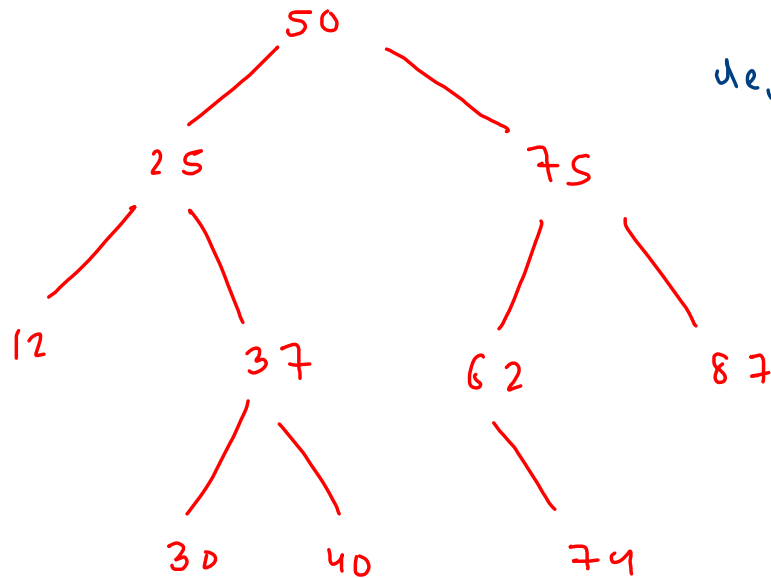


Binary
search tree



$\forall \text{ nodes in } < \text{node.val} < \forall \text{ nodes}$

left subtree

in right subtree

Inorder: L N R

BST inorder sorted.

inorder: 12 25 30 37 40 50 62 74 75 87

Construct

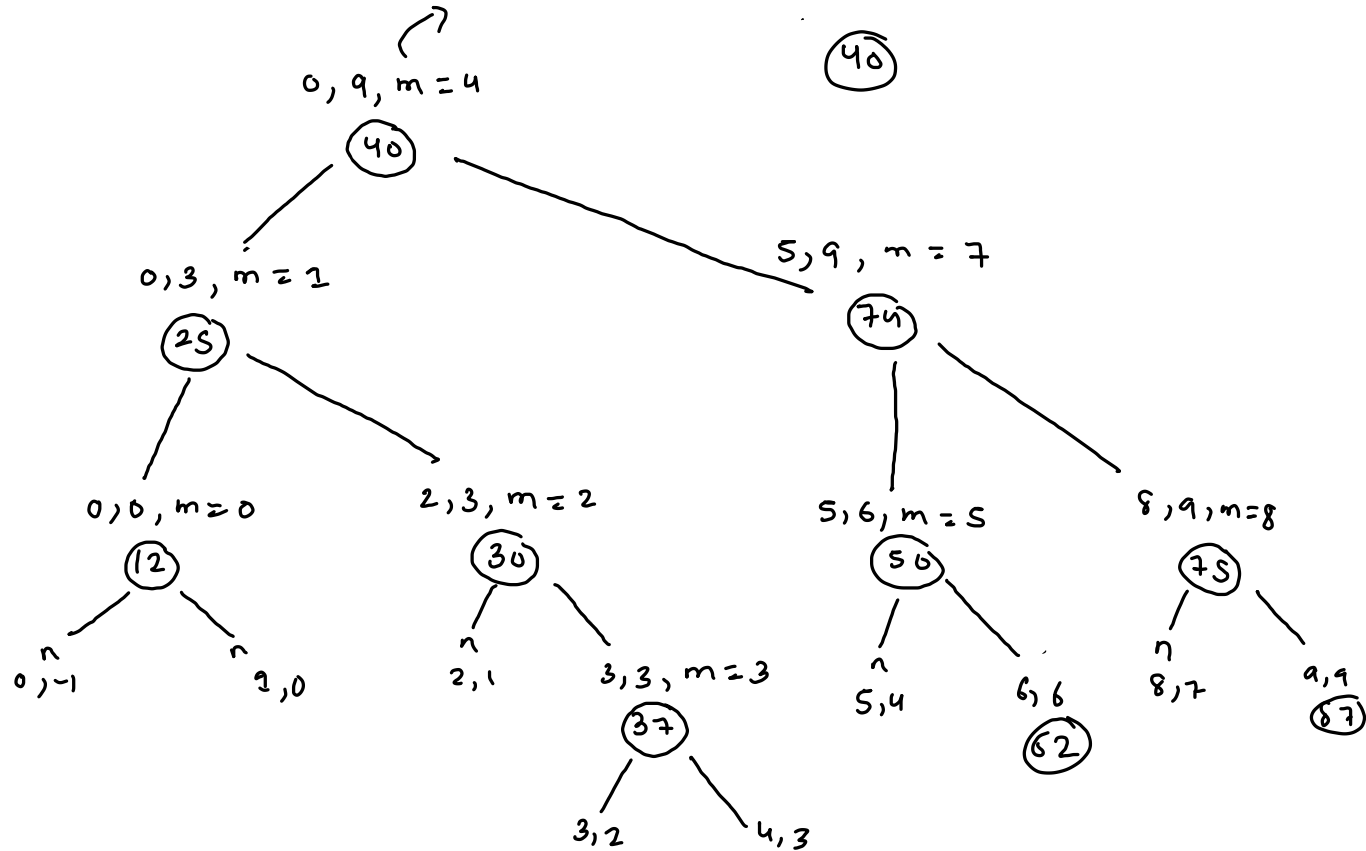
sorted array \rightarrow balanced bst

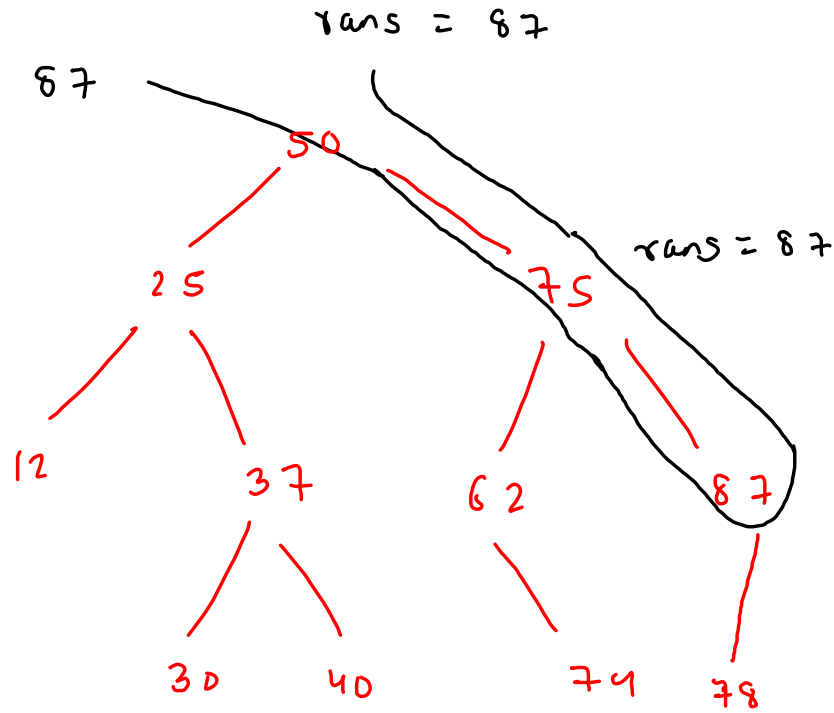
12 25 30 37 40 50 62 74 75 87
0 1 2 3 4 5 6 7 8 9

```
public TreeNode helper(int[] nums, int lo, int hi) {
    if (lo > hi) {
        return null;
    }
    int mid = (lo + hi) / 2;
    TreeNode node = new TreeNode(nums[mid]);
    node.left = helper(nums, lo, mid - 1);
    node.right = helper(nums, mid + 1, hi);
    return node;
}
```

left: lo, mid-1

right: mid+1, hi



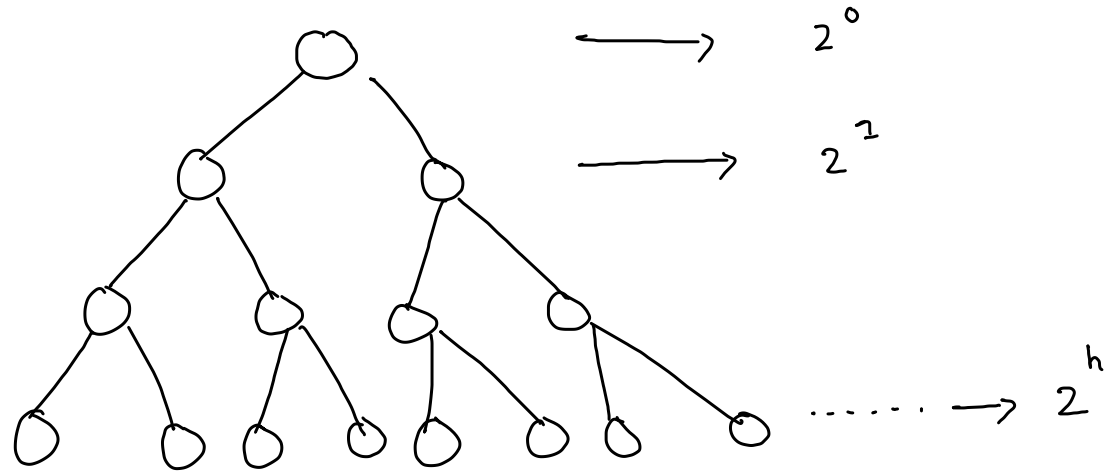


```

public static int max(Node node) {
    if(node.right != null) {
        int rans = max(node.right);
        return rans;
    }
    else {
        return node.data;
    }
}

```

$O(h)$



$$n = 2^0 + 2^1 + \dots + 2^h$$

$$= 2(2^{h+1} - 1)$$

$$n = 2^{h+1}$$

$$\log_2 n = h+1$$

$$h \propto \log_2 n$$

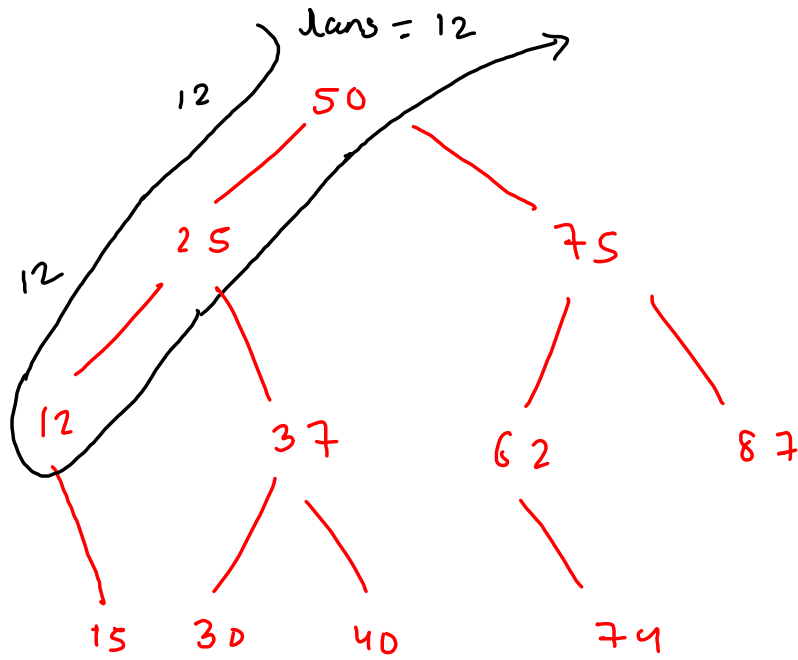
GP

$$a = 1$$

$$r = 2$$

$$t = h+1$$

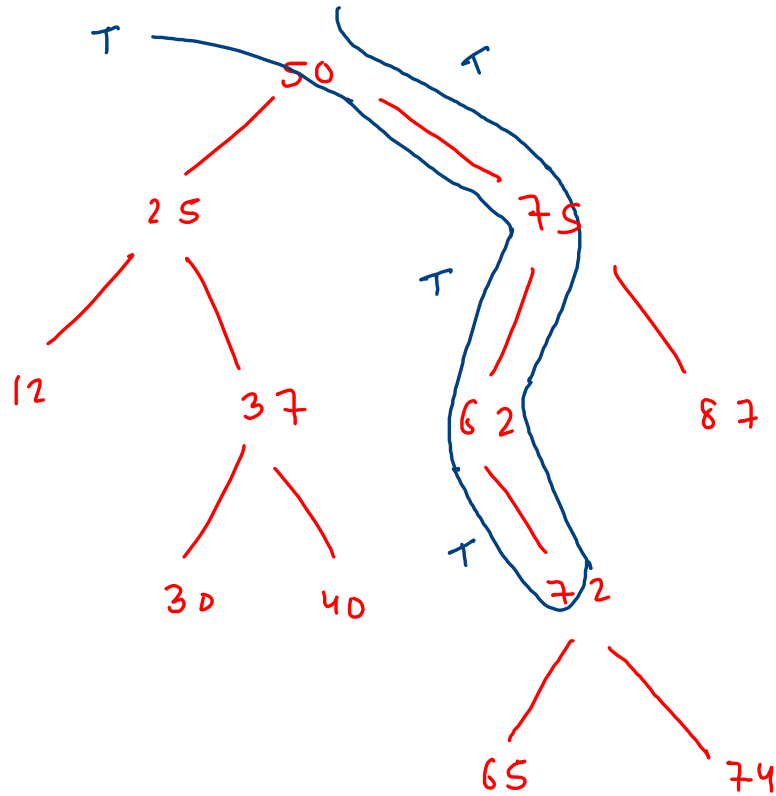
$$S = \frac{a(r^t - 1)}{r - 1}$$



```
public static int min(Node node) {  
    if(node.left != null) {  
        int lans = min(node.left);  
        return lans;  
    }  
    else {  
        return node.data;  
    }  
}
```

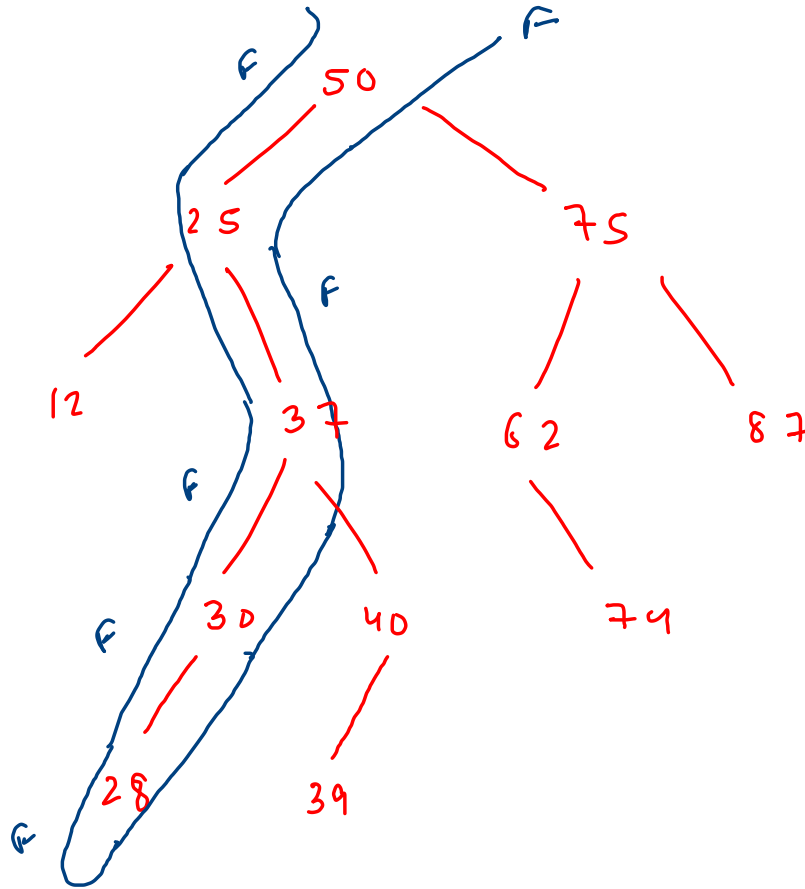
find

data = 72



```
public static boolean find(Node node, int data){
    if(node == null) {
        return false;
    }

    if(node.data < data) {
        //go to right
        return find(node.right, data);
    }
    else if(node.data > data) {
        //go to left
        return find(node.left, data);
    }
    else {
        return true;
    }
}
```



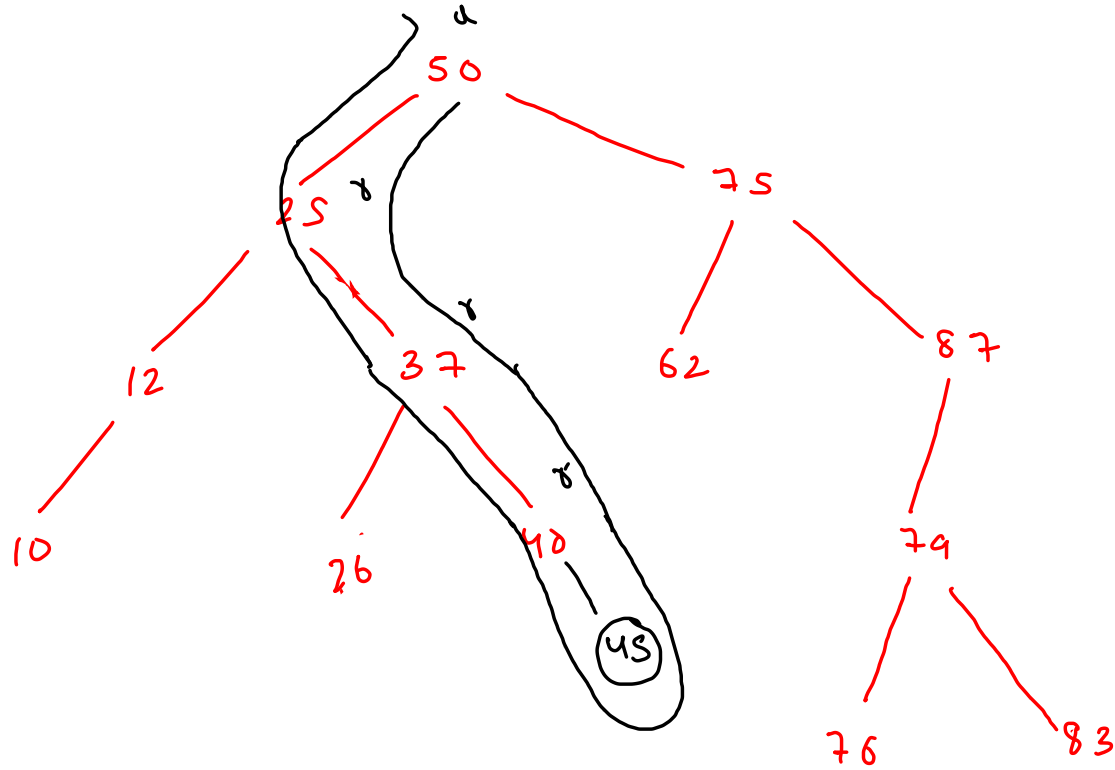
```

public static boolean find(Node node, int data){
    if(node == null) {
        return false;
    }

    if(node.data < data) {
        //go to right
        return find(node.right,data);
    }
    else if(node.data > data) {
        //go to left
        return find(node.left,data);
    }
    else {
        return true;
    }
}

```

data = 26



add(28)

add(77)

add(37) no work

add(45)

```

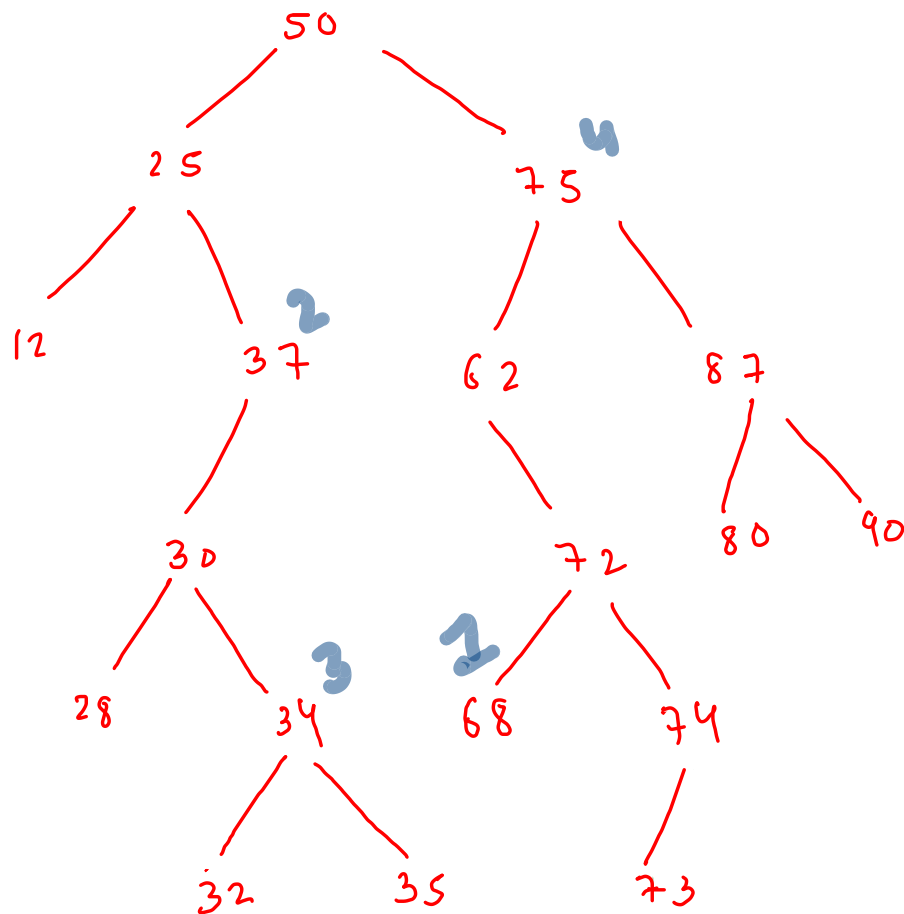
public static Node add(Node node, int data) {
    if(node == null) {
        return new Node(data,null,null);
    }

    if(node.data < data) {
        //go to right
        node.right = add(node.right,data);
    }
    else if(node.data > data) {
        //go to left
        node.left = add(node.left,data);
    }
    else {
        //do nothing
    }

    return node;
}

```

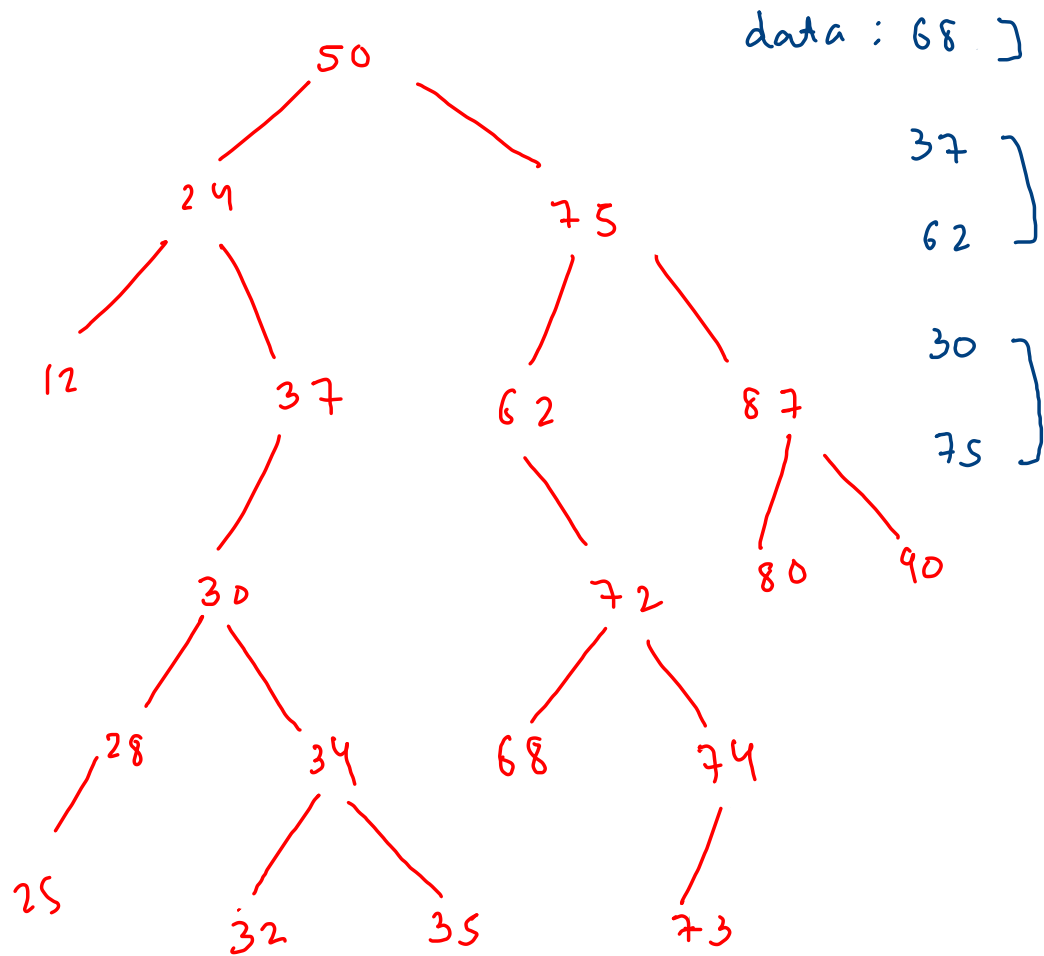

remove
node



① node \rightarrow 0 children
return null on your
behalf.

② node \rightarrow 1 child
return your single
child on your behalf

③ node \rightarrow 2 child
node.data = dmax;
remove(node.left, dmax);



```

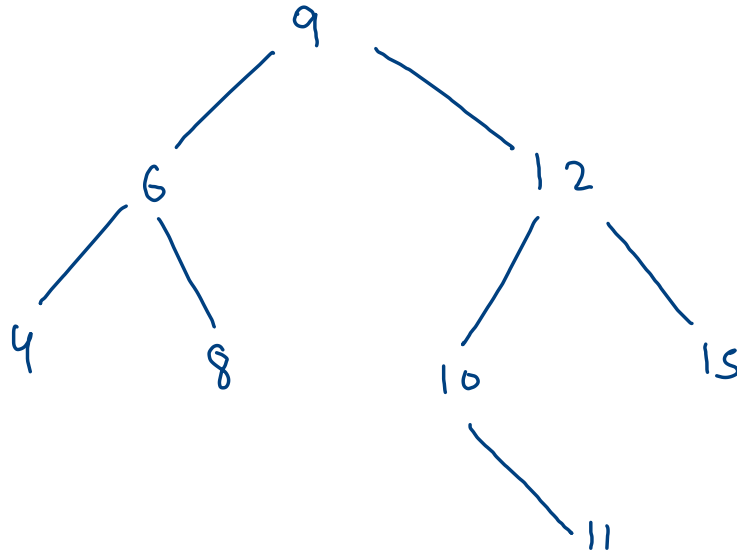
public static Node remove(Node node, int data) {
    if(node == null) {
        //data is not present in the tree
        return null;
    }

    if(node.data < data) {
        node.right = remove(node.right, data);
    }
    else if(node.data > data) {
        node.left = remove(node.left, data);
    }
    else {
        //perform removal
        if(node.left == null && node.right == null) {
            //node is a leaf node
            return null;
        }
        else if(node.left == null) {
            //single child -> right child
            return node.right;
        }
        else if(node.right == null) {
            //single child -> left child
            return node.left;
        }
        else {
            //node has both the childs
            int lmax = max(node.left);
            node.data = lmax;
            node.left = remove(node.left, lmax);
        }
    }

    return node;
}
  
```

replace with
sum of larger

Sum = 0



regular inorder

L N R

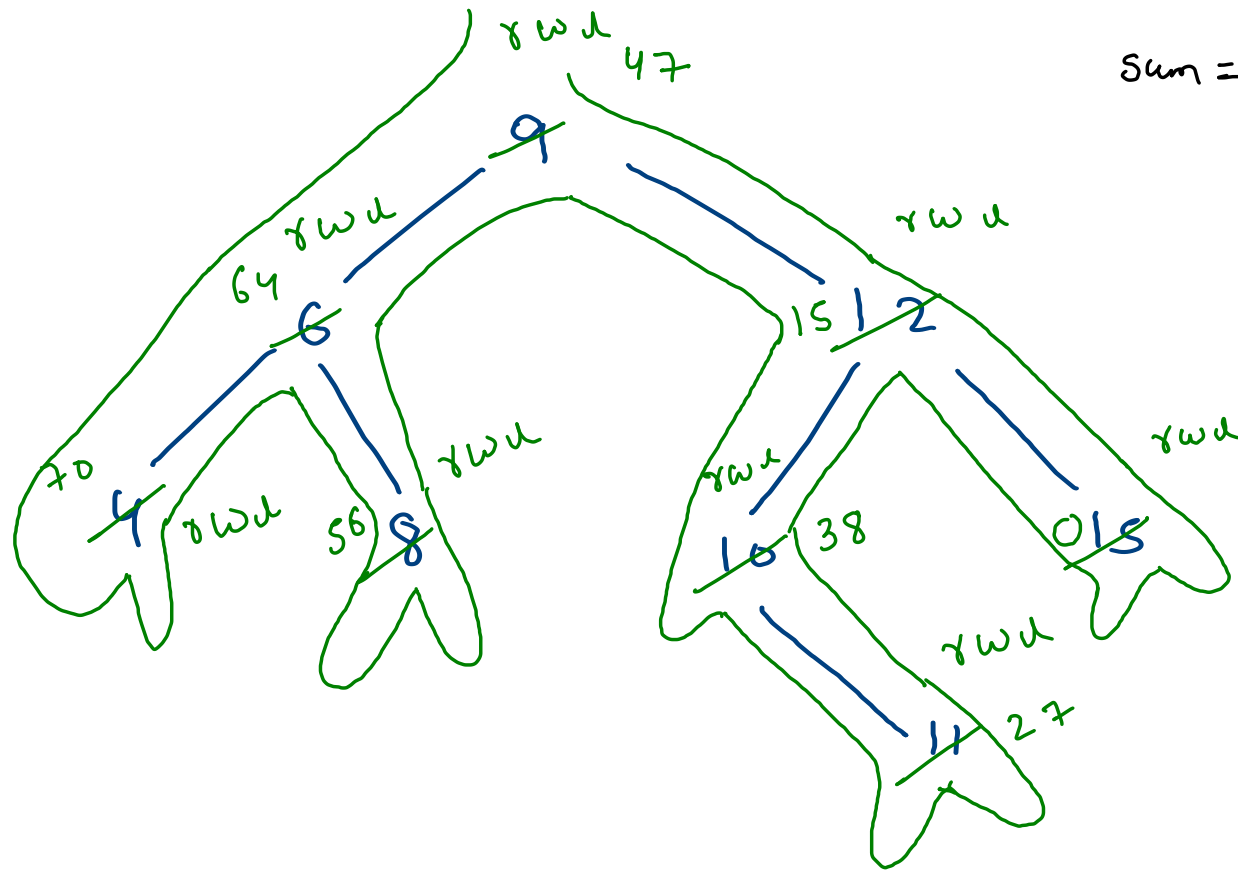
reverse inorder

R N L

in :

4 6 8 9 10 11 12 15

```
[ call (node.right);  
  work();  
  call (node.left);
```



$$\text{sum} = 0 + 15 + 12 + 11$$

$$+ 10 + 9 + 8 + 6 + 4$$

```
static int sum = 0;
public static void rwsol(Node node){
    if(node == null) {
        return;
    }

    rwsol(node.right);

    //work
    int temp = node.data;
    node.data = sum;
    sum += temp;

    rwsol(node.left);
}
```