

# Probability and Random Variables

## Assignment 3

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# Outline

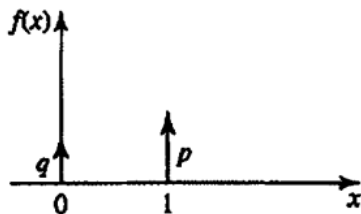
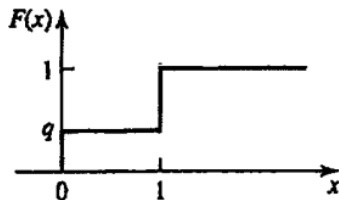
1 Problem

2 Solution

# Problem

In the coin-tossing experiment, the probability of heads equals  $p$  and the probability of tails equals  $q$ . We define the random variable  $x$  such that  $x(h)=1$ ,  $x(t)=0$ . We shall find its distribution function  $F(x)$  for every  $x'$  from  $-\infty$  to  $\infty$ .

# Solution



If  $x \geq 1$ , then  $x(h)=1$  and  $x(t)=0 \leq x$ .

Hence  $F(x)=P\{x \leq x\} = P(h,t)=1$ ,  $x \geq 1$ . If  $0 \leq x \leq 1$ , then  $x(h)=1$  and  $x(t)=0 \leq x$ . Hence

$$F(x)=P\{x \leq x\} = P\{t\}=q, 0 \leq x \leq 1.$$

If  $x < 0$ , then  $x(h)=1 > x$  and  $x(t)=0 > x$ . Hence,

$$F(x)=P\{x \leq x\}=P\{\emptyset\} = 0, x < 0$$