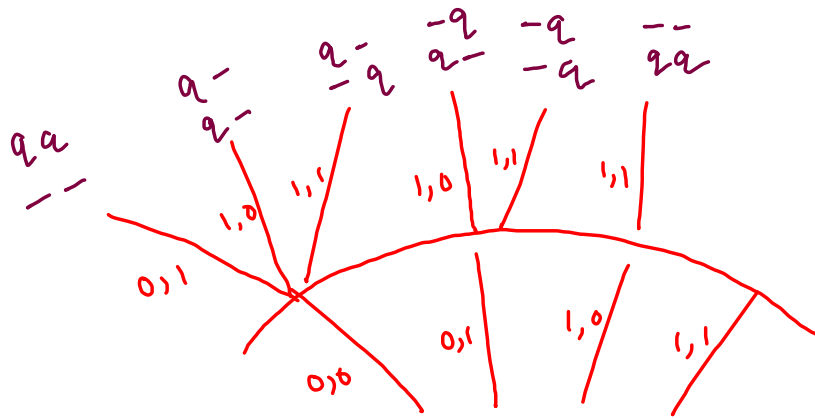


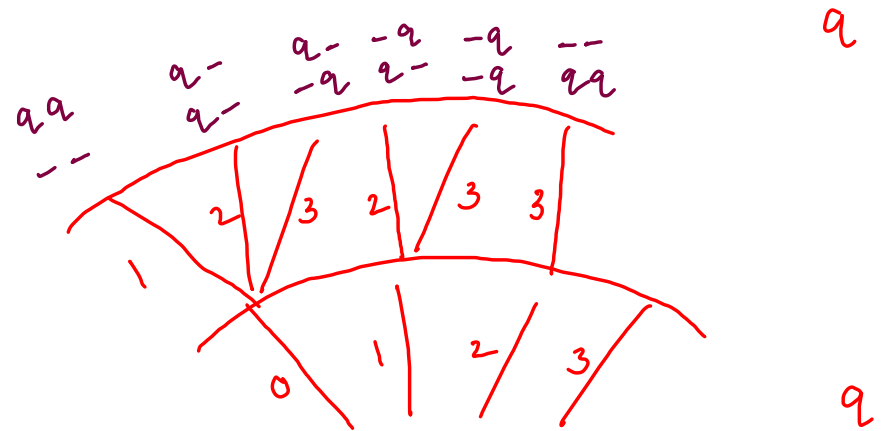
	0	1
0		
1		

queen combinations  
(queen chooses)

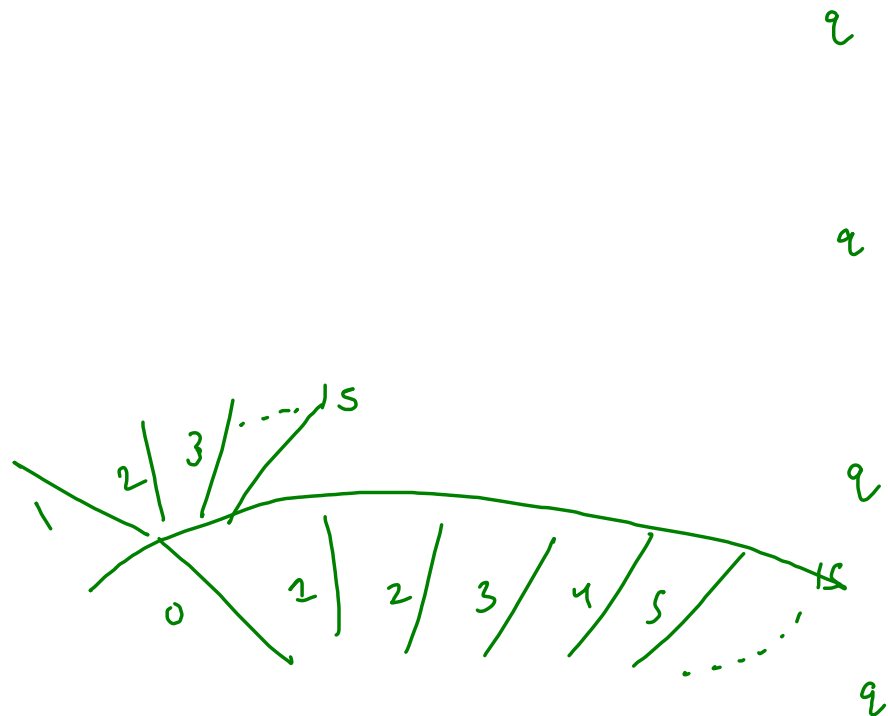
2d as 2d

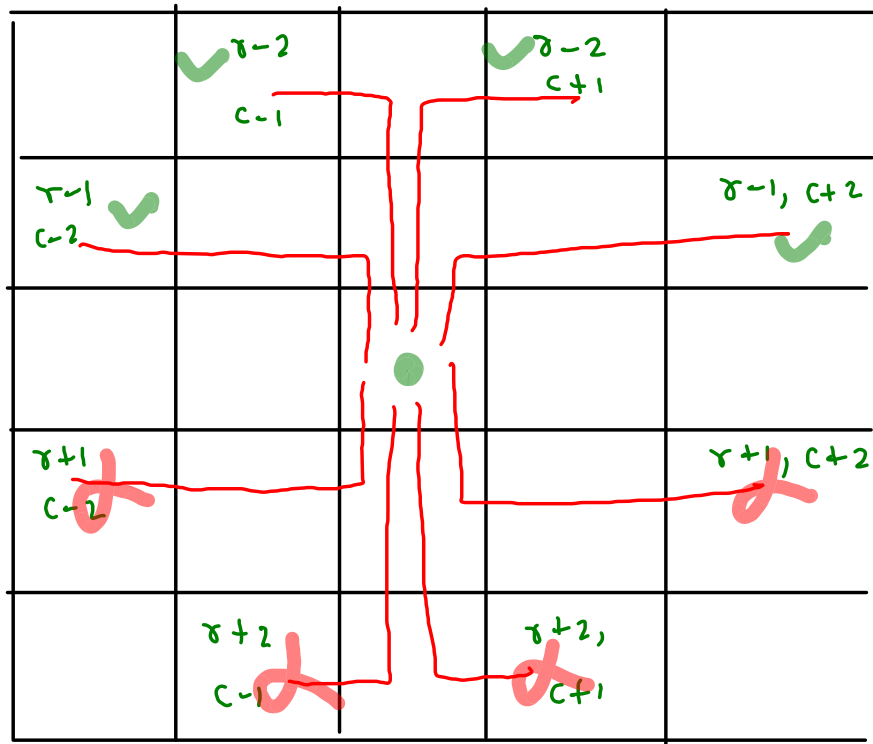


2d as 1d



0	1	2	3
4	5	(i, j)	7
8	9	10	11
12	13	14	15





# queen permutation

	q		
			q
q			
		q	

1 24

		q	
q			
			q
	q		

1  
24

	q <sub>1</sub>		
			q <sub>2</sub>
q <sub>3</sub>			
		q <sub>4</sub>	

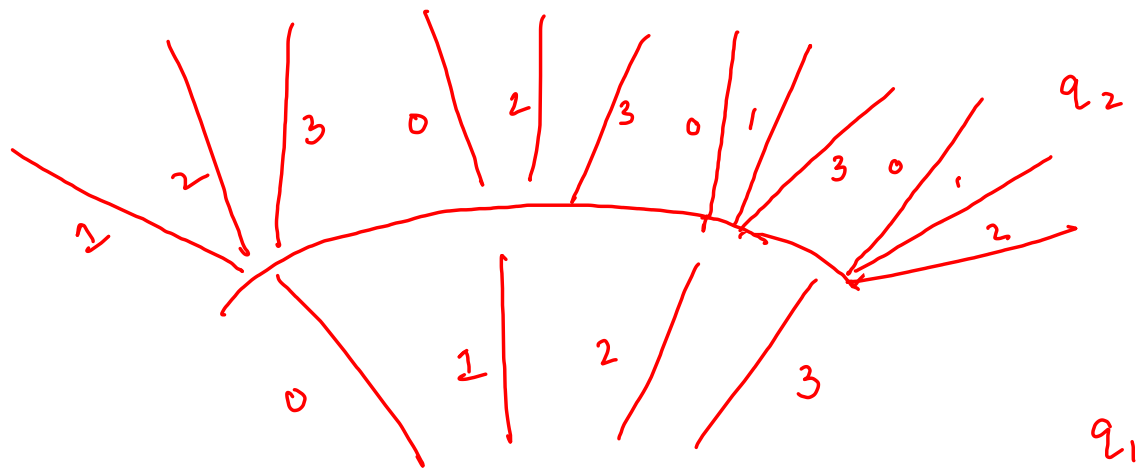
	q <sub>1</sub>		
			q <sub>2</sub>
q <sub>4</sub>			
		q <sub>3</sub>	

	q <sub>1</sub>		
			q <sub>3</sub>
q <sub>2</sub>			
		q	

98 permutation

	0	1
0	0	1
1	2	3

$$4p_2 = 12$$



top : -1, 0

left : 0, -1

down : 1, 0

right : 0, 1

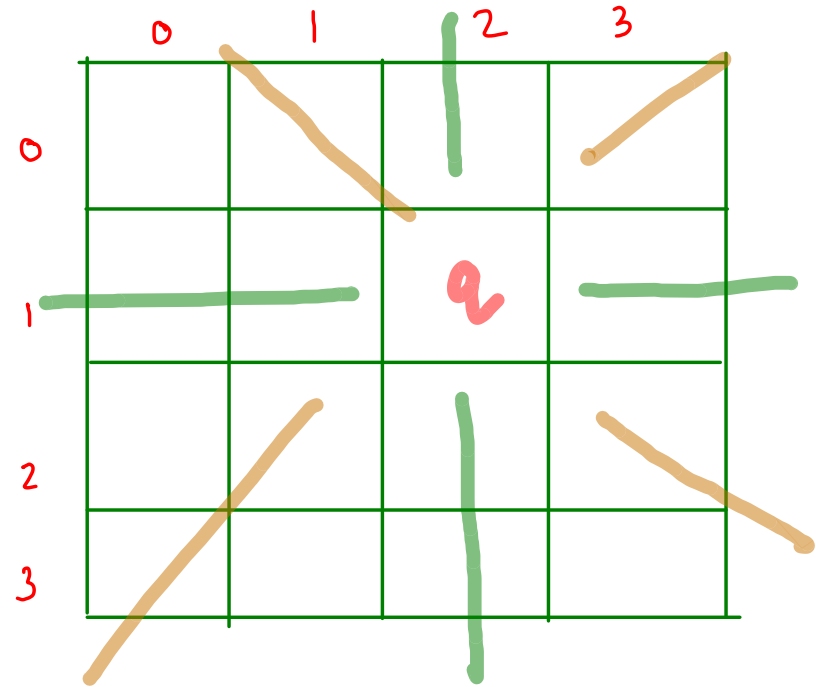
top-left diagonal : -1, -1

bottom-left diagonal : 1, -1

top-right diagonal : -1, 1

bottom-right diagonal : 1, 1

```
public static void nqueens(int qpsf, int N, int[][] chess) {  
    // write your code here  
    if(qpsf == N) {  
        for(int i=0; i < N; i++) {  
            for(int j=0; j < N; j++) {  
                if(chess[i][j] == 0) {  
                    System.out.print("-\t");  
                }  
                else {  
                    System.out.print("q" + chess[i][j] + "\t");  
                }  
            }  
            System.out.println();  
        }  
        System.out.println();  
        return;  
    }  
  
    for(int b = 0; b < N*N ; b++) {  
        int i = b / N;  
        int j = b % N;  
  
        if(chess[i][j] == 0 && isQueenSafe(chess, i, j) == true) {  
            chess[i][j] = qpsf+1;  
            nqueens(qpsf+1, N, chess);  
            chess[i][j] = 0;  
        }  
    }  
}
```



```

public static boolean IsQueenSafe(int[][] chess, int row, int col) {
    int[][] dir = {{-1,0},{1,0},{0,-1},{0,1},{-1,-1},{1,-1},{-1,1},{1,1}};

    for(int k=0; k < 8; k++) {
        for(int i = row + dir[k][0], j = col + dir[k][1]; i >= 0 && i < chess.length && j >= 0 && j < chess[0].length; ) {
            if(chess[i][j] == true) {
                return false;
            }
            i += dir[k][0];
            j += dir[k][1];
        }
    }

    return true;
}

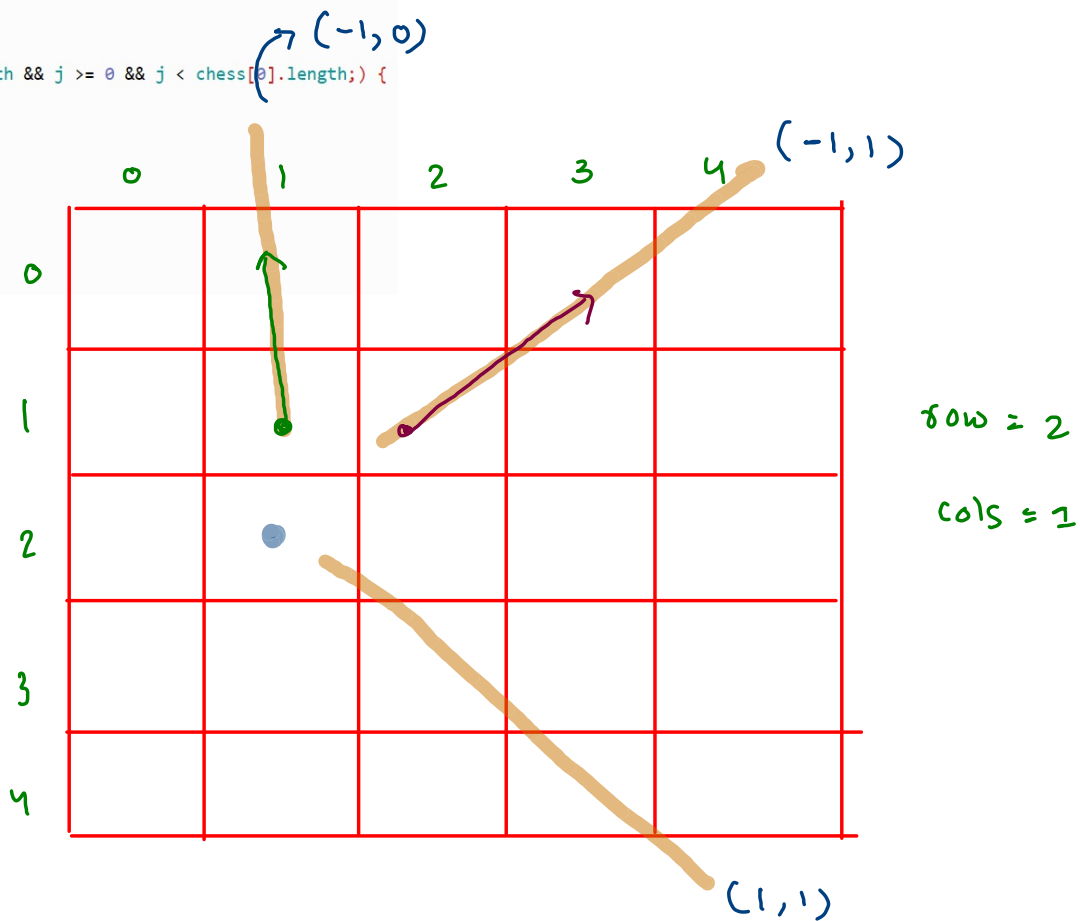
```

$dir[k][0] = -1$

$dir[k][1] = 1$

$i = -1$

$j = 4$



	0	1	2	3
0	0	1	2	3
1	4	5	6	7
2	8	9	10	11

$bno \rightarrow i, j$

$i = bno / cols;$

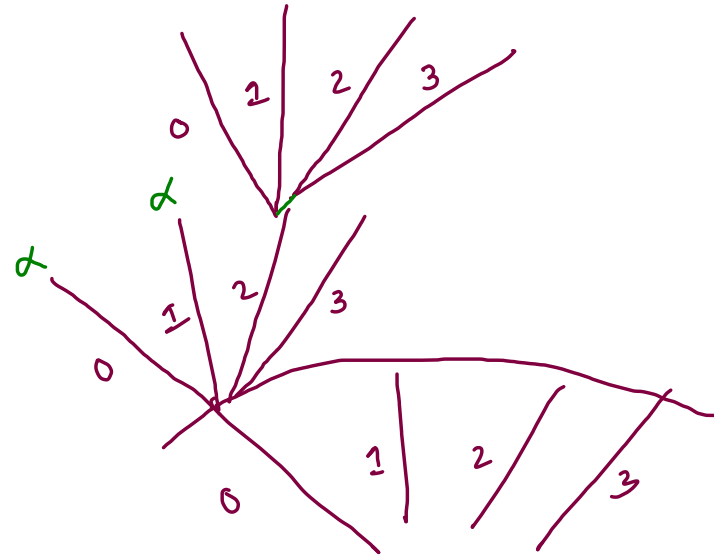
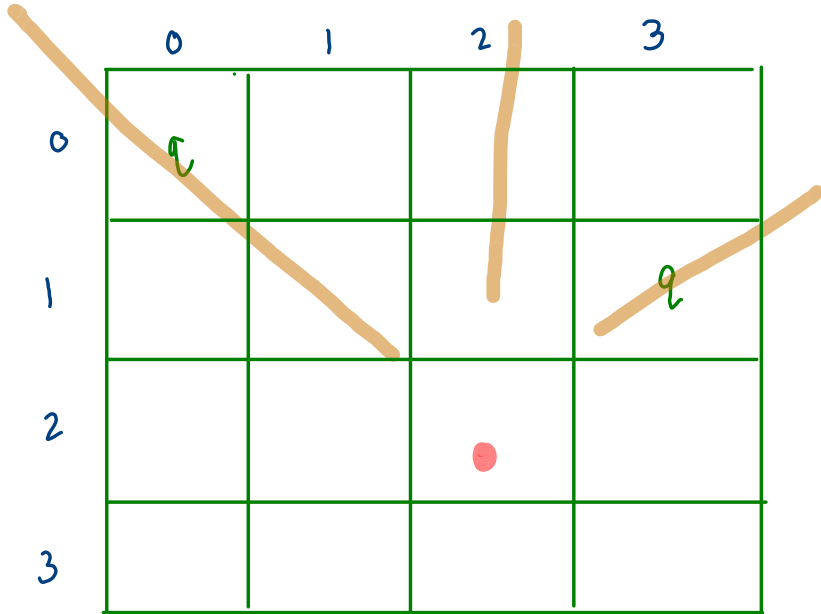
$j = bno \% cols;$

$i, j \rightarrow bno.$

$bno = i * cols + j$



# N-queens branch and bound



3

2

1

0

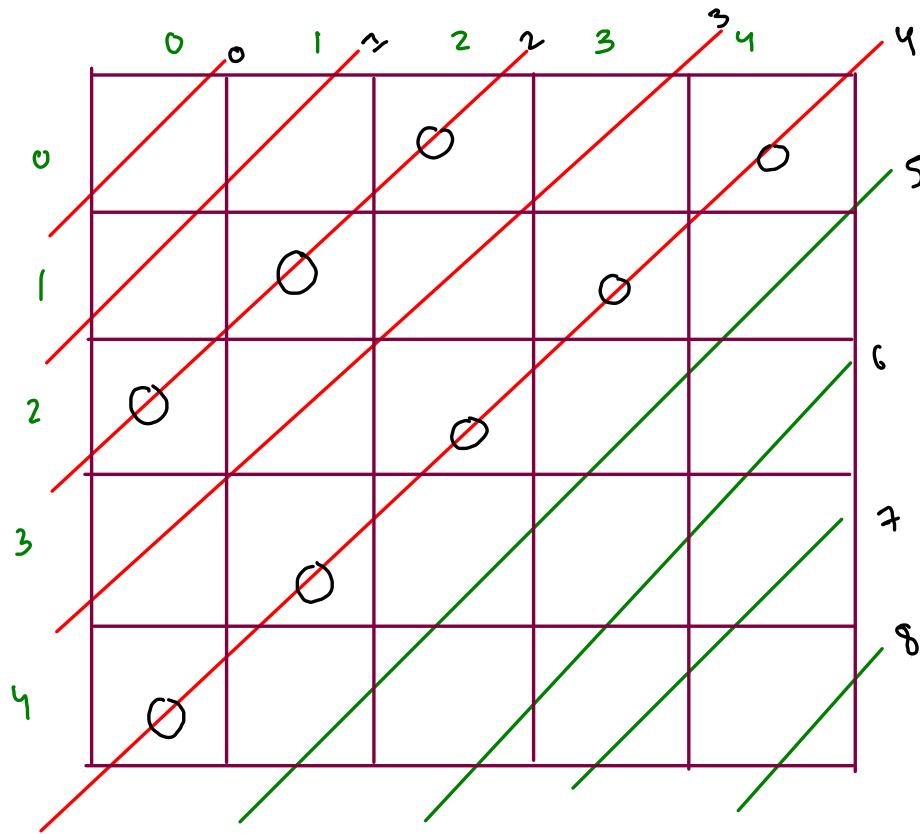


row

	0	1	2	3	4
0					
1					
2					
3					
4					

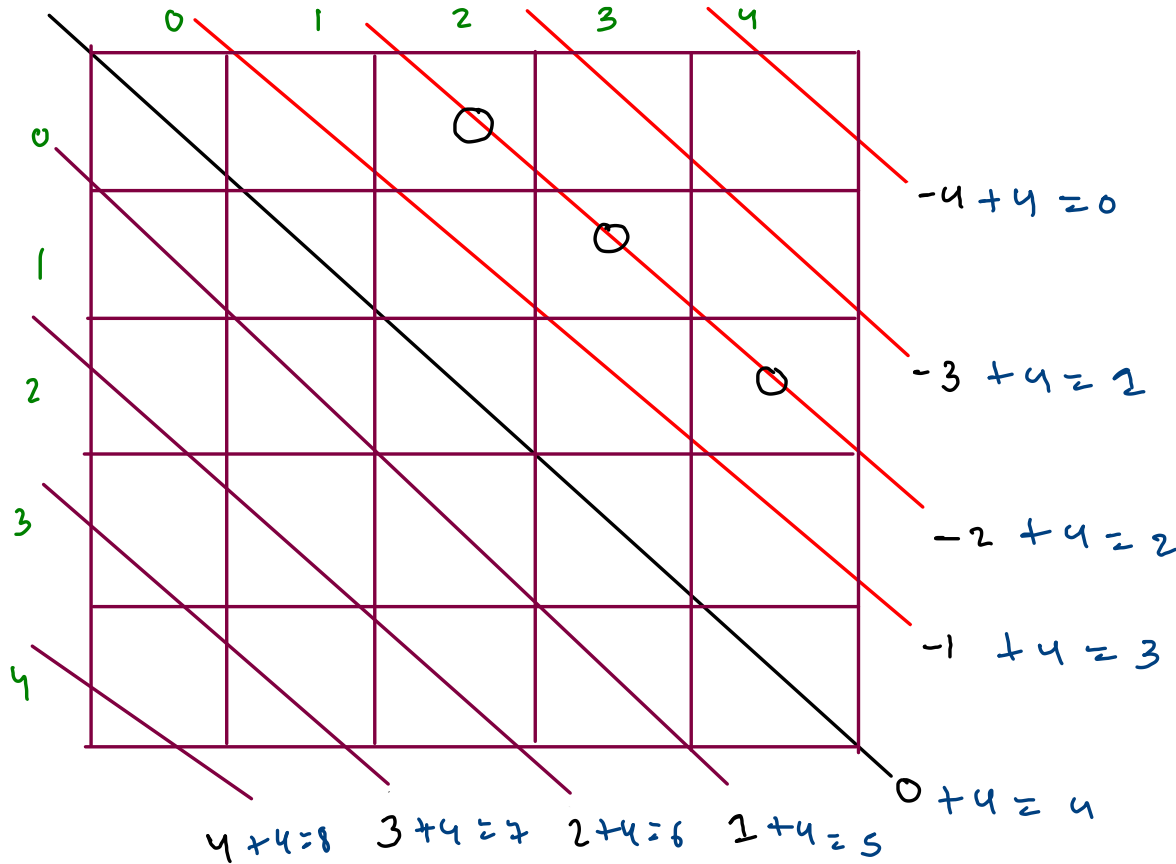
colb

T		T		
---	--	---	--	--



$i+j = \text{reg. diagonal no.}$

$$2 \times N - 1$$



rev-diagonal

$$\text{rev-diag} = (i - j + \overbrace{N-1})$$



shift

row

	0	1	2	3	4
0	q				
1			q		
2					q
3					
4					

$(i, j)$

$colB[j]$

$regdB[i+j]$

$rowdB[i-j+N-1]$

$(2, 4)$

colB

T		T		T
0	1	2	3	4

regdB

T			T			T		
0	1	2	3	4	5	6	7	8

rowdB

		T	T	T				
0	1	2	3	4	5	6	7	8

col =

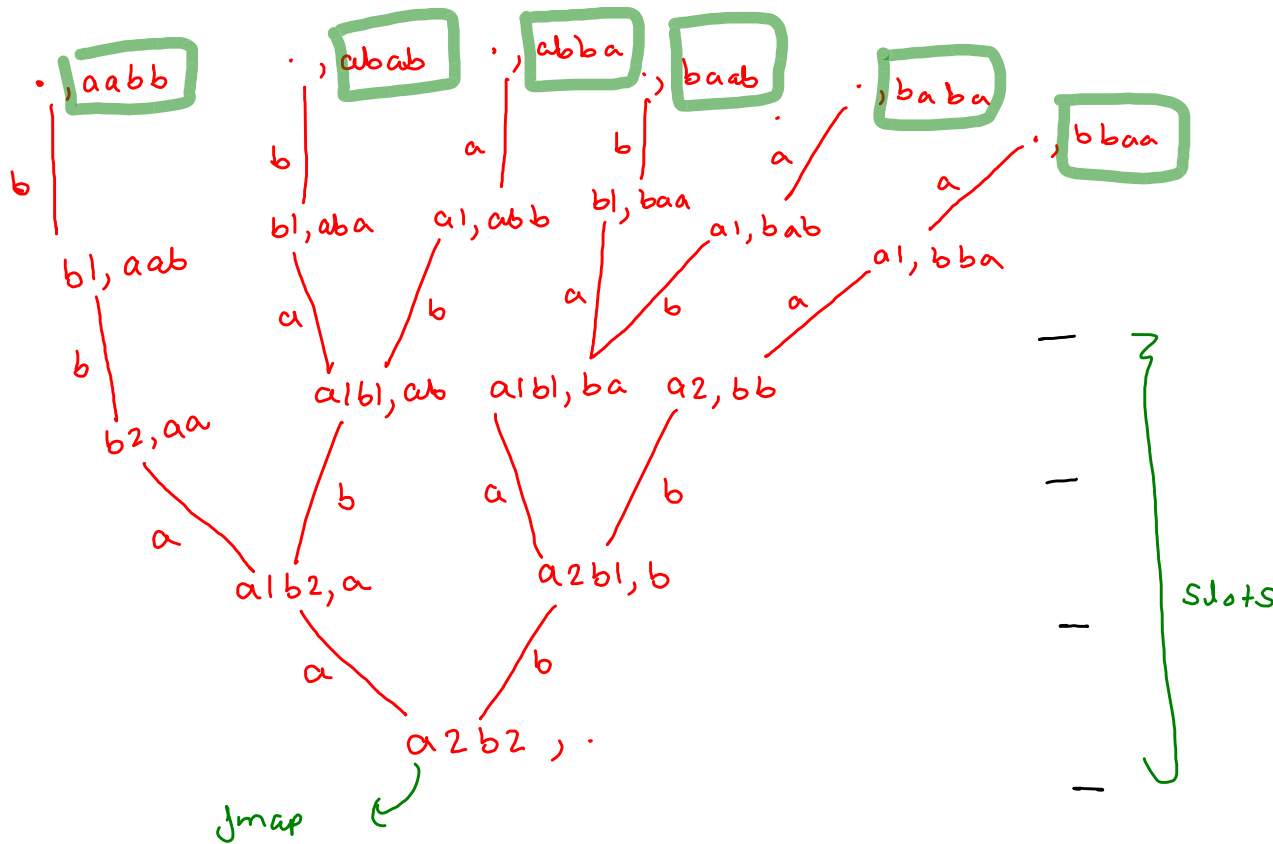
regdB =

rowdB =

# Permutations words - 1

$$\frac{4!}{2! \times 2!} = \frac{24}{4} = 6$$

aabb



```

public static void generateWords(int cs, int ts, HashMap<Character, Integer> fmap, String asf) {
    if(cs > ts) {
        System.out.println(asf);
        return;
    }

    for(char uch : fmap.keySet()) {
        if(fmap.get(uch) > 0) {
            fmap.put(uch, fmap.get(uch)-1);
            generateWords(cs+1, ts, fmap, asf + uch);
            fmap.put(uch, fmap.get(uch)+1);
        }
    }
}

```

abab

<p>a - 2</p> <p>b - 2</p>
---------------------------

