

### 684. Redundant Connection

0, 1, ✓

1,4 ✓

S, 2 • ✓

2, 6

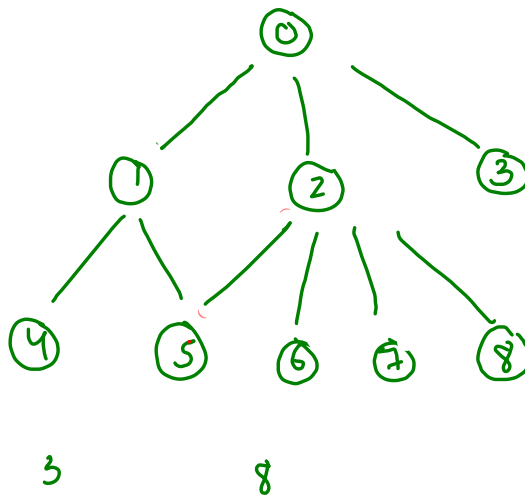
0, 2 ✓

6, 7 ✓

1.3.9

0, 3

7,8



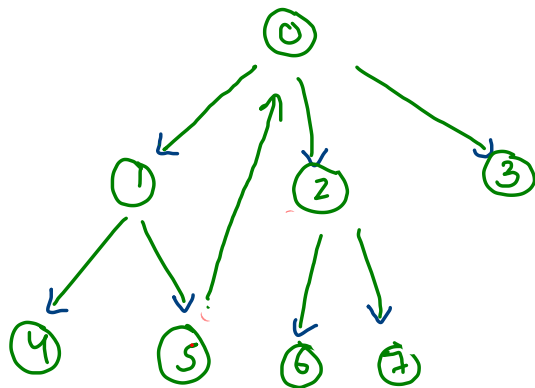
9 v  
8 edges

redundant connection

a connected acyclic graph is tree.

## 685. Redundant Connection II

cycle



0 3

1 4

2 6

1 5 ✓

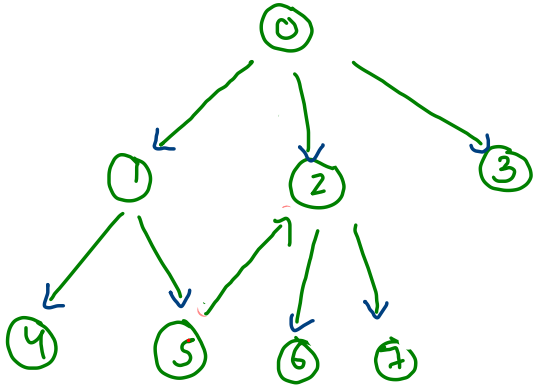
5 0 ✓

2 7

0 2

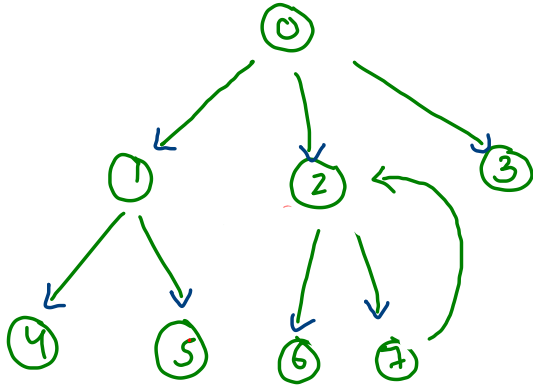
0 1 ✓

2 parent



(i) detect vtx which has  
2 parent.

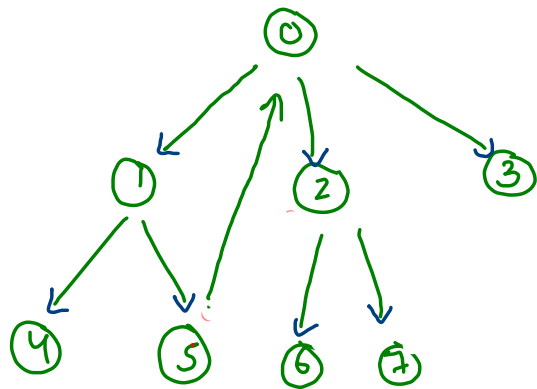
2 parent, cycle



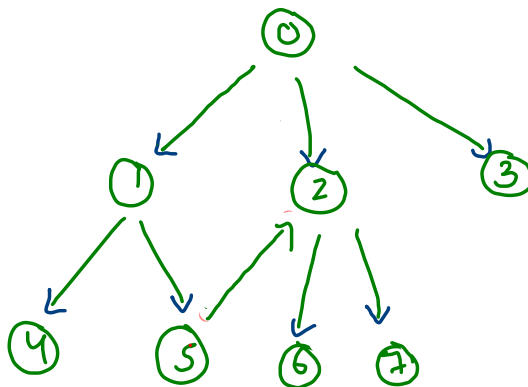
$\alpha$  0 2

$\alpha$  2 7

$\sim$  7 2



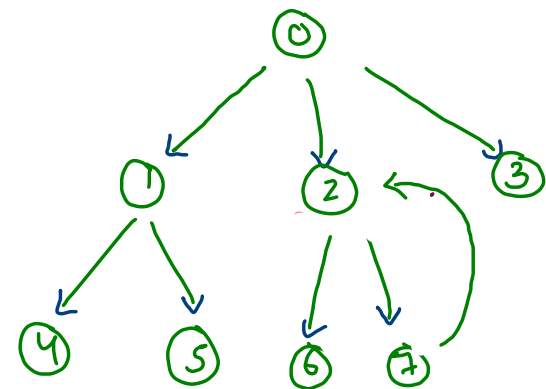
cycle



2 parent +

bd1

bd2



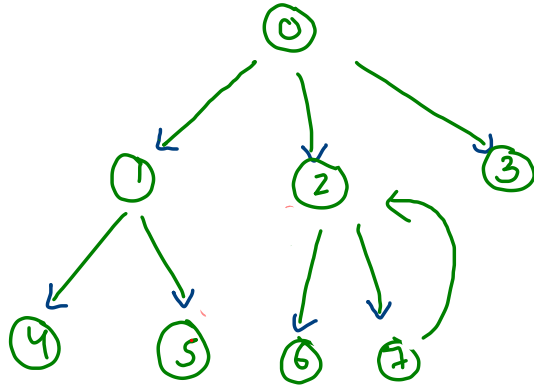
2 parent, cycle

DSU (same: cycle, 1 cycle)

RC 1

-1	-1	-1	-1	-1	-1	-1	-1
0	1	2	3	4	5	6	7

2 Parent , cycle



0 → 7 2

1 → 0 3

2 → 2 6

3 → 1 4

4 → 2 7

5 → 0 2

6 → 0 1

7 → 1 5

bl1

bl2

-1	-1	-1	-1	-1	-1	-1	-1
0	1	2	3	4	5	6	7

```

int bl1 = -1;
int bl2 = -1;
for(int i=0; i < edges.length;i++) {
    int u = edges[i][0]; u--;
    int v = edges[i][1]; v--;

    if(indegree[v] == -1) {
        indegree[v] = i;
    }
    else {
        bl1 = indegree[v];
        bl2 = i;
        break;
    }
}

if(bl1 == -1) {
    //case 1 : cycle
    int ei = dsu(-1,edges);
    return edges[ei];
}
else {
    //case 2 : 2 parent, case3 : 2 parent & cycle
    int ei = dsu(bl2,edges);
    if(ei == -1) {
        return edges[bl2];
    }
    else {
        return edges[bl1];
    }
}

```

# Eulerian path & circuit

Eulerian Path is a path in graph that visits every edge exactly once. (travel all edges exactly once)

Undirected graph : (i) if all vertices have even degree  $\rightarrow$  eulerian circuit

(ii) if  $(V-2)$  vertices have even degree  $\rightarrow$  eulerian path  
but any two have odd degree.

---

$\hookrightarrow$  use one of them as source and the other one as dest.

directed graph : (i) each vertex  $\text{indegree} = \text{outdegree}$  — eulerian circuit

(ii)  $(v-2)$  vertices have  $\text{indegree} = \text{outdegree}$

two vertices, one of them should have extra  
 $\text{indegree (dest)}$  and the other should

have extra  $\text{outdegree (src)}$ .