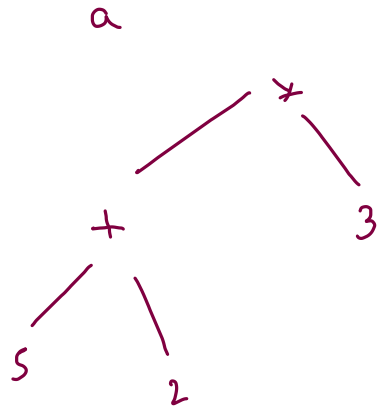


Expressions

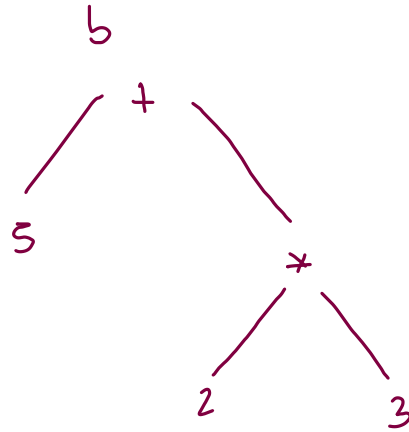
- infix $a + b$
- prefix $+ab$
- postfix $ab +$



inorder : $5 + 2 * 3$

preorder : $* + 5 2 3$

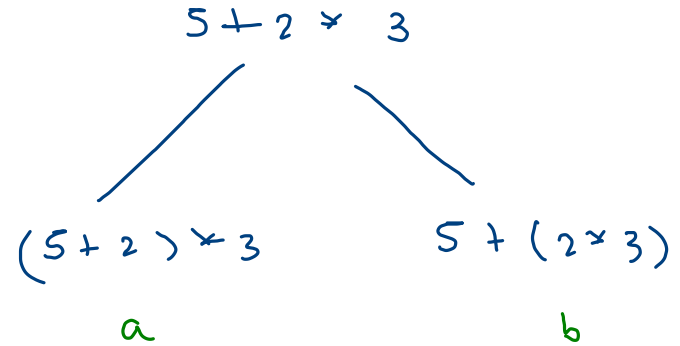
postorder : $5 2 + 3 *$



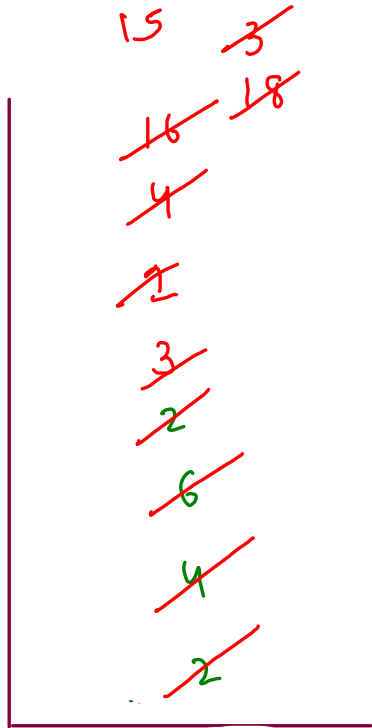
$5 + 2 * 3$

$+ 5 * 2 3$

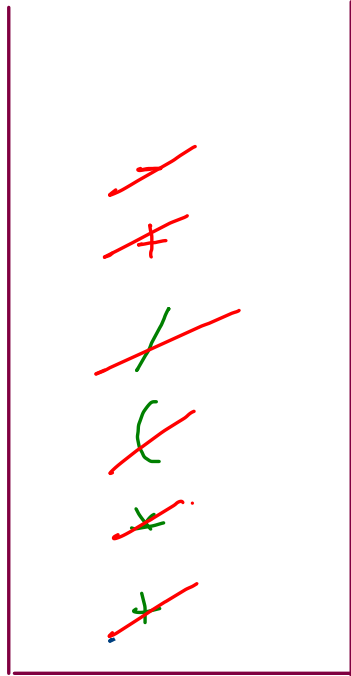
$5 2 3 * +$



$$2 + 4 * (6 / 2 + 1) - 3$$



Operand



Operator

(i) operand \rightarrow push it in operand stack.

(ii) operator \rightarrow evaluate high or equal operator first, then push this current operator.

(iii) (\rightarrow push it in operator stack.

(iv)) \rightarrow evaluate till opening.

$$2 + 4 * (6 / 2 + 1) - 3.$$

```
public static int infix_evaluation(String exp) {
    Stack<Integer>operand = new Stack<>();
    Stack<Character>operator = new Stack<>();

    for(int i=0; i < exp.length(); i++) {
        char ch = exp.charAt(i);

        if(ch == '(') {
            operator.push(ch);
        }
        else if(ch >= '0' && ch <= '9') {
            //ch -> operand
            operand.push(ch-'0');
        }
        else if(ch == ')') {
            //evaluate till opening bracket
            while(operator.peek() != '(') {
                char opr = operator.pop();
                int b = operand.pop();
                int a = operand.pop();

                int val = calculate(a,b,opr);
                operand.push(val);
            }
            operator.pop(); //pop '('
        }
        else if(ch == '+' || ch == '-' || ch == '*' || ch == '/') {
            //ch -> operator
            while(operator.size() > 0 && operator.peek() != '(' && priority(ch) <= priority(operator.peek())) {
                char opr = operator.pop();
                int b = operand.pop();
                int a = operand.pop();

                int val = calculate(a,b,opr);
                operand.push(val);
            }
            operator.push(ch);
        }
    }

    while(operator.size() > 0) {
        char opr = operator.pop();
        int b = operand.pop();
        int a = operand.pop();

        int val = calculate(a,b,opr);
        operand.push(val);
    }
}
```

```
public static int calculate(int a,int b,char opr) {
    if(opr == '+') {
        return a+b;
    }
    else if(opr == '-') {
        return a-b;
    }
    else if(opr == '*') {
        return a*b;
    }
    else if(opr == '/') {
        return a/b;
    }
    else {
        return -1;
    }
}
```

```
public static int priority(char opr) {
    if(opr == '+' || opr == '-') {
        return 1;
    }
    else if(opr == '*' || opr == '/') {
        return 2;
    }
    else {
        return -1;
    }
}
```

3
~~18~~
~~16~~
4
~~2~~
3
~~2~~
~~6~~
4
~~2~~

operand

~~+~~
~~+~~
~~+~~
~~+~~
~~+~~
~~+~~

operator

$$/^{*}a+-bcde$$

Handwritten notes for 'L' and 'K'.

L

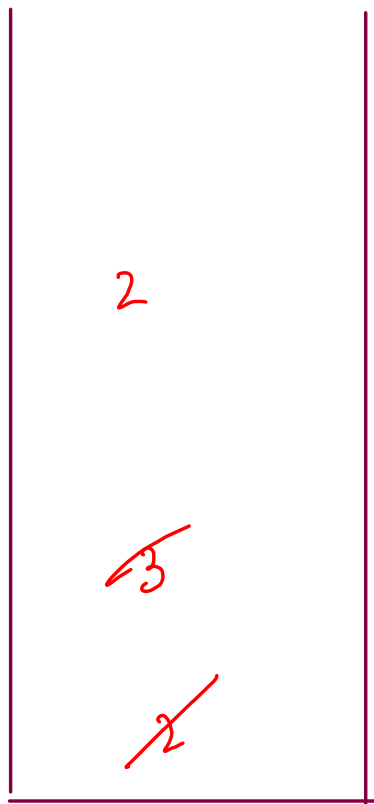
- Handwritten 'L' with a red checkmark.
- Handwritten 'L' with a red checkmark.
- Handwritten 'L' with a red checkmark.
- Handwritten 'L' with a red checkmark.
- Handwritten 'L' with a red checkmark.

K

- Handwritten 'K' with a red checkmark.
- Handwritten 'K' with a red checkmark.
- Handwritten 'K' with a red checkmark.
- Handwritten 'K' with a red checkmark.
- Handwritten 'K' with a red checkmark.

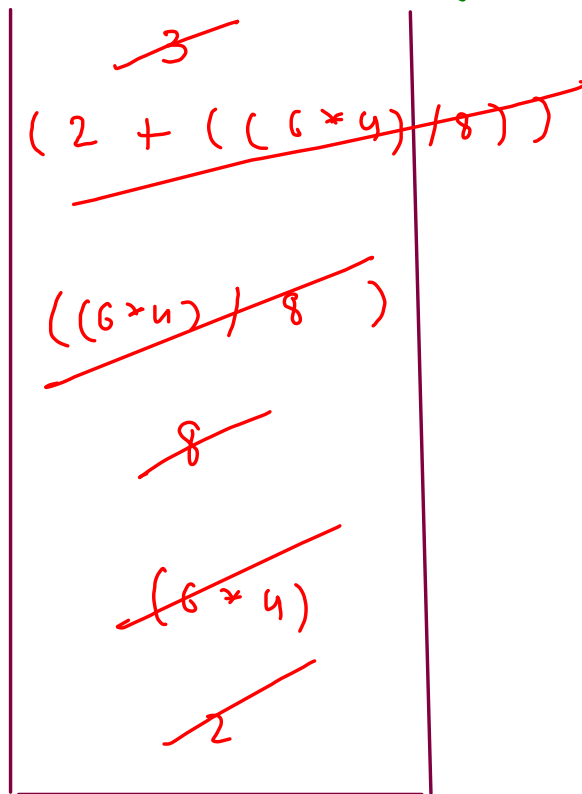
$$/ x a + - b c d e /$$
$$\begin{array}{l} \cancel{e} \\ \cancel{* a + -bcd} \\ \cancel{+ -bcd} \\ \cancel{d} \\ \cancel{-bc} \\ \cancel{c} \\ \cancel{b} \\ \cancel{a} \end{array}$$
$$abc - 2 + xef$$
$$\begin{array}{r} \cancel{a} \cancel{bc} - \cancel{d} + x \\ \cancel{bc} - \cancel{d} + \\ \cancel{d} \\ \cancel{bc} - \\ \cancel{c} \\ \cancel{b} \\ \cancel{a} \end{array}$$

$$2 \ 6 \ 4 \ * \ 8 \ / \ + \ 3 \ -$$



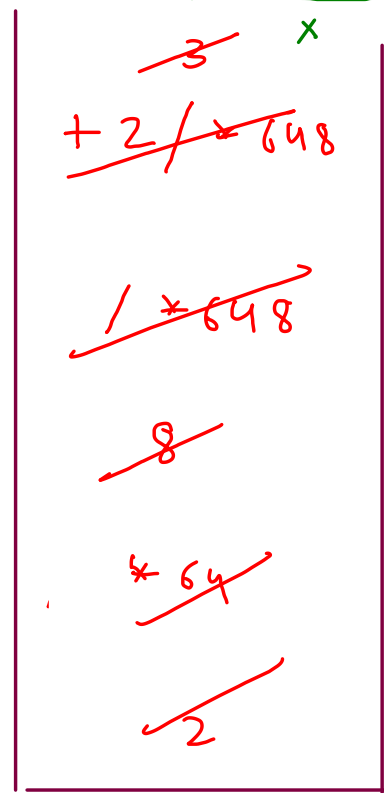
evaluation

$$\underbrace{((2 + ((6 * 4) / 8)))}_{x} - \underbrace{3}_{y}$$



infix

$$\underbrace{+ \ 2 \ / \ * \ 6 \ 4 \ 8 \ 3}_{x} \quad y$$



postfix

$$\begin{aligned} &2 \\ &((2 + ((6 * 4) / 8)) - 3) \\ &- + 2 / * 6 4 8 3 \end{aligned}$$

$-+2/*6483$

~~2~~
~~8~~
~~2~~
~~3~~
~~24~~
~~8~~
~~3~~

eval

$((2 + ((6 * 4) / 8)) - 3)$

~~$(2 + ((6 * 4) / 8))$~~

~~2~~
 ~~$((6 * 4) / 8)$~~

~~$(6 * 4)$~~
~~6~~

~~4~~
~~8~~
~~3~~

infix

$264 * 8 / + 3 -$

~~$264 * 8 / +$~~
~~2~~
 ~~$64 * 8 /$~~

~~$64 *$~~
~~6~~
~~4~~
~~8~~
~~3~~

postfix

queue introduction

FIFO



q.add(10)

q.add(20)

q.add(30)

q.remove() → 10

q.peek() → 20

add

remove

peek

size

$$n = 3$$

0 1 0

0 1 1

1 0 1

1 1 0

1 1 1

0	1	0	10	11	010	011	101	110	111
--------------	--------------	--------------	---------------	---------------	-----	-----	-----	-----	-----

01
|
0

10 11
 \ /
 1