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### Assignment 2

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#### 1

Language  $L$  consists of strings of length  $2n$  where last  $n$  characters are all ones where  $n \geq 0$ .

Let there are 2 strings  $a, b$  where  $|a| = n$  and  $|b| = m$  where  $n \neq m$ . We will show that relation  $R_L$  has infinite index. Taking  $n < m$  and for all pairs of  $a, m$  appending  $0^{m+1}$  at end of both strings.

we will show that  $a0^{m+1} \in L$  and  $b0^{m+1} \notin L$ .  
 $a0^{m+1} \in L$  as taking  $w$  as  $a0$  and it has length  $n+1$  and string has  $n+1$  1's at end. So it belongs to  $L$ .

$b0^{m+1} \notin L$  as total length is  $m+n+2$ . So it must have  $(m+n+2)/2$  1's at end but it has only  $n+1$  1's which are less than required which can be shown as follows:-

$n < m$  and add  $n+2$  both sides gives  
 $2n+2 < m+n+2$  and dividing by 2 gives desired result.

So  $a$  and  $b$  must be in different classes for all  $n$  and  $m$ .  
Hence number of classes of  $R_L$  are infinite and by Myhill-Nerode theorem  $L$  is non-regular.

#### 2

Language  $L$  consists of strings of length  $2n$  where last  $n$  characters are complement of first  $n$  characters where  $n \geq 0$ .

Let there are two strings  $a$  and  $b$  where  $a = 0^n$  and  $b = 0^m$  where  $n \neq m$ .

We will show that relation  $R_L$  has infinite index. Taking  $n < m$  and for all pairs of  $a, m$  appending  $1^n$  at end of both strings.

we will show that  $0^n 1^n \in L$  and  $0^m 1^n \notin L$ .  
As  $0^n 1^n \in L$  is trivial as taking  $w$  as  $0^n$  gives required string. Hence  $0^n 1^n \in L$ .

Also  $0^m 1^n \notin L$  is trivial as  $n \neq m$  So, it can never be in  $L$ .  
So  $a$  and  $b$  are in different classes for all  $n$  and  $m$ .

Hence number of classes of  $R_L$  are infinite and by Myhill-Nerode theorem  $L$  is non-regular.