:-

$$\begin{aligned} \mathbf{M} &= (\mathbf{Q}, \sum, \tau, \, \delta, \, q_0, \, \mathbf{B}, \, q_h) \text{ where} \\ \mathbf{Q} &= \{q_0, \, q_1, \, q_2, \, q_3, \, q_4, \, q_5, \, q_6, \, q_h\} \\ \sum &= \{0.1\} \, , \, \tau = \{0.1.8\} \end{aligned}$$

 δ is represented by Transition table and q_0 is starting state and B is blank symbol.

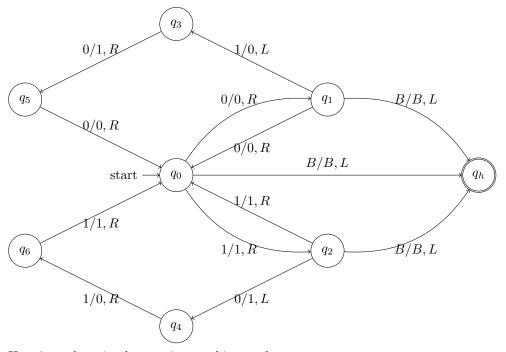
 q_h is accepting and halt state to show process is completed and input is converted to output.

Here logic of Machine is that we manipulate 2 alphabets starting from q_0 and coming back again to q_0 and whenever we encounter a Blank symbol meaning that string is finished we move to q_h halt state and at last our control will be pointing to last alphabet of output string.

Transition table -

present state, input symbol	destination state, overwrite, direction
$q_0,0$	$q_1,\!0,\!\mathrm{R}$
$q_0,1$	$q_2,1,R$
$q_0,$ B	$q_h,\!\mathrm{B,\!L}$
$q_1,0$	$q_0,\!0,\!\mathrm{R}$
$q_1,1$	$q_3,\!0,\!\mathrm{L}$
$q_1,\!\mathrm{B}$	$q_h,\!\mathrm{B,\!L}$
$q_2,0$	$q_4,\!1,\!\mathrm{L}$
$q_2,1$	$q_0,1,R$
$q_2,\!\mathrm{B}$	$q_h,\! m B,\! m L$
$q_{3},0$	$q_5,\!1,\!\mathrm{R}$
$q_{5},0$	$q_0,\!0,\!\mathrm{R}$
$q_4,1$	$q_6,\!0,\!\mathrm{R}$
$q_{6},1$	$q_1,1,R$

Turing Machine M -



Here is explanation how turing machine works -

Firstly we are at q_0 . Here we scan input alphabet. Let's say it is 0 then we move to q_1 and move right. In q_1 we check current alphabet if it is 0 then we again go to q_0 and move right as 00 will have no effect of swap. But if its 1 we change it 0 and go to q_3 and move left. Now we know here its alphabet is 0. So we change it to 1 and move to q_4 and move right. Now we can see that we have swapped both alphabets thus we move to q_0 and move right.

Let's say input alphabet is 1 then we move to q_2 and move right. In q_2 we

check current alphabet if it is 1 then we move to q_0 and move right as 11 will have no effect of swap. But if its 0 we change it 1 and go to q_4 and move left. Now we know here its alphabet is 1. So we change it to 0 and move to q_6 and move right. Now we can see that we have swapped both alphabets thus we move to q_0 and move right.

Here are 2 cases that whether string length is odd or even - If string length is even and starting from q_0 we scan 2 alphabets and swap them so after processing whole string we will be reaching at q_0 again and have Blank symbol. So we make a transition to q_h when ever we encounter a blank symbol meaning string is processed.

Here on the states q_3, q_4, q_5, q_6 we do not need any other transitions as we know what was previous alphabet.

If string length is odd and starting from q_0 we scan 2 alphabet and swap them. So here we will be processing whole string except last symbol as it do not have a pair and in our machine when we scan first symbol we reach either q_1 or q_2 , and given in question this alphabet needs to be remain same. So we make transitions from these states to q_h whenever they get a Blank symbol Showing that our string is processed.