

Assignment 3

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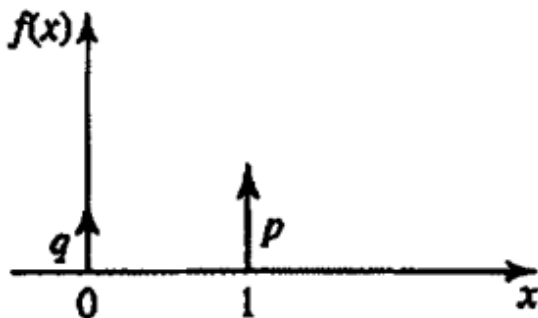
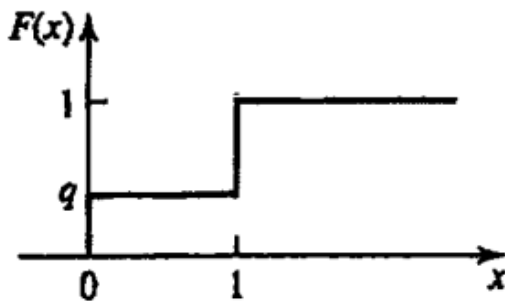
Question

In the coin-tossing experiment, the probability of heads equals p and the probability of tails equals q . We define the random variable x such that

$$x(h)=1, x(t)=0$$

We shall find its distribution function $F(x)$ for every x from $-\infty$ to ∞ .

Solution



If $x \geq 1$, then $x(h)=1 \leq x$ and $x(t)=0 \leq x$.

Hence $F(x)=P\{x \leq x\} = P(h,t)=1$, $x \geq 1$. If $0 \leq x \leq 1$, then $x(h)=1 > x$ and $x(t)=0 \leq x$. Hence

$$F(x)=P\{x \leq x\} = P\{t\}=q, 0 \leq x \leq 1.$$

If $x < 0$, then $x(h)=1 > x$ and $x(t)=0 > x$. Hence,

$$F(x)=P\{x \leq x\}=P\{\emptyset\} = 0, x < 0$$