

4x4

4 queens place

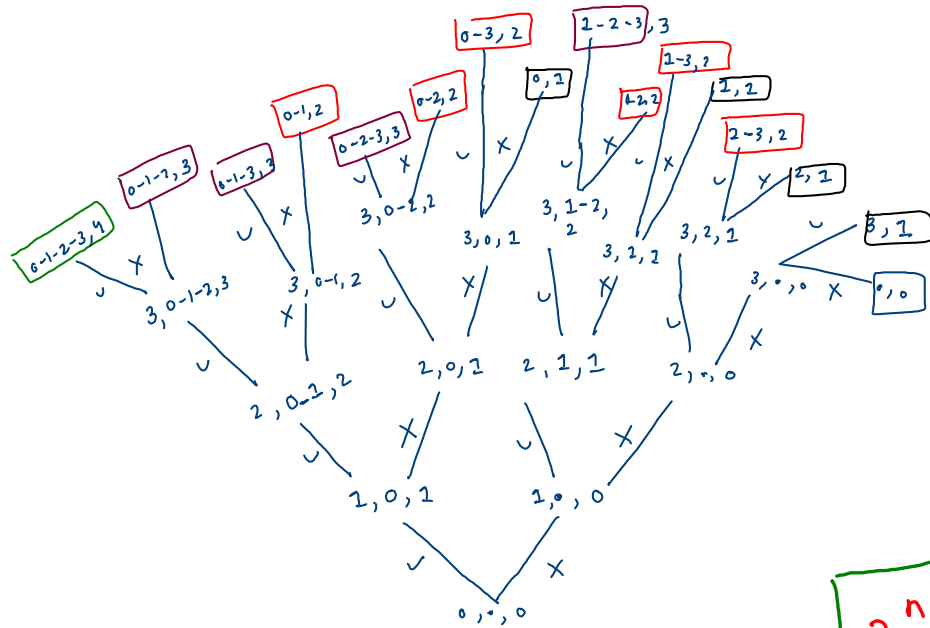
→ total ways

2 queens

6, 8, 9, 10

$N \times N$ matrix ,

$60 \times 65 \rightarrow 4 = n$



0 queens $\rightarrow 1 = 4_{c_0}$

1 queens $\rightarrow 4 = 4_{c_1}$

2 queens $\rightarrow 6 = 4_{c_2}$

3 queen $\rightarrow 4 = 4_{c_3}$

4 queen $\rightarrow 1 = 4_{c_4}$

$$2^n = {}^nC_0 + {}^nC_1 + {}^nC_2 + \dots + {}^nC_n$$

	0	1	2	3
0	0	1	2	3
1	4	5	6	7
2	8	9	10	11
3	12	13	14	15

i, j to b.no.

$$b = i * n + j$$

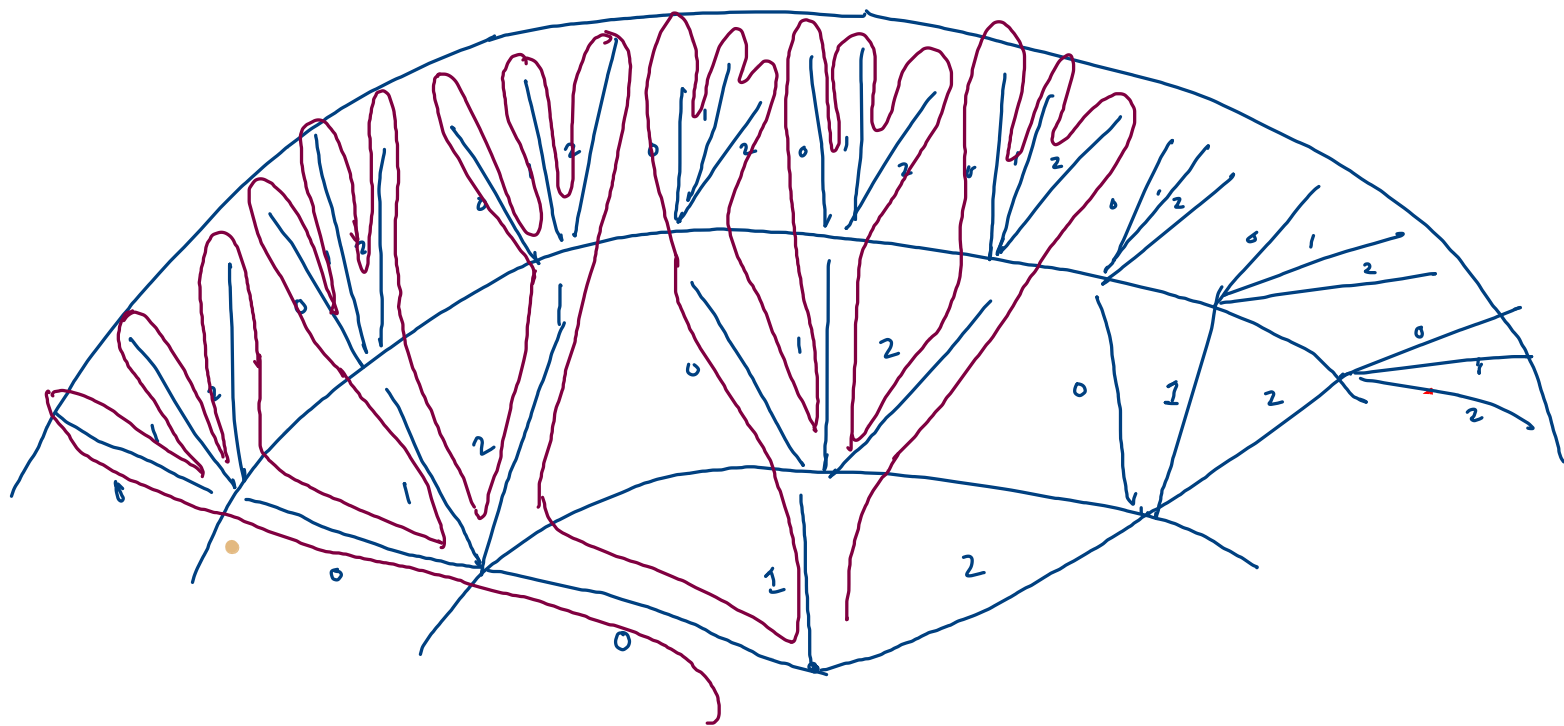
b.no to i, j

$$i = b / n$$

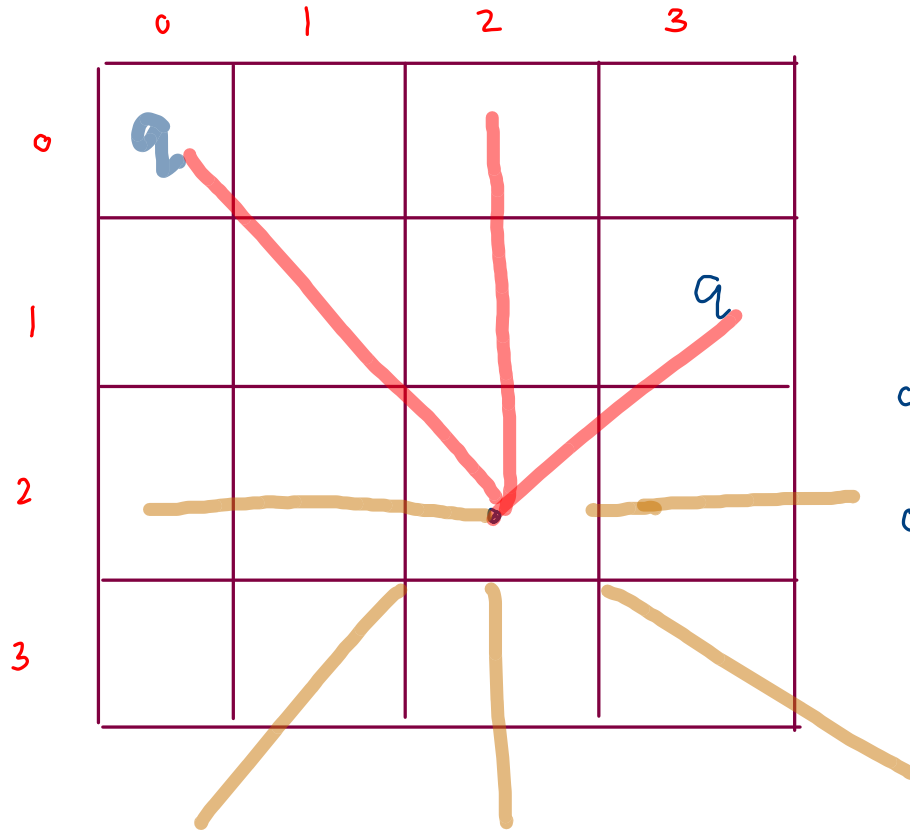
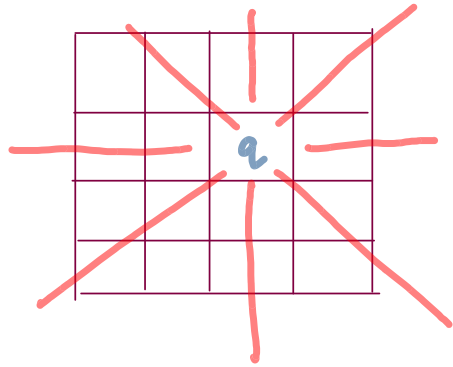
$$j = b \% n$$

	0	1	2
0			
1			
2			

$N \times N$, matrix N queen
each row \rightarrow one queen



N-queens



0-0, 1-2

0-1, 1-3, 2-0, 3-2

0-2, 1-0, 2-3, 3-1

01-13-20-32

```
public static boolean isQueenSafe(int[][] chess, int r, int c) {
    //vertical
    for(int i = r-1; i >= 0; i--) {
        if(chess[i][c] == 1) {
            return false;
        }
    }

    //top right diagonal
    for(int i = r-1, j = c+1; i >= 0 && j < chess.length; i--, j++) {
        if(chess[i][j] == 1) {
            return false;
        }
    }

    //top left diagonal
    for(int i = r-1, j = c-1; i >= 0 && j >= 0; i--, j--) {
        if(chess[i][j] == 1) {
            return false;
        }
    }

    return true;
}
```

```
public static void printNQueens(int[][] chess, String psf, int row) {
    if(row == chess.length) {
        System.out.println(psf + ".");
        return;
    }

    for(int col = 0; col < chess.length; col++) {
        if(isQueenSafe(chess, row, col) == true) {
            //place the queen at row, col
            chess[row][col] = 1;
            //make call to next row
            printNQueens(chess, psf + row + "-" + col + ", ", row + 1);
            //unplace the queen at row, col
            chess[row][col] = 0;
        }
    }
}
```

	0	1	2	3
0		q		
1				q
2	q			
3			q	

$r = 2$
 $c = 1$

	0	1	2	3	4
0	19	2	13	8	21
1	12	7	20	3	14
2	1	18	15	22	9
3	6	11	24	17	4
4	25	16	5	10	23

25 2 13 8 23
 12 7 24 3 14
 1 18 15 22 9
 6 11 20 17 4
 19 16 5 10 21

```
public static void printKnightsTour(int[][] chess, int r, int c, int move) {
    if(r < 0 || c < 0 || r >= chess.length || c >= chess.length || chess[r][c] != 0) {
        return;
    }

    if(move == chess.length * chess.length) {
        chess[r][c] = move;
        displayBoard(chess);
        chess[r][c] = 0;
        return;
    }

    chess[r][c] = move;

    printKnightsTour(chess, r-2, c+1, move+1);
    printKnightsTour(chess, r-1, c+2, move+1);
    printKnightsTour(chess, r+1, c+2, move+1);
    printKnightsTour(chess, r+2, c+1, move+1);
    printKnightsTour(chess, r+2, c-1, move+1);
    printKnightsTour(chess, r+1, c-2, move+1);
    printKnightsTour(chess, r-1, c-2, move+1);
    printKnightsTour(chess, r-2, c-1, move+1);

    chess[r][c] = 0;
}
```

