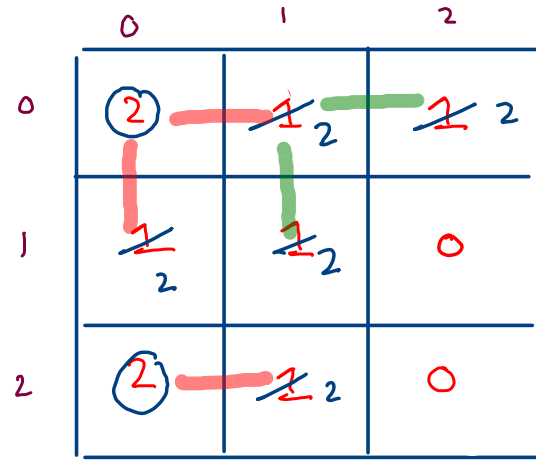


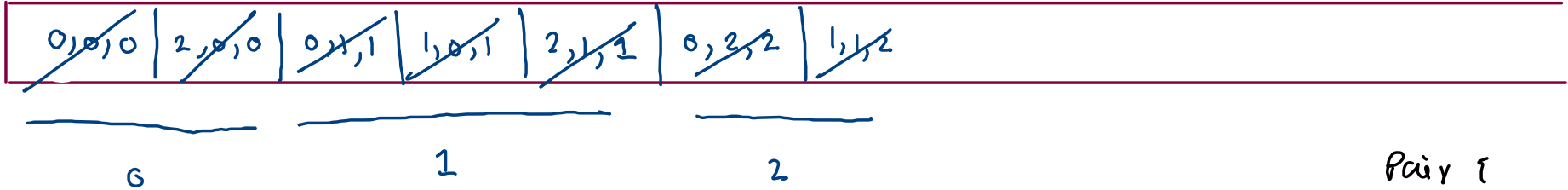
Rotting Oranges

```
[[2,1,1],[1,1,0],[0,1,1]]
```

ans: 2



(i) multiple src



pair {
 int i;
 int j;
 int t;

BFS

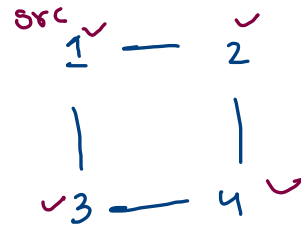
remove

mark *

work

add unvisited nbr

marking on
removal



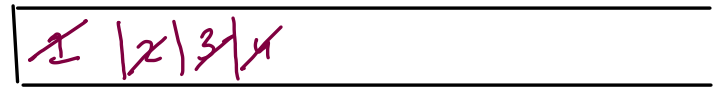
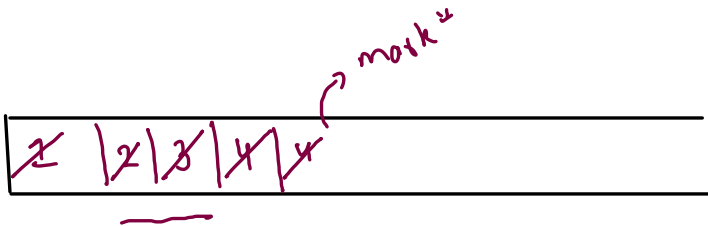
remove

work

add unvisited

→ mark nbr

marking on addition



```

//bfs
int ans = 0;
while(q.size() > 0) {
    Pair rem = q.remove();

    ans = rem.t;

    //add unvisited nbr
    for(int k=0; k < 4;k++) {
        int ni = rem.i + dir[k][0];
        int nj = rem.j + dir[k][1];

        if(ni >= 0 && ni < grid.length && nj >= 0 && nj < grid[0].length && grid[ni][nj] == 1) {
            q.add(new Pair(ni,nj,rem.t + 1));
            grid[ni][nj] = 2; //marking on addition
        }
    }
}

return fo == 0 ? ans : -1;

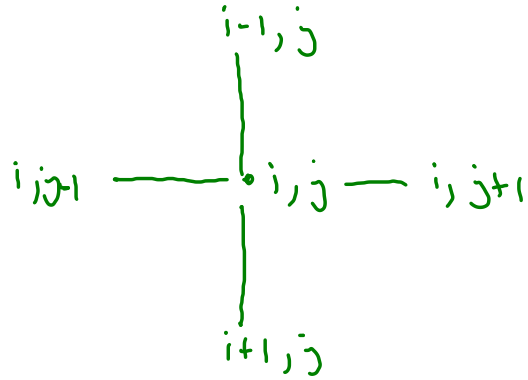
```

ans = 4

	0	1	2	3
0	0	2	0	2
1	1 ²	1 ²	1 ²	1 ²
2	2	1 ²	0	0
3	0	1 ²	0	0

$10 = 7$
 6
 8
 4
 3
 2
 20

0,1,0	2,0,0	1,1,1	1,0,1	2,1,1	1,2,2	3,1,2	1,3,3	0,3,4
0	1	2	3	4				



	0	1	2
0	0	1	0
1	1	2	1
2	0	1	0

```
int[][] dir = {{-1, 0}, {0, -1}, {1, 0}, {0, 1}};
```

\uparrow
 \downarrow
 \leftarrow
 \rightarrow

$1, 1, 0$

$0, 1, 2$

```
//add unvisited nbr
for(int k=0; k < 4; k++) {
    int ni = rem.i + dir[k][0];
    int nj = rem.j + dir[k][1];

    if(ni >= 0 && ni < grid.length && nj >= 0 && nj < grid[0].length && grid[ni][nj] == 1) {
        q.add(new Pair(ni, nj, rem.t + 1));
        grid[ni][nj] = 2; //marking on addition
    }
}
```

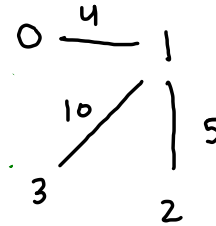
Minimum Cost To Connect All Cities

There are n cities and there are roads in between some of the cities. Somehow all the roads are damaged simultaneously. We have to repair the roads to connect the cities again. There is a fixed cost to repair a particular road. Find out the minimum cost to connect all the cities by repairing roads.

0 — 1	4
1 — 2	5
1 — 3	10
0 — 3	15

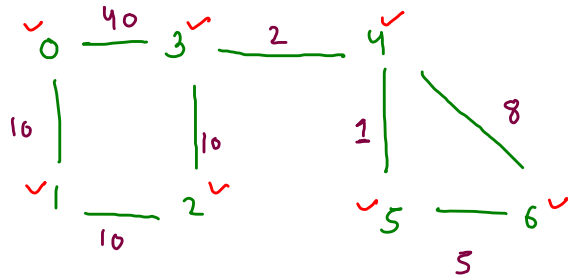
MST

(Prims)



Dijkstra: (i) Shortest path (single src all dest)

(ii) Failure: fails on -ve wt (greedy)



remove
mark*
work
add unvisited nbr

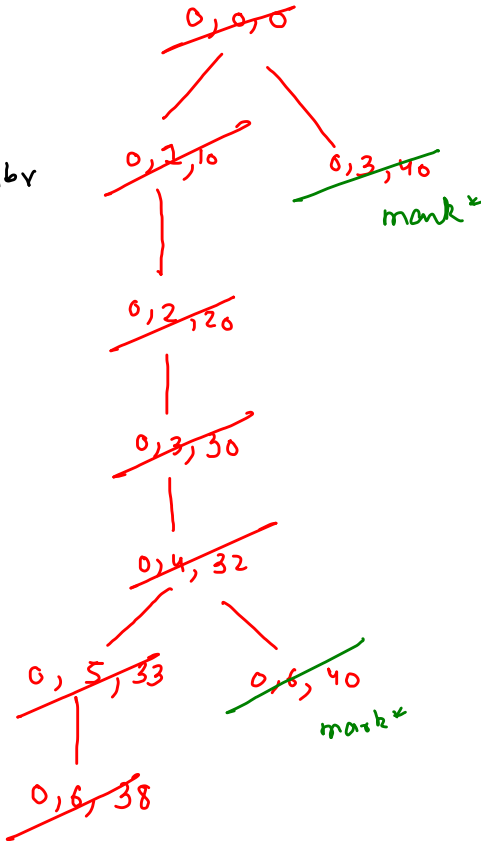
0	10	20	30	32	33	38
0	1	2	3	4	5	6

src to 4 ans

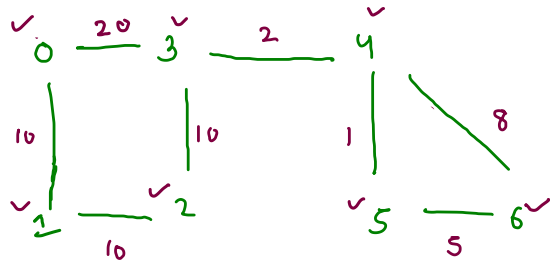
src, dest, wsf

src = 0

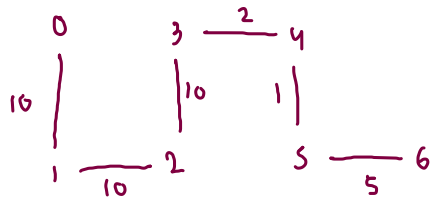
u, v, wsf



Prims : (i) MST (minimum spanning tree)



remove
mark =
work
add unvisited nbr



v, aq, wt

~~0, -1, 0~~

Tree : A connected
acyclic graph is
a tree.

~~3, 0, 20~~
continue

~~1, 0, 10~~

~~2, 1, 10~~

~~3, 2, 10~~

~~4, 3, 2~~

~~5, 4, 1~~

~~6, 4, 8~~
continue

~~6, 5, 5~~

min cost to connect all cities

```
public static int minCost(ArrayList<ArrayList<Edge>>graph) {
    int cost = 0;
    PriorityQueue<Edge>pq = new PriorityQueue<>();

    pq.add(new Edge(0,0));
    boolean[]vis = new boolean[graph.size()];

    while(pq.size() > 0) {
        //remove
        Edge rem = pq.remove();

        //mark*
        if(vis[rem.v] == true) {
            continue;
        }
        vis[rem.v] = true;

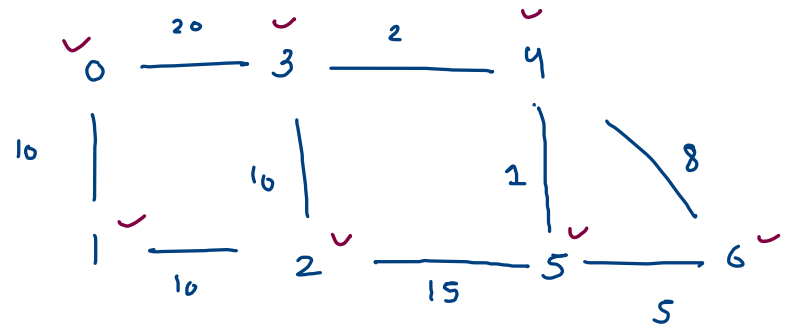
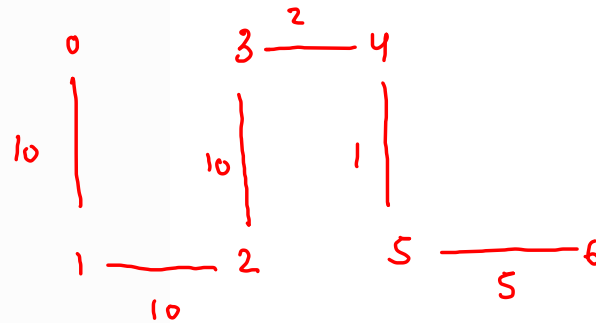
        //work
        cost += rem.wt;

        //add unvisited nbr
        for(Edge edge : graph.get(rem.v)) {
            int nbr = edge.v;
            int wt = edge.wt;

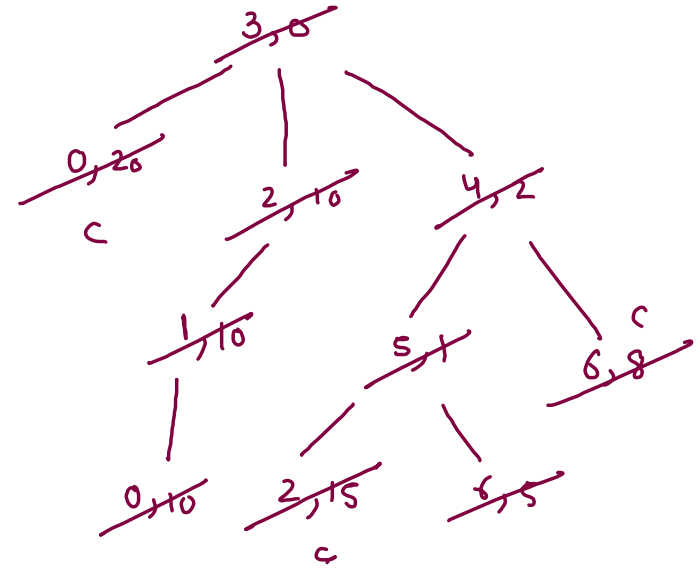
            if(vis[nbr] == false) {
                pq.add(new Edge(nbr,wt));
            }
        }
    }

    return cost;
}
```

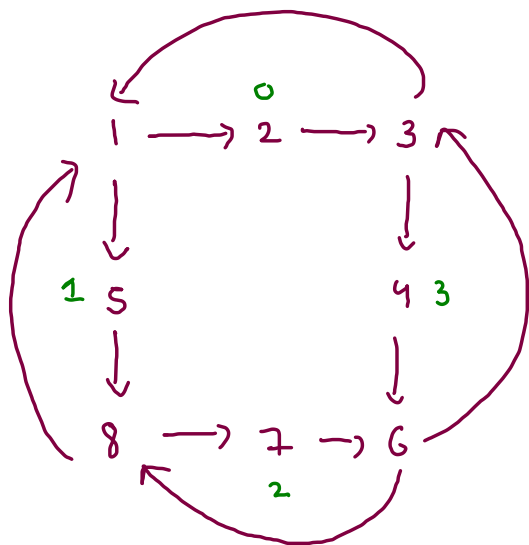
cost : 2 + 1 + 5 + 10 + 10 + 10



v, wt



815. Bus Routes

$$[\underset{0}{[1, 2, 3]}, \underset{1}{[1, 5, 8]}, \underset{2}{[8, 7, 6]}, \underset{3}{[3, 4, 6]}]$$


src bs = 2

dest bs = 6

$$2 \xrightarrow{0} 1 \xrightarrow{1} 8 \xrightarrow{2} 6 \quad (\text{bases: } 3)$$
$$2 \xrightarrow{0} 3 \xrightarrow{3} 6 \quad (\text{bytes: } 2)$$

routes: $\left[\begin{matrix} [1, 2, 3] \\ 0 \end{matrix}, \begin{matrix} [1, 5, 8] \\ 1 \end{matrix}, \begin{matrix} [8, 7, 6] \\ 2 \end{matrix}, \begin{matrix} [3, 4, 6] \\ 3 \end{matrix} \right]$

1 \rightarrow 0, 1

2 \rightarrow 0

3 \rightarrow 0, 3

4 \rightarrow 3

5 \rightarrow 1

6 \rightarrow 2, 3

7 \rightarrow 2

8 \rightarrow 1, 2

map

map: bus stand vs bus

Integer vs $AL < Integer >$

bfs, marking on addition

Normal BFS

vis: bus stand

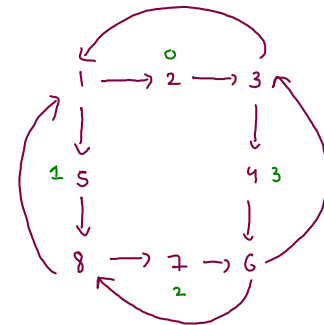
vis: buses

Pair $\{$

int bus_stand;

int den;

$\}$



routes: $\left[\begin{matrix} [1, 2, 3] \\ 0 \end{matrix}, \begin{matrix} [1, 5, 8] \\ 1 \end{matrix}, \begin{matrix} [8, 7, 6] \\ 2 \end{matrix}, \begin{matrix} [3, 4, 6] \\ 3 \end{matrix} \right]$

1 \rightarrow 0, 1

2 \rightarrow 0

3 \rightarrow 0, 3

4 \rightarrow 3

5 \rightarrow 1

6 \rightarrow 2, 3

7 \rightarrow 2

8 \rightarrow 1, 2

map

vis \rightarrow bus stand : 2, 1, 3, 5, 8, 4, 6, 7

bus : 0, 1, 3, 2

src = 2

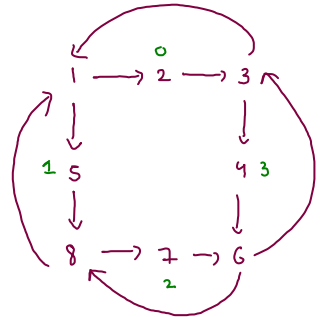
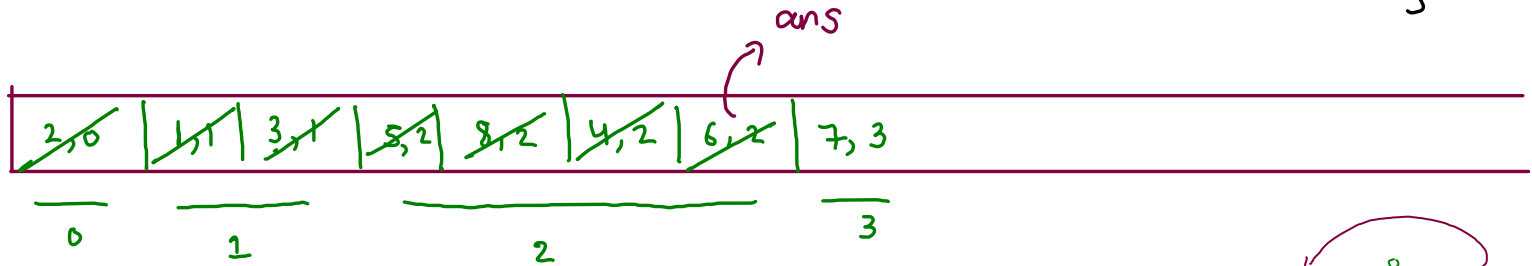
dest = 6

Pair {

bus stand;

int den;

}



map: bus stand vs bus

```

for(int i=0; i < routes.length;i++) {
    for(int j=0; j < routes[i].length;j++) {
        int bus_no = i;
        int bus_stop_no = routes[i][j];

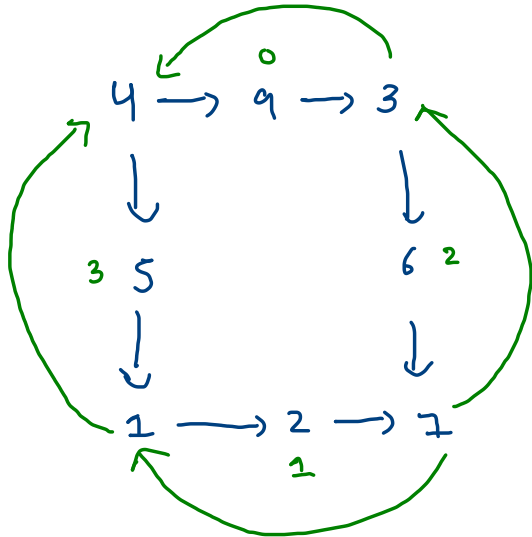
        if(map.containsKey(bus_stop_no) == false) {
            ArrayList<Integer>list = new ArrayList<>();
            list.add(bus_no);
            map.put(bus_stop_no,list);
        }
        else {
            ArrayList<Integer>list = map.get(bus_stop_no);
            list.add(bus_no);
            map.put(bus_stop_no,list);
        }
    }
}

```

routes :

[[4,9,3], [1,2,7], [3,6,7], [4,5,1]]

0
1
2
3



bus stop vs buses

4 → 0,3

9 → 0

3 → 0,2

1 → 1,3

2 → 1

7 → 1,2

6 → 2

5 → 3

```
q.add(new Pair(src,0));
bus_stop_vis.add(src); //marking on addition

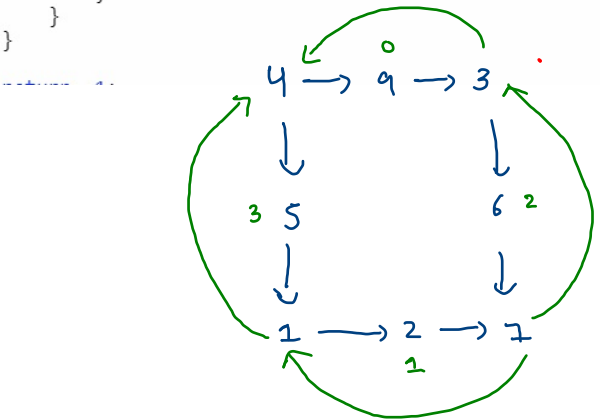
while(q.size() > 0) {
    //remove
    Pair rem = q.remove();

    //work
    if(rem.bus_stop == dest) {
        return rem.lev;
    }

    //add unvisited nbr
    ArrayList<Integer>buses = map.get(rem.bus_stop);

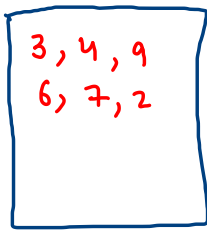
    for(int bus : buses) {
        if(bus_vis.contains(bus) == false) {
            bus_vis.add(bus);

            //travel all the unvisited bus_stop of this bus
            for(int bus_stop : routes[bus]) {
                if(bus_stop_vis.contains(bus_stop) == false) {
                    q.add(new Pair(bus_stop,rem.lev + 1));
                    bus_stop_vis.add(bus_stop);
                }
            }
        }
    }
}
```

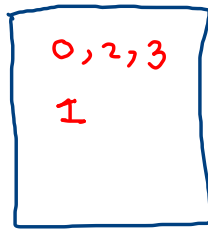


4 -> 0,3
9 -> 0
3 -> 0,2
1 -> 1,3
2 -> 1
7 -> 1,2
6 -> 2
5 -> 3

bus_stop_vis



bus_vis



bus_stop vs buses

src = 3
dest = 5

ans = 2

