

< pi <

if (arr[j] > pi) {

j++ ; \rightarrow 1's

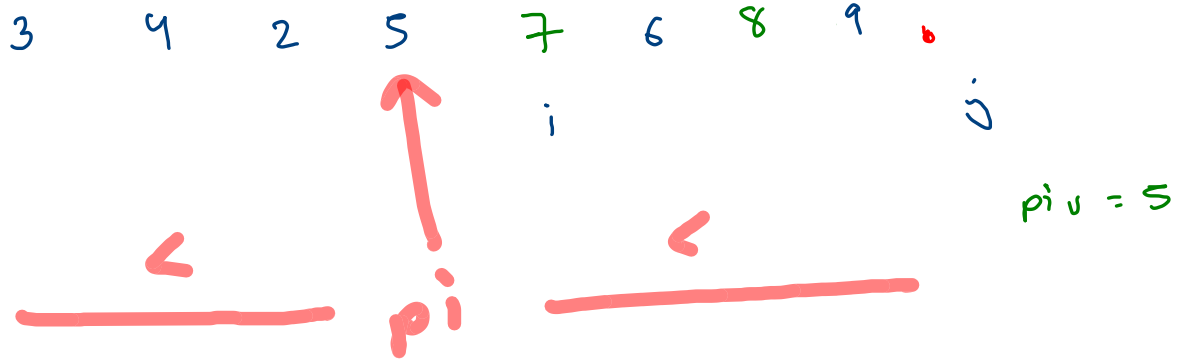
}

else {

swap(i, j); \rightarrow 0's

i++; j++;

}



0 to i-1 \rightarrow \leq pi

i to j-1 \rightarrow $>$ pi

j to n-1, all

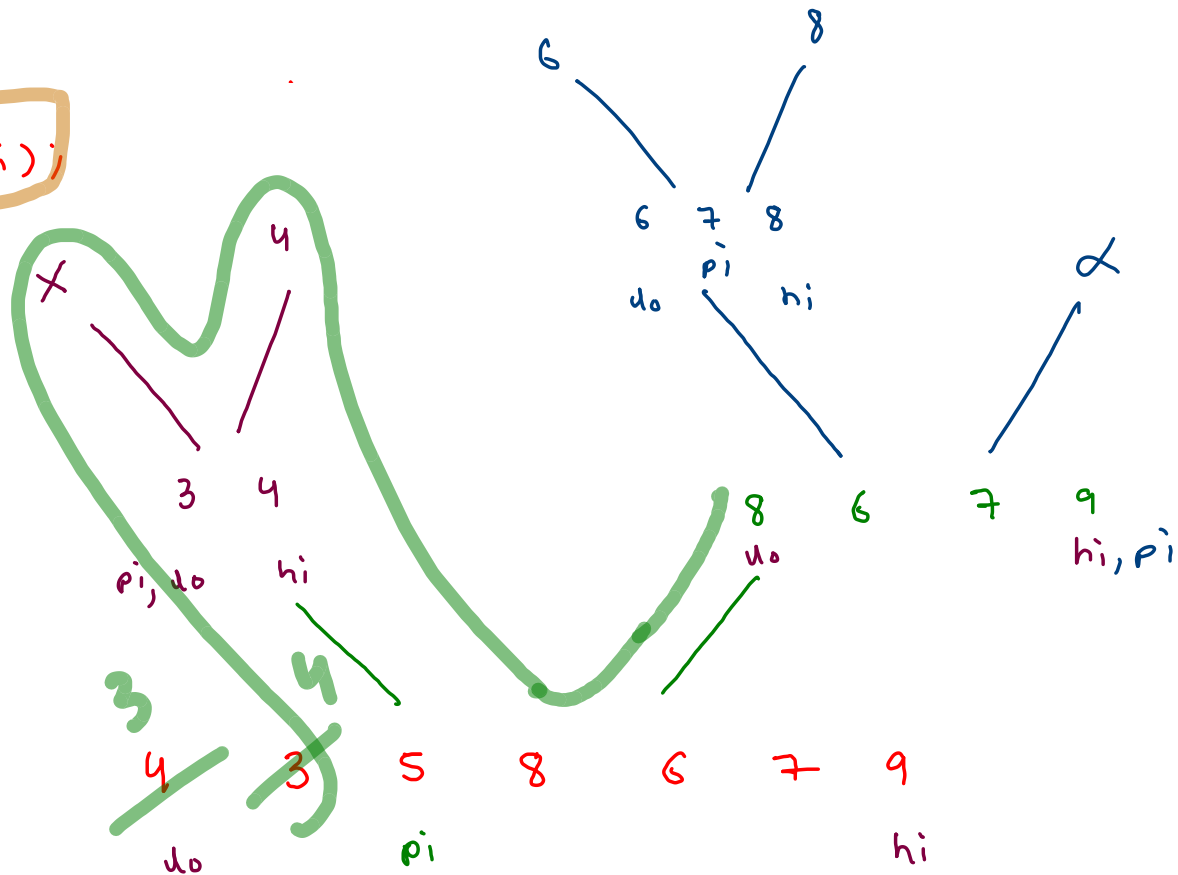
```
void qs (arr, lo, hi) {
```

```
    int pi = partition(arr, arr[hi], lo, hi);
```

```
    qs(arr, lo, pi-1);
```

```
    qs(arr, pi+1, hi);
```

```
}
```



411 =

2₀

3₂

4₂

5₃

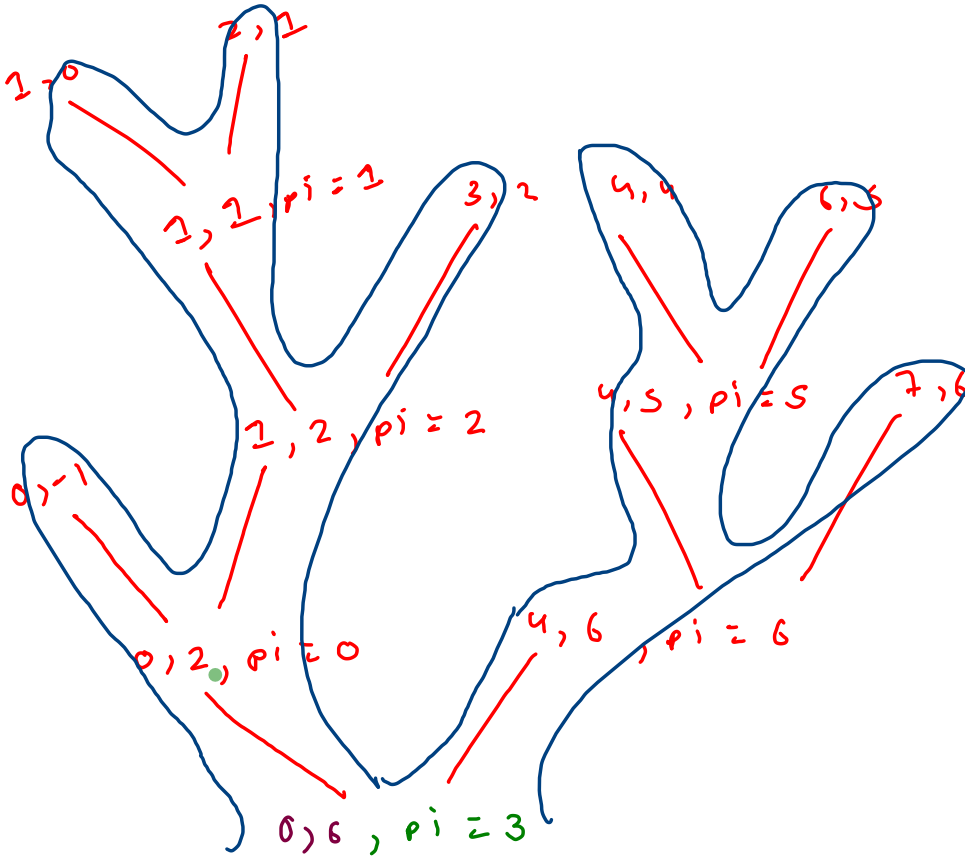
6₄

8₅

9₆

```
public static void quickSort(int[] arr, int lo, int hi) {  
    if(lo > hi) {  
        return;  
    }  
  
    int pi = partition(arr, arr[hi], lo, hi);  
    quickSort(arr, lo, pi-1);  
    quickSort(arr, pi+1, hi);  
}
```

```
int i = lo, j = hi;  
while (i <= j) {  
    if (arr[i] <= pivot) {  
        swap(arr, i, j);  
        i++;  
        j++;  
    } else {  
        i++;  
    }  
}  
System.out.println("pivot index -> " + (j - 1));  
return (j - 1);
```



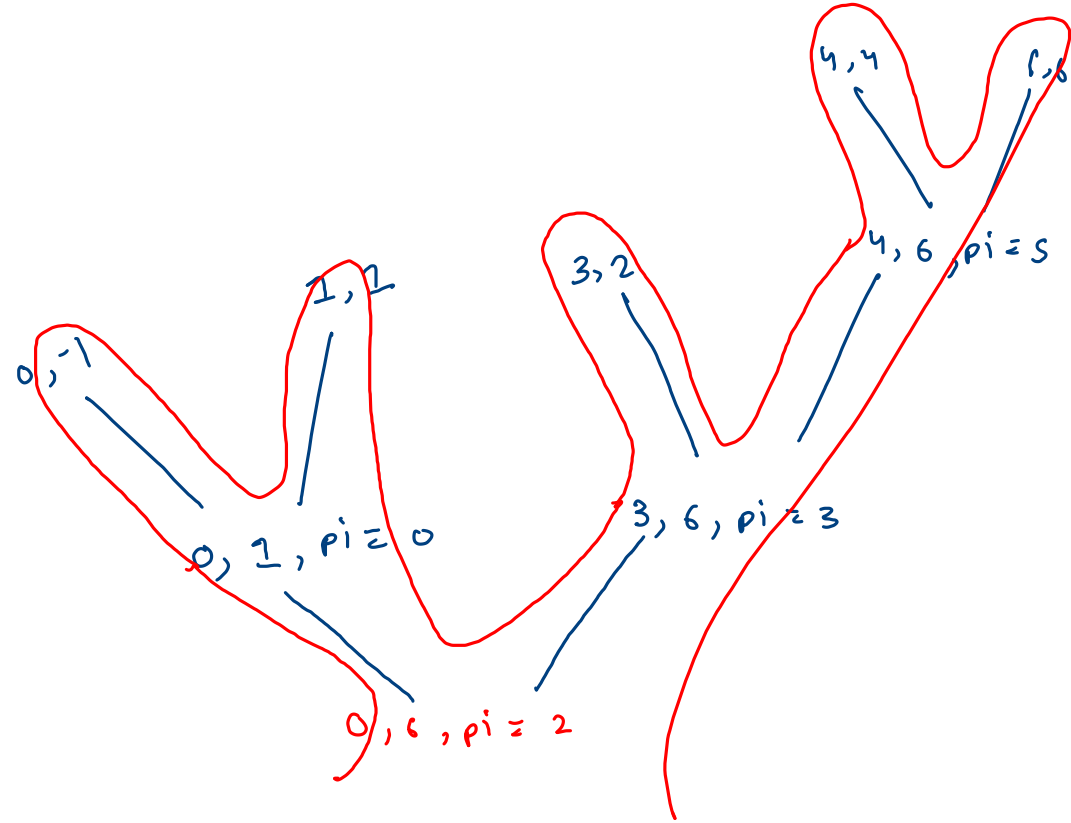
arr ;

| | | | | | | |
|---|---|---|---|---|---|---|
| 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |

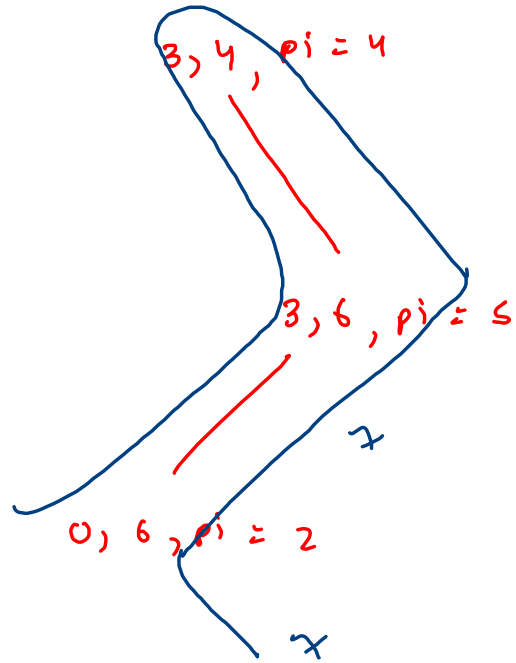
```
public static void quickSort(int[] arr, int lo, int hi) {  
    if (lo > hi) {  
        return;  
    }  
  
    int pi = partition(arr, arr[hi], lo, hi);  
    quickSort(arr, lo, pi-1);  
    quickSort(arr, pi+1, hi);  
}
```

```
int i = lo, j = hi;  
while (i <= j) {  
    if (arr[i] <= pivot) {  
        swap(arr, i, j);  
        i++;  
        j++;  
    } else {  
        i++;  
    }  
}  
System.out.println("pivot index -> " + (j - 1));  
return (j - 1);
```

9 4 6 3 7 8 5



| | | | | | | |
|---|---|---|---|---|---|---|
| 4 | 3 | 5 | 6 | 7 | 8 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |



$k = 5$

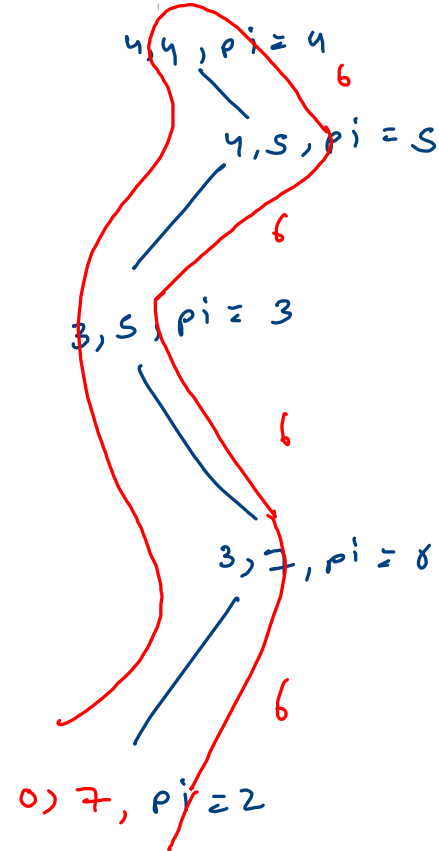
$idx = 4$

3 2 4 5 6 7 8 9
0 1 2 3 4 5 6 7

```
public static int quickSelect(int[] arr, int lo, int hi, int k) {
    //write your code here

    int pi = partition(arr, arr[hi], lo, hi);

    if(pi == k) {
        return arr[pi];
    }
    else if(pi < k) {
        return quickSelect(arr, pi+1, hi, k);
    }
    else {
        return quickSelect(arr, lo, pi-1, k);
    }
}
```



$k = 4$
 $(s + h \text{ small})$

count sort

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|
| 9 | 6 | 3 | 5 | 3 | 4 | 3 | 9 | 6 | 4 | 6 | 5 | 8 | 9 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 3 | 3 | 3 | 4 | 4 | 5 | 5 | 6 | 6 | 6 | 8 | 9 | 9 | 9 | 9 |

$$\text{min} = 3$$

$$\text{freq} \rightarrow 9 - 3 + 1 = 7$$

$$\text{max} = 9$$

| | | | | | | |
|---|---|---|---|---|---|---|
| 3 | 2 | 2 | 3 | 0 | 1 | 4 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |

(3) (4) (5) (6) (7) (8) (9)

| | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|
| 9 | 6 | 3 | 5 | 3 | 4 | 3 | 9 | 6 | 4 | 6 | 5 | 8 | 9 | 9 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 3 | 3 | 3 | 4 | 4 | 5 | 5 | 6 | 6 | 6 | 8 | 9 | 9 | 9 | 9 |

min = 3 max = 9

size = 7

freq

| (3) | (4) | (5) | (6) | (7) | (8) | (9) |
|-----|-----|-----|-----|-----|-----|-----|
| 3 | 2 | 2 | 3 | 0 | 1 | 4 |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 |

ps

| | | | | | | |
|--------------|--------------|--------------|---------------|----|----|---------------|
| 3 | 5 | 7 | 10 | 10 | 10 | 13 |
| 2 | 4 | 6 | 9 | | | 12 |
| 2 | | 5 | 8 | 7 | | 11 |
| 0 | 3 | | | | | |

```
//write your code here
int size = max - min + 1;
int[] freq = new int[size];

//fill freq array
for(int i=0; i < arr.length;i++) {
    .....
    freq[arr[i]-min]++;
}

//prefix sum array
int[] ps = new int[freq.length];
ps[0] = freq[0];

for(int i=1; i < freq.length;i++) {
    .....
    ps[i] = ps[i-1] + freq[i]; //0 to i ka sum
}

//create ans array
int[] ans = new int[arr.length];

for(int i=arr.length-1; i >= 0;i--) {
    int idx = ps[arr[i] - min] - 1;
    .....
    ans[idx] = arr[i];
    ps[arr[i]-min]--;
}
}
```


(i) stable sort

(ii) count sort \rightarrow stable sort

(iii) why stability \rightarrow radix sort

2 6 7
3 5 8
2 9 4

→ 2 9 4
2 6 7
3 5 8

→ 3 5 6
2 6 7
2 9 4

2 6 7
2 9 4
3 5 6

2 1 3 ✓

0 9 7 ✓

7 1 8 ✓

1 2 3 ✓

0 3 7 ✓

4 4 4 ✓

9 8 2 ✓

6 4 ✓

3 7 5 ✓

6 8 3 ✓

→

9 8 2 ✓

2 1 3 ✓

1 2 3 ✓

6 8 3 ✓

4 4 4 ✓

6 4 ✓

3 7 5 ✓

0 9 7 ✓

0 3 7 ✓

7 1 8 ✓

→

2 1 3 ✓

7 1 8 ✓

1 2 3 ✓

0 3 7 ✓

4 4 4 ✓ →

0 6 4 ✓

2 7 5 ✓

9 8 2 ✓

6 8 3 ✓

0 9 7 ✓

0 3 7

0 6 4

0 9 7

1 2 3

2 1 3

3 7 5

9 9 4

6 8 3

7 1 8

9 6 2

