

# User's Manual for **elegant**

Program Version 2019.4  
Advanced Photon Source  
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Note: another source of help for **elegant** is the on-line forum. Users are encouraged to join and participate. At minimum, users should subscribe to the “Bugs” topic, since this is where bug notifications are posted.

A set of examples and scripts is available from the software download page that demonstrates many features of **elegant**. A brief overview of **elegant** is also available, which introduces the capabilities at a high level.

## 1 Highlights of What's New in Version 2019.4.0

Here is a summary of what's changed since release 2019.3.0. Historical change logs are collected in Section 13.

### 1.1 Bug Fixes for Elements

- The **ILMATRIX** element lacked path-length terms related to the betatron amplitude, and also did not properly handle non-zero  $\alpha_{x,y}$  and  $\eta'_{x,y}$ , as pointed out by forum user Teresia.
- A bug was fixed in back-tracking for **SBEN** elements with nonzero values for **HGAP** and **FINT**. This was reported by Y. Park (UCLA).

### 1.2 Bug Fixes for Commands

- The **bunched\_beam** command was not generating particle ID values when **use\_moments\_output\_values=1**, as reported by Z. Duan (IHEP).

### 1.3 New and Modified Elements

- Added **SPARSE\_INTERVAL** parameter to the **WATCH** element, to allow sparsing coordinate output with regular spacing. This supplements the **FRACTION** parameter, which provides random sampling, and the **START\_PID** and **END\_PID** parameters, which provide sampling of a subset defined by particle ID.
- Added **RPN\_PARAMETERS** parameter to the **SCRIPT** element, which directs the program to load **SDDS** parameter values from the script output file into **rpn** variables, where they may be used for optimization. This provides the user the ability to perform script-based analysis of particle distributions and then optimize the results of that analysis.

- The `N_BINS` parameter of the `WAKE` and `TRWAKE` elements now defaults to zero, which prevents some undesirable behavior when warnings are overlooked. This was requested by R. Lindberg (ANL).
- The `EDRIFT`, `EHVCOR`, `EHCOR`, `EVCOR`, `CSBEND`, `KQUAD`, `KSEXT`, `KOCT`, and `UKICKMAP` elements can now be used with back-tracking (see `run_setup`).

#### 1.4 New and Modified Commands

- The `chaos_map` command is now available. As the name suggests, it is similar to a frequency map, but provides other measures of chaotic motion. This includes a promising new approach outlined by Y. Li *et al.* [56].
- The `optimization_variable` command has a new parameter `differential_limits`, which permits specifying that the lower and upper limits are being given relative to the initial value, rather than in absolute terms.
- The `tune_footprint` command has a new parameter `separate_xy_for_delta`, which permits specifying that tracking for the x and y momentum-dependent tunes should be done either in a combined fashion (default) or separately. The latter might be helpful if nonlinear coupling of y motion into the x plane causes the x tune to be poorly determined for small x amplitudes.
- Added `egaussian` mode to the `ion_effects` command. This mode results in computation of the fields from the electrons assuming a gaussian distribution, as normal, but determines the kick to the ions based purely on momentum conservation. This was inspired by the work of M. Blasciewicz (BNL) and implemented with J. Calvey (ANL).
- Added `multiple_ionization_energy_peak` and `multiple_ionization_energy_rms` parameters to the `ion_effects` command, allowing control of the peak and rms energy of ions produced by multiple ionization. This was done by J. Calvey (ANL).

#### 1.5 Changes Specific to the MPI Parallel Version

- None.

#### 1.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

#### 1.7 Changes to Related Programs and Files

- None.

## 1.8 Known Bugs, Problems, and Limitations

- Floor coordinates are not correct following a BRAT element.
- The REFERENCE\_CORRECTION feature of the CSBEND element is ignored while performing calculations related to the `moments_output` command.
- Setting `CHANGE_T=1` on RFCA and RFCW elements can give invalid results when tracking beams with very large time spread compared to the bunch length.
- Twiss output contains entries for the higher-order dispersion, tune shifts with amplitude, higher-order chromaticity, and tune spreads due to chromaticity and amplitude *even when these are not calculated*, which is potentially misleading. The values are zero when the calculation is not requested.
- Computation of closed orbits and Twiss parameters will not always include the effects of synchrotron radiation losses when these are imposed using SREFFECTS elements. See the documentation for SREFFECTS for details.
- Computation of beam moments does not include synchrotron radiation effects from UKICKMAP elements.
- The file created with the parameters field of `run_setup` does not contain any non-numerical parameters of the lattice.
- Computation of radiation integrals does not include the effect of steering magnets.
- There is a bug related to using ILMATRIX that will result in a crash if one does not request computation of the twiss parameters. If you encounter this problem, just add the following statement after the `run_setup` command:

```
&twiss_output
    matched = 1
&end
```

- The OUTPUT\_FILE feature of the TFBDRIVER will produce a file with missing data at the end of the buffer if the OUTPUT\_INTERVAL parameter is not a divisor of the number of passes.
- When the KQUAD element was split (with the `divide_elements` command or `element_divisions`, any edge multipoles get evaluated at the interior boundaries. In addition, the LEFFECTIVE cannot be used.

## 2 Credits

Contributors to `elegant` include M. Borland, M. Carla', N. Carmignani, M. Ehrlichman, L. Emery, W. Guo, R. Lindberg, V. Sajaev, R. Soliday, Y.-P. Sun, C.-X. Wang, Y. Wang, Y. Wu, and A. Xiao. Contributors to related programs and scripts include M. Borland, R. Dejus, L. Emery, A. Petrenko, H. Shang, Y. Wang, A. Xiao, and B. Yang. R. Soliday is responsible for multi-platform builds and distribution. Of course, we also appreciate the many suggestions, comments, and bug reports from users.

If you use `elegant` in your research, we appreciate a citation. For `elegant`, the citation is

M. Borland, "elegant: A Flexible SDDS-Compliant Code for Accelerator Simulation," Advanced Photon Source LS-287, September 2000.

Additional contributors for the parallel version include Y. Wang and H. Shang. The additional citation for **Pelegant** is

Y. Wang and M. Borland, "Pelegant: A Parallel Accelerator Simulation Code for Electron Generation and Tracking", Proceedings of the 12th Advanced Accelerator Concepts Workshop, AIP Conf. Proc. 877, 241 (2006).

Additional contributors for the GPU version include K. Amyx, J. R. King, and I. V. Pogorelov. The additional citation for the GPU version is

I. V. Pogorelov, J. R. King, K. M. Amyx, M. Borland, and R. Soliday, "Current status of the GPU-accelerated ELEGANT," Proceedings of 2015 International Particle Accelerator Conference, 623 (2015).

### 3 Introduction

**elegant** stands for "ELEctron Generation ANd Tracking," a somewhat out-of-date description of a fully 6D accelerator program that now does much more than generate particle distributions and track them. **elegant**, written entirely in the C programming language[1], uses a variant of the MAD[2] input format to describe accelerators, which may be either transport lines, circular machines, or a combination thereof. Program execution is driven by commands in a namelist format.

This document describes the features available in **elegant**, listing the commands and their arguments. The differences between **elegant** and MAD formats for describing accelerators are listed. A series of examples of **elegant** input and output are given. Finally, appendices are included describing the post-processing programs.

#### 3.1 Program Philosophy

For all its complexity, **elegant** is not a stand-alone program. For example, most of the output is not human-readable, and **elegant** itself has no graphics capabilities. These tasks are handled by a suite of post-processing programs that serve both **elegant** and other physics programs. These programs, collectively known as the SDDS Toolkit[8, 9], provide sophisticated data analysis and display capabilities. They also serve to prepare input for **elegant**, supporting multi-stage simulation.

Setting up for an **elegant** run thus involves more than creating input files for **elegant** per se. A complicated run will typically involve creation of a post-processing command file that processes **elegant** output and puts it in the most useful form, typically a series of graphs. Users thus have the full power of the SDDS Toolkit, the resident command interpreter (e.g., the UNIX shell), and their favorite scripting language (e.g., Tcl/Tk) at their disposal. The idea is that instead of continually rewriting the physics code to, for example, make another type of graph or squeeze another item into a crowded table, one should allow the user to tailor the output to his specific needs using a set of generic post-processing programs. This approach has been quite successful, and is believed particularly suited to the constantly changing needs of research.

Unlike many other programs, **elegant** allows one to make a single run simulating an arbitrary number of randomizations or variations of an accelerator. By using the SDDS toolkit to postprocess the data, the user's postprocessing time and effort do not depend on how many random seeds or

situations are chosen. Hence, instead of doing a few simulations with a few seed numbers or values, the user can simulate hundreds or even thousands of instances of one accelerator to get an accurate representation of the statistics or dependence on parameters, with no more work invested than in doing a few simulations.

In addition, complex simulations such as start-to-end jitter simulations[11] and top-up tracking[12] can be performed involving hundreds or thousands of runs, with input created by scripts depending on the SDDS toolkit. These simulations make use of concurrent computing on about 20 workstation using the Distributed Queueing System[10]. Another example is the **elegantRingAnalysis** script, which allows using many workstations for simulation of storage ring dynamic and momentum aperture, frequency maps, and so on. Clearly, use of automated postprocessing tools greatly increases the scale and sophistication of simulations possible.

In passing, we note another “philosophical” point about **elegant**, namely, the goal of complete backward compatibility. We consider it unacceptable if a new version of the program gives different answers than an old version, unless the old version was wrong. Hence, there are sometimes less-than-ideal default settings in **elegant**, incorrect spelling of parameters, etc., that are never fixed, because doing so would break old input files. It helps to read the manual pages carefully for the more complex features to ensure that the defaults are understood and appropriate.

### 3.2 Capabilities of elegant

**elegant** started as a tracking code, and it is still well-suited to this task. **elegant** tracks in the 6-dimensional phase space  $(x, x', y, y', s, \delta)$ , where  $x$  ( $y$ ) is the horizontal (vertical) transverse coordinate, primed quantities are slopes,  $s$  is the *total, equivalent* distance traveled, and  $\delta$  is the fractional momentum deviation[3]. Note that these quantities are commonly referred to as  $(x, xp, y, yp, s, dp)$  in the namelists, accelerator element parameters, and output files. (“dp” is admittedly confusing—it is supposed to remind the user of  $\Delta P/P_0$ . Sometimes this quantity is referred to as “delta.”)

Tracking may be performed using matrices (of selectable order), canonical kick elements, numerically integrated elements, or any combination thereof. For most elements, second-order matrices are available; matrix concatenation can be done to any order up to third. Canonical kick elements are available for bending magnets, quadrupoles, sextupoles, and higher-order multipoles; all of these elements also support optional classical synchrotron radiation losses. Among the numerically integrated elements available are extended-fringe-field bending magnets and traveling-wave accelerators. A number of hybrid elements exist that have first-order transport with exact time dependence, e.g., RF cavities. Some of the more unusual elements available are third-order alpha-magnets[5, 4], time-dependent kicker magnets, voltage-ramped RF cavities, beam scrapers, and beam-analysis “screens.”

Several elements support simulation of collective effects, such as short- and long-range wakefields, resonator impedances, intra-beam scattering, coherent synchrotron radiation, and the longitudinal space charge impedance.

A wide variety of output is available from tracking, including centroid and sigma-matrix output along the accelerator, phase space output at arbitrary locations, turn-by-turn moments at arbitrary locations, histograms of particle coordinates, coordinates of lost particles, and initial coordinates of transmitted particles. In addition to tracking internally generated particle distributions, **elegant** can track distributions stored in external files, which can either be generated by other programs or by previous **elegant** runs. Because **elegant** uses SDDS format for reading in and writing out particle coordinates, it is relatively easy to interface **elegant** to other programs using files that can also be used with SDDS to do post-processing for the programs.

**elegant** allows the addition of random errors to virtually any parameter of any accelerator element. One can correct the orbit (or trajectory), tunes, and chromaticity after adding errors, then compute Twiss parameters, track, or perform a number of other operations. **elegant** makes it easy to evaluate a large number of ensembles (“seeds”) in a single run. Alternatively, different ensembles can be readily run on different CPUs and the SDDS output files combined.

In addition to randomly perturbing accelerator elements, **elegant** allows one to systematically vary any number of elements in a multi-dimensional grid. As before, one can track or do other computations for each point on the grid. This is a very useful feature for the simulation of experiments, e.g., emittance measurements involving beam-size measurements during variation of one or more quadrupoles[6].

Like many accelerator codes, **elegant** does accelerator optimization. It will optimize a user defined function of the transfer matrix elements (up to third-order), beta functions, tunes, chromaticities, radiation integrals, natural emittance, floor coordinates, beam moments, etc. It also has the ability to optimize results of tracking using a user-supplied function of the beam parameters at one or more locations. This permits solution of a wide variety of problems, from matching a kicker bump in the presence of nonlinearities to optimizing dynamic aperture by adjusting sextupoles.

**elegant** provides several methods for determining accelerator aperture, whether dynamic or physical. One may do straightforward tracking of an ensemble of particles that occupies a uniform grid in (x, y) space. One may also invoke a search procedure that finds the aperture boundary. A related feature is the ability to determine the frequency map for an accelerator, to help identify aperture-limiting resonances.

In addition to using analytical expressions for the transport matrices, **elegant** supports computation of the first-order matrix and linear optics properties of a circular machine based on tracking. A common application of this is to compute the tune and beta-function variation with momentum offset by single-turn tracking of a series of particles. This is much more efficient than, for example, tracking and performing FFTs (though **elegant** will do this also). This both tests analytical expressions for the chromaticity and allows computations using accelerator elements for which such expressions do not exist (e.g., a numerically integrated bending magnet with extended fringe fields).

A common application of random error simulations is to set tolerances on magnet strength and alignment relative to the correctability of the closed orbit. A more efficient way to do these calculations is to use correct-orbit amplification factors[6]. **elegant** computes amplification factors and functions for corrected and uncorrected orbits and trajectories pertaining to any element that produces an orbit or trajectory distortion. It simultaneously computes the amplification functions for the steering magnets, in order to determine how strong the steering magnets will need to be.

## 4 Digression on the Longitudinal Coordinate Definition

A word is in order about the definition of  $s$ , which we’ve described as the *total*, *equivalent* distance traveled. First, by *total* distance we mean that  $s$  is *not* measured relative to the bunch center or a fiducial particle. It is entirely a property of the individual particle and its path through the accelerator.

To explain what we mean by *equivalent* distance, note that the relationship between  $s$  and arrival time  $t$  at the observation point is, for each particle,  $s = \beta c t$ , where  $\beta c$  is the instantaneous velocity of the particle. Whenever a particle’s velocity changes, **elegant** recomputes  $s$  to ensure that this relationship holds.  $s$  is thus the “equivalent” distance the particle would have traveled at the present velocity to arrive at the observation point at the given time. This book-keeping is

required because **elegant** was originally a matrix-only code using  $s$  as the longitudinal coordinate.

Users should keep the meaning of  $s$  in mind when viewing statistics for  $s$ , for example, in the **sigma** or **watch** point output files. A quantity like **Ss** is literally the rms spread in  $s$ . It is *not* defined as  $\sigma_t/(\langle\beta\rangle c)$ . A nonrelativistic beam with velocity spread will show no change in **Ss** in a drift space, because the distance traveled is the same for all particles.

## 5 Fiducialization in elegant

In some tracking codes, there is a “fiducial particle” that is tracked along with the beam. This particle follows the ideal trajectory or orbit, with the ideal momentum, and at the ideal phase. There is no fiducial particle in **elegant**. Instead, fiducialization is typically based on statistical properties of the bunch. This can be performed on a bunch-by-bunch basis, or for the first bunch seen in a run. The latter method must be used if one wants to look at the effects of changing phase, voltage, or magnets relative to some nominal configuration.

Internally, **elegant** fiducializes each element in the beamline. Fiducializing an element means determining the reference momentum and arrival time (or phase) for that element. If the reference momentum does not change along a beamline and no time-dependent elements are involved, then fiducialization is irrelevant. All elements are fiducialized at the central momentum defined in **run\_setup**.

A number of commands have parameters for controlling fiducialization:

- The **always\_change\_p0** parameter of **run\_setup** causes **elegant** to re-establish the central momentum after each element when fiducializing. This may be more convenient than setting the **CHANGE\_P0** parameter on the elements themselves. However, it can have unexpected consequences, such as changing the central momentum to match changes in beam momentum due to synchrotron radiation.
- **run\_control** has four parameters that affect fiducialization, which come into play when multi-step runs are made. Typically, these are runs that involve variation of elements, addition of errors, or loading of multiple sets of parameters.
  - **reset\_rf\_for\_each\_step** — If nonzero, the rf phases are re-established for each beam tracked. If this is 1 (the default), the time reference is discarded after each bunch is tracked. This means that bunch-to-bunch phasing errors due to time-of-flight differences would be lost.
  - **first\_is\_fiducial** — The first bunch seen is taken to establish the fiducial phases and momentum profile. If one is simulating, for example, successive beams in a fixed accelerator, this should be set to 1. Otherwise, the momentum reference is discarded after each bunch is tracked. N.B.: as of version 27.0.1, setting **first\_is\_fiducial**=1 does not imply **always\_change\_p0**=1. You must set this separately, or use the **CHANGE\_P0** parameter on various elements (e.g., **RFCA**) to further specify how to set the fiducial momentum profile.
  - **restrict\_fiducialization** — If nonzero, then momentum profile fiducialization occurs only after elements that are known to possibly change the momentum. It would not occur, for example, after a scraper that changes the average beam momentum by removing a low-momentum tail. This is a convenience that, essentially, allows modifying the impact of setting **always\_change\_p0**=1.

- `n_passes_fiducial` — If positive, sets the number passes used for fiducial tracking to be different from the `n_passes` value. For ring fiducialization, should probably always be set to 1.
- The `bunched_beam` command has a `first_is_fiducial` parameter that is convenient for use with the `first_is_fiducial` mode established by `run_control`. If nonzero, this parameter causes `elegant` to generate a first bunch with only one particle. This is very useful if one wants to track with many particles but doesn't want to waste time fiducializing with a many-particle bunch.

Here are some examples that may be helpful.

- *Scanning a phase error in a linac with a bunch compressor:* The scan is performed using the `vary_element` command. For this to work properly, it is necessary to fiducialize the system with zero phase error. Hence, one must use the enumeration feature of `vary_element` to provide an input file with the phase errors and the file must be sorted so that the row with zero phase error is first. Further, one must set `reset_rf_for_each_step = 0` and `first_is_fiducial = 1` in `run_control`, and `CHANGE_P0=1` on all rf cavity elements. (See the `bunchComp/phaseSweep` and `bunchComp/dtSweep` examples.)
- *Scanning the voltage of a linac to simulate different operating energy choices at the compressor:* In this case, one scans the linac voltage, but wants to fiducialize the system for each voltage. (It's a change in design, not an error or perturbation.) One again uses `vary_element`, but nothing special needs to be done about the order of the voltage values. One must set `reset_rf_for_each_step = 1` and `first_is_fiducial = 0` in `run_control`, and `CHANGE_P0=1` on all rf cavity elements. (See the `bunchComp/energySweep` example.)
- *Simulation of phase and voltage jitter:* In this case, one uses the `error_elements` command to impart errors to the `PHASE` and `VOLT` parameters of rf cavity elements. However, the first beam through the system must not see any errors. This is accomplished by setting `no_errors_for_first_step=1` in `error_control`. One can also (optionally) use a 1-particle beam for fiducialization by setting `first_is_fiducial=1` in `bunched_beam`. In addition, one must set `reset_rf_for_each_step = 0` and `first_is_fiducial = 1` in `run_control`, and `CHANGE_P0=1` on all rf cavity elements. (See the `bunchCompJitter/jitter` example.)

## 6 Preparing beams for bunch-mode simulations

Certain collective-effects elements in `elegant` can operate under the assumption that the beam is organized into bunches. This includes the `FRFMODE`, `FTRFMODE`, `LRWAKE`, `RFMODE`, `WAKE`, `TRFMODE`, `TRWAKE`, `ZLONGIT`, and `ZTRANSVERSE` elements. At present, this behavior is only available when loading a beam from an external file using the `sdds_beam` command. A typical sequence is to run `elegant` once to generate a beam file using `bunched_beam`, then load that beam into a subsequent run.

This beam file may either contain the entire beam (all the bunches) or it may contain a single bunch. In the latter case, the single bunch must be duplicated using the `n_duplicates` and `duplicate_stagger` parameters of `sdds_beam`. Otherwise, in the beam-generation run, the `run_control` command must be used to specify both the number of bunches (using `n_steps`) and the bunch frequency (using `bunch_frequency`). The beamline for this run would typically consist simply of a zero-length drift space, so that the output file from the `run_setup` command



contains the coordinates for each bunch as generated, with no modifications. Once the beam is generated, it can be used as the input file for `sdds_beam` with `track_pages_separately=0` and `use_bunched_mode=1`.

For those who prepare beams using other programs, it may be helpful to understand how the organization of the beam into bunches is specified. The relevant data from the beam file are the values in the `IDSLOTSPerBunch` parameter and `particleID` column. The `particleID` is generally a unique positive integer for each particle. When  $S = \text{IDSLOTSPerBunch}$  is non-zero, the bunch index is computed as  $\lfloor (I - 1) / S \rfloor$ , where  $I$  is the particle ID. For example, with `IDSLOTSPerBunch=1000`, particle IDs from 1 to 1000 would be in bunch 0, from 2001-3000 would be bunch 1, and so on. This mechanism allows specifying the bunch structure without adding columns to the beam file, and also handles particle loss automatically.

Note that although in the case of beams generated with `bunched_beam` the individual bunches appear in separate pages of the beam file, this is not necessary.

## 7 Namelist Command Dictionary

The main input file for an `elegant` run consists of a series of namelists, which function as commands. Most of the namelists direct `elegant` to set up to run in a certain way. A few are “action” commands that begin the actual simulation. FORTRAN programmers should note that, unlike FORTRAN namelists, these namelists need not come in a predefined order; `elegant` is able to detect which namelist is next in the file and react appropriately.

### 7.1 Commandline Syntax

The commandline syntax for `elegant` is of the form

```
elegant {inputfile|-pipe=in} [-rpnDefns=filename] [-configuration=filename]
[-macro=tag1=value1[, tag2=value2...]
```

*inputfile* is the name of the command input file, which is a series of namelist commands directing the calculations. Alternatively, one may give the `-pipe=in` option, allowing `elegant` to be fed a stream of commands by another program or script. The `-rpnDefns` option allows providing the name of the RPN definitions file as an alternative to defining the `RPN_DEFNS` environment variable. The `-configuration` option allows providing the name of an input file to be read prior to *inputfile*; this can be used for configuring `elegant` using, e.g., the `global_settings` command; this is an alternative to using the `ELEGANT_CONFIGURATION` environment variable. The `-macro` option allows performing text substitutions in the command stream. Multiple `-macro` options may be given. Usage is described in more detail below.

### 7.2 General Command Syntax

Each namelist has a number of variables associated with it, which are used to control details of the run. These variables come in three data types: (1) `long`, for the C long integer type. (2) `double`, for the C double-precision floating point type. (3) `STRING`, for a character string enclosed in double quotation marks. All variables have default values, which are listed on the following pages. `STRING` variables often have a default value listed as `NULL`, which means no data; this is quite different from the value `""`, which is a zero-length character string. `long` variables are often used as logical flags, with a zero value indicating false and a non-zero value indicating true.

On the following pages the reader will find individual descriptions of each of the namelist commands and their variables. Each description contains a sequence of the form

```
&<namelist-name>
    <variable-type> <variable-name> = <default-value>;
    .
    .
    .
&end
```

This summarizes the parameters of the namelist. Note, however, that the namelists are invoked in the form

```
&<namelist-name>
    [<variable-name> = <value> ,]
    [<array-name>[<index>] = <value> [,<value> ...] ,]
    .
    .
    .
&end
```

The square-brackets enclose an optional component. Not all namelists require variables to be given—the defaults may be sufficient. However, if a variable name is given, it must have a value. Values for **STRING** variables must be enclosed in double quotation marks. Values for **double** variables may be in floating-point, exponential, or integer format (exponential format uses the ‘e’ character to introduce the exponent).

Array variables take a list of values, with the first value being placed in the slot indicated by the subscript. As in C, the first slot of the array has subscript 0, *not* 1. The namelist processor does not check to ensure that one does not put elements into nonexistent slots beyond the end of the array; doing so may cause the processor to hang up or crash.

Wildcards are allowed in a number of places in **elegant** and the SDDS Toolkit. The wildcard format is very similar to that used in UNIX:

- \* — stands for any number of characters, including none.
- ? — stands for any single character.
- [<list-of-characters>] — stands for any single character from the list. The list may include ranges, such as **a-z**, which includes all characters between and including ‘a’ and ‘z’ in the ASCII character table.

The special characters \*, ?, [, and ] are entered literally by preceeding the character by a backslash (e.g., \\*).

In many places where a filename is required in an **elegant** namelist, the user may supply a so-called “incomplete” filename. An incomplete filename has the sequence “%s” imbedded in it, for which is substituted the “rootname.” The rootname is by default the filename (less the extension) of the command (i.e., main input) file. The most common use of this feature is to cause **elegant** to create names for all output files that share a common filename but differ in their extensions. Post-processing can be greatly simplified by adopting this naming convention, particularly if one consistently uses the same extension for the same type of output. Recommended filename extensions are given in the lists below.

Note that this substitution feature is not generally available for input files, though there are some exceptions (e.g., `load_parameters`). Another convenience for input file organization is the search-path feature, which can be set from the `run_setup` command. By default, `elegant` assumes input filenames give the full pathname. If the search path is specified, `elegant` will instead look for files in one of the listed directories.

When `elegant` reads a namelist command, one of its first actions is to print the namelist back to the standard output. This printout includes all the variables in the namelist and their values. Occasionally, the user may see a variable listed in the printout that is not in this manual. These are often obsolete and are retained only for backward compatibility, or else associated with a feature that is not fully supported. Use of such “undocumented features” is discouraged.

`elegant` supports substitution of fields in namelists using the commandline `macro` option. This permits making runs with altered parameters without editing the input file. Macros inside the input file have one of two forms: `<tag>` or `\$tag`. To perform substitution, use the syntax

```
elegant inputfile|-pipe=in -macro=tag1=value1[, tag2=value2...]
```

When using this feature, it is important to substitute the value of `rootname` (in `run_setup`) so that one can get a new set of output files (assuming use of the suggested “%s” field in all the output file names). One may give the `macro` option any number of times, or combine all substitutions in one option. The name of the input file is available using the macro `INPUTFILENAME`.

`elegant` also allows execution of commands in the shell as part of evaluation of a namelist field. To invoke this, one encloses the commandline string in curly braces. E.g.,

```
betax = "{sdds2stream -parameter=betaxFinal data.twi}"
```

(Note that the quotes are also required.) In this example, `betax` is assigned the value of the parameter `betaxFinal` from the file `data.twi`.

It is also possible to perform calculations using `elegant`’s built-in RPN calculator. (It is identical to the commandline programs `rpn` and `rpn1` supplied with the SDDS toolkit.) To do this in the command file, one must use quotation marks and enclose the expression in parentheses, as in

```
betax = "(8 2 / pi /)"
```

(Note that this is different from using such expressions in the lattice file; in that case, one doesn’t need the parentheses.) One can not only make such computations, but also use the stack and variables. So, for example, one might use

```
betax = "(8 2 / pi / sto betax0)"
betay = "(betax0)"
```

One can also mix subcommands and RPN expressions, as in

```
betax = "({sdds2stream -parameter=betaxFinal data.twi} 2 /)"
```

would assign to `betax` half the value of the parameter `betaxFinal` from the file `data.twi`.

### 7.3 Setup and Action Commands

A subject of frequent confusion for `elegant` users is the distinction between setup and action commands. An “action” command causes `elegant` to immediately perform a specific computation or set of computations. In contrast, a “setup” command tells `elegant` how to perform computations when it later encounters a “major” action command (one of `analyze_map`, `find_aperture`,

`frequency_map`, `momentum_aperture`, `optimize`, or `track`). (N.B.: After each major action command, the problem space is wiped clear. To perform further computations requires introduction of a new `run_setup` command.)

Several commands are switchable between action and setup modes. These include the `coupled_twiss_output`, `correction_matrix_output`, `twiss_output`, `find_aperture`, `matrix_output`, and `sasefel` commands. Except for `find_aperture`, all of the commands that can run in both modes have the `output_at_each_step` parameter, which is used to switch between the modes. In the case of `find_aperture`, the switch is accomplished using the `optimization_mode` parameter. Regardless of which parameter is present, unless the parameter is given a value of 1, the command operates in action mode. Further, if the command is used in setup mode and no relevant action command is present later in the file, then the requested will not be performed.

Typically one wants to use these switchable commands in setup mode whenever one is simulating random errors, performing a parameter scan, or performing optimization. When in setup mode, the indicated computations will be performed repeatedly, e.g., for each set of errors, for each step in the parameter scan, or for use in each evaluation of the optimization penalty function.

## 7.4 Table of elegant commands and their functions

| Command name                                 | Type                  | Description   |
|--|-----------------------|---|
| <code>alter_elements</code>                  | action                | Change an element parameter from the command file.  |
| <code>amplification_factors</code>           | action                | Compute orbit amplification functions.  |
| <code>analyze_map</code>                     | major<br>action       | Determine first-order matrix from tracking.   |
| <code>aperture_data</code>                   | setup                 | Define aperture using an SDDS file.   |
| <code>bunched_beam</code>                    | setup                 | Set up beam generation.   |
| <code>change_particle</code>                 | action                | Change the type of particle. Default is electron.   |
| <code>chaos_map</code>                       | action                | Compute a map of the degree of chaos in particle motion.  |
| <code>chromaticity</code>                    | setup                 | Correct the chromaticity.   |
| <code>closed_orbit</code>                    | setup                 | Compute the closed orbit.   |
| <code>correct</code>                         | setup                 | Correct the orbit or trajectory.  |
| <code>correction_matrix_output</code>        | action/setup          | Obtain orbit/trajectory correction matrix in a file.  |
| <code>correct_tunes</code>                   | setup                 | Correct the tunes.  |
| <code>coupled_twiss_output</code>            | setup/action          | Compute and output coupled twiss parameters.  |
| <code>divide_elements</code>                 | setup                 | Specify division of elements into pieces.   |
| <code>elastic_scattering</code>              | major<br>action       | Use tracking to determine local scattering aperture and loss locations due to elastic gas scattering.   |
| <code>error_element</code>                   | setup                 | Define errors for a set of elements.  |
| <code>error_control</code>                   | setup                 | Set up and control error generation process.  |
| <code>find_aperture</code>                   | setup/major<br>action | Determine the transverse (e.g., dynamic) aperture.  |
| <code>floor_coordinates</code>               | action                | Compute and output floor coordinates.   |
| <code>frequency_map</code>                   | major<br>action       | Compute and output frequency map.   |
| <code>global_settings</code>                 | action                | Change global settings.   |
| <code>ignore_elements</code>                 | setup                 | Ignore specified elements during tracking.  |
| <code>inelastic_scattering</code>            | major<br>action       | Use tracking to determine local scattering aperture and loss locations due to inelastic gas scattering. |
| <code>insert_elements</code>                 | action                | Insert elements into the lattice at many places.  |
| <code>insert_sceffects</code>                | action                | Insert space charge kick elements.  |
| <code>linear_chromatic_tracking_setup</code> | setup                 | Set up for fast tracking with chromatic effects.  |
| <code>link_control</code>                    | setup                 | Control linking of element parameters.  |

|                               |              |   |
|-------------------------------|--------------|---|
| link_elements                 | setup        | Define link between parameters of two elements.               |
| load_parameters               | setup/action | Load element parameters from SDDS file.                       |
| matrix_output                 | setup/action | Output transfer matrix along beamline.                        |
| modulate_elements             | setup        | Set up time-dependent modulation of elements.                 |
| moments_output                | setup/action | Compute coupled beam moments, with radiation option.          |
| momentum_aperture             | major action | Determine s-dependent momentum aperture.                      |
| optimize                      | major action | Execute an optimization.                                      |
| optimization_covariable       | setup        | Define a dependent parameter for optimization.                |
| optimization_setup            | setup        | Perform initial optimization setup.                           |
| optimization_term             | setup        | Define a term of penalty function.                            |
| optimization_variable         | setup        | Define an optimization variable.                              |
| parallel_optimization_setup   | setup        | Perform initial parallel optimization setup.                  |
| print_dictionary              | action       | Print the element dictionary.                                 |
| ramp_elements                 | setup        | Set up turn-by-turn ramping of elements.                      |
| rf_setup                      | setup/action | Set up RF cavity elements for storage rings.                  |
| rpn_expression                | action       | Execute an expression in the rpn interpreter.                 |
| rpn_load                      | action       | Load values from SDDS file into rpn interpreter.              |
| run_control                   | setup        | Set up simulation steps and passes.                           |
| run_setup                     | setup        | Define global simulation parameters and output files.         |
| sasefel                       | setup/action | Evaluate SASE FEL gain etc.                                   |
| save_lattice                  | action       | Save new lattice file.  |
| sdds_beam                     | setup        | Define loading of particles from SDDS file.                   |
| semaphores                    | setup        | Define file semaphores for start/end of run.                  |
| set_reference_particle_output | setup        | Define reference particle distribution for optimization       |
| slice_analysis                | setup        | Perform slice analysis along beamline.                        |
| subprocess                    | action       | Execute a command in the shell.                               |
| steering_element              | setup        | Define element parameters as steering correctors.             |
| transmute_elements            | setup        | Transmute elements from one type to another.                  |
| tune_footprint                | setup/action | Compute and optimize chromatic and amplitude tune footprints. |

|  |              |   |
|--|--------------|---|
| <code>twiss_analysis</code>            | setup        | Define subset of beamline for twiss parameter analysis. |
| <code>twiss_output</code>              | setup/action | Set up twiss parameter and related computation.         |
| <code>track</code>                     | major action | Execute tracking of particles and other operations.     |
| <code>tune_shift_with_amplitude</code> | setup        | Compute tune shifts with amplitude.                     |
| <code>vary_element</code>              | setup        | Vary element parameters in loops.                       |

Table 1: Table of **elegant** commands and their functions.

## alter\_elements

### 7.5 alter\_elements

- type: action command.
- function: modify the value of a parameter for one or more elements
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&alter_elements
  STRING name = NULL;
  STRING item = NULL;
  STRING type = NULL;
  STRING exclude = NULL;
  double value = 0;
  STRING string_value = NULL;
  long differential = 0;
  long multiplicative = 0;
  long alter_at_each_step = 0;
  long alter_before_load_parameters = 0;
  long verbose = 0;
  long allow_missing_elements = 0;
  long allow_missing_parameters = 0;
  long start_occurrence = 0;
  long end_occurrence = 0;
  double s_start = -1;
  double s_end = -1;
  STRING before = NULL;
  STRING after = NULL;
&end
```

- **name** — A possibly-wildcard-containing string giving the names of the elements to alter. If not specified, then one must specify **type**.
- **item** — The name of the parameter to alter.
- **type** — A possibly-wildcard-containing string giving the names of element *types* to alter. May be specified with **name** or by itself.
- **exclude** — A possibly-wildcard-containing string giving the names of elements to excluded from alteration.
- **value**, **string\_value** — The new value for the parameter. Use **string\_value** only if the parameter takes a character string as its value.
- **differential** — If nonzero, the new value is the predefined value of the parameter plus the quantity given with **value**.



- **multiplicative** — If nonzero, the new given value is the predefined value of the parameter times the quantity given with **value**.
- **alter\_at\_each\_step** — If nonzero, the changes requested by the command are performed at each simulation step. Note that if **differential** or **multiplicative** are non-zero, then changes will accumulate. (A more conventional way to perform such variation is with **vary\_elements**.)
- **alter\_before\_load\_parameters** — If **alter\_at\_each\_step**, by default the alteration takes place after any **load\_parameters** commands are processed. If this control is non-zero, the alteration takes place before any **load\_parameters** commands are processed.
- **verbose** — If nonzero, information is printed to the standard output describing what elements are changed.
- **allow\_missing\_elements** — If nonzero, then it is not an error if an element matching **name** does not exist. Normally, such an occurrence is an error and terminates the program.
- **allow\_missing\_parameters** — If nonzero, then it is not an error if an element does not have the parameter named with **item**. Normally, such an occurrence is an error and terminates the program.
- **start\_occurrence, end\_occurrence** — If nonzero, these give the starting and ending occurrence numbers of elements that will be altered. N.B.: if wildcards are used, occurrence number counting is for each set of identically-named elements separately, rather than for the sequence of matched elements.
- **s\_start, s\_end** — If non-negative, these give the giving and ending position limits for the end-of-element locations of elements to be altered.
- **after** — The name of an element. If given, the alteration is applied only to elements that follow the named element in the beamline.
- **before** — The name of an element. If given, the alteration is applied only to elements that precede the named element in the beamline.

## amplification\_factors

### 7.6 amplification\_factors

- type: action command.
- function: compute corrected and uncorrected orbit amplification factors and functions.
- sequence: must be the last command in a sequence.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&amplification_factors
  STRING output = NULL;
  STRING uncorrected_orbit_function = NULL;
  STRING corrected_orbit_function = NULL;
  STRING kick_function = NULL;
  STRING name = NULL;
  STRING type = NULL;
  STRING item = NULL;
  STRING plane = NULL;
  double change = 1e-3;
  long number_to_do = -1;
  double maximum_z = 0;
&end
```

- **output** — The (incomplete) name of a file for text output. Recommended value: “%s.af”.
- **uncorrected\_orbit\_function** — The (incomplete) name of a file for an SDDS-format output of the uncorrected-orbit amplification function. Recommended value: “%s.uof”.
- **corrected\_orbit\_function** — The (incomplete) name of a file for an SDDS-format output of the corrected-orbit amplification function. Recommended value: “%s.cof”.
- **kick\_function** — The (incomplete) name of a file for an SDDS-format output of the kick amplification function. Recommended value: “%s.kaf”.
- **name** — The optionally wildcarded name of the orbit-perturbing elements.
- **type** — The optional type name of the the orbit-perturbing elements.
- **item** — The parameter of the elements producing the orbit.
- **plane** — The plane (“h” or “v”) to examine.
- **change** — The parameter change to use in computing the amplification.
- **number\_to\_do** — The number of elements to perturb.
- **maximum\_z** — The maximum z coordinate of the elements to perturb.

## analyze\_map

### 7.7 analyze\_map

- type: major action command.
- function: find the transport matrix up to third order based on particle tracking, based on method described in [4]. Also find related quantities, such as chromaticity.
- sequence: must follow `run_control`.
- can use parallel resources (Pelegant)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&analyze_map
  STRING output = NULL;
  long output_order = 1;
  STRING printout = NULL;
  STRING printout_format = "%22.15e ";
  long printout_order = 2;
  double delta_x = 5e-5;
  double delta_xp = 5e-5;
  double delta_y = 5e-5;
  double delta_yp = 5e-5;
  double delta_s = 5e-5;
  double delta_dp = 5e-5;
  double accuracy_factor = 1e-12;
  long center_on_orbit = 0;
  long verbosity = 0;
  long canonical_variables = 0;
  long periodic = 1;
  double beta_x = 1;
  double alpha_x = 0;
  double eta_x = 0;
  double etap_x = 0;
  double beta_y = 1;
  double alpha_y = 0;
  double eta_y = 0;
  double etap_y = 0;
  long n_points = 9;
  long max_fit_order = 8;
&end
```

- `output` — The (incomplete) name of a file for SDDS output.
  - Recommended value: “%s.ana”.
  - File contents: A series of pages, each consisting of a single data point containing the centroid offsets for a single turn, the single-turn R matrix, the matched Twiss parameters, tunes, and dispersion functions.

- **printout** — The (incomplete) name of a file for text output of the matrix.
- **printout\_format** — The C-style formatting statement for the matrix elements. A space, comma, or other separator should appear at the end of the string.
- **delta\_X** — The amount by which to change the quantity X in computing the derivatives that give the matrix elements.
- **accuracy\_factor** — The fraction of the maximum absolute value of the final coordinate that is considered meaningful. Used to estimate errors and eliminate spurious matrix elements.
- **canonical\_variables** — If non-zero, the matrix is expressed in terms of canonical variables  $(x, q_x, y, q_y, -s, \delta)$  instead of the default  $(x, x', y, y', s, \delta)$ .
- **center\_on\_orbit** — A flag directing the expansion to be made about the closed orbit instead of the design orbit.
- **verbosity** — The larger this value, the more output is printed during computations.
- **printout\_order** — Order of the matrix to be printed to the **printout** file.
- **periodic** — If non-zero, system is assumed to be periodic and lattice functions, tunes, chromaticities, etc are computed.
- **beta\_x, alpha\_x, eta\_x, etap\_x, beta\_y, alpha\_y, eta\_y, etap\_y** — If **periodic**=0, these are the starting values for the lattice functions.
- **n\_points** — Number of points in each phase-space dimension.
- **max\_fit\_order** — Maximum order of fits using in determining the matrix elements.

## aperture\_data

### 7.8 aperture\_data

- type: setup command.
- function: specify a file from which to take x and y aperture data vs s.
- note: this command is also available under the name **aperture\_input**.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&aperture\_data

```
    STRING input = NULL;  
    long periodic = 1;  
    long persistent = 0;  
    long disable = 0;
```

&end

- **input** — Name of SDDS file supplying the aperture data. The following columns are all required, in double or float type, with units of **m** (meters).
  1. **s** — Distance along the central trajectory.
  2. **xHalfAperture** — Half aperture in the horizontal.
  3. **yHalfAperture** — Half aperture in the vertical.
  4. **xCenter** — Center of the aperture in the horizontal.
  5. **yCenter** — Center of the aperture in the vertical.
- **periodic** — If non-zero, the aperture is a periodic function of **s**, with period equal to the range of the data.
- **persistent** — If non-zero, the aperture data persists across subsequent **run\_setup** commands. By default, the aperture data is forgotten when a new **run\_setup** command is seen.
- **disable** — If non-zero, the command is ignored.

## bunched\_beam

### 7.9 bunched\_beam

- type: setup command.
- sequence: must follow `run_control`.
- function: set up for tracking of particle coordinates with various distributions.
- In *Pelegant*, the exact particles generated will change as the number of cores is changed.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&bunched\_beam

```
STRING bunch = NULL;
long n_particles_per_bunch = 1;
double time_start = 0;
STRING matched_to_cell = NULL;
double emit_x = 0;
double emit_nx = 0;
double beta_x = 1.0;
double alpha_x = 0.0;
double eta_x = 0.0;
double etap_x = 0.0;
double emit_y = 0;
double emit_ny = 0;
double beta_y = 1.0;
double alpha_y = 0.0;
double eta_y = 0.0;
double etap_y = 0.0;
long use_twiss_command_values = 0;
long use_moments_output_values = 0;
double Po = 0.0;
double sigma_dp = 0.0;
double sigma_s = 0.0;
double dp_s_coupling = 0;
double emit_z = 0;
double beta_z = 0;
double alpha_z = 0;
double momentum_chirp = 0;
long one_random_bunch = 1;
long symmetrize = 0;
long halton_sequence[3] = {0, 0, 0};
long halton_radix[6] = {0, 0, 0, 0, 0, 0};
long optimized_halton = 0;
long randomize_order[3] = {0, 0, 0};
long limit_invariants = 0;
long limit_in_4d = 0;
long enforce_rms_values[3] = {0, 0, 0};
```

```

double distribution_cutoff[3] = {2, 2, 2};
STRING distribution_type[3] = {"gaussian","gaussian","gaussian"};
double centroid[6] = {0.0, 0.0, 0.0, 0.0, 0.0, 0.0};
long first_is_fiducial = 0;
long save_initial_coordinates = 1;
&end

```

- **bunch** — The (incomplete) name of an SDDS file to which the phase-space coordinates of the bunches are to be written. Recommended value: “%s.bun”.
- **n\_particles\_per\_bunch** — Number of particles in each bunch.
- **time\_start** — The central value of the time coordinate for the bunch.
- **matched\_to\_cell** — The name of a beamline from which the Twiss parameters of the bunch are to be computed.
- **emit\_X** — RMS emittance for the X plane.
- **emit\_nX** — RMS normalized emittance for the X plane. Ignored if **emit\_X** is nonzero.
- **beta\_X, alpha\_X, eta\_X, etap\_X** — Twiss parameters for the X plane.
- **use\_twiss\_command\_values** — If nonzero, then the values for  $\beta$ ,  $\alpha$ ,  $\eta$ , and  $\eta'$  are taken from the **twiss\_output** command. It is an error if no **twiss\_output** command has been given.
- **use\_moments\_output\_values** — If nonzero, then the beam is generated to match the 6D matched, equilibrium beam moments computed by the **moments\_output** command. The distribution type must be gaussian. This mode is incompatible with using closed orbit correction with **start\_from\_centroid=1** (the default value).
- **Po** — Central momentum of the bunch.
- **sigma\_dp, sigma\_s** — Fractional momentum spread, ffi, and bunch length. Note that **sigma\_s** is actually the length in  $\beta_z * c * t$ , so that for  $\beta_z \ll 1$  the length of the bunch in time will be greater than one might expect.
- **dp\_s\_coupling** — Specifies the coupling between s and ffi, defined as  $\langle sffi \rangle / (\alpha_s \alpha_{ffi})$ .

- **emit\_z, beta\_z, alpha\_z** — Provide another way to specify the longitudinal phase space, either separately from or in combination with **sigma\_dp, sigma\_s**, and **dp\_s\_coupling**.

Basically, which values **elegant** uses depends on what one sets to nonzero values. If one sets **emit\_z**, then **sigma\_dp, sigma\_s**, and **dp\_s\_coupling** are ignored. If one doesn't set **emit\_z**, then **elegant** uses **sigma\_dp** and **sigma\_s**; it additionally uses **alpha\_z** if it is nonzero, otherwise it uses **dp\_s\_coupling**. For reference, the relationship between them is  $C = \frac{\Sigma_{56}}{\sqrt{\Sigma_{55}\Sigma_{66}}} = -\frac{\alpha}{\sqrt{1+\alpha^2}}$ . Note that to impart a chirp that results in compression for  $R_{56} < 0$  (e.g., a normal four-dipole chicane), one must have  $\alpha_z < 0$  or  $C > 0$ .

- **momentum\_chirp** — Permits imparting an additional momentum chirp to the beam, in units of 1/m. E.g., a value of 1 indicates that a 1mm long bunch has a linear variation in momentum of 0.1% from end-to-end. A positive chirp is needed to provide compression of a bunch with an ordinary  $R_{56} < 0$  four-dipole chicane.

- **one\_random\_bunch** — If non-zero, then only one random particle distribution is generated. Otherwise, a new distribution will be generated for every simulation step.
- **enforce\_rms\_values[3]** — Flags, one for each plane, indicating whether to force the distribution to have the specified RMS properties.
- **distribution\_cutoff[3]** — Distribution cutoff parameters for each plane. For gaussian distributions, this is the number of sigmas to use. For other distributions (except dynamic aperture), this number simply multiplies the sizes. This is potentially confusing and hence it is suggested that the distribution cutoff be set to 1 for nongaussian beams.

The exception is “dynamic-aperture” distribution type. In this case, the cutoff value is the number of grid points in the dimension in question.

- **distribution\_type[3]** — Distribution type for each plane. May be “gaussian”, “hard-edge”, “uniform-ellipse”, “shell”, “dynamic-aperture”, “line”, “halo(gaussian)”.

For the transverse plane, the interpretation of the emittance is different for the different beam types. For gaussian beams, the emittances are rms values. For all other types,  $\sqrt{\epsilon * \beta}$  times the distribution cutoff defines the edge of the beam in position space, while  $\sqrt{\epsilon * (1 + \alpha^2)}/\beta$  times the distribution cutoff defines the edge of the beam in slope space.

A hard-edge beam is a uniformly-filled parallelogram in phase space. A uniform-ellipse beam is a uniformly-filled ellipse in phase space. A shell beam is a hollow ellipse in phase space. A dynamic aperture beam has zero slope and uniform spacing in position coordinates. A line beam is a line in phase space. A “halo(gaussian)” beam is the part of the gaussian distribution *beyond* the distribution cutoff.

- **limit\_invariants** — If non-zero, the distribution cutoffs are applied to the invariants, rather than to the coordinates. This is useful for gaussian beams when the distribution cutoff is small.
- **limit\_in\_4d** — If non-zero, then the transverse distribution is taken to be a 4-d gaussian or uniform distribution. One of these must be chosen using the **distribution\_type** control. It must be the same for x and y. This is useful, for example, if you want to make a cylindrically symmetric beam.
- **symmetrize** — If non-zero, the distribution is symmetric under changes of sign in the coordinates. Automatically results in a zero centroid for all coordinates.
- **halton\_sequence[3]** and **halton\_radix[6]** and **optimized\_halton** — This provides a “quiet-start” feature by choosing Halton sequences in place of random number generation. There are three new variables that control this feature. **halton\_sequence** is an array of three flags that permit turning on Halton sequence generation for the horizontal, vertical, or longitudinal planes. For example, **halton\_sequence[0] = 3\*1** will turn on Halton sequences for all three planes, while **halton\_sequence[2] = 1**, will turn it on for the longitudinal plane only.  
  
**halton\_radix** is an array of six integers that permit giving the radix for each sequence (i.e., x, x', y, y', t, p). Each radix must be a prime number. One should never use the same prime for two sequences, unless one randomizes the order of the sequences relative to each other (see the next item). If these are left at zero, then elegant chooses values that eliminate phase-space banding to some extent. The user is cautioned to plot all coordinate combinations for the initial phase space to ensure that no unacceptable banding is present.



A suggested way to use Halton sequences is to set `halton_radix[0] = 2, 3, 2, 3, 2, 3` and to set `randomize_order[0] = 2, 2, 2, .`. This avoids banding that may result from choosing larger radix values.

`optimized_halton` uses the improved halton sequence [33]. (Algorithm 659, Collected Algorithm from ACM. Derandom Algorithm is added by Hongmei CHI (CS/FSU)). It avoids the banding problem automatically and the `halton_radix` values are ignored.

- `randomize_order[3]` — Allows randomizing the order of assigned coordinates for the pairs  $(x, x')$ ,  $(y, y')$ , and  $(t, p)$ . 0 means no randomization; 1 means randomize  $(x, x', y, y', t, p)$  values independently, which destroys any  $x$ - $x'$ ,  $y$ - $y'$ , and  $t$ - $p$  correlations; 2 means randomize  $(x, x')$ ,  $(y, y')$ , and  $(t, p)$  in pair-wise fashion. This is used with Halton sequences to remove banding. It is suggested that the user employ `sddsanalyzebeam` to verify that the beam properties when randomization is used.
- `centroid[6]` — Centroid offsets for each of the six coordinates.
- `first_is_fiducial` — Specifies that the first beam generated shall be a single particle beam, which is suitable for fiducialization. See the section on “Fiducialization in `elegant`” for more discussion.
- `save_initial_coordinates` — A flag that, if set, results in saving initial coordinates of tracked particles in memory. This is the default behavior. If unset, the initial coordinates are not saved, but are regenerated each time they are needed. This is more memory efficient and is useful for tracking very large numbers of particles.

## change\_particle

### 7.10 change\_particle

- type: action command.
- function: change the particle type from the default value of “electron.”
- sequence: must precede `run_setup`.
- N.B.: this feature has had limited testing, mostly to verify that electron tracking is not impacted by the implementation. Please use with caution and be alert for suspicious results.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&change_particle
  STRING name = "electron";
  double mass_ratio = 0;
  double charge_ratio = 0;
&end
```

- `name` — The name of the particle to use. Possible values are `electron`, `positron`, `proton`, `muon`, and `custom`.
- `mass_ratio`, `charge_ratio` — If the particle name is “custom,” these parameters specify the mass and charge of the particle relative to the electron. E.g., for an anti-proton, one would use a mass ratio of 1836.18 and a charge ratio of 1.

## chaos\_map

### 7.11 chaos\_map

- type: major action command.
- function: compute chaos map from tracking. Note that the number of turns tracked is set by the `run_control` command.
- can use parallel resources (Pelegant)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- NB: this feature is new in 2019.4 and somewhat experimental. Please report problems on the forum.

```
&chaos_map
  STRING output = NULL;
  double xmin = -0.1;
  double xmax = 0.1;
  double ymin = 1e-6;
  double ymax = 0.1;
  double delta_min = 0;
  double delta_max = 0;
  long nx = 20;
  long ny = 21;
  long ndelta = 1;
  long forward_backward = 0;
  double change_x = 1e-6;
  double change_y = 1e-6;
  long verbosity = 1;
&end
```

- **output** — The (incomplete) name of an SDDS file to send output to. Recommended value: “%s.cmap”. For the parallel version, particles will be listed in essentially random order. If needed, `sddssort` can be used to sort particles by initial coordinates.
- **xmin, xmax** — Limits of grid of initial x coordinates for tracking.
- **ymin, ymax** — Limits of grid of initial y coordinates for tracking. **ymin** should be a small, positive value so that there is some betatron oscillation from which to get the tune.
- **delta\_min, delta\_max** — Limits of grid of initial  $\delta$  coordinates for tracking. Note that particles are not centered around the dispersive closed orbit. Hence, the tracking is appropriate to simulation of dynamics from a touschek scattering event.
- **nx** — Number of values of x coordinate in the grid.
- **ny** — Number of values of y coordinate in the grid.
- **ndelta** — Number of values of  $\delta$  coordinate in the grid.

- **forward\_backward** — If non-zero, uses the forward/backward integration technique of Y. Li *et al.* [56]. The number of passes tracked is still controlled by the **n\_passes** parameter of **run\_control**. In addition, the number of iterations of forward and backward tracking is given by the value of **forward\_backward**. If zero, a less interesting technique is used that computes the change in  $J_x$  and  $J_y$  from tracking with small changes in initial conditions.
- **change\_x, change\_y** — If **forward\_backward** is zero, gives the perturbation to initial x and y used to assess chaotic motion from divergence of trajectories.
- **verbosity** — If nonzero, prints possibly useful information while running.

## chromaticity

### 7.12 chromaticity

- type: setup command.
- function: set up for chromaticity correction.
- sequence: should follow `twiss_output`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&chromaticity
  STRING sextupoles = NULL;
  STRING exclude = NULL;
  double dnux_dp = 0;
  double dnuy_dp = 0;
  double sextupole_tweek = 1e-3;
  double correction_fraction = 0.9;
  long n_iterations = 5;
  double tolerance = 0;
  STRING strength_log = NULL;
  long change_defined_values = 0;
  double strength_limit = 0;
  long use_perturbed_matrix = 0;
  long exit_on_failure = 0;
  long update_orbit = 0;
  long verbosity = 1;
  double dK2_weight = 1;
&end
```

- **sextupoles** — List of names of elements to use to correct the chromaticities. Several names may be given and names may include wildcards. If so, then sextupoles in each group are changed by the same amount for each iteration. This would typically be used when the sextupoles are nominally identical (though perhaps differing in strength because of introduced errors). If that's not the case, the iteration may fail to converge.
- **exclude** — List of names of elements to exclude. This may be used to exclude some sextupoles that are matched by wildcards in the **sextupole** list.
- **dK2\_weight** — Weighting factor that is used to minimize the mean-square changes in  $K_2$  values in the event that there are more than two families.
- **dnux\_dp**, **dnuy\_dp** — Desired chromaticity values.
- **sextupole\_tweek** — Amount by which to tweak the sextupoles to compute derivatives of chromaticities with respect to sextupole strength. [The word “tweak” is misspelled “tweek” in the code.]
- **correction\_fraction** — Fraction of the correction to apply at each iteration. In some cases, correction is unstable at this number should be reduced.

- **n\_iterations** — Number of iterations of the correction to perform.
- **tolerance** — Stop iterating when chromaticities are within this value of the desired values.
- **strength\_log** — The (incomplete) name of an SDDS file to which the sextupole strengths will be written. Recommended value: “%s.ssl”.
- **change\_defined\_values** — Changes the defined values of the sextupole strengths. This means that when the lattice is saved (using **save\_lattice**), the sextupoles will have the corrected values. This would be used for correcting the chromaticity of a design lattice, for example, but not for correcting chromaticity of a perturbed lattice.
- **strength\_limit** — Limit on the absolute value of sextupole strength ( $K_2$ ).
- **use\_perturbed\_matrix** — If nonzero, requests use of the perturbed correction matrix in performing correction. For difficult lattices with large errors, this may be necessary to obtain correction. In general, it is not necessary and only slows the simulation.
- **exit\_on\_failure** — If nonzero, then failure to reach the desired chromaticities within the tolerance results in the program exiting.
- **update\_orbit** — If non-zero, the orbit calculation is updated after each  $n^{th}$  adjustment of the sextupoles.
- **verbosity** — Increasing positive values result in increasing amounts of information printed during execution.

## closed\_orbit

### 7.13 closed\_orbit

- type: setup command.
- function: set up for computation of the closed orbit.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&closed_orbit
  STRING output = NULL;
  long output_monitors_only = 0;
  long start_from_centroid = 1;
  long start_from_dp_centroid = 0;
  double closed_orbit_accuracy = 1e-12;
  long closed_orbit_iterations = 40;
  long fixed_length = 0;
  long start_from_recirc = 0;
  long verbosity = 0;
  double iteration_fraction = 0.9;
  double fraction_multiplier = 1.05;
  double multiplier_interval = 5;
  long output_monitors_only = 0;
  long tracking_turns = 0;
  long disable = 0;
&end
```

- **output** — The (incomplete) name of an SDDS file to which the closed orbits will be written. Recommended value: “%s.clo”.
- **output\_monitors\_only** — If non-zero, indicates that the closed orbit output should include only the data at the locations of the beam-position monitors.
- **start\_from\_centroid** — A flag indicating whether to force the computation to start from the centroids of the beam distribution.
- **start\_from\_dp\_centroid** — A flag indicating whether to force the computation to use the momentum centroid of the beam for the closed orbit. This can allow computing the closed orbit for an off-momentum beam, then starting the beam on that orbit using the **offset\_by\_orbit** or **center\_on\_orbit** parameters of the **track** command. In contrast to the **start\_from\_centroid**, this command doesn’t force the algorithm to start from the beam transverse centroids.
- **closed\_orbit\_accuracy** — The desired accuracy of the closed orbit, in terms of the difference between the start and end coordinates, in meters.
- **closed\_orbit\_iterations** — The number of iterations to take in finding the closed orbit.
- **iteration\_fraction** — Fraction of computed change that is used each iteration. For lattices that are very nonlinear or close to unstable, a number less than 1 can be helpful. Otherwise, it only slows the simulation.

- **fixed\_length** — A flag indicating whether to find a closed orbit with the same length as the design orbit by changing the momentum offset.
- **start\_from\_recirc** — A flag indicating whether to compute the closed orbit from the recirculation (**recirc**) element in the beamline. In general, if one has a recirculation element, one should give this flag.
- **verbosity** — A larger value results in more printouts during the computations.
- **iteration\_fraction** — Controls the fraction of the update to apply when iterating toward a closed orbit. Smaller numbers give less chance of instability at the price of slower convergence.
- **fraction\_multiplier** — Multiplier to apply to the iteration fraction if iteration is converging.
- **multiplier\_interval** — Interval in number of iterations at which to adjust the iteration fraction.
- **output\_monitors\_only** — If non-zero, output file contains data only at beam position monitors, i.e., at **MONI**, **HMON**, and **VMON** elements.
- **tracking\_turns** — If non-zero, the number of turns to track for determination of the closed orbit by averaging. This may be useful if the regular closed orbit algorithm complains about convergence issues.
- **disable** — If non-zero, disables the command.



## correct

### 7.14 correct

- type: setup command.
- sequence: must follow `run_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- function: set up for correction of the trajectory or closed orbit.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

`&correct`

```
STRING mode = "trajectory";
STRING method = "global";
STRING trajectory_output = NULL;
STRING corrector_output = NULL;
STRING statistics = NULL;
STRING bpm_output = NULL;
double corrector_tweek[2] = {1e-3, 1e-3};
double corrector_limit[2] = {0, 0};
double correction_fraction[2] = {1, 1};
double correction_accuracy[2] = {1e-6, 1e-6};
long do_correction[2] = {1, 1};
long remove_smallest_SVs[2] = {0, 0};
long keep_largest_SVs[2] = {0, 0};
double minimum_SV_ratio[2] = {0, 0};
long auto_limit_SVs[2] = {1, 1};
long removed_pegged[2] = {0, 0};
long threading_divisor[2] = {100, 100};
long threading_correctors[2] = {-1, -1};
double bpm_noise[2] = {0, 0};
double bpm_noise_cutoff[2] = {1.0, 1.0};
STRING bpm_noise_distribution[2] = {"uniform", "uniform"};
long verbose = 1;
long fixed_length = 0;
long fixed_length_matrix = 0;
long n_xy_cycles = 1;
long minimum_cycles = 1;
long force_alteration = 0;
long n_iterations = 1;
long prezero_correctors = 1;
long track_before_and_after = 0;
long start_from_centroid = 1;
long use_actual_beam = 0;
double closed_orbit_accuracy = 1e-12;
long closed_orbit_iterations = 10;
double closed_orbit_iteration_fraction = 1;
double closed_orbit_tracking_turns = 0;
```

```

    long use_perturbed_matrix = 0;
    long disable = 0;
    long use_response_from_computed_orbits = 0;
&end

```

In the case of array variables with dimension 2, the first entry is for the horizontal plane and the second is for the vertical plane.

- **mode** — Either “trajectory” or “orbit”, indicating correction of a trajectory or a closed orbit.
- **method** — For trajectories, may be “one-to-one”, “one-to-best”, “one-to-next”, “thread”, or “global”. “One-to-one” and “one-to-next” are the same: steering is performed by pairing one corrector with the next downstream BPM. “One-to-best” attempts to find a BPM with a large response to each corrector. “Thread” does corrector sweeps to work the beam through a beamline with apertures; it is quite slow. “Global” simply uses the global response matrix; it is the best choice if the trajectory is not lost on an aperture. For closed orbit, must be “global”.
- **trajectory\_output** — The (incomplete) name of an SDDS file to which the trajectories or orbits will be written. Recommended value: “%s.traj” or “%s.orb”.
- **corrector\_output** — The (incomplete) name of an SDDS file to which information about the final corrector strengths will be written. Recommended value: “%s.cor”. N.B.: although this file looks as if it can be used with the `load_parameters` command, care must be exercised because the data for the horizontal and vertical planes is on separate pages. Typically, one will need to use `sddscombine -merge=Step ...` in order to place the data from both planes on the same page. Also, be aware that if all correctors have the same name, using `change_defined_values=1` on `load_parameters` will not produce the expected results. See the documentation for `load_parameters` for more details.
- **statistics** — The (incomplete) name of an SDDS file to which statistical information about the trajectories (or orbits) and corrector strengths will be written. Recommended value: “%s.scor”.
- **bpm\_output** — The (incomplete) name of an SDDS file to which post-correction BPM errors will be written. The errors are the residual after correction, and include the effects of offsets (DX and DY), setpoints (XSETPOINT, YSETPOINT, and SETPOINT), and tilts (TILT). Recommended value: “%s.bpm”.
- **corrector\_tweek[2]** — The amount by which to change the correctors in order to compute correction coefficients for transport lines. [The word “tweak” is misspelled “tweek” in the code.] The default value, 1 mrad, may be too large for systems with small apertures. If you get an error message about “tracking failed for test particle,” try decreasing this value.
- **corrector\_limit[2]** — The maximum strength allowed for a corrector.
- **correction\_fraction[2]** — The fraction of the computed correction strength to actually use for any one iteration.
- **correction\_accuracy[2]** — The desired accuracy of the correction in terms of the RMS BPM values.

- `do_correction[2]` — Flags to allow disabling correction in one or both planes (if set to zero).
- `remove_smallest_SVs`, `keep_largest_SVs`, `minimum_SV_ratio`, `auto_limit_SVs` — These parameters control the elimination of singular vectors from the inverse response matrix, which can help deal with degeneracy in the correctors and reduce corrector strength. By default, the number of singular vectors is limited to the number of BPMs, which is a basic condition for stability; this can be defeated by setting `auto_limit_SVs` to 0 for the desired planes. Set `remove_smallest_SVs` to require removal of a given number of vectors with the smallest singular values; this is ignored if `auto_limit_SVs` is also requested and would remove more SVs. Set `keep_largest_SVs` to require keeping at most a given number of the largest SVs. Set `minimum_SV_ratio` to require removal of any vectors with singular values less than a given factor of the largest singular value.
- `remove_pegged[2]` — If nonzero, then for the plane in question pegged correctors will be removed from the correction matrix. This results in recomputation of the matrix, following which correction continues with the reduced set of correctors. The pegged corrector is left at its last value.
- `threading_divisor` — In threading mode trajectory correction, each corrector is varied between 0 and  $\pm\theta_{\max}$ , where  $\theta_{\max}$  is the strength limit. This parameter sets the number of steps to divide the corrector range into on the positive and negative sides. A smaller value results in faster execution but is less reliable.
- `threading_correctors` — In threading mode trajectory correction, gives the number of correctors upstream of the loss point to use for threading the beam further through the system.
- `bpm_noise[2]` — The BPM noise level.
- `bpm_noise_cutoff[2]` — Cutoff values for the random distributions of BPM noise.
- `bpm_noise_distribution[2]` — May be either “gaussian”, “uniform”, or “plus\_or\_minus”.
- `verbose` — If non-zero, information about the correction is printed during computations.
- `fixed_length` — Indicates that the closed orbit length should be kept the same as the design orbit length by changing the momentum offset of the beam.
- `fixed_length_matrix` — Indicates that for fixed-length orbit correction, the fixed-length matrix should be computed and used. This will improve convergence but isn’t always needed.
- `n_xy_cycles` — Number of times to alternate between correcting the x and y planes.
- `force_alternation` — Forces alternation between x and y correction even if one plane appears to have converged.
- `minimum_cycles` — The minimum number of x-y cycles to perform, even if the correction does not improve.
- `n_iterations` — Number of iterations of the correction in each plane for each x/y cycle.
- `prezero_correctors` — Flag indicating whether to set the correctors to zero before starting.

- `track_before_and_after` — Flag indicating whether tracking should be done both before and after correction.
- `start_from_centroid` — Flag indicating that correction should start from the beam centroid. For orbit correction, only the beam momentum centroid is relevant.
- `use_actual_beam` — Flag indicating that correction should employ tracking of the beam distribution rather than a single particle. This is valid for trajectory correction only.
- `closed_orbit_accuracy` — Accuracy of closed orbit computation.
- `closed_orbit_iterations` — Number of iterations of closed orbit computation.
- `closed_orbit_iteration_fraction` — Fraction of change in closed orbit to use at each iteration.
- `closed_orbit_tracking_turns` — If non-zero, the absolute value gives the number of turns to track for determination of the closed orbit by averaging. This may be useful if the regular closed orbit algorithm complains about convergence issues. If less than zero, then *only* this method is used. If greater than zero, then regular orbit determination is tried first, and tracking is used as a fallback.
- `use_perturbed_matrix` — If nonzero, specifies that prior to each correction `elegant` shall recompute the response matrix. This is useful if the lattice is changing significantly between corrections.
- `disable` — If nonzero, the command is ignored.
- `use_response_from_computed_orbits` — If nonzero, in-plane response matrices are computed using differences of closed orbits, which is slower but may be more accurate. For cross-plane matrices, this is always the case.

## correction\_matrix\_output

### 7.15 correction\_matrix\_output

- type: setup/action command.
- function: provide output of the orbit/trajectory correction matrix.
- sequence: must follow `run_setup` and definition of steering elements (if wanted, with `steering_element`).
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&correction_matrix_output
  STRING response[4] = NULL, NULL;
  STRING inverse[2] = NULL, NULL;
  long KnL_units = 0;
  long BnL_units = 0;
  long output_at_each_step = 0;
  long output_before_tune_correction = 0;
  long fixed_length = 0;
  long coupled = 0;
  long use_response_from_computed_orbits = 0;
&end
```

- **response** — Array of (incomplete) filenames for SDDS output of the x and y response matrices, plus the cross-plane response matrices. Recommended values, in order: “%s.hrm” (horizontal response to horizontal correctors), “%s.vrm” (vertical response to vertical correctors), “%s.vhrm” (vertical response to horizontal correctors), and “%s.hvrn” (horizontal response to vertical correctors).
- **inverse** — Array of (incomplete) filenames for SDDS output of the x and y inverse response matrices. Recommended values: “%s.hirm” and “%s.virm”.
- **KnL\_units** — Flag that, if set, indicates use of “units” of m/K0L rather than m/rad. This results in a sign change for the horizontal data.
- **BnL\_units** — Flag that, if set, indicates use of “units” of m/(T\*m) rather than m/rad. This is useful for linac work in that the responses are automatically scaled with beam momentum.
- **output\_at\_each\_step** — Flag that, if set, specifies output of the data at each simulation step. By default, the data is output immediately for the defined lattice.
- **output\_before\_tune\_correction** — Flag that, if set, specifies that when `output_at_each_step` is set, that output shall occur prior to correcting the tunes.
- **fixed\_length** — Flag that, if set, specifies output of the fixed-path-length matrix.
- **coupled** — If nonzero, the cross-plane response matrices are computed.
- **use\_response\_from\_computed\_orbits** — If nonzero, in-plane response matrices are computed using differences of closed orbits, which is slower but may be more accurate. For cross-plane matrices, this is always the case.

## correct\_tunes

### 7.16 correct\_tunes

- type: setup command.
- function: set up for correction of the tunes.
- sequence: should follow `twiss_output`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&correct_tunes
  STRING quadrupoles = NULL;
  STRING exclude = NULL;
  double tune_x = 0;
  double tune_y = 0;
  long n_iterations = 5;
  double correction_fraction = 0.9;
  double tolerance = 0;
  long step_up_interval = 0;
  double max_correction_fraction = 0.9;
  double delta_correction_fraction = 0.1;
  long update_orbit = 0;
  STRING strength_log = NULL;
  long change_defined_values = 0;
  long use_perturbed_matrix = 0;
  double dK1_weight = 1;
&end
```

- **quadrupoles** — List of names of quadrupoles to be used. Several names may be given and the names may include wildcards. If so, then quadrupoles in each group are changed by the same amount for each iteration. This would typically be used when the quadrupoles are nominally identical (though perhaps differing in strength because of introduced errors). If that's not the case, the iteration may fail to converge
- **exclude** — List of names of elements to exclude. This may be used to exclude some quadrupoles that are matched by wildcards in the **quadrupoles** list.
- **dK1\_weight** — Weighting factor that is used to minimize the mean-square changes in  $K_1$  values in the event that there are more than two families.
- **tune\_x**, **tune\_y** — Desired x and y tune values. If not given, the desired values are assumed to be the unperturbed tunes.
- **n\_iterations** — The number of iterations of the correction to perform.
- **correction\_fraction** — The fraction of the correction to apply at each iteration.
- **tolerance** — When both tunes are within this value of the desired tunes, the iteration is stopped.

- `step_up_interval` — Interval between increases in the correction fraction.
- `max_correction_fraction` — Maximum correction fraction to allow.
- `delta_correction_fraction` — Change in correction fraction after each `step_up_interval` steps.
- `update_orbit` — If non-zero, the orbit calculation is updated after each  $n^{th}$  adjustment of the quadrupoles.
- `strength_log` — The (incomplete) name of a SDDS file to which the quadrupole strengths will be written as correction proceeds. Recommended value: “%s.qst”.
- `change_defined_values` — Changes the defined values of the quadrupole strengths. This means that when the lattice is saved (using `save_lattice`), the quadrupoles will have the corrected values. This would be used for correcting the tunes of a design lattice, for example, but not for correcting tunes of a perturbed lattice.
- `use_perturbed_matrix` — If nonzero, requests use of the perturbed correction matrix in performing correction. For difficult lattices with large errors, this may be necessary to obtain correction. In general, it is not necessary and only slows the simulation.

## coupled\_twiss\_output

### 7.17 coupled\_twiss\_output

- type: setup/action command.
- function: set up or execute computation of coupled twiss parameters and beam sizes
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&coupled_twiss_output
  STRING filename = NULL;
  long output_at_each_step = 0;
  long emittances_from_twiss_command = 1;
  double emit_x = 0;
  double emittance_ratio = 0.01;
  double sigma_dp = 0;
  long calculate_3d_coupling = 1;
  long verbosity = 0;
  long concat_order = 2;
&end
```

- **filename** — The (incomplete) name of the SDDS file to which coupled twiss parameters and beam sizes will be written. Suggested value: “%s.ctwi”.
- **output\_at\_each\_step** — If nonzero, then this is a setup command and results in computations occurring for each simulation step (e.g., for each perturbed machine if errors are included). If zero, then this is an action command and computations are done immediately (e.g., for the unperturbed machine). If you wish to compute Twiss parameters on a closed orbit or after other calculations, be sure to set this control to a nonzero value.
- **emittances\_from\_twiss\_command** — If nonzero, then the values of the horizontal emittance and the momentum spread are taken from the uncoupled computation done with the `twiss_output` command. In this case, the user must issue a `twiss_output` command prior to the `coupled_twiss_output`. If zero, then the values of the horizontal emittance and the momentum spread are taken from the parameters `emit_x` and `sigma_dp`, respectively.
- **emit\_x** — Gives the horizontal emittance, if `emittances_from_twiss_command=0`.
- **emittance\_ratio** — Gives the ratio of the x and y emittances. Used to determine the vertical emittance from the horizontal emittance. Note that the computation is not self-consistent. I.e., the user is free to enter any emittance ratio desired, whether it is consistent with the machine optics or now.
- **sigma\_dp** — Gives the momentum spread, if `emittances_from_twiss_command=0`.

This feature was added to `elegant` using code supplied by V. Sajaev, based on Ripkin’s method. The code computes the coupled lattice functions, then uses the supplied emittance, emittance ratio, and momentum spread to compute the beam sizes, bunch length (if rf is included), and beam tilt.



## divide\_elements

### 7.18 divide\_elements

- type: setup command.
- function: define how to subdivide certain beamline elements.
- sequence: must precede `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - Any number of these commands may be given.
  - Not effective unless given prior to `run_setup`.
  - The `element_divisions` field in `run_setup` provides a simpler, but less flexible, method of performing element division. At present, these element types may be divided: `CSBEND`, `CSRDRIFT`, `DRIFT`, `EDRIFT`, `KOCT`, `KQUAD`, `KQUSE`, `KSEXT`, `OCTU`, `QUAD`, `RBEND`, `RFCA`, `SBEND`, `SEXT`, and `SOLE`.
  - Only effective if given prior to the `run_setup` command.
- warnings:
  - Using `save_lattice` and element divisions together will produce an incorrect lattice file.
  - Element subdivision may produce unexpected results when used with `load_parameters` or parameters saved via the `parameter` entry of the `run_setup` command. If you wish to load parameters while doing element divisions or if you wish to load parameters from a run that had element divisions in effect, you should not load length data for any elements that are (or were) split. The name and item pattern features of `load_parameters` are helpful in restricting what is loaded.

```
&divide_elements
  STRING name = NULL;
  STRING type = NULL;
  STRING exclude = NULL;
  long divisions = 0;
  double maximum_length = 0;
  long clear = 0;
&end
```

- `name` — A possibly wildcard-containing string specifying the elements to which this specification applies.
- `type` — A possibly wildcard-containing string specifying the element types to which this specification applies.
- `exclude` — A possibly wildcard-containing string specifying elements to be excluded from the specification.

- `divisions` — The number of times to subdivide the specified elements. If zero, then `maximum_length` should be nonzero.
- `maximum_length` — The maximum length of a slice. This is usually preferable to specifying the number of divisions, particularly when the elements divided may be of different lengths. If zero, then `divisions` should be nonzero.
- `clear` — If nonzero, all prior division specifications are deleted.

## elastic\_scattering

### 7.19 elastic\_scattering

- type: major action command
- function: perform simulation of elastic scattering at multiple  $s$  locations, for use in computing elastic gas scattering lifetime and loss distribution
- sequence: must follow `run_control`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - Only available in Pelegant.
  - Data may be postprocessed with the command `elasticScatteringAnalysis`.

```
&elastic_scattering
  STRING losses = NULL;
  STRING output = NULL;
  STRING log_file = NULL;
  double theta_min = 0.001;
  double theta_max = 0.010;
  long n_theta = 11;
  long n_phi = 37;
  long twiss_scaling = 0;
  double s_start = 0;
  double s_end = DBL_MAX;
  STRING include_name_pattern = NULL;
  STRING include_type_pattern = NULL;
  long verbosity = 1;
&end
```

- **losses** — The (incomplete) name of an SDDS file to which the record of initial scattering location, initial scattering angle, and loss coordinates will be written.
- **output** — The (incomplete) name of an SDDS file to which the final coordinates of all surviving particles will be written.
- **log\_file** — The (incomplete) name of an SDDS file to which statistical data will be written as the simulations run. Users should check the **MinParticles** and **MaxParticles** columns as the simulation runs to ensure reasonable load balance (e.g., within 10-20%). If balance is poor, consider changing the values of **n\_phi** and **n\_theta** slightly. The product of these values should not evenly divide the number of working cores (which is one less than the total number of cores).
- **theta\_min** — Minimum polar scattering angle in radians. Should be small enough that no particle scattered by this angle are lost, regardless of the scattering location. See also **twiss\_scaling**.

- **theta\_max** — Maximum polar scattering angle in radians. Should be large enough that no particle scattered by this angle survives, regardless of scattering location.
- **n\_theta** — Number of polar scattering angle values on the range **theta\_min** to **theta\_max**.
- **n\_phi** — Number of azimuthal scattering angles on the range  $[0, \pi]$ .
- **twiss\_scaling** — If nonzero, then **theta\_min** is scaled by  $\min(\sqrt{\beta_x(0)/\beta_x(s)}, \sqrt{\beta_y(0)/\beta_y(s)})$ , where  $s$  is the location of the scattering location and  $s = 0$  is the start of the lattice.
- **s\_start, s\_end** — Range of  $s$  location for simulated scattering sites.
- **include\_name\_pattern** — Wildcard-containing string to match to element names in selecting scattering sites.
- **include\_type\_pattern** — Wildcard-containing string to match to element types in selecting scattering sites.
- **verbosity** — Higher values may result in more verbose informational output.

## error\_element

### 7.20 error\_element

- type: setup command.
- sequence: must follow `run_control`.
- function: assert a random error definition for the accelerator.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&error_element
  STRING name = NULL;
  STRING element_type = NULL;
  STRING item = NULL;
  STRING type = "gaussian";
  double amplitude = 0.0;
  double cutoff = 3.0;
  long bind = 1;
  long bind_number = 0;
  longn bind_across_names = 0;
  long post_correction = 0;
  long fractional = 0;
  long additive = 1;
  long allow_missing_elements = 0;
  STRING after = NULL;
  STRING before = NULL;
&end
```

- **name** — The possibly wildcarded name of the elements for which errors are being specified.
- **element\_type** — An optional, possibly wildcarded string giving the type of elements to which the errors should be applied. E.g., `element_type=*MON*` would match all beam position monitors. If this item is given, then **name** may be left blank.
- **item** — The parameter of the elements to which the error pertains.
- **type** — The type of random distribution to use. May be one of “uniform”, “gaussian”, or “plus\_or\_minus”. A “plus\_or\_minus” error is equal in magnitude to the amplitude given, with the sign randomly chosen.
- **amplitude** — The amplitude of the errors.
- **cutoff** — The cutoff for the gaussian random distribution in units of the amplitude. Ignored for other distribution types.
- **bind**, **bind\_number**, **bind\_across\_names** — These parameters control “binding” of errors among elements, which means assigning the same error contribution to several elements. This occurs if **bind** is nonzero, **which it is by default!** If **bind** is negative, then the sign of the error will alternate between successive elements. **bind\_number** can be used to limit the number of elements bound together. In particular, if **bind\_number** is positive, then a positive

value of **bind** indicates that **bind\_number** successive elements having the same name will have the same error value. Finally, by default, **elegant** only binds the errors of objects having the same name, even if they are assigned errors by the same **error\_element** command (i.e., through a wildcard **name**). If **bind\_across\_names** is nonzero, then binding is done even for elements with different names.

- **post\_correction** — A flag indicating whether the errors should be added after orbit, tune, and chromaticity correction.
- **fractional** — A flag indicating whether the errors are fractional, in which case the amplitude refers to the amplitude of the fractional error.
- **additive** — A flag indicating that the errors should be added to the prior value of the parameter. If zero, then the errors replace the prior value of the parameter.
- **allow\_missing\_elements** — A flag indicating that execution may continue even if no matching elements are found.
- **after** — The name of an element. If given, the error is applied only to elements that follow the named element in the beamline.
- **before** — The name of an element. If given, the error is applied only to elements that precede the named element in the beamline.

## error\_control

### 7.21 error\_control

- type: setup command
- sequence: must follow `run_control`.
- function: overall control of random errors.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&error_control
  long clear_error_settings = 1;
  long summarize_error_settings = 0;
  long no_errors_for_first_step = 0;
  STRING error_log = NULL;
  double error_factor = 1;
&end
```

- `clear_error_settings` — Clear all previous error settings.
- `summarize_error_settings` — Summarize current error settings. *If non-zero, then the command has no other function except showing a summary of the current error settings.*
- `no_errors_for_first_step` — If non-zero, then there will be no errors for the first step. This can be useful for fiducialization of phase and momentum profiles.
- `error_log` — The (incomplete) name of a SDDS file to which error values will be written. Recommended value: “%s.erl”.
- `error_factor` — A value by which to multiply the error amplitudes in all `error` commands.

The proper use of this command can be confusing. A typical sequence will be as follows:

```
&error_control
  clear_error_settings = 1,
  error_log = %s.erl
&end

&error_element ... &end
&error_element ... &end
.
.
.
&error_element ... &end

&error_control
  summarize_error_settings = 1
&end
```

## find\_aperture

### 7.22 find\_aperture

- type: setup/major action command.
- function: find the aperture in (x, y) space for an accelerator.
- N.B.: can use parallel resources (**Pelegant**). Recommend using n-line mode with `nx*n_splits` greater than the number of cores (e.g., a factor of 10).
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&find_aperture
  STRING output = NULL;
  STRING search_output = NULL;
  STRING boundary = NULL;
  STRING mode = "many-particle";
  double xmin = -0.1;
  double xmax = 0.1;
  double xpmmin = 0.0;
  double xpmmax = 0.0;
  double ymin = 0.0;
  double ymax = 0.1;
  double ypmmin = 0.0;
  double ypmmax = 0.0;
  long nx = 21;
  long ny = 11;
  long n_splits = 0;
  double split_fraction = 0.5;
  double desired_resolution = 0.01;
  long assume_nonincreasing = 0;
  long verbosity = 0;
  long offset_by_orbit = 0;
  long n_lines = 11;
  long optimization_mode = 0;
  long full_plane = 0;
&end
```

- **output** — The (incomplete) name of an SDDS file to send output to. Recommended value: “%s.aper”.
- **mode** — May be “many-particle”, “single-particle”, “one-line”, “three-lines”, or “n-lines”. Many-particle searching is much faster than single-particle, but does not allow interval splitting to search for the aperture boundary. Both “many-particle” and “single-particle” modes involve searching from the outside inward, which improves speed but may result in including islands.

The line modes avoid this by searching from the origin outward. Of these, the one-line and three-line modes are special: one-line mode searches the line from the origin to  $(x_{max}, y_{max})$ . three-line mode searches this line, plus the lines from the origin to  $(x_{max}, 0)$  and  $(0, y_{max})$ .



For n-line mode, the number of lines is set with the `n_lines` parameter. With  $n > 3$ ,  $n$  lines are explored from  $(0,0)$  to  $(x_{max} * \sin(\theta), y_{max} * \cos(\theta))$ , where  $\theta$  takes values from  $-\pi/2$  to  $\pi/2$ . In these modes, the output file contains a parameter called “Area,” which gives the area of the dynamic aperture.

Also still recognized are other modes, namely, “five-line”, “seven-line”, “nine-line”, and “eleven-line”.

- **search\_output** — The (incomplete) name of an SDDS file for output of detailed information on each tracked particle (single-particle mode only). Recommended value: “%s.apso”.
- **boundary** — The (incomplete) name of an SDDS file for the boundary points of the aperture search. Recommended value: “%s.bnd”. Valid for many- and single-particle modes.
- **xmin, xmax, ymin, ymax** — Region of the aperture search, in spatial coordinates. The minimum values are relevant only for many- and single-particle modes.
- **xpmin, xpmax, ypmin, ypmax** — Region of the aperture search, in slope coordinates. The minimum values are relevant only for many- and single-particle modes. Ignored unless `xmin=xmax` and `ymin=ymax`.
- **nx** — For many- and single-particle modes, the number of x values to take in initial search. For line modes, this determines the initial x and y step sizes via  $\Delta x = x_{max}/n_x$  and  $\Delta y = y_{max}/n_x$ .
- **ny** — For many- and single-particle modes, the number of y values to take in search. Ignored for line modes.
- **n\_splits** — If positive, the number of times to do interval splitting. Interval splitting refers to searching between the original grid points in order to refine the results. This is done only for single-particle and line modes.
- **split\_fraction** — If interval splitting is done, how the interval is split.
- **desired\_resolution** — If interval splitting is done, fraction of `xmax-xmin` to which to resolve the aperture. Ignored for all but single-particle mode.
- **assume\_nonincreasing** — If this variable is non-zero, the search assumes that the aperture at  $y + \text{sign}(y) * \Delta y$  is no larger than that at  $y$ . This results in tracking of fewer particles but may give a pessimistic result. Used only for single- and multi-particle modes.
- **offset\_by\_orbit** — A flag indicating whether to offset the transverse beam coordinates by the closed orbit before tracking. The default value is zero for backward compatibility, but the recommended value is 1.
- **verbosity** — A larger value results in more printouts during computations.
- **n\_lines** — In “n-lines” mode, the number of lines to search.
- **optimization\_mode** — If non-zero, then `find_aperture` is a setup command and can be used with `elegant`’s internal optimizer. The quantity `DaArea` is defined, giving the area of the dynamic aperture for use in the penalty function. This is available only for the line search modes.

- `full_plane` — If non-zero, then the search covers both positive and negative y values. Only available in line-search modes.

## floor\_coordinates

### 7.23 floor\_coordinates

- type: action command.
- function: compute floor coordinates for an accelerator.
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&floor_coordinates
  STRING filename = NULL;
  double X0 = 0.0;
  double Z0 = 0.0;
  double theta0 = 0.0;
  long include_vertices = 0;
  long vertices_only = 0;
  long magnet_centers = 0;
  long store_vertices = 0;
&end
```

- **filename** — The (incomplete) name of an SDDS file to send output to. Recommended value: “%s.flr”.
- **X0, Z0, theta0** — Initial X, Z, and angle coordinate of the beamline.
- **include\_vertices** — Flag that, if set, specifies including in the output the coordinates of the vertices of bending magnets.
- **vertices\_only** — Flag that, if set, specifies that output will contain only the coordinates of the vertices of bending magnets.
- **magnet\_centers** — Flag that, if set, specifies that output will contain the coordinates of the centers of all magnets, where the center is defined as the average of the entrance and exit points. By default, the coordinates of the downstream end are given.
- **store\_vertices** — Flag that, if set, results in storing the floor coordinates for dipole magnet vertex points. The coordinates are stored in variables with names of the form *magnetName#occurrenceNumber-VP.property*, where *property* is X, Y, Z, theta, phi, and psi.

The “vertex point” for a dipole or string of dipoles is defined as the intersection of the straight lines from the ideal entrance and exit trajectories. The **s** quantity for the vertex is defined as the sum of the actual distance traveled to the start of the dipole or string of dipoles plus the straight-line distance from the entrance to the vertex. Hence, one cannot subtract the **s** values for two successive vertices and expect to get the distance between the vertices.

## frequency\_map

### 7.24 frequency\_map

- type: major action command.
- function: compute frequency map from tracking Note that the number of turns tracked is set by the `run_control` command.
- can use parallel resources (Pelegant)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&frequency_map
  STRING output = NULL;
  double xmin = -0.1;
  double xmax = 0.1;
  double ymin = 1e-6;
  double ymax = 0.1;
  double delta_min = 0;
  double delta_max = 0;
  long nx = 21;
  long ny = 21;
  long ndelta = 1;
  long verbosity = 1;
  long include_changes = 0;
  long quadratic_spacing = 0;
  long full_grid_output = 0;
&end
```

- **output** — The (incomplete) name of an SDDS file to send output to. Recommended value: “%s.fma”. For the parallel version, particles will be listed in essentially random order. If needed, `sddssort` can be used to sort particles by initial coordinates.
- **xmin, xmax** — Limits of grid of initial x coordinates for tracking.
- **ymin, ymax** — Limits of grid of initial y coordinates for tracking. **ymin** should be a small, positive value so that there is some betatron oscillation from which to get the tune.
- **delta\_min, delta\_max** — Limits of grid of initial  $\delta$  coordinates for tracking. Note that particles are not centered around the dispersive closed orbit. Hence, the tracking is appropriate to simulation of dynamics from a touschek scattering event.
- **nx** — Number of values of x coordinate in the grid.
- **ny** — Number of values of y coordinate in the grid.
- **ndelta** — Number of values of  $\delta$  coordinate in the grid.
- **verbosity** — If nonzero, prints possibly useful information while running.

- **include\_changes** — If nonzero, then computes not only the tunes, but also the changes in the tunes. This is expressed in terms of the diffusion, which is defined as

$$d = \log_{10} (\Delta\nu_x^2 + \Delta\nu_y^2) \quad (1)$$

where  $\Delta\nu_x$  and  $\Delta\nu_y$  are respectively the differences in x and y tunes from the first and second half of the tracking (the total number of turns is equal to the value set in **run\_setup**). The diffusion rate,

$$d_r = \log_{10} \left( \frac{\sqrt{\Delta\nu_x^2 + \Delta\nu_y^2}}{N} \right), \quad (2)$$

is also computed.  $d_r$  is the more conventional quantity, computed by programs such as TRACY and MAD [53].

- **quadratic\_spacing** — If non-zero, the spacing of points is quadratic rather than linear, thus emphasizing the higher amplitude regions.
- **full\_grid\_output** — If non-zero, all grid points are represented in the output file, even if tracking or tune determination failed. This makes it possible to plot with programs (e.g., **sddscontour**) that require a strictly uniform grid.

## global\_settings

### 7.25 global\_settings

- type: action command.
- sequence: should precede `run_setup`.
- function: change global settings.
- Command syntax, including use of equations and subcommands, is discussed in 7.2. One way to use the `global_settings` command is in a configuration file, which can be supplied via the `-configuration` option or `ELEGANT_CONFIGURATION` environment variable; an example of using this would be to set MPI I/O options on a per-system basis. N.B.: unlike other commands, values given for parameters in `global_settings` commands become the new default for subsequent invocations of the command during the same run. Hence multiple commands can be used to set individual values without overriding previously-given settings.

```
&global_settings
    long inhibit_fsync = 0;
    long echo_namelist = 1;
    long mpi_randomization_mode = 3;
    long exact_normalized_emittance = 0;
    double SR_gaussian_limit = 3.0;
    long inhibit_seed_permutation = 0;
    STRING log_file = NULL;
    STRING error_log_file = NULL;
    long mpi_io_force_file_sync = 0;
    long usleep_mpi_io_kludge = 0;
    long mpi_io_read_buffer_size = 0;
    long mpi_io_write_buffer_size = 0;
    long parallel_tracking_based_matrices = 1;
    long share_tracking_based_matrices = 1;
    double tracking_matrix_step_factor = 1;
    double tracking_matrix_points = 9;
&end
```

- `inhibit_fsync` — By default, `elegant` forces file synchronization across a network file system to ensure that users see up-to-date files as soon as possible. In cases where a great deal of output is generated, this can degrade performance. Setting this parameter to 1 will turn off synchronization until the end of the run.
- `echo_namelist` — By default, `elegant` echoes all namelist input to the terminal. If this parameter is set to 0, this output will be inhibited.
- `SR_gaussian_limit` — By default, `elegant` uses a  $3\text{-}\sigma$  cutoff for the gaussian random numbers used in simulation of synchrotron radiation from `CSBEND`, `CSRCSBEND`, `KQUAD`, `KSEXT`, and `\verb$SREFF$`. This parameter allows changing the cutoff.
- `inhibit_seed_permutation` — If nonzero, randomization of the user-supplied random number seed is *not* performed. This feature is useful in that it provides a higher degree of apparent randomness, in that small changes in the seed result in very different random sequences.

- **log\_file** — By default, **elegant** writes status information to the terminal. If a filename is supplied for this parameter, the output will instead go to the file. On Linux and Unix, using `/dev/null` will result in the output being discarded.
- **error\_log\_file** — By default, **elegant** writes error messages to the terminal. If a filename is supplied for this parameter, the output will instead go to the file. On Linux and Unix, using `/dev/null` will result in the output being discarded.
- **share\_tracking\_based\_matrices** — If non-zero, then the matrices determined by tracking for various elements (e.g., BRAT, BGGEXP, CCBEND) are computed only once for a set of identical elements, then shared. This can save considerable computation time.
- **mpi\_randomization\_mode** — Controls how the random numbers are seeded on multiple processors
  - 1 — This is the original default, which showed issues in some simulations. The seed on the  $i^{th}$  processor is  $s_0 + 2 * i$ .
  - 2 — The seed on the  $i^{th}$  processor is  $s_0 + 2 * i^2$ .
  - 3 — This is the new default. The seed on the  $i^{th}$  processor is  $s_0 + i * (i + 1)$ .
  - 4 — The seed on the  $i^{th}$  processor is  $s_0 + R_i$ , where  $R_i$  is the  $i^{th}$  random integer returned by the system `rand()` function.
- **exact\_normalized\_emittance** — By default, **elegant** uses an approximate computation for the normalized emittance, namely,  $\epsilon_n = \epsilon \langle \beta \gamma \rangle$ , where  $\epsilon$  is the geometric emittance computed from the trace-space coordinates. If this variable is set to a non-zero value, **elegant** instead uses a slower but more accurate method, namely, using the momentum coordinates. [43]. The results will show up in the **sigma** and **final** output files, if these are requested in the **run\_setup** command.
- **mpi\_io\_force\_file\_sync** — If non-zero, **Pelegant** will perform a file synchronization after writing each row of an SDDS file. This can *significantly* impact performance, but can solve problems on some filesystems that result in corrupted files or files in which zeros appear in place of the expected data.
- **mpi\_io\_read\_buffer\_size** — If non-zero, **Pelegant** will change the read buffer size to the given value. May allow improving read performance, but should be used with care.
- **mpi\_io\_write\_buffer\_size** — If non-zero, **Pelegant** will change the write buffer size to the given value. May allow improving write performance, but should be used with care.
- **usleep\_mpi\_io\_kludge** — If non-zero, **Pelegant** will sleep for the given number of microseconds after writing each row of an SDDS file. This can impact performance, but can solve problems on some filesystems that result in corrupted files or files in which zeros appear in place of the expected data. It may give better performance than setting **mpi\_io\_force\_file\_sync=1**. A value of 100 is suggested as a starting point, but this will be highly system-dependent.
- **parallel\_tracking\_based\_matrices** — If non-zero, then the matrices determined by tracking for various elements (e.g., BRAT, BGGEXP, CCBEND) are computed using parallel resources in **Pelegant**. This can save considerable wall clock time. N.B.: This is set to zero when using **parallel\_optimization\_setup**.

- **share\_tracking\_based\_matrices** — If non-zero, then the matrices determined by tracking for various elements (e.g., BRAT, BGGEXP, CCBEND) are computed only once for a set of identical elements, then shared.
- **tracking\_matrix\_step\_factor** — The default step size for tracking-based matrices is  $5 \times 10^{-5}$  (in the appropriate units for each coordinate). This can be increased or decreased by supplying a value for **tracking\_matrix\_step\_factor**.
- **tracking\_matrix\_points** — By default, five grid points are used in each dimension for tracking-based matrix determination. This can be increased by setting **tracking\_matrix\_points** to a larger, odd value, at the expense of longer running time. (The run time scales approximately as the sixth power of this value.)
- **tracking\_matrix\_step\_size** — Sets the step sizes, in each of the six coordinates, used for tracking-based matrix determination



## ignore\_elements

### 7.26 ignore\_elements

- type: setup command.
- function: causes specified elements to be ignored during tracking.
- Must precede `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - Any number of these commands may be given.
  - This command can provide improved *parallel* performance in cases where large numbers of non-transforming elements (e.g., `MARK` or `MONI` elements) exist in a beamline. (These elements can impact performance because `elegant` checks particles against aperture limits after *every* element.) Using the `show_element_timing` flag in `run_setup` can help determine if this will help.
  - This command cannot be used if `centroid` or `sigma` output is requested in `run_setup`.

```
&ignore_elements
STRING name = NULL,
STRING type = NULL,
STRING exclude = NULL,
    long disable = 0;
    long clear = 0;
    long completely = 0;
&end
```

- `name` — Possibly wild-card containing string specifying the elements to which the operation is to be applied.
- `type` — Possibly wild-card containing string specifying the element types to which the operation is to be applied.
- `exclude` — Possibly wild-card containing string specifying elements to be excluded from the operation. Does not affect elements included by other specifications.
- `disable` — If nonzero, the command is ignored.
- `clear` — If nonzero, all prior specifications are deleted.
- `completely` — If nonzero, the element is ignore not only for tracking, but for all purposes. (This allows, for example, requesting `sigma` and `centroid` output from `run_setup`.)

## inelastic\_scattering

### 7.27 inelastic\_scattering

- type: major action command
- function: perform simulation of inelastic scattering at multiple  $s$  locations, for use in computing inelastic gas scattering lifetime and loss distribution
- sequence: must follow `run_control`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - Only available in `Pelegant`.
  - Data may be postprocessed with the command `inelasticScatteringAnalysis`.

```
&inelastic_scattering
  STRING losses = NULL;
  STRING output = NULL;
  STRING log_file = NULL;
  double k_min = 0.001;
  STRING momentum_aperture = NULL;
  double momentum_aperture_scale = 0.90;
  double momentum_aperture_periodicity = 0;
  long n_k = 101;
  double s_start = 0;
  double s_end = DBL_MAX;
  STRING include_name_pattern = NULL;
  STRING include_type_pattern = NULL;
  long verbosity = 1;
  long soft_failure = 0;
  long allow_watch_file_output = 0;
&end
```

- `losses` — The (incomplete) name of an SDDS file to which the record of initial scattering location, initial scattering  $\delta$ , and loss coordinates will be written.
- `output` — The (incomplete) name of an SDDS file to which the final coordinates of all surviving particles will be written.
- `log_file` — The (incomplete) name of an SDDS file to which statistical data will be written as the simulations run. Users should check the `MinParticles` and `MaxParticles` columns as the simulation runs to ensure reasonable load balance (e.g., within 10-20%). If balance is poor, consider changing the value of `n_delta` slightly.
- `k_min` — Minimum energy  $k$  of the brehmsstrahlung photon as a fraction of the beam energy. The electron has  $\delta = -k$  after scattering. `k_min` should be small enough that no electron scattered by `-k_min` is lost, regardless of the scattering location.
- `n_k` — Number of scattering values on the range `k_min` to 1.

- **momentum\_aperture, momentum\_aperture\_scale** — If given, names a file giving the momentum aperture vs  $s$ , which is interpolated at the scattering locations to obtain the local momentum aperture. Such a file may be obtained from running the **momentum\_aperture** command. The absolute values of the values in the **deltaNegative** column will be used in place of **k\_min**. The **k\_min** values thus obtained are multiplied by **momentum\_aperture\_scale**, so there is some assurance that the minimally-scattered particles will survive. This ensures that the results are valid for computation of loss rates, for example.
- **momentum\_aperture\_periodicity** — If nonzero, the momentum aperture data from **momentum\_aperture** is periodic with the given periodicity.
- **s\_start, s\_end** — Range of  $s$  location for simulated scattering sites.
- **include\_name\_pattern** — Wildcard-containing string to match to element names in selecting scattering sites.
- **include\_type\_pattern** — Wildcard-containing string to match to element types in selecting scattering sites.
- **verbosity** — Higher values may result in more verbose informational output.
- **soft\_failure** — If nonzero, failure to kind a loss does not result in aborting the run.
- **allow\_watch\_file\_output** — If nonzero, **WATCH** elements provide output during tracking.

## insert\_elements

### 7.28 insert\_elements

- type: action command.
- function: Insert elements into a beamline at specified locations. This is a convenient way to add elements to a beamline without modifying the lattice file.
- sequence: must follow `run_setup`.
- notes: The modified beamline can be saved through `save_lattice` command. Be sure to use “output\_seq = 1” option in that command.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&insert_elements
    STRING name = NULL;
    STRING type = NULL;
    STRING exclude = NULL;
    double s_start = -1;
    double s_end = -1;
    long skip = 1;
    long disable = 0;
    long insert_before = 0;
    long add_at_end = 0;
    long add_at_start = 0;
    STRING element_def = NULL;
    long total_occurrences = 0;
    long occurrence[100]={0};
&end
```

- **name** — Possibly wild-card containing string specifying the names of the elements after which the new element is inserted. A list of comma- or space-separated names may be given.
- **type** — Possibly wild-card containing string specifying the type of the elements after which the new element is inserted.
- **exclude** — Possibly wild-card containing string specifying the names of elements to be excluded from the specification.
- **skip** — New elements are inserted at every  $n^{th}$  specified location.
- **s\_start, s\_end** — If positive, these give the starting and ending s locations for insertion of new elements. Note that the s locations are not updated as elements are inserted, but only after completion of all insertions covered by a single command.
- **disable** — If nonzero, the command is ignored.
- **insert\_before** — If nonzero, the insertions are before the selected elements. By default, insertion is after the selected elements.

- `add_at_end` — If nonzero, the element is also inserted to the end of the beamline.
- `add_at_start` — If nonzero, the element is also inserted to the start of the beamline, ahead of all other elements.
- `element_def` — The definition of the new element should be just as it would be entered in the lattice file.
- `total_occurrences`, `occurrence` — These parameters are used to insert the new elements after specified occurrences of the element **name**. `total_occurrences` specifies how many new elements to add, up to a maximum of 100, while the entries in the array `occurrence` specify the occurrences after which to add the new elements. If `total_occurrences` is non-zero, then **skip** must be set to zero and the **name** must be the exact name (no wild-card matching).

## insert\_sceffects

### 7.29 insert\_sceffects

- type: setup command.
- function: set up for transverse space charge calculation.
- sequence: must precede `run_setup`.
- NB: this command is intended only for simulation of space-charge kicks in rings. Please read the manual page for `SCMULT` for details on the algorithm.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&insert_sceffects
    STRING name = NULL;
    STRING type = NULL;
    STRING exclude = NULL;
    long disable = 0;
    long clear = 0;
    STRING element_prefix = "MYSC";
    long skip = 0;
    long vertical = 0;
    long horizontal = 0;
    long nonlinear = 0;
long uniform_distribution = 0;
    long verbosity = 0;
    double averaging_factor = 1;
&end
```

- **name** — Possibly wild-card containing string specifying the name of the elements after which to insert the space charge kick element.
- **type** — Possibly wild-card containing string specifying the type of the elements after which to insert the space charge kick element.
- **exclude** — Possibly wild-card containing string specifying the name of elements to be excluded from the insertion of the space charge kick element.
- **disable** — If nonzero, the command is ignored.
- **clear** — If nonzero, all prior space charge insertions are deleted.
- **element\_prefix** — Name under which the space charge kick will appear in the beamline.
- **skip** — If nonzero, the given number of insertion locations are skipped. If zero, only one space charge kick is inserted at the end of beamline.
- **vertical, horizontal, nonlinear** — If non-zero, then space charge is included in the plane in question.

- **uniform\_distribution** — Used for bi-Gaussian distributed beam (coasting beam), i.e., beam that is uniform in  $z$  but gaussian in  $x$  and  $y$ .
- **verbosity** — Larger non-zero values request greater amounts of detail in printouts.
- **averaging\_factor** — For nonlinear space charge mode only, this parameter allows applying an infinite-impulse-response (IIR) filter to the turn-by-turn beam size data in order to reduce the effects of noise. A value of 1 means that only data from the present turn is used, while values approaching 0 will tend to use the initial beam sizes only. In more detail, the effective rms beam size  $\hat{\sigma}$  used in the calculation of the kicks for the  $i^{th}$  turn is

$$\hat{\sigma}_i = f\sigma_i + (1 - f)\hat{\sigma}_i, \quad (3)$$

where  $\sigma_i$  is the actual rms beam size. N.B.: strictly speaking, simulations performed with  $f \neq 1$  are invalid, as the effect of strong space charge could be understated. However, judicious use of this parameter may allow valid simulations with fewer particles. The user should vary the parameter to ensure that results are insensitive to the value.

#### Important notes:

- By default **skip**=0, which results in only one **SCMULT** element at the end of the beamline, regardless of whether values are given for the **name** or **type** fields.
- This element is not designed for space charge calculations in guns or linacs. It is only intended for simulating space charge in rings.
- This command can not work with concatenation-based matrix tracking.
- Some users use **matched\_to\_cell** in the **bunched\_beam** command. This will erase **SCMULT** assignments along the beamline. In this case, issue another **twiss\_output** command just before tracking.

## ion\_effects

### 7.30 ion\_effects

- type: setup command.
- function: set up for modeling of residual gas ions.
- sequence: must follow `run_setup`.
- Notes:
  1. This feature is considered experimental and should be used with caution. Feedback is welcome. The fitting-based methods, i.e., `bigaussian`, `bilorentzian`, `trigaussian`, and `trilorentzian`, typically show instability when it is not expected and may well have noise challenges that have not been resolved.
  2. One or more `IONEFFECTS` elements must be inserted in the lattice. This can be done manually, or using the `insert_elements` command.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&ion\_effects

```
    STRING pressure_profile = NULL;
double pressure_factor = 1.0;
    STRING ion_properties = NULL;
    STRING beam_output = NULL;
    long beam_output_all_locations = 0;
    STRING ion_density_output = NULL;
    long ion_output_all_locations = 1;
    long ion_species_output = 0;
    STRING field_calculation_method = NULL;
double distribution_fit_target = 0.03;
double distribution_fit_tolerance = 1e-5;
long distribution_fit_evaluations = 300;
long distribution_fit_passes = 3;
long distribution_fit_restarts = 10;
long hybrid_simplex_comparison_interval = -1;
STRING fit_residual_type = NULL;
    long macro_ions = 0;
    long symmetrize = 0;
    long generation_interval = 1;
    long multiple_ionization_interval = 100;
double multiple_ionization_energy_peak = 20;
double multiple_ionization_energy_rms = 10;
    double ion_span[2] = {0, 0};
double ion_bin_divisor[2] = {10.0, 10.0};
double ion_range_multiplier[2] = {2.0, 2.0};
double ion_sigma_limit_multiplier[2] = {0, 0};
long ion_histogram_max_bins = 1000;
long ion_histogram_min_per_bin = 5;
```



```

STRING ion_histogram_output = NULL;
double ion_histogram_output_s_start = -1;
double ion_histogram_output_s_end = -1;
long ion_histogram_output_interval = 1000;
long ion_histogram_min_output_bins = 200;
long disable_until_pass = 0;
long freeze_ions_until_pass = 0;
long freeze_electrons_until_pass = 0;
    long verbosity = 0;
&end

```

- **pressure\_profile** — Name of an SDDS file giving the s-dependent gas pressure for various gas species. Column names will be matched to the entries in the **SourceName** column of the **ion\_properties** file.
- **pressure\_factor** — Factor by which to multiply the pressures given in the **pressure\_profile**.
- **ion\_properties** — Name of an SDDS file giving properties of ions. Column names are
  - **IonName** — String column giving the name of the ion.
  - **Mass** — Floating-point column giving the ion mass, in AMU.
  - **ChargeState** — Integer column giving the ion charge state (a positive integer).
  - **SourceName** — String column giving the name of the source gas for this ion. Alternately, for a multiply ionized molecule (e.g. CO++) one can give a source ion (e.g. CO+). The source ion must also be defined in the **ion\_properties** file.
  - **CrossSection** — Floating-point column giving the cross section for producing the ion from the source, in *Mb*.
- **beam\_output** — Possibly incomplete name of an SDDS file to which beam data will be written. Asking for this output can significantly reduce performance, so it should generally be used for testing only.
- **beam\_output\_all\_locations** — If nonzero, **beam\_output** includes data at the location of all IONEFFECTS elements. By default, only the first element is included.
- **ion\_density\_output** — Possibly incomplete name of an SDDS file to which ion density data will be written.
- **ion\_output\_all\_locations** — If nonzero, **ion\_density\_output** includes data at the location of all IONEFFECTS elements. By default, only the first element is included.
- **ion\_species\_output** — If nonzero, **ion\_density\_output** includes data for each ion species.
- **field\_calculation\_method** — By default, the fields are computed on the assumption that the beam and ion distributions are gaussian. This is a good assumption for the beam, but not highly accurate for the ions. More accurate, but slower, methods is sums of two or three gaussians, or sums of two or three lorentzians, which can be invoked by setting **field\_calculation\_method** to "bigaussian", "trigaussian", "bilorentzian", or "trilorentzian";

these are collectively referred to as “histogram fitting methods” below. In the bigaussian case, the charge distribution is of the form

$$\rho(x, y) = (G(x, h_{x,1}, \sigma_{x,1}, c_{x,1}) + G(x, h_{x,2}, \sigma_{x,2}, c_{x,2})) * (G(y, h_{y,1}, \sigma_{y,1}, c_{y,1}) + G(y, h_{y,2}, \sigma_{y,2}, c_{y,2})), \quad (4)$$

where  $G(q, h, \sigma, c) = h \exp -(q - c)^2 / (2\sigma^2)$ . The charge distribution for the bilorentzian is

$$\rho(x, y) = (L(x, h_{x,1}, a_{x,1}, c_{x,1}) + L(x, h_{x,2}, a_{x,2}, c_{x,2})) * (L(y, h_{y,1}, a_{y,1}, c_{y,1}) + L(y, h_{y,2}, a_{y,2}, c_{y,2})), \quad (5)$$

where  $L(q, h, a, c) = h / (1 + (q - c)^2 / a^2)$ .

- **distribution\_fit\_target** — If the distribution field calculation method is selected, gives the target for the fractional deviation of the fit. Smaller numbers will result in long run times.
- **distribution\_fit\_tolerance** — If the distribution field calculation method is selected, gives the tolerance for the fractional deviation of the fit. Smaller numbers will result in long run times but higher likelihood of reaching the target.
- **distribution\_fit\_evaluations, distribution\_fit\_passes, distribution\_fit\_restarts** — Parameters for the simplex optimizer that performs the distribution fit. Note that in **Pelegant**, a hybrid simplex method is used, which appears to converge quickly if the default parameters are used.
- **fit\_residual\_type** — Residual type for distribution fitting. The default is **max-ad-plus-ad-charge**, which indicates using the sum of the maximum absolute deviation and the normalized absolute deviation of the total charge, where the latter is computed from difference of the actual total ion charge and the analytical integral of the charge in the summed distributions; this tends to ensure that there are no hidden spikes in the distribution due to overfitting. Other options are **sum-ad** (sum of normalized absolute deviation), **rms-dev** (sum of normalized rms deviation), **max-ad** (maximum normalized absolute deviation), **max-ad-plus-rms-dev** (sum of maximum normalized absolute deviation and normalized rms deviation), **sum-ad-plus-rms-dev**, **rms-dev-plus-ad-sum**, **sum-ad-plus-ad-sum**, **rms-dev-plus-centroid**, and **rms-dev-plus-ad-charge**.
- **macro\_ions** — The number of macro ions to generate per bunch on each turn for which generation is done. The macro ion charge is adjusted according to the cross section and bunch charge. May be overridden by the **MACRO\_IONS** parameter on individual **IONEFFECTS** elements. If this value is too small, the ion distribution will be noisy, which may result in unreliable results. When using the parallel version, setting **macro\_ions** to 1,000 or higher is not unreasonable.
- **symmetrize** — If nonzero, ions are emitted in symmetric pairs to ensure that the centroids don’t deviate from the electron beam centroids because of noise. Doubles the number of macro ions that are emitted. Intended primarily for testing purposes.
- **generation\_interval** — The number of bunches between generation of ions. The macro ion charge is adjusted to account for this, so the effective ion charge after many turns is the same. May be overridden with the **GENERATION\_INTERVAL** parameter on individual **IONEFFECTS** elements. The actual condition for generation of ions is such that the generating bunches vary on each turn. This can be used to effectively reduce **macro\_ions** below 1, to prevent generation of too many macro ions. This will result in noisy histograms and should be used with caution.

- `multiple_ionization_interval` — The number of bunches between multiple ionization calculations. The macro ion charge is adjusted to account for this, so the effective ion charge after many turns is the same.
- `multiple_ionization_energy_peak`, `multiple_ionization_energy_rms` — Specifies the distribution of the energy of multiply-ionized ions in terms of the peak (or centroid) of the distribution and its rms width, in eV.
- `ion_span` — The transverse half-extent, in meters, of the region within which ions are modeled. Ions moving outside this region are considered lost. May be overridden by the `X_SPAN` and `Y_SPAN` parameters on individual `IONEFFECTS` elements.
- `ion_bin_divisor` — For histogram fitting methods, the number of ion bins per rms parameter of the electron beam.
- `ion_range_multiplier` — For histogram fitting methods, used to determine the full span of the ion binning region bins in units of the rms parameter of the ion distribution. The sign of the value determines which algorithm is used. For  $m < 0$ , the binning range is  $|m|\sigma_{ion}$ . For  $m = 0$ , the full span of the ion distribution is included; this may result in a very large number of bins being used to cover a few outlying ions, and is not recommended. For  $m > 0$ , the code first finds the approximate range containing the central 80% of the ions, then multiplies by  $m$  to get the range used.
- `ion_sigma_limit_multiplier` — For histogram fitting methods, the minimum value for either of the ion sigmas (for bigaussian) or size parameters (for bilorentizan) in units of the bin size. Use to prevent one of the gaussians or lorentzians from being too delta-function-like.
- `ion_histogram_max_bins` — Maximum number of ion bins for fitting methods. If this limit is reached, the *span* of the histograms will be reduced to ensure that the central portion is resolved. If the value is too large, the histograms may be noisy, which will make the fits unreliable. Also, a large value will result in reduced parallel efficiency, as processors must pass around more data.
- `ion_histogram_min_per_bin` — Minimum number of ions per bin (on average).
- `ion_histogram_output`, `ion_histogram_output_s_start`, `ion_histogram_output_s_end`, `ion_histogram_output_interval`, `ion_histogram_max_bins` — Controls for the output of ion histograms when using histogram fitting methods. `ion_histogram_output` gives the (incomplete) filename. `ion_histogram_output_s_start` and `ion_histogram_output_s_end` give limits on the *s* coordinate of the `IONEFFECTS` element. `ion_histogram_output_interval` gives the interval in passes between output.
- `verbosity` — Larger values result in more output during running. Used for debugging only.

The user is strongly advised to study the ion histograms by using the `ion_histogram_output` parameter to request this data. The histograms should not be excessively noisy. The data also includes the fits, which should be close to the data. (For “gaussian” mode, this is generally not possible.) A sample command to examine the histograms and fits for the y plane (generally the most difficult) is

```
sddsplot -column=Position,Charge* run.ionHist -split=page -groupby=page -separate=page -graph=
```

## linear\_chromatic\_tracking\_setup

### 7.31 linear\_chromatic\_tracking\_setup

- type: setup command.
- function: define chromatic variation of beta functions, tunes, etc. for using in fast linear-chromatic tracking
- sequence: must follow `run_setup`.
- N.B.: This command is deprecated and no longer maintained. Use a beamline containing one or more `ILMATRIX` elements instead. This provides much more functionality.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&linear_chromatic_tracking_setup
  double nux[4] = {-1, 0, 0, 0};
  double betax[2] = {1.0, 0.0};
  double alphax[2] = {0.0, 0.0};
  double etax[2] = {0.0, 0.0};
  double etapx[2] = {0.0, 0.0};
  double nuy[4] = {-1, 0, 0, 0};
  double betay[2] = {1.0, 0.0};
  double alphay[2] = {0.0, 0.0};
  double etay[2] = {0.0, 0.0};
  double etapx[2] = {0.0, 0.0};
  double alphac[2] = {0.0, 0.0};
&end
```

- **nux** — Provide the horizontal tune plus its first three chromatic derivatives, i.e.,  $\partial\nu_x/\partial\delta$ ,  $\partial^2\nu_x/\partial\delta^2$ , and  $\partial^3\nu_x/\partial\delta^3$ .
- **betax** — Provide the horizontal beta function plus its chromatic derivative.
- **alphax** — Provide the horizontal alpha function plus its chromatic derivative.
- **etax** — Provide the first- and second-order horizontal dispersion:  $\eta_x = \eta_x[0] + \eta_x[1]\delta$ .
- **etapx** — Provide the first- and second-order horizontal dispersion slope.
- **alphac** — Provide the first and second-order momentum compaction. N.B: if you are tracking with an rf cavity, be sure that your lattice length equal to the actual circumference. See the example below.

## link\_control

### 7.32 link\_control

- type: setup command.
- function: overall control of element parameter links.
- sequence: must follow `run_control`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&link_control
  long clear_links = 1;
  long summarize_links = 0;
  long verbosity = 0;
&end
```

- `clear_links` — Clear all previously set links.
- `summarize_links` — Summarize all current set links.
- `verbosity` — A larger value results in more output during computations.

## link\_elements

### 7.33 link\_elements

- type: setup command.
- function: assert a link between parameters of accelerator elements.
- sequence: must follow `run_control` and `link_control`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&link_elements
  STRING target = NULL;
  STRING exclude = NULL;
  STRING item = NULL;
  STRING source = NULL;
  STRING source_from_target_edit = NULL;
  STRING source_position = "before";
  STRING mode = "dynamic";
  STRING equation = NULL;
  double minimum = -DBL_MAX;
  double maximum = DBL_MAX;
  long exclude_self = 1;
&end
```

- **target** — The name of the elements to be modified by the link. May contain wild-cards.
- **exclude** — Wildcard sequence to match to element names. If a match is found, the element is excluded from the link.
- **item** — The parameter that will be modified.
- **source** — The name of the elements to be linked to.
- **source\_from\_target\_edit** — If given and if **source** is not given, an editing command to create the name of the elements to be linked to from the name of the target. Uses the syntax of the `editstring` program.
- **source\_position** — May be one of “first”, “before”, “after”, “adjacent”, “nearest”, or “same-occurrence”.
- **mode** — May be either “dynamic” or “static”. A dynamic link is asserted whenever the source is changed (during correction, for example). A static link is asserted only when an error or variation is imparted to the source, and at the end of correction.
- **equation** — An `rpn` equation for the new item value in terms of the item values for the source. The prior value of the item is on the top of the stack. To refer to the source parameter values, use the name of the parameters. To refer to the initial source parameter values, append “0” to the parameter name. These names must appear in capital letters.
- **minimum, maximum** — Minimum and maximum values that will be assigned to the target parameter.

- `exclude_self` — If nonzero, self-links are blocked. It is not recommended to change this.

## load\_parameters

### 7.34 load\_parameters

- type: setup command.
- function: load parameters for elements from an SDDS file.
- sequence: must follow `run_setup` and precede `run_control` and `error_control` (if present).
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&load_parameters
    STRING filename = NULL;
    STRING filename_list = NULL;
    STRING include_name_pattern = NULL;
    STRING exclude_name_pattern = NULL;
    STRING include_item_pattern = NULL;
    STRING exclude_item_pattern = NULL;
    STRING include_type_pattern = NULL;
    STRING exclude_type_pattern = NULL;
    STRING edit_name_command = NULL;
    long change_defined_values = 0;
    long clear_settings = 0;
    long allow_missing_elements = 0;
    long allow_missing_parameters = 0;
    long allow_missing_files = 0;
    long force_occurrence_data = 0;
    long verbose = 0;
    long skip_pages = 0;
    long use_first = 0;
&end
```

- **filename** — Name (possibly containing the “%s” field) of SDDS file from which to take data. The file must contain some of the following columns:
  - **ElementName** — Required string column. The name of the element to change.
  - **ElementParameter** — Required string column. The name of the parameter of the element to change.
  - **ParameterValue** — Optional double column. If given, gives value of the parameter named in **ElementParameter** for element named in **ElementName**.
  - **ParameterValueString** — Optional string column. If **ParameterValue** is not present, then this column must be present. The string data will be scanned, if necessary, to obtain a value for the parameter.
  - **ParameterMode** — Optional string column. If given, for each row the value must be one of “absolute”, “differential”, “ignore”, or “fractional”. The meaning of these modes is as follows: absolute mode means the given value is used as the new value for the parameter; differential mode means the given value is added to the existing value for the parameter; ignore mode means the value is ignored; fractional mode means the existing



value is increased by the product of the given value and the existing value (i.e., the given value is a fractional change).

Unless `change_defined_values` is set, successive pages of the file are used for successive steps of the simulation. Several `elegant` commands generate output that may be used (on a subsequent run) with `load_parameters`; among these are the tune and chromaticity correction commands and the `run_setup` command (parameters output).

- `filename_list` — A list of filenames, which may be given in place of `filename`. If used, each file in the list is treated as if it was separately supplied with an individual `load_parameters` command.
- `include_name_pattern`, `exclude_name_pattern` — A comma- or space-separated list of wildcard patterns to be used in selecting, respectively, which elements to include and which to exclude from loading. To be used, data must match at least one inclusion pattern and no exclusion patterns.
- `include_item_pattern`, `exclude_item_pattern` — A comma- or space-separated list of wildcard patterns to be used in selecting, respectively, which items (i.e., which element parameters) to include and which to exclude from loading. To be used, data must match at least one inclusion pattern and no exclusion patterns.
- `include_type_pattern`, `exclude_type_pattern` — Wildcard patterns to be used in selecting, respectively, which element types (e.g., QUAD, DRIFT) to include and which to exclude from loading. To be used, data must match at least one inclusion pattern and no exclusion patterns.
- `edit_name_command` — A command using the syntax of the `editstring` program, allowing the strings in the `ElementName` column to be modified before values are assigned.
- `change_defined_values` — Changes the defined values of the parameters. This means that when the lattice is saved (using `save_lattice`), the parameters will have the altered values. Also, if one wants to alter the values for all steps of the simulation, one must set this flag.

Note that the `ElementOccurrence` data is normally ignored if `change_defined_values` is nonzero. This is because there is only one definition of each element, even if it is used multiple times. This behavior can be altered with the next control.

- `force_occurrence_data` — If set, then occurrence data is used even in `change_defined_values` mode. When loading data for a highly repetitive system, where many elements have identical names, this can greatly speed completion of the operation.
- `use_first` — It is possible that the input file will contain multiple lines for any given parameter. In this case, `elegant` will by default process all lines. For example, if the lines give differential values, then all would be included. However, if the lines give absolute values, then the last one will overwrite the previous values; this flag allows overriding the behavior in this case to force `elegant` to use the first value. This can have speed advantages for cases where there are many identical occurrences of the same element with identical values for the parameters.
- `clear_settings` — If set, clear all settings and files being used for loading parameters.

- `allow_missing_elements` — If set, allow elements in the file that are not in the lattice. In this case, the nonapplicable data is simply ignored.
- `allow_missing_parameters` — If set, it is not an error if any element in the lattice lacks a parameter that exists in the file.
- `allow_missing_files` — If set, it is not an error if any listed file is missing.
- `verbose` — If set, provide informational printouts about changes to parameters.
- `skip_pages` — Specify the number of pages of input to skip.

## matrix\_output

### 7.35 matrix\_output

- type: setup/action command.
- function: generate matrix output, or set up to do so later.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&matrix_output
  STRING printout = NULL;
  long printout_order = 1;
  STRING printout_format = "%22.15e ";
  long full_matrix_only = 0;
  long mathematica_full_matrix = 0;
  long print_element_data = 1;
  STRING SDDS_output = NULL;
  long SDDS_output_order = 1;
  long individual_matrices = 0;
  STRING SDDS_output_match = NULL;
  long output_at_each_step = 0;
  STRING start_from = NULL;
  long start_from_occurence = 1;
&end
```

- **printout** — The (incomplete) name of a file to which the matrix output will be printed (as text). Recommended value: “%s.mpr”.
- **printout\_order** — The order to which the matrix is printed.
- **printout\_format** — The C-style formatting statement for the matrix elements. A space, comma, or other separator should appear at the end of the string.
- **full\_matrix\_only** — A flag indicating that only the matrix of the entire accelerator is to be output.
- **print\_element\_data** — A flag indicating whether the element data should be printed out.
- **SDDS\_output** — The (incomplete) name of an SDDS file to which the matrix will be written. Recommended value: “%s.mat”.
- **SDDS\_output\_order** — The order to which the matrix is output in SDDS format.
- **individual\_matrices** — If non-zero, the matrices in the SDDS file are the individual *on-trajectory* matrices of the elements, rather than the concatenated matrix of the beamline.
- **SDDS\_output\_match** — A wildcard string which element names must match in order for data to appear in the SDDS output file.
- **output\_at\_each\_step** — A flag indicating whether matrix output is desired at every simulation step.

- **start\_from** — The optional name of the accelerator element from which to begin concatenation and output.
- **start\_from\_occurence** — If **start\_from** is not NULL, the number of the occurrence of the named element from which to start.

## modulate\_elements

### 7.36 modulate\_elements

- type: setup command.
- function: define parameters for time-dependent modulation of elements
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&modulate_elements
  STRING name = NULL;
  STRING item = NULL;
  STRING type = NULL;
  STRING expression = NULL;
  STRING filename = NULL;
  STRING time_column = NULL;
  STRING amplitude_column = NULL;
  long refresh_matrix = 0;
  long differential = 1;
  long multiplicative = 0;
  long start_occurrence = 0;
  long end_occurrence = 0;
  double s_start = -1;
  double s_end = -1;
  STRING before = NULL;
  STRING after = NULL;
  long verbose = 0;
  double verbose_threshold = 0;
  STRING record = NULL;
  long flush_record = 1;
&end
```

N.B.: This command will produce unpredictable results when used with `error_element`, `alter_elements`, and `load_parameters` (except when `change_defined_values=1`). It should work properly with `link_elements` in turn-by-turn mode when the source element is modulated, but not when the target element is modulated.

- **name** — A possibly-wildcard-containing string giving the names of the elements to modulate. If not specified, then one must specify **type**.
- **item** — The name of the parameter to modulate.
- **type** — A possibly-wildcard-containing string giving the names of element *types* to modulate. May be specified with **name** or by itself.
- **expression** — RPN expression for the modulation amplitude *A*. The value of the time is on top of the stack.

- **filename** — Name of SDDS file from which to read modulation data, if **expression** is not used.
- **time\_column** — Name of column in **filename** giving time data for the modulation table.
- **amplitude\_column** — Name of column in **filename** giving amplitude data for the modulation. Together, **time\_column** and **amplitude\_column** define a function  $A(t)$ .
- **refresh\_matrix** — Frequently there is a matrix associated with an element even if tracking through the element does not use the matrix. In this case, **elegant** doesn't normally update the matrix for the element as it modulates the element, since that may involve a significant time penalty. If this parameter is set to a non-zero value, the matrix will be updated. For elements that use a matrix for tracking, the matrix is always updated.
- **differential, multiplicative** — Determine how the amplitude function  $A(t)$  is used to obtain the new value of the parameter. There are four cases
  - **differential=1, multiplicative=0**:  $v(t) = v_0 + A(t)$  (default).
  - **differential=0, multiplicative=0**:  $v(t) = A(t)$ .
  - **differential=1, multiplicative=1**:  $v(t) = v_0 + v_0 A(t)$ .
  - **differential=0, multiplicative=1**:  $v(t) = v_0 A(t)$ .
- **start\_occurrence, end\_occurrence** — If nonzero, these give the starting and ending occurrence numbers of elements that will be modulated. N.B.: if wildcards are used, occurrence number counting is for each set of identically-named elements separately, rather than for the sequence of matched elements.
- **s\_start, s\_end** — If non-negative, these give the starting and ending position limits for the end-of-element locations of elements to be modulated.
- **after** — The name of an element. If given, the modulation is applied only to elements that follow the named element in the beamline.
- **before** — The name of an element. If given, the modulation is applied only to elements that precede the named element in the beamline.
- **verbose** — If nonzero, information is printed to the standard output as changes are made. Use for debugging only, since otherwise it may slow the simulation.
- **verbose\_threshold** — If nonzero, verbose information is printed only when the fractional change exceeds the given value.
- **record** — Gives a possibly incomplete filename to which will be written a record of the values of the modulation.
- **flush\_record** — Gives the interval in steps at which to flush the record file. Higher values result in less frequent updates to the record, but may improve performance.

## moments\_output

### 7.37 moments\_output

- type: action/setup command.
- function: compute periodic or propagate non-periodic beam moments without tracking, optionally including radiation.
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&moments_output
  STRING filename = NULL;
  long output_at_each_step = 0;
  long output_before_tune_correction = 0;
  long final_values_only = 0;
  long verbosity = 0;
  long matched = 1;
  long equilibrium = 1;
  long radiation = 1;
  long n_slices = 10;
  long slice_etilted = 1;
  double emit_x = 0;
  double beta_x = 0;
  double alpha_x = 0;
  double eta_x = 0;
  double etap_x = 0;
  double emit_y = 0;
  double beta_y = 0;
  double alpha_y = 0;
  double eta_y = 0;
  double etap_y = 0;
  double emit_z = 0;
  double beta_z = 0;
  double alpha_z = 0;
&end
```

- `filename` — The (incomplete) name of a file to which the moments results will be written. Recommended value: “%s.mom”.
- `output_at_each_step` — A flag indicating, if set, that computations and/or output is desired at each step of the simulation. If you wish to compute Twiss parameters on a closed orbit or after other calculations, be sure to set this control to a nonzero value.
- `output_before_tune_correction` — A flag indicating, if set, that output is desired both before and after tune correction.
- `final_values_only` — A flag indicating, if set, that only the final values of the Twiss parameters should be output, and not the parameters as a function of `s`.

- **verbosity** — Larger numbers result in an increasing amount of informational output to the standard output stream.
- **matched** — A flag indicating, if set, that the periodic or matched moments should be found.
- **equilibrium** — A flag indicating, if set, that the equilibrium moments should be found. If **matched=1** and **equilibrium=0**, then the initial twiss parameters are computed from the periodic solution for the beamline.
- **radiation** — A flag indicating, if set, that synchrotron radiation effects should be included. N.B.: this flag is all that needs to be set if the lattice contains no kick elements. However, if the lattice contains **CSBEND**, **CSRCSBEND**, **KQUAD**, or **KQUAD** elements (or other elements with **SYNCH\_RAD** and **ISR** parameters), then the **SYNCH\_RAD** and **ISR** must be set to 1 as well.
- **n\_slices** — The number of slices into which to cut individual dipoles, quadrupoles, and sextupoles for computations. 10 has been found to work for all rings tested, but users are advised to ensure it is sufficient for their cases.
- **emit\_x**, **beta\_x**, **alpha\_x**, **eta\_x**, **etap\_x**, and related quantities for **y** and **z** — If **matched=0**, then these specify the starting beam ellipses in all three planes.

This command performs several functions. In the most basic form, it propagates beam moments, i.e., the 6x6 sigma matrix, from the beginning to the end of a transport line, including coupling from rotated elements or offset sextupoles. This can be performed with or without synchrotron radiation effects in dipoles, quadrupoles, and sextupoles. These computations include the evolution of the trajectory due to errors and (if included) synchrotron radiation.

If desired, the command will instead compute the periodic beam moments. In this case, the user must include an appropriate rf cavity in the lattice in order to get valid results. (By “appropriate rf cavity” we mean that it must have the right voltage, frequency, and phase to support stored beam.) It is also suggested that the user compute the closed orbit using **closed\_orbit** so that the computations are performed on the closed orbit.

The results of moments computation may be subjected to optimization using values at marker elements. See the documentation for **MARK** for more details.

#### Notes:

- When using **CSBEND**, **KQUAD**, and **KSEXT** elements, one may find that the calculations of **moments\_output** do not make sense. This is because, by default, synchrotron radiation is disabled on these elements. To resolve the issue, set **ISR=1** and **SYNCH\_RAD=1** on **CSBEND** at a minimum. If a closed orbit is present, making the same setting on the **KQUAD** and **KSEXT** is also suggested. It is essential to do this if there is an rf frequency offset.
- When bending magnets are tilted, **elegant** has problems computing the moments and closed orbit self-consistently when the bending radius is small. To address this, the **n\_slices** parameter is set to 1 for tilted bending magnets when **slice\_etilted=0**. This reduces the accuracy of the calculations. **Users are strongly advised to check that this is acceptable.**
- The program **sddsmatchmoments** is available to transform a particle distribution so that its 6x6 beam moments match those given in a **moments\_output** output filename. In addition, the **bunched\_beam** command provides a similar capability for generating a distribution from computed moments.



## momentum\_aperture

### 7.38 momentum\_aperture

- type: major action command.
- function: determine momentum aperture as a function of position in the lattice by tracking
- can use parallel resources (Pelegant)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&momentum_aperture
  STRING output = NULL;
  double x_initial = 0;
  double y_initial = 0;
  double delta_negative_start = 0.0;
  double delta_positive_start = 0.0;
  double delta_negative_limit = -0.10;
  double delta_positive_limit = 0.10;
  double delta_step_size = 0.01;
  long steps_back = 1;
  long splits = 2;
  long split_step_divisor = 10;
  long skip_elements = 0;
  long process_elements = 2147483647;
  double s_start = 0;
  double s_end = DBL_MAX;
  STRING include_name_pattern = NULL;
  STRING include_type_pattern = NULL;
  long fiducialize = 0;
  long verbosity = 1;
  long soft_failure = 0;
  long output_mode = 0;
  long forbid_resonance_crossing = 0;
&end
```

- **output** — The (incomplete) name of a file to which the momentum aperture results will be written. Recommended value: “%s.mmap”. The data are related to the momentum aperture at the exit of the named elements.
- **x\_initial, y\_initial** — The initial x and y coordinate values for tracking. It is essential that **y\_initial** be nonzero if one wants to see losses due to vertical resonances.
- **delta\_negative\_start, delta\_positive\_start** — Starting values of scans in the negative and positive directions.
- **delta\_negative\_limit, delta\_positive\_limit** — Limiting values of scans in the negative and positive directions.
- **delta\_step\_size** — Initial size of steps in  $\delta$ . This should be fairly large in order to save time.

- **steps\_back** — Number of steps to back up after a particle is lost, relative to the last surviving  $\delta$ , before continuing with a smaller step size. If this is set to zero, there is a risk of finding a too-large momentum aperture (a stable island).
- **splits** — Number of times to split the step size in order to refine the location of the maximum surviving momentum offsets. When a particle is lost, the algorithm steps back to a momentum offset where a particle survived, subdivides the step size, and continues searching.
- **split\_step\_divisor** — Factor by which to subdivide the step size for each split.
- **skip\_elements** — Number of elements to skip before starting to compute momentum apertures.
- **process\_elements** — Number of elements for which to compute momentum aperture.
- **s\_start, s\_end** — Limiting  $s$  coordinates of the elements from which tracking will start. The default values will exclude no elements.
- **include\_name\_pattern** — If given, tracking will start only at the entrance to elements that match the given wildcard pattern.
- **include\_type\_pattern** — If given, tracking will start only at the entrance to elements whose type matches the given wildcard pattern.
- **fiducialize** — If given, an initially on-energy particle is tracked before the momentum aperture search begins, in order to fiducialize the reference momentum. This is useful if there are synchrotron radiation losses or energy gain due to cavities in the system.
- **verbosity** — Larger values result in more detailed printouts as calculations proceed. Mostly for debugging.
- **soft\_failure** — Normally, if **elegant** fails to find the momentum aperture, it aborts. If **soft\_failure** is non-zero, it instead assigns a momentum aperture equal to the search limit.
- **output\_mode** — Normally, **elegant** puts the values for positive and negative momentum aperture in different columns. Each element thus has a single row of data in the output file. If **output\_mode=1**, **elegant** instead puts the values for positive and negative apertures in successive rows, with a reduced number of columns. This is mostly advantageous for the parallel version, since it allows using twice as many simultaneous processors. If **output\_mode=2**, **elegant** tracks many more probe particles simultaneously, which is better for massively parallel systems. The number of particles tracked is the number of elements selected times the number of probe points between **delta\_negative\_limit** and **delta\_positive\_limit**.
- **forbid\_resonance\_crossing** — Normally, **elegant** allows the momentum aperture search to cross integer and half-integer resonances if no unstable particles are found. If this is undesirable, this flag can be set to 1.

The idea for this command is from M. Belgroune *et al.*, “Refined Tracking Procedure for the SOLEIL Energy Acceptance Calculation,” Proceedings of PAC 2003, p 896, as implemented for TRACYII. In particular, the energy aperture as a function of position around the ring is determined by tracking. Starting at the beginning of the lattice and working downstream, particles are tracked starting from the exit of each selected element. The betatron coordinates are initially zero (or very

small), while the momentum deviation is gradually increased until loss of the particle is observed. This defines the momentum aperture at that location.

In **elegant** version 19.0 and later, the algorithm is as follows. For simplicity in wording, we'll assume the momentum deviations are positive values, although the method is applied separately for negative values as well:

1. Start with  $\delta = 0$ , i.e., zero momentum offset.
2. Track a particle to see if it gets lost. If so, proceed to step 4.
3. Increase  $\delta$  by step size  $\Delta\delta$  and return to step 2.
4. If no splitting steps remain, proceed to the next step. Otherwise:
  - (a) Change  $\delta$  to  $\delta_s - s_b\Delta\delta$ , where  $\delta_s$  is the largest  $\delta$  for which the particle survived, and  $s_b$  is the **steps\_back** parameter.
  - (b) Divide the step size by **split\_step\_divisor** to get a new step size  $\Delta\delta$ .
  - (c) Set  $\delta = \delta + \Delta\delta$ .
  - (d) Decrement the “splits remaining” counter by 1.
  - (e) Continue from step 2.
5. Stop. The momentum aperture is  $\delta_s$ .

This command can be used for both rings and transport lines. For rings it is most appropriate to have an rf cavity (i.e., an **RFCA** element) in the lattice. One should also include radiation loss using either of two methods:

1. **SREFFECTS** element, with **QEXCITATION=0**. To set up this element more easily, one can include a **twiss\_output** command with **radiation\_integrals=1**.
2. Use **CSBEND** and **KQUAD** elements with **SYNCH\_RAD=1** and **ISR=0**.

When including radiation loss, one must be certain to set the frequency and phase of the rf cavity correctly. The **rf\_setup** command can be used for this purpose. It is also a good idea to track for several synchrotron oscillation periods.

**Note for Pelegant:** Unlike for **elegant**, the data in the output file will not be sorted by **s**. To sort the data, simply use **sddssort** from the commandline, e.g.,

```
sddssort -column=s output.mmap
```

Also, if it is desirable for the output from **Pelegant** to have exactly the same form as that from **elegant**, then the script **reorganizeMmap** should be used. This script is provided with **elegant** and **Pelegant** distributions.

## optimize

### 7.39 optimize

- type: major action command.
- function: perform optimization.
- sequence: must follow **optimization\_setup** and beam definition (**bunched\_beam** or **sdds\_beam**).
- can use parallel resources (**Pelegant**) for tracking-based optimization.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- note: on UNIX systems, the user may press Control-C to force **elegant** to terminate optimization and proceed as if optimization had converged. (To genuinely terminate the run during optimization press Control-C twice.) This is very useful if one wants to get a look at the partially optimized result. If one uses parameter saving (**run\_setup**) or **save\_lattice** one can make a new run that starts from the optimized result.

```
&optimize
    long summarize_setup = 0;
&end
```

- **summarize\_setup** — A flag indicating, if set, that a summary of the optimization parameters should be printed.

## optimization\_constraint

### 7.40 optimization\_constraint

- type: setup command.
- function: define a constraint for optimization.
- sequence: must follow `optimization_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- N.B.: This command is *disparaged*. It is *far* better to put constraints into the optimization equation (via the `equation` parameter of `optimization_setup` or via `optimization_term`). The reason is that the hard constraints imposed by `optimization_constraint` may make it more difficult for the optimizer to converge. See the discussion of the `selt` and `segt` macros in the manual entry to `optimization_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&optimization_constraint
  STRING quantity = NULL;
  double lower = 0;
  double upper = 0;
&end
```

- `quantity` — The quantity to be constrained, given as the name of a quantity from among the optimization variables, optimization covariables, and the “final” parameters (see the entry for `run_setup` for the last of these). The optimization (co)variables are referred to as `<element-name>.<parameter-name>`, in all capital letters. Other quantities, such as Twiss parameters or anything else but what is listed just above, are not recognized. Expressions involving multiple quantities are not supported.
- `lower`, `upper` — The lower and upper limits allowed for the expression.

## optimization\_covariable

### 7.41 optimization\_covariable

- type: setup command.
- function: define an element parameter to be varied as a function of optimization parameters.
- sequence: must follow `optimization_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- N.B.: It is not possible to optimize an element if the element name starts with one of the following characters: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ., +, or -. The reason is that `elegant` will attempt to make an SDDS parameter name containing the element name, and these characters are disallowed at the beginning of such a name.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&optimization_covariable
  STRING name = NULL;
  STRING item = NULL;
  STRING equation = NULL;
  long disable = 0;
&end
```

- `name` — The name of the element.
- `item` — The parameter of the element to be changed.
- `equation` — An `rpn` equation for the value of the parameter in terms of the values of any parameters of any optimization variable. These latter appear in the equation in the form `<element-name>.<parameter-name>`, in all capital letters. The original values of all variables and covariable may be accessed via names like `<element-name>.<parameter-name>0`.
- `disable` — If nonzero, the covariable is ignored.

## optimization\_setup

### 7.42 optimization\_setup

- type: setup command.
- function: define overall optimization parameters and methods.
- sequence: must precede beam definition (`bunched_beam` or `sdds_beam`)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&optimization_setup
  STRING equation = NULL;
  STRING mode = "minimize";
  STRING method = "simplex";
  double tolerance = -0.01;
  double target = 0;
  long center_on_orbit = 0;
  long center_momentum_also = 1;
  long soft_failure = 1;
  long n_passes = 2;
  long n_evaluations = 500;
  long n_restarts = 0;
  long matrix_order = 1;
  STRING log_file = NULL;
  STRING term_log_file = NULL;
  long output_sparsing_factor = 0;
  long balance_terms = 0;
  double restart_worst_term_factor = 1;
  long restart_worst_terms = 1;
  long verbose = 1;
  long balance_terms = 0;
  double simplex_divisor = 3;
  double simplex_pass_range_factor = 1;
  long include_simplex_1d_scans = 1;
  long start_from_simplex_vertex1 = 0;
  long restart_random_numbers = 0;
  STRING interrupt_file = "%s.interrupt";
  long interrupt_file_check_interval = 0;
&end
```

- **equation** — An `rpn` equation for the optimization function, expressed in terms of any parameters of any optimization variables, the “final” parameters of the beam (as recorded in the final output file available in the `run_setup` namelist), and selected quantities from Twiss parameter, tune shift with amplitude, closed orbit, beam moments, driving terms, and other computations. The optimization variables or covariables may appear in the equation in the form `<element-name>.<parameter-name>`, all in capital letters. In addition, initial values of variables and covariables are available in the form `<element-name>.<parameter-name>0`.

Data from MARK elements with FITPOINT=1 and from beam position monitors with CO\_FITPOINT=1 may be used via symbols of the form *elementName#occurrenceNum.parameterName*. See the documentation for the MARK, MONI, HMON, and VMON elements for detailed discussion and listing.

If response matrix calculation is requested, response matrix values are available in variables with names *PlaneR\_bpmName#occurrence\_corrName#occurrence\_corrParam*, where *Plane* is H (horizontal) or V (vertical) and *corrParam* is the parameter of the corrector used for changing the orbit (e.g., HKICK or VKICK for a KICKER element).

If cross-plane response matrix calculation is requested, response matrix values are available in variables with names *BpmPlaneCorrPlaneR\_bpmName#occurrence\_corrName#occurrence\_corrParam*, where *BpmPlane* and *CorrPlane* are H (horizontal) or V (vertical) and *corrParam* is the parameter of the corrector used for changing the orbit (e.g., HKICK or VKICK for a KICKER element).

Many quantities are made available for optimization if `twiss_output` command is given with `output_at_each_step=1`:

- Final Twiss parameters, e.g., `betax`, `alphax`, `etax`. The names are the same as the column names in the twiss output file.
- Linear acceptances `Ax` and `Ay` for the horizontal and vertical planes, respectively.
- Statistics of Twiss parameters in the form `<statistic>.<parameter-name>`, where `<statistic>` is `min`, `max`, `ave`, `p99`, `p98`, or `p96`. `p99` is the 99<sup>th</sup> percentile value, a similarly for `p98` and `p96`.
- Tunes and chromaticities via symbols `nux`, `dnux/dp`, (and corresponding symbols for y).
- Chromatic derivatives of beta and alpha functions, via symbols `dbetax/dp`, `dbetay/dp`, `dalphax/dp`, and `dalphay/dp`.
- First- and second-order momentum compaction factors via symbols `alphac` and `alphac2`.
- If radiation integral computation is requested, one may use `ex0` and `Sdelta0` for the equilibrium emittance and momentum spread, plus `J<plane>` and `tau<plane>` for the damping partition and damping time, where `<plane>` is `x`, `y`, or `delta`. One may also use `I1` through `I5` for the individual radiation integrals.
- If `compute_driving_terms=1`, then the quantities `h11001`, `h00111`, `h20001`, `h00201`, `h10002`, `h21000`, `h30000`, `h10110`, `h10020`, `h10200`, `h22000`, `h11110`, `h00220`, `h31000`, `h40000`, `h20110`, `h11200`, `h20020`, `h20200`, `h00310`, `h00400`, `dnux/dJx`, `dnux/dJy`, and `dnuy/dJy` may be used. Table 2 explains the meaning of the terms.
- The coupling integral and emittance ratio due to x-y coupling may be accessed using the symbols `couplingIntegral` and `emittanceRatio`. See section 3.1.4.4 of [19].
- If higher-order chromaticity is requested, then one may use the symbols `dnux/dp2`, `dnux/dp3`, `dnuy/dp2`, `dnuy/dp3`, `etax2`, `etax3`, `etay2`, `etay3`, `nuxChromLower`, `nuxChromUpper`, `nuyChromLower`, and `nuyChromUpper`.
- If the `tune_shift_with_amplitude` command was also given and one may use the symbols `dnux/dAx`, `dnux/dAy`, `dnuy/dAx`, `dnuy/dAy`, `dnux/dAx2`, `dnux/dAy2`, `dnux/dAxAy`, `dnuy/dAx2`, `dnuy/dAy2`, `dnuy/dAxAy`, `nuxTswaLower`, `nuxTswaUpper`, `nuyTswaLower`, and `nuyTswaUpper`.

If the `floor_coordinates` command was given, one may use `X`, `Z`, and `theta` to refer to the final values of the floor coordinates.



If the `sasefel` command was given, one may use variables of the form `SASE.<property>`, where `<property>` is one of `gainLength`, `saturationLength`, `saturationPower`, or `lightWavelength`.

Finally, one may use any of the names from the “final” output file (see `run_setup`), e.g., `Sx` (x beamsize) or `eny` (y normalized emittance). These refer to tracked properties of the beam.

The equation may be left blank, in which case the user must give one or more `optimization_term` commands. These use the same symbols, of course.

There are several `rpn` functions that are useful in constructing a good optimization equation. These are “soft-edge” greater-than, less-than, and not-equal functions, which have the names `segt`, `selt`, and `sene`, respectively. The usage is as follows:

- `V1 V2 T segt`. Returns a nonzero value if and only if value `V1` is greater than `V2`. The returned value is  $((V_1 - V_2)/T)^2$ . Typically used to constraint a quantity from above. E.g., to limit the maximum horizontal beta function to 10m with a tolerance of  $T = 0.1m$ , one would use `max.betax 10 .1 segt`.
- `V1 V2 T selt`. Returns a nonzero value if and only if value `V1` is less than value `V2`. The returned value is  $((V_1 - V_2)/T)^2$ . Typically used to constrain a value from below. E.g., to limit a beta function to greater than 3 m with a tolerance of 0.1 m, one would use `betax 3 .1 selt`.
- `V1 V2 T sene`. Returns a nonzero value if and only if `V1` and `V2` differ by more than `tol`. If  $V_1 > V_2$ , returns  $((V_1 - (V_2 + T))/T)^2$ . If  $V_2 > V_1$ , returns  $((V_2 - (V_1 + T))/T)^2$ .

- `mode` — May be either “minimize” or “maximize”.
- `method` — May be one of “simplex”, “grid”, “powell”, “randomwalk”, “randomsample”, or “sample”. Recommended methods are “simplex” and “randomwalk”. The latter is very useful when the lattice is unstable or nearly so.
- `tolerance` — The convergence criterion for the optimization, with a negative value indicating a fractional criterion.
- `target` — The value which, if reached, results in immediate termination of the optimization, whether it has converged or not.
- `center_on_orbit` — A flag indicating whether to center the beam transverse coordinates on the closed orbit before tracking.
- `center_momentum_also` — A flag indicating whether to center the momentum coordinate also.
- `soft_failure` — A flag indicating, if set, that failure of an optimization pass should not result in termination of the optimization.
- `n_evaluations` — The number of allowed evaluations of the optimization function. If simplex optimization is used, this is the number of allowed evaluations per pass.
- `n_passes` — The number of optimization passes made to achieve convergence (“simplex” only). A pass ends (roughly) when the number of evaluations is completed or the function doesn’t change within the tolerance. A new pass involves starting the optimization again using step sizes determined from the range of the simplex and the factor `simplex_pass_factor`.

- **n\_restarts** — The number of complete restarts of the optimization (simplex only). This is an additional loop around the **n\_passes** loop. The difference is that a restart involves using the optimized result but the original step sizes. It is highly recommended that this feature be used if convergence problems are seen.
- **restart\_worst\_term\_factor**, **restart\_worst\_terms** — Often when there are convergence problems, it is because a few terms are causing difficulty. Convergence can often be obtained by *increasing* the weighting of these terms. If **restart\_worst\_term\_factor** is positive, then **elegant** will multiply the weight of the **restart\_worst\_terms** largest terms by this factor at the beginning of a restart.
- **matrix\_order** — Specifies the highest order of matrix elements that should be available for fitting. Elements up to third order are available for the terminal point of the beamline, and up to second order for interior fit points. Names for first-, second-, and third-order elements are of the form *R<sub>ij</sub>*, *T<sub>ijk</sub>*, and *U<sub>ijkl</sub>*.
- **log\_file** — A file to which progress reports will be written as optimization proceeds. For SDDS data, use the **final** output file from the **run\_setup** namelist.
- **term\_log\_file** — This names a file to which the values of the optimization terms are written at the completion of optimization, which can be convenient when large numbers of terms are used. For example, by using **sddsort** one could find which terms are contributing most to the penalty value.
- **output\_sparsing\_factor** — If set to a value larger than 0, results in sparsing of output to the “final” file (see **run\_setup**). This can make a significant difference in the optimization speed.
- **balance\_terms** — If nonzero, then all terms of the optimization expression have their weights adjusted so they make equal contributions to the penalty function. This can help prevent optimization of a single term at the expense of others. It is performed only for the initial value of the optimization function.
- **simplex\_divisor** — The factor by which simplex step sizes are changed as the optimization algorithm searches for a valid initial simplex.
- **simplex\_pass\_range\_factor** — When starting a new pass, the simplex optimizer takes the range over the previous simplex of each variable times this factor as the starting step size for that variable. This can be useful if the optimization brings the system close to an instability. In such a case, the simplex routine may have trouble constructing an initial simplex if the range of the variables is large. Setting this control to a value less than 1 may help.
- **include\_simplex\_1d\_scans** — If nonzero, optimizer performs single-variable scans prior to starting simplex optimization. This is usually a good idea, but in some cases it will cause problems. For example, if your design is on the edge of being unstable, you may get some many errors from the initial steps that the single-variable optimizer can’t continue. Disabling the single-variable scans will sometimes solve this.
- **start\_from\_simplex\_vertex1** — If nonzero, optimizer uses the initial simplex vertex as the starting point for each new 1d scan. Otherwise, it uses the result of the previous scan.

- `restart_random_numbers` — If nonzero, the random number generators used by `elegant` are reset for each evaluation of the optimization function. This is valuable if one is optimizing tracking results that involve random processes (e.g., ISR or scattering).
- `interrupt_file` — Gives the name of a file that will be monitored by the program as it runs. If the file is created or modified while optimization is running, the optimizer will complete the present step and cleanly terminate, allowing subsequent commands, if any, to proceed.
- `interrupt_file_check_interval` — If nonzero, then gives the interval in function evaluations between checks of the interrupt file. If zero, the interrupt file is only checked at the end of a simplex pass. N.B.: Depending on the responsiveness of the file system and the time required for a function evaluation, setting this to a small value could have a significant adverse impact on the run time.

## parallel\_optimization\_setup

### 7.43 parallel\_optimization\_setup

- type: setup command (for Pelegant only).
- function: define overall parallel optimization parameters and methods.
- N.B.: In addition to the optimization parameters used in the optimization\_setup command, several new parameters are added for parallel optimization. User should replace optimization\_setup with parallel\_optimization\_setup and append necessary parameters.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&parallel_optimization_setup
  STRING method = "simplex";
  double hybrid_simplex_tolerance = -0.01;
  double hybrid_simplex_tolerance_count = 2;
  long hybrid_simplex_comparison_interval = 0;
  double random_factor = 1
  long n_iterations = 10000;
  long max_no_change = 10000;
  long population_size = 100;
  STRING population_log = NULL;
  long print_all_individuals = 0;
  long output_sparsing_factor = 1;
  STRING crossover = "twopoint";
  STRING simplex_log = NULL;
  long simplex_log_interval = 1;
&end
```

- **method** — May be one of “genetic”, “hybridsimplex” or “swarm”. If the default “simplex” method is chosen, all the processors will do the same optimization as the serial version if there is only one particle for optimization tracking, or do optimization tracking in parallel if the number of particles is larger than the number of CPUs. All algorithms can be used for global optimization. “swarm” is recommended when there is sufficient computation resource available, so it can reach the optimization target fast. “hybridsimplex” is recommended when the initial point is close to the optimal result. “genetic” can be chosen for a global optimizer with a random start point (0 should be avoided for any initial coordinate).
- **random\_factor** — The factor to scale the step size for both parallel swarm and genetic methods.
- **n\_restarts** — For the parallel “hybridsimplex” method, this number should be set larger than 1, so the the best result across all processors can be used for the next restart. The parameter is not used for the swarm method.
- **hybrid\_simplex\_tolerance** , **hybrid\_simplex\_tolerance\_count** — For the parallel “hybridsimplex” method, these set, respectively, the tolerance value for changes between full iterations (restarts). If the result does not improve by more than **hybrid\_simplex\_tolerance** after **hybrid\_simplex\_tolerance\_count** iterations, the optimization terminates.

- **hybrid\_simplex\_comparison\_interval** — For the parallel “hybridsimplex” method, sets the interval between comparisons of progress among the several optimizations, in units of function evaluations. Once any of the optimizations is below the **target** value, all optimizations are sent an abort command. Ignored if zero or negative, in which case all optimizations run to completion. Depending on the time required to perform a single function evaluation, setting this to a small value may *increase* the required run time due to the overhead of frequency interprocessor communication.
- **simplex\_log** — For the parallel “hybridsimplex” method, rootname for files to which data from each simplex optimization will be written. Intended only for debugging as it will adversely impact performance.
- **simplex\_log\_interval** — Interval at which **simplex\_log** files will be updated.
- **n\_iterations** — The maximal number of generations/iterations for the parallel genetic and particle swarm optimization.
- **population\_size** — The number of individuals to be generated for each generation/iteration for the swarm and genetic method. For the hybridsimplex method, the number of individuals is equal to the number of processors used.
- **max\_no\_change** — The maximal number of generations in which no change in the best evaluation is allowed before the genetic method stops (genetic method only).
- **n\_evaluations** — This is not used as a stop condition in the genetic optimization. The **n\_iterations** or **max\_no\_change** can be used instead. For the hybridsimplex method, this is the number of allowed evaluations per restart.
- **population\_log** — An SDDS file to which the best individual in a population can be written after each iteration as optimization proceeds. Recommended value: “%s.pop”. For the parallel genetic method, user can choose to print out all the individuals (See **print\_all\_individuals**).
- **print\_all\_individuals** — If nonzero, all the strings in a population will be recorded in the **population\_log** file. This is supported for the genetic method only.
- **output\_sparsing\_factor** — For genetic optimization, this is used to set the frequency of printing strings in the log file with the number of generations as the interval.
- **crossover** — For genetic optimization, it allows the user to choose a crossover type from “onepoint”, “twopoint” and “uniform”. “twopoint” is the default crossover type. If the dimension is 2, it will be set to onepoint crossover.

Note:

- Genetic optimization in **Pelegant** terminates when at least one of the stopping rules specified has been met. The two stopping rules are:
  - generation limit (**n\_iterations**) exceeded
  - no change in the best solution found in a given number of generations. The default is to stop when the generation limit (10000 is the default value) is reached. While the **max\_no\_change** is more favorite to use, as it will stop until the result can not be improved after a certain number of iterations (10000 is the default value). The **n\_iterations** can be set to a very large number to use this rule as the stop condition alone.

- step size control – The mutation step size in the genetic optimization is selected from a Gaussian distribution with mean 0 and standard deviation `step_size`, where `step_size` is provided by user. All the dimensions will use the same standard deviation for an iteration. The `step_size` of the first dimension provided by user will be used as the original step size for all the dimensions. The step size will be reduced by the golden ratio (1.618) if the best value is unchanged after every 3000 iterations. After every 3000 iterations since the last time the step size is reduced, the step size will be increased by the golden ratio.
- As the genetic optimization implementation in **Pelegant** internally updates individuals with a relative change of the current value for a variable, 0 should be avoided to use as an initial value.

## optimization\_term

### 7.44 optimization\_term

- type: setup command.
- function: define optimization equation via individual terms
- sequence: must follow `optimization_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&optimization_term
  STRING term = NULL;
  double weight = 1.0;
  STRING field_string = NULL;
  long field_initial_value = 0;
  long field_final_value = 0;
  long field_interval = 1;
  STRING input_file = NULL;
  STRING input_column = NULL;
  long verbose = 0;
&end
```

- **term** — An `rpn` expression giving one term to be optimized. If more than one `optimization_term` command is given, then the terms are added. The advantage of using this command over giving an equation via `optimization_setup` is that `elegant` will report the value of each term as it performs the optimization (if a `log_file` is given to `optimization_setup`). This permits determination of which terms are causing problems for the optimization.

Please see the entry for `equation` under `optimization_setup` for details on designing optimization terms.

- **weight** — The weight to assign to this term. If zero, the term is ignored.
- **field\_string**, **field\_initial\_value**, **field\_final\_value**, **field\_interval** — These parameters are used to perform substitution of a series of values into the string given by **term**. This can be used to make an identical constraint at a number of instances of the same marker. For example, to constraint `Cx` to zero at instances 1, 3, 5, ..., 39, of marker `M1`, one could use

```
&optimization_term
  term = "M1#@.Cx sqr",
  field_string = @,
  field_initial_value = 1, field_final_value = 39, field_interval = 2
&end
```

- **input\_file**, **input\_column** — If given, **input\_file** is taken as the name of an SDDS file, which is expected to have a string column named by **input\_column**. Each row of the column is taken as a separate optimization term.
- **verbose** — If nonzero, optimization terms are echoed to the terminal as they are created or read from the input file.

## optimization\_variable

### 7.45 optimization\_variable

- type: setup command.
- function: defines a parameter of an element to be used in optimization.
- sequence: must follow `optimization_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- N.B.: It is not possible to optimize an element if the element name starts with one of the following characters: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ., +, or -. The reason is that `elegant` will attempt to make an SDDS parameter name containing the element name, and these characters are disallowed at the beginning of such a name.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&optimization_variable
  STRING name = NULL;
  STRING item = NULL;
  double lower_limit = 0;
  double upper_limit = 0;
  long differential_limits = 0;
  double step_size = 1;
  long disable = 0;
  long force_inside = 0;
  long no_element = 0;
  double initial_value = 0;
&end
```

- `name` — The name of the element.
- `item` — The parameter of the element to be varied.
- `lower_limit`, `upper_limit` — The lower and upper limits allowed for the parameter. If these are equal, the range of the parameter is unlimited.
- `differential_limits` — If nonzero, then the lower and upper limits are being given relative to the initial value, rather than in absolute terms.
- `step_size` — The initial step size (“simplex” optimization) or the grid size in this dimension (“grid” or “sample” optimization).
- `disable` — If nonzero, the variable is ignored.
- `force_inside` — If nonzero, the initial value is forced inside the allowed range defined by the `lower_limit` and `upper_limit` parameters.
- `no_element`, `initial_value` — Allows defining a variable that is not connected to a beamline element, and giving the initial value for the variable. The variable can then be used in other optimization-related commands, e.g., `optimization_covariable`.



## print\_dictionary

### 7.46 print\_dictionary

- type: action command.
- function: print dictionary of supported accelerator elements.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&print_dictionary  
  STRING filename = NULL;  
  long SDDS_form = 0;  
&end
```

- **filename** — The name of a file to which the dictionary will be written. By default, the output is in  $\text{\LaTeX}$  format.
- **SDDS\_form** — If non-zero, then the output is in SDDS format.

## ramp\_elements

### 7.47 ramp\_elements

- type: setup command.
- function: define parameters for time-dependent ramping of elements
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&ramp_elements
  STRING name = NULL;
  STRING item = NULL;
  STRING type = NULL;
  long start_pass = 0;
  long end_pass = LONG_MAX;
  double start_value = 0;
  double end_value = 0;
  long differential = 1;
  long multiplicative = 0;
  long start_occurence = 0;
  long end_occurence = 0;
  double exponent = 1;
  double s_start = -1;
  double s_end = -1;
  STRING before = NULL;
  STRING after = NULL;
  long verbose = 0;
  STRING record = NULL;
&end
```

N.B.: This command will produce unpredictable results when used with `error_element`, `alter_elements`, `modulate_elements`, and `load_parameters` (except when `change_defined_values=1`). It should work properly with `link_elements` in turn-by-turn mode when the source element is ramped, but not when the target element is ramped.

- **name** — A possibly-wildcard-containing string giving the names of the elements to modulate. If not specified, then one must specify **type**.
- **item** — The name of the parameter to modulate.
- **type** — A possibly-wildcard-containing string giving the names of element *types* to modulate. May be specified with **name** or by itself.
- **start\_pass**, **end\_pass** — The starting and ending pass,  $i_{\text{start}}$  and  $i_{\text{end}}$  for the ramp. For passes less than **start\_pass**, the ramp value is **start\_value**. For passes greater than **end\_pass**, the ramp value is **end\_value**.
- **start\_value**, **end\_value** — The end-point values  $S$  (start) and  $E$  (end) of the ramp.

- **exponent** — The exponent  $p$  for the variation of values between the start and end of the ramp. The ramp function  $R(i)$  is

$$R(i) = S + (E - S) * \left( \frac{i - i_{\text{start}}}{i_{\text{end}} - i_{\text{start}}} \right)^p. \quad (6)$$

Note that  $i = 0$  on the first pass.

- **differential, multiplicative** — Determine how the amplitude function  $A(t)$  is used to obtain the new value of the parameter. There are four cases
  - **differential=1, multiplicative=0**:  $v(t) = v_0 + R(i)$  (default).
  - **differential=0, multiplicative=0**:  $v(t) = R(i)$ .
  - **differential=1, multiplicative=1**:  $v(t) = v_0 + v_0 R(i)$ .
  - **differential=0, multiplicative=1**:  $v(t) = v_0 R(i)$ .
- **start\_occurrence, end\_occurrence** — If nonzero, these give the starting and ending occurrence numbers of elements that will be modulated. N.B.: if wildcards are used, occurrence number counting is for each set of identically-named elements separately, rather than for the sequence of matched elements.
- **s\_start, s\_end** — If non-negative, these give the giving and ending position limits for the end-of-element locations of elements to be modulated.
- **after** — The name of an element. If given, the modulation is applied only to elements that follow the named element in the beamline.
- **before** — The name of an element. If given, the modulation is applied only to elements that precede the named element in the beamline.
- **verbose** — If nonzero, information is printed to the standard output as changes are made. Use for debugging only, since otherwise it may slow the simulation.
- **record** — Gives a possibly incomplete filename to which will be written a record of the values of the ramp.

## rf\_setup

### 7.48 rf\_setup

- type: setup/action command.
- function: set up rf cavity frequency, phase, and voltage for a storage ring
- sequence: must follow `run_setup`. In action mode, must follow action-mode instance of `twiss_output`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&rf_setup
  STRING filename = NULL;
  STRING name = NULL;
  long start_occurrence = -1;
  long end_occurrence = -1;
  double s_start = -1;
  double s_end = -1;
  long set_for_each_step = 0;
  double near_frequency = 0;
  long harmonic = -1;
  double bucket_half_height = 0;
  double over_voltage = 0;
  double total_voltage = 0;
  long disable = 0;
  long output_only = 0;
  long track_for_frequency = 0;
&end
```

This command must follow a `twiss_output` command that includes radiation integral computation, since the energy loss per turn is needed to set up the rf cavities. Note that the command includes features to allow selecting a subset of the RFCA elements in the beamline. The selected subset is assumed to include all of the cavities that will impart net energy to the beam.

This command stores values for bunch length in symbols `Sz0` and `St0`, and also stores the fractional energy spread in `Sdelta0`, where they can be used in `rpn` expressions in subsequent commands, e.g.,

```
&bunched_beam
  sigma_dp = "(Sdelta0)",
  sigma_s = "(Sz0)",
  ...
&end
```

- `filename` — Name of a file to which data related to the rf settings will be written.
- `name` — A possibly-wildcard-containing string giving the names of the elements to set. If not given, all RFCA elements are selected.

- **start\_occurence, end\_occurence** — If nonzero, these give the starting and ending occurrence numbers of elements that will be set.
- **s\_start, s\_end** — If non-negative, these give the starting and ending position limits for the end-of-element locations of elements to be set.
- **set\_for\_each\_step** — If nonzero, then the setup is repeated at each simulation step. In this case, one must also give **output\_at\_each\_step=1** for **twiss\_output**.
- **near\_frequency** — If nonzero, then the rf frequency is chosen to be the closest harmonic to the given frequency.
- **harmonic** — If nonzero, then the rf frequency is set to the given harmonic of the revolution frequency.
- **bucket\_half\_height** — If nonzero, the voltage is computed so as to give the specified bucket half height.

$$\left(\frac{\Delta p}{p}\right)_{\text{bucket}} = \sqrt{\frac{U_0}{\pi \alpha h E}} \sqrt{F(q)}, \quad (7)$$

where  $U_0$  is the energy loss per turn,  $\alpha$  is the momentum compaction factor,  $h$  is the harmonic,  $E$  is the beam energy,

$$F(q) = 2 \left( \sqrt{q^2 - 1} - \arccos \frac{1}{q} \right), \quad (8)$$

and  $q$  is the overvoltage factor, related to the rf voltage by  $q = V/U_0$ . (See Wiedemann, Vol. 1, 8.2.2.)

- **over\_voltage** — If nonzero, the voltage is set to the given factor relative to the energy loss per turn.
- **total\_voltage** — If nonzero, the total rf voltage is set to the given value. The frequency and phase are computed for this voltage.
- **disable** — If nonzero, command does nothing.
- **output\_only** — If nonzero, command generates output file but does not change rf cavity settings.
- **track\_for\_frequency** — If nonzero, particle tracking is used to determine the rf frequency. If zero, the ideal length of the lattice is used.

## replace\_elements

### 7.49 replace\_elements

- type: action command.
- function: Replace old element with a newly defined element, or just remove it from beamline. This is a convenient way to modify lattice in an elegant run. See also `transmute_elements`.
- sequence: must follow `run_setup`.
- notes: The modified lattice can be saved through `save_lattice` command. Be sure to use “output\_seq = 1” option in that command.
- warning: The element’s occurrence is re-calculated after each usage of this command. If you need to repeat this command for SAME named element several times, you have to re-calculate it occurrence every time. For example, you want to remove Q1 at occurrence position (1,3,5), and use ‘replace\_elements” twice. If in the first command you use “occurrence[0]=1,3”, then in the second command you have to use “occurrence[0]=3”, since after remove of (1,3) Q1s, the 5th Q1 now becoming 3rd Q1.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&replace_elements
    STRING name = NULL;
    STRING type = NULL;
    STRING exclude = NULL;
    long skip = 1;
    long disable = 0;
    STRING element_def = NULL;
    long total_occurrences = 0;
    long occurrence[100]={0};
&end
```

- **name** — Possibly wild-card containing string specifying the name of the elements to be removed or replaced.
- **type** — Possibly wild-card containing string specifying the type of the elements to be removed or replaced.
- **exclude** — Possibly wild-card containing string specifying the name of elements to be excluded from this command.
- **skip** — The element is removed or replaced at every  $n^{th}$  specified location.
- **disable** — If nonzero, the command is ignored.
- **element\_def** — If NULL, the specified elements are removed from the beamline. If not NULL, the specified elements are replaced with the new element defined here. The definition of the element should be just as it would be entered in the lattice file.

- **total\_occurrences**, **occurrence** — These parameters are used to replace or delete specified occurrences of the element **name**. **total\_occurrences** specifies how many elements to replace or delete up to a maximum of 100, while the entries in the array **occurrence** specify the occurrences to replace or delete. If **total\_occurrences** is non-zero, then **skip** must be set to zero and the **name** must be the exact name (no wild-card matching).

## `rpn_expression`

### 7.50 `rpn_expression`

- type: action/setup command.
- function: pass an expression directly to the `rpn` submodule for execution.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

`&rpn_expression`

`STRING expression = NULL;`

`&end`

- **expression** — An `rpn` expression. This expression is executed immediately and can be used, for example, to read in `rpn` commands from a file or store values in `rpn` memories.



## rpn\_load

### 7.51 rpn\_load

- type: action/setup command.
- function: load data from SDDS file into RPN variables.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&rpn_load
  STRING tag = NULL;
  STRING filename = NULL;
  STRING match_column = NULL;
  STRING match_column_value = NULL;
  long matching_row_number = -1;
  STRING match_parameter = NULL;
  STRING match_parameter_value = NULL;
  long use_row = -1;
  long use_page = -1;
  long load_parameters = 0;
&end
```

This command is used to facilitate multi-stage optimization runs by allowing convenient loading of data from SDDS files into RPN variables. For example, one may match the final Twiss parameters of a lattice to the parameters stored in an SDDS file from a different run.

- **tag** — Option string that will be pre-pended to the names of all the numerical columns in the file in order to create RPN variable names. E.g., if the input file was from the `twiss_output` command and `tag = tw1` was given, then RPN variables `tw1.betax`, `tw1.alphax`, etc. would be used. *N.B.: If the tag is blank, then nothing is appended to the names from the file. This can be dangerous since the names may conflict with the names of other variables!*
- **filename** — The (incomplete) name of the SDDS file from which to read data. By default, data is taken from all columns from the last row of the last page of the file. This default behavior can be altered using one or more of the following parameters:
  - **match\_column** — The name of a string column to use in selecting the row from which data will be taken.
  - **match\_column\_value** — The value that the column named by **match\_column** must have to be selected from the file. By default, the last row with a matching value is used.
  - **matching\_row\_number** — If a nonnegative value is given, then the **matching\_row\_number**<sup>th</sup> matching row is selected (0 is the first row, 1 the second, etc). Otherwise, the last match row is used. Ignored if **match\_column** is not given.
  - **match\_parameter** — The name of a string parameter to use in selecting the page from which data will be taken.
  - **match\_parameter\_value** — The value that the parameter named by **match\_parameter** must have to be selected from the file. By default, the last page with a matching value is used.

- **use\_row** — If nonnegative, specifies the row number to use, starting at 0 for the first row. Ignored if **match\_column** is given.
- **use\_page** — If nonnegative, specifies the page number to use, starting at 1 for the first page. Takes precedence over **\match\_parameter** if both are given.
- **load\_parameters** — If nonzero, specifies loading the SDDS parameter data rather than the column data.

## run\_control

### 7.52 run\_control

- type: setup command.
- function: set up the number of simulation steps and passes.
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&run_control
    long n_steps = 1;
    double bunch_frequency = 0;
    long n_indices = 0;
    long n_passes = 1;
    long n_passes_fiducial = 0;
    long reset_rf_for_each_step = 1;
    long first_is_fiducial = 0;
    long restrict_fiducialization = 0;
&end
```

- `n_steps` — The number of separate repetitions of the action implied by the next action command. If random errors are defined, this is also the number of separate error ensembles.
- `bunch_frequency` — The frequency to use in calculating the time delay between repetitions.
- `n_indices` — The number of looping indices for which to expect definitions in subsequent `vary_element` commands. If nonzero, then `n_steps` is ignored.
- `n_passes` — The number of passes to make through the beamline per repetition.
- `n_passes_fiducial` — The number of passes to make through the beamline per repetition for the fiducial beam. If non-positive, use `n_passes`. For ring tracking, should probably always be set to 1.
- `reset_rf_for_each_step` — If nonzero, the rf phases are established anew for each bunch tracked. Should be zero to simulate phase and timing jitter.
- `first_is_fiducial` — If nonzero, the first bunch seen is taken to establish the reference phases and momentum profile. If zero, each bunch is treated as a new fiducializing bunch.
- `restrict_fiducialization` — If nonzero, then momentum profile fiducialization occurs only after elements that are intended change the momentum, such as rf cavities. If zero, then each element is fiducialized to the average momentum of the beam. Active only if `first_is_fiducial=1` and overrides the `always_change_p0` setting in `run_setup`.

## run\_setup

### 7.53 run\_setup

- type: setup command.
- function: set global parameters of the simulation and define primary input and output files.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&run_setup
  STRING lattice = NULL;
  STRING use_beamline = NULL;
  STRING rootname = NULL;
  STRING output = NULL;
  STRING centroid = NULL;
  STRING sigma = NULL;
  STRING final = NULL;
  STRING acceptance = NULL;
  STRING losses = NULL;
  STRING magnets = NULL;
  STRING semaphore_file = NULL;
  STRING parameters = NULL;
  long combine_bunch_statistics = 0;
  long wrap_around = 1;
  long final_pass = 0;
  long default_order = 2;
  long concat_order = 0;
  long print_statistics = 0;
  long show_element_timing = 0;
  long monitor_memory_usage = 0;
  long random_number_seed = 987654321;
  long correction_iterations = 1;
  double p_central = 0.0;
  double p_central_mev = 0.0;
  long always_change_p0 = 0;
  STRING expand_for = NULL;
  long tracking_updates = 1;
  long echo_lattice = 0;
  STRING search_path = NULL;
  long element_divisions = 0;
  long load_balancing_on = 0;
  long back_tracking = 0;
&end
```

- `lattice` — Name of the lattice definition file.
- `echo_lattice` — If nonzero, the lattice input is echoed to the standard output as the lattice is parsed. This can help detect certain problems with the lattice that cause **elegant** to crash.

- **use\_beamline** — Name of the beamline to use.
- **rootname** — Filename fragment used in forming complete names from incomplete filenames. By default, the filename minus extension of the input file is used.
- **output** — The (incomplete) name of an SDDS file into which final phase-space coordinates will be written. Recommended value: “%s.out”.
- **centroid** — The (incomplete) name of an SDDS file into which beam centroids as a function of *s* will be written. Recommended value: “%s.cen”.
- **sigma** — The (incomplete) name of an SDDS file into which the beam sigma matrix as a function of *z* will be written. Recommended value: “%s.sig”. N.B.: confusion sometimes occurs about some of the quantities related to the *s* coordinate in this file. Please see Section 4 above.
- **final** — The (incomplete) name of an SDDS file into which final beam and transport parameters will be written. Recommended value: “%s.fin”. N.B.: confusion sometimes occurs about some of the quantities related to the *s* coordinate in this file. Please see Section 4 above.
- **acceptance** — The (incomplete) name of an SDDS file into which the initial coordinates of transmitted particles will be written. Recommended value: “%s.acc”.
- **losses** — The (incomplete) name of an SDDS file into which information on lost particles will be written. Recommended value: “%s.lost”.
- **magnets** — The (incomplete) name of an SDDS file into which a magnet layout representation will be written. Recommended value: “%s.mag”.
- **semaphore\_file** — The (incomplete) name of file that will be created just before exit from the program, but only if no errors occurred. If the file exists, it is deleted. This file can be used to record the fact that the run completed without error.
- **parameters** — The (incomplete) name of an SDDS file into which parameters of accelerator elements are written. N.B.: this file does not contain any non-numerical parameters of the lattice. Hence, it is not a complete description of the settings of the lattice.
- **combine\_bunch\_statistics** — A flag indicating whether to combine statistical information for all simulation steps. If non-zero, then the **sigma** and **centroid** data will be combined over all simulation steps.
- **wrap\_around** — A flag indicating whether the *s* coordinate should wrap-around or increase monotonically in multipass simulations. If zero, then the centroid and sigma data is computed for each turn with the *s* coordinate increasing continuously.
- **final\_pass** — A flag indicating whether the centroid and sigma output should be computed only from the data from the final pass. By default, the statistics include data from all passes.
- **default\_order** — The default order of transfer matrices used for elements having matrices.
- **concat\_order** — If non-zero, the order of matrix concatenation used.

- **print\_statistics** — A flag indicating whether to print information as each element is tracked. If greater than 0, information is printed after each element from the beginning of tracking. If equal to  $n$  with  $n < 0$ , information is printed only after pass  $|n|$ .
- **show\_element\_timing** — A flag indicating whether to collect and report execution time statistics binned by element type.
- **monitor\_memory\_usage** — A flag indicating whether to monitor memory usage during tracking to detect memory leaks.
- **random\_number\_seed** — A seed for the random number generators. If zero, a seed will be generated from the system clock.
- **correction\_iterations** — Number of iterations of tune and chromaticity correction.
- **p\_central** — Central momentum of the beamline, about which expansions are done. This is  $\beta\gamma$ .
- **p\_central\_mev** — Central momentum of the beamline in MeV/c, about which expansions are done. Ignored if **p\_central** is nonzero.
- **always\_change\_p0** — If nonzero, then **elegant** will match the reference momentum to the beam momentum after each element. For example, in a beamline with radiation losses, one might want to adjust downstream magnets to match the energy of the incoming beam.
- **expand\_for** — Name of an SDDS file containing particle information, from which the central momentum will be set. The file contents are the same as required for **elegant** input with the **sdds\_beam** namelist.
- **tracking\_updates** — A flag indicating whether to print summary information about tracking.
- **search\_path** — Specify a list of pathnames in which to look for input files, including lattice files, wakefield input, particle input, etc. This allows storing common input files in a convenient location without having to put the location into every filename.
- **element\_divisions** — Specify how many pieces to split elements into. Only certain elements (basically, those with a matrix) are split. Results in creation of **element\_divisions** new elements having the same name as each split element.
- **load\_balancing\_on** — If 1, load-balancing is performed for parallel mode. This can result in non-deterministic results if the load-balancing is different on two otherwise identical runs. Load-balancing variations may occur in heterogeneous clusters, clusters with multiple users, or for other reasons. In such situations, turning off load balancing can be useful if, for example, one is performing parameter scans and wishes to eliminate spurious sources of variation. If -1, then the load balance is checked and reported, but no rebalancing takes place.
- **back\_tracking** — If nonzero, then back-tracking is performed. The beamline is reversed in order and the beam is propagated backwards through the elements. Only a selection of elements are supported at present, including CHARGE, CSBEND, DRIF, EDRIFT, EHCOR, EHVCOR, EVCOR, HMON, KOCT, KQUAD, KSEXT, MARK, MONI, QUAD, RFCA, SBEN, SEXT, TRWAKE, UKICKMAP, VMON, WAKE, and WATCH.

## sasefel

### 7.54 sasefel

- type: setup/action command.
- function: set parameters for computation of SASE FEL gain and other properties.
- sequence: must follow `run_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

`&sasefel`

```
STRING output = NULL;  
STRING model = "Ming Xie";  
double beta = 0;  
double undulator_K = 3.1;  
double undulator_period = 0.033;  
double slice_fraction = 0.0;  
long n_slices = 0;
```

`&end`

- `output` — The (incomplete) filename of an SDDS file to which output will be written.
- `model` — The name of the FEL model used. At present, only one model is supported; the “Ming-Xie” model is based on the simple parametrization M. Xie[13].
- `beta` — The value of the beta function, in meters.
- `undulator_K` — The K parameter of the undulator.
- `undulator_period` — The undulator period, in meters.
- `slice_fraction, n_slices` — The fraction of beam beam contained by each analysis slice and the number of such slices. By default, no slice analysis is done. Instead, the beam is analyzed only as a whole. If `slice_fraction*n_slices` is less than 1, then the slice analysis is centered on the median of the time distribution. E.g., if `n_slices=1` and `slice_fraction=0.1`, then the central 10% of the beam would be analyzed. More typically, one gives values such that `slice_fraction*n_slices` is equal to 1, so that every part of the beam is analyzed. There are separate values in the output file for each slice, plus the whole-beam and slice-averaged results.

## save\_lattice

### 7.55 save\_lattice

- type: action command.
- function: save the current accelerator element and beamline definitions.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&save\_lattice

    STRING filename = NULL;

    long output\_seq = 0;

&end

- **filename** — The (incomplete) name of a file to which the element and beamline definitions will be written. Recommended value: “%s.new”.
- **output\_seq** — If non-zero, the lattice will be saved as a single beamline sequence. Elements used for the beamline are re-arranged according to their type. Note: sub-beamline definitions in the original lattice file will be destroyed from the output file. This feature is intended to be used together with **insert\_elements** and **replace\_elements**.



## sdds\_beam

### 7.56 sdds\_beam

- type: setup command.
- function: set up for tracking and histogram analyzing of particle coordinates stored in an SDDS file.
- sequence: must follow `run_control`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&sdds_beam
  STRING input = NULL;
  STRING input_list = NULL;
  STRING input_type = "elegant";
  long n_particles_per_ring = 0;
  STRING selection_parameter = NULL;
  STRING selection_string = NULL;
  long one_random_bunch = 0;
  long reuse_bunch = 0;
  long prebunched = -1;
  long track_pages_separately = 0;
  long use_bunched_mode = 0;
  long fiducialization_bunch = 0;
  long sample_interval = 1;
  long n_tables_to_skip = 0;
  long center_transversely = 0;
  long center_arrival_time = 0;
  double sample_fraction = 1;
  double p_lower = 0.0;
  double p_upper = 0.0;
  long save_initial_coordinates = 1;
  long reverse_t_sign = 0;
  long n_duplicates = 0;
  double duplicate_stagger[6] = {0, 0, 0, 0, 0, 0};
&end
```

- `input` — Name of an SDDS file containing coordinates of input particles.
- `input_type` — May be “elegant” or “spiffe”, indicating the name of the program that wrote the input file. The expected data quantities for the different types are:
  - `elegant`: (x, xp, y, yp, t, p), where x and y are in meters,  $xp = x'$  and  $yp = y'$  are dimensionless, t is in seconds, and p = fiff is the dimensionless momentum. If this file is to be generated by the user, the expected units string in the column definitions should be “m”, “s”, and “m\$be\$nc” for meters, seconds and the dimensionless momentum, respectively. The `particleID` column may also be given; it should contain a positive integer that is unique for each particle.

- **spiffe**:  $(r, z, pr, pz, pphi, t)$ , where  $r$  and  $z$  are in meters,  $pr = f_r fl$ ,  $pz = f_z fl$ ,  $p_{CE} = lrf/c$ , and  $t$  is in seconds. If this file is to be generated by the user use the units strings described above.
- **n\_particles\_per\_ring** — For **spiffe** data, gives the number of particles to generate for each ring of charge.
- **selection\_parameter** — The name of a parameter in the SDDS file to be used for selection of pages of data.
- **selection\_string** — The value of the **selection\_parameter** selection parameter required for a page to be used. E.g., if one has a file from the **shower** program containing positrons, electrons, and photons, one might want to select only the positrons.
- **one\_random\_bunch** — A flag indicating whether, for **spiffe** data, a new random distribution should be calculated for each step of the simulation.
- **reuse\_bunch** — A flag indicating whether to use the bunch again or not. If set, then the first bunch in the file is used repeatedly for as many tracking steps as requested. Otherwise, each bunch is used only once and the number of steps is limited to the number of bunches (e.g., the number of pages in the file when **prebunched**=0).
- **prebunched** — Deprecated. Use **track\_pages\_separately** instead.
- **track\_pages\_separately** — If non-zero, then separate pages of the input file are tracked separately. Otherwise, the entire file is tracked together.
- **use\_bunched\_mode** — If non-zero, then the **IDSslotsPerBunch** parameter is used to determine the bunch assignment of particles in the beam based on values in the **particleID** column. In particular, the bunch number is  $\lfloor (I - 1)/S \rfloor$ , where  $I$  is the particle ID and  $S = \text{IDSslotsPerBunch}$ .
- **fiducialization\_bunch** — If non-negative, then rf cavities (e.g., RFCA, RFDF, RAMPRF) are phased to the indicated bunch (0 is the first bunch). Otherwise, rf cavities are phased to the entire beam (which is probably not what is wanted).
- **sample\_interval** — If non-zero, only every **sample\_interval**<sup>th</sup> particle is used.
- **n\_tables\_to\_skip** — Number of SDDS pages to skip at the beginning of the file.
- **center\_transversely** — If non-zero, the transverse centroids of the distribution are made to be zero.
- **center\_arrival\_time** — If non-zero, the mean arrival time of particles at the start of the accelerator is set to zero.
- **sample\_fraction** — If non-unity, the randomly selected fraction of the distribution to use.
- **p\_lower, p\_upper** — If different, the lower and upper limit on **fl** of particles to use.
- **save\_initial\_coordinates** — A flag that, if set, results in saving initial coordinates of tracked particles in memory. This is the default behavior. If unset, the initial coordinates are not saved, but are reread from disk each time they are needed. This is more memory efficient and is useful for tracking very large numbers of particles.

- **n\_duplicates** — This specifies duplicating the particles from the input file to allow tracking more particles. **n\_duplicates** specifies the number of duplications, where the default value of 0 indicates no duplication. If  $n$ -fold duplication is invoked, the particle ID of a new particle is equal to the particle ID of its parent particle plus  $iN_p$ , where  $i = 1, \dots, n+1$  is the duplication index and  $N_p$  is the number of particles in the parent bunch. This should be kept in mind when using the particle ID to segregate the beam into bunches.
- **duplicate\_stagger** — Specifies offsetting of the coordinates  $x$ ,  $x'$ ,  $y$ ,  $y'$ ,  $t$ , and  $\delta$  for each duplication by the specified amounts. One assumes that some stochastic process such as synchrotron radiation will cause further differentiation of duplicate particles. One can also use **SCATTER** or **DSCATTER** elements in the beamline for this purpose.

## semaphores

### 7.57 semaphores

- type: setup command.
- function: set up names for semaphore files, which are used to mark the start and end of program execution.
- sequence: must precede `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&semaphores

```
STRING started = ‘‘%s.started’’;  
STRING done    = ‘‘%s.done’’;  
STRING failed  = ‘‘%s.failed’’;
```

&end

- **started** — Gives the (incomplete) filename of a file to create when a valid `run_setup` command is given.
- **done** — Gives the (incomplete) filename of a file to create when the program exits without error. If the file exists, it is deleted when a valid `run_setup` command is given.
- **failed** — Gives the (incomplete) filename of a file to create when the program exits with an error. If the file exists, it is deleted when a valid `run_setup` command is given.

## set\_reference\_particle\_output

### 7.58 set\_reference\_particle\_output

- type: setup command.
- function: Allows defining a reference set of particle coordinates to which tracked coordinates will be compared for purposes of optimization.
- sequence: must follow `optimization_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- Usage notes: The purpose of this command is to allow optimization of a transport system to produce the same particle distribution as was obtained by tracking through some other system. For example, one might track a collection of particles through a **CWIGGLER** or **BGGEXP** element, then attempt to match the output particles with a different element or set of elements that offer faster tracking. In this case, the optimization run must use the same input distribution as the run that is being matched.

```
&set_reference_particle_output
    STRING match_to = NULL;
    double weight[6] = {1, 1, 1, 1, 0, 1};
    STRING comparison_mode = NULL;
&end
```

- `match_to` — Name of an SDDS file from which a particle distribution will be read. The coordinates of this distribution will be compared to those from tracking to compute a contribution to the optimization penalty function.
- `weight` — Weight to be assigned to each plane. By default, path-length coordinates are not compared.
- `comparison_mode` — May be one of “max-ad”, “sum-ad”, and “sum-sqr”, corresponding to maximum absolute deviation, sum of absolute deviations, and sum of squared deviations. The default is maximum absolute deviation.

## slice\_analysis

### 7.59 slice\_analysis

- type: setup command.
- function: set parameters for slice analysis of the beam along a beamline. Also, results in placing the final slice analysis (at the end of the beamline) in symbols for use in optimization equations. The names of the symbols are the same as the names of the columns in the output file.
- sequence: must follow `run_setup` and precede beam definition (`bunched_beam` or `sdds_beam`).
- N.B.: slice analysis uses an approximate computation of the normalized emittance, regardless of the setting of the `exact_normalized_emittance` flag in the `global_settings` command.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&slice_analysis
STRING output = NULL;
long n_slices = 0;
double s_start = 0;
double s_end = 1e300;
long final_values_only = 0;
&end
```

- `output` — The (incomplete) filename of the output file. Recommended value is “%s.slan”.
- `n_slices` — Number of slices to use.
- `s_start`, `s_end` — Position in beamline at which to start and stop performing slice analysis.
- `final_values_only` — If nonzero, then slice quantities are computed only at the end of the beamline.

## subprocess

### 7.60 subprocess

- type: action command.
- function: execute a system command in a shell.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&subprocess

    STRING command = NULL;

&end

- **command** — The text of the command to execute. The command may use the sequence “%s” for substitution of the rootname as set by `run_setup`. A literal “%s” must be entered as “%%s”.

## steering\_element

### 7.61 steering\_element

- type: setup command.
- function: setup for use of a given parameter of a given element as a steering corrector.
- sequence: must precede **correct**.
- N.B.: any use of this command disables the built-in definition of HKICK, VKICK, and HVKICK elements as steering elements.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&steering_element
  STRING name = NULL;
  STRING element_type = NULL;
  STRING item = NULL;
  STRING plane = "h";
  double tweek = 1e-3;
  double limit = 0;
  long start_occurrence = 0;
  long end_occurrence = 0;
  long occurrence_step = 1;
  double s_start = -1;
  double s_end = -1;
  STRING after = NULL;
  STRING before = NULL;
&end
```

- **name** — Optional: the (possibly wild-carded) name of the element to add to the steering list. If not given, then **element\_type** must be given.
- **element\_type** — Optional: the (possibly wild-carded) name of the element type to add to the steering list. If not given, then **name** must be given.
- **item** — The parameter of the element to be varied.
- **plane** — May be either “h” or “v”, for horizontal or vertical correction.
- **tweek** — The amount by which to change the item to compute the steering strength.
- **limit** — The maximum allowed absolute value of the item.
- **start\_occurrence**, **end\_occurrence** — If nonzero, these give the starting and ending occurrence numbers of elements that will be included. N.B.: if wildcards are used, occurrence number counting is for each set of identically-named elements separately, rather than for the sequence of matched elements.
- **s\_start**, **s\_end** — If non-negative, these give the giving and ending position limits for the end-of-element locations of elements to be included.



- **after** — The name of an element. If given, only elements that follow the named element in the beamline are included.
- **before** — The name of an element. If given, only elements that precede the named element in the beamline are included.

## touschek\_scatter

### 7.62 touschek\_scatter

- type: setup/action command.
- function: Simulate Touschek scattering process at each **TSCATTER** element based on Monte Carlo method. The local scattering rate is calculated by using Piwinski's formula and from the Monte Carlo simulation. Scattered particles can be tracked through the entire beamline (one pass only), and beam loss information is recorded.
- sequence: must follow **run\_setup** and **twiss\_output**.
- can use parallel resources (**Pelegant**)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - A momentum aperture file is required previous using this command. It should contain momentum aperture at least at each **TSCATTER** element and can be obtained by running **momentum\_aperture** command.
  - The simulation can be done for a Gaussian distributed beam or an arbitrary particle distribution given by histogram file(s) (See **MHISTOGRAM**).
  - When using histogram file as input, it should contain data at least at each **TSCATTER** element. This can be done by inserting a **MHISTOGRAM** element following each **TSCATTER** element. With **lumped=1** option, a multi page SDDS file will be output automatically or you can combine individual output file into a multi page SDDS file before using this command.
  - The input particle distribution can be given in 3 ways:  $2D(x-x')+2D(y-y')+2D(dt-dp)$ ; or  $4D(x-x'-y-y')+2D(dt-dp)$ ; or  $6D(x-x'-y-y'-dt-dp)$ ; base on user's choice. We recommend to use lower "order" histogram table if the original particle number which used to generate these table is not large enough.
  - The **emit\_\***, **emit\_dp** and **sigma\_s** is always required for running the simulation (Used for Piwinski's rate). Use closed value when simulate a non-Gaussian distributed bunch.

```
&touschek_scatter
    double charge = 0;
    double frequency = 1;
    double emit_x = 0;
    double emit_nx = 0;
    double emit_y = 0;
    double emit_ny = 0;
    double sigma_dp = 0;
    double sigma_s = 0;
    double distribution_cutoff[3] = {3, 3, 3};
    double Momentum_Aperture_scale = 0.85;
    STRING Momentum_Aperture = NULL;
    STRING XDist = NULL;
```

```

    STRING YDist = NULL;
    STRING ZDist = NULL;
    STRING TranDist = NULL;
    STRING FullDist = NULL;
    STRING bunch = NULL;
    STRING loss = NULL;
    STRING distribution = NULL;
    STRING initial = NULL;
    STRING output = NULL;
    long nbins = 100;
    double sbin_step = 1;
    long n_simulated = 5000000;
    double ignored_portion = 0.01;
    long i_start = 0;
    long i_end = 1;
    long do_track = 0;
    long match_position_only = 0;
    long overwrite_files = 1;
    long verbosity = 0;
&end

```

- **charge** — Bunch charge in Coulombs. May not be zero.
- **frequency** — Bunch repetition frequency in Hz. The product of the **charge** and **frequency** gives the average current in Amps.
- **emit\_x**, **emit\_y** — RMS emittance for the x and y planes. Ignored if RMS normalized emittance is nonzero.
- **emit\_nx**, **emit\_ny** — RMS normalized emittance for the x and y planes.
- **sigma\_dp**, **sigma\_s** — Rms fractional momentum spread,  $\sigma_\delta$ , and rms bunch length.
- **distribution\_cutoff** — The number of sigmas to use in each plane for Gaussian beam.
- **Momentum\_Aperture** — Input file containing the estimated momentum aperture at each TSCATTER element. This can be obtained from the **momentum\_aperture** command in a separate run. (If using the parallel version to obtain the momentum aperture, it will be necessary to use **output\_mode=0** or else reorganize the data if **output\_mode**  $\neq$  0. Also, it will be necessary to use **sddssort** to sort the data by the **s** column.)
- **Momentum\_Aperture\_scale** — This value times the aperture value from **Momentum\_Aperture** file sets up the limit on  $\delta_m$  in the simulation. Only particles that have  $\delta > \delta_m$  will be kept for tracking. And the scattering rate is calculated at this value.
- **XDist**, **YDist**, **ZDist** — Input filename of 2D histogram table of X, Y, and Z plane. X and Y are ignored when **TranDist** or **FullDist** is present.
- **TranDist** — Input file name of the 4D histogram table of transverse plane. Has to be used together with **ZDist**.
- **FullDist** — Input file name of the 6D histogram table. If present, all other tables are ignored.

- **bunch** — The (incomplete) name of an SDDS file to which the phase-space coordinates of the simulated scattered particles are to be written. Recommended value: “%s-%03ld.bun”. If “%03ld” or the equivalent is not provided then only the last simulated bunch is kept (one bunch for one TSCATTER element).
- **loss** — The (incomplete) name of an SDDS file to which the original and final phase-space coordinates of the lost simulated scattered particles are to be written. Recommended value: “%s-%03ld.los”. Used together with `do_track = 1`.
- **distribution** — The (incomplete) name of an SDDS file to which the one-dimensional histogram of simulated scattered particles are to be written. Recommended value: “%s-%03ld.dis”
- **initial** — The (incomplete) name of an SDDS file to which the one dimension histogram of simulated particles before scattering are to be written. Recommended value: “%s-%03ld.ini”
- **output** — The (incomplete) name of an SDDS file. The average loss rate (particles per second) over a step size of `sbin_step` at location `s` is written to this file. Recommended value: “%s-%03ld.out”
- **sbin\_step** — Bin size for loss rate summary output to the `output` file.
- **nbins** — Number of bins used for the `distribution` and `initial` table.
- **n\_simulated** — The total number of simulated scattered particles with  $\delta > \delta_m$ . Choosing too small a value will cause unreliable results. Note: use an integer number here. A number such as 5E6 sometimes will cause you trouble.
- **ignored\_portion** — Fraction of the total scattering rate ignored in tracking. Using this parameter will greatly increase the tracking speed. For example, if the total loss rate is 50% of the total scattering rate, then ignoring for tracking purposes 5% (0.05) of the scattered particles will cause a  $\sim 10\%$  error, but the simulation is greatly sped up.
- **i\_start, i\_end** — The simulation will be done from the `i_startth` to the `i_endth` TSCATTER element along the beamline.
- **do\_track** — If non-zero, scattered particles will be tracked from their generation location for `n_passes` (given by `run_control`). If non-zero, the `run_control` command must proceed the `|touschek_scatter|` command. The loss property can be analysed using `output` or `loss`.
- **match\_position\_only** — If non-zero, then matching of the momentum aperture data to the lattice is done using the position data only (`s` column), rather than the element names. Can be helpful if errors appear about files ending prematurely or data not matching.
- **overwrite\_files** — If non-zero, then output files will be overwritten. If set to zero, then when output files are found, the corresponding computations are skipped. This can be used to restart a Touschek scattering run, provided the output filenames are index (e.g., of the form “%s-%03ld.los” rather than “%s.los”).

**Note:** If using `Pelegant` to compute the momentum aperture with `output_mode=1`, it is necessary to first run the script `reorganizeMmap` to put the data into the form needed by `touschekLifetime`.

## transmute\_elements

### 7.63 transmute\_elements

- type: setup command.
- function: Changes the type of selected elements, which may be used to turn off unneeded diagnostics and speed up tracking when concatenation is being used.
- Must be preceded by `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- notes:
  - Any number of these commands may be given.
  - The only property of the original element that is preserved is the length. For example, transmuting a SBEN into a CSBEN will not have the expected result.

```
&transmute_elements
STRING name = NULL,
STRING type = NULL,
STRING exclude = NULL,
    STRING new_type = "DRIF",
    long disable = 0;
    long clear = 0;
&end
```

- `name` — Possibly wild-card containing string specifying the elements to which the transmutation specification is to be applied.
- `type` — Possibly wild-card containing string specifying the element types to which the transmutation specification is to be applied.
- `exclude` — Possibly wild-card containing string specifying elements to be excluded from the specified transmutation. Does not affect elements transmuted due to other specifications.
- `new_type` — Type into which specified elements will be transmuted.
- `disable` — If nonzero, the command is ignored.
- `clear` — If nonzero, all prior transmutation specifications are deleted.

## tune\_footprint

### 7.64 tune\_footprint

- type: action/setup command.
- function: compute frequency map from tracking and use it to determine the chromatic and amplitude tune footprints.
- sequence: must follow `run_control`.
- can use parallel resources (Pelegant)
- N.B.: the number of turns tracked is set by the `run_control` command.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&tune_footprint
  STRING delta_output = NULL,
  STRING xy_output = NULL,
  double xmin = -0.02,
  double xmax = 0.02,
  double ymin = 1e-6,
  double ymax = 0.02,
  double x_for_delta = 1e-6,
  double y_for_delta = 1e-6,
  double delta_min = 0,
  double delta_max = 0,
  long ndelta = 21,
  long separate_xy_for_delta = 0;
  long nx = 20,
  long ny = 21,
  long verbosity = 1,
  long quadratic_spacing = 1,
  long compute_diffusion = 1;
  long diffusion_rate_limit = -5,
  long immediate = 0
  long filtered_output = 1;
  long ignore_half_integer = 0;
&end
```

- `delta_output` — The optional (incomplete) name of an SDDS file to send tune and diffusion rate vs  $\delta$  output to. Recommended value: “%s.dtf”. If optimization is done, this file is written only at the end of optimization.
- `xy_output` — The optional (incomplete) name of an SDDS file to send tune and diffusion rate vs (x, y) output to. Recommended value: “%s.atf”. If optimization is done, this file is written only at the end of optimization.
- `xmin`, `xmax` — Limits of grid of initial x coordinates for tracking.

- **ymin, ymax** — Limits of grid of initial  $y$  coordinates for tracking. **ymin** should typically be a small, positive value so that there is some betatron oscillation from which to get the tune.
- **delta\_min, delta\_max** — Limits of grid of initial  $\delta$  coordinates for tracking. Not that particles are not centered around the dispersive closed orbit.
- **ndelta** — Number of values of  $\delta$  coordinate in the grid. If zero, chromatic footprint is not determined.
- **separate\_xy\_for\_delta** — If nonzero, tracking for the  $x$  and  $y$  momentum-dependent tunes will be done separately, so that when  $x$ -plane tracking is performed,  $y = 0$  initially. This might be helpful if nonlinear coupling of  $y$  motion into the  $x$  plane causes the  $x$  tune to be poorly determined for small  $x$  amplitudes. Increase the tracking time by a factor of two.
- **nx** — Number of values of  $x$  coordinate in the grid. If zero, amplitude footprint is not determined.
- **ny** — Number of values of  $y$  coordinate in the grid. If zero, amplitude footprint is not determined.
- **verbosity** — If nonzero, prints possibly useful information while running.
- **quadratic\_spacing** — If nonzero, points are spaced “quadratically,” which actually means that their squares are spaced linearly. It is highly recommended to keep this turned on, since otherwise problems determining the tune when  $x \approx 0$  may result in invalid results.
- **compute\_diffusion** — If nonzero, diffusion is computed, which requires tracking twice as many turns.
- **diffusion\_rate\_limit** — Value of the diffusion rate  $d_r$  above which the particle is considered unstable, where

$$d_r = \log_{10} \left( \frac{\Delta\nu_x^2 + \Delta\nu_y^2}{N} \right), \quad (9)$$

where  $N$  is the number of turns tracked to determine each tune (equal to half of **n\_passes**).

- **immediate** — If nonzero, the calculations take place immediately. If zero, then two modes are possible
  - If you wish to compute parameters on a closed orbit or after other calculations, be sure to set this control to zero and ask for an output file with **xy\_output** or **delta\_output**.
  - If you want to use this command to create quantities for optimization (see below), be sure to set this control to zero and *do not* ask for an output file with **xy\_output** or **delta\_output**.
- **filtered\_output** — If nonzero, output is only provided for particles inside the stable footprint.
- **ignore\_half\_integer** — If nonzero, half-integer resonances are ignored in determining the tune footprint.

This command makes available the following quantities for optimization. All quantities are limited by particle survival, crossing of integer and half-integer resonances, and the diffusion rate limit.

- `FP.nuxSpreadChrom, FP.nuySpreadChrom` — Spread in tunes due to chromaticity.
- `FP.nuxChromMin`, `FP.nuxChromMax`, `FP.nuyChromMin`, `FP.nuyChromMax` — Minimum and maximum values of the x and y tunes from chromatic tune footprint.
- `FP.deltaLimit` — Minimum of absolute values of positive and negative  $\delta$  limits.
- `FP.nuxSpreadAmp`, `FP.nuySpreadAmp` — Spread in tunes due to amplitude.
- `FP.nuxAmpMin`, `FP.nuxAmpMax`, `FP.nuyAmpMin`, `FP.nuyAmpMax` — Minimum and maximum values of the x and y tunes from amplitude tune footprint.
- `FP.xSpread`, `FP.ySpread` — Spread in x and y values.
- `FP.xyArea` — Area of the limited x-y region, comparable to a dynamic acceptance. However, this area is determined from a fixed grid and is not suitable to optimization by itself.
- `FP.diffusionRateMaxChrom`, `FP.diffusionRateMaxAmp` — Maximum diffusion rates in chromatic and amplitude scans.

Typically, one strives to minimize `FP.nuxSpreadChrom`, `FP.nuySpreadChrom`, `FP.nuxSpreadAmp`, `FP.nuySpreadAmp`, `FP.diffusionRateMaxChrom`, and/or `FP.diffusionRateMaxAmp` while maximizing `FP.deltaLimit`, `FP.xSpread`, and/or `FP.ySpread`, and ensuring that `FP.xyArea`, at minimum, doesn't decrease. I.e., one wants the maximum stable region for momentum and position deviations with the minimum spread in tunes and minimum diffusion.



## twiss\_analysis

### 7.65 twiss\_analysis

- type: setup command.
- function: analyze Twiss parameters within a user-defined region for purposes of optimization.
- sequence: must precede `twiss_output`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

`&twiss_analysis`

```
    STRING match_name = NULL;  
    STRING start_name = NULL;  
    STRING end_name = NULL;  
    double s_start = -1;  
    double s_end = -1;  
    STRING tag = NULL;  
    long verbosity = 0;  
    long clear = 0;
```

`&end`

- `match_name` — Optional wildcard string to match to element names for selection of elements to include in the analysis.
- `start_name` — Name of the element at which to start analysis. If the element occurs more than once, the first occurrence is used.
- `end_name` — Name of the element at which to end analysis. If the element occurs more than once, the first occurrence is used.
- `s_start` — Position (in meters) at which to start analysis.
- `s_end` — Position (in meters) at which to end analysis.
- `tag` — Name prefix for quantities computed by the analysis. The quantity names will have the form *tag.statistic.quantity*, where *statistic* is one of `min`, `max`, and `ave`, and *quantity* is one of `betax`, `betay`, `etax`, `etay`, `alphax`, `alphay`, `etaxp`, and `etayp`. E.g., if *tag* is `region1`, then one could use expressions like `region1.max.betax` in optimization.
- `clear` — If nonzero, all previously defined analysis regions are deleted.

## twiss\_output

### 7.66 twiss\_output

- type: action/setup command.
- function: compute and output uncoupled Twiss parameters, or set up to do so.
- sequence: must follow `run_setup`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- N.B.: the output of this command is strictly correct only when the beamline has vanishingly small x-y coupling. For rings, use of `coupled_twiss_output` is an option when that requirement is not sufficiently well satisfied.

```
&twiss_output
  STRING filename = NULL;
  long matched = 1;
  long output_at_each_step = 0;
  long output_before_tune_correction = 0;
  long final_values_only = 0;
  long statistics = 0;
  long radiation_integrals = 0;
  long concat_order = 3;
  long higher_order_chromaticity = 0;
  long higher_order_chromaticity_points = 5;
  double higher_order_chromaticity_range = 4e-4;
  double chromatic_tune_spread_half_range = 0;
  long quick_higher_order_chromaticity = 0;
  double beta_x = 1;
  double alpha_x = 0;
  double eta_x = 0;
  double etap_x = 0;
  double beta_y = 1;
  double alpha_y = 0;
  double eta_y = 0;
  double etap_y = 0;
  STRING reference_file = NULL;
  STRING reference_element = NULL;
  long reference_element_occurrence = 0;
  long reflect_reference_values = 0;
  long cavities_are_drifts_if_matched = 1;
  long compute_driving_terms = 0;
  long leading_order_driving_terms_only = 0;
  STRING s_dependent_driving_terms_file = NULL;
  long local_dispersion = 1;
&end
```

- `filename` — The (incomplete) name of an SDDS file to which the Twiss parameters will be written. Recommended value: “%s.twi”.

- **matched** — A flag indicating, if set, that the periodic or matched Twiss parameters should be found. If zero, calculations are performed in transport line mode starting from the given initial values of **betax**, **alphax**, etc. N.B.: This may give different values for the chromaticity even if the initial values are identical to those for a periodic solution. The reason has to do with different assumptions about the initial conditions for particles in a transport line vs a ring.
- **output\_at\_each\_step** — A flag indicating, if set, that output is desired at each step of the simulation. If you wish to compute Twiss parameters on a closed orbit or after other calculations, be sure to set this control to a nonzero value.
- **output\_before\_tune\_correction** — A flag indicating, if set, that output is desired both before and after tune correction.
- **final\_values\_only** — A flag indicating, if set, that only the final values of the Twiss parameters should be output, and not the parameters as a function of  $s$ .
- **statistics** — A flag indicating, if set, that minimum, maximum, and average values of Twiss parameters should be computed and included in output.
- **radiation\_integrals** — A flag indicating, if set, that radiation integrals should be computed and included in output. *N.B.: Radiation integral computation is not correct for systems with vertical bending, nor does it take into account coupling. See the **moments\_output** command if you need such computations.*
- **beta\_X, alpha\_X, eta\_X, etap\_X** — If **matched** is zero, the initial values for the X plane.
- **concat\_order** — Order of matrix concatenation to use for determining matrix for computation of Twiss parameters. Using a lower order will result in inaccuracy for nonlinear lattices with orbits and/or momentum errors. However, for on-momentum conditions with zero orbit, it is much faster to use **concat\_order=1**.
- **higher\_order\_chromaticity** — If nonzero, requests computation of the second- and third-order chromaticity. To obtain reliable values, the user should use **concat\_order=3** in this namelist and the highest available order for all beamline elements. **elegant** computes the higher-order chromaticity by finding the trace of off-momentum matrices obtained by concatenation of the matrix for **higher\_order\_chromaticity\_points** values of  $\delta$  over the full range **higher\_order\_chromaticity\_range**. If **quick\_higher\_order\_chromaticity** is nonzero, then a quicker concatenation method is used that gives the second-order chromaticity only.
- **chromatic\_tune\_spread\_half\_range** — Half range of  $\delta$  for which the chromatic tune spread is computed. The results are available in for optimization and in the twiss output file under the names **nuxChromUpper**, **nuxChromLower**, and similarly for the y plane. This computation uses the chromaticities.
- **reference\_file** — If given, the name of a file from which twiss parameter data will be taken to give the starting values. Ignored if **matched** is nonzero. The file should have the beta and alpha functions with the same names as the file created by this command.
- **reference\_element** — Element in **reference\_file** at which to take the twiss parameter values. If not given, the values at the last element in **reference\_file** are used.

- **reference\_element\_occurrence** — Ignored if **reference\_element** is not given. Otherwise, the occurrence number of **reference\_element** to use. If 0, the last occurrence is used.
- **reflect\_reference\_values** — If nonzero, reference values of  $\alpha_{x,y}$  and  $\eta'_{x,y}$  are multiplied by -1. This permits matching backwards from the reference point.
- **cavities\_are\_drifts\_if\_matched** — By default, if **matched**=1, **elegant** treats rf cavities as drift spaces, allowing the user to have a cavity in the ring definition without it affecting the lattice functions. By setting **cavities\_are\_drifts\_if\_matched**=0, one can force **elegant** to use the actual matrix for the rf cavity. The differences between the results are generally small, but the default behavior disagrees with the results of **moments\_output**. This feature is not available for cavities that change the beam energy (**CHANGE\_P0**=1 in element definition or **always\_change\_p0**=1 on **run\_setup**).
- **compute\_driving\_terms** — If nonzero, then resonance driving terms [29, 36, 37] and tune shifts with amplitude are computed by summing over dipole, quadrupole, sextupole, and octupole elements. For dipoles, only the effects of gradients and sextupole terms are included; curvature effects are not present in the theory. In addition, these quantities may be optimized by using those names in optimization terms (see list below).
- **leading\_order\_driving\_terms\_only** — If nonzero, only the leading order driving terms are computed. I.e., terms involving double sums over sextupole and quadrupole strengths are not computed. However, leading-order octupole terms are computed, even though they affect the same terms as the second-order sextupole and quadrupole terms. This option is provided because computing the higher-order terms is time-consuming and not always worthwhile.
- **s\_dependent\_driving\_terms\_file** — The (incomplete) name of a SDDS file to which magnitude, real and imaginary parts of s-dependent driving terms will be written. If you wish to compute s-dependent driving terms, be sure to set this parameter. The following first order resonant driving terms are implemented as defined in [42]: **f10010**, **f10100**, **f30000**, **f12000**, **f10200**, **f01200**, **f01110**, **f00300**, **f00120**, **f20100**, **f20010** and **f11010**. Please note that the notation and meaning of the driving terms differs from those computed when **compute\_driving\_terms**=1!
- **local\_dispersion** — Normally, **elegant** will ignore acceleration in computing the dispersion. That is, the dispersion would be the “local” dispersion  $\frac{\partial x}{\partial \delta}$ , where  $\delta$  was the local fractional momentum deviation. In a linear system, the local dispersion is related to the beam moments by  $\eta_x = \langle x\delta \rangle / \langle \delta^2 \rangle$ . In a linac or other systems with rf elements, one might also be interested in the “global” dispersion  $\frac{\partial x}{\partial \delta_0}$ , where  $\delta_0$  is the energy deviation at the beginning of the system. In this case, set **local\_dispersion**=0. Alternatively, one may look at the  $R_{i6}$  elements of the matrix from **matrix\_output**.

The output file from this command contains the following columns, giving values of quantities at the exit of each element, unless otherwise noted.

- **s** — The arc length.
- **ElementName** — The name of the element.
- **ElementType** — The type name of the element.
- **betax** and **betay** — The horizontal and vertical beta functions.

- **alphax** and **alphay** — The horizontal and vertical alpha functions, where  $\alpha = -\frac{d\beta}{2ds}$ .
- **psix** and **psiy** — The horizontal and vertical betatron phase advance in radians.
- **etax** and **etay** — The horizontal and vertical dispersion functions.
- **etaxp** and **etayp** — The slopes of the horizontal and vertical dispersion functions.
- **xAperture** and **yAperture** — The horizontal and vertical apertures. If undefined, will have a value of 10m. If the beam trajectory is non-zero, then the aperture will be changed (usually reduced) accordingly. Hence, these are best understood as the **effective** apertures. They are used in determining the horizontal and vertical acceptance parameters, **Ax** and **Ay**.
- **pCentral0** — The central momentum ( $\beta\gamma$ ) at the **entrance** to the element.
- **dIn** — Contribution to radiation integral  $In$ . Radiation integrals take account of horizontal bending only.

The output file contains the following parameters. Note that chromatic quantities depend on the order settings of the individual elements, the default order (in **run\_setup**), and the concatenation order given in the **twiss\_output** command. These quantities pertain to the end of the lattice or to the lattice as a whole.

- **nux** and **nuy** — The horizontal and vertical tunes.
- **dnux/dp** and **dnuy/dp** — The horizontal and vertical chromaticities, defined as  $d\nu/d\delta$ .
- **dnux/dp2** and **dnuy/dp2** — The horizontal and vertical 2nd-order chromaticities, defined as  $d^2\nu/d\delta^2$ . Will be zero if **higher\_order\_chromaticity** is zero.
- **dnux/dp3** and **dnuy/dp3** — The horizontal and vertical 3rd-order chromaticities, defined as  $d^3\nu/d\delta^3$ . Will be zero if **higher\_order\_chromaticity** is zero.
- **dbetax/dp** and **dbetay/dp** — Chromatic derivatives of the horizontal and vertical beta functions, defined as  $\frac{d\beta}{d\delta}$ .
- **dalphax/dp** and **dalphay/dp** — Chromatic derivatives of the horizontal and vertical alpha functions, defined as  $\frac{d\alpha}{d\delta}$ .
- **etax2**, **etax3**, **etay2**, **etay3** — Higher order dispersion in the horizontal and vertical planes. For example, for the horizontal plane, the closed orbit at the end of the lattice depends on  $\delta$  according to  $x = \eta_x\delta + \eta_{x2}\delta^2 + \eta_{x3}\delta^3$ . This differs from the chromaticity expansion, which is given in terms of successive derivatives of  $\nu(\delta)$ .
- **dnux/dAx**, **dnux/dAy**, **dnuy/dAx**, **dnuy/dAy** — Tune shifts with amplitude, where amplitude is defined as  $A_q = (1 + \alpha_q)q^2/\beta_q$ , with  $q = x$  or  $q = y$ . These will be zero unless the **tune\_shift\_with\_amplitude** command is given.
- **h11001**, **h00111**, **h20001**, **h00201**, **h10002**, **h21000**, **h30000**, **h10110**, **h10020**, **h10200**, **h22000**, **h11110**, **h00220**, **h31000**, **h40000**, **h20110**, **h11200**, **h20020**, **h20200**, **h00310**, **h00400** — Resonance driving terms[29]. These will be zero unless **compute\_driving\_terms** is nonzero. See table 2 for an explanation of each term.

- `dnux/dJx`, `dnux/dJy`, and `dnuy/dJy` — Tune shifts with amplitude from Bengtsson’s theory [29]. See documentation for `tune_shift_with_amplitude` for discussion and comparison with `dnux/dAx` etc. These will be zero unless `compute_driving_terms` is nonzero.
- `Ax` and `Ay` — The horizontal and vertical acceptance. These will be zero if no apertures are defined.
- `alphac`, `alphac2` — First- and second-order momentum compaction. The path length is  $s = s_o + \alpha_c L \delta + \alpha_{c2} L \delta^2$ .
- `couplingIntegral`, `couplingDelta`, and `emittanceRatio` — These quantities are defined in section 3.1.4.4 of [19]. The computations include tilted quadrupoles, vertical orbit in sextupoles, vertical sextupole displacement, and solenoids. Note that the emittance ratio *does not* include the effect of vertical dispersion.
- `In` — The  $n^{\text{th}}$  radiation integral.
- `taux`, `tauy`, `taudelta` — Radiation damping times for x, y, and  $\delta$ .
- `Jx`, `Jy`, `Jdelta` — Damping partition factors for x, y, and  $\delta$ .
- `ex0`, `enx0` — Horizontal equilibrium geometric and normalized emittances.
- `Sdelta0` — Equilibrium fractional rms energy spread.
- `U0` — Energy loss per turn.

N.B.: the higher-order dispersion and higher-order chromaticity are computed using the concatenated third-order matrix. However, `elegant` only has third-order matrices for three elements: alpha magnets, quadrupoles, and sextupoles. This may be acceptable if any dipoles (for example) have large bending radius. Users who are concerned about these effects should perform off-energy tracking using canonical elements (i.e., `CSBEND`, `KQUAD`, `KSEXT`, and `MULT`), which include energy dependence to all orders.

Also, note that by default all elements are computed to second order only. You must change the `default\_order` parameter on `run\_setup` to 3 in order to use the third-order matrices for alpha magnets, quadrupoles, and sextupoles. You may also use the `ORDER` parameter on individual element definitions.

Table 2: Meaning of the various driving terms[29].

| Term Name | Explanation                                  |
|-----------|--|
| h11001    | drives x chromaticity                        |
| h00111    | drives y chromaticity                        |
| h20001    | drives synchro-betatron resonances           |
| h00201    | drives momentum-dependence of beta functions |
| h10002    | drives second order dispersion               |
| h21000    | drives $\nu_x$                               |
| h30000    | drives $3\nu_x$                              |
| h10110    | drives $\nu_x$                               |
| h10020    | drives $\nu_x - 2\nu_y$                      |
| h10200    | drives $\nu_x + 2\nu_y$                      |
| h22000    | drives $d\nu_x/dJ_x$                         |
| h11110    | drives $d\nu_x/dJ_y$                         |
| h00220    | drives $d\nu_y/dJ_y$                         |
| h31000    | drives $2\nu_x$                              |
| h40000    | drives $4\nu_x$                              |
| h20110    | drives $2\nu_x$                              |
| h11200    | drives $2\nu_y$                              |
| h20020    | drives $2\nu_x - 2\nu_y$                     |
| h20200    | drives $2\nu_x + 2\nu_y$                     |
| h00310    | drives $2\nu_y$                              |
| h00400    | drives $4\nu_y$                              |

## track

### 7.67 track

- type: major action command.
- function: track particles.
- sequence: must follow `run_setup`, `run_control`, and beam definition with `bunched_beam` or `sdds_beam`.
- can use parallel resources (Pelegant)
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

&track

```

long center_on_orbit = 0;
long center_momentum_also = 1;
long offset_by_orbit = 0;
long offset_momentum_also = 1;
long soft_failure = 1;
long stop_tracking_particle_limit = -1;
```

```

    long check_beam_structure = 0;
    STRING interrupt_file = "%s.interrupt";
&end

```

- **center\_on\_orbit** — A flag indicating whether to center the beam transverse coordinates on the closed orbit before tracking.
- **center\_momentum\_also** — A flag indicating whether to center the momentum coordinate also.
- **offset\_by\_orbit** — A flag indicating whether to offset the transverse beam coordinates by the closed orbit before tracking. Similar to **center\_on\_orbit**, but the initial centroids of the beam are preserved. The beam is simply displaced by the closed orbit rather than being centered on it.
- **offset\_momentum\_also** — A flag indicating whether to also offset the beam momentum to the momentum of the closed orbit. If the **start\_from\_centroid** or **start\_from\_dp\_centroid** parameters are used on the **closed\_orbit** command, this flag should be set to 0; otherwise, one will offset the beam central momentum by its own value.
- **soft\_failure** — If there is an error during tracking (e.g., a failure of orbit correction), continue to produce file output. This creates essentially empty slots in the files corresponding to the failed steps.
- **stop\_tracking\_particle\_limit** — If a non-negative is given, then **elegant** will stop tracking when the number of particles falls below the given value. It will be as if all the particles were lost.
- **check\_beam\_structure** — For debugging use only.
- **interrupt\_file** — Gives the (possibly incomplete) name of a file to monitor as a semaphore to interrupt the tracking. If the file is created or updated during tracking, then tracking will terminate on completion of the next pass. Output already written to **WATCH** files is preserved, but unwritten data (e.g., buffered, but not written to disk) is lost.

There are also several deprecated parameters:

- **use\_linear\_chromatic\_matrix** — For each particle, a first-order matrix is computed for the particular momentum offset of the particle using the linear chromaticity and linear dependence of the beta functions on momentum. Use **ILMATRIX** elements instead.
- **longitudinal\_ring\_only** — Tracks longitudinal coordinates only for a ring. Use **ILMATRIX** elements instead.



## tune\_shift\_with\_amplitude

### 7.68 tune\_shift\_with\_amplitude

- N.B.: this command is deprecated, because it is too difficult to tune it to get reliable answers. The use of driving term computation in `twiss_output` is recommended instead, even though it doesn't include all possibly relevant effects. For tune-spread calculations, the `tune_footprint` command provides more versatility.
- type: setup command.
- function: prepare for computation of tune shifts with amplitude.
- sequence: must follow `twiss_output`.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.
- methods:

Method 1 : tune shifts with amplitude are computed via tracking a series of particles at different amplitudes or by a matrix method. NAFF is used to determine the tunes from the tracking data. It is the user's responsibility to optimize the parameters to ensure that results are reasonable.

Method 2 : tune shifts are computed using a concatenated multi-turn third-order matrix. This appears to be reliable for many cases we've tested.

Method 3 : tune shifts can be computed quickly using Bengtsson's formulae [29] by setting `compute_driving_term` in `twiss_output`. For cases where all methods are valid, the results will differ by a factor of 2 from the results obtained with this command. Also, the present command has more general validity because it includes dipole curvature effects.

The quantities computed are  $\frac{\partial}{\partial A_x^n \partial A_y^m} \nu_p$ , where  $n \geq 0$  and  $m \geq 0$  are integers and  $p$  is  $x$  or  $y$ .  
 $A_q = (1 + \alpha_q)q^2/\beta_q$ , with  $q = x$  or  $q = y$ .

```
&tune_shift_with_amplitude
long turns = 2048;
double x0 = 1e-6;
double y0 = 1e-6;
double x1 = 3e-4;
double y1 = 3e-4;
long grid_size = 6;
long lines_only = 0;
long sparse_grid = 0;
long spread_only = 0;
double nux_roi_width = 0.02;
double nuy_roi_width = 0.02;
double scale_down_factor = 2;
double scale_up_factor = 1.05;
double scale_down_limit = 0.01;
double scale_up_limit = 1e-4;
long scaling_iterations = 10;
```

```

    long use_concatenation = 0;
    long verbose = 0;
    long order = 2;
    STRING tune_output = NULL;
&end

```

- **turns** — The number of turns to track. If zero, then the concatenated matrix is used instead of tracking, and all other parameters of this command are irrelevant. The matrix method doesn't work well with all lattices. The order of the concatenated matrix is given by the `concat_order` control in `twiss_output`.
- **x0, y0** — The initial x and y amplitudes to use for determining the small-amplitude tunes.
- **x1, y1** — The initial x and y amplitudes to user for determining the tune shifts. These values should be small enough to ensure linearity in the tune shift.
- **grid\_size** — Size of the grid of points in x and y.
- **lines\_only** — If nonzero, then instead of a full set of `grid_size`<sup>2</sup> particles, only two lines of particles with  $x = 0$  and/or  $y = 0$  are tracked. In this case, no  $A_x^i * A_y^j$  terms are computed (except for  $i = 0$  or  $j = 0$ ). However, in addition to being faster, the results may be more reliable, e.g.,  $\partial\nu_x/\partial A_y = \partial\nu_y/\partial A_x$  may be more closely satisfied.
- **sparse\_grid** — If nonzero, then instead of a full set of `grid_size`<sup>2</sup> particles, a sparse grid of particles is tracked. Will save time at some expense in accuracy.
- **spread\_only** — Compute the tune spread only and don't bother with the tune shift coefficients. These tune spreads can be optimized and appear in the twiss output file under the names `nuxTswaLower`, `nuxTswaUpper`, and similarly for the y plane. This is the recommended way to reduce tune shift with amplitude, as the tune spread is more reliable than the coefficients of the expansion. (Particles that get lost are automatically ignored in both types of computations.)
- **nux\_roi\_width, nuy\_roi\_width** — Widths of the region of interest for x and y tunes. As the grid is filled in, `elegant` finds the tune for each tracked particle on the grid. Successive tune values are looked for in the region of the given width around the previous tune value. This prevents jumping from the main tune peak to another peak, which can happen when the tune spectrum has many lines.
- **scale\_down\_factor, scale\_up\_factor, scale\_down\_limit, scale\_up\_limit, scaling\_iterations** — These control automatic scaling of the amplitudes. If `elegant` sees a tune shift larger than `scale_down_limit` it will decrease `x0` (or `y0`) by the factor `scale_down_factor`. If `elegant` sees a tune shift smaller than `scale_up_limit` it will increase `x0` (or `y0`) by the factor `scale_up_factor`. Suggestion: if you find yourself playing with these values and the initial amplitudes in order to get reliable TSWA coefficients, try just using the tune spread.
- **verbose** — If nonzero, information about the progress of the algorithm is printed to the screen.
- **use\_concatenation** — If nonzero, then tracks with the concatenated matrix instead of element-by-element. The order of the concatenated matrix is given by the `concat_order` control in `twiss_output`. The user should experiment with this option to see if the results are reliable for a particular lattice.

## vary\_element

### 7.69 vary\_element

- type: setup command.
- function: define an index and/or tie a parameter of an element to it.
- sequence: must follow `run_control`
- N.B.: It is not possible to vary an element if the element name starts with one of the following characters: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, ., +, or -. The reason is that `elegant` will attempt to make an SDDS parameter name containing the element name, and these characters are disallowed at the beginning of such a name.
- Command syntax, including use of equations and subcommands, is discussed in 7.2.

```
&vary_element
    long index_number = 0;
    long index_limit = 0;
    STRING name = NULL;
    STRING item = NULL;
    double initial = 0;
    double final = 0;
    long differential = 0;
    long multiplicative = 0;
    long geometric = 0;
    STRING enumeration_file = NULL;
    STRING enumeration_column = NULL;
&end
```

- `index_number` — A non-negative integer giving the number of the index.
- `index_limit` — A positive integer giving the number of values the index will take. Must be given if this `index_number` has not been listed in a previous `vary_element` command, unless `enumeration_file` is given.
- `name` — The name of an element.
- `item` — The parameter of the element to vary.
- `initial`, `final` — The initial and final values of the parameter.
- `enumeration_file` — Name of an SDDS file giving values for the item.
- `enumeration_column` — Column of the SDDS file giving the values.
- `differential` — If nonzero, the initial and final values are taken as offsets from the predefined value of the parameter.
- `multiplicative` — If nonzero, the initial and final values are taken as multipliers to be applied to the predefined value of the parameter in order to obtain the actual initial and final values.
- `geometric` — If nonzero, then variation is geometric rather than arithmetic.

## 8 Specialized Tools for Use with `elegant`

A number of specialized programs are available that work with `elegant`. Most are SDDS-compliant, so they will also work with any program that reads or writes appropriate SDDS data. The following is a brief description of each program. Full descriptions for many programs are available on subsequent pages. Most programs will return a help message if the program name is given with no arguments, which should be sufficient documentation and may be more up-to-date than these manual pages.

- **abrat** — A program to integrate particles through a 3D magnetic field map. The name stands for Asymmetric Bend RAY trace. This program uses the same method as the **BRAT** element in `elegant`.
- **analyzeMagnets** — Generates SDDS and latex files giving magnet parameters. (Program by M. Borland.)
- **astra2elegant** — Converts ASCII particle output from ASTRA [30] to a binary SDDS file suitable for use with `elegant`. This program is recommended over the `astra2sdds` program on the ASTRA website, because the latter produces ASCII SDDS files that are quite slow to read and does not perform the correct computations for low-energy beams. (Program by M. Borland.)
- **bremsstrahlungLifetime** — Computes gas bremsstrahlung lifetime from local momentum acceptance and Twiss parameter output, assuming a constant gas pressure. (Program by M. Borland.)
- **bremsstrahlungLifetimeDetailed** — Computes gas bremsstrahlung lifetime from local momentum acceptance and Twiss parameter output, using a user-supplied, s-dependent gas pressure. (Program by M. Borland.)
- **computeCoherentFraction** — Computes the coherent fraction for undulator radiation.
- **computeGeneralizedGradients** — Computes generalized gradients for use with the **BGGEXP** element.
- **computeSCTuneSpread** — Compute space charge tune spread.
- **coreEmittance** — Computes the slice emittance for the beam core (e.g., 80% of the beam). (Program by X. Dong.)
- **csrImpedance** — Computes the shielded steady-state CSR impedance for a dipole magnet. The output can be used immediately with `elegant`'s **ZLONGIT** element. (Program by Y. Wang, H. Shang, and M. Borland.) See also the `makeSummedCsrZ` script.
- **doubleDist6** — Increases the number of particles in a particle input file by successively doubling the number. Intended to be used to increase the number of particles produced by a photoinjector simulation to improve stability of CSR and LSC simulations. See also `smoothDist6`. (Program by M. Borland.)
- **elasticScatteringAnalysis** — Computes elastic gas scattering lifetime and loss distribution from multi-location tracking data, Twiss parameter output, and gas pressure distribution. Use with output of the `elastic_scattering` command in `Pelegant`. (Program by M. Borland.)

- **elasticScatteringLifetime** — Computes elastic gas scattering lifetime from single-location dynamic acceptance and Twiss parameter output, assuming a constant gas pressure. (Program by M. Borland.)
- **elasticScatteringLifetimeDetailed** — Computes elastic gas scattering lifetime from single-location dynamic acceptance and Twiss parameter output, using a user-supplied, s-dependent gas pressure. (Program by M. Borland.)
- **elegant2astra** — This program translates **elegant** phase space files into ASTRA [30] format. (Program by M. Borland.)
- **elegant2track** — This program translates **elegant** phase space files into TRACK [32] format. The ASCII version of TRACK is assumed. (Program by M. Borland.)
- **elegant2genesis** — This program performs slice analysis of particle output files, which are suitable for use with the SDDS-compliant APS version of GENESIS[14]. This program is part of the SDDS toolkit. See the SDDS toolkit manual for documentation. (Program by R. Soliday and M. Borland.)
- **elegantto** — Translates an **elegant**-style lattice file (or a MAD file, with some restrictions) into formats accepted by other programs, such as COSY, PARMELA, PATPET, PATRICIA, TRANSPORT, XORBIT, and MAD8. Will also generate an SDDS file containing lattice data. (Program by M. Borland.)
- **haissinski** — Computes the steady-state longitudinal distribution in an electron storage ring. Requires as input a file containing the Twiss parameters around the ring, such as that provided by the **twiss\_output** command. Wakes can be specified with either a L, R model, a BBR resonator model or a wake function. Other inputs are external rf system parameters, with possibility of a harmonic cavity. Output is a charge or current profile with longitudinal time coordinate (front of bunch is at positive times). (Program by L. Emery and M. Borland.)
- **ibsEmittance** — Computes local intra-beam scattering rates for both storage ring and linac. Also computes the equilibrium transverse and longitudinal emittances of a beam in an electron storage ring, resulting from the combination of quantum excitation, damping, and intra-beam scattering. Requires as input a file containing the Twiss parameters, such as that provided by the **twiss\_output** command. (Program by L. Emery, M. Borland, and A. Xiao)
- **impact2elegant** — Translates IMPACT-T [31] output into **elegant** conventions. (Program by M. Borland.)
- **impact2sdds** — Translates IMPACT-T output files into SDDS for easier postprocessing. (Program by M. Borland.)
- **ionTrapping** — Uses lattice function data from **elegant** to compute ion trapping condition in a ring. (Program by M. Borland.)
- **LFBFirSetup** — This script prepares data that can be used to configure turn-by-turn longitudinal feedback using TFBDRIVER and TFBPICKUP elements. (Program by M. Borland.)
- **longitCalcs** — Performs calculations of longitudinal dynamics parameters in storage rings, using output from **elegant**'s **twiss\_output** command. Can also compute voltages for bunch lengthening and output these to a file that can be use with **load\_parameters**. (Program by M. Borland.)

- **makeSummedCsrZ** — Computes the shielded or free-space steady-state CSR impedance for a ring composed of one or more types of dipole magnet. The output can be used immediately with **elegant**'s **ZLONGIT** element. (Program by M. Borland.)
- **plotTwiss** — Plots the twiss parameters using data from the **twiss\_output** command. (Program by L. Emery and M. Borland.)
- **plotTwissBeamsize** — Plots the beam sizes using data from the **twiss\_output** command.
- **prepareTAPAs** — Allows processing files from **twiss\_output** into a form that is accepted by the Android App TAPAs [46]. The resultant files can be copied to, e.g., the downloads area on the Android device, from which they can be read by TAPAs for configuration of the Storage Ring Scaling activity. (Program by M. Borland.)
- **radiationEnvelope** — A tool for use with the output of **sddsbrightness** and **sddsfluxcurve**. It analyzes data for many harmonics and produces a single curve that shows the envelope of maximum brightness or flux over all harmonics. (Program by M. Borland.)
- **removeBackDrifts** — Allows post-processing s-dependent files to remove negative drifts, which improves the appearance of plots and is needed for certain types of analysis. (Program by M. Borland.)
- **sddsanalyzebeam** — Analyzes a beam of macro-particles and produces an SDDS file containing beam moments, emittances, equivalent beta functions, etc. The beam file is of the type written by **elegant** using the **output** field of the **run\_setup** command, or the **WATCH** element. (Program by M. Borland.)
- **sddsbrightness** — Uses twiss parameter output or data from **sddsanalyzebeam** to compute undulator brightness curves. (Program by H. Shang, R. Dejus, M. Borland, X. Jiao.)
- **sddsbs** — Computes bending magnet spectra. (Program by H. Shang and M. Borland.)
- **sdds bunchingfactor** — Computes bunching factor vs frequency from phase space data. (Program by M. Borland.)
- **sddsemitproc** — Analyzes quadrupole scan emittance measurement data. Accepts a file containing the transport matrix for each point and measured beam sizes. The file may, for example, be the file produced by the **final** field of the **run\_setup** command. The quadrupole scan can be executed inside of **elegant** using **vary\_elements**. (Program by M. Borland.)
- **sdds4x4sigmaproc** — Analyzes quadrupole scan beam moment measurement data to determine the initial 4x4 sigma matrix of the beam. Accepts a file containing the transport matrix for each point and measured beam sizes. The file may, for example, be the file produced by the **final** field of the **run\_setup** command. The quadrupole scan can be executed inside of **elegant** using **vary\_elements**. (Program by M. Borland.)
- **sdds5x5sigmaproc** — Analyzes quadrupole scan beam moment measurement data to determine the initial 5x5 sigma matrix of the beam. Accepts a file containing the transport matrix for each point and measured beam sizes. The file may, for example, be the file produced by the **final** field of the **run\_setup** command. The quadrupole scan can be executed inside of **elegant** using **vary\_elements**. To work, requires a horizontal bending magnet in the beamline and variation quadrupoles before and after the bending magnet. (Program by M. Borland.)

- **sddsfindresonances** — Uses output from frequency map analysis to find and identify resonance lines. (Program by H. Shang, M. Borland.)
- **sddsfluxcurve** — Uses twiss parameter output or data from **sddsanalyzebeam** to compute undulator flux tuning curves. (Program by M. Borland, H. Shang, R. Dejus.)
- **sddsmatchmoments** — Transforms a beam of macro-particles to match a given set of 6x6 beam moments, where the moments are stored in an output file from **moments\_output**.
- **sddsmatchtwiss** — Transforms a beam of macro-particles to match to given beta functions and dispersion. The beam file is of the type written by **elegant** using the **output** field of the **run\_setup** command, or the **WATCH** element. (Program by M. Borland.)
- **sddsws** — Computes wiggler spectra, using code from WS (by R. Dejus). (Program by H. Shang.)
- **sddsurgent** — Uses algorithms from the programs US (by R. Dejus) and URGENT (by R. Walker) for computation of undulator radiation properties, including power density and intensity distributions. (Program by H. Shang, R. Dejus, M. Borland, X. Jiao.)
- **sddsrandmult** — Simulates the effect of random mechanical errors in a quadrupole or sextupole, generating multipole error data that can be used with **elegant**'s **KQUAD** and **KSEXT** elements. (Program by M. Borland.)
- **sddssampledlist** — This program allows creating particle distributions from user-designed distribution functions. It is thus a more flexible alternative to **bunched\_beam**. This program is part of the SDDS toolkit. See the SDDS toolkit manual for documentation. (Program by M. Borland and H. Shang.)
- **smoothDist6s** — Increases the number of particles in an input particle distribution. At the same time, smooths the distribution and adds optional energy and density modulation. Intended to be used to increase the number of particles produced by a photoinjector simulation to improve stability of CSR and LSC simulations. Also useful in studying the growth rate for energy and density modulations. See also **doubleDist6**. (Program by M. Borland.)
- The script **spiffe2elegant** allows converting the output of the PIC code **spiffe** to the same form as output by **elegant**. Note that **elegant** will read **spiffe** output directly. This script just allows converting the data for use with related programs, such as **sddsanalyzebeam**. (Program by M. Borland.)
- **TFBFirSetup** — This script prepares data that can be used to configure turn-by-turn transverse feedback using **TFBDRIVER** and **TFBPICKUP** elements. (Program by M. Borland.)
- **touschekLifetime** — This program calculates Touschek lifetime using A. Piwinski's formula. Input files are generated from "twiss\_output" and "momentum\_aperture". (Program by A. Xiao and M. Borland.)
- **track2sdds** — Translates output files, including phase space files, from version 39 of TRACK (with ASCII output [32]) into SDDS. (Program by M. Borland.)
- **track2mag** — Uses TRACK output files to create a file similar to the magnets output file from **elegant**. This gives a profile of the beamline that can be plotted with other data. (Program by M. Borland.)

- The scripts `makeSkewResponseCP` and `correctCoupling` can be used to compute the cross-plane response matrices for skew quadrupoles and to perform coupling correction using those matrices. (Program by M. Borland.)
- `view3dGeometry` — Uses `freewrl` viewer to display 3D geometry of a lattice. (Program by A. Petrenko and M. Borland.)



## abrat

### 8.1 abrat

- **description:** Integrates particle trajectories through an symmetric or asymmetric bending magnet. The name stands for "Asymmetric Bend RAY Tracing." Features include the ability to optimize the magnet strength and position to ensure, if possible, that the magnet joins two user-defined trajectories. The results of these optimizations can be used in *elegant* with the BRAT element.

- **synopsis:**

```
abrat field-file [-3dFieldFile]
[-interpolateField=parameterName,[,order=n][,extrapolate][,permissive]]
[-scan=x | xp | y | yp | delta,lower,upper,number | -beamFiles=input,output
] -vertex=x-in-meters,z-in-meters -nominalEntrance=x,y -nominalExit=x,y
-theta=targetInDegrees -rigidity=Tesla-meters [-output=filename]
[-fsc=value] [-dxDipole=m] [-dzDipole=m] [-yawDipole=value]
[-optimize=[verbose][fse,dx,dz,yaw]] -fseLimit=min,max -dxLimit=min,max
-dzLimit=min,max -yawLimit=min,max
[-fieldmapOutput=filename,zmin,zmax,nz,xmin,xmax,nx]
[-tolerance=integration-tolerance] [-quiet]
```

- **files:**

- *field-file* — Field map file. Normally, needs to contain columns *x*, *z*, and *B*, giving the field in the midplane. In 3D mode, when the `-3dFieldFile` option is given, then the file should contain *x*, *y*, *z*, *Bx*, *By*, and *Bz*. In all cases, the beam is assumed to move from left ( $z < 0$ ) to right ( $z > 0$ ) with the field bending counter clockwise. Positive *x* is away from the center of curvature.

- **switches:**

- `-3dFieldFile` — If given, then *field-file* is expected to contain a 3D field map. See above for details.
- `-interpolate` — If given, then *field-file* is expected to contain at least two 2D field maps on separate pages of the file. These field maps could be, for example, from measurements with different excitation currents, with the excitation current for each case being stored in a named parameter; the pages must be arranged so that the parameter values increase monotonically. *abrat* will then automatically interpolate among the field maps to determine the required excitation current (for example); this overrides the `fse` parameter of the `-optimize` option. By default, linear interpolation is used (`order=1`). By default, the search will not go outside the range of the parameter values in the data; if `extrapolate` is given, however, extrapolation outside this range is performed. By default, the grid parameters of the several pages must match exactly; if `permissive` is given, however, this requirement is not enforced.
- `-scan` — If given, then the value of the named accelerator coordinate is scanned to create a bundle of incoming rays. Output is provided for each ray.

- **-beamFiles** — If given, then an **elegant**-style beam is read and the particles therein are tracked through the dipole. A similar file is created for the output coordinates. Coordinates are defined at the nominal entrance and exit planes. Back-drifts are used to ensure that integration begins and ends outside the magnetic field region (i.e., all of the defined field is included).
- **-output** — If given, particle trajectories are written to the named file.
- **-fsc** — If given, the fractional strength change to apply to the field. Typically taken from a previous optimization run.
- **-dxDipole** — If given, the x positional change to apply to the field. A positive value moves the field away from the center of curvature. Typically taken from a previous optimization run.
- **-dzDipole** — If given, the z positional change to apply to the field. A positive value moves the field further from the incoming beam. Typically taken from a previous optimization run.
- **-yawDipole** — If given, the yaw to apply to the field. A positive value rotates the magnet in the direction of bending. Typically taken from a previous optimization run.
- **-optimize, -fseLimit, dxLimit, dzLimit, yawLimit** — Invokes optimization of the various strength and alignment parameters and specifies the allow range of variation.
- **-fieldMapOutput** — Requests output of a field map, allowing confirmation of the input data.
- **-tolerance** — Integration tolerance.
- N.B.: The usage message describes additional switches that have had limited testing. Use with caution.

- **authors:** M. Borland (ANL/APS).

## astra2elegant

### 8.2 astra2elegant

- **description:** Converts ASCII particle output from ASTRA to a binary SDDS file suitable for use with **elegant**. This program is recommended over the `astra2sdds` program on the ASTRA website, because the latter produces ASCII SDDS files that are quite slow to read.

- **synopsis:**

```
astra2elegant [inputFile] [outputFile] [-centerReference]
[-pipe=[input][,output]]
```

- **files:**

- `inputFile` — ASCII particle output file from ASTRA.
- `outputFile` — SDDS file containing phase space data. May be used directly with **elegant**.

- **switches:**

- `-centerReference` — Normally, **astra2elegant** offsets the arrival time of all particles by the arrival time of the reference particle. This behavior can be suppressed by giving the `-centerReference` option. In that case, the arrival time of the reference particle is defined as 0.
- `-pipe[=input][,output]` — Standard SDDS toolkit pipe option.

- **authors:** M. Borland (ANL/APS).

## computeGeneralizedGradients

### 8.3 computeGeneralizedGradients

- **description:** Converts data of the form  $B_\rho(z, \phi)$  into a set of generalized gradients [50] for use with `elegant`'s `BGGEXP` element.

- **synopsis:**

```
computeGeneralizedGradients -input filename -output rootname -mainHarmonic  
integer -nHarmonics integer [-allHarmonics 1]
```

- **switches:**

- **input** — Give the name of the input file, which must be an SDDS file having two columns and two parameters. The columns are **phi** and **Br**, giving respectively the polar angle in radians and the radial magnetic field in Tesla. Each page should have the same number of rows  $n$ . The **phi** values are assumed to be equispaced starting at 0 and ending at  $2\pi(1 - 1/n)$ . The pages are labeled by the parameter **z**, which gives the longitudinal coordinate in meters for the data on that page. These **z** values are assumed to be equispaced and to cover the entire length of the magnet, starting and ending well outside the magnet. (For periodic systems, the `onePeriod` option may be appropriate. See below.) Finally, a parameter **R** must exist that gives the radius in meters for the **Br** values.
- **output** — Give the root name for the output files. The main output file, which has extension **ggrad** and is used directly with the `BGGEXP` element, will contain the generalized gradients for the normal (non-skew) components of the magnetic field. Each page corresponds to a different harmonic.
- **mainHarmonic** — The main harmonic of the field, where 2 is quadrupole, 3 is sextupole, etc. For fields with several designed-in harmonics, use the lowest, and see the entry for **allHarmonics**.
- **nHarmonics** — The number of harmonics to include.
- **allHarmonics** — Normally, only allowed harmonics of the main harmonic are included. However, if the magnet has several main harmonics (e.g., a combined-function quadrupole and sextupole), this may be inappropriate. In that case, use this option to force use of all harmonics greater than the given main harmonic.

- **authors:** M. Borland, R. Lindberg (ANL/APS).

## coreEmittance

### 8.4 coreEmittance

- **description:** Computes the slice emittance for 80%, 85%, 90%, 95%, and 100% fractions of the beam.

- **synopsis:**

```
coreEmittance -input inputFilename [-nSlices numberOfSlices] [-pngRoot  
<string>] [-pngThickness <integer>(2)]
```

- **files:**

- The input file is a particle output file from **elegant** or a compatible program.

- **switches**

- **-input** — Specify the name of the input file.
- **-nSlices** — Optionally specify the number of longitudinal slices. The default is 100.
- **-pngRoot** — Optionally specify the file rootname for PNG graphics files. If omitted, no PNG files are created.
- **-pngThickness** — Optionally change the thickness of lines for PNG graphics. The default is 2.

- **author:** X. Dong.

## csrImpedance

### 8.5 csrImpedance

- **description:** Computes the steady-state CSR impedance with shielding by parallel plates. By default, the computed impedance is for a dipole magnet that bends the beam in a complete circle.

- **synopsis:**

```
csrImpedance outputFile | -pipe[=out] -height=valueInMeters  
-radius=valueInMeters -frequencyLimit=maximum=valueInHz[,minimum=valueInHz]  
-n=integer [-filter=cutoff1,cutoff2] [-angle=radians]
```

- **files:**

- *outputFile* — SDDS file containing computed impedance. May be used directly with *elegant*’s ZLONGIT element.

- **switches:**

- *-height* — The full height of the vacuum chamber, in meters.
- *-radius* — The radius of the bending magnet, in meters.
- *-angle* — The angle of the bending magnet, in radians. The default is  $2\pi$ .
- *frequencyLimit* — Allows specifying the upper frequency limit (required), as well as the lower frequency limit, for the computed impedance. *elegant* will not accept the data if the lower limit is not 0. If the rms bunch length is  $\sigma_t$ , then it is suggested to have the maximum frequency much greater than  $1/(2\pi\sigma_t)$ .
- *-n* — Allows specifying the number of data points to be computed. The number of points computed is  $2^n + 1$ , which is required by *elegant*. A reasonable value is  $n = 10$  to  $n = 14$ .
- *-filter* — Allows specifying the starting and ending frequency for a simple low-pass filter. The frequencies are given as fractions of the maximum frequency. The filter ramps linearly from 1 to 0 between the two cutoff values. If, for example, the cutoff is 0.2, then the highest frequency in the impedance corresponds to a wavelength of 10 bins ( $2/0.2$ ) in *elegant*.

- **authors:** Y. Wang, H. Shang, ANL/APS. Based on a simplified form[26] of Warnock’s [25] formula.
- **Note:** The script *makeSummedCsrZ* is more convenient for computing the CSR impedance of rings with several types of dipoles, and also handles the free-space case.

## doubleDist6

### 8.6 doubleDist6

- **description:** Increases the number of particles in a particle input file by successively doubling the number. Intended to be used to increase the number of particles produced by a photoinjector simulation to improve stability of CSR and LSC simulations.

The algorithm is as follows:

- For each doubling, insert a new particle “near” every pair of existing particles in time. The particle has a new  $t$  value, but the same  $(x, xp, y, yp, p)$  as one of the original particles.
- Bin the beam according to  $t$  into a large number of bins. Randomize the assignment of  $p$  values relative to other coordinates across particles in the same bin, while additionally adding a small random value to each  $p$  value.

- **synopsis:**

```
doubleDist6 -input name -output name -doublings number -nt bins
```

- **files:**

- **input** — A particle distribution file, such as might be used with `sdds_beam`.
- **output** — A particle distribution file, such as might be used with `sdds_beam`.

- **switches:**

- **-doublings  $n$**  — The number of times to double the size of the distribution. The number of particles in the output file is  $2^n$  times the number in the input file.
- **-nt *bins*** — The number of time bins to use for momentum randomization. This helps to avoid having many particles with exactly same momentum.

- **author:** M. Borland, ANL/APS.

- **see also:** `smoothDist6s`

## haissinski

### 8.7 haissinski

- **description:** haissinski solves the Haissinski equation for the bunch steady-state longitudinal distribution in the presence of various impedances.

- **synopsis:**

```
haissinski twissFile resultsFile
-wakeFunction=file,tColumn=name,wColumn=name |
-model=[L=Henry|Zn=Ohms],R=Ohm -charge=C | -particles=value |
-bunchCurrent=A -steps=numberOfChargeSteps -outputLastStepOnly
-RF=Voltage=V,harmonic=value[,phase=offsetInRadians] | -length=s
-harmonicCavity=Voltage=V,factor=harmonicFactor[,phase=radians]
-superPeriods=number -energy=GeV
-integrationParameters=deltaTime=s,points=number,startTime=s,
iterations=number,fraction=value,tolerance=value
```

- **files:**

- *twissFile* — Twiss output file from elegant, including radiation integral calculations.
- *resultsFile* — SDDS file containing computed bunch longitudinal distributions as columns, along with analysis and conditions as parameters.

- **switches:**

- -wakeFunction=*file*,tColumn=*name*,wColumn=*name* — Optionally specifies the impedance as a Greens function using values in an SDDS file. The time points must be equi-spaced.
- -model=[L=*Henry*|Zn=*Ohms*],R=*Ohm* — Optionally specifies the impedance as an inductor L or broad-band value Zn, along with a resistance R.
- -charge=*C* | -particles=*value* | -bunchCurrent=*A* — Various ways to specify the charge in each bunch.
- -steps=*numberOfChargeSteps* — Number of values of bunch charge to compute up to the value specified with on the just-described options. Using more values can help convergence, as the result of each prior step is used as the starting point for the new step.
- -outputLastStepOnly — Requests output for the last charge step (full charge) only.
- -RF=Voltage=*V*,harmonic=*value*[,phase=*offset*] | -length=*s* — Two ways to specify the nominal bunch length. The phase value is an offset from the synchronous phase, in radians, and is used only when a harmonic cavity is included.
- -harmonicCavity=Voltage=*V*,factor=*harmonicFactor*[,phase=*radians*] — Specifies a harmonic cavity voltage, phase, and the ratio of the harmonic cavity frequency to the main frequency.
- -superPeriods=*number* — Number of superperiods of the lattice specified in *twissfile* to simulate. If one has an N cell ring but only gives 1 cell in the input, this value should be N. If one gives the whole ring, this value should be 1.



- `-energy=GeV` — Beam energy. If not given, the value in the *twissfile* is used.
- `-integrationParameters=deltaTime=s,points=number,startTime=s,iterations=number,fraction=value,tolerance=value` — Integration parameters, which must be set. `deltaTime` is the time interval for wake function and charge density evaluation. `points` is the number of time points, while `startTime` is the time (relative to synchronous phase) at which the time region starts. These values must be set by the user based on knowledge of the likely bunch length. For the others, we suggest 1000 iterations, a fraction of 0.01, and a tolerance of  $10^{-4}$ .
- **authors:** L. Emery, M. Borland, ANL/APS.

## ibsEmittance

### 8.8 ibsEmittance

- **description:** `ibsEmittance` computes growth rates and equilibrium emittances for electron rings due to intrabeam scattering (IBS). It will also integrate the growth rates to show the time evolution of the emittances. The IBS algorithm is based on the Bjorken and Mtingwa's [15] formula, and with an extension of including vertical dispersion. The program can also estimate IBS growth rates for and transport line or linac beam, provided special attention paid to the beam's energy change (splitting RF cavities as needed).
- **examples:** This example computes the IBS equilibrium parameters and the contributions to the growth rates (at equilibrium) vs position in the APS lattice.

```
ibsEmittance aps.twi aps.ibs -charge=5 -coupling=0.02  
-rf=voltage=9,harmonic=1296
```

- **synopsis:**

```
ibsEmittance twissFile resultsFile -charge=nC|-particles=value  
-coupling=value|-emityInput=value [-emitInput=value] [-deltaInput=value]  
[-emit0=value] [-delta0=value] [-superperiods=value] [-isRing=1|0]  
-RF=Voltage=MV,harmonic=value|-length=mm [-energy=MeV] [-growthRatesOnly |  
-integrate=turns=number[,stepSize=number]] [-noWarning]
```

- **files:** *twissFile* is a twiss parameter file from the `twiss_output` command of `elegant`. You must use the `radiation_integrals` flag in `twiss_output`.

- **switches:**

- **-charge, -particles** — Give the charge (in nanocoulombs) or the number of electrons.
- **-coupling** — Give the emittance or “coupling” ratio,  $\epsilon_y/\epsilon_x$ .
- **-emityInput** — Give the initial vertical emittance in meters.
- **-emitInput** — Give the initial total emittance in meters. If not specified, the value from the parameter `ex0` in *twissFile* is used.
- **-deltaInput** — Give the initial rms fractional momentum spread. If not specified, the value from the parameter `Sdelta0` in *twissFile* is used.
- **-emit0, -delta0** — Redefine the equilibrium emittance and rms energy spread, if different from what is given in the twiss input file. Can be used, e.g., to include additional source of energy spread, such as microwave instability, from an external calculation.
- **-superperiods=value** — If given, the number of superperiods in the lattice. *twissFile* is taken to pertain to a single sector.
- **-isRing** — Specify the calculation is done for stored beam (`isRing=1`, default) or transport line/linac beam (`isRing=0`). When `isRing` is set to 0, the energy scaling and integration calculation will be disabled.
- **-RF=Voltage=MV,harmonic=value** — Specify rf voltage and harmonic number.
- **-length=mm** — Specify the rms bunch length.

- **-energy=MeV** — Specify the beam energy. By default, this is taken from the **pCentral** parameter in *twissFile*.
  - **-growthRatesOnly** — If given, only the initial growth rates are computed. Equilibrium emittance values are not computed. *resultsFile* will contain columns of initial growth rate contributions from individual elements. Without this option, *resultsFile* would normally contain columns of growth rate contributions at equilibrium.
  - **-integrate=turns=number[,stepSize=number]** — If given, then *resultsFile* contains the result of integrating the differential equations for the emittances for the given number of turns and not the contributions of individual elements of growth rates. The step size is the number of turns for each integration step, and can be adjusted to get faster results. The options **-growthRatesOnly** and **-integrate** are not compatible.
  - **-noWarning** — Removes warning messages.
- **author:** A. Xiao, L. Emery, M. Borland, ANL/APS.

## ionTrapping

### 8.9 ionTrapping

- **description:** Computes ion trapping conditions using `elegant` twiss parameter output as input.

- **synopsis:**

```
ionTrapping -twiss filename -superPeriods number -kappa ratio -output
filename -current mA -bunches number
```

- **switches:**

- **twiss** — Give the name of a Twiss output file from `elegant`. It is advisable to subdivide the elements finely enough to get smooth representations of the lattice functions. The file should be computed the radiation integrals turned on, since the natural emittance and energy spread are needed.
- **superPeriods** — Give the number of superperiods of the basic cell described by the Twiss output file.
- **kappa** — Give the ratio  $\epsilon_y/\epsilon_x$ . The emittances are computed from  $\epsilon_0$  using  $\epsilon_x = \frac{\epsilon_0}{1 + \frac{J_y}{J_x} \kappa}$  and  $\epsilon_y = \kappa \epsilon_x$ .
- **output** — Give the name of the output file. The file contains the information in the input file, with the following added elements, among others:
  - \* Column **Acrit** —  $A_{crit}(s)$  is defined as[49]

$$A_{crit}(s) = \frac{N_e r_p S_b}{2 \min(\sigma_x(s), \sigma_y(s)) (\sigma_x(s) + \sigma_y(s))}, \quad (10)$$

where  $N_e$  number of electrons per bunch,  $r_p$  is the classical proton radius,  $S_b$  is the bunch separation in meters,  $\sigma_x(s)$  is the local horizontal rms beam size, and  $\sigma_y(s)$  is the local vertical rms beam size. Any singly-ionized species with atomic mass greater than  $A_{crit}$  will be trapped.

- \* Parameters **ex, ey** — The horizontal and vertical emittances.
- \* Parameter **AcritMin** — Minimum value of  $A_{crit}(s)$ .
- \* Parameters **speciesTrappedFraction**, where *species* is H2, H2O, CH4, CO, and CO2. These give the fraction of the circumference over which H<sub>2</sub>, H<sub>2</sub>O, CH<sub>4</sub>, CO, and CO<sub>2</sub>, respectively, are trapped.
- **current** — Give the total beam current milliAmps.
- **bunches** — Give the number of bunches.
- **authors:** M. Borland (ANL/APS).

## elegantto

### 8.10 elegantto

- **description:** `elegantto` translates an `elegant`-style (or a MAD file, with some restrictions) into formats accepted by other programs, such as COSY, PARMELA, PATPET, PATRICIA, TRANSPORT, and XORBIT. Will also generate an SDDS file containing lattice data.
- **examples:** The following command would translate the `elegant` lattice file `lattice.lte` into a TRANSPORT lattice file with 10mm quadrupole aperture and 5mm sextupole aperture, at an energy of 1.5 GeV.

```
elegantto lattice.lte lattice.trin -transport=10,5,1.5
```

- **synopsis:**

```
elegantto inputfile outputfile {-patricia | -patpet |  
-transport[=quadAper(mm),sextAper(mm),p(GeV/c)] |  
-parmela[=quadAper(mm),sextAper(mm),p(GeV/c)] | -sdds[=p(GeV/c)] |  
-cosy=quadAper(mm),sextAper(mm),p(MeV/c) | -xorbit | -mad8 }  
[-angle_tolerance=value] [-flip_k_signs] [-magnets=filename]  
[-header=filename] [-ender=filename]
```

- **files:**

- *inputfile* — An `elegant`-style lattice file.
- *outputfile* — A file containing lattice data in the chosen format.

- **switches:**

- **-cosy** — Provide data for the program COSY INFINITY. This can take a little while as the program must figure out the Enge coefficients that correspond to the FINT and HGAP values for all the dipoles. The user should test the output carefully.
- **-mad8** — Provide data for the program MAD8.
- **-patricia** — Provide data for the program PATRICIA.
- **-patpet** — Provide data for the program PATPET, a merging of the programs PATRICIA and PETROS.
- **-transport[=*quadAper(mm)*,*sextAper(mm)*,*p(GeV/c)*]** — Provide data for the program TRANSPORT (original style). One may give apertures for the quadrupoles and sextupoles, as well as the beam momentum in GeV/c.
- **-parmela[=*quadAper(mm)*,*sextAper(mm)*,*p(GeV/c)*]** — Provide data for the program PARMELA. One may give apertures for the quadrupoles and sextupoles, as well as the beam momentum in GeV/c.
- **-sdds[=*p(GeV/c)*]** — Provide data in SDDS form. One may give the beam momentum in GeV/c.
- **-angle\_tolerance=*value*** — PATPET and PATRICIA only allow sector and rectangular bends. This tolerance, in radians, determines how far from sector or rectangular a bend definition may be and still get processed.

- **-flip\_k\_signs** — Changes the signs of all quadrupoles.
  - **-magnets=*filename*** — Results in output of an additional SDDS file with the magnet layout. This is the same file that would be generated by the **magnets** field of the **run\_setup** command in **elegant**.
  - **-header=*filename*, -ender=*filename*** — Allow specification of files to be prepended and appended to the lattice output. For example, if additional commands are required prior to the lattice definition to set up the run, they would be put in the **header** file. If additional commands are needed after the lattice definition to initiate processing, they would be put in the **ender** file.
- **author:** M. Borland, ANL/APS.

## sddsanalyzebeam

### 8.11 sddsanalyzebeam

- **description:** sddsanalyzebeam analyzes a beam of macro-particles and produces an SDDS file containing beam moments, emittances, equivalent beta functions, etc. The beam file is of the type written by **elegant** using the **output** field of the **run\_setup** command, or the **WATCH** element.

- **examples:**

```
sddsanalyzebeam run.out run.analysis
```

- **synopsis:**

```
sddsanalyzebeam [-pipe=[input][,output]] [inputfile] [outputfile]  
[-nowarnings] [-correctedOnly] [-canonical]
```

- **files:**

- *inputfile* — An SDDS file containing the columns **x**, **xp**, **y**, **yp**, **t**, and **p**, giving the six phase-space coordinates for a set of macroparticles. This file can be produced from **elegant**, for example, using the **output** field of the **run\_setup** command, the **bunch** field of the **bunched\_beam** command, or the **WATCH** element in coordinate mode.
- *outputfile* — An SDDS file containing columns giving moments, emittances, equivalent Twiss parameters, and so on, for the macro-particles. Each row of this file corresponds to a page of the input file. The names and meanings of the columns are identical to what is used for **elegant**’s **final** output file from the **run\_setup** command. The file from **elegant**, however, stores the results as parameters instead of columns; to convert *outputfile* to that convention, use the SDDS toolkit program **sddsexpand**.

- **switches:**

- **pipe** — The standard SDDS Toolkit pipe option.
- **nowarnings** — Suppresses warning messages.
- **correctedOnly** — If given, only the “corrected” twiss parameters and emittances are computed and output. The corrected twiss parameters have the dispersive component subtracted. Normally, these are computed but given names like **betacx**, **ecx**, etc. whereas the uncorrected values are **betax**, **ex**, etc. The corrected parameters are the correct ones to match a beamline to, since they have the dispersive and mono-energetic terms properly separated. The uncorrected values are more relevant if the dispersion is spurious (i.e., uncorrected or due to something like CSR that doesn’t admit of correction).
- **-canonical** — If given, all computations are performed using canonical momenta  $q_x = p_x/p_0 = x'(1 + \delta)/\sqrt{1 + x'^2 + y'^2}$  etc.

- **author:** M. Borland, ANL/APS.

## sddsbrightness

### 8.12 sddsbrightness

- **description:** sddsbrightness computes undulator brightness curves using Twiss parameter data from elegant or sddsanalyzebeam. Several calculation methods are available.

- **examples:**

```
sddsbrightness run.twi run.bri -harmonics=3
-Krange=start=0.2,end=2.2,points=100
-current=0.1 -totalLength=2.4 -periodLength=0.027 -coupling=0.01

sddsanalyzebeam run.out -pipe=out -correctedOnly
| sddsbrightness -pipe=in run.bri -harmonics=3
-Krange=start=0.2,end=2.2,points=100
-current=0.1 -totalLength=2.4 -periodLength=0.027 -coupling=0.01
```

- **synopsis:**

```
sddsbrightness [-pipe=[input][,output]] [twissFile] [SDDSoutputfile]
-harmonics=integer -Krange=start=value,end=value,points=integer
-current=Amps -totalLength=meters -periodLength=meters
[-emittanceRatio=value | -coupling=value] [-noSpectralBroadening]
[-method=string,device=string,neks=value]
```

- **files:**

- *twissFile* — A Twiss output file from elegant, with radiation integral calculations included, or an output from sddsanalyzebeam. In the latter case, the -correctedOnly option should be used.
- *SDDSoutputFile* — Contains the brightness data in column form. For each requested harmonic *i*, there are columns *photonEnergyi*, *wavelengthi*, and *Brightnessi*.

- **switches:**

- *pipe* — The standard SDDS Toolkit pipe option.
- *harmonics* — The number of harmonics to compute.
- *Krange=start=value,end=value,points=integer* — The range of the K parameter for the undulator and the number of points to compute on that range.
- *-current=Amps* — The current in amperes. If one gives the average current, one gets the average brightness.
- *-totalLength=meters* — The total length of the undulator, in meters.
- *-periodLength=meters* — The period length of the undulator, in meters.
- *-emittanceRatio=value | -coupling=value* — In the case of a twiss output file from elegant, which does not contain the vertical emittance, one must supply one of these options. If *-emittanceRatio=R* is given,  $\epsilon_y = \epsilon_0 * R$  and  $\epsilon_x = \epsilon_0$ ; this isn't how things work physically, but is provided for historical reasons. If *-coupling=k* is given,  $\epsilon_x =$



$\epsilon_0/(1 + Jy * k / Jx)$  and  $\epsilon_y = k * \epsilon_x$ .  $\epsilon_0$  is the equilibrium emittance from the twiss output of **elegant**.

In the case of twiss output from **sddsanalyzebeam**, both emittances are present and these options are ignored.

- **-method=string,device=string,neks=value** — Choose which method to use for brightness calculations. Options are
  - \* **borland** — M. Borland’s approximation method. Fast, but not as reliable as others.
  - \* **dejus** — R. Dejus’ non-zero emittance, infinite-N+convolution method. This is the default.
  - \* **walkerinfinite** — R. Walker’s method. Dejus’ method is derived from this method.
  - \* **walkerfinite** — R. Walker’s method using finite N without convolution. This is quite slow.

The **device** qualifier may be **planar** or **helical**. **neks** is used to change the number of points used for finding the peak of the distribution.

- **authors:** M. Borland, H. Shang, R. Dejus (ANL).

## sddsbunchingfactor

### 8.13 sddsbunchingfactor

- **description:** `sddsbunchingfactor` computes bunching factors for beams from `elegant`, e.g., from WATCH elements in coordinate mode or the `output` file from `run_setup`.

The bunching factor  $B(\omega)$  is defined as

$$B(\omega) = \frac{1}{N} \sqrt{\left( \sum_{i=1}^N \cos \omega t_i \right)^2 + \left( \sum_{i=1}^N \sin \omega t_i \right)^2}, \quad (11)$$

where  $\omega$  is the angular frequency and  $t_i$  is the time coordinate of the  $i^{th}$  of  $N$  particles.

- **examples:**

```
sddsbunchingfactor run.out run.bfac -omegaRange=1e9,1e12 -points=300
-mode=log
```

- **synopsis:**

```
sddsbunchingfactor [-pipe=[input][,output]] [SDDSinputfile]
[SDDSoutputfile>] [-omegaRange=lowerHz,upperHz] [-points=number]
[-mode={linear|logarithmic}] [-combinePages]
```

- **switches:**

- `pipe` — The standard SDDS Toolkit pipe option.
- `omegaRange` — Give the range of  $\omega$  values, in Hz.
- `points` — Give the number of points over the range of  $\omega$  values.
- `mode` — Choose linear or logarithmic spacing of  $\omega$  values.
- `combinePages` — Pages of the input file are combined, i.e., treated as a single bunch.

- **authors:** M. Borland (ANL).

## sddsemitproc

### 8.14 sddsemitproc

- **description:**

**sddsemitproc** analyzes quadrupole scan emittance measurement data. It accepts a file containing the transport matrix for each data point and measured beam sizes. Because **sddsemitproc** uses the matrix rather than a thin-lens model, it can analyze data from arbitrarily complex scans, involving, for example, multiple thick-lens quadrupoles.

The matrix data can be prepared using **elegant**. For example, the **vary\_element** command can be used to vary one or more quadrupoles. In addition, the beam size data may be prepared using **elegant**, to allow simulation of emittance measurements.

**sddsemitproc** will perform error analysis using a Monte Carlo technique. A user-specified number of random error sets are generated and added to all measurements. Analysis is performed for each error set. Statistics over all the error sets provide most likely values and error bars.

The beam parameters computed by **sddsemitproc** pertain to the beginning of whatever system is simulated in **elegant**.

- **examples:**

```
elegant quadScan.ele sddscollapse quadScan.fin -pipe=out
| sddsxref -pipe=in quadScan.data -take=SigmaX,SigmaY
| sddsemitproc -pipe=in emitResults.sdds
```

- **synopsis:**

```
sddsemitproc [inputfile] [outputfile] [-pipe=input][,output]]
[-sigmaData=xName,yName] [-variableName=columnName] [-errorData=xName,yName
| -errorLevel=valueInm,[{gaussian,nSigmas | uniform}]] [-nErrorSets=number]
[-seed=integer] [-limitMode=resolution | zero][,reject]
[-deviationLimit=xLevelm,yLevelm] [-resolution=xResolutionm,yResolutionm]
[-verbosity=level]
```

- **files:**

- *inputfile* — An SDDS file containing one or more pages with columns named  $R_{ij}$ , where  $ij$  is 11, 12, 33, and 34. These give elements of the horizontal and vertical transport matrices from the beginning of a system to the observation point. The sigma matrix inferred will be that for the beginning of the system. Typically, one starts with the **final** file from the **run\_setup** command in **elegant**, and collapses it using **sddscollapse**. Each page of *inputfile* corresponds to a different emittance measurement.

In addition to this data, *inputfile* must also contain columns giving the rms beam sizes in x and y. The user supplies the names of the columns using the **-sigmaData** option; otherwise, they default to **Sx** and **Sy**. These columns may be from **elegant** (e.g., **Sx** and **Sy**), if one wants to simulate an emittance measurement. Note that the theory behind the emittance measurement is strictly correct only for true RMS beamsizes measurements. Use of FWHM or some other measure will give unreliable results.

- *outputfile* — A file containing one page for each page of *inputfile*. The parameters of *outputfile* give the measured geometric rms emittance, sigma matrix, and Twiss parameters of the beam in the horizontal and vertical planes. If error sets were requested (using `-nErrorSets`), then there are also parameters giving the error bars (“sigma’s”) of the measured values.

- **switches:**

- `-variableName=columnName` — Supplies the name of a column in *inputFile* that will be copied into *outputFile* for use in plotting. Does not affect any results.
- `-sigmaData=xName,yName` — Supplies the names of the columns in *inputfile* from which the x and y rms beam sizes are to be taken. Default values are *Sx* and *Sy*, which are the data provided by *elegant*.
- `-errorLevel=valueInm,[gaussian,nSigmas | uniform]` — Supplies the standard deviation of random errors to be added to the measured beam sizes for Monte Carlo error analysis.
- `-errorData=xName,yName` — May be used to supply the names of columns in the input file that contain the error level for each measurement. This is an option instead of using `-errorLevel`, which allows varying the measurement error for each point.
- `-nErrorSets=number` — The number of sets of random errors to generate and add to the measurements. Each error set is used to perturb the original measurement data. The results are analyzed separately for each error set, then combined to give means and error bars.
- `-seed=integer` — Seed for the random number generator. Recommend a large, positive, odd integer less than  $2^{31}$ . If no seed is given or if the given seed is negative, then a seed is generated from the system clock.
- `-resolution=xResolutionm,yResolutionm` — The resolution of the beam size measurements, in meters. These values are subtracted in quadrature from the measured beam sizes to obtain the true beam sizes.
- `-limitMode=resolution | zero[,reject]` — If measured or perturbed beam sizes are less than the resolution or less than zero, then errors will result. One can use this option to limit minimum beam size values or reject points. In general, if one has to do this the measurement is probably bad.
- `-deviationLimit=xLevelm,yLevelm` — Specifies the maximum deviation, in meters, from the fit that data points may have and still be included. An initial fit is performed for each randomized set or the raw data, as appropriate. Outliers are then removed and the fit is repeated.
- `-verbosity=level` — Higher values of *level* result in more informational printouts as the program runs.

- **author:** M. Borland, ANL/APS.

## sddsfindresonances

### 8.15 sddsfindresonances

- **description:** sddsfindresonances scans frequency map analysis data and identifies resonances.

- **examples:**

```
sddsfindresonances run.fma run.res -multipoles=dipole,quad,sext,oct
-type=skew sddsfindresonances run.fma run.res -multipoles=sext,oct
-type=skew,norm
```

- **synopsis:**

```
sddsfindresonances [-pipe=[input],[output]] [inputFile] [outputfile]
-multipoles=[all=integer] | [dipole,] [quadrupole,] [sextupole,] [octupole,]
[-type=[normal,] [skew]] [-variables=firstColumn,secondColumn]
```

- **files:**

- *inputFile* — By default, frequency map analysis output file from `elegant`'s `frequency_map` command or equivalent, containing at minimum the columns `x`, `y`, `nux`, and `nuy`. Each page of the file is treated separately.
- *outputFile* — Contains the identified resonance lines, one resonance line per page. The file contains the columns `x`, `y`, `nux`, and `nuy`, along with parameters that identify the resonance.

- **switches:**

- `pipe` — The standard SDDS Toolkit pipe option.
- `multipoles=[all=integer] | [dipole,] [quadrupole,] [sextupole,] [octupole,]` — Choose what order of resonances to search for by naming the type of magnet that nominally drives it, or by giving the maximum order to search (`all` option).
- `-type=[normal,] [skew]` — Specify normal- or skew-driven resonances. Default is both.
- `-variables=firstColumn,secondColumn` — Use to change the default names for the coordinate variables.

- **authors:** H. Shang, M. Borland. (ANL).

## sddsfluxcurve

### 8.16 sddsfluxcurve

- **description:** sddsfluxcurve computes undulator fluxcurve curves using Twiss parameter data from elegant or sddsanalyzebeam. Several calculation methods are available.

- **examples:**

```
sddsfluxcurve run.twi run.bri -harmonics=3
-electronBeam=current=0.1,coupling=0.01
-undulator=period=0.033,numberOfPeriods=70,kmin=0.01,kmax=2.7,points=100
-pinhole=distance=30,xsize=0.0025,ysize=0.001
```

- **synopsis:**

```
sddsfluxcurve [-pipe=[input][,output]] [twissFile] [SDDSoutputfile]
[-harmonics=integer] [-method=methodName[,neks=integer]]
[-mode=pinhole|density|total]
-undulator=period=meters,numberOfPeriods=integer,kmin=value,kmax=value[,points=number]
[-electronBeam=current=amps[,coupling=value | emittanceRatio=value]]
[-pinhole=distance=meters,xsize=meters,ysize=meters
[,xnumber=integer][,ynumber=integer][,xposition=meters][,yposition=meters]]
[-nowarnings]
```

- **files:**

- *twissFile* — A Twiss output file from elegant, with radiation integral calculations included, or an output from sddsanalyzebeam. In the latter case, the -correctedOnly option should be used.
- *SDDSoutputFile* — Contains the flux data in column form. For each requested harmonic *i*, there are columns photonEnergy*i* and wavelength*i*, plus a column for the flux (TotalFlux*i*, PinholeFlux*i*, or FluxDensity*i*).

- **switches:**

- **pipe** — The standard SDDS Toolkit pipe option.
- **harmonics** — The number of harmonics to compute.
- **-method=*string*,neks=*value*]** — Choose which method to use for calculations. Options are
  - \* **dejus** — R. Dejus' non-zero emittance, infinite-N+convolution method. This is the default.
  - \* **walkerinfinite** — R. Walker's method. Dejus' method is derived from this method.**neks** is used to change the number of points used for finding the peak of the distribution.
- **mode=pinhole|density|total** — Specify whether to compute the flux through a pinhole, the flux density, or the total flux.

- `-undulator=period=meters,numberOfPeriods=integer,kmin=value,kmax=value[,points=number]`  
— Specify undulator parameters. `points` is the number of  $K$  values to use on the interval  $[K_{min}, K_{max}]$ .
- `electronBeam=current=amps,[,coupling=value | emittanceRatio=value]` — Specify parameters of the electron beam. The current defaults to 0.1 A. Either the coupling or emittance ratio must be given, unless the input file contains the parameter `ey0` or the column `ey`.
- `-pinhole=distance=meters,xsize=meters,ysize=meters[,xnumber=integer][,ynumber=integer][,xposition=meters][,yposition=meters]` — Specify the parameters of the pinhole. Required for `-mode=pinhole`. By default `xnumber=20`, `ynumber=20`, `xposition=0`, and `yposition=0`.
- **authors:** M. Borland, H. Shang, R. Dejus (ANL).

## sddsmatchtwiss

### 8.17 sddsmatchtwiss

- **description:** `sddsmatchtwiss` transforms a beam of macro-particles to match to given beta functions and dispersion. This can be useful in taking macro-particle data from one simulation and using it in another. For example, a beam file from PARMELA could be given the right beta functions for use with a specific lattice in an `elegant` run, saving the trouble of rematching to join the two simulations. Similarly, a beam from `elegant` could be matched into an FEL simulation.

- **examples:**

```
sddsmatchtwiss elegantBeam.out FELBeam.in -xPlane=beta=1.0,alpha=-0.2
-yPlane=beta=0.5,alpha=0.2
```

- **synopsis:**

```
sddsmatchtwiss [-pipe=[input][,output]] inputfile outputfile
[-saveMatrices=filename] [-loadMatrices=filename]
[-xPlane=[beta=meters,alpha=value] [,etaValue=meters] [,etaSlope=value]]
[-yPlane=[beta=meters,alpha=value] [,etaValue=meters] [,etaSlope=value]]
[-zPlane=[deltaStDev=value] [,tStDev=value]
[,correlation=seconds|alpha=value] [,chirp=1/seconds] [,betaGamma=value]]
[-nowarnings]
```

- **files:**

*inputfile* is an SDDS file containing one or more pages of data giving the phase-space coordinates of macro particles. The macro particle data is stored in columns named `x`, `xp`, `y`, `yp`, and `p`. The units are those used by `elegant` for the `output` file from `run_setup`, the `bunch` file from `bunched_beam`, and the coordinate-mode output from the `WATCH` element. The data from these columns is used together with the commandline arguments to produce new values for these columns; the new values are delivered to `outputfile`. Other columns may be present in `inputfile`; if so, they are passed to `outputfile` unchanged.

- **switches:**

- `-xPlane=[beta=meters,alpha=value] [,etaValue=meters] [,etaSlope=value]` — Specifies the desired parameters for the beam in the horizontal plane. `beta` and `alpha` give  $\beta$  and  $\alpha = -\frac{1}{2} \frac{\partial \beta}{\partial s}$ ; they must both be given or both be omitted. `etaValue` and `etaSlope` give the dispersion,  $\eta$ , and its slope,  $\frac{\partial \eta}{\partial s}$ .
- `-yPlane=[beta=meters,alpha=value] [,etaValue=meters] [,etaSlope=value]` — Same as `-xPlane`, except for the vertical plane.
- `-zPlane=[deltaStDev=value] [,tStDev=value] [, {correlation=seconds|alpha=value}] [,chirp=`  
— `deltaStDev` is  $\sigma_\delta = \langle \sqrt{(\delta - \langle \delta \rangle)^2} \rangle$ , `tStDev` is  $\sigma_t = \langle \sqrt{(t - \langle t \rangle)^2} \rangle$ , and `correlation` is  $\sigma_{t,\delta} = \langle (\delta - \langle \delta \rangle)((t - \langle t \rangle)) \rangle$ , in terms of which the longitudinal emittance is  $\epsilon = \sqrt{\sigma_t^2 * \sigma_\delta^2 - \sigma_{t,\delta}^2}$ . `alpha` is  $-\sigma_{t,\delta}/\epsilon$ . The `chirp`, if requested, is added after generation of the beam according to the other parameters. If `betaGamma` is given, the beam is “accelerated” to the given average value of  $\beta\gamma$  in an idealized sense, preserving the momentum spread and transforming the transverse coordinates by the factor  $\sqrt{\langle \beta\gamma \rangle_0 / (\beta\gamma)_{\text{desired}}}$ .



- `-saveMatrices=filename` — Requests saving the transformation matrices to a file.
- `-loadMatrices=filename` — Requests loading the transformation matrices from a file.
- `-nowarnings` — Suppresses warning messages.

- **authors:** M. Borland, H. Shang, ANL/APS.

## sddsrandmult

### 8.18 sddsrandmult

- **description:** `sddsrandmult` computes the multipole errors in a quadrupole or sextupole due to various construction errors. The program is based on the analysis of Halbach[16], with which I'll assume the reader is familiar. Instead of separately evaluating the effect of certain types of mechanical errors, it allows one to simulate several types of errors in order to get statistical distributions for the multipole perturbations.

- **examples:**

```
sddsrandmult quadpert.in
```

- **synopsis:**

```
sddsrandmult inputFile
```

- **usage:**

*inputFile* is a text file containing a series of namelist commands specifying the parameters of a quadrupole or sextupole, the type and amplitude of the errors to include, and the filenames for output. Each namelist command results in a complete computation and generation of output files.

The namelist command is `perturbations`. It has the following fields:

- `type` — A string value, either “quadrupole” (default) or “sextupole”.
- `name` — An optional string value giving the name of the element. This is used in preparing data for `elegant`.
- `SDDS_output` — An required string value giving the name of an SDDS file to which data for each seed will be written. This file can be used to compute statistics or perform histograms.
- `elegant_output` — An optional string value giving the name of a text file to which `elegant` commands and element definitions will be written. Note that this file is a mixture of commands and element definitions. As such, the user must manually edit the file and place the appropriate parts in the lattice file and the command file.
- `kmult_output` — An optional string value giving the name of an SDDS file to which data will be written in the format accepted by the `RANDOM_MULTIPOLES` feature of the `KQUAD` and `KSEXT` elements. *This is the recommended data to use with `elegant`.*
- `effective_length` — The effective length of the magnet, in meters.
- `bore_radius` — The bore radius of the magnet, in meters.
- `reference_radius` — The reference radius for the multipole output, in meters.
- `dx_pole` — The rms error, in meters, to be imparted to the horizontal position of each pole.
- `dy_pole` — The rms error, in meters, to be imparted to the vertical position of each pole.
- `dradius` — The rms error, in meters, in the bore radius.

- **dx\_split** — The rms error, in meters, to be imparted to the horizontal distance between the left and right sides of the magnet.
- **dy\_split** — The rms error, in meters, to be imparted to the vertical distance between the top and bottom halves of the magnet.
- **dphi\_halves** — The rms error, in radians, to be imparted to the relative rotation of the top and bottom halves of the magnet.
- **n\_cases** — The number of cases to simulate (default is 1000).
- **n\_harm** — The number of harmonics to simulate. The default is 0, which results in computing all the harmonics for which Halbach indicates his treatment applies.
- **random\_number\_seed** — The initial seed for the random number generator. Should be a large integer.
- **long suppress\_main\_error** — If non-zero, harmonics for the main multipole and lower orders are suppressed. It is implicitly assumed that these are correctable through alignment and calibration.

- **author:** M. Borland, ANL/APS.

## sddsurgent

### 8.19 sddsurgent

- **description:** sddsurgent uses algorithms from the program US (by R. Dejus) and URGENT (by R. Walker) for computation of undulator radiation properties, including power density and intensity distributions.
- **examples:** Take particle data from a tracking run and compute the power density using a 1 mm by 1 mm pinhole for a 72-period, 3.3-cm-period undulator set for a 5 keV first harmonic.

```
sddsanalyzebeam run.out -pipe=out -correctedOnly
| sddsurgent -pipe=in power.sdds -electronbeam=current=0.025
-calc=method=dejus,mode=powerDensity -us
-pinhole=dist=30,xsize=1,ysize=1,xnum=100,ynum=100
-undulator=period=0.033,number=72,energy=5e3
```

- **synopsis:**

```
sddsurgent inputFile outputFile
[-calculation=mode=modeString,method=methodString,harmonics=integer]
[-undulator=period=meters,numberOfPeriods=integer,
kx=value,ky=value,phase=value,energy=eV]
[-electronBeam=current=Amp,energy=GeV,spread=fraction,
xsigma=mm,ysigma=mm,xprime=mrad,yprime=mrad,nsigma=number]
[-pinhole=distance=m,xposition=value,yposition=value,
xsize=value,ysize=value,xnumber=integer,ynumber=integer]
[-alpha=steps=integer,delta=value] [-omega=steps=integer,delta=value]
[-nphi=integer] [-us] [-photonEnergy=maximum=eV,minimum=eV,points=number]
[-nowarnings] [-coupling=value | -emittanceRatio=value]
```

- **files:**

- *inputFile* — A Twiss output file from **elegant**, with radiation integral calculations included, or an output from **sddsanalyzebeam**. In the latter case, the **-correctedOnly** option should be used with **sddsanalyzebeam**.
- *outputFile* — Contains the output data, which varies depending on the calculation mode. Use **sddsquery** to view the file contents.

- **switches:**

- **pipe** — The standard SDDS Toolkit pipe option.
- **-calculation=mode=*modeString*,method=*methodString*,harmonics=*integer*** — Choose which calculation to perform and what method to us, as well as the number of undulator harmonics to compute. Values for *modeString* are
  - \* 1 | **fluxDistribution**: Angular/spatial flux density distribution.
  - \* 2 | **fluxSpectrum**: Angular/spatial flux density spectrum
  - \* 3 | **brightness** | **brilliance**: On-axis brilliance spectrum

- \* 4 | **pinholeSpectrum**: Flux spectrum through a pinhole
- \* 5 | **integratedSpectrum**: Flux spectrum integrated over all angles
- \* 6 | **powerDensity**: Power density and integrated power

Values for *methodString* are

- \* 1: Non-zero emittance; finite-N.
  - \* 2: Non-zero emittance; infinite-N.
  - \* 3 | **WalkerFinite**: Zero emittance; finite-N.
  - \* 4 | **Dejus**: Non-zero emittance; infinite-N + convolution (Dejus, with **-us** only).
  - \* 14 | **WalkerInfinite**: Non-zero emittance; infinite-N + convolution (Walker, with **-tt us** only).
- **-emittanceRatio=***value* | **-coupling=***value* — In the case of a twiss output file from **elegant**, which does not contain the vertical emittance, one must supply one of these options. If **-emittanceRatio=R** is given,  $\epsilon_y = \epsilon_0 * R$  and  $\epsilon_x = \epsilon_0$ . If **-coupling=k** is given,  $\epsilon_x = \epsilon_0 / (1 + k)$  and  $\epsilon_y = k * \epsilon_x$ .  $\epsilon_0$  is the equilibrium emittance from the twiss output of **elegant**.
- In the case of twiss output from **sddsanalyzebeam**, both emittances are present and these options are ignored.
- **undulator=period=***meters*, **numberOfPeriods=***integer*, **kx=***value*, **ky=***value*, **phase=***value*, **energy=eV** — Specify undulator parameters. If energy (of first-harmonic photons) is given, **kx=0** and **ky** is computed, corresponding to a horizontally deflecting undulator. **phase** specifies the phase difference in degrees for a canted undulator.
- **-electronBeam=current=***Amps*, **energy=***GeV*, **spread=***fraction*, **xsigma=***mm*, **ysigma=***mm*, **xprime=***mrad*, **yprime=***mrad*, **nsigma=***numbers* specifies electron beam parameters. Only the current is needed, as other data will be drawn from the input file.
- \* **current** — electron beam current in A. (default is 0.1A).
  - \* **energy** — electron energy in Gev. (default is 7.0Gev).
  - \* **spread** — electron energy spread.
  - \* **xsigma** — horizontal RMS beam size (mm)
  - \* **ysigma** — vertical RMS beam size (mm)
  - \* **xprime** — horizontal RMS divergence (mrad)
  - \* **yprime** — vertical RMS divergence (mrad)
  - \* **nsigma** — no. of standard deviations of electron beam dimensions (size and divergence) to be included.
- **-pinhole=distance=***m*, **xposition=***value*, **yposition=***value*, **xsize=***value*, **ysize=***value*, **xnumber=***integer*, **ynumber=***integer* — Specifies pinhole parameters. Pinhole parameters are not needed for computing on-axis brilliance (i.e., **mode=3**).
- \* **distance** — distance from the source (m) (distance=0.0 gives angular flux).
  - \* **xposition** — X-coordinate for center of pinhole (mm) or (mrad for distance=0)
  - \* **yposition** — Y-coordinate for center of pinhole (mm) or (mrad for distance=0)
  - \* **xsize** — X-size of pinhole (full width) (mm) or (mrad for distance=0)
  - \* **ysize** — y-size of pinhole (full width) (mm) or (mrad for distance=0)

- \* **xnumber** — Number of subdivisions of pinhole in X (max 500)
- \* **ynumber** — Number of subdivisions of pinhole in Y (max 500)
- **nphi=number** — Specifies number of steps in phi between 0 and  $\pi/2$ . Must be less than 100. used in (calculation mode=1,2,3,4,5 calculation method=1,2).
- **alpha=steps=integer,delta=value** — Specifies the number of steps in angle alpha ( $\gamma\theta$ ) ( $\leq 100$ ). Delta specifies range of angles in  $\alpha^2$  to be used, in units of the angular equivalent to  $1/N$ . Used in (mode=1, method=1) and method=3.
- **omegasteps=integer,delta=value** — Specifies the number of steps in photon energy for the natural lineshape ( $\leq 5000$ ). delta specifies range of photon energies to be included in the natural lineshape in units (energy of fundamental/ $N$ ). The default value covers the range  $\pm 2/N$  of the natural lineshape. Used in mode=2,3,4,5 method=1.
- **photonEnergy=maximum=eV,minimum=eV,points=number** — Specifies the maximum and minimum photon energy in eV, and the number of energy points to be computed.

- **authors:** H. Shang, R. Dejus, M. Borland, X. Jiao (ANL).

## smoothDist6

### 8.20 smoothDist6

- **description:** Increases the number of particles in a particle input file by sampling a simplified distribution based the input file. Intended to be used to increase the number of particles produced by a photoinjector simulation to improve stability of CSR and LSC simulations. Can also add energy and density modulations for performing gain studies.

The algorithm is as follows:

1. Fit a 12<sup>th</sup>-order polynomial to  $p$  as a function of  $t$ . Evaluate the polynomial at 10,000 equispaced points to generate a lookup table for the momentum variation with time.
2. Compute the standard deviation of the momentum  $p_{sd}$  for blocks of 2,000 successive particles. Fit this data with a 12<sup>th</sup>-order polynomial and evaluate it a 10,000 equispaced points to generate a lookup table for  $p_{sd}$  as a function of  $t$ .
3. Create a histogram of  $t$  and smooth it with a low-pass filter having a cutoff at 0.1 THz. This may resulting in ringing at the ends of the histogram, which is clipped off by masking with the original histogram.
4. Optionally modulate the histogram  $H(t)$  with a sinusoid, by multiplying the histogram by  $(1 + d_m) \cos 2\pi ct / \lambda_m$ , where  $d_m$  is the modulation depth and  $\lambda_m$  is the modulation wavelength. For non-zero  $d_m$ , this will result in a longitudinal-density-modulated distribution when the histogram is used as a probability distribution and sampled to create time coordinates.
5. Sample the time histogram  $N$  times using a “quiet start” Halton sequence with radix 2, where  $N$  is the number of desired particles. The sampling operation is performed by first numerically computing the cumulative distribution function  $C(t) = \int_{-\infty}^t H(t') dt' / \int_{-\infty}^{\infty} H(t') dt'$ . Inverting this to obtain  $t(C)$ , we generate each sample from  $H(t)$  by evaluating  $t(U)$ , where  $U$  is a quantity on the interval  $[0, 1]$  generated from the Halton sequence.
6. Create samples for other coordinates by quiet-sampling of gaussian distributions:
  - (a) Scaled transverse coordinates  $\hat{x}$ ,  $\hat{x}'$ ,  $\hat{y}$ , and  $\hat{y}'$  using Halton radices 3, 5, 7, and 11, respectively. For convenience in scaling (step 9), these are defined such that the standard deviation of each coordinate is  $10^{-4}$  and all coordinates are uncorrelated.
  - (b) Scaled fractional momentum deviation  $\delta_1$  using Halton radix 13, with unit standard deviation.
7. Interpolate the look-up tables to determine the mean  $p_{mean}$  and standard deviation  $p_{sd}$  of the momentum at each particle's time coordinate. Use these to compute the individual particle momenta using  $p = p_{mean} + \delta_1 p_{sd}$ .
8. Compute the projected transverse rms emittances and Twiss parameters for the original beam.
9. Transform the scaled transverse phase-space coordinates to give the desired projected Twiss parameters in the x and y planes. The x and y planes are assumed to be uncorrelated.

- **synopsis:**

```
smoothDist6 -input name -output name -factor number -rippleAmplitude %
-rippleWavelength microns -smoothPasses num(500) -energyMod % -betaSlices n
```

- **files:**
  - `input` — A particle distribution file, such as might be used with `sdds_beam`.
  - `output` — A particle distribution file, such as might be used with `sdds_beam`.
- **switches:**
  - `-factor number` — Factor by which to multiply the number of particles.
  - `-rippleAmplitude value` — Density ripple amplitude, in percent.
  - `-energyMod value` — Energy modulation amplitude, in percent. The wavelength is fixed at 1  $\mu\text{m}$ .
  - `-rippleWavelength value` — Density ripple and energy modulation wavelength, in microns.
  - `-betaSlices n` — Number of longitudinal slices to use for analysis of twiss parameters. The twiss parameters of the beam will vary step-wise from slice to slice. This discontinuous variation may cause problems (e.g., unstable behavior).
  - `-smoothPases num` — Presently ignored.
- **author:** M. Borland, ANL/APS.
- **see also:** `doubleDist6`



## TFBFirSetup

### 8.21 TFBFirSetup

- **description:** TFBFirSetup computes FIR (Finite Impulse Response) filter coefficients for use with TFBDRIVER elements to perform turn-by-turn transverse feedback. The method uses time-domain least-squares fitting [47].

- **examples:**

```
TFBSetup -twiss Basic.twi -pickup XPICKUP -driver XDRIIVER -plane x -output
xfb.param -terms 6
```

- **synopsis:**

```
TFBFirSetup -twiss twissFile -pickup elementName -driver elementName -plane
{x|y} -output filename -terms numberOfTerms
```

- **switches:**

- **-twiss** — A twiss parameter file from `elegant`. The beamline used for the computations must include a TFBDRIVER and TFBFEEDBACK element for the plane in question.
- **-pickup** — Specifies the name of the pickup element in the lattice. One and only one occurrence of the element is required in the *twissFile*. Note that generally the name of the pickup should be all uppercase.
- **-driver** — Specifies the name of the driver element in the lattice. One and only one occurrence of the element is required in the *twissFile*. Note that generally the name of the driver should be all uppercase.
- **-plane** — Specifies the plane of the feedback.
- **-output** — Specifies output filename to which FIR configuration is written. The file should be loaded with `load_parameters`, e.g.,

```
&load_parameters
  filename = xfb.param,
  change_defined_values = 1
&end
```

- **-terms** — Number of terms in the filter, between 1 and 30, inclusive.

- **author:** M. Borland, ANL/APS.
- **acknowledgments:** H. Shang, C.-Y. Yao.

## touschekLifetime

### 8.22 touschekLifetime

- **description:** `touschekLifetime` computes Touschek lifetime using A. Piwinski's formula [23, 24]. A longitudinally non-Gaussian distributed bunch lifetime (such as ring with harmonic cavity) can be computed if the bunch profile is inputted through beam option.

- **examples:**

```
touschekLifetime aps.life -twiss=aps.twi -aper=aps.aper -part=2e10
-coupling=0.01 -length=6
```

- **synopsis:**

```
touschekLifetime outputFile -twiss=twissFile -aperture=momentumApertureFile
[-beam=beamProfile | -sliceAnalysis=filename] -charge=nC|-particles=value
{-coupling=value|-emityInput=value} -RF=Voltage=MV,harmonic=value[,limit] |
-length=mm [-emitInput=valueInMeters] [-deltaInput=value] [-verbosity=value]
[-ignoreMismatch] [-deltaLimit=valueInPercent] [-method=0/1]
```

- **files:** *outputFile* — Contains resulting Touschek lifetime.

- **switches:**

- **-twiss** — A twiss parameter file from `elegant`. You must use the `radiation_integrals` flag in `twiss_output`.
- **-aperture** — A momentum aperture file from `elegant`. This file can contain a subset of elements of `twissFile` (for example: only Quadrupole elements). However, the Twiss and momentum aperture files *must* cover the same beamline. Having one file for a part of beamline (e.g., a few sectors) and one for the entire ring will yield incorrect results.
- **-beam** — Give beam profile file from `elegant2genesis`. If this option is given, other input beam parameters are ignored. You can use this option to compute touschek lifetime for a non-Gaussian longitudinally distributed bunch.
- **-sliceAnalysis** — Give slice analysis file from the `SLICE` element in `elegant`. If this option is given, other input beam parameters are ignored. You can use this option to compute touschek lifetime for a non-Gaussian longitudinally distributed bunch.
- **-charge, -particles** — Give the charge (in nanocoulombs) or the number of electrons.
- **-emitInput** — Give the initial total emittance in meters (if **-coupling** is used) or the initial x emittance in meters (if **-emityInput** is used).. If not specified, the value from the parameter `ex0` in *twissFile* is used.
- **-coupling** — Give the emittance coupling ratio,  $\epsilon_y/\epsilon_x$ . This is used to compute the horizontal and vertical emittance from the natural emittance.
- **-emityInput** — Give the vertical emittance in meters.
- **-deltaInput** — Give the initial rms fractional momentum spread. If not specified, the value from the parameter `Sdelta0` in *twissFile* is used.

- `-RF=Voltage=MV,harmonic=value[,limit]` — Specify rf voltage and harmonic number. The `limit` qualifier, if given means that the momentum acceptance is limited by the bucket half-height. N.B.: If the data files cover only a portion of the ring, using this option will give incorrect results!
  - `-length=mm` — Specify the rms bunch length. This is an alternative to giving rf parameters.
  - `-verbosity` — If nonzero, program execution information is printed to the standard output.
  - `-ignoreMismatch` — If given, then mismatch of element names between the twiss and momentum aperture files is ignored. May be useful if there are zero-length elements.
  - `-deltaLimit` — Give the maximum value for the momentum aperture, in percent. If not specified, the values in the momentum aperture input file are used, possibly altered by the use of the `-RF` option with the `limit` qualifier. If both `-deltaLimit` and `-RF=limit...` are given, the smaller is enforced.
  - `-method` — The integral of Piwinski’s formula can be done in two ways. “0” - direct integral of parameter  $\tau$ , this method is also used in `elegant`. 1 - substitute variable  $\tau$  with variable  $k$ , with  $\tau = \tan^2(k)$ . These two methods give you same results.
- **Note:** If using `Pelegant` to compute the momentum aperture with `output_mode=1`, it is necessary to first run the script `reorganizeMmap` to put the data into the form needed by `touschekLifetime`.
  - **author:** A. Xiao, ANL/APS.

## view3dGeometry

### 8.23 view3dGeometry

- **description:** Allows viewing the 3D geometry of a beamline using the freewrl viewer.
- **examples:** To generate 3d data and view:

```
view3dGeometry -rootname aps -showNames '*QUAD* *BEN*' -showCoordinates  
 '*MON*'
```

To view again:

```
freewrl aps.x3d
```

- **synopsis:**

```
view3dGeometry -rootname string -showNames listOfElementTypes  
-showCoordinates listOfElementTypes [-nviewpoints number(10)]
```

- **input files:**

- *rootname.flr* — Contains floor coordinate output from `elegant` (`floor_coordinates` command).
- *rootname.param* — Contains parameter output from `elegant` (`run_setup` command).

- **output files:** *rootname.x3d* — Input data to freewrl.

- **switches:**

- `-rootname` — Gives the rootname of the run, used to identify the input and output files.
- `-showNames` — Gives list of element types, with optional wildcards, for which the element name will be shown in the viewer. Default: “\*SBEN\*”.
- `-showCoordinates` — Gives list of element types, with optional wildcards, for which the local coordinate system will be shown in the viewer. Default: “MARK\* WATCH\*”.
- `nviewpoints` — Number of viewpoints to generate and embed in file. Moving between viewpoints using keystroke commands is easier than “flying” using the keypad.

- **author:** A. Petrenko, BINP. (Modified by M. Borland.)

## 9 Accelerator and Element Description

As mentioned in the introduction, **elegant** uses a variant of the MAD input format for describing accelerators. With some exceptions, the accelerator description for one program can be read by the other with no modification. Among the differences:

- **elegant** does not support the use of MAD-style equations to compute the value of a quantity. The **link\_elements** namelist command can be used for this purpose, and is actually more flexible than the method used by MAD. Also, **rpn**-style equations may be given in double-quotes; these are evaluated once only when the lattice is parsed.
- **elegant** does not support substitution of parameters in beamline definitions.
- **elegant** contains many elements that MAD does not have, such as kick elements, wake fields, and numerically integrated elements.
- The length of an input line is not limited to 80 characters in **elegant**, as it is in MAD. However, for compatibility, any lattice created by **elegant** will conform to this limit.
- The maximum length of the name of an element or beamline is 100 characters.

`elegant`'s lattice parser translates all input into upper case, except where the input is protected by double quotes. However, various commands (such as `vary_element` or `link_elements`) that accept element names as input do not perform any translation. Hence, when referring to element names in commands, the user must enter the names in upper case unless they are protected by double quotes in the lattice file.

When the lattice file is very complex, it is sometimes convenient to separate it into several files. These can then be imported into a main lattice file using the `#INCLUDE` directive, as in

```
#INCLUDE: part1.lte
#INCLUDE: part2.lte
```

The rules for naming elements and beamlines are as follows:

- The name should start with an alphabetic character (i.e., a-z A-Z).
- The name may contain any of the following characters in addition to alphabetic characters and numbers: ~ @ \$ % ^ & - \_ + = { } [ ] \ | / ? < > . : |\verb
- The name should not contain any of the following: # \* ! ‘ ’ ‘
- The name should not contain spaces, tabs, or non-printing characters.

If using unusual characters in a name, it is a good idea to enclose the name in double quotes. This is required if `:` is in the name.

`elegant's print_dictionary` command allows the user to obtain a list of names and short descriptions of all accelerator elements recognized by the program, along with the names, units, types, and default values of all parameters of each element. The present output of this command is listed in the next section. The reader is referred to the MAD manual[2] for details on sign conventions for angles, focusing strength, and so forth.

Comments may be embedded in the lattice file by *starting* a line with an exclamation point (“!”). Rpn expressions may be embedded separately from an element definition by starting a line with a percent sign (“%”). For example

```

! Define Pi (actually "pi" is already defined, but this is just an example)
% 1 atan 4 * sto Pi
% Pi 40 / sto myAngle
! Define a rectangular bend for a ring with 80 equal bends
B1: SBEN,L=1.0,ANGLE="myAngle",E1="myAngle 2 /",E2="myAngle 2 /"

```

Note that to use an RPN expression the value of a parameter, one must enclose the expression in double quotes.

## 9.1 Magnet Strength

There are many conventions for specifying magnetic fields in terms of a multipole, polynomial, or Taylor expansion, which leads to potential confusion. In *elegant* (as in MAD[2]), magnet strengths are specified in terms of Taylor series. For normal multipoles and  $y = 0$ , the expansion is

$$B_y(x, 0) = \sum_{n=0}^{\infty} \frac{B_n x^n}{n!}, \quad (12)$$

where  $B_0$  is the dipole,  $B_1$  is the quadrupole, etc. In general,

$$B_n = \left( \frac{\partial^n B_y}{\partial x^n} \right)_{x=y=0}. \quad (13)$$

*elegant* follows MAD [2] in using a right-handed coordinate system  $(x, y, z)$  in which  $z$  is along the beam direction,  $x$  is to the left, and  $y$  is up.

This expansion for the normal multipole terms can be related to a multipole expansion that includes both normal and skew components. In this convention, positive normal multipole coefficients give positive  $B_y$  for  $x > 0$  and  $y = 0$ . Rotating a positive normal multipole with  $N$  poles  $\pi/N$  clockwise about the vector along the beam direction will convert it into a positive skew multipole. As a result, for a positive skew multipole,  $B_y$  will be non-negative and  $B_x$  will be negative for  $x > 0$  along the line  $\phi = \pi/N$ .

We can satisfy these conventions if we write the scalar potential as

$$V = \sum_{n=1}^{\infty} \frac{iA_{n-1} - B_{n-1}}{n!} (x + iy)^n e^{-in\Delta\phi}, \quad (14)$$

where, as we'll see,  $A_m$  are skew components and  $B_m$  are normal components for a  $2(m+1)$ -pole. The coordinates  $(x, y)$  are in a right-handed system with the longitudinal coordinate  $z$ .  $\Delta\phi$  is the rotation angle of the magnet, where a clockwise rotation about the nominal trajectory corresponds to  $\Delta\phi > 0$ . The minus sign in  $e^{-in\Delta\phi}$  is because we rotate the magnet while keeping the coordinate system fixed.

The magnetic fields are

$$B_y = -\Im \frac{\partial V}{\partial y} = \Im \sum_{n=0}^{\infty} \frac{A_n + iB_n}{n!} (x + iy)^n e^{-i(n+1)\Delta\phi}, \quad (15)$$

and

$$B_x = -\Im \frac{\partial V}{\partial x} = \Im \sum_{n=0}^{\infty} \frac{-iA_n + B_n}{n!} (x + iy)^n e^{-i(n+1)\Delta\phi}, \quad (16)$$

We can relate the coefficients to the  $B_m$  quantities used in MAD and **elegant** by noting that for  $\Delta\phi = 0$

$$B_m = \left( \frac{\partial^m B_y}{\partial x^m} \right)_{x=y=0} \quad (17)$$

and

$$A_m = - \left( \frac{\partial^m B_x}{\partial x^m} \right)_{x=y=0} \quad (18)$$

Note the minus sign in the last equation, which differs from commonly asserted conventions.

Multipole errors are typically specified as fractions of the main field harmonic at a reference radius  $R$ , e.g.,

$$F_n = \frac{K_n R^n / n!}{K_m R^m / m!}, \quad (19)$$

where  $m$  is the main harmonic and  $n$  is the error harmonic.

For electrons, the deflection from a thin element is

$$\theta(x, y = 0) = \frac{1}{H} \int B(x, y = 0) dl, \quad (20)$$

where  $H = B\rho = -p/e$  is the beam rigidity and  $p = m_e c \beta \gamma$  is the momentum. The geometric strengths  $K_n$  are defined as

$$K_n = \frac{B_n}{H}. \quad (21)$$

By convention in **elegant**, a positive  $K_n$  value deflects a particle at  $x > 0$  toward  $x = 0$ . E.g., a positive  $K_1$  value indicates a horizontally focusing quadrupole.

## 10 Element Dictionary



## ALPH

### 10.1 ALPH—An alpha magnet implemented as a matrix, up to 3rd order.

An alpha magnet implemented as a matrix, up to 3rd order.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| XMAX           | $M$   | double | 0.0     | size of alpha  |
| XS1            | $M$   | double | 0.0     | inner scraper position relative to XMAX  |
| XS2            | $M$   | double | 0.0     | outer scraper position relative to XMAX  |
| DP1            |       | double | -1      | inner scraper fractional momentum deviation  |
| DP2            |       | double | 1       | outer scraper fractional momentum deviation  |
| XPUCK          | $M$   | double | -1      | position of scraper puck   |
| WIDTHPUCK      | $M$   | double | 0.0     | size of scraper puck   |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| DZ             | $M$   | double | 0.0     | misalignment   |
| TILT           |       | double | 0.0     | rotation about incoming longitudinal axis  |
| PART           |       | short  | 0       | 0=full, 1=first half, 2=second half  |
| ORDER          |       | short  | 0       | matrix order [1,3]   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element provides a matrix-based implementation of an alpha magnet [5]. Matrices up to third order are available [4].

The parameter **XMAX** determines the size of the alpha, which is related to the gradient  $g$  in the magnet and the central momentum  $\beta\gamma$  by

$$x_{max}[m] = 0.07504986 \sqrt{\frac{\beta\gamma}{g[T/m]}}. \quad (22)$$

The path length of the central particle is  $2.554x_{max}$ .

Because an alpha magnet has large dispersion at the midplane, it is often used for momentum filtration in addition to bunch compression. The dispersion at the center is given by the simple

relation

$$R_{16} = -\frac{1}{2}x_{max}. \quad (23)$$

To use an alpha magnet for momentum filtration in **elegant**, one must split the alpha magnet into two pieces. One may then either use the scraper features of the **ALPH** element or other elements such as **SCRAPER** or **RCOL**.

To split an alpha magnet, one uses the **PART** parameter. E.g.,

```
! First half, with momentum filter between -5% and +2.5%
AL1: ALPH,XMAX=0.11,PART=1,DP1=-0.05,DP2=0.025
! Second half
AL2: ALPH,XMAX=0.11,PART=2
AL: LINE=(AL1,AL2)
```

As just illustrated, the parameters **DP1** and **DP2** may be used to filter the momentum by providing fractional momentum deviation limits. These are implemented in a physical fashion by computing the corresponding horizontal position deviations and imposing these as limits on the particle coordinates. One may also do this directly using the **XS1** and **XS2** parameters, which specify maximum acceptable deviations from the nominal horizontal position. **XS1** is the allowed deviation on the low-energy side while **XS2** is the allowed deviation on the high-energy side.

## APCONTOUR

### 10.2 APCONTOUR—An aperture (or its inverse) defined by (x, y) points in an SDDS file.

An aperture (or its inverse) defined by (x, y) points in an SDDS file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| L              | <i>M</i>   | double | 0.0     | length   |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX             | <i>M</i>   | double | 0.0     | misalignment   |
| DY             | <i>M</i>   | double | 0.0     | misalignment   |
| DZ             | <i>M</i>   | double | 0.0     | misalignment   |
| RESOLUTION     | <i>M</i>   | double | 0.0     | z resolution of finding intersection   |
| INVERT         |            | long   | 0       | if non-zero, contour defines an obstruction rather than an aperture  |
| FILENAME       |            | STRING | NULL    | name of file containing contour data   |
| XCOLUMN        |            | STRING | NULL    | name of column containing x data   |
| YCOLUMN        |            | STRING | NULL    | name of containing y data  |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## BGGEXP

### 10.3 BGGEXP—A magnetic field element using generalized gradient expansion.

A magnetic field element using generalized gradient expansion.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name       | Units       | Type   | Default | Description   |
|----------------------|-------------|--------|---------|---|
| L                    | $M$         | double | 0.0     | insertion length  |
| LFIELD               | $M$         | double | -1      | expected length of the field map. If negative, use L.   |
| FILENAME             | <i>NULL</i> | STRING | NULL    | name of file generalized gradient data  |
| STRENGTH             | <i>NULL</i> | double | 1       | factor by which to multiply field   |
| TILT                 | $RAD$       | double | 0.0     | rotation about longitudinal axis  |
| DX                   | $M$         | double | 0.0     | misalignment  |
| DY                   | $M$         | double | 0.0     | misalignment  |
| DZ                   | $M$         | double | 0.0     | misalignment  |
| BX                   | $T$         | double | 0.0     | add BX*STRENGTH to Bx field   |
| BY                   | $T$         | double | 0.0     | add BY*STRENGTH to By field   |
| MAXIMUM_M            |             | short  | -1      | data with m greater than this is ignored  |
| MAXIMUM_2N           |             | short  | -1      | data with 2*n greater than this is ignored  |
| Z_INTERVAL           |             | short  | 1       | input z data is sampled at this interval  |
| SYMPLECTIC           |             | short  | 0       | if nonzero, use implicit symplectic integrator. At minimum, should always be used to validate the sufficiency of the non-symplectic integrator. |
| SYNCH_RAD            |             | short  | 0       | if nonzero, include classical, single-particle synchrotron radiation  |
| ISR                  |             | short  | 0       | if nonzero, include incoherent synchrotron radiation (quantum excitation)   |
| PARTICLE_OUTPUT_FILE |             | STRING | NULL    | name of file for phase-space and field output. Use for debugging only!  |
| IS_BEND              |             | short  | 0       | if nonzero, magnet is a bending magnet; vertex, entry, and exit points should be defined.   |

## BGEXP continued

A magnetic field element using generalized gradient expansion.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| XVERTEX        | $M$   | double | 0.0     | For dipoles: x position of vertex in coordinate system of the fields.  |
| ZVERTEX        | $M$   | double | 0.0     | For dipoles: z position of vertex in coordinate system of the fields.  |
| XENTRY         | $M$   | double | 0.0     | For dipoles: x position of reference entry point in coordinate system of the fields.   |
| ZENTRY         | $M$   | double | 0.0     | For dipoles: z position of reference entry point in coordinate system of the fields.   |
| XEXIT          | $M$   | double | 0.0     | For dipoles: x position of reference exit point in coordinate system of the fields.  |
| ZEXIT          | $M$   | double | 0.0     | For dipoles: z position of reference exit point in coordinate system of the fields.  |
| DXEXPANSION    | $M$   | double | 0.0     | x position of expansion relative to coordinate system of the fields.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates transport through a 3D magnetic field specified in terms of a generalized gradient expansion [50]. After reconstructing the field, it simply integrates the equations of motion based on the Lorentz force equation in cartesian coordinates.

The generalized gradients are provided in an SDDS file with the following floating-point columns:

- **z** — Longitudinal coordinate. Units should be “m”.
- **Cnmn** — The  $n^{th}$  generalized gradient of the  $m^{th}$  harmonic, where  $n = 0, 2, 4, \dots$ . There is no preset limit to the number of generalized gradients. Units are ignored, but should be SI.
- **dCnmn/dz** — The longitudinal derivative of the  $n^{th}$  generalized gradient, for the  $m^{th}$  harmonic, where  $n = 0, 2, 4, \dots$ . The number of derivatives must match the number of generalized gradients **Cnmn**.

In addition, the file must contain a parameter:

- **m** — The multipole index, using the convention where  $m = 1$  is dipole,  $m = 2$  is quadrupole, etc. N.B.: this convention conforms with [50] but is not the usual one used by **elegant**. This should be stored as a short integer. N. B.: for  $m = 1$ , if the system has net bending, the results will not be correct as the required coordinate transformations are not performed.

The generalized gradient file can be prepared using the script **computeGeneralizedGradients**, which is provided with **elegant**. The input file for that script must be organized into many pages, with each page giving  $B_r(\phi)$  on radius  $r = R$  for a single  $z$  location. The file must contain two floating-point columns:

- **phi** — The angle, in radians.  $\phi = 0$  corresponds to  $x = R$  and  $y = 0$ , while  $\phi = \pi/2$  corresponds to  $x = 0$  and  $y = R$ . It is assumed that  $\phi$  runs from 0 to  $2\pi - \Delta\phi$  in steps of  $\Delta\phi$ .
- **Br** — The radial field at the reference radius  $R$ , Tesla.

In addition, the file must contain two floating-point parameters:

- **R** — The radius, in meters.
- **z** — The longitudinal coordinate, in meters.  $z$  should extend from the zero-field region upstream of the magnet to the zero-field region downstream of the magnet.

Synchrotron radiation can be included by setting **SYNCH\_RAD=1** for classical radiation only and also **ISR=1** for incoherent (quantum) effects. This will impact the results of **moments\_output** calculation as well as tracking.

Important notes and limitations:

1. The calculations of **twiss\_output**, including radiation integrals, are at this point not affected, nor is the setup of rf cavities for storage rings via the **rf\_setup** command.
2. The symplectic integrator, in addition to being symplectic, is typically more accurate than the non-symplectic integrator. It is also considerably slower. However, at minimum, users should use the symplectic integrator to verify that the accuracy of the non-symplectic integrator is adequate.
3. The **BX** and **BY** parameters allow imposing uniform horizontal and vertical magnetic fields on the device. This can be helpful if the terminal trajectory deviates from the expected value, e.g., an on-axis particle ends up off-axis. This may happen if the device has a dipolar field that is truncated at the ends before it has decayed sufficiently. Note that these values are multiplied by the **STRENGTH** factor before being applied to the beam.

If **IS\_BEND** is non-zero, the magnet is assumed to be a bending magnet, in which case additional parameters are required.

- **ZVERTEX**, **XVERTEX** — Coordinates of the vertex point in coordinate frame of the field data. For a symmetric dipole, **ZVERTEX** is typically zero, while **XVERTEX** would be the displacement of the vertex point from the cylinder axis.
- **ZENTRY**, **XENTRY** — Coordinates of the nominal entry plane.
- **ZEXIT**, **XEXIT** — Coordinates of the nominal exit plane.

## BMAPXY

### 10.4 BMAPXY—A map of Bx and By vs x and y.

A map of Bx and By vs x and y.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| STRENGTH       | <i>NULL</i> | double | 0.0     | factor by which to multiply field  |
| ACCURACY       | <i>NULL</i> | double | 0.0     | integration accuracy   |
| METHOD         | <i>NULL</i> | STRING | NULL    | integration method (runge-kutta, bulirsch-stoer, modified-midpoint, two-pass modified-midpoint, leap-frog, non-adaptive runge-kutta)                       |
| FILENAME       | <i>NULL</i> | STRING | NULL    | name of file containing columns (x, y, Fx, Fy) giving normalized field (Fx, Fy) vs (x, y)  |
| FX             | <i>NULL</i> | STRING | NULL    | rpn expression for Fx in terms of x and y  |
| FY             | <i>NULL</i> | STRING | NULL    | rpn expression for Fy in terms of x and y  |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates transport through a transverse magnetic field specified as a field map. It does this by simply integrating the Lorentz force equation in cartesian coordinates. It does not incorporate changes in the design trajectory resulting from the fields. I.e., if you input a dipole field, it is interpreted as a steering element.

The field map file is an SDDS file with the following columns:

- **x, y** — Transverse coordinates in meters (units should be “m”).
- **Fx, Fy** — Normalized field values (no units). The field is multiplied by the value of the STRENGTH parameter to convert it to a local bending radius. For example, if Fx=y and Fy=x, then STRENGTH is the K1 quadrupole parameter.
- **Bx, By** — Field values in Tesla (units should be “T”). The field is still multiplied by the value of the STRENGTH parameter, which is dimensionless. Note: the default value of STRENGTH is 0, so if you don’t set it to something, you’ll get no effect!



The field map file must contain a rectangular grid of points, equispaced (separately) in x and y. There should be no missing values in the grid (this is not checked by **elegant**). In addition, the x values must vary fastest as the values are accessed in row order. To ensure that this is the case, use the following command on the field file:

```
sddssort fieldFile -column=y,incr -column=x,incr
```

## BMXYZ

### 10.5 BMXYZ—A map of (Bx, By, Bz) vs (x, y, z), for straight elements only

A map of (Bx, By, Bz) vs (x, y, z), for straight elements only

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name       | Units       | Type   | Default | Description  |
|----------------------|-------------|--------|---------|--|
| L                    | <i>M</i>    | double | 0.0     | insertion length   |
| DX                   | <i>M</i>    | double | 0.0     | misalignment   |
| DY                   | <i>M</i>    | double | 0.0     | misalignment   |
| DZ                   | <i>M</i>    | double | 0.0     | misalignment   |
| TILT                 | <i>RAD</i>  | double | 0.0     | rotation about longitudinal axis   |
| LFIELD               | <i>M</i>    | double | -1      | expected length of the field map. If negative, determined from field data.   |
| STRENGTH             | <i>NULL</i> | double | 1       | factor by which to multiply field  |
| ACCURACY             | <i>NULL</i> | double | 0.0     | integration accuracy   |
| METHOD               | <i>NULL</i> | STRING | NULL    | integration method (runge-kutta, bulirsch-stoer, modified-midpoint, two-pass modified-midpoint, leap-frog, non-adaptive runge-kutta)         |
| FILENAME             | <i>NULL</i> | STRING | NULL    | name of file containing columns (x, y, z) and either (Bx, By, Bz) or (Fx, Fy, Fz)  |
| SYNCH_RAD            |             | short  | 0       | include classical, single-particle synchrotron radiation?  |
| CHECK_FIELDS         |             | short  | 0       | check fields by computing divB and curlB errors?   |
| INJECT_AT_Z0         |             | short  | 0       | By default, particles are placed at the entrance to the field map regardless of the z coordinate values. If nonzero, particles start at z=0. |
| DRIFT_MATRIX         |             | short  | 0       | If non-zero, instead of tracking to determine the matrix, just assume a drift-space matrix.  |
| PARTICLE_OUTPUT_FILE | <i>NULL</i> | STRING | NULL    | name of file for phase-space output inside element. Use for debugging only in serial version.  |

## BMXYZ continued

A map of (Bx, By, Bz) vs (x, y, z), for straight elements only

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates transport through a 3D magnetic field specified as a field map. It does this by simply integrating the Lorentz force equation in cartesian coordinates. It does not incorporate changes in the design trajectory resulting from the fields. I.e., if you input a dipole field, it is interpreted as a steering element.

The field map file is an SDDS file with the following columns:

- **x, y, x** — Transverse coordinates in meters (units should be “m”).
- **Fx, Fy, Fx** — Normalized field values (no units). The field is multiplied by the value of the STRENGTH parameter to convert it to a local bending radius. For example, an ideal quadrupole could be simulated by setting (Fx=y, Fy=x, Fz=0), in which case STRENGTH is the K1 quadrupole parameter.
- **Bx, By, Bz** — Field values in Tesla (units should be “T”). The field is still multiplied by the value of the STRENGTH parameter, which is dimensionless.

The field map file must contain a rectangular grid of points, equispaced (separately) in x, y, and z. There should be no missing values in the grid (this is not checked by **elegant**). In addition, the x values must vary fastest as the values are accessed in row order, then the y values. To ensure that this is the case, use the following command on the field file:

```
sddssort fieldFile -column=z,incr -column=y,incr -column=x,incr
```

This element is an alternative to **FTABLE** using a more conventional integration method.

## BOFFAXE

### 10.6 BOFFAXE—A straight magnetic field element using off-axis expansion from an on-axis derivative.

A straight magnetic field element using off-axis expansion from an on-axis derivative.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name       | Units       | Type   | Default | Description   |
|----------------------|-------------|--------|---------|---|
| L                    | $M$         | double | 0.0     | insertion length  |
| LFIELD               | $M$         | double | -1      | expected length of the field map for verification purposes only.          |
| FILENAME             | <i>NULL</i> | STRING | NULL    | name of file containing derivative data                                   |
| Z_COLUMN             | <i>NULL</i> | STRING | z       | name of longitudinal coordinate column in the data file                   |
| FIELD_COLUMN         | <i>NULL</i> | STRING | NULL    | name of derivative column in the data file                                |
| ORDER                |             | short  | 1       | order of transverse derivative  |
| EXPANSION_ORDER      |             | short  | 0       | order of expansion in x and y. If zero, determined by data in file.       |
| STRENGTH             | <i>NULL</i> | double | 1       | factor by which to multiply field   |
| TILT                 | $RAD$       | double | 0.0     | rotation about longitudinal axis  |
| DX                   | $M$         | double | 0.0     | misalignment  |
| DY                   | $M$         | double | 0.0     | misalignment  |
| DZ                   | $M$         | double | 0.0     | misalignment  |
| BX                   | $T$         | double | 0.0     | add $BX \cdot STRENGTH$ to $B_x$ field                                    |
| BY                   | $T$         | double | 0.0     | add $BY \cdot STRENGTH$ to $B_y$ field                                    |
| Z_INTERVAL           |             | short  | 1       | input z data is sampled at this interval                                  |
| Z_SUBDIVISIONS       |             | short  | 1       | Number of subdivisions of z interval to use in integration                |
| SYNCH_RAD            |             | short  | 0       | if nonzero, include classical, single-particle synchrotron radiation      |
| ISR                  |             | short  | 0       | if nonzero, include incoherent synchrotron radiation (quantum excitation) |
| PARTICLE_OUTPUT_FILE |             | STRING | NULL    | name of file for phase-space and field output. Use for debugging only!    |

## BOFFAXE continued

A straight magnetic field element using off-axis expansion from an on-axis derivative.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This somewhat experimental element simulates transport through a 3D magnetic field constructed from an off-axis expansion. At present, it is restricted to non-bending elements and in fact to quadrupoles.

This method of expanding the fields is prone to corruption by noise, to a much greater degree than the generalized gradient expansion used by **BGGEXP**. However, it uses data that can very readily be obtained from magnetic measurements with a Hall probe. Users are cautioned to take care in deciding how far to trust the expansion.

For quadrupoles, we use the on-axis gradient  $g(z)$  and its  $z$  derivatives  $g^{(n)}(z)$ . The scalar potential can be written

$$\Phi = \frac{x^5 y^5 g^{(8)}(z)}{86400} - \frac{g^{(6)}(z) (x^5 y^3 + x^3 y^5)}{4320} + \frac{1}{720} g^{(4)}(z) (x^5 y + x y^5) + \frac{1}{108} x^3 y^3 g^{(4)}(z) - \frac{1}{12} (x^3 y + x y^3) g''(z) + x y g(z) \quad (24)$$

From which we find

$$B_x = \frac{x^4 y^5 g^{(8)}(z)}{17280} - \frac{g^{(6)}(z) (5x^4 y^3 + 3x^2 y^5)}{4320} + \frac{1}{720} g^{(4)}(z) (5x^4 y + y^5) + \frac{1}{36} x^2 y^3 g^{(4)}(z) - \frac{1}{12} (3x^2 y + y^3) g''(z) + y g(z) \quad (25)$$

$$B_y = \frac{x^5 y^4 g^{(8)}(z)}{17280} - \frac{g^{(6)}(z) (3x^5 y^2 + 5x^3 y^4)}{4320} + \frac{1}{720} g^{(4)}(z) (x^5 + 5x y^4) + \frac{1}{36} x^3 y^2 g^{(4)}(z) - \frac{1}{12} (x^3 + 3x y^2) g''(z) + x g(z) \quad (26)$$

and

$$B_z = \frac{x^5 y^5 g^{(9)}(z)}{86400} - \frac{g^{(7)}(z) (x^5 y^3 + x^3 y^5)}{4320} + \frac{1}{720} g^{(5)}(z) (x^5 y + x y^5) + \frac{1}{108} x^3 y^3 g^{(5)}(z) - \frac{1}{12} g^{(3)}(z) (x^3 y + x y^3) + x y g'(z) \quad (27)$$

These equations satisfy Maxwell's curl equation exactly while satisfying the divergence equation to  $10^{th}$  order.

The gradient  $g(z)$  is specified in the column named by the **FIELD\_COLUMN** parameter. The names for the columns containing  $z$  derivatives of  $g(z)$  are constructed from the name of the gradient. Assume for concreteness that **FIELD\_COLUMN**=**"Gradient"**. **elegant** looks for  $g^{(1)}(z)$  in column **GradientDeriv** and  $g^{(n)}(z)$  for  $n > 1$  in columns **GradientDeriv2**, **GradientDeriv3**, etc. Even if the expansion is limited by the **ORDER** parameter, all gradients will be used for interpolation with respect to  $z$  if the **Z\_SUBDIVISIONS** parameter is larger than 1. The expansion is truncated if the needed columns do not exist in the input file.

The needed derivatives can be obtained using the program **sddsderiv**, e.g.,

```
sddsderiv gradient.sdds gradient1.sdds -differ=Gradient -versus=z -savitzky=7,7,7,1
sddsderiv gradient.sdds gradient2.sdds -differ=Gradient -versus=z -savitzky=7,7,7,2
sddsderiv gradient.sdds gradient3.sdds -differ=Gradient -versus=z -savitzky=7,7,7,3
sddsxref gradient.sdds gradient[123].sdds gradients.sdds -take=*Deriv*
```

(In this example, we use a Savitzky-Golay filter to compute the first three  $z$  derivatives of  $g(z)$  using a  $7^{th}$  order fit with 7 points ahead of and behind the evaluation location.) The file `gradients.sdds` would then be given as the value of `FILENAME`.

High-order numerical derivative are of course prone to corruption by measurement noise. Examining the derivatives is strongly recommended to ensure this is not an issue.

## BRANCH

### 10.7 BRANCH—Conditional branch instruction to jump to another part of the beamline

Conditional branch instruction to jump to another part of the beamline

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| COUNTER         |       | long   | 0       | Counter, which is decremented by 1 for each pass. Set to negative value for unconditional branch.  |
| INTERVAL        |       | long   | 0       | Interval between branching. If non-positive, use COUNTER-based method instead.   |
| OFFSET          |       | long   | 0       | If INTERVAL method used, offset of branch passes.  |
| VERBOSITY       |       | long   | 0       | Larger values result in more output during running.  |
| DEFAULT_TO_ELSE |       | long   | 0       | If non-zero, defaults to ELSE_TO when performing tracking for closed orbit, twiss_output, etc.   |
| BRANCH_TO       |       | STRING | NULL    | Optional name of element to which to jump when counter is non-positive.  |
| ELSE_TO         |       | STRING | NULL    | Optional name of element to which to jump when counter is positive.  |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is experimental and should be used with care. It may not work well with other features, e.g., orbit correction or twiss parameter output. It should work well with tracking.

The element permits switching tracking between two segments of a beamline. This can be done once per run or periodically. For the former, the **COUNTER** parameter should be used to specify the pass number (which is zero on the first pass) on which to branch. For the latter, the **INTERVAL**  $i$  and (optionally) **OFFSET**  $o$  parameters should be used; the branch will occur when  $(p - o) \% i == 0$ .

The application that inspired creation of this element is to switch from tracking using lumped elements to tracking using element-by-element methods. More specifically, imagine we want to



track for 10,000 turns to reach an equilibrium, then perform a beam abort. The equilibrium state can be accurately and rapidly modeled using lumped elements, such as ILMATRIX and SREFFECTS, but the beam abort needs to be modeled using comparatively slow element-by-element tracking.

```
RING1: ILMATRIX,...
SR1: SREFFECTS,...
...
RINGFULL: line=(SECTOR1, SECTOR2, ..., SECTOR40)
M1: MARK
M2: MARK
RF: RFCA,...
BR1: BRANCH,COUNTER=10000,BRANCH_TO="M1"
BR2: BRANCH,COUNTER=-1,BRANCH_TO="M2"
BL: line=(BR1,RING1,SR1,M1,RINGFULL,M2,RF)
```

Another application is to model a periodic bypass, e.g.,

```
RINGA: line=(...)
RINGB: line=(...)
RINGC: line=(...)
BYPASS: line=(...)
M1: MARK
M2: MARK
BR1: BRANCH,INTERVAL=100,BRANCH_TO="M1",ELSE_TO="M2"
BR2: BRANCH,COUNTER=-1,BRANCH_TO="M3"
BL: line=(RINGA,BR1,M1,BYPASS,BR2,M2,RINGB,M3,RINGC)
```

In this example, the full ring is composed of three sections, RINGA, RINGB, and RINGC. Every 100 passes, the RINGB portion is bypassed in favor of BYPASS.

## BRAT

### 10.8 BRAT—Bending magnet RAY Tracing using (Bx, By, Bz) vs (x, y, z).

Bending magnet RAY Tracing using (Bx, By, Bz) vs (x, y, z).

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| ANGLE          | <i>RAD</i>  | double | 0.0     | Nominal bending angle. Will be refined to match geometry specified by input/output and vertex coordinates  |
| FSE            | <i>NULL</i> | double | 0.0     | fractional strength error  |
| ACCURACY       | <i>NULL</i> | double | 0.0     | integration accuracy   |
| METHOD         | <i>NULL</i> | STRING | NULL    | Ignored. Method defaults to Bulirsch-Stoer.  |
| FILENAME       | <i>NULL</i> | STRING | NULL    | name of file containing columns (x, y, z, Bx, By, Bz)  |
| XVERTEX        | <i>M</i>    | double | 0.0     | x coordinate of vertex point   |
| ZVERTEX        | <i>M</i>    | double | 0.0     | z coordinate of vertex point   |
| XENTRY         | <i>M</i>    | double | 0.0     | x coordinate of nominal entry point  |
| ZENTRY         | <i>M</i>    | double | 0.0     | z coordinate of nominal entry point  |
| XEXIT          | <i>M</i>    | double | 0.0     | x coordinate of nominal exit point   |
| ZEXIT          | <i>M</i>    | double | 0.0     | z coordinate of nominal exit point   |
| DXMAP          | <i>M</i>    | double | 0.0     | x displacement of map  |
| DZMAP          | <i>M</i>    | double | 0.0     | z displacement of map  |
| YAWMAP         | <i>RAD</i>  | double | 0.0     | yaw of map about x=z=0   |
| FACTOR         |             | double | 1       | factor by which to multiply fields   |
| USE_FTABLE     |             | short  | 0       | If nonzero, use FTABLE method for integration. Value gives the number of kicks.  |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Bending magnet RAY Tracing using (Bx, By, Bz) vs (x, y, z). This element is a companion

to the commandline program **abrat**. It integrates through a 3-D field map for a bending magnet, including coordinate transformations. No synchrotron radiation calculations are included at this time.

### **Coordinates**

The coordinates of the field map are right-handed system (x, y, z), where z is along the length of the magnet, x is to the right as viewed along the direction of beam propagation, and y is up. The user must specify the (x, z) coordinates of three points:

- Nominal entrance point: **XENTRY** and **ZENTRY**. These give the coordinates of reference trajectory at the exit of the previous element. In the limit of a hard-edge model, this would be at the entrance to the magnetic field region.
- Vertex point: **XVERTEX** and **ZVERTEX**. These give the coordinates of vertex point, which is the intersection of the reference lines from the entrance and exit.
- Nominal exit point: **XEXIT** and **ZEXIT**. These give the coordinates of reference trajectory at the exit of the previous element. In the limit of a hard-edge model, this would be at the exit from the magnetic field region.

The bending angle is equal to the angle between two lines: the line from **ENTRY** to **VERTEX** and the line from **VERTEX** to **EXIT**. The **L** and **ANGLE** parameters supplied by the user are used for geometry calculations (e.g., floor coordinates) only.

The **DXMAP**, **DZMAP**, **YAWMAP**, and **FSE** values can be used to optimize the field map to ensure that the horizontal reference trajectory is not displaced at the exit of the element. The optimization feature of the **abrat** program can be used to determine these values.

### **Matrix generation**

**elegant** will use tracking to determine the transport matrix for **BRAT** elements, which is needed for computation of twiss parameters and other operations. This can require some time, so **elegant** will cache the matrices and re-use them for identical elements.

### **Integration methods**

The original (and default) integration method is Bulirsch-Stoer integration of the Lorentz force equation. As an alternative, one can use the faster, rotation-based method of the **FTABLE** element. For repeated use, the two methods should be compared and a choice made based on the user's needs.

### **Limitations**

Floor coordinates are incorrect following a **BRAT** element.

## BUMPER

### 10.9 BUMPER—A time-dependent kicker magnet with optional spatial dependence of the kick and no fringe effects. The waveform is in SDDS format, with time in seconds and amplitude normalized to 1. The optional spatial dependence is also specified as an SDDS file.

A time-dependent kicker magnet with optional spatial dependence of the kick and no fringe effects. The waveform is in SDDS format, with time in seconds and amplitude normalized to 1. The optional spatial dependence is also specified as an SDDS file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units   | Type   | Default | Description  |
|-----------------|---------|--------|---------|--|
| L               | $M$     | double | 0.0     | length   |
| ANGLE           | $RAD$   | double | 0.0     | kick angle   |
| TILT            | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| DX              | $M$     | double | 0.0     | misalignment   |
| DY              | $M$     | double | 0.0     | misalignment   |
| DZ              | $M$     | double | 0.0     | misalignment   |
| B2              | $1/M^2$ | double | 0.0     | Sextupole term:<br>$B_y = B_0 * (1 + b_2 * x^2)$   |
| TIME_OFFSET     | $S$     | double | 0.0     | time offset of waveform  |
| PERIODIC        |         | long   | 0       | is waveform periodic?  |
| PHASE_REFERENCE |         | long   | 0       | phase reference number (to link with other time-dependent elements)  |
| FIRE_ON_PASS    |         | long   | 0       | pass number to fire on   |
| N_KICKS         |         | long   | 0       | Number of kicks to use for simulation. 0 uses an exact result but ignores b2.  |
| WAVEFORM        |         | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving kick factor vs time   |
| DEFLECTION_MAP  |         | STRING | NULL    | optional filename giving the spatial variation of the deflection   |
| GROUP           |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a time-dependent kicker magnet as a rectangular dipole with no fringe

field effects. To use this element, you must supply an SDDS file giving the time-dependent waveform. The element is called BUMPER to because HKICK, VKICK, KICKER are used for steering magnets.

The arrival time of the beam is taken to define the reference time,  $t = 0$ . Hence, if the waveform file has the maximum amplitude at  $t = 0$ , the beam will get kicked at the peak of the waveform. If the waveform peaks at  $t = t_{peak}$ , then setting TIME\_OFFSET equal to  $-t_{peak}$  will ensure that the beam is kicked at the peak amplitude.

By default, the kicker fires on the first beam passage. However, if FIRE\_ON\_PASS is used, then the kicker is treated like a drift space until the specified pass.

If PHASE\_REFERENCE is non-zero, then the initial timing is taken from the first time-dependent element that has the same PHASE\_REFERENCE value. This would allow, for example, simulating several kickers firing at the same time. Delays relative to this reference time can then be given with positive adjustments to TIME\_OFFSET.

The waveform input file need not have equispaced points in time. However, the time values should increase monotonically.

The deflection map, if provided, should have four floating-point columns

1. Transverse coordinates  $x$  and  $y$ , with units of m.
2. Kick multipliers  $xpFactor$  and  $ypFactor$ , which are dimensionless quantities.

The resulting kick in each plane for a particle with coordinates  $(x, y, t, \delta)$  is

$$\Delta q'(x, y, t, \delta) = \frac{\theta A(t) f_q(x, y)}{1 + \delta}, \quad (28)$$

where  $q$  stands for  $x$  or  $y$ ,  $\theta$  is the specified deflection angle,  $A(t)$  is the time-dependent amplitude waveform, and  $f_q(x, y)$  is the deflection map factor for the  $q$  plane at the particle's location.

The data in the deflection map file must be sorted so that  $x$  changes fastest, which can be accomplished using the command

```
sddssort input.sdds -column=y,incr -column=x,incr
```

This element simulates a dipole kicker only. For multipole kickers, see the MBUMPER element.

**Explanation of <filename>=<x>+<y> format:** Several elements in *elegant* make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is `waveform.sdds=t+A`, then it means that columns `t` and `A` will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## CCBEND

### 10.10 CCBEND—A canonically-integrated straight dipole magnet, assumed to have multipoles defined in Cartesian coordinates.

A canonically-integrated straight dipole magnet, assumed to have multipoles defined in Cartesian coordinates.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name        | Units   | Type   | Default | Description   |
|-----------------------|---------|--------|---------|---|
| L                     | $M$     | double | 0.0     | arc length (not chord length!)                          |
| ANGLE                 | $RAD$   | double | 0.0     | bend angle  |
| K1                    | $1/M^2$ | double | 0.0     | geometric quadrupole strength                           |
| K2                    | $1/M^3$ | double | 0.0     | geometric sextupole strength                            |
| K3                    | $1/M^4$ | double | 0.0     | geometric octupole strength                             |
| K4                    | $1/M^5$ | double | 0.0     | geometric decapole strength                             |
| K5                    | $1/M^6$ | double | 0.0     | geometric 12-pole strength                              |
| K6                    | $1/M^7$ | double | 0.0     | geometric 14-pole strength                              |
| K7                    | $1/M^8$ | double | 0.0     | geometric 16-pole strength                              |
| K8                    | $1/M^9$ | double | 0.0     | geometric 18-pole strength                              |
| TILT                  | $RAD$   | double | 0.0     | rotation about incoming longitudinal axis               |
| YAW                   | $RAD$   | double | 0.0     | rotation about vertical axis through entrance point     |
| HGAP                  | $M$     | double | 0.0     | half-gap between poles                                  |
| FINT1                 |         | double | 0.0     | edge integral for entrance                              |
| FINT2                 |         | double | 0.0     | edge integral for exit                                  |
| DX                    | $M$     | double | 0.0     | misalignment  |
| DY                    | $M$     | double | 0.0     | misalignment  |
| DZ                    | $M$     | double | 0.0     | misalignment  |
| FSE                   |         | double | 0.0     | fractional strength error                               |
| FSE_DIPOLE            |         | double | 0.0     | fractional strength error of dipole component           |
| FSE_QUADRUPOLE        |         | double | 0.0     | fractional strength error of quadrupole component       |
| ETILT                 | $RAD$   | double | 0.0     | error rotation about incoming longitudinal axis         |
| N_KICKS               |         | long   | 4       | number of kicks   |
| INTEGRATION_ORDER     |         | short  | 4       | integration order (2 or 4)                              |
| SYSTEMATIC_MULTIPOLES |         | STRING | NULL    | input file for systematic multipoles                    |
| EDGE_MULTIPOLES       |         | STRING | NULL    | input file for systematic entrance/exit edge multipoles |

## CCBEND continued

A canonically-integrated straight dipole magnet, assumed to have multipoles defined in Cartesian coordinates.

| Parameter Name              | Units | Type   | Default | Description  |
|-----------------------------|-------|--------|---------|--|
| EDGE1_MULTIPOLES            |       | STRING | NULL    | input file for systematic entrance edge multipoles. Overrides EDGE_MULTIPOLES.   |
| EDGE2_MULTIPOLES            |       | STRING | NULL    | input file for systematic exit edge multipoles. Overrides EDGE_MULTIPOLES.   |
| RANDOM_MULTIPOLES           |       | STRING | NULL    | input file for random multipoles   |
| SYSTEMATIC_MULTIPOLE_FACTOR |       | double | 1       | Factor by which to multiply systematic and edge multipoles   |
| RANDOM_MULTIPOLE_FACTOR     |       | double | 1       | Factor by which to multiply random multipoles  |
| REFERENCE_ORDER             |       | short  | 0       | Reference order for multipole errors. Overridden by value in multipole files, if those are given.                                |
| SYNCH_RAD                   |       | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                         |       | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| ISR1PART                    |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| USE_RAD_DIST                |       | short  | 0       | If nonzero, overrides SYNCH_RAD and ISR, causing simulation of radiation from distributions, optionally including opening angle. |
| ADD_OPENING_ANGLE           |       | short  | 1       | If nonzero, radiation opening angle effects are added if USE_RAD_DIST is nonzero.  |
| OPTIMIZE_FSE                |       | short  | 1       | Optimize strength (FSE) to obtain the ideal deflection angle.  |

## CCBEND continued

A canonically-integrated straight dipole magnet, assumed to have multipoles defined in Cartesian coordinates.

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| OPTIMIZE_DX       |       | short  | 1       | Optimize x offset to obtain centered trajectory.   |
| OPTIMIZE_FSE_ONCE |       | short  | 0       | If nonzero, the FSE offset is optimized only once, even if relevant parameters are changed.  |
| OPTIMIZE_DX_ONCE  |       | short  | 0       | If nonzero, the x offset is optimized only once, even if relevant parameters are changed.  |
| COMPENSATE_KN     |       | short  | 0       | If nonzero, K1 and K2 strengths are adjusted to compensate for the changes in FSE needed to center the trajectory.   |
| EDGE_ORDER        |       | short  | 3       | Gives order of edge effects. Does not affect edge multipoles.  |
| VERBOSE           |       | short  | 0       | If nonzero, print messages showing optimized FSE and x offset.   |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element provides a symplectic straight-pole, bending magnet with the exact Hamiltonian in Cartesian coordinates. The quadrupole, sextupole, and other multipole terms are defined in Cartesian coordinates. The magnet at present is restricted to having rectangular ends with symmetric entry and exit. This is quite different from *CSBEND*, where the edge angles are user-defined and where the field expansion is in curvilinear coordinates. Strictly speaking, *CSBEND* is only valid when the dipole is built with curved, beam-following poles.

Integration of particles in *CCBEND* is very similar to what's done for *KQUAD*, *KSEXT*, and *KOCT*. The only real difference is that coordinate transformations are performed at the entrance and exit to orient the incoming central trajectory to the straight magnet axis. In addition, the fractional strength error is adjusted to ensure that the outgoing central trajectory is correct.

By default, two adjustments are made at start-up and whenever the length, angle, gradient, or sextupole term change:

1. The fractional strength error is altered to ensure the correct deflecting angle. This is required because the bending field varies along the trajectory. By default, this affects all field compo-



nents together, per the usual convention in `elegant`. To restrict the strength change to the dipole term, set `COMPENSATE_KN=1`. To turn off this optimization, set `OPTIMIZE_FSE=0`.

2. The transverse position is adjusted to center the trajectory in the magnet. If the sagitta is  $\sigma$  and `ANGLE` is positive, the initial and final  $x$  coordinates are  $x = -\sigma/2$ , while the center coordinate is  $x = \sigma/2$ . To turn off this optimization, set `OPTIMIZE_DX=0`.

One can block the re-optimization of these parameters by setting `OPTIMIZE_FSE_ONCE` and `OPTIMIZE_DX_ONCE` to 1. Note also that the optimization is performed with all error-defining parameters (`DX`, `DY`, `DZ`, `FSE`, and `ETILT`) set to zero.

#### Edge angles and edge effects

The edge angle treatment in `CCBEND` is relatively simple, consisting of a vertical focusing effect with momentum dependence to all orders. Also included are edge pseudo-sextupoles (due to the body  $K_1$  term) and pseudo-octupoles (due to the body  $K_2$  term). The user may also specify edge multipoles using the `EDGE_MULTIPOLE` parameter.

#### Multipole errors

Multipole errors are specified for the body and edge in the same fashion as for the `KQUAD` element. The reference is the dipole field by default, but this may be changed using the `REFERENCE_ORDER` parameter.

#### Radiation effects

Incoherent synchrotron radiation, when requested with `ISR=1`, normally uses gaussian distributions for the excitation of the electrons. Setting `USE_RAD_DIST=1` invokes a more sophisticated algorithm that uses correct statistics for the photon energy and number distributions. In addition, if `USE_RAD_DIST=1` one may also set `ADD_OPENING_ANGLE=1`, which includes the photon angular distribution when computing the effect on the emitting electron.

#### Adding errors

When adding errors, care should be taken to choose the right parameters. The `FSE` and `ETILT` parameters are used for assigning errors to the strength and alignment relative to the ideal values given by `ANGLE` and `TILT`. One can also assign errors to `ANGLE` and `TILT`, but this has a different meaning: in this case, one is assigning errors to the survey itself. The reference beam path changes, so there is no orbit/trajectory error. The most common thing is to assign errors to `FSE` and `ETILT`. Note that when adding errors to `FSE`, the error is assumed to come from the power supply, which means that multipole strengths also change.

#### Splitting dipoles

The `CCBEND` element does not support splitting. **Important:** Users *should not* attempt to split `CCBEND` elements by hand, since this will not result in the correct geometry entering and exiting the various parts.

#### Matrix generation

`elegant` will use tracking to determine the transport matrix for `CCBEND` elements, which is needed for computation of twiss parameters and other operations. This can require some time, so `elegant` will cache the matrices and re-use them for identical elements.

## CENTER

### 10.11 CENTER—An element that centers the beam transversely on the ideal trajectory.

An element that centers the beam transversely on the ideal trajectory.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| X              |       | long   | 1       | center x coordinates?  |
| XP             |       | long   | 1       | center x' coordinates?   |
| Y              |       | long   | 1       | center y coordinates?  |
| YP             |       | long   | 1       | center y' coordinates?   |
| S              |       | long   | 0       | center s coordinates?  |
| DELTA          |       | long   | 0       | center delta coordinates?  |
| T              |       | long   | 0       | center t coordinates?  |
| ONCE_ONLY      |       | long   | 0       | compute centering offsets for first beam only, apply to all?   |
| ON_PASS        |       | long   | -1      | If nonnegative, do centering on the nth pass only.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## CEPL

### 10.12 CEPL—A numerically-integrated linearly-ramped electric field deflector.

A numerically-integrated linearly-ramped electric field deflector.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| L               | $M$   | double | 0.0         | length   |
| RAMP_TIME       | $S$   | double | 1e-09       | time to ramp to full strength  |
| TIME_OFFSET     | $S$   | double | 0.0         | offset of ramp-start time  |
| VOLTAGE         | $V$   | double | 0.0         | maximum voltage between plates due to ramp   |
| GAP             | $M$   | double | 0.01        | gap between plates   |
| STATIC_VOLTAGE  | $V$   | double | 0.0         | static component of voltage  |
| TILT            | $RAD$ | double | 0.0         | rotation about longitudinal axis   |
| ACCURACY        |       | double | 0.0001      | integration accuracy   |
| X_MAX           | $M$   | double | 0.0         | x half-aperture  |
| Y_MAX           | $M$   | double | 0.0         | y half-aperture  |
| DX              | $M$   | double | 0.0         | misalignment   |
| DY              | $M$   | double | 0.0         | misalignment   |
| PHASE_REFERENCE |       | long   | 0           | phase reference number (to link with other time-dependent elements)  |
| N_STEPS         |       | long   | 100         | number of steps (for nonadaptive integration)  |
| METHOD          |       | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL        |       | STRING | t,median    | {t p},{median min max ave first light} (e.g., "t,median")  |
| GROUP           |       | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## CHARGE

### 10.13 CHARGE—An element to establish the total charge of a beam. Active on first pass only. If given, overrides all charge specifications on other elements.

An element to establish the total charge of a beam. Active on first pass only. If given, overrides all charge specifications on other elements.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name     | Units       | Type   | Default | Description  |
|--------------------|-------------|--------|---------|--|
| TOTAL              | $C$         | double | 0.0     | total charge in beam   |
| PER_PARTICLE       | $C$         | double | 0.0     | charge per macroparticle   |
| ALLOW_TOTAL_CHANGE | <i>NULL</i> | long   | 0       | If nonzero, allow total charge to change while tracking even if number of particles does not change. Useful for ramping of charge.                         |
| GROUP              |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This is the preferred way to assign charge to a beam, which is needed for the use of CSR simulation (CSRCSBEND, CSRDRIFT), wake simulation (WAKE, TRWAKE, LRWAKE, ZLONGIT, ZTRANSVERSE), rf mode simulation (RFMODE, TRFMODE, FRFMODE, RTRFMODE), space charge simulation (LSCDRIFT, RFCW, SCMULT), and intrabeam scattering simulation (IBSCATTER).

## CLEAN

### 10.14 CLEAN—Cleans the beam by removing outlier particles.

Cleans the beam by removing outlier particles.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default     | Description  |
|----------------|-------|--------|-------------|--|
| MODE           |       | STRING | stdeviation | stdeviation, absdeviation, or absvalue   |
| XLIMIT         |       | double | 0.0         | Limit for x  |
| XPLIMIT        |       | double | 0.0         | Limit for x'   |
| YLIMIT         |       | double | 0.0         | Limit for y  |
| YPLIMIT        |       | double | 0.0         | Limit for y'   |
| TLIMIT         |       | double | 0.0         | Limit for t  |
| DELTALIMIT     |       | double | 0.0         | Limit for $(p-p_0)/p_0$  |
| GROUP          |       | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## CORGPIPE

### 10.15 CORGPIPE—A corrugated round pipe, commonly used as a dechirper in linacs.

A corrugated round pipe, commonly used as a dechirper in linacs.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| L               | $M$   | double | 0.0     | length   |
| RADIUS          | $M$   | double | 0.0     | pipe radius  |
| PERIOD          | $M$   | double | 0.0     | period of corrugations (<< radius recommended)   |
| GAP             | $M$   | double | 0.0     | gap in corrugations (< period required)  |
| DEPTH           | $M$   | double | 0.0     | depth of corrugations (<< radius, > period recommended)  |
| DT              | $S$   | double | 0.0     | maximum time duration of wake (0 for autoscale)  |
| TMAX            | $S$   | double | 0.0     | maximum time duration of wake (0 for autoscale)  |
| N_BINS          |       | long   | 0       | number of bins for charge histogram (0 for autoscale)  |
| INTERPOLATE     |       | long   | 0       | interpolate wake?  |
| SMOOTHING       |       | long   | 0       | Use Savitzky-Golay filter to smooth current histogram?   |
| SG_HALFWIDTH    |       | long   | 4       | Savitzky-Golay filter half-width for smoothing   |
| SG_ORDER        |       | long   | 1       | Savitzky-Golay filter order for smoothing  |
| CHANGE_P0       |       | long   | 0       | change central momentum?   |
| ALLOW_LONG_BEAM |       | long   | 0       | allow beam longer than wake data?  |
| RAMP_PASSES     |       | long   | 0       | Number of passes over which to linearly ramp up the wake to full strength.   |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element implements the longitudinal wake for a corrugated pipe using a model by K. Bane [38]. The method used is identical to that for the WAKE element. The only difference is that instead

of providing a file to specify the wake, one specifies the parameters of Bane's model, as described above.

Setting the `N_BINS` and `TMAX` parameters to 0 is recommended. This results in auto-scaling of the number of bins and the time spacing of the wake to ensure sufficient length to cover the beam and a sufficiently fine time step to resolve the oscillations in the wake.

As with `WAKE`, the default degree of smoothing (`SG_HALFWIDTH=4`) may be excessive. It is suggested that users vary this parameter to verify that results are reliable if smoothing is employed (`SMOOTHING=1`).

## CSBEND

### 10.16 CSBEND—A canonical kick sector dipole magnet.

A canonical kick sector dipole magnet.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default | Description                                       |
|----------------|---------|--------|---------|---|
| L              | $M$     | double | 0.0     | arc length  |
| ANGLE          | $RAD$   | double | 0.0     | bend angle  |
| K1             | $1/M^2$ | double | 0.0     | geometric quadrupole strength                     |
| K2             | $1/M^3$ | double | 0.0     | geometric sextupole strength                      |
| K3             | $1/M^4$ | double | 0.0     | geometric octupole strength                       |
| K4             | $1/M^5$ | double | 0.0     | geometric decapole strength                       |
| K5             | $1/M^6$ | double | 0.0     | geometric 12-pole strength                        |
| K6             | $1/M^7$ | double | 0.0     | geometric 14-pole strength                        |
| K7             | $1/M^8$ | double | 0.0     | geometric 16-pole strength                        |
| K8             | $1/M^9$ | double | 0.0     | geometric 18-pole strength                        |
| E1             | $RAD$   | double | 0.0     | entrance edge angle                               |
| E2             | $RAD$   | double | 0.0     | exit edge angle                                   |
| TILT           | $RAD$   | double | 0.0     | rotation about incoming longitudinal axis         |
| H1             | $1/M$   | double | 0.0     | entrance pole-face curvature                      |
| H2             | $1/M$   | double | 0.0     | exit pole-face curvature                          |
| HGAP           | $M$     | double | 0.0     | half-gap between poles                            |
| FINT           |         | double | 0.5     | edge-field integral                               |
| FINT1          |         | double | -1      | edge-field integral. If negative, use FINT.       |
| FINT2          |         | double | -1      | edge-field integral. If negative, use FINT.       |
| DX             | $M$     | double | 0.0     | misalignment                                      |
| DY             | $M$     | double | 0.0     | misalignment                                      |
| DZ             | $M$     | double | 0.0     | misalignment                                      |
| FSE            |         | double | 0.0     | fractional strength error of all components       |
| FSE_DIPOLE     |         | double | 0.0     | fractional strength error of dipole component     |
| FSE_QUADRUPOLE |         | double | 0.0     | fractional strength error of quadrupole component |
| ETILT          | $RAD$   | double | 0.0     | error rotation about incoming longitudinal axis   |



## CSBEND continued

A canonical kick sector dipole magnet.

| Parameter Name     | Units   | Type   | Default | Description   |
|--------------------|---------|--------|---------|---|
| N_KICKS            |         | long   | 4       | number of kicks   |
| NONLINEAR          |         | short  | 1       | include nonlinear field components?   |
| SYNCH_RAD          |         | short  | 0       | include classical, single-particle synchrotron radiation?                     |
| EDGE1_EFFECTS      |         | short  | 1       | include entrance edge effects?  |
| EDGE2_EFFECTS      |         | short  | 1       | include exit edge effects?  |
| EDGE_ORDER         |         | short  | 1       | order to which to include edge effects  |
| INTEGRATION_ORDER  |         | short  | 4       | integration order (2 or 4)  |
| EXPAND_HAMILTONIAN |         | short  | 0       | If 1, Hamiltonian is expanded to leading order.                               |
| EDGE1_KICK_LIMIT   |         | double | -1      | maximum kick entrance edge can deliver  |
| EDGE2_KICK_LIMIT   |         | double | -1      | maximum kick exit edge can deliver  |
| KICK_LIMIT_SCALING |         | short  | 0       | scale maximum edge kick with FSE?   |
| USE_BN             |         | short  | 0       | use $b_{<n>}$ instead of $K_{<n>}$ ?  |
| EXPANSION_ORDER    |         | short  | 0       | Order of field expansion. (0=auto)  |
| B1                 | $1/M$   | double | 0.0     | $K1 = b1/\rho$ , where $\rho$ is bend radius                                  |
| B2                 | $1/M^2$ | double | 0.0     | $K2 = b2/\rho$  |
| B3                 | $1/M^3$ | double | 0.0     | $K3 = b3/\rho$  |
| B4                 | $1/M^4$ | double | 0.0     | $K4 = b4/\rho$  |
| B5                 | $1/M^5$ | double | 0.0     | $K5 = b5/\rho$  |
| B6                 | $1/M^6$ | double | 0.0     | $K6 = b6/\rho$  |
| B7                 | $1/M^7$ | double | 0.0     | $K7 = b7/\rho$  |
| B8                 | $1/M^8$ | double | 0.0     | $K8 = b8/\rho$  |
| XREFERENCE         | $M$     | double | 0.0     | reference x for interpretation of fn values                                   |
| F1                 |         | double | 0.0     | Fractional normal field error $f_n = b_n * x^n / n!$ , adds to $K1$ or $b1$ . |

## CSBEND continued

A canonical kick sector dipole magnet.

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| F2             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , adds to K2 or b2. |
| F3             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| F4             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| F5             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| F6             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| F7             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| F8             |       | double | 0.0     | Fractional normal field error $f_n = b_n * x_{r\hat{n}} / n!$ , additive.         |
| G1             |       | double | 0.0     | Fractional skew field error.  |
| G2             |       | double | 0.0     | Fractional skew field error.  |
| G3             |       | double | 0.0     | Fractional skew field error.  |
| G4             |       | double | 0.0     | Fractional skew field error.  |
| G5             |       | double | 0.0     | Fractional skew field error.  |
| G6             |       | double | 0.0     | Fractional skew field error.  |
| G7             |       | double | 0.0     | Fractional skew field error.  |
| G8             |       | double | 0.0     | Fractional skew field error.  |
| ISR            |       | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?                    |
| ISR1PART       |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1                 |

## CSBEND continued

A canonical kick sector dipole magnet.

| Parameter Name           | Units     | Type   | Default | Description  |
|--------------------------|-----------|--------|---------|--|
| SQRT_ORDER               |           | short  | 0       | Ignored, kept for backward compatibility only.   |
| USE_RAD_DIST             |           | short  | 0       | If nonzero, overrides SYNCH_RAD and ISR, causing simulation of radiation from distributions, optionally including opening angle.                           |
| ADD_OPENING_ANGLE        |           | short  | 1       | If nonzero, radiation opening angle effects are added if USE_RAD_DIST is nonzero.  |
| PHOTON_OUTPUT_FILE       |           | STRING | NULL    | output file for photons, if USE_RAD_DIST=1   |
| PHOTON_LOW_ENERGY_CUTOFF | <i>eV</i> | double | 0.0     | Lower limit of photon energy to output.  |
| REFERENCE_CORRECTION     |           | short  | 0       | If nonzero, reference trajectory is subtracted from particle trajectories to compensate for inaccuracy in integration.                                     |
| TRACKING_MATRIX          |           | short  | 0       | If nonzero, gives order of tracking-based matrix up to third order to be used for twiss parameters etc. If zero, 2nd-order analytical matrix is used.      |
| FSE_CORRECTION           |           | short  | 0       | If nonzero, FSE is adjusted to compensate for edge effects when EDGE1_EFFECTS or EDGE2_EFFECTS = 2   |
| GROUP                    |           | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element provides a symplectic bending magnet with the exact Hamiltonian. For example, it retains all orders in the momentum offset and curvature. The field expansion is available to eighth order.

One pitfall of symplectic integration is the possibility of orbit and path-length errors for the reference orbit if too few kicks are used. This may be an issue for rings. Hence, one must verify that a sufficient number of kicks are being used by looking at the trajectory closure and length of an

on-axis particle by tracking. Using `INTEGRATION_ORDER=4` is recommended to reduce the number of required kicks.

As of version 28.0 and later, the `REFERENCE_CORRECTION` feature is available to compensate for errors inherent in the numerical integration of the trajectories. In particular, depending on the number of kicks used, as well as the bending radius and angle, an on-axis particle may emerge from the element with a non-zero trajectory and a path-length error. With `REFERENCE_CORRECTION` set to a non-zero value, these errors are subtracted from the coordinates of all particles. There are some pitfalls to using this feature: first, one may not realize that the number of kicks is too small to provide good results, since the output trajectory of the central particle will always be (nearly) identically zero. Second, in a magnet with a gradient or other field nonuniformities, a particle may emerge centered on the ideal trajectory yet still see the impact of the gradient, sextupole, etc. For these reasons, this feature should be used with caution and only when the residual trajectory is large enough to cause problems.

### Higher-order field components

Normally, one specifies the higher-order components of the field with the `Kn`, with  $n = 1$  through 8. The field expansion in the midplane is  $B_y(x) = B_o * (1 + \sum_{n=1}^8 \frac{K_n \rho_o}{n!} x^n)$ . By setting the `USE_bn` flag to a nonzero value, one may instead specify the `bn` parameters, which are defined by the expansion  $B_y(x) = B_o * (1 + \sum_{n=1}^8 \frac{b_n}{n!} x^n)$ . This is convenient if one is varying the dipole radius but wants to work in terms of constant field quality.

Setting `NONLINEAR=0` turns off all the terms above `K_1` (or `b_1`) and also turns off effects due to curvature that would normally result in a gradient producing terms of higher order.

The `EXPANSION_ORDER` parameter controls the order of the expansion of the nonlinear fields, so that terms are limited to  $x^i y^j$  with  $i+j \leq \text{EXPANSION\_ORDER}$ . By default, when `EXPANSION\_ORDER=0`, the expansion order is set automatically, as follows: If the highest non-zero multipole order (specified by `Kn`, `Bn`, `Fn`, or `Gn`) is  $n$  (with  $n = 1$  being quadrupole), then the expansion order is set to  $n + 3$ . However, the expansion order is never automatically set to less than 4, unless all the multipole terms are zero, in which case the expansion always yields a constant. Since the number of polynomial terms increases like the square of the expansion order, using many multipole terms can significantly increase run time. The maximum value for the expansion order is 10.

### Edge angles and edge effects

Some confusion may exist about the edge angles, particularly the signs. For a sector magnet, we have of course `E1=E2=0`. For a symmetric rectangular magnet, `E1=E2=ANGLE/2`. If `ANGLE` is negative, then so are `E1` and `E2`. To understand this, imagine a rectangular magnet with positive `ANGLE`. If the magnet is flipped over, then `ANGLE` becomes negative, as does the bending radius  $\rho$ . Hence, to keep the focal length of the edge  $1/f = -\tan E_i / \rho$  constant, we must also change the sign of  $E_i$ .

Several models are available for edge (or fringe) effects. Which is used depends on the settings of the `EDGE_ORDER`, `EDGE1_EFFECTS`, and `EDGE2_EFFECTS` parameters. `EDGE1_EFFECTS` controls entrance edge effects while `EDGE2_EFFECTS` controls exit edge effects, as follows:

- 1: — Edge effects using non-symplectic method [3].
  - `EDGE_ORDER<2` — linear edge focusing with  $\delta$ -dependence to all orders. Generally not recommended if symplecticity is important, though when the edge effects are weak it appears acceptable.
  - `EDGE_ORDER>=2` — second-order matrix edge focusing with  $\delta$ -dependence to all orders. Use of this model is strongly discouraged when symplecticity matters.

- 2: — Edge effects using K. Hwang’s symplectic method [45]. Note that there will be a trajectory offset when using this method that is particularly evident for small bending radii, due to extension of the fringe field outside the body of the magnet. To suppress this, adjustment of the FSE parameter can be performed automatically if `FSE_CORRECTION` is set to a non-zero value. If `FSE_CORRECTION=1`, the path-length is adjusted to match the nominal length, which is not physical; this behavior can be suppressed by setting `FSE_CORRECTION=2`.
  - `EDGE_ORDER<2` — include only terms linear in transverse coordinates, but  $\delta$ -dependence to all orders. Recommended for applications where symplecticity matters.
  - `EDGE_ORDER>=2` — include all terms. This settings has been observed to produce emittance damping in some cases (particularly with large emittance and small bending radii), so users are advised to be cautious.
- 3: — Edge effects using symplectic method similar to [3]. The value of `EDGE_ORDER` is ignored. Recommended for applications where symplecticity matters.
- Other: — No edge effects.

### Radiation effects

Incoherent synchrotron radiation, when requested with `ISR=1`, normally uses gaussian distributions for the excitation of the electrons. Setting `USE_RAD_DIST=1` invokes a more sophisticated algorithm that uses correct statistics for the photon energy and number distributions. In addition, if `USE_RAD_DIST=1` one may also set `ADD_OPENING_ANGLE=1`, which includes the photon angular distribution when computing the effect on the emitting electron.

### Adding errors

When adding errors, care should be taken to choose the right parameters. The `FSE` and `ETILT` parameters are used for assigning errors to the strength and alignment relative to the ideal values given by `ANGLE` and `TILT`. One can also assign errors to `ANGLE` and `TILT`, but this has a different meaning: in this case, one is assigning errors to the survey itself. The reference beam path changes, so there is no orbit/trajectory error. The most common thing is to assign errors to `FSE` and `ETILT`. Note that when adding errors to `FSE`, the error is assumed to come from the power supply, which means that multipole strengths also change.

### Splitting dipoles

When dipoles are long, it is common to want to split them into several pieces, to get a better look at the interior optics. When doing this, care must be exercised not to change the optics. `elegant` has some special features that are designed to reduce or manage potential problems. At issue is the need to turn off edge effects between the portions of the same dipole.

First, one can simply use the `divide_elements` command to set up the splitting. Using this command, `elegant` takes care of everything.

Second, one can use a series of dipoles *with the same name*. In this case, `elegant` automatically turns off interior edge effects. This is true when the dipole elements directly follow one another or are separated by a `MARK` element.

Third, one can use a series of dipoles with different names. In this case, one must also use the `EDGE1_EFFECTS` and `EDGE2_EFFECTS` parameters to turn off interior edge effects.

## CSRCSBEND

### 10.17 CSRCSBEND—Like CSBEND, but incorporates a simulation of Coherent Synchrotron radiation.

Like CSBEND, but incorporates a simulation of Coherent Synchrotron radiation.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description   |
|----------------|---------|--------|---------|---|
| L              | $M$     | double | 0.0     | arc length  |
| ANGLE          | $RAD$   | double | 0.0     | bend angle  |
| K1             | $1/M^2$ | double | 0.0     | geometric quadrupole strength                             |
| K2             | $1/M^3$ | double | 0.0     | geometric sextupole strength                              |
| K3             | $1/M^4$ | double | 0.0     | geometric octupole strength                               |
| K4             | $1/M^5$ | double | 0.0     | geometric decapole strength                               |
| K5             | $1/M^6$ | double | 0.0     | geometric 12-pole strength                                |
| K6             | $1/M^7$ | double | 0.0     | geometric 14-pole strength                                |
| K7             | $1/M^8$ | double | 0.0     | geometric 16-pole strength                                |
| K8             | $1/M^9$ | double | 0.0     | geometric 18-pole strength                                |
| E1             | $RAD$   | double | 0.0     | entrance edge angle                                       |
| E2             | $RAD$   | double | 0.0     | exit edge angle   |
| TILT           | $RAD$   | double | 0.0     | rotation about incoming longitudinal axis                 |
| H1             | $1/M$   | double | 0.0     | entrance pole-face curvature                              |
| H2             | $1/M$   | double | 0.0     | exit pole-face curvature                                  |
| HGAP           | $M$     | double | 0.0     | half-gap between poles                                    |
| FINT           |         | double | 0.5     | edge-field integral                                       |
| DX             | $M$     | double | 0.0     | misalignment  |
| DY             | $M$     | double | 0.0     | misalignment  |
| DZ             | $M$     | double | 0.0     | misalignment  |
| FSE            |         | double | 0.0     | fractional strength error                                 |
| ETILT          | $RAD$   | double | 0.0     | error rotation about incoming longitudinal axis           |
| N_KICKS        |         | long   | 4       | number of kicks   |
| NONLINEAR      |         | short  | 1       | include nonlinear field components?                       |
| LINEARIZE      |         | short  | 0       | use linear matrix instead of symplectic integrator?       |
| SYNCH_RAD      |         | short  | 0       | include classical, single-particle synchrotron radiation? |
| EDGE1_EFFECTS  |         | short  | 1       | include entrance edge effects?                            |

## CSRCSBEND continued

Like CSBEND, but incorporates a simulation of Coherent Synchrotron radiation.

| Parameter Name        | Units | Type   | Default | Description  |
|-----------------------|-------|--------|---------|--|
| EDGE2_EFFECTS         |       | short  | 1       | include exit edge effects?   |
| EDGE_ORDER            |       | short  | 1       | order to which to include edge effects   |
| INTEGRATION_ORDER     |       | short  | 4       | integration order (2 or 4)   |
| BINS                  |       | long   | 0       | number of bins for CSR wake  |
| BIN_ONCE              |       | short  | 0       | bin only at the start of the dipole?   |
| BIN_RANGE_FACTOR      |       | double | 1.2     | Factor by which to increase the range of histogram compared to total bunch length. Large value eliminates binning problems in CSRDRIFTs. |
| SG_HALFWIDTH          |       | short  | 0       | Savitzky-Golay filter half-width for smoothing current histogram. If less than 1, no SG smoothing is performed.                          |
| SG_ORDER              |       | short  | 1       | Savitzky-Golay filter order for smoothing current histogram  |
| SGDERIV_HALFWIDTH     |       | short  | 0       | Savitzky-Golay filter half-width for taking derivative of current histogram. Defaults to SG_HALFWIDTH (if positive) or else 1.           |
| SGDERIV_ORDER         |       | short  | 1       | Savitzky-Golay filter order for taking derivative of current histogram   |
| TRAPAZOID_INTEGRATION |       | short  | 1       | Select whether to use trapazoid-rule integration (default) or a simple sum.  |
| OUTPUT_FILE           |       | STRING | NULL    | output file for CSR wakes  |
| OUTPUT_INTERVAL       |       | long   | 1       | interval (in kicks) of output to OUTPUT_FILE   |
| OUTPUT_LAST_WAKE_ONLY |       | short  | 0       | output final wake only?  |
| STEADY_STATE          |       | short  | 0       | use steady-state wake equations?   |

## CSRCSBEND continued

Like CSBEND, but incorporates a simulation of Coherent Synchrotron radiation.

| Parameter Name           | Units   | Type   | Default | Description  |
|--------------------------|---------|--------|---------|--|
| IGF                      |         | short  | 0       | use integrated Greens function (requires STEADY_STATE=1)?  |
| USE_BN                   |         | short  | 0       | use b<n> instead of K<n>?  |
| EXPANSION_ORDER          |         | short  | 0       | Order of field expansion. (0=auto)   |
| B1                       | $1/M$   | double | 0.0     | $K1 = b1/\rho$ , where $\rho$ is bend radius   |
| B2                       | $1/M^2$ | double | 0.0     | $K2 = B2/\rho$   |
| B3                       | $1/M^3$ | double | 0.0     | $K3 = B3/\rho$   |
| B4                       | $1/M^4$ | double | 0.0     | $K4 = B4/\rho$   |
| B5                       | $1/M^5$ | double | 0.0     | $K5 = B5/\rho$   |
| B6                       | $1/M^6$ | double | 0.0     | $K6 = B6/\rho$   |
| B7                       | $1/M^7$ | double | 0.0     | $K7 = B7/\rho$   |
| B8                       | $1/M^8$ | double | 0.0     | $K8 = B8/\rho$   |
| ISR                      |         | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| ISR1PART                 |         | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| CSR                      |         | short  | 1       | enable CSR computations?   |
| BLOCK_CSR                |         | short  | 0       | block CSR from entering CSR-DRIFT?   |
| DERBENEV_CRITERION_MODE  |         | STRING | disable | disable, evaluate, or enforce  |
| PARTICLE_OUTPUT_FILE     |         | STRING | NULL    | name of file for phase-space output  |
| PARTICLE_OUTPUT_INTERVAL |         | long   | 0       | interval (in kicks) of output to PARTICLE_OUTPUT_FILE  |
| SLICE_ANALYSIS_INTERVAL  |         | long   | 0       | interval (in kicks) of output to slice analysis file (from slice_analysis command)   |
| LOW_FREQUENCY_CUTOFF0    |         | double | -1      | Highest spatial frequency at which low-frequency cutoff filter is zero. If not positive, no low-frequency cutoff filter is applied. Frequency is in units of Nyquist ( $0.5/\text{binsize}$ ). |



## CSRCSBEND continued

Like CSBEND, but incorporates a simulation of Coherent Synchrotron radiation.

| Parameter Name         | Units | Type   | Default | Description   |
|------------------------|-------|--------|---------|---|
| LOW_FREQUENCY_CUTOFF1  |       | double | -1      | Lowest spatial frequency at which low-frequency cutoff filter is 1. If not given, defaults to LOW_FREQUENCY_CUTOFF1.  |
| HIGH_FREQUENCY_CUTOFF0 |       | double | -1      | Spatial frequency at which smoothing (high-frequency cutoff) filter begins. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize). |
| HIGH_FREQUENCY_CUTOFF1 |       | double | -1      | Spatial frequency at which smoothing (high-frequency cutoff) filter is 0. If not given, defaults to HIGH_FREQUENCY_CUTOFF0.   |
| CLIP_NEGATIVE_BINS     |       | short  | 1       | If non-zero, then any bins with negative counts after the filters are applied have the counts set to zero.  |
| WAKE_FILTER_FILE       |       | STRING | NULL    | Name of file supplying wakefield filtering data.  |
| WFF_FREQ_COLUMN        |       | STRING | NULL    | Name of column supplying frequency values for wakefield filtering data.   |
| WFF_REAL_COLUMN        |       | STRING | NULL    | Name of column supplying real values for wakefield filtering data.  |
| WFF_IMAG_COLUMN        |       | STRING | NULL    | Name of column supplying imaginary values for wakefield filtering data.   |
| GROUP                  |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup                          |

For a discussion of the method behind this element, see M. Borland, “Simple method for particle tracking with coherent synchrotron radiation,” Phys. Rev. ST Accel. Beams 4, 070701 (2001) and G. Stupakov and P. Emma, SLAC LCLS-TN-01-12 (2001).

**Recommendations for using this element.** The default values for this element are not the best ones to use. They are retained only for consistency through upgrades. In using this element, it is recommended to have 50 to 100 k particle in the simulation. Setting `BINS=600` and `SG_HALFWIDTH=1` is also recommended to allow resolution of fine structure in the beam and to avoid excessive smoothing. It is strongly suggested that the user vary these parameters and view the histogram output to verify that the longitudinal distribution is well represented by the histograms (use `OUTPUT_FILE` to obtain the histograms). For LCLS simulations, we find that the above parameters give essentially the same results as obtained with 500 k particles and up to 3000 bins.

In order to verify that the 1D approximation is valid, the user should also set `DERBENEV_CRITERION_MODE = 'evaluate'` and view the data in `OUTPUT_FILE`. Generally, the criterion should be much less than 1. See equation 11 of [20].

In order respects, this element is just like the `CSBEND` element, which provides a symplectic bending magnet that is accurate to all orders in momentum offset. Please see the manual page for `CSBEND` for more details about features not related to CSR.

**Splitting dipoles:** Splitting dipoles with continuation of CSR effects is possible provided the dipole sections (all of which must have the same name) are either consecutive or separated only by `MARK`, `WATCH`, or `LSCDRIFT` elements. The `LSCDRIFT` elements must have `L=0` and should have `LEFFECTIVE` set to the length of the upstream dipole segment. This allows simulating LSC and CSR within a single dipole.

## CSRDRIFT

### 10.18 CSRDRIFT—A follow-on element for CSRCSBEND that applies the CSR wake over a drift.

A follow-on element for CSRCSBEND that applies the CSR wake over a drift.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name           | Units | Type   | Default       | Description  |
|--------------------------|-------|--------|---------------|--|
| L                        | $M$   | double | 0.0           | length   |
| ATTENUATION_LENGTH       | $M$   | double | 0.0           | exponential attenuation length for wake  |
| DZ                       |       | double | 0.0           | interval between kicks   |
| N_KICKS                  |       | long   | 1             | number of kicks (if DZ is zero)  |
| SPREAD                   |       | short  | 0             | use spreading function?  |
| USE_OVERTAKING_LENGTH    |       | short  | 0             | use overtaking length for ATTENUATION_LENGTH?                                      |
| OL_MULTIPLIER            |       | double | 1             | factor by which to multiply the overtaking length to get the attenuation length    |
| CSR                      |       | short  | 1             | do CSR calculations  |
| USE_SALDIN54             |       | short  | 0             | Use Saldin et al eq. 54 (NIM A 398 (1997) 373-394 for decay vs $z$ ?               |
| SALDIN54POINTS           |       | long   | 1000          | Number of values of position inside bunch to average for Saldin eq 54.             |
| SALDIN54NORM_MODE        |       | STRING | peak          | peak or first  |
| SPREAD_MODE              |       | STRING | full          | full, simple, or radiation-only  |
| WAVELENGTH_MODE          |       | STRING | sigmaz        | sigmaz or peak-to-peak   |
| BUNCHLENGTH_MODE         |       | STRING | 68-percentile | rms, 68-percentile, or 90-percentile   |
| SALDIN54_OUTPUT          |       | STRING | NULL          | Filename for output of CSR intensity vs. $z$ as computed using Saldin eq 54.       |
| USE_STUPAKOV             |       | short  | 0             | Use treatment from G. Stupakov's note of 9/12/2001?                                |
| STUPAKOV_OUTPUT          |       | STRING | NULL          | Filename for output of CSR wake vs. $s$ as computed using Stupakov's equations.    |
| STUPAKOV_OUTPUT_INTERVAL |       | long   | 1             | Interval (in kicks) between output of Stupakov wakes.                              |
| SLICE_ANALYSIS_INTERVAL  |       | long   | 0             | interval (in kicks) of output to slice analysis file (from slice_analysis command) |

## CSRDRIFT continued

A follow-on element for CSRCSBEND that applies the CSR wake over a drift.

| Parameter Name             | Units | Type   | Default | Description   |
|----------------------------|-------|--------|---------|---|
| LINEARIZE                  |       | short  | 0       | use linear optics for drift pieces?   |
| LSC_INTERPOLATE            |       | short  | 1       | Interpolate computed LSC wake?  |
| LSC_BINS                   |       | long   | 0       | If non-zero, include LSC with given number of bins.   |
| LSC_LOW_FREQUENCY_CUTOFF0  |       | double | -1      | Highest spatial frequency at which low-frequency cutoff filter is zero. If not positive, no low-frequency cutoff filter is applied. Frequency is in units of Nyquist (0.5/binsize). |
| LSC_LOW_FREQUENCY_CUTOFF1  |       | double | -1      | Lowest spatial frequency at which low-frequency cutoff filter is 1. If not given, defaults to LOW_FREQUENCY_CUTOFF1.  |
| LSC_HIGH_FREQUENCY_CUTOFF0 |       | double | -1      | Spatial frequency at which smoothing filter begins for LSC. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize).                 |
| LSC_HIGH_FREQUENCY_CUTOFF1 |       | double | -1      | Spatial frequency at which smoothing filter is 0 for LSC. If not given, defaults to HIGH_FREQUENCY_CUTOFF0.   |
| LSC_RADIUS_FACTOR          |       | double | 1.7     | Radius factor for LSC computation.  |
| GROUP                      |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup                          |

This element has a number of models for simulation of CSR in drift spaces following CSRCSBEND elements. Note that all models allow support splitting the drift into multiple CSRDRIFT elements. One can also have intervening elements like quadrupoles, as often happens in chicanes. The CSR effects inside such intervening elements are applied in the CSRDRIFT downstream of the element.

For a discussion of some of the methods behind this element, see M. Borland, “Simple method

for particle tracking with coherent synchrotron radiation,” Phys. Rev. ST Accel. Beams 4, 070701 (2001).

**N.B.:** by default, this element uses 1 CSR kick (`N_KICKS=1`) at the center of the drift. This is usually not a good choice. I usually use the `DZ` parameter instead of `N_KICKS`, and set it to something like 0.01 (meters). The user should vary this parameter to assess how small it needs to be.

The models are as following, in order of decreasing sophistication and accuracy:

- G. Stupakov’s extension of Saldin et al. Set `USE_STUPAKOV=1`. The most advanced model at present is based on a private communication from G. Stupakov (SLAC), which extends equation 87 of the one-dimensional treatment of Saldin et al. (NIM A 398 (1997) 373-394) to include the post-dipole region. This model includes not only the attenuation of the CSR as one proceeds along the drift, but also the change in the shape of the “wake.”

This model has the most sophisticated treatment for intervening elements of any of the models. For example, if you have a sequence `CSRCSBEND-CSRDRIFT-CSRDRIFT` and compare it with the sequence `CSRCSBEND-CSRDRIFT-DRIFT-CSRDRIFT`, keeping the total drift length constant, you’ll find no change in the CSR-induced energy modulation. The model back-propagates to the beginning of the intervening element and performs the CSR computations starting from there.

This is the slowest model to run. It uses the same binning and smoothing parameters as the upstream `CSRCSBEND`. If run time is a problem, compare it to the other models and use only if you get different answers.

- M. Borland’s model based on Saldin et al. equations 53 and 54. Set `USE_SALDIN54=1`. This model computes the fall-off of the CSR wake from the work of Saldin and coworkers, as described in the reference above. It does not compute the change in the shape of the wake. The fall-off is computed approximately as well, based on the fall-off for a rectangular current distribution. The length of this rectangular bunch is taken to be twice the bunch length computed according to the `BUNCHLENGTH_MODE` parameter (see below). If your bunch is nearly rectangular, then you probably want `BUNCHLENGTH_MODE` of “90-percentile”.
- Exponential attenuation of a CSR wake with unchanging shape. There are two options here. First, you can provide the attenuation length yourself, using the `ATTENUATION_LENGTH` parameter. Second, you can set `USE_OVERTAKING_LENGTH=1` and let **elegant** compute the overtaking length for use as the attenuation length. In addition, you can multiply this result by a factor if you wish, using the `OL_MULTIPLIER` parameter.
- Beam-spreading model. This model is not recommended. It is based on the seemingly plausible idea that CSR spreads out just like any synchrotron radiation, thus decreasing the intensity. The model doesn’t reproduce experiments.

The “Saldin 54” and “overtaking-length” models rely on computation of the bunch length, which is controlled with the `BUNCHLENGTH_MODE` parameter. Nominally, one should use the true RMS, but when the beam has temporal spikes, it isn’t always clear that this is the best choice. The choices are “rms”, “68-percentile”, and “90-percentile”. The last two imply using half the length determined from the given percentile in place of the rms bunch length. I usually use 68-percentile, which is the default.

## CWIGGLER

### 10.19 CWIGGLER—Tracks through a wiggler using canonical integration routines of Y. Wu (Duke University).

Tracks through a wiggler using canonical integration routines of Y. Wu (Duke University).

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name    | Units       | Type   | Default | Description  |
|-------------------|-------------|--------|---------|--|
| L                 | $M$         | double | 0.0     | Total length   |
| B_MAX             | $T$         | double | 0.0     | Maximum on-axis magnetic field.  |
| BX_MAX            | $T$         | double | 0.0     | Maximum on-axis magnetic field. Ignored if B_MAX is nonzero.                             |
| BY_MAX            | $T$         | double | 0.0     | Maximum on-axis magnetic field. Ignored if B_MAX is nonzero.                             |
| TGU_GRADIENT      | $1/M$       | double | 0.0     | Transverse gradient divided by maximum on-axis field, used if TGU=1.                     |
| TGU_COMP_FACTOR   | <i>NULL</i> | double | 1       | Use to adjust constant field component to reduce trajectory error.                       |
| POLE1_FACTOR      | <i>NULL</i> | double | 1       | Use to adjust first and last pole strength, e.g., to reduce trajectory error.            |
| POLE2_FACTOR      | <i>NULL</i> | double | 1       | Use to adjust second and penultimate pole strength, e.g., to reduce trajectory error.    |
| POLE3_FACTOR      | <i>NULL</i> | double | 1       | Use to adjust third and third-from-last pole strength, e.g., to reduce trajectory error. |
| DX                | $M$         | double | 0.0     | Misalignment.  |
| DY                | $M$         | double | 0.0     | Misalignment.  |
| DZ                | $M$         | double | 0.0     | Misalignment.  |
| TILT              | $RAD$       | double | 0.0     | Rotation about beam axis.  |
| PERIODS           |             | long   | 0       | Number of wiggler periods.   |
| STEPS_PER_PERIOD  |             | long   | 10      | Integration steps per period.  |
| INTEGRATION_ORDER |             | short  | 4       | Integration order (2 or 4).  |
| BY_FILE           |             | STRING | NULL    | Name of SDDS file with By harmonic data.   |

## CWIGGLER continued

Tracks through a wiggler using canonical integration routines of Y. Wu (Duke University).

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| BX_FILE        |       | STRING | NULL    | Name of SDDS file with Bx harmonic data.  |
| BY_SPLIT_POLE  |       | short  | 0       | Use "split-pole" expansion for By?  |
| BX_SPLIT_POLE  |       | short  | 0       | Use "split-pole" expansion for Bx?  |
| SYNCH_RAD      |       | short  | 0       | Include classical, single-particle synchrotron radiation?   |
| ISR            |       | short  | 0       | Include incoherent synchrotron radiation (quantum excitation)?  |
| ISR1PART       |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1   |
| SINUSOIDAL     |       | short  | 0       | Ideal sinusoidal wiggler? If non-zero, BX_FILE and BY_FILE are not used.  |
| VERTICAL       |       | short  | 0       | If SINUSOIDAL is non-zero, then setting this to non-zero gives a vertical wiggler. Default is horizontal.   |
| HELICAL        |       | short  | 0       | Ideal helical wiggler? If non-zero and SINUSOIDAL is also non-zero, BX_FILE and BY_FILE are not used.   |
| TGU            |       | short  | 0       | Ideal transverse gradient undulator? If non-zero and SINUSOIDAL is also non-zero, BX_FILE and BY_FILE are not used. Give gradient in TGU_GRADIENT.                |
| FORCE_MATCHED  |       | short  | 1       | Force matched dispersion for first harmonics? If non-zero, start and end of magnetic field will be inset from the ends of the device if phase is not 0 or $\pi$ . |

## CWIGGLER continued

Tracks through a wiggler using canonical integration routines of Y. Wu (Duke University).

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| FIELD_OUTPUT   |       | STRING | NULL    | Name of file to which field samples will be written. Slow, so use only for debugging.  |
| VERBOSITY      |       | short  | 0       | A higher value requires more detailed printouts related to computations.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a wiggler or undulator using a modified version of Ying Wu's canonical integration code for wigglers. To use the element, one must supply an SDDS file giving harmonic analysis of the wiggler field. The field expansion used by the code for a horizontally-deflecting wiggler is (Y. Wu, Duke University, private communication).

$$B_y = -|B_0| \sum_{m,n} C_{mn} \cos(k_{xl}x) \cosh(k_{ym}y) \cos(k_{zn}z + \theta_{zn}), \quad (29)$$

where  $|B_0|$  is the peak value of the on-axis magnetic field, the  $C_{mn}$  give the relative amplitudes of the harmonics, the wavenumbers satisfy  $k_{ym}^2 = k_{xl}^2 + k_{zn}^2$ , and  $\theta_{zn}$  is the phase.

The file must contain the following columns:

- The harmonic amplitude,  $C_{mn}$ , in column **Cmn**.
- The phase, in radians, in column **Phase**. The phase of the first harmonic should be 0 or  $\pi$  in order to have matched dispersion.
- The three wave numbers, normalized to  $k_w = 2\pi/\lambda_w$ , where  $\lambda_w$  is the wiggler period. These are given in columns **KxOverKw**, **KyOverKw**, and **KzOverKw**.

In Version 17.3 and later, for matrix computations **elegant** uses a first-order matrix derived from particle tracking when it encounterse a CWIGGLER. Tests show that this gives good agreement in the tunes from tracking and Twiss parameter calculations. For radiation integrals, an idealized sinusoidal wiggler model is used with bending radius equal to  $B\rho/(B_0 \sum C_{mn})$  for each plane. Energy loss, energy spread, and horizontal emittance should be estimated accurately.

**elegant** allows specifying field expansions for on-axis  $B_y$  and  $B_x$  components, so one can model a helical wiggler. However, in this case one set of components should have  $\theta_{zn} = 0$  or  $\theta_{zn} = \pi$ , while the other should have  $\theta_{zn} = \pm\pi/2$ . Using Wu's code, the latter set will not have matched dispersion. Our modified version solves this by delaying the beginning of the field components in question by  $\lambda/4$  and ending the field prematurely by  $3\lambda/4$ . This causes all the fields to start and end at the crest, which ensures matched dispersion. The downside is that the (typically) vertical



wiggler component is missing a full period of field. One can turn off this behavior by setting `FORCE_MATCHED=0`.

#### Additional field expansions

Y. Wu's code included field expansions for a vertically-deflecting wiggler as well as the horizontally-deflecting wiggler given above. In both cases, these expansions are suitable for a wiggler with two poles that are above/below or left/right of the beam axis. They are not always suitable for devices with more complex pole geometries.

Another geometry that is important is a "split pole" wiggler, in which each pole is made from two pieces. Such configurations are seen, for example, in devices used to produce variable polarization. In such cases, the expansion given above may not be appropriate. Here, we summarize the form of the various expansions that `elegant` supports. For brevity, we show the form of a single harmonic component.

Horizontal wiggler, normal poles, produces  $B_y$  only on-axis. Specified by setting `BY_SPLIT_POLE=0`, and giving `BY_FILE` or `SINUSOIDAL=1` with `VERTICAL=0`.

$$B_x = |B_0| \frac{k_x \cos(k_z z + \phi) \sin(k_x x) \sinh(k_y y)}{k_y} \quad (30)$$

$$B_y = -|B_0| \cos(k_x x) \cos(k_z z + \phi) \cosh(k_y y) \quad (31)$$

where  $k_y^2 = k_x^2 + k_z^2$ .

**Experimental feature:** Horizontal wiggler, normal poles, with transverse gradient, produces  $B_y$  only on-axis. Specified by setting `BY_SPLIT_POLE=0`, `SINUSOIDAL=1`, `TGU=1`, `VERTICAL=0`. The TGU normalized gradient is given using the `TGU_GRADIENT` parameter. Taking  $a$  as the normalized gradient, the fields are[54]

$$B_x = \frac{a |B_0| \sinh k_u y \cos k_u z}{k_u} \quad (32)$$

$$B_y = |B_0| \left( (1 + ax) \cosh k_u y \cos k_u z + \frac{aC}{2k_u^2} \frac{e |B_0|}{\gamma m_e c} \right) \quad (33)$$

$$B_z = -|B_0| (1 + ax) \sinh k_u y \sin k_u z, \quad (34)$$

where  $k_u = k_y = k_z$ ,  $k_x = 0$  is assumed,  $\gamma$  is the central relativistic factor for the beam and  $C$  is given by the `TGU_COMP_FACTOR` parameter. This factor, and the term it multiplies, is present in order to help suppress the trajectory error at the end of the device. It may require adjustment in order to achieve the desired level of correction. In addition, the user may need to adjust the pole-strength factors and include external misalignments and steering magnets in order to suppress not only the trajectory error, but also dispersion errors.

Horizontal wiggler, split poles, produces  $B_y$  only on-axis. Specified by setting `BY_SPLIT_POLE=1`, and giving `BY_FILE` or `SINUSOIDAL=1` with `VERTICAL=0`.

$$B_x = -|B_0| \frac{k_x \cos(k_z z + \phi) \sin(k_y y) \sinh(k_x x)}{k_y} \quad (35)$$

$$B_y = -|B_0| \cos(k_y y) \cos(k_z z + \phi) \cosh(k_x x) \quad (36)$$

where  $k_x^2 = k_y^2 + k_z^2$ .

Vertical wiggler, normal poles, produces  $B_x$  only on-axis. Specified by setting `BX_SPLIT_POLE=0`, and giving `BX_FILE` or `SINUSOIDAL=1` with either `VERTICAL=1` or `HELICAL=1`.

$$B_x = |B_0| \cos(k_y y) \cos(k_z z + \phi) \cosh(k_x x) \quad (37)$$

$$B_y = -|B_0| \frac{k_y \cos(k_z z + \phi) \sin(k_y y) \sinh(k_x x)}{k_x} \quad (38)$$

where  $k_x^2 = k_y^2 + k_z^2$ .

Vertical wiggler, split poles, produces  $B_x$  only on-axis. Specified by setting `BX_SPLIT_POLE=1`, and giving `BX_FILE` or `SINUSOIDAL=1` with either `VERTICAL=1` or `HELICAL=1`.

$$B_x = |B_0| \cos(k_x x) \cos(k_z z + \phi) \cosh(k_y y) \quad (39)$$

$$B_y = |B_0| \frac{k_y \cos(k_z z + \phi) \sin(k_x x) \sinh(k_y y)}{k_x} \quad (40)$$

where  $k_y^2 = k_x^2 + k_z^2$ .

## DRIF

### 10.20 DRIF—A drift space implemented as a matrix, up to 2nd order. Use EDRIFT for symplectic tracking.

A drift space implemented as a matrix, up to 2nd order. Use EDRIFT for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| ORDER          |       | short  | 0       | matrix order   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## DSCATTER

### 10.21 DSCATTER—A scattering element to add random changes to particle coordinates according to a user-supplied distribution function

A scattering element to add random changes to particle coordinates according to a user-supplied distribution function

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| PLANE           |       | STRING | NULL    | Plane to scatter: xp, yp, dp (dp is deltaP/P)  |
| FILENAME        |       | STRING | NULL    | Name of SDDS file containing distribution function.  |
| VALUENAME       |       | STRING | NULL    | Name of column containing the independent variable for the distribution function data.             |
| CDFNAME         |       | STRING | NULL    | Name of column containing the cumulative distribution function data.                               |
| PDFNAME         |       | STRING | NULL    | Name of column containing the probability distribution function data.                              |
| ONCEPERPARTICLE |       | long   | 0       | If nonzero, each particle can only get scattered once by this element.                             |
| FACTOR          |       | double | 1       | Factor by which to multiply the independent variable values.                                       |
| PROBABILITY     |       | double | 1       | Probability that any particle will be selected for scattering.                                     |
| GROUPLD         |       | long   | -1      | Group ID number (nonnegative integer) for linking once-per-particle behavior of multiple elements. |
| RANDOMSIGN      |       | long   | 0       | If non-zero, then the scatter is given a random sign. Useful if distribution data is one-sided.    |
| LIMITPERPASS    |       | long   | -1      | Maximum number of particles that will be scattered on each pass.                                   |
| LIMITTOTAL      |       | long   | -1      | Maximum number of particles that will be scatter for each step.                                    |

## DSCATTER continued

A scattering element to add random changes to particle coordinates according to a user-supplied distribution function

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| STARTONPASS    |       | long   | 0       | Pass number to start on.   |
| ENDONPASS      |       | long   | -1      | Pass number to end on (inclusive). Ignored if negative.  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## ECOL

### 10.22 ECOL—An elliptical collimator.

An elliptical collimator.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| X_MAX          | $M$   | double | 0.0     | half-axis in x   |
| Y_MAX          | $M$   | double | 0.0     | half-axis in y   |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| OPEN_SIDE      |       | STRING | NULL    | which side, if any, is open (+x, -x, +y, -y)   |
| EXPONENT       |       | short  | 2       | Exponent for boundary equation. 2 is ellipse.  |
| YEXPONENT      |       | short  | 0       | y exponent for boundary equation. 2 is ellipse. If 0, defaults to EXPONENT   |
| INVERT         |       | short  | 0       | If non-zero, particles inside the aperture are lost while those outside are transmitted.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## EDRIFT

### 10.23 EDRIFT—Tracks through a drift with no approximations (Exact DRIFT).

Tracks through a drift with no approximations (Exact DRIFT).

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## EHKICK

### 10.24 EHKICK—A horizontal steering dipole implemented using an exact hard-edge model

A horizontal steering dipole implemented using an exact hard-edge model

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name            | Units      | Type   | Default | Description  |
|---------------------------|------------|--------|---------|--|
| L                         | <i>M</i>   | double | 0.0     | length   |
| KICK                      | <i>RAD</i> | double | 0.0     | kick angle   |
| TILT                      | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX                        | <i>M</i>   | double | 0.0     | misalignment   |
| DY                        | <i>M</i>   | double | 0.0     | misalignment   |
| DZ                        | <i>M</i>   | double | 0.0     | misalignment   |
| CALIBRATION               |            | double | 1       | factor applied to obtain kick  |
| LERAD                     |            | double | 0.0     | if L=0, use this length for radiation computations   |
| STEERING                  |            | short  | 1       | use for steering?  |
| SYNCH_RAD                 |            | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                       |            | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| STEERING_MULTIPOLES       |            | STRING | NULL    | input file for systematic multipole content of steering kicks  |
| RANDOM_MULTIPOLES         |            | STRING | NULL    | input file for random multipoles content of steering kicks   |
| RANDOM_MULTIPOLE_FACTOR   |            | double | 1       | Factor by which to multiply random multipoles  |
| STEERING_MULTIPOLE_FACTOR |            | double | 1       | Factor by which to multiply steering multipoles  |
| GROUP                     |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Note that `closed_orbit` and `correct` command may report orbit convergence problems when using EHKICK in place of HKICK. This may be resolved by increasing the `closed_orbit_accuracy` parameter.

If requested, synchrotron radiation effects are imposed as a kick at the end of the element.



## EKICKER

### 10.25 EKICKER—A combined horizontal/vertical steering dipole implemented using an exact hard-edge model

A combined horizontal/vertical steering dipole implemented using an exact hard-edge model

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name            | Units      | Type   | Default | Description  |
|---------------------------|------------|--------|---------|--|
| L                         | <i>M</i>   | double | 0.0     | length   |
| HKICK                     | <i>RAD</i> | double | 0.0     | horizontal kick angle  |
| VKICK                     | <i>RAD</i> | double | 0.0     | vertical kick angle  |
| TILT                      | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX                        | <i>M</i>   | double | 0.0     | misalignment   |
| DY                        | <i>M</i>   | double | 0.0     | misalignment   |
| DZ                        | <i>M</i>   | double | 0.0     | misalignment   |
| HCALIBRATION              |            | double | 1       | factor applied to obtain horizontal kick   |
| VCALIBRATION              |            | double | 1       | factor applied to obtain vertical kick   |
| LERAD                     |            | double | 0.0     | if L=0, use this length for radiation computations   |
| STEERING                  |            | short  | 1       | use for steering?  |
| SYNCH_RAD                 |            | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                       |            | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| STEERING_MULTIPOLES       |            | STRING | NULL    | input file for systematic multipole content of steering kicks  |
| RANDOM_MULTIPOLES         |            | STRING | NULL    | input file for random multipoles content of steering kicks   |
| RANDOM_MULTIPOLE_FACTOR   |            | double | 1       | Factor by which to multiply random multipoles  |
| STEERING_MULTIPOLE_FACTOR |            | double | 1       | Factor by which to multiply steering multipoles  |
| GROUP                     |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Note that `closed_orbit` and `correct` command may report orbit convergence problems when using `EKICKER` in place of `KICKER`. This may be resolved by increasing the `closed_orbit_accuracy` parameter.

If requested, synchrotron radiation effects are imposed as a kick at the end of the element.

## EMATRIX

### 10.26 EMATRIX—Explicit matrix input with data in the element definition, rather than in a file.

Explicit matrix input with data in the element definition, rather than in a file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| L              | $M$   | double | 0.0     | Length (used only for position computation) |
| ANGLE          | $RAD$ | double | 0.0     | Angle (used only for position computation)  |
| DX             | $M$   | double | 0.0     | misalignment                                |
| DY             | $M$   | double | 0.0     | misalignment                                |
| DZ             | $M$   | double | 0.0     | misalignment                                |
| TILT           | $RAD$ | double | 0.0     | Tilt angle                                  |
| YAW            | $RAD$ | double | 0.0     | Yaw angle                                   |
| PITCH          | $RAD$ | double | 0.0     | Pitch angle                                 |
| ORDER          |       | short  | 0       |   |
| C1             | $M$   | double | 0.0     |   |
| C2             |       | double | 0.0     |   |
| C3             | $M$   | double | 0.0     |   |
| C4             |       | double | 0.0     |   |
| C5             | $M$   | double | 0.0     |   |
| C6             |       | double | 0.0     | Change in momentum offset                   |
| DELTAP         |       | double | 0.0     | Change in central momentum (beta*gamma)     |
| R11            |       | double | 0.0     |   |
| R12            | $M$   | double | 0.0     |   |
| R13            |       | double | 0.0     |   |
| R14            | $M$   | double | 0.0     |   |
| R15            |       | double | 0.0     |   |
| R16            | $M$   | double | 0.0     |   |
| R21            | $1/M$ | double | 0.0     |   |
| R22            |       | double | 0.0     |   |
| R23            | $1/M$ | double | 0.0     |   |
| R24            |       | double | 0.0     |   |
| R25            | $1/M$ | double | 0.0     |   |
| R26            |       | double | 0.0     |   |
| R31            |       | double | 0.0     |   |
| R32            | $M$   | double | 0.0     |   |
| R33            |       | double | 0.0     |   |
| R34            | $M$   | double | 0.0     |   |
| R35            |       | double | 0.0     |   |

# EMATRIX continued

Explicit matrix input with data in the element definition, rather than in a file.

| Parameter Name | Units | Type   | Default | Description |
|----------------|-------|--------|---------|-------------|
| R36            | $M$   | double | 0.0     |             |
| R41            | $1/M$ | double | 0.0     |             |
| R42            |       | double | 0.0     |             |
| R43            | $1/M$ | double | 0.0     |             |
| R44            |       | double | 0.0     |             |
| R45            | $1/M$ | double | 0.0     |             |
| R46            |       | double | 0.0     |             |
| R51            |       | double | 0.0     |             |
| R52            | $M$   | double | 0.0     |             |
| R53            |       | double | 0.0     |             |
| R54            | $M$   | double | 0.0     |             |
| R55            |       | double | 0.0     |             |
| R56            | $M$   | double | 0.0     |             |
| R61            | $1/M$ | double | 0.0     |             |
| R62            |       | double | 0.0     |             |
| R63            | $1/M$ | double | 0.0     |             |
| R64            |       | double | 0.0     |             |
| R65            | $1/M$ | double | 0.0     |             |
| R66            |       | double | 0.0     |             |
| T111           | $1/M$ | double | 0.0     |             |
| T121           |       | double | 0.0     |             |
| T122           | $M$   | double | 0.0     |             |
| T131           | $1/M$ | double | 0.0     |             |
| T132           |       | double | 0.0     |             |
| T133           | $1/M$ | double | 0.0     |             |
| T141           |       | double | 0.0     |             |
| T142           | $M$   | double | 0.0     |             |
| T143           |       | double | 0.0     |             |
| T144           | $M$   | double | 0.0     |             |
| T151           | $1/M$ | double | 0.0     |             |
| T152           |       | double | 0.0     |             |
| T153           | $1/M$ | double | 0.0     |             |
| T154           |       | double | 0.0     |             |
| T155           | $1/M$ | double | 0.0     |             |
| T161           |       | double | 0.0     |             |
| T162           | $M$   | double | 0.0     |             |

# EMATRIX continued

Explicit matrix input with data in the element definition, rather than in a file.

| Parameter Name | Units   | Type   | Default | Description |
|----------------|---------|--------|---------|-------------|
| T163           |         | double | 0.0     |             |
| T164           | $M$     | double | 0.0     |             |
| T165           |         | double | 0.0     |             |
| T166           | $M$     | double | 0.0     |             |
| T211           | $1/M^2$ | double | 0.0     |             |
| T221           | $1/M$   | double | 0.0     |             |
| T222           |         | double | 0.0     |             |
| T231           | $1/M^2$ | double | 0.0     |             |
| T232           | $1/M$   | double | 0.0     |             |
| T233           | $1/M^2$ | double | 0.0     |             |
| T241           | $1/M$   | double | 0.0     |             |
| T242           |         | double | 0.0     |             |
| T243           | $1/M$   | double | 0.0     |             |
| T244           |         | double | 0.0     |             |
| T251           | $1/M^2$ | double | 0.0     |             |
| T252           | $1/M$   | double | 0.0     |             |
| T253           | $1/M^2$ | double | 0.0     |             |
| T254           | $1/M$   | double | 0.0     |             |
| T255           | $1/M^2$ | double | 0.0     |             |
| T261           | $1/M$   | double | 0.0     |             |
| T262           |         | double | 0.0     |             |
| T263           | $1/M$   | double | 0.0     |             |
| T264           | 1       | double | 0.0     |             |
| T265           | $1/M$   | double | 0.0     |             |
| T266           |         | double | 0.0     |             |
| T311           | $1/M$   | double | 0.0     |             |
| T321           |         | double | 0.0     |             |
| T322           | $M$     | double | 0.0     |             |
| T331           | $1/M$   | double | 0.0     |             |
| T332           |         | double | 0.0     |             |
| T333           | $1/M$   | double | 0.0     |             |
| T341           |         | double | 0.0     |             |
| T342           | $M$     | double | 0.0     |             |
| T343           |         | double | 0.0     |             |
| T344           | $M$     | double | 0.0     |             |
| T351           | $1/M$   | double | 0.0     |             |

# EMATRIX continued

Explicit matrix input with data in the element definition, rather than in a file.

| Parameter Name | Units   | Type   | Default | Description |
|----------------|---------|--------|---------|-------------|
| T352           |         | double | 0.0     |             |
| T353           | $1/M$   | double | 0.0     |             |
| T354           |         | double | 0.0     |             |
| T355           | $1/M$   | double | 0.0     |             |
| T361           |         | double | 0.0     |             |
| T362           | $M$     | double | 0.0     |             |
| T363           |         | double | 0.0     |             |
| T364           | $M$     | double | 0.0     |             |
| T365           |         | double | 0.0     |             |
| T366           | $M$     | double | 0.0     |             |
| T411           | $1/M^2$ | double | 0.0     |             |
| T421           | $1/M$   | double | 0.0     |             |
| T422           |         | double | 0.0     |             |
| T431           | $1/M^2$ | double | 0.0     |             |
| T432           | $1/M$   | double | 0.0     |             |
| T433           | $1/M^2$ | double | 0.0     |             |
| T441           | $1/M$   | double | 0.0     |             |
| T442           |         | double | 0.0     |             |
| T443           | $1/M$   | double | 0.0     |             |
| T444           |         | double | 0.0     |             |
| T451           | $1/M^2$ | double | 0.0     |             |
| T452           | $1/M$   | double | 0.0     |             |
| T453           | $1/M^2$ | double | 0.0     |             |
| T454           | $1/M$   | double | 0.0     |             |
| T455           | $1/M^2$ | double | 0.0     |             |
| T461           | $1/M$   | double | 0.0     |             |
| T462           |         | double | 0.0     |             |
| T463           | $1/M$   | double | 0.0     |             |
| T464           | 1       | double | 0.0     |             |
| T465           | $1/M$   | double | 0.0     |             |
| T466           |         | double | 0.0     |             |
| T511           | $1/M$   | double | 0.0     |             |
| T521           |         | double | 0.0     |             |
| T522           | $M$     | double | 0.0     |             |
| T531           | $1/M$   | double | 0.0     |             |
| T532           |         | double | 0.0     |             |

# EMATRIX continued

Explicit matrix input with data in the element definition, rather than in a file.

| Parameter Name | Units   | Type   | Default | Description |
|----------------|---------|--------|---------|-------------|
| T533           | $1/M$   | double | 0.0     |             |
| T541           |         | double | 0.0     |             |
| T542           | $M$     | double | 0.0     |             |
| T543           |         | double | 0.0     |             |
| T544           | $M$     | double | 0.0     |             |
| T551           | $1/M$   | double | 0.0     |             |
| T552           |         | double | 0.0     |             |
| T553           | $1/M$   | double | 0.0     |             |
| T554           |         | double | 0.0     |             |
| T555           | $1/M$   | double | 0.0     |             |
| T561           |         | double | 0.0     |             |
| T562           | $M$     | double | 0.0     |             |
| T563           |         | double | 0.0     |             |
| T564           | $M$     | double | 0.0     |             |
| T565           |         | double | 0.0     |             |
| T566           | $M$     | double | 0.0     |             |
| T611           | $1/M^2$ | double | 0.0     |             |
| T621           | $1/M$   | double | 0.0     |             |
| T622           |         | double | 0.0     |             |
| T631           | $1/M^2$ | double | 0.0     |             |
| T632           | $1/M$   | double | 0.0     |             |
| T633           | $1/M^2$ | double | 0.0     |             |
| T641           | $1/M$   | double | 0.0     |             |
| T642           |         | double | 0.0     |             |
| T643           | $1/M$   | double | 0.0     |             |
| T644           |         | double | 0.0     |             |
| T651           | $1/M^2$ | double | 0.0     |             |
| T652           | $1/M$   | double | 0.0     |             |
| T653           | $1/M^2$ | double | 0.0     |             |
| T654           | $1/M$   | double | 0.0     |             |
| T655           | $1/M^2$ | double | 0.0     |             |
| T661           | $1/M$   | double | 0.0     |             |
| T662           |         | double | 0.0     |             |
| T663           | $1/M$   | double | 0.0     |             |
| T664           | 1       | double | 0.0     |             |
| T665           | $1/M$   | double | 0.0     |             |

## EMATRIX continued

Explicit matrix input with data in the element definition, rather than in a file.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| T666           |       | double | 0.0     |  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Note that the default value of all matrix elements is 0. This can produce unexpected results if one imagines by mistake that the default values give a unit matrix, for example.



## EMITTANCE

### 10.27 EMITTANCE—Applies a linear transformation to the beam to force the emittance to given values.

Applies a linear transformation to the beam to force the emittance to given values.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| EMITX          | $M$   | double | -1      | horizontal emittance   |
| EMITY          | $M$   | double | -1      | vertical emittance   |
| EMITNX         | $M$   | double | -1      | horizontal normalized emittance  |
| EMITNY         | $M$   | double | -1      | vertical normalized emittance  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows changing the emittance of a beam during tracking. It is intended to be used to modify the emittance “slightly” to agree with, for example, experimental measurements.

The LCLS provides an example application: we track a beam from a photo-injector simulation through a laser/undulator beam heater and then through the entire linac. The beam emittance and twiss parameters are measured at a diagnostic downstream of the laser heater. We can insert an EMITTANCE element and a TWISS element at the location of the diagnostic to force the beam properties to the exact values that are measured. This compensates for imperfect modeling of the photo-injector while allowing us to conveniently model the system between the photo-injector and the point at which the emittance is measured.

## ENERGY

### 10.28 ENERGY—An element that matches the central momentum to the beam momentum, or changes the central momentum or energy to a specified value.

An element that matches the central momentum to the beam momentum, or changes the central momentum or energy to a specified value.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name   | Units  | Type   | Default | Description  |
|------------------|--------|--------|---------|--|
| CENTRAL_ENERGY   | $MC^2$ | double | 0.0     | desired central gamma  |
| CENTRAL_MOMENTUM | $MC$   | double | 0.0     | desired central beta*gamma   |
| MATCH_BEAMLINE   |        | long   | 0       | if nonzero, beamline reference momentum is set to beam average momentum  |
| MATCH_PARTICLES  |        | long   | 0       | if nonzero, beam average momentum is set to beamline reference momentum  |
| GROUP            |        | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## EVKICK

### 10.29 EVKICK—A vertical steering dipole implemented using an exact hard-edge model

A vertical steering dipole implemented using an exact hard-edge model

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name            | Units      | Type   | Default | Description  |
|---------------------------|------------|--------|---------|--|
| L                         | <i>M</i>   | double | 0.0     | length   |
| KICK                      | <i>RAD</i> | double | 0.0     | kick angle   |
| TILT                      | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX                        | <i>M</i>   | double | 0.0     | misalignment   |
| DY                        | <i>M</i>   | double | 0.0     | misalignment   |
| DZ                        | <i>M</i>   | double | 0.0     | misalignment   |
| CALIBRATION               |            | double | 1       | factor applied to obtain kick  |
| LERAD                     |            | double | 0.0     | if L=0, use this length for radiation computations   |
| STEERING                  |            | short  | 1       | use for steering?  |
| SYNCH_RAD                 |            | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                       |            | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| STEERING_MULTIPOLES       |            | STRING | NULL    | input file for systematic multipole content of steering kicks  |
| RANDOM_MULTIPOLES         |            | STRING | NULL    | input file for random multipoles content of steering kicks   |
| RANDOM_MULTIPOLE_FACTOR   |            | double | 1       | Factor by which to multiply random multipoles  |
| STEERING_MULTIPOLE_FACTOR |            | double | 1       | Factor by which to multiply steering multipoles  |
| GROUP                     |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Note that `closed_orbit` and `correct` command may report orbit convergence problems when using `EVKICK` in place of `VKICK`. This may be resolved by increasing the `closed_orbit_accuracy` parameter.

If requested, synchrotron radiation effects are imposed as a kick at the end of the element.

## FLOOR

### 10.30 FLOOR—Sets floor coordinates

Sets floor coordinates

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| X              |       | double | 0.0     | X coordinate   |
| Y              |       | double | 0.0     | Y coordinate   |
| Z              |       | double | 0.0     | Z coordinate   |
| THETA          |       | double | 0.0     | theta value  |
| PHI            |       | double | 0.0     | phi value  |
| PSI            |       | double | 0.0     | psi value  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## FMULT

### 10.31 FMULT—Multipole kick element with coefficient input from an SDDS file.

Multipole kick element with coefficient input from an SDDS file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| TILT           | $RAD$ | double | 0.0     | rotation about longitudinal axis   |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| DZ             | $M$   | double | 0.0     | misalignment   |
| FSE            |       | double | 0.0     | fractional strength error  |
| N_KICKS        |       | long   | 1       | number of kicks  |
| SYNCH_RAD      |       | short  | 0       | include classical, single-particle synchrotron radiation?  |
| FILENAME       |       | STRING | NULL    | name of file containing multipole data   |
| SQRT_ORDER     |       | short  | 0       | Ignored, kept for backward compatibility only.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a multipole element using a 4th-order symplectic integration. Specification of the multipole strength is through an SDDS file. The file is expected to contain a single page of data with the following elements:

1. An integer column named **order** giving the order of the multipole. The order is defined as  $(N_{poles} - 2)/2$ , so a quadrupole has order 1, a sextupole has order 2, and so on.
2. A floating point column named **KnL** giving the integrated strength of the multipole,  $K_n L$ , where  $n$  is the order. The units are  $1/m^n$ .
3. A floating point column named **JnL** giving the integrated strength of the skew multipole,  $J_n L$ , where  $n$  is the order. The units are  $1/m^n$ .

The **MULT** element is also available, which allows the same functionality without an external file, for a single component.

The transport matrix for FMULT elements is determined by tracking and will affect the tunes, chromaticities, etc.

## FRFMODE

### 10.32 FRFMODE—One or more beam-driven TM monopole modes of an RF cavity, with data from a file.

One or more beam-driven TM monopole modes of an RF cavity, with data from a file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| FILENAME            |       | STRING | NULL    | input file   |
| BIN_SIZE            | $S$   | double | 0.0     | bin size for current histogram (use 0 for autosize)  |
| N_BINS              |       | long   | 20      | number of bins for current histogram   |
| RIGID_UNTIL_PASS    |       | long   | 0       | don't affect the beam until this pass  |
| USE_SYMM_DATA       |       | long   | 0       | use "Symm" columns from URMEL output file?   |
| FACTOR              |       | double | 1       | factor by which to multiply shunt impedances   |
| CUTOFF              | $HZ$  | double | 0.0     | If >0, cutoff frequency. Modes above this frequency are ignored.   |
| OUTPUT_FILE         |       | STRING | NULL    | Output file for voltage in each mode.  |
| FLUSH_INTERVAL      |       | long   | 1       | Interval in passes at which to flush output data.  |
| RAMP_PASSES         |       | long   | 0       | Number of passes over which to linearly ramp up the impedance to full strength.  |
| RESET_FOR_EACH_STEP |       | long   | 1       | If nonzero, voltage and phase are reset for each simulation step.  |
| LONG_RANGE_ONLY     |       | long   | 0       | If nonzero, induced voltage from present turn does not affect bunch. Short range wake should be included via WAKE or ZLONGIT element.                      |
| N_CAVITIES          |       | long   | 1       | effect is multiplied by this number, simulating N identical cavities   |
| BUNCHED_BEAM_MODE   |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a set of beam-driven monopole modes in a cavity using the fundamental theorem of beam loading and phasor rotation. It is similar to **RFMODE**, but it allows faster simulation of more than one mode. Also, the mode data is specified in an SDDS file. This file can be generated using the APS version of URMEL, or by hand. It must have the following columns and units:



1. **Frequency** — The frequency of the mode in Hz. Floating point.
2. **Q** — The quality factor. Floating point.
3. **ShuntImpedance** or **ShuntImpedanceSymm** — The shunt impedance in Ohms, defined as  $V^2/(2 * P)$  (i.e., the “circuit definition”). Floating point. By default, **ShuntImpedance** is used. However, if the parameter **USE\_SYMM\_DATA** is non-zero, then **ShuntImpedanceSymm** is used. The latter is the full-cavity shunt impedance that URMEL computes by assuming that the input cavity used is one half of a symmetric cavity.

The file may also have the following column:

1. **beta** — Normalized load impedance (dimensionless). Floating point. If not given, the  $\beta = 0$  is assumed for all modes.

In many simulations, a transient effect may occur when using this element because, in the context of the simulation, the impedance is switched on instantaneously. This can give a false indication of the threshold for instability. The **RAMP\_PASSES** parameter should be used to prevent this by slowly ramping the impedance to full strength. This idea is from M. Blaskiewicz (BNL).

Normally, the field dumped in the cavity by one particle affects trailing particles in the same turn. However, if one is also using a **WAKE** or **ZLONGIT** element to simulate the short-range wake of the cavity, this would be double-counting. In that case, one can use **LONG\_RANGE\_ONLY=1** to suppress the same-turn effects of the **RFMODE** element.

## FTABLE

### 10.33 FTABLE—Tracks through a magnetic field which is expressed by a SDDS table.

Tracks through a magnetic field which is expressed by a SDDS table.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| L              | <i>M</i>   | double | 0.0     | The effective field length measured along a straight line.   |
| ANGLE          | <i>RAD</i> | double | 0.0     | The designed bending angle   |
| L1             | <i>M</i>   | double | 0.0     | The left fringe field length.  |
| L2             | <i>M</i>   | double | 0.0     | The right fringe field length. L1+L+L2=Total z span in the input field table.  |
| E1             | <i>RAD</i> | double | 0.0     | The designed entrance edge angle   |
| E2             | <i>RAD</i> | double | 0.0     | The designed exit edge angle   |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about incoming longitudinal axis  |
| DX             | <i>M</i>   | double | 0.0     | misalignment   |
| DY             | <i>M</i>   | double | 0.0     | misalignment   |
| DZ             | <i>M</i>   | double | 0.0     | misalignment   |
| FACTOR         |            | double | 1       | Factor by which to multiply field data.  |
| THRESHOLD      |            | double | 1e-08   | Fields smaller than this are considered 0.   |
| INPUT_FILE     |            | STRING | NULL    | Name of SDDS file which contains field data.   |
| N_KICKS        |            | long   | 1       | Number of kicks into which to split the element.   |
| VERBOSE        |            | short  | 0       | Used for debugging code. Not applicable to Pelegant  |
| SIMPLEINPUT    |            | short  | 0       | If non-zero, use simple input format.  |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is used for tracking through an arbitrary magnetic field when its values are known at regularly spaced grid points and it is hard to find a suitable model to describe it. The input

magnet parameter and coordinate system definition are illustrated in Fig:1.

The **THRESHOLD** parameter sets the magnitude of magnetic field below which the field is considered zero. If this is too small, there may be numerical problems.

The field data is provided in an SDDS file, with two formats available. The recommended format can be used if the **SIMPLE\_INPUT** parameter is non-zero.

**Simple input format** — This format is shared with the **BMXYZ** and **BRAT** elements and is more convenient than the original, default format. The field map file is an SDDS file with the following columns:

- **x, y, z** — Transverse coordinates in meters (units should be “m”).
- **Bx, By, Bz** — Field values in Tesla (units should be “T”).

The field map file must contain a rectangular grid of points, equispaced (separately) in x, y, and z. There should be no missing values in the grid (this is not checked by **elegant**). In addition, the x values must vary fastest as the values are accessed in row order, then the y values. To ensure that this is the case, use the following command on the field file:

```
sddsort fieldFile -column=z,incr -column=y,incr -column=x,incr
```

N.B.: Particles are injected into the field region with  $z=0$ . Hence, one would normally want the minimum value of z to be 0.

**Original input format** — This format is difficult to understand and set up. Although it is not recommended, it is the default at present for historical reasons.

The field data is saved in a 3 pages ( $B_x$ ,  $B_y$ ,  $B_z$ ) 3D histogram SDDS table (see **MHISTOGRAM** for detail). An example is shown in Fig:2. This SDDS file must have one column **Frequency** to store the field data in Tesla, and following parameters:

- **ND** — Type “long”; Value “3”.
- **Variable00Name, Variable01Name, Variable02Name** — Type “string”; Value “x”, “y”, “z”.
- **Variable00Min, Variable01Min, Variable02Min** — Type “double”; Value: the minimum boundary coordinates of “x”, “y”, “z” in meter. **Variable02Min** ( $z_{\min}$ ) must start from zero.
- **Variable00Max, Variable01Max, Variable02Max** — Type “double”; Value: the maximum boundary coordinates of “x”, “y”, “z” in meter.
- **Variable00Interval, Variable01Interval, Variable02Interval** — Type “double”; Value of the grid size of “x”, “y”, “z” in meter.
- **Variable00Dimension, Variable01Dimension, Variable02Dimension** — Type “long”; Value of total number of grid points in “x”, “y”, “z”. For example:  $\text{Variable00Dimension} = (\text{Variable00Max} - \text{Variable00Min}) / \text{Variable00Interval} + 1$ .

N.B.: Particles are injected into the field region with  $z=0$ . Hence, one would normally want **Variable02Min**=0. If **Variable02Min**<0, data ahead of the injection point.

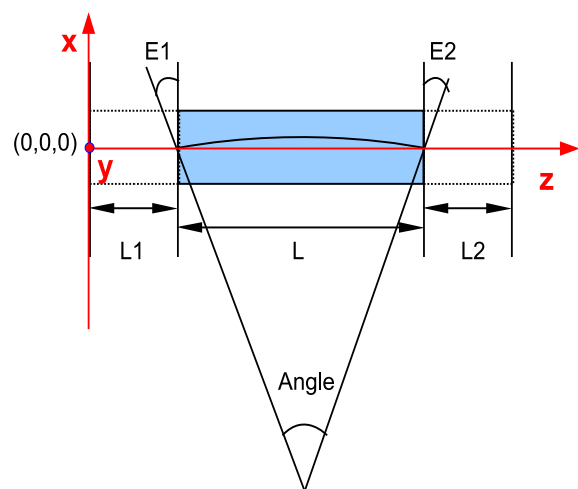


Figure 1: Illustration of coordinate system and magnet definition.

sddsprintout -para=\* ftable.input

|                          |               |                          |               |
|--------------------------|---------------|--------------------------|---------------|
| ND =                     | 3             | Variable00Name =         | x             |
| Variable01Name =         | y             | Variable02Name =         | z             |
| Variable00Min (m) =      | -1.700000e-02 | Variable01Min (m) =      | -5.000000e-03 |
| Variable02Min (m) =      | 0.000000e+00  | Variable00Max (m) =      | 1.700000e-02  |
| Variable01Max (m) =      | 5.000000e-03  | Variable02Max (m) =      | 1.250000e-01  |
| Variable00Interval (m) = | 1.000000e-03  | Variable01Interval (m) = | 1.000000e-03  |
| Variable02Interval (m) = | 1.250000e-0   | Variable00Dimension =    | 35            |
| Variable01Dimension =    | 11            | Variable02Dimension =    | 101           |

sddsprintout -col=\* ftable.input (page 2, By field)

| x_index | y_index | z_index | Frequency<br>T |
|---------|---------|---------|----------------|
| 0       | 0       | 0       | 1              |
| 0       | 0       | 100     | 1              |
| ...     | ...     | ...     | ...            |
| 0       | 10      | 100     | 1              |
| ...     | ...     | ...     | ...            |
| 1       | 10      | 100     | 1              |
| ...     | ...     | ...     | ...            |
| 34      | 10      | 100     | 1              |

Figure 2: Example of SDDS input file. The column x\_index, y\_index, z\_index is not the necessary part, it's shown here just for clarifying how the data is arranged

## FTRFMODE

### 10.34 FTRFMODE—One or more beam-driven TM dipole modes of an RF cavity, with data from a file.

One or more beam-driven TM dipole modes of an RF cavity, with data from a file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units | Type   | Default | Description   |
|---------------------|-------|--------|---------|---|
| FILENAME            |       | STRING | NULL    | input file  |
| BIN_SIZE            | $S$   | double | 0.0     | bin size for current histogram (use 0 for autosize)   |
| N_BINS              |       | long   | 20      | number of bins for current histogram  |
| RIGID_UNTIL_PASS    |       | long   | 0       | don't affect the beam until this pass   |
| USE_SYMM_DATA       |       | long   | 0       | use "Symm" columns from URMEL output file?  |
| DX                  | $M$   | double | 0.0     | misalignment  |
| DY                  | $M$   | double | 0.0     | misalignment  |
| XFACTOR             |       | double | 1       | factor by which to multiply shunt impedances  |
| YFACTOR             |       | double | 1       | factor by which to multiply shunt impedances  |
| CUTOFF              | $HZ$  | double | 0.0     | If >0, cutoff frequency. Modes above this frequency are ignored.  |
| OUTPUT_FILE         |       | STRING | NULL    | Output file for voltage in each mode.   |
| FLUSH_INTERVAL      |       | long   | 1       | Interval in passes at which to flush output data.   |
| RAMP_PASSES         |       | long   | 0       | Number of passes over which to linearly ramp up the impedance to full strength.   |
| RESET_FOR_EACH_STEP |       | long   | 1       | If nonzero, voltage and phase are reset for each simulation step.   |
| LONG_RANGE_ONLY     |       | long   | 0       | If nonzero, induced voltage from present turn does not affect bunch. Short range wake should be included via WAKE or ZLONGIT element. |
| N_CAVITIES          |       | long   | 1       | effect is multiplied by this number, simulating N identical cavities  |

## FTRFMODE continued

One or more beam-driven TM dipole modes of an RF cavity, with data from a file.

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| BUNCHED_BEAM_MODE |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a set of beam-driven dipole modes in a cavity using the fundamental theorem of beam loading and phasor rotation. It is similar to TRFMODE, but it allows faster simulation of more than one mode. Also, the mode data is specified in an SDDS file. This file can be generated using the APS version of URMEL, or by hand. It must have the following columns and units:

1. **Frequency** — The frequency of the mode in Hz. Floating point.
2. **Q** — The quality factor. Floating point.
3. **ShuntImpedance** or **ShuntImpedanceSymm** — The shunt impedance in Ohms/m, defined as  $V^2/(2 * P)/x$  or  $V^2/(2 * P)/y$  (i.e., “circuit definition”). Floating point. By default, **ShuntImpedance** is used. However, if the parameter **USE\_SYMM\_DATA** is non-zero, then **ShuntImpedanceSymm** is used. The latter is the full-cavity shunt impedance that URMEL computes by assuming that the input cavity used is one half of a symmetric cavity.

The file may also have the following columns:

1. **beta** — Normalized load impedance (dimensionless). Floating point. If not given, the  $\beta = 0$  is assumed for all modes.
2. **xMode** — If given, then only modes for which the value is nonzero will produce an x-plane kick. Integer. If not given, all modes affect the x plane.
3. **yMode** — If given, then only modes for which the value is nonzero will produce an y-plane kick. Integer. If not given, all modes affect the y plane.

In many simulations, a transient effect may occur when using this element because, in the context of the simulation, the impedance is switched on instantaneously. This can give a false indication of the threshold for instability. The **RAMP\_PASSES** parameter should be used to prevent this by slowly ramping the impedance to full strength. This idea is from M. Blaskiewicz (BNL).

Normally, the field dumped in the cavity by one particle affects trailing particles in the same turn. However, if one is also using a **TRWAKE** or **ZTRANSVSE** element to simulate the short-range wake of the cavity, this would be double-counting. In that case, one can use **LONG\_RANGE\_ONLY=1** to suppress the same-turn effects of the **RFMODE** element.

## GFWIGGLER

### 10.35 GFWIGGLER—Tracks through a wiggler using generate function method of J. Bahrtdt and G. Wuestefeld (BESSY, Berlin, Germany).

Tracks through a wiggler using generate function method of J. Bahrtdt and G. Wuestefeld (BESSY, Berlin, Germany).

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| L              | $M$   | double | 0.0     | Total length  |
| B_MAX          | $T$   | double | 0.0     | Maximum on-axis magnetic field at gap=GAP0 and equal longitudinal phases of PHASE_1,2,3,4   |
| SHIM_SCALE     |       | double | 1       | Scaling factor of shim correction field.  |
| DX             | $M$   | double | 0.0     | Misalignment.   |
| DY             | $M$   | double | 0.0     | Misalignment.   |
| DZ             | $M$   | double | 0.0     | Misalignment.   |
| TILT           | $RAD$ | double | 0.0     | Rotation about beam axis.   |
| PERIODS        |       | long   | 0       | Total number of wiggler periods. Include end poles  |
| STEP           |       | long   | 1       | Number of normal periods to track for each step   |
| ORDER          |       | short  | 0       | Order=3 including the 3rd order terms. Otherwise using 2nd order formula.   |
| END_POLE       |       | short  | 1       | The ending poles are treated as 2 half periods at each sides of the wiggler with reducing field strength, such as 0.25, -0.75, ..., 0.75, -0.25. Periods has to > 2 |
| SHIM_ON        |       | short  | 0       | Include shim correction   |
| INPUT_FILE     |       | STRING | NULL    | Name of SDDS file with By harmonic data given at GAP0 and equal longitudinal phases.  |
| SHIM_INPUT     |       | STRING | NULL    | Name of SDDS file with shim field integral harmonic data given at GAP0.   |
| SYNCH_RAD      |       | short  | 0       | Include classical, single-particle synchrotron radiation?   |
| ISR            |       | short  | 0       | Include incoherent synchrotron radiation (quantum excitation)?  |



## GFWIGGLER continued

Tracks through a wiggler using generate function method of J. Bahrtdt and G. Wuestefeld (BESSY, Berlin, Germany).

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| ISR1PART       |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| X0             | $M$   | double | 0.0     | Offset of magnet row center in meter.  |
| GAP0           | $M$   | double | 0.0     | Nominal magnetic gap.  |
| D_GAP          | $M$   | double | 0.0     | Delta gap: actual gap - nominal gap  |
| PHASE_1        | $RAD$ | double | 0.0     | Longitudinal phase of the first row (top right)  |
| PHASE_2        | $RAD$ | double | 0.0     | Longitudinal phase of the second row (top left)  |
| PHASE_3        | $RAD$ | double | 0.0     | Longitudinal phase of the third row (bottom left)  |
| PHASE_4        | $RAD$ | double | 0.0     | Longitudinal phase of the fourth row (bottom right)  |
| VERBOSITY      |       | short  | 0       | A higher value requires more detailed printouts related to computations.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

N.B.: at present this element is *not* included in computations of beam moments (`moments_output` command).

This element simulates a wiggler or undulator using the generate function method given by J. Bahrtdt and G. Wüstefeld (“Symplectic tracking and compensation of dynamic field integrals in complex undulator structures,” PRSTAB 14, 040703, 2011.).

To use the element, one must supply an SDDS file giving harmonic analysis of the wiggler field. The field expansion used by the code is for a wiggler working at the nominal gap and provide pure horizontal deflecting to the on-axis beam. See CWIGGLER, horizontal wiggler with normal poles, for detail explanation of the field expansion and format of the input file. Besides the required columns of `Cmn`, `KxOverKw`, `KyOverKw`, and `KzOverKw` by the CWIGGLER elements, two more input columns are needed:

- The longitudinal harmonic number,  $n$ , in column `zHarm`.
- The horizontal harmonic number of  $l$ , in column `xHarm`.

If a file include all required columns from `CWIGGLER` and `GFWIGGLER` then user can use either of the both methods for simulating a horizontal planar wiggler.

An universal wiggler field, which be used for generating an arbitrary polarization, can be derived by given different longitudinal phase parameters: `PHASE_1,2,3,4`. The photon energy can be varied by a non-zero `D_GAP` value.

## HISTOGRAM

### 10.36 HISTOGRAM—Request for histograms of particle coordinates to be output to SDDS file.

Request for histograms of particle coordinates to be output to SDDS file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| FILENAME        |       | STRING |         | filename for histogram output, possibly incomplete (see below)   |
| INTERVAL        |       | long   | 1       | interval in passes between output  |
| START_PASS      |       | long   | 0       | starting pass for output   |
| BINS            |       | long   | 50      | number of bins   |
| FIXED_BIN_SIZE  |       | short  | 0       | if nonzero, bin size is fixed after the first histogram is made  |
| X_DATA          |       | short  | 1       | histogram x and x'?  |
| Y_DATA          |       | short  | 1       | histogram y and y'?  |
| LONGIT_DATA     |       | short  | 1       | histogram t and p?   |
| BIN_SIZE_FACTOR |       | double | 1       | multiply computed bin size by this factor before histogramming   |
| NORMALIZE       |       | short  | 1       | normalize histogram with bin size and number of particles?   |
| DISABLE         |       | short  | 0       | If nonzero, no output will be generated.   |
| SPARSE          |       | short  | 0       | If nonzero, only bins with non-zero counts will be output.   |
| START_PID       |       | long   | -1      | starting particleID for particles to include   |
| END_PID         |       | long   | -1      | ending particleID for particles to include   |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The output filename may be an incomplete filename. In the case of the HISTOGRAM point element, this means it may contain one instance of the string format specification “%s” and one occurrence of an integer format specification (e.g., “%ld”). **elegant** will replace the format with the rootname (see **run\_setup**) and the latter with the element’s occurrence number. For example,

suppose you had a repetitive lattice defined as follows:

```
H1: HISTOGRAM,FILENAME=' '%s-%03ld.h1' '  
Q1: QUAD,L=0.1,K1=1  
D: DRIFT,L=1  
Q2: QUAD,L=0.1,K1=-1  
CELL: LINE=(H1,Q1,D,2*Q2,D,Q1)  
BL: LINE=(100*CELL)
```

The element H1 appears 100 times. Each instance will result in a new file being produced. Successive instances have names like “*rootname-001.h1*”, “*rootname-002.h1*”, “*rootname-003.h1*”, and so on up to “*rootname-100.h1*”. (If instead of “%03ld” you used “%ld”, the names would be “*rootname-1.h1*”, “*rootname-2.h1*”, etc. up to “*rootname-100.h1*”. This is generally not as convenient as the names don’t sort into occurrence order.)

The files can easily be plotted together, as in

```
% sddsplot -column=dt,dtFrequency *-???.h1 -separate
```

They may also be combined into a single file, as in

```
% sddscombine *-???.h1 all.h1
```

In passing, note that if H1 was defined as

```
H1: HISTOGRAM,FILENAME=' '%s.h1' '
```

or

```
H1: HISTOGRAM,FILENAME=' 'output.h1' '
```

only a single file would be produced, containing output from the last instance only.

## HKICK

### 10.37 HKICK—A horizontal steering dipole implemented as a matrix, up to 2nd order. Use EHKICK for symplectic tracking.

A horizontal steering dipole implemented as a matrix, up to 2nd order. Use EHKICK for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| KICK           | $RAD$   | double | 0.0     | kick strength  |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| B2             | $1/M^2$ | double | 0.0     | normalized sextupole strength<br>(kick = KICK*(1+B2*x <sup>2</sup> )<br>when y=0)  |
| CALIBRATION    |         | double | 1       | strength multiplier  |
| EDGE_EFFECTS   |         | short  | 0       | include edge effects?  |
| ORDER          |         | short  | 0       | matrix order   |
| STEERING       |         | short  | 1       | use for steering?  |
| SYNCH_RAD      |         | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR            |         | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| LERAD          |         | double | 0.0     | if L=0, use this length for radiation computations   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## HKPOLY

**10.38 HKPOLY**—Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description                                   |
|----------------|-------|--------|---------|---|
| L              | $M$   | double | 0.0     | length for geometry only, ignored in tracking |
| K00            |       | double | 0.0     | Coefficient of polynomial for kicks—ignored   |
| K01            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K02            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K03            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K04            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K05            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K06            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K10            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K11            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K12            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K13            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K14            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K15            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K16            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K20            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K21            |       | double | 0.0     | Coefficient of polynomial for kicks           |
| K22            |       | double | 0.0     | Coefficient of polynomial for kicks           |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                         |
|----------------|-------|--------|---------|-------------------------------------|
| K23            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K24            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K25            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K26            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K30            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K31            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K32            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K33            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K34            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K35            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K36            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K40            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K41            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K42            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K43            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K44            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K45            |       | double | 0.0     | Coefficient of polynomial for kicks |
| K46            |       | double | 0.0     | Coefficient of polynomial for kicks |



## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| K50            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K51            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K52            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K53            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K54            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K55            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K56            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K60            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K61            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K62            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K63            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K64            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K65            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| K66            |       | double | 0.0     | Coefficient of polynomial for kicks                     |
| D00            |       | double | 0.0     | Coefficient of polynomial for generalized drift—ignored |
| D01            |       | double | 0.0     | Coefficient of polynomial for generalized drift         |
| D02            |       | double | 0.0     | Coefficient of polynomial for generalized drift         |
| D03            |       | double | 0.0     | Coefficient of polynomial for generalized drift         |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                     |
|----------------|-------|--------|---------|---|
| D04            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D05            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D06            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D10            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D11            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D12            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D13            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D14            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D15            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D16            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D20            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D21            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D22            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D23            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D24            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D25            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D26            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D30            |       | double | 0.0     | Coefficient of polynomial for generalized drift |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                     |
|----------------|-------|--------|---------|---|
| D31            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D32            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D33            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D34            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D35            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D36            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D40            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D41            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D42            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D43            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D44            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D45            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D46            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D50            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D51            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D52            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D53            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D54            |       | double | 0.0     | Coefficient of polynomial for generalized drift |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                     |
|----------------|-------|--------|---------|---|
| D55            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D56            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D60            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D61            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D62            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D63            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D64            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D65            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| D66            |       | double | 0.0     | Coefficient of polynomial for generalized drift |
| E000           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E001           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E002           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E003           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E004           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E005           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E006           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E010           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |
| E011           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts     |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E012           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E013           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E014           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E015           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E016           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E020           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E021           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E022           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E023           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E024           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E025           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E026           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E030           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E031           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E032           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E033           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E034           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E035           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E036           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E040           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E041           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E042           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E043           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E044           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E045           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E046           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E050           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E051           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E052           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E053           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E054           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E055           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E056           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E060           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E061           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E062           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E063           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E064           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E065           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E066           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E100           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E101           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E102           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E103           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E104           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E105           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E106           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E110           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E111           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E112           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E113           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E114           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E115           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E116           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E120           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E121           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E122           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E123           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E124           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E125           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E126           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E130           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E131           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E132           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E133           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E134           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E135           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E136           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E140           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E141           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E142           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E143           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |



## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E144           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E145           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E146           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E150           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E151           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E152           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E153           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E154           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E155           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E156           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E160           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E161           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E162           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E163           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E164           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E165           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E166           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E200           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E201           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E202           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E203           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E204           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E205           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E206           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E210           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E211           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E212           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E213           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E214           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E215           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E216           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E220           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E221           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E222           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E223           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E224           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E225           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E226           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E230           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E231           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E232           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E233           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E234           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E235           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E236           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E240           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E241           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E242           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E243           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E244           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E245           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E246           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E250           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E251           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E252           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E253           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E254           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E255           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E256           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E260           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E261           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E262           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E263           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E264           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E265           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E266           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E300           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E301           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E302           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E303           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E304           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E305           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E306           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E310           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E311           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E312           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E313           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E314           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E315           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E316           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E320           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E321           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E322           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E323           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E324           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E325           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E326           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E330           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E331           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E332           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E333           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E334           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E335           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E336           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E340           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E341           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E342           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E343           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E344           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E345           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E346           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E350           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E351           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E352           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E353           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E354           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E355           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E356           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E360           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E361           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E362           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E363           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E364           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E365           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E366           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E400           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E401           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E402           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E403           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E404           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E405           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E406           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E410           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E411           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E412           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E413           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E414           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E415           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E416           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E420           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E421           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E422           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E423           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E424           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E425           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E426           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E430           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E431           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E432           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E433           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E434           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E435           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E436           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E440           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |



## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E441           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E442           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E443           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E444           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E445           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E446           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E450           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E451           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E452           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E453           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E454           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E455           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E456           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E460           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E461           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E462           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E463           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E464           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E465           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E466           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E500           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E501           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E502           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E503           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E504           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E505           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E506           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E510           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E511           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E512           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E513           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E514           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E515           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E516           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E520           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E521           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E522           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E523           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E524           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E525           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E526           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E530           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E531           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E532           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E533           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E534           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E535           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E536           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E540           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E541           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E542           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E543           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E544           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E545           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E546           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E550           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E551           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E552           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E553           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E554           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E555           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E556           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E560           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E561           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E562           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E563           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E564           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E565           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E566           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E600           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E601           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E602           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E603           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E604           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E605           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E606           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E610           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E611           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E612           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E613           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E614           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E615           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E616           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E620           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E621           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E622           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E623           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E624           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E625           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E626           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units | Type   | Default | Description                                 |
|----------------|-------|--------|---------|---|
| E630           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E631           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E632           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E633           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E634           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E635           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E636           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E640           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E641           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E642           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E643           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E644           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E645           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E646           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E650           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E651           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E652           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |
| E653           |       | double | 0.0     | Coefficient of polynomial for type 2 drifts |

## HKPOLY continued

Applies kick according to a Hamiltonian that's a polynomial function of  $x$  and  $y$  together with a generalized drift also given as a polynomial of  $qx$  and  $qy$

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| E654           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E655           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E656           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E660           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E661           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E662           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E663           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E664           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E665           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| E666           |            | double | 0.0     | Coefficient of polynomial for type 2 drifts  |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX             | <i>M</i>   | double | 0.0     | misalignment   |
| DY             | <i>M</i>   | double | 0.0     | misalignment   |
| DZ             | <i>M</i>   | double | 0.0     | misalignment   |
| FACTOR         |            | double | 1       | additional factor to apply   |
| N_REPEATS      |            | long   | 1       | Number of times to repeat the drift-kick-drift sequence. Strength of each application is reduced by this factor.   |
| DRIFT_TYPE     |            | short  | 1       | If 1, then use $D[i][j]$ . If 2, then use $E[i][j][k]$ .   |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element imposes kicks on the beam according to a Hamiltonian that is a polynomial

function of  $x$  and  $y$

$$H_k \Delta s = \sum_{i=0}^6 \sum_{j=0}^6 K_{ij} x^i y^j \quad (41)$$

where  $K_{00}$  is ignored. The changes to the momenta are determined via Hamilton's equations, e.g.,

$$\Delta q_x = -\frac{\partial H_k \Delta s}{\partial x} \quad (42)$$

It also implements a generalized drift that is described by another Hamiltonian

$$H_d \Delta s = (1 + \delta) \sum_{i=0}^6 \sum_{j=0}^6 D_{ij} \left( \frac{q_x}{1 + \delta} \right)^i \left( \frac{q_y}{1 + \delta} \right)^j \quad (43)$$

where  $D_{00}$  is ignored. Again, the changes to the positions are determined via Hamilton's equations, e.g.,

$$\Delta x = \frac{\partial H_d \Delta s}{\partial q_x} \quad (44)$$

In version 2019.1.0, another option was added for the drift Hamiltonian. This is activated by setting the paramter `DRIFT_TYPE` to 2 (the default is 1) and setting the `E` values instead of the `D` values. In this case, the  $\delta$  dependence is under user control

$$H_d \Delta s = \sum_{i=0}^6 \sum_{j=0}^6 \sum_{k=0}^6 E_{ijk} q_x^i q_y^j \delta^k \quad (45)$$

where  $E_{000}$  is ignored.

In more detail, the drift Hamiltonian is applied on both sides of the kick Hamiltonian, but with half strength.

For example, a quadrupole of length  $L$  with integrated strength  $K_1 L$  could be specified by setting  $K_{20} = -K_{02} = K_1 L/2$  and  $D_{20} = D_{02} = L/2$ . A sextupole with integrated strength  $K_2 L$  could be specified by setting  $K_{30} = K_{21} = K_{12} = K_2 L/6$  and  $D_{30} = D_{21} = D_{12} = L/2$ . The purpose, however, is not to simulate such elements, since they can be more conveniently simulated with `KQUAD` or `KSEXT`. It is rather to simulate elements that may not be described by the usual multipoles.



## HMON

### 10.39 HMON—A horizontal position monitor, accepting a rpn equation for the readout as a function of the actual position (x).

A horizontal position monitor, accepting a rpn equation for the readout as a function of the actual position (x).

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units    | Type   | Default | Description  |
|----------------|----------|--------|---------|--|
| L              | <i>M</i> | double | 0.0     | length   |
| DX             | <i>M</i> | double | 0.0     | misalignment   |
| DY             | <i>M</i> | double | 0.0     | misalignment   |
| WEIGHT         |          | double | 1       | weight in correction   |
| TILT           |          | double | 0.0     | rotation about longitudinal axis   |
| CALIBRATION    |          | double | 1       | calibration factor for readout   |
| SETPOINT       | <i>M</i> | double | 0.0     | steering setpoint  |
| ORDER          |          | short  | 0       | matrix order   |
| READOUT        |          | STRING | NULL    | rpn expression for readout (actual position supplied in variable x)  |
| CO_FITPOINT    |          | short  | 0       | If nonzero, then closed orbit value is placed in variable <name>#<occurrence>.xco  |
| GROUP          |          | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## IBSCATTER

### 10.40 IBSCATTER—A simulation of intra-beam scattering.

A simulation of intra-beam scattering.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| FACTOR              |       | double | 1       | factor by which to multiply growth rates before using  |
| DO_X                |       | long   | 1       | do x-plane scattering?   |
| DO_Y                |       | long   | 1       | do y-plane scattering?   |
| DO_Z                |       | long   | 1       | do z-plane scattering?   |
| NSLICE              |       | long   | 1       | The number of slices per bunch   |
| SMOOTH              |       | long   | 1       | Use smooth method instead of random numbers?   |
| FORCE_MATCHED_TWISS |       | long   | 0       | Force computations to be done with twiss parameters of the beamline, not the beam.   |
| ISRING              |       | long   | 1       | Is it storage ring?  |
| INTERVAL            |       | long   | 1       | Interval in passes at which to update output file.   |
| FILENAME            |       | STRING | NULL    | Output filename.   |
| BUNCHED_BEAM_MODE   |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| VERBOSE             |       | long   | 0       | If non-zero, then print updates during calculations.   |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is used for simulating intra-beam scattering (IBS) effect. The IBS algorithm is based on the Bjorken and Mtingwa's [15] formula, and with an extension of including vertical dispersion. It can be used for both storage ring and Linac.

To initialize IBS calculation, one or more IBSCATTER elements must be inserted into the beamline. **elegant** calculates the integrated IBS growth rates between IBSCATTERs (or from beginning of the beamline to the first IBSCATTER), then scatter particles at each IBSCATTER element. Beam's parameters are updated for use in downstream elements.

This method requires that IBSCATTER can not be installed at the beginning of beamline. The number of other elements between IBSCATTERs or from the beginning of beamline to the first IBSCATTER has to be 2 or more. For storage ring, an IBSCATTER must be installed at the end

of beamline.

Because the IBS growth rates are energy dependent, special caution is needed for calculations with accelerating beam. The user needs to split their accelerating cavity into several pieces, so that  $\gamma$  has no large changes between elements.

The user can examine the calculation through an optional SDDS output file - *filename*. The file has a multiple page structure. Each slice at pass  $i$  at each IBSCATTER element occupies one page. Each page contains integrated IBS growth rates between IBSCATTERs (or from beginning of the beamline to first IBSCATTER) as parameters, and local rates for elements in between as tabular data.

## ILMATRIX

### 10.41 ILMATRIX—An Individualized Linear Matrix for each particle for fast symplectic tracking with chromatic and amplitude-dependent effects

An Individualized Linear Matrix for each particle for fast symplectic tracking with chromatic and amplitude-dependent effects

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description   |
|----------------|---------|--------|---------|---|
| L              | $M$     | double | 0.0     | Length (used for position and time-of-flight computation) |
| NUX            |         | double | 0.0     | Horizontal tune   |
| NUY            |         | double | 0.0     | Vertical tune   |
| NUX1M          |         | double | 0.0     | First chromatic derivative of the horizontal tune         |
| NUY1M          |         | double | 0.0     | First chromatic derivative of the vertical tune           |
| NUX2M          |         | double | 0.0     | Second chromatic derivative of the horizontal tune        |
| NUY2M          |         | double | 0.0     | Second chromatic derivative of the vertical tune          |
| NUX3M          |         | double | 0.0     | Third chromatic derivative of the horizontal tune         |
| NUY3M          |         | double | 0.0     | Third chromatic derivative of the vertical tune           |
| NUX1AX         | $1/M$   | double | 0.0     | First amplitude derivative of the horizontal tune wrt Ax  |
| NUY1AX         | $1/M$   | double | 0.0     | First amplitude derivative of the vertical tune wrt Ax    |
| NUX1AY         | $1/M$   | double | 0.0     | First amplitude derivative of the horizontal tune wrt Ay  |
| NUY1AY         | $1/M$   | double | 0.0     | First amplitude derivative of the vertical tune wrt Ay    |
| NUX2AX         | $1/M^2$ | double | 0.0     | Second amplitude derivative of the horizontal tune wrt Ax |
| NUY2AX         | $1/M^2$ | double | 0.0     | Second amplitude derivative of the vertical tune wrt Ax   |
| NUX2AY         | $1/M^2$ | double | 0.0     | Second amplitude derivative of the horizontal tune wrt Ay |
| NUY2AY         | $1/M^2$ | double | 0.0     | Second amplitude derivative of the vertical tune wrt Ay   |

## ILMATRIX continued

An Individualized Linear Matrix for each particle for fast symplectic tracking with chromatic and amplitude-dependent effects

| Parameter Name | Units   | Type   | Default | Description   |
|----------------|---------|--------|---------|---|
| NUX1AX1AY      | $1/M^2$ | double | 0.0     | Amplitude derivative of the horizontal tune wrt Ax and Ay |
| NUY1AX1AY      | $1/M^2$ | double | 0.0     | Amplitude derivative of the vertical tune wrt Ax and Ay   |
| BETAX          | $M$     | double | 0.0     | On-momentum horizontal beta function                      |
| BETAY          | $M$     | double | 0.0     | On-momentum vertical beta function                        |
| BETAX1M        | $M$     | double | 0.0     | First chromatic derivative of horizontal beta function    |
| BETAY1M        | $M$     | double | 0.0     | First chromatic derivative of vertical beta function      |
| ALPHAX         |         | double | 0.0     | On-momentum horizontal alpha function                     |
| ALPHAY         |         | double | 0.0     | On-momentum vertical alpha function                       |
| ALPHAX1M       |         | double | 0.0     | First chromatic derivative of horizontal alpha function   |
| ALPHAY1M       |         | double | 0.0     | First chromatic derivative of vertical alpha function     |
| ETAX           | $M$     | double | 0.0     | On-momentum horizontal eta function                       |
| ETAPX          |         | double | 0.0     | On-momentum horizontal eta' function                      |
| ETAY           | $M$     | double | 0.0     | On-momentum vertical eta function                         |
| ETAPY          |         | double | 0.0     | On-momentum vertical eta' function                        |
| ETAX1          | $M$     | double | 0.0     | First chromatic derivative of horizontal eta function     |
| ETAPX1         |         | double | 0.0     | First chromatic derivative of horizontal eta' function    |
| ETAY1          | $M$     | double | 0.0     | First chromatic derivative of vertical eta function       |
| ETAPY1         |         | double | 0.0     | First chromatic derivative of vertical eta' function      |

## ILMATRIX continued

An Individualized Linear Matrix for each particle for fast symplectic tracking with chromatic and amplitude-dependent effects

| Parameter Name  | Units      | Type   | Default | Description  |
|-----------------|------------|--------|---------|--|
| ALPHAC          |            | double | 0.0     | First-order momentum compaction factor   |
| ALPHAC2         |            | double | 0.0     | Second-order momentum compaction factor  |
| ALPHAC3         |            | double | 0.0     | Third-order momentum compaction factor   |
| DS1AX           |            | double | 0.0     | First amplitude derivative of the path length wrt Ax   |
| DS1AY           |            | double | 0.0     | First amplitude derivative of the path length wrt Ay   |
| DS2AX           | $1/M$      | double | 0.0     | Second amplitude derivative of the path length wrt Ax  |
| DS2AY           | $1/M$      | double | 0.0     | Second amplitude derivative of the path length wrt Ay  |
| DS1AX1AY        | $1/M$      | double | 0.0     | Amplitude derivative of the path length wrt Ax and Ay  |
| TILT            | <i>RAD</i> | double | 0.0     | Rotation angle about the longitudinal axis.  |
| CROSS_RESONANCE |            | short  | 0       | If zero, then particles that cross an integer or half-integer resonance are considered lost.   |
| VERBOSITY       |            | short  | 0       | If nonzero, then information about particle losses is printed out.   |
| GROUP           |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows fast, symplectic tracking of transport through a periodic cell with chromatic and amplitude-dependent tunes, beta functions, and dispersion. This is done by computing a linear matrix for every particle using Twiss parameters, tunes, dispersion, etc., supplied by the user. The user can also supply selected chromatic and amplitude derivatives of these quantities, which are used to compute the individual particle's beta functions, tune, dispersion, etc., which in turn allows computing the individual particle's linear matrix.

The starting point is the well-known expression for the one-turn linear matrix in terms of the lattice functions

$$R_q = \begin{pmatrix} \cos 2\pi\nu_q + \alpha_q \sin 2\pi\nu_q & \beta_q \sin 2\pi\nu_q \\ -\gamma_q \sin 2\pi\nu_q & \cos 2\pi\nu_q - \alpha_q \sin 2\pi\nu_q \end{pmatrix} \quad (46)$$

where  $\nu_q$  is the tune in the  $q$  plane. We can expand the quantities in the matrix using

$$\nu_q = \nu_{q,0} + \sum_{n=1}^3 \left( \frac{\partial^n \nu_q}{\partial \delta^n} \right)_0 \frac{\delta^n}{n!} + \sum_{n=1}^2 \left( \frac{\partial^n \nu_q}{\partial A_x^n} \right)_0 \frac{A_x^n}{n!} + \sum_{n=1}^2 \left( \frac{\partial^n \nu_q}{\partial A_y^n} \right)_0 \frac{A_y^n}{n!} + \left( \frac{\partial^2 \nu_q}{\partial A_x \partial A_y} \right)_0 A_x A_y \quad (47)$$

where  $\delta = (p - p_0)/p_0$  is the fractional momentum offset,  $A_q = (q_\beta^2 + (\alpha_q q_\beta + \beta_q q'_\beta)^2)/\beta_q$  is the betatron amplitude, and the betatron coordinates are computed using

$$q_\beta = q - \delta \left( \eta_q + \left( \frac{\partial \eta_q}{\partial \delta} \right)_0 \delta \right) \quad (48)$$

and

$$q'_\beta = q' - \delta \left( \eta'_q + \left( \frac{\partial \eta'_q}{\partial \delta} \right)_0 \delta \right) \quad (49)$$

At each turn,  $\delta$ ,  $A_x$ , and  $A_y$  are computed for each particle. The user-supplied values of the various derivatives are then used to compute the tunes for each particle. Similar expansions are used to compute the other lattice functions. This allows computing the 2x2 transfer matrices for the betatron coordinates in the x and y planes, then advancing the betatron coordinates one turn, after which the full coordinates are recomputed by adding back the momentum-dependent closed orbit.

The pathlength is computed using the expansion

$$\Delta s = L \sum_{n=1}^3 \alpha_{c,n} \delta^n + \sum_{n=1}^4 R_{5n} x_{\beta,n} + \sum_{n=1}^2 \left( \frac{\partial^n s}{\partial A_x^n} \right)_0 \frac{A_x^n}{n!} + \sum_{n=1}^2 \left( \frac{\partial^n s}{\partial A_y^n} \right)_0 \frac{A_y^n}{n!} + \left( \frac{\partial^2 s}{\partial A_x \partial A_y} \right)_0 A_x A_y \quad (50)$$

where  $\alpha_{c,1}$  is the linear momentum compaction factor. Note that in keeping with convention the higher-order momentum compaction is expressed by polynomial coefficients, not derivatives. The terms dependent on betatron amplitude are expressed in terms of the more typical derivatives. Note the difference between the  $R_{5n}$  terms (added in version 2019.4) and those dependent on  $A_{x,y}$ : the former are oscillatory while the latter will accumulate. The `frequency_map` command can be used to compute path-length dependence on betatron amplitude.

Using this element is very similar to using the `setup_linear_chromatic_tracking` command. The advantage is that using `LMATRIX`, one can split a ring into segments and place, for example, impedance elements between the segments.

This element was inspired by requests from Y. Chae (APS).

N.B.: There is a bug related to using `ILMATRIX` that will result in a crash if one does not request computation of the twiss parameters. If you encounter this problem, just add the following statement after the `run_setup` command:

```
&twiss_output
    matched = 1
&end
```

## IONEFFECTS

### 10.42 IONEFFECTS—Simulates ionization of residual gas and interaction with the beam.

Simulates ionization of residual gas and interaction with the beam.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name           | Units | Type   | Default | Description   |
|--------------------------|-------|--------|---------|---|
| DISABLE                  |       | long   | 0       | If non-zero, turn off ion effects in the region covered by this element.  |
| MACRO_IONS               |       | long   | 0       | If positive, overrides the default value set in the ion_effects command, giving the number of macro ions generated per bunch passage. |
| GENERATION_INTERVAL      |       | long   | 0       | If positive, overrides the default value set in the ion_effects command, giving the number of macro ions generated per bunch passage. |
| X_SPAN                   |       | double | 0.0     | If positive, gives the region over which ions are kept.   |
| Y_SPAN                   |       | double | 0.0     | If positive, gives the region over which ions are kept.   |
| X_BIN_DIVISOR            |       | double | 0.0     | If positive, gives the ratio of electron beam sigma to bin size for ion field calculation.  |
| Y_BIN_DIVISOR            |       | double | 0.0     | If positive, gives the ratio of electron beam sigma to bin size for ion field calculation.  |
| X_RANGE_MULTIPLIER       |       | double | 0.0     | If positive, gives the ratio of ion binning region size to ion 80% x range.   |
| Y_RANGE_MULTIPLIER       |       | double | 0.0     | If positive, gives the ratio of ion binning region size to ion 80% y range.   |
| X_SIGMA_LIMIT_MULTIPLIER |       | double | 0.0     | If positive, gives lower limit on bi-gaussian fit sigma values in units of the ion bin size.  |
| Y_SIGMA_LIMIT_MULTIPLIER |       | double | 0.0     | If positive, gives lower limit on bi-gaussian fit sigma values in units of the ion bin size.  |



## IONEFFECTS continued

Simulates ionization of residual gas and interaction with the beam.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| STARTPASS      |       | long   | 0       | If positive, gives the pass on which ion effects start.  |
| ENDPASS        |       | long   | -1      | If positive, gives the pass on which ion effects end.  |
| PASSINTERVAL   |       | long   | 1       | Interval between ion effects modeling.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

NB: This element is new and considered experimental. Please report issues back to the developers.

This element provides serial or parallel simulation of the interaction of residual gas ions with the electron beam. It must be used in concert with the `ion_effects` command, described in 7.30.

Modeling of residual ions has these features:

- s-dependent gas pressure profiles for any number of species.
- Arbitrary ion species, specified by a user-provided file that includes the cross sections.
- User-defined locations for ion generation. Each **IONEFFECTS** element represents the ions present in a segment of the accelerator. The segments start and end half way between successive **IONEFFECTS** elements.
- Arbitrary fill patterns. Uniform fills can be set up using the `bunched_beam` command, while custom fills can be set up by generating the beam externally and using the `sdds_beam` command.
- Multiple ionization of trapped ions. For example, a CO<sup>+</sup> ion could multiply ionize into CO<sup>++</sup>, or dissociate into C<sup>+</sup>.

Some limitations of the model include:

- Fields from electron bunches are computed based on gaussian parameters, which is a reasonably good approximation.
- By default, fields from ions are computed based on gaussian parameters, which is often a somewhat poor approximation. Alternatively, a bi-gaussian form may be used, which uses a sum of two gaussians. This is a much better approximation to the typical distribution, which often has a hot core and long tails.
- Ions move only transversely and exist only outside of magnets.

Performing ion simulations involves the following steps

1. Prepare file describing the ion properties, as described in 7.30. Each ion is generated by either a source gas or source ion.
2. Prepare file giving gas pressure vs s for the source gases described in the ion properties file.
3. Insert **IONEFFECTS** elements in the lattice. This can be performed using the **insert\_elements** command (described in 7.28), or manually by editing the lattice file.
4. Insert **ion\_effects** command after the **run\_setup** command. See 7.30 for syntax. Note that certain properties of the individual **IONEFFECTS** elements can override the global settings given by in the **ion\_effects** command.
5. Generate a bunched beam, using either the **bunched\_beam** command or providing an externally-generated beam to the **sdds\_beam** command. Section 6 gives more information about bunched beams in **elegant**.

For each bunch passage, the **IONEFFECTS** element does the following:

1. Advance existing ions during bunch gap
2. Eliminate ions that are outside of given boundaries
3. Generate ions
4. Apply kick from beam to ions
5. Apply kick from ions to beam

The line density of ions generated by a single bunch in a single pass is:

$$\lambda_{ion} = \sigma_{ion} \frac{P}{k_B T} N_b \quad (51)$$

where  $\sigma_{ion}$  is the ionization cross section,  $P$  is the pressure,  $k_B$  is the Boltzmann constant,  $T$  is the temperature, and  $N_b$  is the bunch population.

The resulting macroparticle charge is:

$$Q_{macro} = \frac{10^{-22} e}{7.5 \times 10^{-3} k_B} \frac{\sigma_{ion} P N_b L_{eff}}{n_{macro} T} \quad (52)$$

Here  $\sigma_{ion}$  has units of Mb,  $P$  has units of Torr,  $k_B = 1.38 \times 10^{-23}$  J/K,  $e$  is the electron charge,  $L_{eff}$  is the effective length of the ion element (in m), and  $n_{macro}$  is the number of macroparticles generated. The initial ion distribution follows the bunch distribution (assumed to be Gaussian).

The **IONEFFECTS** element also supports multiple ionization. In the **ion\_properties** file, one can define the **SourceName** for a given **IonName** to be another ion. In this case, each macro-ion of type **SourceName** has a chance of being multiply ionized into type **IonName**. The calculation is done every **multiple\_ionization\_interval** bunch passes. The probability of multiple ionization depends on the cross section and local beam density.

The kick on the ions from the beam is calculated using the Basetti-Erskine formula [52], which assumes the beam is Gaussian in both transverse dimensions. This may be a poor assumption for the ions, in which case the **field\_calculation\_method** parameter can be set to **bigaussian**, which

uses a sum of two gaussians. This provides a much better model for the actual distribution, at the expense of a considerable increase in run time. The `ion_bin_divisor` and `ion_range_multiplier` parameters can be used to control the bin size and range, respectively, of the histogram used to approximate the ion charge distribution. The `ion_bin_divisor` gives the ratio of the rms size of the electron bunch in the plane in question to the bin size.

The `ion_range_multiplier` parameter is used to determine the range of the histogram. If positive, a rough histogram of the ion distribution (with ten times the desired bin size) is used to estimate the range required to encompass 80% of the ions; half this value is multiplied by the absolute value of `ion_range_multiplier` to get the half range of the full histogram; a value of 1.5 is suggested. If zero, the histogram encompasses all of the ions, which may result in a sparse histogram when a few ions have large coordinates. If negative gives the range of the binned coordinates in units of the rms size of the ion distribution.

The `ion_histogram_output` parameter and related parameters can be used to request output of the ion distribution and the bi-gaussian fit, which is advisable when setting the binning parameters.

The change in momentum of an ion due to the bunch passage is:

$$\Delta p_y + i\Delta p_x = \frac{cN_b r_e m_e}{\gamma} \sqrt{\frac{2\pi}{\sigma_x^2 - \sigma_y^2}} \left[ w \left( \frac{x + iy}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) - \exp \left( \frac{-x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2} \right) w \left( \frac{\frac{\sigma_y}{\sigma_x}x + i\frac{\sigma_x}{\sigma_y}y}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) \right] \quad (53)$$

where  $c$  is the speed of light,  $N_b$  is the bunch population,  $r_e$  is the classical electron radius ( $2.82 \times 10^{-15}$  m),  $m_e$  is the electron mass,  $\gamma$  is the relativistic factor ( $\sim 1$  for the ions),  $\sigma_{x,y}$  are the horizontal and vertical beam sizes,  $w$  is the complex error function, and  $x$  and  $y$  are the distance from the ion to the bunch center.

## KICKER

### 10.43 KICKER—A combined horizontal-vertical steering magnet implemented as a matrix, up to 2nd order. For time-dependent kickers, see BUMPER.

A combined horizontal-vertical steering magnet implemented as a matrix, up to 2nd order. For time-dependent kickers, see BUMPER.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| HKICK          | $RAD$   | double | 0.0     | x kick angle   |
| VKICK          | $RAD$   | double | 0.0     | y kick angle   |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| B2             | $1/M^2$ | double | 0.0     | normalized sextupole strength (e.g., kick = $KICK*(1+B2*x^2)$ )  |
| HCALIBRATION   |         | double | 1       | factor applied to obtain x kick  |
| VCALIBRATION   |         | double | 1       | factor applied to obtain y kick  |
| EDGE_EFFECTS   |         | long   | 0       | include edge effects?  |
| ORDER          |         | long   | 0       | matrix order   |
| STEERING       |         | long   | 1       | use for steering?  |
| SYNCH_RAD      |         | long   | 0       | include classical, single-particle synchrotron radiation?  |
| ISR            |         | long   | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| LERAD          |         | double | 0.0     | if L=0, use this length for radiation computations   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

# KOCT

## 10.44 KOCT—A canonical kick octupole.

A canonical kick octupole.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name        | Units   | Type   | Default | Description  |
|-----------------------|---------|--------|---------|--|
| L                     | $M$     | double | 0.0     | length   |
| K3                    | $1/M^4$ | double | 0.0     | geometric strength   |
| TILT                  | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| BORE                  | $M$     | double | 0.0     | bore radius  |
| B                     | $T$     | double | 0.0     | field at pole tip (used if bore nonzero)   |
| DX                    | $M$     | double | 0.0     | misalignment   |
| DY                    | $M$     | double | 0.0     | misalignment   |
| DZ                    | $M$     | double | 0.0     | misalignment   |
| FSE                   |         | double | 0.0     | fractional strength error  |
| N_KICKS               |         | long   | 4       | number of kicks (rounded up to next multipole of 4 if INTEGRATION_ORDER=4)   |
| SYSTEMATIC_MULTIPOLES |         | STRING | NULL    | input file for systematic multipoles   |
| RANDOM_MULTIPOLES     |         | STRING | NULL    | input file for random multipoles   |
| INTEGRATION_ORDER     |         | short  | 4       | integration order (2 or 4)   |
| SQRT_ORDER            |         | short  | 0       | Ignored, kept for backward compatibility only.   |
| SYNCH_RAD             |         | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                   |         | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| ISR1PART              |         | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| EXPAND_HAMILTONIAN    |         | short  | 0       | If 1, Hamiltonian is expanded to leading order.  |
| GROUP                 |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## KPOLY

### 10.45 KPOLY—A thin kick element with polynomial dependence on the coordinates in one plane.

A thin kick element with polynomial dependence on the coordinates in one plane.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units        | Type   | Default | Description  |
|----------------|--------------|--------|---------|--|
| COEFFICIENT    | $M^{-ORDER}$ | double | 0.0     | coefficient of polynomial  |
| TILT           | $RAD$        | double | 0.0     | rotation about longitudinal axis   |
| DX             | $M$          | double | 0.0     | misalignment   |
| DY             | $M$          | double | 0.0     | misalignment   |
| DZ             | $M$          | double | 0.0     | misalignment   |
| FACTOR         |              | double | 1       | additional factor to apply   |
| ORDER          |              | long   | 0       | order of polynomial  |
| PLANE          |              | STRING | x       | plane to kick (x, y)   |
| GROUP          |              | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## KQUAD

### 10.46 KQUAD—A canonical kick quadrupole.

A canonical kick quadrupole.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name              | Units   | Type   | Default | Description  |
|-----------------------------|---------|--------|---------|--|
| L                           | $M$     | double | 0.0     | length   |
| K1                          | $1/M^2$ | double | 0.0     | geometric strength   |
| TILT                        | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| BORE                        | $M$     | double | 0.0     | bore radius  |
| B                           | $T$     | double | 0.0     | pole tip field (used if bore nonzero)                                      |
| DX                          | $M$     | double | 0.0     | misalignment   |
| DY                          | $M$     | double | 0.0     | misalignment   |
| DZ                          | $M$     | double | 0.0     | misalignment   |
| FSE                         |         | double | 0.0     | fractional strength error  |
| N_KICKS                     |         | long   | 4       | number of kicks (rounded up to next multipole of 4 if INTEGRATION_ORDER=4) |
| HKICK                       | $RAD$   | double | 0.0     | horizontal correction kick   |
| VKICK                       | $RAD$   | double | 0.0     | vertical correction kick   |
| HCALIBRATION                |         | double | 1       | calibration factor for horizontal correction kick                          |
| VCALIBRATION                |         | double | 1       | calibration factor for vertical correction kick                            |
| HSTEERING                   |         | short  | 0       | use for horizontal correction?   |
| VSTEERING                   |         | short  | 0       | use for vertical correction?   |
| SYNCH_RAD                   |         | short  | 0       | include classical, single-particle synchrotron radiation?                  |
| SYSTEMATIC_MULTIPOLES       |         | STRING | NULL    | input file for systematic multipoles                                       |
| EDGE_MULTIPOLES             |         | STRING | NULL    | input file for systematic edge multipoles                                  |
| RANDOM_MULTIPOLES           |         | STRING | NULL    | input file for random multipoles   |
| STEERING_MULTIPOLES         |         | STRING | NULL    | input file for multipole content of steering kicks                         |
| SYSTEMATIC_MULTIPOLE_FACTOR |         | double | 1       | Factor by which to multiply systematic and edge multipoles                 |

## KQUAD continued

A canonical kick quadrupole.

| Parameter Name            | Units | Type   | Default | Description  |
|---------------------------|-------|--------|---------|--|
| RANDOM_MULTIPOLE_FACTOR   |       | double | 1       | Factor by which to multiply random multipoles                                |
| STEERING_MULTIPOLE_FACTOR |       | double | 1       | Factor by which to multiply steering multipoles                              |
| INTEGRATION_ORDER         |       | short  | 4       | integration order (2 or 4)   |
| SQRT_ORDER                |       | short  | 0       | Ignored, kept for backward compatibility only.                               |
| ISR                       |       | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?               |
| ISR1PART                  |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1            |
| EDGE1_EFFECTS             |       | short  | 0       | include entrance edge effects?   |
| EDGE2_EFFECTS             |       | short  | 0       | include exit edge effects?   |
| LEFFECTIVE                | $M$   | double | 0.0     | Effective length. Ignored if non-positive.                                   |
| I0P                       | $M$   | double | 0.0     | i0+ fringe integral  |
| I1P                       | $M^2$ | double | 0.0     | i1+ fringe integral  |
| I2P                       | $M^3$ | double | 0.0     | i2+ fringe integral  |
| I3P                       | $M^4$ | double | 0.0     | i3+ fringe integral  |
| LAMBDA2P                  | $M^3$ | double | 0.0     | lambda2+ fringe integral   |
| I0M                       | $M$   | double | 0.0     | i0- fringe integral  |
| I1M                       | $M^2$ | double | 0.0     | i1- fringe integral  |
| I2M                       | $M^3$ | double | 0.0     | i2- fringe integral  |
| I3M                       | $M^4$ | double | 0.0     | i3- fringe integral  |
| LAMBDA2M                  | $M^3$ | double | 0.0     | lambda2- fringe integral   |
| EDGE1_LINEAR              |       | short  | 1       | Use to selectively turn off linear part if EDGE1_EFFECTS nonzero.            |
| EDGE2_LINEAR              |       | short  | 1       | Use to selectively turn off linear part if EDGE2_EFFECTS nonzero.            |
| EDGE1_NONLINEAR_FACTOR    |       | double | 1       | Use to selectively scale non-linear entrance edge effects if EDGE1_EFFECTS>1 |



## KQUAD continued

A canonical kick quadrupole.

| Parameter Name         | Units | Type   | Default | Description  |
|------------------------|-------|--------|---------|--|
| EDGE2_NONLINEAR_FACTOR |       | double | 1       | Use to selectively scale non-linear exit edge effects if EDGE2_EFFECTS>1   |
| RADIAL                 |       | short  | 0       | If non-zero, converts the quadrupole into a radially-focusing lens   |
| EXPAND_HAMILTONIAN     |       | short  | 0       | If 1, Hamiltonian is expanded to leading order.  |
| TRACKING_MATRIX        |       | short  | 0       | If nonzero, gives order of tracking-based matrix up to third order to be used for twiss parameters etc. If zero, 2nd-order analytical matrix is used.      |
| GROUP                  |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a quadrupole using a kick method based on symplectic integration. The user specifies the number of kicks and the order of the integration. For computation of twiss parameters and response matrices, this element is treated like a standard thick-lens quadrupole; i.e., the number of kicks and the integration order become irrelevant.

Specification of systematic and random multipole errors is supported through the **SYSTEMATIC\_MULTIPOLES**, **EDGE\_MULTIPOLES**, and **RANDOM\_MULTIPOLES** fields. These specify, respectively, fixed multipole strengths for the body of the element, fixed multipole strengths for the edges of the element, and random multipole strengths for the body of the element. These fields give the names of SDDS files that supply the multipole data. The files are expected to contain a single page of data with the following elements:

1. Floating point parameter **referenceRadius** giving the reference radius for the multipole data.
2. An integer column named **order** giving the order of the multipole. The order is defined as  $(N_{poles} - 2)/2$ , so a quadrupole has order 1, a sextupole has order 2, and so on.
3. Floating point columns **normal** and **skew** giving the values for the normal and skew multipole strengths, respectively. (N.B.: previous versions used the names **an** and **bn**, respectively. This is still accepted but deprecated) These are defined as a fraction of the main field strength measured at the reference radius, R:  $f_n = \frac{K_n R^n / n!}{K_m R^m / m!}$ , where  $m = 1$  is the order of the main field and  $n$  is the order of the error multipole. A similar relationship holds for the skew multipole fractional strengths. For random multipoles, the values are interpreted as rms values for the distribution.

Specification of systematic higher multipoles due to steering fields is supported through the **STEERING\_MULTIPOLES** field. This field gives the name of an SDDS file that supplies the multipole data. The file is expected to contain a single page of data with the following elements:

1. Floating point parameter **referenceRadius** giving the reference radius for the multipole data.
2. An integer column named **order** giving the order of the multipole. The order is defined as  $(N_{poles} - 2)/2$ . The order must be an even number because of the quadrupole symmetry.
3. Floating point column **normal** giving the values for the normal multipole strengths, which are driven by the horizontal steering field. (N.B.: previous versions used the name **an** for this data. This is still accepted but deprecated) **normal** specifies the multipole strength as a fraction  $f_n$  of the steering field strength measured at the reference radius, R:  $f_n = \frac{K_n R^n / n!}{K_m R^m / m!}$ , where  $m = 0$  is the order of the steering field and  $n$  is the order of the error multipole. The skew values (for vertical steering) are deduced from the **normal** values, specifically,  $g_n = f_n * (-1)^{n/2}$ .

The dominant systematic multipole term in the steering field is a sextupole. Note that **elegant** presently *does not* include such sextupole contributions in the computation of the chromaticity via the **twiss\_output** command. However, these chromatic effects will be seen in tracking.

Apertures specified via an upstream **MAXAMP** element or an **aperture\_input** command will be imposed inside this element.

As of version 29.2, this element incorporates the ability to have different values for the insertion and effective lengths. This is invoked when **LEFFECTIVE** is positive. In this case, the **L** parameter is understood to be the physical insertion length. Using **LEFFECTIVE** is a convenient way to incorporate the fact that the effective length may differ from the physical length and even vary with excitation, without having to modify the drift spaces on either side of the quadrupole element.

Fringe field effects are based on publications of D. Zhuo *et al.* [34] and J. Irwin *et al.* [35], as well as unpublished work of C. X. Wang (ANL). The fringe field is characterized by 10 integrals given in equations 19, 20, and 21 of [34]. However, the values input into **elegant** should be normalized by  $K_1$  or  $K_1^2$ , as appropriate.

For the exit-side fringe field, let  $s_1$  be the center of the magnet,  $s_0$  be the location of the nominal end of the magnet (for a hard-edge model), and let  $s_2$  be a point well outside the magnet. Using  $K_{1,he}(s)$  to represent the hard edge model and  $K_1(s)$  the actual field profile, we define the normalized difference as  $\tilde{k}(s) = (K_1(s) - K_{1,he}(s))/K_1(s_1)$ . (Thus,  $\tilde{k}(s) = \tilde{K}(s)/K_0$ , using the notation of Zhou *et al.*)

The integrals to be input to **elegant** are defined as

$$i_0^- = \int_{s_1}^{s_0} \tilde{k}(s) ds \quad i_0^+ = \int_{s_0}^{s_2} \tilde{k}(s) ds \quad (54)$$

$$i_1^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0) ds \quad i_1^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0) ds \quad (55)$$

$$i_2^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0)^2 ds \quad i_2^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0)^2 ds \quad (56)$$

$$i_3^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0)^3 ds \quad i_3^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0)^3 ds \quad (57)$$

$$\lambda_2^- = \int_{s_1}^{s_0} ds \int_s^{s_0} ds' \tilde{k}(s) \tilde{k}(s')(s' - s) \quad \lambda_2^+ = \int_{s_0}^{s_2} ds \int_s^{s_2} ds' \tilde{k}(s) \tilde{k}(s')(s' - s) \quad (58)$$

Normally, the effects are dominated by  $i_1^-$  and  $i_1^+$ . The script `computeQuadFringeIntegrals`, packaged with `elegant`, allows computing these integrals and the effective length if provided with data giving the gradient vs  $s$ .

The `EDGE1_EFFECTS` and `EDGE2_EFFECTS` parameters can be used to turn fringe field effects on and off, but also to control the order of the implementation. If the value is 1, linear fringe effects are included. If the value is 2, leading-order (cubic) nonlinear effects are included. If the value is 3 or higher, higher order effects are included.

## KQUSE

### 10.47 KQUSE—A canonical kick element combining quadrupole and sextupole fields.

A canonical kick element combining quadrupole and sextupole fields.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name     | Units   | Type   | Default | Description  |
|--------------------|---------|--------|---------|--|
| L                  | $M$     | double | 0.0     | length   |
| K1                 | $1/M^2$ | double | 0.0     | geometric quadrupole strength  |
| K2                 | $1/M^3$ | double | 0.0     | geometric sextupole strength   |
| TILT               | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| DX                 | $M$     | double | 0.0     | misalignment   |
| DY                 | $M$     | double | 0.0     | misalignment   |
| DZ                 | $M$     | double | 0.0     | misalignment   |
| FSE1               | $M$     | double | 0.0     | fractional strength error for K1   |
| FSE2               | $M$     | double | 0.0     | fractional strength error for K2   |
| N_KICKS            |         | long   | 4       | number of kicks  |
| INTEGRATION_ORDER  |         | short  | 4       | integration order (2 or 4)   |
| SYNCH_RAD          |         | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR                |         | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| ISR1PART           |         | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| MATRIX_TRACKING    |         | short  | 0       | For testing only.  |
| EXPAND_HAMILTONIAN |         | short  | 0       | If 1, Hamiltonian is expanded to leading order.  |
| GROUP              |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## KSEXT

### 10.48 KSEXT—A canonical kick sextupole, which differs from the MULT element with ORDER=2 in that it can be used for chromaticity correction.

A canonical kick sextupole, which differs from the MULT element with ORDER=2 in that it can be used for chromaticity correction.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name        | Units   | Type   | Default | Description  |
|-----------------------|---------|--------|---------|--|
| L                     | $M$     | double | 0.0     | length   |
| K2                    | $1/M^3$ | double | 0.0     | geometric strength   |
| K1                    | $1/M^2$ | double | 0.0     | geometric quadrupole strength error. See notes below!                      |
| J1                    | $1/M^2$ | double | 0.0     | geometric skew quadrupole strength error. See notes below!                 |
| TILT                  | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| BORE                  | $M$     | double | 0.0     | bore radius  |
| B                     | $T$     | double | 0.0     | field at pole tip (used if bore nonzero)                                   |
| N_KICKS               |         | long   | 4       | number of kicks (rounded up to next multipole of 4 if INTEGRATION_ORDER=4) |
| DX                    | $M$     | double | 0.0     | misalignment   |
| DY                    | $M$     | double | 0.0     | misalignment   |
| DZ                    | $M$     | double | 0.0     | misalignment   |
| FSE                   |         | double | 0.0     | fractional strength error  |
| HKICK                 | $RAD$   | double | 0.0     | horizontal correction kick   |
| VKICK                 | $RAD$   | double | 0.0     | vertical correction kick   |
| HCALIBRATION          |         | double | 1       | calibration factor for horizontal correction kick                          |
| VCALIBRATION          |         | double | 1       | calibration factor for vertical correction kick                            |
| HSTEERING             |         | short  | 0       | use for horizontal correction?   |
| VSTEERING             |         | short  | 0       | use for vertical correction?   |
| SYNCH_RAD             |         | short  | 0       | include classical, single-particle synchrotron radiation?                  |
| SYSTEMATIC_MULTIPOLES |         | STRING | NULL    | input file for systematic multipoles                                       |
| EDGE_MULTIPOLES       |         | STRING | NULL    | input file for systematic edge multipoles                                  |

## KSEXT continued

A canonical kick sextupole, which differs from the MULT element with ORDER=2 in that it can be used for chromaticity correction.

| Parameter Name              | Units | Type   | Default | Description  |
|-----------------------------|-------|--------|---------|--|
| RANDOM_MULTIPOLES           |       | STRING | NULL    | input file for random multipoles   |
| STEERING_MULTIPOLES         |       | STRING | NULL    | input file for multipole content of steering kicks   |
| SYSTEMATIC_MULTIPOLE_FACTOR |       | double | 1       | Factor by which to multiply systematic and edge multipoles   |
| RANDOM_MULTIPOLE_FACTOR     |       | double | 1       | Factor by which to multiply random multipoles  |
| STEERING_MULTIPOLE_FACTOR   |       | double | 1       | Factor by which to multiply steering multipoles  |
| INTEGRATION_ORDER           |       | short  | 4       | integration order (2 or 4)   |
| SQRT_ORDER                  |       | short  | 0       | Ignored, kept for backward compatibility only.   |
| ISR                         |       | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| ISR1PART                    |       | short  | 1       | Include ISR for single-particle beam only if ISR=1 and ISR1PART=1  |
| EXPAND_HAMILTONIAN          |       | short  | 0       | If 1, Hamiltonian is expanded to leading order.  |
| GROUP                       |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a sextupole using a kick method based on symplectic integration. The user specifies the number of kicks and the order of the integration. For computation of twiss parameters, chromaticities, and response matrices, this element is treated like a standard thick-lens sextupole; i.e., the number of kicks and the integration order become irrelevant. Specification of systematic and random multipole errors is supported through the **SYSTEMATIC\_MULTIPOLES**, **EDGE\_MULTIPOLES**, and **RANDOM\_MULTIPOLES** fields. These specify, respectively, fixed multipole strengths for the body of the element, fixed multipole strengths for the edges of the element, and random multipole strengths for the body of the element. These fields give the names of SDDS files that supply the multipole data. The files are expected to contain a single page of data with the following elements:

1. Floating point parameter **referenceRadius** giving the reference radius for the multipole data.

2. An integer column named **order** giving the order of the multipole. The order is defined as  $(N_{poles} - 2)/2$ , so a quadrupole has order 1, a sextupole has order 2, and so on.
3. Floating point columns **normal** and **skew** giving the values for the normal and skew multipole strengths, respectively. (N.B.: previous versions used the names **an** and **bn**, respectively. This is still accepted but deprecated) These are defined as a fraction of the main field strength measured at the reference radius, R:  $f_n = \frac{K_n R^n / n!}{K_m R^m / m!}$ , where  $m = 2$  is the order of the main field and  $n$  is the order of the error multipole. A similar relationship holds for the skew multipole fractional strengths. For random multipoles, the values are interpreted as rms values for the distribution.

Specification of systematic higher multipoles due to steering fields is supported through the **STEERING\_MULTIPOLES** field. This field gives the name of an SDDS file that supplies the multipole data. The file is expected to contain a single page of data with the following elements:

1. Floating point parameter **referenceRadius** giving the reference radius for the multipole data.
2. An integer column named **order** giving the order of the multipole. The order is defined as  $(N_{poles} - 2)/2$ . The order must be an even number because of the quadrupole symmetry.
3. Floating point column **normal** giving the values for the normal multipole strengths, which are driven by the horizontal steering field. (N.B.: previous versions used the name **an** for this data. This is still accepted but deprecated) **normal** specifies the multipole strength as a fraction  $f_n$  of the steering field strength measured at the reference radius, R:  $f_n = \frac{K_n R^n / n!}{K_m R^m / m!}$ , where  $m = 0$  is the order of the steering field and  $n$  is the order of the error multipole. The skew values (for vertical steering) are deduced from the **normal** values, specifically,  $g_n = f_n * (-1)^{n/2}$ .

Another way of introducing errors is via the **K1** and **J1** parameters, which allow introducing a normal and skew quadrupole **error** term. For tracking, the strength of these values can be arbitrarily high without introducing errors. However, the matrix analysis (e.g., for determination of tunes and beta functions) assumes that these are weak effects and high accuracy should not be expected if this is not true. If **K1** is significant, then use of the **KQUSE** element is preferred.

Apertures specified via an upstream **MAXAMP** element or an **aperture\_input** command will be imposed inside this element.

## LMIRROR

### 10.49 LMIRROR—A mirror for light optics

A mirror for light optics

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| RX             | $M$   | double | 0.0     | radius in horizontal plane   |
| RY             | $M$   | double | 0.0     | radius in vertical plane   |
| THETA          | $RAD$ | double | 0.0     | angle of incidence (in horizontal plane)   |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| DZ             | $M$   | double | 0.0     | misalignment   |
| TILT           | $RAD$ | double | 0.0     | misalignment rotation about longitudinal axis  |
| YAW            | $RAD$ | double | 0.0     | misalignment rotation about vertical axis  |
| PITCH          | $RAD$ | double | 0.0     | misalignment rotation about transverse horizontal axis   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |



## LRWAKE

### 10.50 LRWAKE—Long-range (inter-bunch and inter-turn) longitudinal and transverse wake

Long-range (inter-bunch and inter-turn) longitudinal and transverse wake

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| INPUTFILE      |       | STRING | NULL    | name of file giving Green function   |
| TCOLUMN        |       | STRING | NULL    | column in INPUTFILE containing time data                                   |
| WXCOLUMN       |       | STRING | NULL    | column in INPUTFILE containing horizontal dipole Green function            |
| WYCOLUMN       |       | STRING | NULL    | column in INPUTFILE containing vertical dipole Green function              |
| WZCOLUMN       |       | STRING | NULL    | column in INPUTFILE containing longitudinal Green function                 |
| QXCOLUMN       |       | STRING | NULL    | column in INPUTFILE containing horizontal quadrupole Green function        |
| QYCOLUMN       |       | STRING | NULL    | column in INPUTFILE containing vertical quadrupole Green function          |
| FACTOR         |       | double | 1       | factor by which to multiply wakes  |
| XFACTOR        |       | double | 1       | factor by which to multiply longitudinal wake                              |
| YFACTOR        |       | double | 1       | factor by which to multiply horizontal dipole wake                         |
| ZFACTOR        |       | double | 1       | factor by which to multiply vertical dipole wake                           |
| QXFACTOR       |       | double | 1       | factor by which to multiply horizontal quadrupole wake                     |
| QYFACTOR       |       | double | 1       | factor by which to multiply vertical quadrupole wake                       |
| URNS_TO_KEEP   |       | long   | 128     | number of turns of data to retain  |
| RAMP_PASSES    |       | long   | 0       | Number of passes over which to linearly ramp up the wake to full strength. |

## LRWAKE continued

Long-range (inter-bunch and inter-turn) longitudinal and transverse wake

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element provides serial and parallel modeling of long range, multi-bunch, multi-pass, non-resonant wakes. Resonant wakes can be modeled using the **\*RFMODE** elements, while short-range wakes are modeled with **WAKE**, **TRWAKE**, **ZLONGIT**, **ZTRANSVERSE**, and **RFCW**.

For the **LRWAKE** element, the beam is assumed to be bunched and wakes are computed bunch-to-bunch. The long-range wake is assumed to be constant within any single bunch.

To use this element, the beam has to be prepared in a special way so that **elegant** can recognize which particles belong to which bunches. See Section 6 for details. Given a properly prepared beam, the algorithm works as follows.

- Each processor uses arrays to record
  - How many particles are in each of  $B$  bunches,
  - The sum of the arrival times  $t$  at the **LRWAKE** element for the particles in each bunch, and
  - The sum of  $x$  and  $y$  at the **LRWAKE** element for the particles in each bunch.
- These arrays are summed across all the processors and used to compute the moments  $\langle t \rangle$ ,  $\langle x \rangle$ , and  $\langle y \rangle$  for each bunch, as well as the charge in each bunch.
- Arrays of length  $B$  from  $N$  prior turns are kept in a buffer
  - Buffer for turns  $N - 1$  to 1 is copied to slots  $N$  through 2, thus overwriting the data for the oldest turn.
  - The data for latest turn is copied into slot 1.
- For each bunch, sums are performed over all prior bunches/turns to compute the voltage. For the longitudinal wake, we have

$$V_z(b) = \sum_{i=b}^{N*B} q_i W_z(\langle t_b \rangle - \langle t_i \rangle). \quad (59)$$

A positive value *decelerates* the particle. For the horizontal dipole wake we have

$$V_x(b) = \sum_{i=b}^{N*B} q_i \langle x_i \rangle W_x(\langle t_b \rangle - \langle t_i \rangle), \quad (60)$$

with the vertical wake being similar. In both cases, a positive value deflects the particle toward positive  $x$  or  $y$  for a positive offset of the driving particle.

- The quadrupole wakes may also be included. In this case, the contribution to the horizontal wake is

$$V_x(b) = \sum_{i=b}^{N*B} q_i x_p W_x(\langle t_b \rangle - \langle t_i \rangle), \quad (61)$$

where  $x_p$  is the coordinate of the probe particle. The vertical wake is similar.

To use LRWAKE, the user provides the wakes (functions of  $t$ ) in an SDDS file. These wakes may extend over an arbitrary number of turns, with the user declaring how many turns to actually use as part of the element definition. However, they should be zero within the region occupied by a single bunch, to avoid double-counting with the true short-range wake. (Note that the above sums include the self-wake.) Similarly, the short-range should be zero for times comparable to the bunch spacing.

Note that the quadrupole wakes are in some cases related to the dipole wakes by constant numerical factors [48]. In such a case, one may name the same column for QXCOLUMN (QYCOLUMN) and WXCOLUMN (WYCOLUMN) and then specify QXFACTOR (QYFACTOR) appropriately.

## LSCDRIFT

### 10.51 LSCDRIFT—Longitudinal space charge impedance

Longitudinal space charge impedance

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name         | Units | Type   | Default | Description   |
|------------------------|-------|--------|---------|---|
| L                      | $M$   | double | 0.0     | length  |
| LEFFECTIVE             | $M$   | double | 0.0     | effective length (used if L=0)  |
| BINS                   |       | long   | 0       | number of bins for current histogram  |
| SMOOTHING              |       | short  | 0       | Use Savitzky-Golay filter to smooth current histogram?  |
| SG_HALFWIDTH           |       | short  | 1       | Savitzky-Golay filter half-width for smoothing current histogram  |
| SG_ORDER               |       | short  | 1       | Savitzky-Golay filter order for smoothing current histogram   |
| INTERPOLATE            |       | short  | 1       | Interpolate wake?   |
| LSC                    |       | short  | 1       | Include longitudinal space-charge impedance? If zero, acts like ordinary drift.   |
| AUTO_LEFFECTIVE        |       | short  | 0       | In nonzero and if L=0, the LEFFECTIVE parameter is set to the length of the previous element.   |
| LOW_FREQUENCY_CUTOFF0  |       | double | -1      | Highest spatial frequency at which low-frequency cutoff filter is zero. If not positive, no low-frequency cutoff filter is applied. Frequency is in units of Nyquist (0.5/binsize). |
| LOW_FREQUENCY_CUTOFF1  |       | double | -1      | Lowest spatial frequency at which low-frequency cutoff filter is 1. If not given, defaults to LOW_FREQUENCY_CUTOFF0.  |
| HIGH_FREQUENCY_CUTOFF0 |       | double | -1      | Spatial frequency at which smoothing filter begins. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize).                         |

## LSCDRIFT continued

Longitudinal space charge impedance

| Parameter Name         | Units | Type   | Default | Description  |
|------------------------|-------|--------|---------|--|
| HIGH_FREQUENCY_CUTOFF1 |       | double | -1      | Spatial frequency at which smoothing filter is 0. If not given, defaults to HIGH_FREQUENCY_CUTOFF0.  |
| RADIUS_FACTOR          |       | double | 1.7     | LSC radius is $(S_x + S_y)/2 * \text{RADIUS\_FACTOR}$  |
| GROUP                  |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates longitudinal space charge in a drift space using the method described in [22]. This is based on the longitudinal space charge impedance per unit length

$$Z_{lsc}(k) = \frac{iZ_0}{\pi k r_b^2} \left[ 1 - \frac{k r_b}{\gamma} K_1 \left( \frac{k r_b}{\gamma} \right) \right] \quad (62)$$

If L is 0 and LEFFECTIVE is not, then the element provides a LSC kick with impedance given by  $Z_{lsc} L_{effective}$ . This can be used to insert an LSC kick that integrates the longitudinal space charge effect of a section of a lattice. This should be used only for cases where there is very little relative longitudinal motion of particles.

Two simple filters are provided.

- The parameters HIGH\_FREQUENCY\_CUTOFF0 and HIGH\_FREQUENCY\_CUTOFF1 are used to filter out high frequencies, i.e., they provide a low-pass or noise filter. The filter has value 1 for  $f < \text{HIGH\_FREQUENCY\_CUTOFF0}$ , value 0 for  $f > \text{HIGH\_FREQUENCY\_CUTOFF1}$ , and linear variation in between.
- The parameters LOW\_FREQUENCY\_CUTOFF0 and LOW\_FREQUENCY\_CUTOFF1 are used to filter out low frequencies, i.e., they provide a high-pass filter. The filter has value 0 for  $f < \text{LOW\_FREQUENCY\_CUTOFF0}$ , value 1 for  $f > \text{LOW\_FREQUENCY\_CUTOFF1}$ , and linear variation in between.

]

## LSRMDLTR

### 10.52 LSRMDLTR—A non-symplectic numerically integrated planar undulator including optional co-propagating laser beam for laser modulation of the electron beam.

A non-symplectic numerically integrated planar undulator including optional co-propagating laser beam for laser modulation of the electron beam.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name   | Units       | Type   | Default                  | Description  |
|------------------|-------------|--------|--------------------------|--|
| L                | $M$         | double | 0.0                      | length   |
| BU               | $T$         | double | 0.0                      | Undulator peak field   |
| TGU_GRADIENT     | $1/M$       | double | 0.0                      | Transverse gradient divided by maximum on-axis field.  |
| TGU_COMP_FACTOR  | <i>NULL</i> | double | 1                        | Use to adjust constant field component to reduce trajectory error.   |
| PERIODS          |             | long   | 0                        | Number of undulator periods.   |
| METHOD           | <i>NULL</i> | STRING | non-adaptive runge-kutta | integration method (runge-kutta, bulirsch-stoer, modified-midpoint, two-pass modified-midpoint, leap-frog, non-adaptive runge-kutta) |
| FIELD_EXPANSION  | <i>NULL</i> | STRING | leading terms            | ideal, exact, or "leading terms"   |
| ACCURACY         | <i>NULL</i> | double | 0.0                      | Integration accuracy for adaptive integration. (Not recommended)   |
| N_STEPS          |             | long   | 0                        | Number of integration steps for non-adaptive integration.  |
| POLE_FACTOR1     |             | double | 0.1557150345504          | Strength factor for the first and last pole.   |
| POLE_FACTOR2     |             | double | 0.380687012288581        | Strength factor for the second and second-to-last pole.  |
| POLE_FACTOR3     |             | double | 0.802829337348179        | Strength factor for the third and third-to-last pole.  |
| LASER_WAVELENGTH | $M$         | double | 0.0                      | Laser wavelength. If zero, the wavelength is calculated from the resonance condition.  |
| LASER_PEAK_POWER | $W$         | double | 0.0                      | laser peak power   |
| LASER_W0         | $M$         | double | 1                        | laser spot size at waist, $w_0 = \sqrt{2}\sigma_x = \sqrt{2}\sigma_y$  |

## LSRMDLTR continued

A non-symplectic numerically integrated planar undulator including optional co-propagating laser beam for laser modulation of the electron beam.

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| LASER_PHASE    | <i>RAD</i>  | double | 0.0     | laser phase  |
| LASER_X0       | <i>M</i>    | double | 0.0     | laser horizontal offset at center of wiggler   |
| LASER_Y0       | <i>M</i>    | double | 0.0     | laser vertical offset at center of wiggler   |
| LASER_Z0       | <i>M</i>    | double | 0.0     | offset of waist position from center of wiggler  |
| LASER_TILT     | <i>RAD</i>  | double | 0.0     | laser tilt   |
| LASER_M        |             | short  | 0       | laser horizontal mode number (<5)  |
| LASER_N        |             | short  | 0       | laser vertical mode number (<5)  |
| SYNCH_RAD      |             | short  | 0       | Include classical, single-particle synchrotron radiation?  |
| ISR            |             | short  | 0       | Include quantum excitation?  |
| HELICAL        |             | short  | 0       | If non-zero, simulate helical undulator.   |
| TIME_PROFILE   | <i>NULL</i> | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving time-dependent modulation of the laser electric and magnetic fields.                            |
| TIME_OFFSET    | <i>S</i>    | double | 0.0     | Time offset of the laser profile.  |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a planar undulator, together with an optional co-propagating laser beam that can be used as a beam heater or modulator. The simulation is done by numerical integration of the Lorentz equation. It is not symplectic, and hence this element is not recommended for long-term tracking simulation of undulators in storage rings.

The fields in the undulator can be expressed in one of three ways. The FIELD\_EXPANSION parameter is used to control which method is used.

- The exact field, given by (see section 3.1.5 of the *Handbook of Accelerator Physics and Engineering*)

$$B_x = 0, \tag{63}$$

$$B_y = B_0 \cosh k_u y \cos k_u z, \quad (64)$$

and

$$B_z = -B_0 \sinh k_u y \sin k_u z, \quad (65)$$

where  $k_u = 2\pi/\lambda_u$  and  $\lambda_u$  is the undulator period. This is the most precise method, but also the slowest.

**Experimental feature:** One may also model a transverse gradient undulator (TGU) by setting the TGU\_GRADIENT parameter to a non-zero value. In this case, taking  $a$  as the normalized gradient, the fields are [54]

$$B_x = \frac{aB_0 \sinh k_u y \cos k_u z}{k_u}, \quad (66)$$

$$B_y = B_0 \left( (1 + ax) \cosh k_u y \cos k_u z + \frac{aC}{2k_u^2} \frac{eB_0}{\gamma m_e c} \right) \quad (67)$$

and

$$B_z = -B_0(1 + ax) \sinh k_u y \sin k_u z, \quad (68)$$

where  $\gamma$  is the central relativistic factor for the beam and  $C$  is given by the TGU\_COMP\_FACTOR parameter. This factor, and the term it multiplies, is present in order to help suppress the trajectory error at the end of the device. It may require adjustment in order to achieve the desired level of correction. In addition, the user may need to adjust the pole-strength factors and include external misalignments and steering magnets in order to suppress not only the trajectory error, but also dispersion errors.

- The field expanded to leading order in  $y$ :

$$B_y = B_0 \left( 1 + \frac{1}{2}(k_u y)^2 \right) \cos k_u z, \quad (69)$$

and

$$B_z = -B_0 k_u y \sin k_u z. \quad (70)$$

In most cases, this gives results that are very close to the exact fields, at a savings of 10% in computation time. This is the default mode.

- The “ideal” field:

$$B_y = B_0 \cos k_u z, \quad (71)$$

$$B_z = -B_0 k_u y \sin k_u z. \quad (72)$$

This is about 10% faster than the leading-order mode, but less precise. Also, *it does not include vertical focusing*, so it is not generally recommended.

If HELICAL is set to a nonzero value, a helical device is modeled by combining the fields of two planar devices, one of which is rotated 90 degrees and displaced one quarter wavelength. Again, the FIELD\_EXPANSION parameter is used to control which method is used.



- The exact fields are

$$B_x = -B_0 \cosh k_u x \sin k_u z, \quad (73)$$

$$B_y = B_0 \cosh k_u y \cos k_u z, \quad (74)$$

and

$$B_z = -B_0 \sinh k_u y \sin k_u z - B_0 \sinh k_u x \cos k_u z, \quad (75)$$

- The field expanded to leading order in  $x$  and  $y$ :

$$B_x = -B_0(1 + \frac{1}{2}(k_u x)^2) \sin k_u z, \quad (76)$$

$$B_y = B_0(1 + \frac{1}{2}(k_u y)^2) \cos k_u z, \quad (77)$$

and

$$B_z = -B_0 k_u y \sin k_u z - B_0 k_u x \cos k_u z. \quad (78)$$

- The “ideal” field is

$$B_x = -B_0 \sin k_u z, \quad (79)$$

$$B_y = B_0 \cos k_u z, \quad (80)$$

$$B_z = 0 \quad (81)$$

This is about 10% faster than the leading-order mode, but less precise. Also, *it does not include vertical focusing*, so it is not generally recommended.

The expressions for the laser field used by this element are from A. Chao’s article “Laser Acceleration — Focussed Laser,” available on-line at <http://www.slac.stanford.edu/~achao/LaserAccelerationFocussed.pdf>. The implementation covers laser modes  $\text{TEM}_{ij}$ , where  $0 \leq i \leq 4$  and  $0 \leq j \leq 4$ .

By default, if the laser wavelength is not given, it is computed from the resonance condition:

$$\lambda_l = \frac{\lambda_u}{2\gamma^2} \left( 1 + \frac{1}{2}K^2 \right), \quad (82)$$

where  $\gamma$  is the relativistic factor for the beam and  $K$  is the undulator parameter.

The adaptive integrator doesn’t work well for this element, probably due to sudden changes in field derivatives in the first and last three poles (a result of the implementation of the undulator terminations). Hence, the default integrator is non-adaptive Runge-Kutta. The integration accuracy is controlled via the `N_STEPS` parameter. `N_STEPS` should be about 100 times the number of undulator periods.

The three pole factors are defined so that the trajectory is centered about  $x = 0$  and  $x' = 0$  with zero dispersion. This wouldn’t be true with the standard two-pole termination, which might cause problems overlapping the laser with the electron beam.

The laser time profile can be specified using the `TIME_PROFILE` parameter to specify the name of an SDDS file containing the profile. If given, the electric and magnetic fields of the laser are multiplied by the profile  $P(t)$ . Hence, the laser intensity is multiplied by  $P^2(t)$ . By default  $t = 0$  in

the profile is lined up with  $\langle t \rangle$  in the electron bunch. This can be changed with the `TIME_OFFSET` parameter. A positive value of `TIME_OFFSET` moves the laser profile forward in time (toward the head of the bunch).

**Explanation of `<filename>=<x>+<y>` format:** Several elements in `elegant` make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ `<filename>=<x>+<y>` format for the parameter value. For example, if the parameter value is `waveform.sdds=t+A`, then it means that columns `t` and `A` will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## LTHINLENS

### 10.53 LTHINLENS—A thin lens for light optics

A thin lens for light optics

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| FX             | $M$   | double | 0.0     | focal length in horizontal plane   |
| FY             | $M$   | double | 0.0     | focal length in vertical plane   |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| DZ             | $M$   | double | 0.0     | misalignment   |
| TILT           | $RAD$ | double | 0.0     | misalignment rotation about longitudinal axis  |
| YAW            | $RAD$ | double | 0.0     | misalignment rotation about vertical axis  |
| PITCH          | $RAD$ | double | 0.0     | misalignment rotation about transverse horizontal axis   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## MAGNIFY

### 10.54 MAGNIFY—An element that allows multiplication of phase-space coordinates of all particles by constants.

An element that allows multiplication of phase-space coordinates of all particles by constants.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| MX             |       | double | 1       | factor for x coordinates   |
| MXP            |       | double | 1       | factor for x' coordinates  |
| MY             |       | double | 1       | factor for y coordinates   |
| MYP            |       | double | 1       | factor for y' coordinates  |
| MS             |       | double | 1       | factor for s coordinates   |
| MDP            |       | double | 1       | factor for (p-pCentral)/pCentral   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## MALIGN

### 10.55 MALIGN—A misalignment of the beam, implemented as a zero-order matrix.

A misalignment of the beam, implemented as a zero-order matrix.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| DXP                 |       | double | 0.0     | delta x'   |
| DYP                 |       | double | 0.0     | delta y'   |
| DX                  | $M$   | double | 0.0     | delta x  |
| DY                  | $M$   | double | 0.0     | delta y  |
| DZ                  | $M$   | double | 0.0     | delta z  |
| DT                  | $S$   | double | 0.0     | delta t  |
| DP                  |       | double | 0.0     | delta p/pCentral   |
| DE                  |       | double | 0.0     | delta gamma/gammaCentral   |
| ON_PASS             |       | long   | -1      | pass on which to apply   |
| FORCE_MODIFY_MATRIX |       | long   | 0       | modify the matrix even if on_pass>=0   |
| START_PID           |       | long   | -1      | starting particleID for particles to affect. By default, all particles are affected.   |
| END_PID             |       | long   | -1      | ending particleID for particles to affect. By default, all particles are affected.   |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The default value of the **PASS** parameter (-1) means that the misalignment is imposed on the beam *every* pass. This is appropriate for static misalignments. When using the **MALIGN** element to kick the beam for beam dynamics studies in rings, **PASS**>=0 is required. If **PASS**=0, closed orbit computation and correction will include the effect of the kick; however, matrix-based computations by default will not (set **FORCE\_MODIFY\_MATRIX**=1 to change this). If **PASS**>0, then closed orbit computation and correction do not include the kick, which is probably what is desired in beam dynamics studies in rings.

## MAPSOLENOID

### 10.56 MAPSOLENOID—A numerically-integrated solenoid specified as a map of (Bz, Br) vs (z, r).

A numerically-integrated solenoid specified as a map of (Bz, Br) vs (z, r).

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default     | Description  |
|----------------|------------|--------|-------------|--|
| L              | <i>M</i>   | double | 0.0         | length   |
| DX             | <i>M</i>   | double | 0.0         | misalignment   |
| DY             | <i>M</i>   | double | 0.0         | misalignment   |
| ETILT          | <i>RAD</i> | double | 0.0         | misalignment   |
| EYAW           | <i>RAD</i> | double | 0.0         | misalignment   |
| EPITCH         | <i>RAD</i> | double | 0.0         | misalignment   |
| N_STEPS        |            | long   | 100         | number of steps (for nonadaptive integration)  |
| INPUTFILE      |            | STRING | NULL        | SDDS file containing (Br, Bz) vs (r, z). Each page should have values for a fixed r.   |
| RCOLUMN        |            | STRING | NULL        | column containing r values   |
| ZCOLUMN        |            | STRING | NULL        | column containing z values   |
| BRCOLUMN       |            | STRING | NULL        | column containing Br values  |
| BZCOLUMN       |            | STRING | NULL        | column containing Bz values  |
| FACTOR         |            | double | 0.0001      | factor by which to multiply fields in file   |
| BXUNIFORM      |            | double | 0.0         | uniform horizontal field to superimpose on solenoid field  |
| BYUNIFORM      |            | double | 0.0         | uniform vertical field to superimpose on solenoid field  |
| LUNIFORM       |            | double | 0.0         | length of uniform field superimposed on solenoid field   |
| ACCURACY       |            | double | 0.0001      | integration accuracy   |
| METHOD         |            | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, nonadaptive runge-kutta, modified midpoint)   |
| GROUP          |            | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## MARK

### 10.57 MARK—A marker, equivalent to a zero-length drift space.

A marker, equivalent to a zero-length drift space.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| DX             | $M$   | double | 0.0     | non-functional misalignment (e.g., for girder)   |
| DY             | $M$   | double | 0.0     | non-functional misalignment (e.g., for girder)   |
| FITPOINT       |       | short  | 0       | Supply local values of Twiss parameters, moments, floor coordinates, matrices, etc. for optimization?  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

If **FITPOINT=0**, this element results only in generation of additional output rows in the various files that contain output vs  $s$ . For example, Twiss parameters, closed orbits, and matrices vs  $s$  will all contain a row for each occurrence of each marker element.

If **FITPOINT=1**, the element has additional functionality in the context of optimizations. In particular, for occurrence  $N$  of the defined element *Element*, a series of symbols are created of the form *Element#N.quantity*, where *quantity* has the following values:

- The quantity **pCentral** will be available, giving the reference value of  $\beta\gamma$  at the marker location.
- The quantities **Cx**, **Cxp**, **Cy**, **Cyp**, **Cs**, and **Cdelta** will be available, giving coordinate centroid values from tracking to the marker location.
- The quantities **Sx**, **Sxp**, **Sy**, **Syp**, **Ss**, and **Sdelta** will be available, giving coordinate rms values  $\sqrt{\langle (x_i - \langle x_i \rangle)^2 \rangle}$  at the marker location from tracking.
- The quantity **Particles** will be available, giving the number of particles tracked to the marker location.
- The quantities **sij** will be available, giving  $\langle (x_i - \langle x_i \rangle)(x_j - \langle x_j \rangle) \rangle$  from tracking at the marker location, where  $1 \leq i \leq 6$  and  $i < j \leq 6$ .
- The quantities **betaxBeam**, **alphaxBeam**, **betayBeam**, and **alphayBeam**, which are the twiss parameters computed from the beam moments obtained by tracking, will be available.

- The quantities **R<sub>ij</sub>** will be available, for  $1 \leq i \leq 6$  and  $1 \leq j \leq 6$ , giving the accumulated first-order transport matrix to the marker location.
- If the default matrix order (as set in **run\_setup**) is 2 or greater, the quantities **T<sub>ijk</sub>** will be available, for  $1 \leq i \leq 6$ ,  $1 \leq j \leq 6$ , and  $1 \leq k \leq j$ , giving the accumulated second-order transport matrix to the marker location.
- If Twiss parameter calculations are being performed (via **twiss\_output** with **output\_at\_each\_step=1**), then the quantities **alphax**, **betax**, **nux**, **psix**, **etax**, **etapx**, and **etaxp**, along with similarly-named quantities for the vertical plane, will be available, giving twiss parameter values at the marker location. Note that **etapx** and **etaxp** are the same, being alternate names for  $\eta'_x$ . If radiation integrals are requested, the values of the radiation integrals are available in the quantities **I1**, **I2**, etc.
- If coupled Twiss parameter calculations are being performed (via **coupled\_twiss\_output** with **output\_at\_each\_step=1**), then the quantities **betax1**, **betax2**, **betay1**, **betay2**, **cetax**, **cetay**, and **tilt** will be available. (These are the two beta functions for x and y, the coupled dispersion values for x and y, and the beam tilt).
- If moments calculations are being performed (via **moments\_output** with **output\_at\_each\_step=1**), then the quantities **s<sub>ijm</sub>**,  $1 \leq i \leq j \leq 6$ , giving the 21 unique elements of the sigma matrix. The quantities **c<sub>im</sub>**,  $1 \leq i \leq 6$ , are also created, giving the 6 centroids from the moments computation. In addition, the emittances of the three modes are available using **e<sub>im</sub>**,  $1 \leq i \leq 3$ . The **m** on the end of the symbols is to distinguish them from the moments computed from tracking.
- If floor coordinate calculations are begin performed (via **floor\_coordinates**), then the quantities **X**, **Y**, **Z**, **theta**, **phi**, **psi**, and **s** will be available. These are, respectively, the three position coordinates, the three angle coordinates, and the total arc length at the marker location.

The misalignment controls for this element are non-functional, in the sense that they do not affect the beam. However, when combined with external scripts and the **GROUP** parameter, one can use this feature to implement girder misalignments using pairs of markers to indicate the ends of the girders. A future version of **elegant** will implement this internally.



## MATR

### 10.58 MATR—Explicit matrix input from a text file, in the format written by the `print_matrix` command.

Explicit matrix input from a text file, in the format written by the `print_matrix` command.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| FRACTION       | <i>NULL</i> | double | 1       | The provided matrix <i>M</i> is interpolated with the identity matrix <i>I</i> according to $f*M+(1-f)*I$ .  |
| FILENAME       |             | STRING |         | input file   |
| ORDER          |             | short  | 1       | matrix order   |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The input file for this element uses a simple text format. It is nearly identical to the output in the `printout` file generated by the `matrix_output` and `analyze_map` commands. For example, for a 1st-order matrix, the file would have the following appearance:

```
C: C1 C2 C3 C4 C5 C6
R1: R11 R12 R13 R14 R15 R16
R2: R21 R22 R23 R24 R25 R26
R3: R31 R32 R33 R34 R35 R36
R4: R41 R42 R43 R44 R45 R46
R5: R51 R52 R53 R54 R55 R56
R6: R61 R62 R63 R64 R65 R66
```

Items in normal type must be entered exactly as shown, whereas those in italics must be provided by the user. The colons are important! For this particular example, one would set `ORDER=1` in the `MATR` definition. Typically, the *C<sub>i</sub>* are zero, except for *C<sub>5</sub>*, which is usually equal to the length of the element (which must be specified with the `L` parameter in the `MATR` definition).

As of release 2019.2, the required format changed slightly. In the new version, the start of the matrix is determined by reading through the file until a line starting with `C:` is found. In the past, instead of starting with `C:`, the first line of the matrix could start with any string terminated by a colon, but that line had to be the first line in the file, which conflicted with the format emitted by `analyze_map`.

The `FRACTION` parameter can be used to interpolate the matrix elements between the matrix

$M_0$  read from `FILENAME` and the identity matrix  $I$ , according to

$$M = fM_0 + (1 - f)I. \tag{83}$$

This can be used, for example, to gradually ramp in the effect as part of an optimization. N.B.: in general, the matrix does not have unit determinant unless  $f = 0$  or  $f = 1$ , so this feature should be used only as a knob to assist finding a solution with  $f = 1$ . Exceptions are when  $M_0$  is a drift space or thin-lens quadrupole matrix, in which cases the determinant of  $M$  is always 1.

## MATTER

### 10.59 MATTER—A Coulomb-scattering and energy-absorbing element simulating material in the beam path.

A Coulomb-scattering and energy-absorbing element simulating material in the beam path.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name         | Units    | Type   | Default | Description   |
|------------------------|----------|--------|---------|---|
| L                      | $M$      | double | 0.0     | length  |
| LEFFECTIVE             | $M$      | double | 0.0     | effective length (used if L=0)  |
| XO                     | $M$      | double | 0.0     | radiation length  |
| ENERGY_DECAY           |          | long   | 0       | If nonzero, then particles will lose energy due to material using a simple exponential model.         |
| ENERGY_STRAGGLE        |          | long   | 0       | Use simple-minded energy straggling model coupled with ENERGY_DECAY=1?                                |
| NUCLEAR_BREMSSTRAHLUNG |          | long   | 0       | Model energy loss to nuclear bremsstrahlung? If enabled, set ENERGY_DECAY=0 to disable simpler model. |
| ELECTRON_RECOIL        |          | long   | 0       | If non-zero, electron recoil during Coulomb scattering is included (results in energy change).        |
| Z                      |          | long   | 0       | Atomic number   |
| A                      | $AMU$    | double | 0.0     | Atomic mass   |
| RHO                    | $KG/M^3$ | double | 0.0     | Density   |
| PLIMIT                 |          | double | 0.05    | Probability cutoff for each slice   |
| WIDTH                  | $M$      | double | 0.0     | Full width of slots. If 0, no slots are present.  |
| SPACING                | $M$      | double | 0.0     | Center-to-center spacing of slots. If 0, no slots are present.  |
| TILT                   | $RAD$    | double | 0.0     | Tilt of slot array about the longitudinal axis.   |
| CENTER                 | $M$      | double | 0.0     | Position of center of slot array in rotated frame.  |
| N_SLOTS                |          | long   | 0       | Number of empty slots in material. If $\leq 0$ , an infinite array is assumed.                        |

## MATTER continued

A Coulomb-scattering and energy-absorbing element simulating material in the beam path.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| START_PASS     |       | long   | -1      | If non-negative, pass on which to start interaction with beam.   |
| END_PASS       |       | long   | -1      | If non-negative, pass on which to end interaction with beam.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is based on section 3.3.1 of the *Handbook of Accelerator Physics and Engineering*, specifically, the subsections **Single Coulomb scattering of spin- $\frac{1}{2}$  particles**, **Multiple Coulomb scattering through small angles**, and **Radiation length**. There are two aspects to this element: scattering and energy loss.

**Scattering.** The multiple Coulomb scattering formula is used whenever the thickness of the material is greater than  $0.001X_o$ , where  $X_o$  is the radiation length. (Note that this is inaccurate for materials thicker than  $100X_o$ .) For this regime, the user need only specify the material thickness (L) and the radiation length (XO).

For materials thinner than  $0.001X_o$ , the user must specify additional parameters, namely, the atomic number (Z), atomic mass (A), and mass density (RHO) of the material. Note that the density is given in units of  $kg/m^3$ . (Multiply by  $10^3$  to convert  $g/cm^3$  to  $kg/m^3$ .) In addition, the simulation parameter PLIMIT may be modified.

To understand this parameter, one must understand how **elegant** simulates the thin materials. First, it computes the expected number of scattering events per particle,  $E = \sigma T n L = \frac{K_1 \pi^3 n L}{K_2^2 + K_2 \pi^2}$ , where  $n$  is the number density of the material,  $L$  is the thickness of the material,  $K_1 = (\frac{2Zr_e}{\beta^2 \gamma})^2$ , and  $K_2 = \frac{\alpha^2 Z^{\frac{2}{3}}}{(\beta \gamma)^2}$ , with  $r_e$  the classical electron radius and  $\alpha$  the fine structure constant. The material is then broken into  $N$  slices, where  $N = E/P_{limit}$ . For each slice, each simulation particle has a probability  $E/N$  of scattering. If scattering occurs, the location within the slice is computed using a uniform distribution over the slice thickness.

For each scatter that occurs, the scattering angle,  $\theta$  is computed using the cumulative probability distribution  $F(\theta > \theta_o) = \frac{K_2(\pi^2 - \theta_o^2)}{\pi^2(K_2 + \theta_o^2)}$ . This can be solved for  $\theta_o$ , giving  $\theta_o = \sqrt{\frac{(1-F)K_2\pi^2}{K_2 + F\pi^2}}$ . For each scatter,  $F$  is chosen from a uniform random distribution on  $[0, 1]$ .

**Energy loss.** There are two ways to compute energy loss in materials, using a simple minded approach and using the bremsstrahlung cross section. The latter is recommended, but the former is kept for backward compatibility.

- To enable bremsstrahlung simulation, simply set **NUCLEAR\_BREMSSTRAHLUNG=1**. Note that the energy loss is not correlated with the scattering angle, which is not entirely physical but should be reasonable for large numbers of scattering events.
- To use the simplified approach:

- Set ENERGY\_DECAY=1. Energy loss simulation is very simple. The energy loss per unit distance traveled,  $x$ , is  $\frac{dE}{dx} = -E/X_o$ . Hence, in traveling through a material of thickness  $L$ , the energy of each particle is transformed from  $E$  to  $Ee^{-L/X_o}$ .
- Optionally, set ENERGY\_STRAGGLE=1. **Not recommended. Exists only for backward compatibility.** This adds variation in the energy lost by particles. The model is *very, very* crude and **not recommended**. It assumes that the standard deviation of the energy loss is equal to half the mean energy loss. This is an overestimate, we think, and is provided to give an upper bound on the effects of energy straggling until a real model can be developed. Note one obvious problem with this: if you split a MATTER element of length  $L$  into two pieces of length  $L/2$ , the total energy loss will not change, but the induced energy spread will be about 30% lower, due to addition in quadrature.

**Slotted absorber.** If the WIDTH and SPACING parameters are set to non-zero values, then a slotted absorber is simulated. The number of slots is by default infinite, but can be limited by setting N\_SLOTS to a positive value; in this case, the slot array is centered about the transverse coordinate given by the CENTER parameter.

Note that the simulation contains a simplification in that particles cannot leave or enter the material through the side of the slot. I.e., if a particle is inside (outside) the material when it hits the front face of the object, it is assumed to remain inside (outside) until it has passed the object. For long objects, breaking the simulation up into multiple MATTER elements is suggested if a slotted arrangement is being simulated.

**One-sided scrapers.** One sided scrapers may be modeled using the SCRAPER element. It uses the same material-modeling algorithm as described here.

## MAXAMP

### 10.60 MAXAMP—A collimating element that sets the maximum transmitted particle amplitudes for all following elements, until the next MAXAMP.

A collimating element that sets the maximum transmitted particle amplitudes for all following elements, until the next MAXAMP.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| X_MAX          | $M$   | double | 0.0     | x half-aperture  |
| Y_MAX          | $M$   | double | 0.0     | y half-aperture  |
| ELLIPTICAL     |       | long   | 0       | is aperture elliptical?  |
| EXPONENT       |       | long   | 2       | exponent for boundary equation in elliptical mode. 2 is a true ellipse.  |
| YEXPONENT      |       | long   | 0       | y exponent for boundary equation in elliptical mode. If zero, defaults to EXPONENT.  |
| OPEN_SIDE      |       | STRING | NULL    | which side, if any, is open (+x, -x, +y, -y)   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element sets the aperture for itself and all subsequent elements. The settings are in force until another MAXAMP element is seen. Settings are also enforced inside of KQUAD, KSEXT, KOCT, KQUSE, CSBEND, and CSRCSBEND elements.

This can introduce unexpected behavior when beamlines are reflected. For example, consider the beamline

```

...
L1:  LINE=( ... )
L2:  LINE=( ... )
MA1: MAXAMP,X_MAX=0.01,Y_MAX=0.005
MA2: MAXAMP,X_MAX=0.01,Y_MAX=0.002
BL1: LINE=(MA1,L1,MA2,L2)
BL:  LINE=(BL1,-BL1)

```

This is equivalent to

```
BL:  LINE=(MA1,L1,MA2,L2,-L2,MA2,-L1,MA1)
```

Note that the aperture **MA1** is the aperture for all of the first instance of beamline **L1**, but that **MA2** is the aperture for the second instance, **-L1**. This is probably not what was intended. To prevent this, it is recommended to always use **MAXAMP** elements in pairs:

```
BL1: LINE=(MA2,MA1,L1,MA1,MA2,L2)
```

```
BL:  LINE=(BL1,-BL1)
```

which is equivalent to

```
BL:  LINE=(MA2,MA1,L1,MA1,MA2,L2,-L2,MA2,MA1,-L1,MA1,MA2)
```

Now, both instances of **L1** have the aperture defined by **MA1** and both instances of **L2** have the aperture defined by **MA2**.

## MBUMPER

### 10.61 MBUMPER—A time-dependent multipole kicker magnet. The waveform is in SDDS format, with time in seconds and amplitude normalized to 1.

A time-dependent multipole kicker magnet. The waveform is in SDDS format, with time in seconds and amplitude normalized to 1.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units      | Type   | Default | Description  |
|-----------------|------------|--------|---------|--|
| L               | <i>M</i>   | double | 0.0     | length   |
| STRENGTH        |            | double | 0.0     | geometric strength in 1/m <sup>order</sup>   |
| TILT            | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| DX              | <i>M</i>   | double | 0.0     | misalignment   |
| DY              | <i>M</i>   | double | 0.0     | misalignment   |
| DZ              | <i>M</i>   | double | 0.0     | misalignment   |
| TIME_OFFSET     | <i>S</i>   | double | 0.0     | time offset of waveform  |
| ORDER           |            | long   | 0       | multipole order, where 1 is quadrupole, 2 is sextupole, etc.   |
| PERIODIC        |            | long   | 0       | is waveform periodic?  |
| PHASE_REFERENCE |            | long   | 0       | phase reference number (to link with other time-dependent elements)  |
| FIRE_ON_PASS    |            | long   | 0       | pass number to fire on   |
| N_KICKS         |            | long   | 0       | Number of kicks to use for simulation.   |
| WAVEFORM        |            | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving kick factor vs time   |
| GROUP           |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a time-dependent multipole kicker magnet. To use this element, you must supply an SDDS file giving the time-dependent waveform. The element is called **MBUMPER** because **HKICK**, **VKICK**, **KICKER** are used for steering magnets.

The arrival time of the beam is taken to define the reference time,  $t = 0$ . Hence, if the waveform file has the maximum amplitude at  $t = 0$ , the beam will get kicked at the peak of the waveform.



If the waveform peaks at  $t = t_{peak}$ , then setting `TIME_OFFSET` equal to  $-t_{peak}$  will ensure that the beam is kicked at the peak amplitude.

By default, the kicker fires on the first beam passage. However, if `FIRE_ON_PASS` is used, then the kicker is treated like a drift space until the specified pass.

If `PHASE_REFERENCE` is non-zero, then the initial timing is taken from the first time-dependent element that has the same `PHASE_REFERENCE` value. This would allow, for example, simulating several kickers firing at the same time. Delays relative to this reference time can then be given with positive adjustments to `TIME_OFFSET`.

The input file need not have equispaced points in time. However, the time values should increase monotonically.

This element simulates a quadrupole or higher order kicker only. For dipole kickers, see the `BUMPER` element.

**Explanation of `<filename>=<x>+<y>` format:** Several elements in `elegant` make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ `<filename>=<x>+<y>` format for the parameter value. For example, if the parameter value is `waveform.sdds=t+A`, then it means that columns `t` and `A` will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## MHISTOGRAM

### **10.62 MHISTOGRAM—Request for multiple dimensions (1, 2, 4 or 6) histogram output of particle coordinates.**

Request for multiple dimensions (1, 2, 4 or 6) histogram output of particle coordinates.

Parallel capable? : no

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| FILE1D         |       | STRING | NULL    | filename for 1d histogram output, possibly incomplete (see below)  |
| FILE2DH        |       | STRING | NULL    | filename for 2d x-x' histogram output, possibly incomplete (see below)   |
| FILE2DV        |       | STRING | NULL    | filename for 2d y-y' histogram output, possibly incomplete (see below)   |
| FILE2DL        |       | STRING | NULL    | filename for 2d dt-deltaP histogram output, possibly incomplete (see below)  |
| FILE4D         |       | STRING | NULL    | filename for 4d x-x'-y-y' histogram output, possibly incomplete (see below)  |
| FILE6D         |       | STRING | NULL    | filename for 6d x-x'-y-y'-dt-deltaP histogram output, possibly incomplete (see below)  |
| INPUT_BINS     |       | STRING | NULL    | Name of SDDS file contains input bin number.   |
| INTERVAL       |       | long   | 1       | interval in passes between output.   |
| START_PASS     |       | long   | 0       | starting pass for output   |
| NORMALIZE      |       | short  | 1       | normalize histogram with number of particles?  |
| DISABLE        |       | short  | 0       | If nonzero, no output will be generated.   |
| LUMPED         |       | short  | 0       | If nonzero, then results at elements with same name will be output to a single multipage SDDS file.  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is used to generate multiple dimension (1, 2, 4, or 6) histogram output of particle coordinates.

The calculation is set up through output filename: `FILE1D`, `FILE2DH`, `FILE2DV`, `FILE2DL`, `FILE4D`, `FILE6D`. They may be an incomplete filename (see `HISTOGRAM` for detail). If `LUMPED` set to non zero, then results are directed to a multi page SDDS file with each page contains data of same elements `MHISTOGRAM` but at difference occurrence instead of multiple SDDS files. In this case the “%ld” in filename is ignored.

The bin number used to do histogram analysis is given through a SDDS file from `INPUT_BINS`. It contains 4 columns: `Bins_1D`, `Bins_2D`, `Bins_4D`, `Bins_6D`; and 6 rows (`x`, `x'`, `y`, `y'`, `dt`, `delta`). A non-zero value in `Bins_1D` is a switch for doing histogram analysis in corresponding dimension, and the maximum value in `Bins_1D` is used as bin number to do the analysis.

The normalization is different from `HISTOGRAM` as we always treat `bin-size = 1`.

The output file uses the general format designed for a n-dimensional histogram data. It must contains a column named “Frequency” (Type: “double”), and following parameters:

- `ND` — Type: long; Value: “n”.
- `Variable??Name` — Type: “string”. “??” counts from “0” to “ND-1” in double digits format, same for all following parameters.
- `Variable??Min` — Type: “double”. Minimum value of “??” variable.
- `Variable??Max` — Type: “double”. Maximum value of “??” variable.
- `Variable??Interval` — Type: “double”. Bin size of “??” variable.
- `Variable??Dimension` — Type: “long”. Total number of bins of “??” variable. `Variable??Dimension = (Variable??Max - Variable??Min)/Variable??Interval+1`.

The data is arranged as it has a “ND” index counter  $[i_{ND-1}|\dots|i_1]$ , where  $i_{ND-1}$  takes value from “0” to “Variable[%02d ND-1]Dimension”.

## MODRF

### 10.63 MODRF—A first-order matrix RF cavity with exact phase dependence, plus optional amplitude and phase modulation.

A first-order matrix RF cavity with exact phase dependence, plus optional amplitude and phase modulation.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default   | Description  |
|-----------------|-------|--------|-----------|--|
| L               | $M$   | double | 0.0       | length   |
| VOLT            | $V$   | double | 0.0       | nominal voltage  |
| PHASE           | $DEG$ | double | 0.0       | nominal phase  |
| FREQ            | $Hz$  | double | 500000000 | nominal frequency  |
| Q               |       | double | 0.0       | cavity Q   |
| PHASE_REFERENCE |       | long   | 0         | phase reference number (to link with other time-dependent elements)  |
| AMMAG           |       | double | 0.0       | magnitude of amplitude modulation (fraction value)   |
| AMPHASE         | $DEG$ | double | 0.0       | phase of amplitude modulation  |
| AMFREQ          | $Hz$  | double | 0.0       | frequency of amplitude modulation  |
| AMDECAY         | $1/s$ | double | 0.0       | exponential decay rate of amplitude modulation   |
| PMMAG           | $DEG$ | double | 0.0       | magnitude of phase modulation  |
| PMPHASE         | $DEG$ | double | 0.0       | phase of phase modulation  |
| PMFREQ          | $Hz$  | double | 0.0       | frequency of phase modulation  |
| PMDECAY         | $1/s$ | double | 0.0       | exponential decay rate of phase modulation   |
| FIDUCIAL        |       | STRING | NULL      | mode for determining fiducial arrival time (light, tmean, first, pmaximum)   |
| GROUP           |       | string | NULL      | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is very similar to the RFCA element, except that the amplitude and phase of the cavity can be modulated.

The phase convention is as follows, assuming a positive rf voltage: PHASE=90 is the crest for

acceleration. **PHASE=180** is the stable phase for a storage ring above transition without energy losses.

The element works by first computing the fiducial arrival time  $\bar{t}$ . Using this, the effective voltage is computed using the amplitude modulation parameters, according to

$$V_e = V_0(1 + A_{am} \sin(\omega_{am}\bar{t} + \phi_{am}) \exp(-\alpha_{am}\bar{t})) \quad (84)$$

where  $V_0$  is the nominal cavity voltage **VOLT**,  $A_{am}$  is **AMMAG**,  $\omega_{am}$  is the angular frequency corresponding to **AMFREQ**,  $\phi_{am}$  is the amplitude modulation phase corresponding to **AMPHASE** (converted from degrees to radians), and  $\alpha_{am}$  is **AMDECAY**.

The phase of the phase modulation is computed using

$$\phi_{pm} = \omega_{pm}\bar{t} + \Delta\phi_{pm}, \quad (85)$$

where  $\omega_{pm}$  is the angular frequency corresponding to **PMFREQ** and  $\Delta\phi_{pm}$  is the phase offset corresponding to **PMPHASE** (converted from degrees to radians). The rf phase for the centroid is then computed using

$$\phi = \omega_0\bar{t} + \phi_0 + \Phi_m \sin(\phi_{pm}) \exp(-\alpha_{pm}\bar{t}), \quad (86)$$

where  $\omega_0$  is the nominal rf angular frequency (corresponding to **FREQ**),  $\phi_0$  corresponds to **PHASE** (converted to radians),  $\Phi_m$  corresponds to **PMMAG** (converted to radians), and  $\alpha_{pm}$  corresponds to **PMDECAY**.

The effective instantaneous rf angular frequency is

$$\omega = \omega_0 + \omega_{pm}\Phi_m \cos \phi_{pm}. \quad (87)$$

Using all of the above, the voltage seen by a particle arriving at time  $t$  is then

$$V = V_e \sin(\omega(t - \bar{t}) + \phi). \quad (88)$$

## MONI

### 10.64 MONI—A two-plane position monitor, accepting two rpn equations for the readouts as a function of the actual positions (x and y).

A two-plane position monitor, accepting two rpn equations for the readouts as a function of the actual positions (x and y).

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units    | Type   | Default | Description  |
|----------------|----------|--------|---------|--|
| L              | <i>M</i> | double | 0.0     | length   |
| DX             | <i>M</i> | double | 0.0     | misalignment   |
| DY             | <i>M</i> | double | 0.0     | misalignment   |
| WEIGHT         |          | double | 1       | weight in correction   |
| TILT           |          | double | 0.0     | rotation about longitudinal axis   |
| XCALIBRATION   |          | double | 1       | calibration factor for x readout   |
| YCALIBRATION   |          | double | 1       | calibration factor for y readout   |
| XSETPOINT      | <i>M</i> | double | 0.0     | x steering setpoint  |
| YSETPOINT      | <i>M</i> | double | 0.0     | y steering setpoint  |
| ORDER          |          | short  | 0       | matrix order   |
| XREADOUT       |          | STRING | NULL    | rpn expression for x readout (actual position supplied in variables x, y)  |
| YREADOUT       |          | STRING | NULL    | rpn expression for y readout (actual position supplied in variables x, y)  |
| CO.FITPOINT    |          | short  | 0       | If nonzero, then closed orbit values are placed in variables <name>#<occurrence>.xco and <name>#<occurrence>.yco   |
| GROUP          |          | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## MRFDF

### 10.65 MRFDF—Zero-length Multipole RF DeFlector from dipole to decapole

Zero-length Multipole RF DeFlector from dipole to decapole

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units      | Type   | Default    | Description  |
|-----------------|------------|--------|------------|--|
| FACTOR          |            | double | 1          | A factor by which to multiply all components.  |
| TILT            | <i>RAD</i> | double | 0.0        | rotation about longitudinal axis   |
| A1              | $V/m$      | double | 0.0        | Vertically-deflecting dipole   |
| A2              | $V/m^2$    | double | 0.0        | Skew quadrupole  |
| A3              | $V/m^3$    | double | 0.0        | Skew sextupole   |
| A4              | $V/m^4$    | double | 0.0        | Skew octupole  |
| A5              | $V/m^5$    | double | 0.0        | Skew decapole  |
| B1              | $V/m$      | double | 0.0        | Horizontally-deflecting dipole   |
| B2              | $V/m^2$    | double | 0.0        | Normal quadrupole  |
| B3              | $V/m^3$    | double | 0.0        | Normal sextupole   |
| B4              | $V/m^4$    | double | 0.0        | Normal octupole  |
| B5              | $V/m^5$    | double | 0.0        | Normal decapole  |
| FREQUENCY1      | <i>HZ</i>  | double | 2856000000 | Dipole frequency   |
| FREQUENCY2      | <i>HZ</i>  | double | 2856000000 | Quadrupole frequency   |
| FREQUENCY3      | <i>HZ</i>  | double | 2856000000 | Sextupole frequency  |
| FREQUENCY4      | <i>HZ</i>  | double | 2856000000 | Octupole frequency   |
| FREQUENCY5      | <i>HZ</i>  | double | 2856000000 | Decapole frequency   |
| PHASE1          | <i>HZ</i>  | double | 0.0        | Dipole phase   |
| PHASE2          | <i>HZ</i>  | double | 0.0        | Quadrupole phase   |
| PHASE3          | <i>HZ</i>  | double | 0.0        | Sextupole phase  |
| PHASE4          | <i>HZ</i>  | double | 0.0        | Octupole phase   |
| PHASE5          | <i>HZ</i>  | double | 0.0        | Decapole phase   |
| PHASE_REFERENCE |            | long   | 0          | phase reference number (to link with other time-dependent elements)  |
| GROUP           |            | string | NULL       | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates an rf deflector with specified multipole content.



Assuming for simplicity that  $y = 0$ , the momentum change in the horizontal plane is

$$\Delta p_x = \frac{e}{mc^2 k} \sum_{i=1}^5 i b_i x^{i-1} \cos \phi_i, \quad (89)$$

where  $k = \omega/c$  and  $p_x = \beta_x \gamma$ . The deflection is

$$\Delta x' \approx \frac{\Delta p_x}{p_z}, \quad (90)$$

where the approximation results from the fact that  $p_z = \beta_z \gamma$  also changes in order to satisfy Maxwell's equations.

## MULT

### 10.66 MULT—A canonical kick multipole.

A canonical kick multipole.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name     | Units        | Type   | Default | Description  |
|--------------------|--------------|--------|---------|--|
| L                  | $M$          | double | 0.0     | length   |
| KNL                | $M^{-ORDER}$ | double | 0.0     | integrated geometric strength  |
| TILT               | $RAD$        | double | 0.0     | rotation about longitudinal axis   |
| BORE               | $M$          | double | 0.0     | bore radius  |
| BTIPL              | $TM$         | double | 0.0     | integrated field at pole tip, used if BORE nonzero   |
| DX                 | $M$          | double | 0.0     | misalignment   |
| DY                 | $M$          | double | 0.0     | misalignment   |
| DZ                 | $M$          | double | 0.0     | misalignment   |
| FACTOR             |              | double | 1       | factor by which to multiply strength   |
| ORDER              |              | short  | 1       | multipole order  |
| N_KICKS            |              | short  | 4       | number of kicks  |
| SYNCH_RAD          |              | short  | 0       | include classical, single-particle synchrotron radiation?  |
| EXPAND_HAMILTONIAN |              | short  | 0       | If 1, Hamiltonian is expanded to leading order.  |
| GROUP              |              | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a multipole element using 4th-order symplectic integration. A single multipole order,  $n$ , is given. The multipole strength is specified by giving

$$K_n L = \left( \frac{\partial^n B_y}{\partial x^n} \right)_{x=y=0} \frac{L}{B\rho}, \quad (91)$$

where  $B\rho$  is the beam rigidity. A quadrupole is  $n = 1$ , a sextupole is  $n = 2$ , and so on. The relationship between the pole tip field and  $K_n L$  is

$$K_n L = \frac{n! B_{tip} L}{r^n (B\rho)}, \quad (92)$$

where  $r$  is the bore radius.

## NIBEND

### 10.67 NIBEND—A numerically-integrated dipole magnet with various extended-fringe-field models.

A numerically-integrated dipole magnet with various extended-fringe-field models.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| L               | $M$   | double | 0.0         | arc length   |
| ANGLE           | $RAD$ | double | 0.0         | bending angle  |
| E1              | $RAD$ | double | 0.0         | entrance edge angle  |
| E2              | $RAD$ | double | 0.0         | exit edge angle  |
| TILT            |       | double | 0.0         | rotation about incoming longitudinal axis  |
| DX              | $M$   | double | 0.0         | misalignment   |
| DY              | $M$   | double | 0.0         | misalignment   |
| DZ              | $M$   | double | 0.0         | misalignment   |
| FINT            |       | double | 0.5         | edge-field integral  |
| HGAP            | $M$   | double | 0.0         | half-gap between poles   |
| FP1             | $M$   | double | 10          | fringe parameter (tanh model)  |
| FP2             | $M$   | double | 0.0         | not used   |
| FP3             | $M$   | double | 0.0         | not used   |
| FP4             | $M$   | double | 0.0         | not used   |
| FSE             |       | double | 0.0         | fractional strength error  |
| ETILT           | $RAD$ | double | 0.0         | error rotation about incoming longitudinal axis  |
| ACCURACY        |       | double | 0.0001      | integration accuracy (for non-adaptive integration, used as the step-size)   |
| MODEL           |       | STRING | linear      | fringe model (hard-edge, linear, cubic-spline, tanh, quintic, engel, engel3, engel5)   |
| METHOD          |       | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, modified-midpoint, two-pass modified-midpoint, leap-frog, non-adaptive runge-kutta) |
| SYNCH_RAD       |       | long   | 0           | include classical, single-particle synchrotron radiation?  |
| ADJUST_BOUNDARY |       | long   | 1           | adjust fringe boundary position to make symmetric trajectory? (Not done if ADJUST_FIELD is nonzero.)                                 |

## NIBEND continued

A numerically-integrated dipole magnet with various extended-fringe-field models.

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| ADJUST_FIELD      |       | long   | 0       | adjust central field strength to make symmetric trajectory?  |
| FUDGE_PATH_LENGTH |       | long   | 1       | fudge central path length to force it to equal the nominal length L?   |
| FRINGE_POSITION   |       | long   | 0       | 0=fringe centered on reference plane, -1=fringe inside, 1=fringe outside.  |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

For the NIBEND element, there are various fringe field models available. In the following descriptions,  $l_f$  is the extend of the fringe field, which starts at  $z = 0$  for convenience in the expressions. Also,  $K = \frac{1}{g} \int_{-\infty}^{\infty} F_y(z)(1 - F_y(z))dz$  is K. Brown's fringe field integral (commonly called FINT), where  $g$  is the full magnet gap and  $\vec{F} = \vec{B}/B_0$ ,  $B_0$  being the value of the magnetic field well inside the magnet.

- **Linear fringe field:**

$$F_y = zF_a \quad (93)$$

$$F_z = yF_a \quad (94)$$

$$F_a = 1/(6Kg) \quad (95)$$

For this model, the user specifies FINT and HGAP only.

- **Cubic-spline fringe field:**

$$F_y = F_az^2 + F_bz^3 + y^2(-F_a - 3F_bz) \quad (96)$$

$$F_z = (2F_az + 3F_bz^2)y \quad (97)$$

$$F_a = 3/l_f^2 \quad (98)$$

$$F_b = -2/l_f^3 \quad (99)$$

$$l_f = 70Kg/9 \quad (100)$$

For this model, the user specifies FINT and HGAP only.

- **Tanh-like fringe field:**

$$F_y = \frac{1}{2}(1 + \tanh F_a z) + \frac{1}{2}(y F_a \operatorname{sech} F_a z)^2 \tanh F_a z + \quad (101)$$

$$\frac{1}{24}(y F_a \operatorname{sech} F_a z)^4 \operatorname{sech} F_a z (11 \sinh F_a z - \sinh 3 F_a z) \quad (102)$$

$$F_z = \frac{1}{2} y F_a \operatorname{sech}^2 F_a z + \frac{1}{6} (y F_a \operatorname{sech} F_a z)^3 \operatorname{sech} F_a z (2 - \cosh 2 F_a z) + \quad (103)$$

$$\frac{1}{120} (y F_a \operatorname{sech} F_a z)^5 \operatorname{sech} F_a z (33 - 26 \cosh 2 F_a z + \cosh 4 F_a z) \quad (104)$$

$$F_a = 1/(2Kg) \quad (105)$$

$$l_f = P_1/F_a \quad (106)$$

For this model, the user specifies **FINT** and **HGAP**, along with the parameter **FP1**, which is the quantity  $P_1$  in the last equation. It determines the length of the fringe field that is integrated.

- **Quintic-spline fringe field, to third order in y:**

$$F_y = (F_a z^3 + F_b z^4 + F_c z^5) + y^2 z (3F_a + 6F_b z + 10F_c z^2) \quad (107)$$

$$F_z = y(3F_a z^2 + 4F_b z^3 + 5F_c z^4) + y^3(-F_a - 4F_b z - 10F_c z^2) \quad (108)$$

$$F_a = 10/l_f^3 \quad (109)$$

$$F_b = -15/l_f^4 \quad (110)$$

$$F_c = 6/l_f^5 \quad (111)$$

$$l_f = 231Kg/25 \quad (112)$$

For this model, the user specifies **FINT** and **HGAP** only.

- **Enge model with 3 coefficients:**

$$F_0 = \frac{1}{1 + e^{a_1 + a_2 z/D + a_3 (z/D)^2}} \quad (113)$$

$$F_y = F_0 - \frac{1}{2} y^2 F_0^{(2)} + \frac{1}{24} y^4 F_0^{(4)} \quad (114)$$

$$F_z = y F_0^{(1)} - \frac{1}{6} y^3 F_0^{(3)} + \frac{1}{120} y^5 F_0^{(5)} \quad (115)$$

where  $F_0^{(n)} = \frac{\partial^n F_0}{\partial z^n}$ .

The user may choose “engel”, “enge3”, or “enge5”, where the number indicates the order of the expansion of  $F_z$  with respect to  $y$ .

The need only specify **FINT** and **HGAP**. The Enge parameters are then automatically determined to give the correct linear focusing.

However, if user gives non-zero value for **FP2**, then **FINT** and **HGAP** are ignored. **FP2**, **FP3**, and **FP4** and taken as the Enge coefficients  $a_1$ ,  $a_2$ , and  $a_3$ , respectively.

## NISEPT

### 10.68 NISEPT—A numerically-integrated dipole magnet with a Cartesian gradient.

A numerically-integrated dipole magnet with a Cartesian gradient.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default     | Description   |
|----------------|-------|--------|-------------|---|
| L              | $M$   | double | 0.0         | arc length  |
| ANGLE          | $RAD$ | double | 0.0         | bend angle  |
| E1             | $RAD$ | double | 0.0         | entrance edge angle   |
| B1             | $1/M$ | double | 0.0         | normalized gradient<br>( $K1=B1*L/ANGLE$ )  |
| Q1REF          | $M$   | double | 0.0         | distance from septum at which<br>bending radius is $L/ANGLE$  |
| FLEN           | $M$   | double | 0.0         | fringe field length   |
| ACCURACY       |       | double | 0.0001      | integration accuracy  |
| METHOD         |       | STRING | runge-kutta | integration method (runge-<br>kutta, bulirsch-stoer,<br>modified-midpoint, two-pass<br>modified-midpoint, leap-frog,<br>non-adaptive runge-kutta                              |
| MODEL          |       | STRING | linear      | fringe model (hard-edge, lin-<br>ear, cubic-spline, tanh, quintic   |
| GROUP          |       | string | NULL        | Optionally used to assign an<br>element to a group, with a<br>user-defined name. Group<br>names will appear in the pa-<br>rameter output file in the col-<br>umn ElementGroup |

## OCTU

### 10.69 OCTU—An octupole implemented as a third-order matrix. Use KOCT for symplectic tracking.

An octupole implemented as a third-order matrix. Use KOCT for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| K3             | $1/M^3$ | double | 0.0     | geometric strength   |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| DX             | $M$     | double | 0.0     | misalignment   |
| DY             | $M$     | double | 0.0     | misalignment   |
| DZ             | $M$     | double | 0.0     | misalignment   |
| FSE            |         | double | 0.0     | fractional strength error  |
| ORDER          |         | short  | 0       | matrix order   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## PEPPOT

### 10.70 PEPPOT—A pepper-pot plate.

A pepper-pot plate.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| L              | <i>M</i>   | double | 0.0     | length   |
| RADII          | <i>M</i>   | double | 0.0     | hole radius  |
| TRANSMISSION   |            | double | 0.0     | transmission of material   |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| THETA_RMS      | <i>RAD</i> | double | 0.0     | rms scattering from material   |
| N_HOLES        |            | long   | 0       | number of holes  |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |



## PFILTER

### 10.71 PFILTER—An element for energy and momentum filtration.

An element for energy and momentum filtration.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| DELTA LIMIT    |       | double | -1      | maximum fractional momentum deviation  |
| LOWER FRACTION |       | double | 0.0     | fraction of lowest-momentum particles to remove  |
| UPPER FRACTION |       | double | 0.0     | fraction of highest-momentum particles to remove   |
| FIX PLIMITS    |       | long   | 0       | fix the limits in p from LOWER FRACTION and UPPER FRACTION applied to first beam   |
| BEAM CENTERED  |       | long   | 0       | if nonzero, center for DELTA LIMIT is average beam momentum  |
| BINS           |       | long   | 1024    | number of bins   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## QUAD

### 10.72 QUAD—A quadrupole implemented as a matrix, up to 3rd order. Use KQUAD for symplectic tracking.

A quadrupole implemented as a matrix, up to 3rd order. Use KQUAD for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default        | Description  |
|----------------|---------|--------|----------------|--|
| L              | $M$     | double | 0.0            | length   |
| K1             | $1/M^2$ | double | 0.0            | geometric strength   |
| TILT           | $RAD$   | double | 0.0            | rotation about longitudinal axis   |
| DX             | $M$     | double | 0.0            | misalignment   |
| DY             | $M$     | double | 0.0            | misalignment   |
| DZ             | $M$     | double | 0.0            | misalignment   |
| FSE            |         | double | 0.0            | fractional strength error  |
| HKICK          | $RAD$   | double | 0.0            | horizontal correction kick   |
| VKICK          | $RAD$   | double | 0.0            | vertical correction kick   |
| HCALIBRATION   |         | double | 1              | calibration factor for horizontal correction kick                                |
| VCALIBRATION   |         | double | 1              | calibration factor for vertical correction kick                                  |
| HSTEERING      |         | short  | 0              | use for horizontal steering?   |
| VSTEERING      |         | short  | 0              | use for vertical steering?   |
| ORDER          |         | short  | 0              | matrix order   |
| EDGE1_EFFECTS  |         | short  | 1              | include entrance edge effects?   |
| EDGE2_EFFECTS  |         | short  | 1              | include exit edge effects?   |
| FRINGE_TYPE    |         | STRING | fixed-strength | type of fringe: "inset", "fixed-strength", or "integrals"                        |
| FFRINGE        |         | double | 0.0            | For non-integrals mode, fraction of length occupied by linear fringe region.     |
| LEFFECTIVE     | $M$     | double | -1             | Effective length. Ignored if non-positive. Cannot be used with non-zero FFRINGE. |
| I0P            | $M$     | double | 0.0            | i0+ fringe integral  |
| I1P            | $M^2$   | double | 0.0            | i1+ fringe integral  |
| I2P            | $M^3$   | double | 0.0            | i2+ fringe integral  |
| I3P            | $M^4$   | double | 0.0            | i3+ fringe integral  |
| LAMBDA2P       | $M^3$   | double | 0.0            | lambda2+ fringe integral   |
| I0M            | $M$     | double | 0.0            | i0- fringe integral  |

## QUAD continued

A quadrupole implemented as a matrix, up to 3rd order. Use KQUAD for symplectic tracking.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| I1M            | $M^2$ | double | 0.0     | i1- fringe integral  |
| I2M            | $M^3$ | double | 0.0     | i2- fringe integral  |
| I3M            | $M^4$ | double | 0.0     | i3- fringe integral  |
| LAMBDA2M       | $M^3$ | double | 0.0     | lambda2- fringe integral   |
| RADIAL         |       | short  | 0       | If non-zero, converts the quadrupole into a radially-focusing lens   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a quadrupole using a matrix of first, second, or third order.

As of version 29.2, this element incorporates the ability to have different values for the insertion and effective lengths. This is invoked when **LEFFECTIVE** is positive. In this case, the **L** parameter is understood to be the physical insertion length. Using **LEFFECTIVE** is a convenient way to incorporate the fact that the effective length may differ from the physical length and even vary with excitation, without having to modify the drift spaces on either side of the quadrupole element.

By default, the element has hard edges and constant field within the defined length, **L**. However, this element supports two different methods of implementing fringe fields. Which method is used is determined by the **FRINGE\_TYPE** parameter.

**Edge integral method** The most recent and preferred implementation of fringe field effects is based on edge integrals and is invoked by setting **FRINGE\_TYPE** to “integrals”. This method is compatible with the use of **LEFFECTIVE**. However, it provides a first-order matrix only.

The model is based on publications of D. Zhuo *et al.* [34] and J. Irwin *et al.* [35], as well as unpublished work of C. X. Wang (ANL). The fringe field is characterized by 10 integrals given in equations 19, 20, and 21 of [34]. However, the values input into **elegant** should be normalized by  $K_1$  or  $K_1^2$ , as appropriate.

For the exit-side fringe field, let  $s_1$  be the center of the magnet,  $s_0$  be the location of the nominal end of the magnet (for a hard-edge model), and let  $s_2$  be a point well outside the magnet. Using  $K_{1,he}(s)$  to represent the hard edge model and  $K_1(s)$  the actual field profile, we define the normalized difference as  $\tilde{k}(s) = (K_1(s) - K_{1,he}(s))/K_1(s_1)$ . (Thus,  $\tilde{k}(s) = \tilde{K}(s)/K_0$ , using the notation of Zhou *et al.*)

The integrals to be input to **elegant** are defined as

$$i_0^- = \int_{s_1}^{s_0} \tilde{k}(s) ds \quad i_0^+ = \int_{s_0}^{s_2} \tilde{k}(s) ds \quad (116)$$

$$i_1^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0) ds \quad i_1^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0) ds \quad (117)$$

$$i_2^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0)^2 ds \quad i_2^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0)^2 ds \quad (118)$$

$$i_3^- = \int_{s_1}^{s_0} \tilde{k}(s)(s - s_0)^3 ds \quad i_3^+ = \int_{s_0}^{s_2} \tilde{k}(s)(s - s_0)^3 ds \quad (119)$$

$$\lambda_2^- = \int_{s_1}^{s_0} ds \int_s^{s_0} ds' \tilde{k}(s) \tilde{k}(s') (s' - s) \quad \lambda_2^+ = \int_{s_0}^{s_2} ds \int_s^{s_2} ds' \tilde{k}(s) \tilde{k}(s') (s' - s) \quad (120)$$

Normally, the effects are dominated by  $i_1^-$  and  $i_1^+$ .

**Trapazoidal models** This method is based on a third-order matrix formalism and the assumption that the fringe fields depend linearly on  $z$ . Although the third-order matrix is computed, it is important to note that the assumed fields do not satisfy Maxwell's equations.

To invoke this method, one specifies “inset” or “fixed-strength” for the **FRINGE\_TYPE** parameter and then provides a non-zero value for **FFRINGE**. If **FFRINGE** is zero (the default), then the magnet is hard-edged regardless of the setting of **FRINGE\_TYPE**. If **FFRINGE** is positive, then the magnet has linear fringe fields of length **FFRINGE**\***L**/2 at each end. That is, the total length of fringe field from both ends combined is **FFRINGE**\***L**.

Depending on the value of **FRINGE\_TYPE**, the fringe fields are modeled as contained within the length **L** (“inset” type) or extending symmetrically outside the length **L** (“fixed-strength” type).

For “inset” type fringe fields, the length of the “hard core” part of the quadrupole is **L**\*(1-**FFRINGE**). For “fixed-strength” type fringe fields, the length of the hard core is **L**\*(1-**FFRINGE**/2). In the latter case, the fringe gradient reaches 50% of the hard core value at the nominal boundaries of the magnet. This means that the integrated strength of the magnet does not change as the **FFRINGE** parameter is varied. This is not the case with “inset” type fringe fields.

## QUFRINGE

### 10.73 QUFRINGE—An element consisting of a linearly increasing or decreasing quadrupole field.

An element consisting of a linearly increasing or decreasing quadrupole field.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| K1             | $1/M^2$ | double | 0.0     | peak geometric strength  |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| DX             | $M$     | double | 0.0     | misalignment   |
| DY             | $M$     | double | 0.0     | misalignment   |
| DZ             | $M$     | double | 0.0     | misalignment   |
| FSE            |         | double | 0.0     | fractional strength error  |
| DIRECTION      |         | long   | 0       | 1=entrance, -1=exit  |
| ORDER          |         | long   | 0       | matrix order   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## RAMPP

### 10.74 RAMPP—A momentum-ramping element that changes the central momentum according to an SDDS-format file of the momentum factor vs time in seconds.

A momentum-ramping element that changes the central momentum according to an SDDS-format file of the momentum factor vs time in seconds.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| WAVEFORM       |       | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving momentum factor vs time   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

**Explanation of <filename>=<x>+<y> format:** Several elements in **elegant** make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is **waveform.sdds=t+A**, then it means that columns **t** and **A** will be taken from file **waveform.sdds**. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## RAMPRF

### 10.75 RAMPRF—A voltage-, phase-, and/or frequency-ramped RF cavity, implemented like RFCA.

A voltage-, phase-, and/or frequency-ramped RF cavity, implemented like RFCA.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default   | Description  |
|-----------------|-------|--------|-----------|--|
| L               | $M$   | double | 0.0       | length   |
| VOLT            | $V$   | double | 0.0       | nominal voltage  |
| PHASE           | $DEG$ | double | 0.0       | nominal phase  |
| FREQ            | $Hz$  | double | 500000000 | nominal frequency  |
| PHASE_REFERENCE |       | long   | 0         | phase reference number (to link with other time-dependent elements)  |
| VOLT_WAVEFORM   |       | STRING | NULL      | <filename>=<x>+<y> form specification of input file giving voltage waveform factor vs time   |
| PHASE_WAVEFORM  |       | STRING | NULL      | <filename>=<x>+<y> form specification of input file giving phase offset vs time (requires FREQ_WAVEFORM)   |
| FREQ_WAVEFORM   |       | STRING | NULL      | <filename>=<x>+<y> form specification of input file giving frequency-factor vs time (requires PHASE_WAVEFORM)  |
| FIDUCIAL        |       | STRING | NULL      | mode for determining fiducial arrival time (light, tmean, first, pmaximum)   |
| GROUP           |       | string | NULL      | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

**Explanation of <filename>=<x>+<y> format:** Several elements in **elegant** make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is **waveform.sdds=t+A**, then it means that columns **t** and **A**

will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.



# RBEN

## 10.76 RBEN—A rectangular dipole, implemented as a SBEND with edge angles, up to 2nd order. Use CSBEND for symplectic tracking.

A rectangular dipole, implemented as a SBEND with edge angles, up to 2nd order. Use CSBEND for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default | Description   |
|----------------|---------|--------|---------|---|
| L              | $M$     | double | 0.0     | magnet (straight) length                              |
| ANGLE          | $RAD$   | double | 0.0     | bend angle  |
| K1             | $1/M^2$ | double | 0.0     | geometric focusing strength                           |
| E1             | $RAD$   | double | 0.0     | entrance edge angle                                   |
| E2             | $RAD$   | double | 0.0     | exit edge angle                                       |
| TILT           | $RAD$   | double | 0.0     | rotation about incoming longitudinal axis             |
| K2             | $1/M^3$ | double | 0.0     | geometric sextupole strength                          |
| H1             | $1/M$   | double | 0.0     | entrance pole-face curvature                          |
| H2             | $1/M$   | double | 0.0     | exit pole-face curvature                              |
| HGAP           | $M$     | double | 0.0     | half-gap between poles                                |
| FINT           |         | double | 0.5     | edge-field integral                                   |
| DX             | $M$     | double | 0.0     | misalignment of entrance                              |
| DY             | $M$     | double | 0.0     | misalignment of entrance                              |
| DZ             | $M$     | double | 0.0     | misalignment of entrance                              |
| FSE            |         | double | 0.0     | fractional strength error of all components           |
| FSE_DIPOLE     |         | double | 0.0     | fractional strength error of dipole component         |
| FSE_QUADRUPOLE |         | double | 0.0     | fractional strength error of quadrupole component     |
| ETILT          | $RAD$   | double | 0.0     | error rotation about incoming longitudinal axis       |
| EDGE1_EFFECTS  |         | short  | 1       | include entrance edge effects?                        |
| EDGE2_EFFECTS  |         | short  | 1       | include exit edge effects?                            |
| ORDER          |         | short  | 0       | matrix order  |
| EDGE_ORDER     |         | short  | 0       | edge matrix order                                     |
| TRANSPORT      |         | short  | 0       | use (incorrect) TRANSPORT equations for T436 of edge? |
| USE_BN         |         | short  | 0       | use B1 and B2 instead of K1 and K2 values?            |
| B1             | $1/M$   | double | 0.0     | $K1 = B1/\rho$ , where $\rho$ is bend radius          |

## RBEN continued

A rectangular dipole, implemented as a SBEND with edge angles, up to 2nd order. Use CSBEND for symplectic tracking.

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| B2             | $1/M^2$ | double | 0.0     | $K2 = B2/\rho$   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

When adding errors, care should be taken to choose the right parameters. The **FSE** and **ETILT** parameters are used for assigning errors to the strength and alignment relative to the ideal values given by **ANGLE** and **TILT**. One can also assign errors to **ANGLE** and **TILT**, but this has a different meaning: in this case, one is assigning errors to the survey itself. The reference beam path changes, so there is no orbit/trajectory error. The most common thing is to assign errors to **FSE** and **ETILT**. Note that when adding errors to **FSE**, the error is assumed to come from the power supply, which means that multipole strengths also change.

*Special note about splitting dipoles:* when dipoles are long, it is common to want to split them into several pieces, to get a better look at the interior optics. When doing this, care must be exercised not to change the optics. **elegant** has some special features that are designed to reduce or manage potential problems. At issue is the need to turn off edge effects between the portions of the same dipole.

First, one can simply use the **divide\_elements** command to set up the splitting. Using this command, **elegant** takes care of everything.

Second, one can use a series of dipoles *with the same name*. In this case, **elegant** automatically turns off interior edge effects. This is true when the dipole elements directly follow one another or are separated by a **MARK** element.

Third, one can use a series of dipoles with different names. In this case, you must also use the **EDGE1\_EFFECTS** and **EDGE2\_EFFECTS** parameters to turn off interior edge effects.

## RCOL

### 10.77 RCOL—A rectangular collimator.

A rectangular collimator.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| X_MAX          | $M$   | double | 0.0     | half-width in x  |
| Y_MAX          | $M$   | double | 0.0     | half-width in y  |
| DX             | $M$   | double | 0.0     | misalignment   |
| DY             | $M$   | double | 0.0     | misalignment   |
| OPEN_SIDE      |       | STRING | NULL    | which side, if any, is open (+x, -x, +y, -y)   |
| INVERT         |       | short  | 0       | If non-zero, particles inside the aperture are lost while those outside are transmitted.   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## RECIRC

### 10.78 RECIRC—An element that defines the point to which particles recirculate in multi-pass tracking

An element that defines the point to which particles recirculate in multi-pass tracking

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| LRECIRC_ELEMENT |       | long   | 0       |  |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## REFLECT

### 10.79 REFLECT—Reflects the beam back on itself, which is useful for multiple beamline matching.

Reflects the beam back on itself, which is useful for multiple beamline matching.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| DUMMY          |       | long   | 0       |  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## REMCOR

### 10.80 REMCOR—An element to remove correlations from the tracked beam to simulate certain types of correction.

An element to remove correlations from the tracked beam to simulate certain types of correction.

Parallel capable? : no

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| X              |       | short  | 1       | remove correlations in x?  |
| XP             |       | short  | 1       | remove correlations in x'?   |
| Y              |       | short  | 1       | remove correlations in y?  |
| YP             |       | short  | 1       | remove correlations in y'?   |
| WITH           |       | short  | 6       | coordinate to remove correlations with (1,2,3,4,5,6)=(x,x',y,y',s,dP/Po)   |
| ONCE_ONLY      |       | short  | 0       | compute correction only for first beam, apply to all?  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## RFCA

### **10.81 RFCA—A first-order matrix RF cavity with exact phase dependence.**

A first-order matrix RF cavity with exact phase dependence.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name   | Units | Type   | Default   | Description  |
|------------------|-------|--------|-----------|--|
| L                | $M$   | double | 0.0       | length   |
| VOLT             | $V$   | double | 0.0       | peak voltage   |
| PHASE            | $DEG$ | double | 0.0       | phase  |
| FREQ             | $Hz$  | double | 500000000 | frequency  |
| Q                |       | double | 0.0       | cavity Q (for cavity that charges up to given voltage from 0)  |
| PHASE_REFERENCE  |       | long   | 0         | phase reference number (to link with other time-dependent elements)  |
| CHANGE_P0        |       | short  | 0         | does cavity change central momentum?   |
| CHANGE_T         |       | short  | 0         | set to 1 for long runs to avoid rounding error in phase  |
| FIDUCIAL         |       | STRING | NULL      | mode for determining fiducial arrival time (light, tmean, first, pmaximum)   |
| END1_FOCUS       |       | short  | 0         | include focusing at entrance?  |
| END2_FOCUS       |       | short  | 0         | include focusing at exit?  |
| BODY_FOCUS_MODEL |       | STRING | NULL      | None (default) or SRS (simplified Rosenzweig/Serafini for standing wave)   |
| N_KICKS          |       | long   | 0         | Number of kicks to use for kick method. Set to zero for matrix method.   |
| DX               | $M$   | double | 0.0       | misalignment   |
| DY               | $M$   | double | 0.0       | misalignment   |
| T_REFERENCE      | $S$   | double | -1        | arrival time of reference particle   |
| LINEARIZE        |       | short  | 0         | Linearize phase dependence?  |
| LOCK_PHASE       |       | short  | 0         | Lock phase to given value regardless of bunch centroid motion?   |
| GROUP            |       | string | NULL      | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The phase convention is as follows, assuming a positive rf voltage: PHASE=90 is the crest for acceleration. PHASE=180 is the stable phase for a storage ring above transition without energy losses.

The body-focusing model is based on Rosenzweig and Serafini, Phys. Rev. E 49 (2), 1599. As



suggested by N. Towne (NSLS), I simplified this to assume a pure pi-mode standing wave.

The `CHANGE_T` parameter may be needed for reasons that stem from `elegant`'s internal use of the total time-of-flight as the longitudinal coordinate. If the accelerator is very long or a large number of turns are being tracked, rounding error may affect the simulation, introducing spurious phase jumps. By setting `CHANGE_T=1`, you can force `elegant` to modify the time coordinates of the particles to subtract off  $NT_{rf}$ , where  $T_{rf}$  is the rf period and  $N = \lfloor t/T_{rf} + 0.5 \rfloor$ . If you are tracking a ring with rf at some harmonic  $h$  of the revolution frequency, this will result in the time coordinates being relative to the ideal revolution period,  $T_{rf} * h$ . If you have multiple rf cavities in a ring, you need only use this feature on one of them. Also, you can use `CHANGE_T=1` if you simply prefer to have the offset time coordinates in output files and analysis.

N.B.: *Do not use `CHANGE_T=1` if you have rf cavities that are not at harmonics of one another or if you have other time-dependent elements that are not resonant.*

## RFCW

### 10.82 RFCW—A combination of RFCA, WAKE, TRWAKE, and LSCDRIFT.

A combination of RFCA, WAKE, TRWAKE, and LSCDRIFT.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name   | Units      | Type   | Default   | Description   |
|------------------|------------|--------|-----------|---|
| L                | <i>M</i>   | double | 0.0       | length  |
| CELL_LENGTH      | <i>M</i>   | double | 0.0       | cell length (used to scale wakes, which are assumed to be given for a cell, according to L/CELL_LENGTH) |
| VOLT             | <i>V</i>   | double | 0.0       | voltage   |
| PHASE            | <i>DEG</i> | double | 0.0       | phase   |
| FREQ             | <i>Hz</i>  | double | 500000000 | frequency   |
| Q                |            | double | 0.0       | cavity Q (for cavity that charges up to voltage from 0)   |
| PHASE_REFERENCE  |            | long   | 0         | phase reference number (to link with other time-dependent elements)                                     |
| CHANGE_P0        |            | long   | 0         | does element change central momentum?   |
| CHANGE_T         |            | long   | 0         | see RFCA documentation  |
| FIDUCIAL         |            | STRING | NULL      | mode for determining fiducial arrival time (light, tmean, first, pmaximum)                              |
| END1_FOCUS       |            | long   | 0         | include focusing at entrance?   |
| END2_FOCUS       |            | long   | 0         | include focusing at exit?   |
| BODY_FOCUS_MODEL |            | STRING | NULL      | None (default) or SRS (simplified Rosenzweig/Serafini for standing wave)                                |
| N_KICKS          |            | long   | 0         | Number of kicks to use for kick method. Set to zero for matrix method.                                  |
| ZWAKE            |            | long   | 1         | If zero, longitudinal wake is turned off.   |
| TRWAKE           |            | long   | 1         | If zero, transverse wakes are turned off.   |
| WAKEFILE         |            | STRING | NULL      | name of file containing Green functions   |
| ZWAKEFILE        |            | STRING | NULL      | if WAKEFILE=NULL, optional name of file containing longitudinal Green function                          |

## RFCW continued

A combination of RFCA, WAKE, TRWAKE, and LSCDRIFT.

| Parameter Name            | Units | Type   | Default | Description   |
|---------------------------|-------|--------|---------|---|
| TRWAKEFILE                |       | STRING | NULL    | if WAKEFILE=NULL, optional name of file containing transverse Green functions   |
| TCOLUMN                   |       | STRING | NULL    | column containing time data   |
| WXCOLUMN                  |       | STRING | NULL    | column containing x Green function  |
| WYCOLUMN                  |       | STRING | NULL    | column containing y Green function  |
| WZCOLUMN                  |       | STRING | NULL    | column containing longitudinal Green function   |
| N_BINS                    |       | long   | 0       | number of bins for current histogram  |
| INTERPOLATE               |       | long   | 0       | interpolate wake?   |
| SMOOTHING                 |       | long   | 0       | Use Savitzky-Golay filter to smooth current histogram?  |
| SG_HALFWIDTH              |       | long   | 4       | Savitzky-Golay filter half-width for smoothing  |
| SG_ORDER                  |       | long   | 1       | Savitzky-Golay filter order for smoothing   |
| DX                        | $M$   | double | 0.0     | misalignment  |
| DY                        | $M$   | double | 0.0     | misalignment  |
| LINEARIZE                 |       | long   | 0       | Linearize phase dependence?   |
| LSC                       |       | long   | 0       | Include longitudinal space-charge impedance?  |
| LSC_BINS                  |       | long   | 1024    | Number of bins for LSC calculations   |
| LSC_INTERPOLATE           |       | long   | 1       | Interpolate computed LSC wake?  |
| LSC_LOW_FREQUENCY_CUTOFF0 |       | double | -1      | Highest spatial frequency at which low-frequency cutoff filter is zero. If not positive, no low-frequency cutoff filter is applied. Frequency is in units of Nyquist (0.5/binsize). |
| LSC_LOW_FREQUENCY_CUTOFF1 |       | double | -1      | Lowest spatial frequency at which low-frequency cutoff filter is 1. If not given, defaults to LOW_FREQUENCY_CUTOFF1.  |

## RFCW continued

A combination of RFCA, WAKE, TRWAKE, and LSCDRIFT.

| Parameter Name             | Units | Type   | Default | Description   |
|----------------------------|-------|--------|---------|---|
| LSC_HIGH_FREQUENCY_CUTOFF0 |       | double | -1      | Spatial frequency at which smoothing filter begins for LSC. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize). |
| LSC_HIGH_FREQUENCY_CUTOFF1 |       | double | -1      | Spatial frequency at which smoothing filter is 0 for LSC. If not given, defaults to HIGH_FREQUENCY_CUTOFF0.   |
| LSC_RADIUS_FACTOR          |       | double | 1.7     | LSC radius is (Sx+Sy)/2*RADIUS_FACTOR   |
| WAKES_AT_END               |       | long   | 0       | Do wake kicks at end of segment (for backward compatibility)?   |
| GROUP                      |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup          |

This element is a combination of the RFCA, WAKE, and TRWAKE elements. As such, it provides combined simulation of an rf cavity with longitudinal and transverse wakes, as well as longitudinal space charge.

For the wakes, the input files and their interpretation are identical to WAKE and TRWAKE, except that the transverse and longitudinal wakes are interpreted as the wakes for a single cell of length given by the CELL\_LENGTH parameter.

Users should read the entries for WAKE, TRWAKE, and RFCA for more details on this element.

This element simulates longitudinal space charge using the method described in [22]. This is based on the longitudinal space charge impedance per unit length

$$Z_{lsc}(k) = \frac{iZ_0}{\pi k r_b^2} \left[ 1 - \frac{k r_b}{\gamma} K_1 \left( \frac{k r_b}{\gamma} \right) \right] \quad (121)$$

## RFDF

### 10.83 RFDF—A simple traveling or standing wave deflecting RF cavity.

A simple traveling or standing wave deflecting RF cavity.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units | Type   | Default    | Description  |
|---------------------|-------|--------|------------|--|
| L                   | $M$   | double | 0.0        | length   |
| PHASE               | $DEG$ | double | 0.0        | phase  |
| TILT                | $RAD$ | double | 0.0        | rotation about longitudinal axis   |
| FREQUENCY           | $HZ$  | double | 2856000000 | frequency  |
| VOLTAGE             | $V$   | double | 0.0        | voltage  |
| FSE                 |       | double | 0.0        | Fractional Strength Error  |
| B2                  |       | double | 0.0        | Normalized sextupole strength, kick=(1+b2*(x <sup>2</sup> -y <sup>2</sup> )/2)...          |
| TIME_OFFSET         | $S$   | double | 0.0        | time offset (adds to phase)  |
| N_KICKS             |       | long   | 0          | number of kicks (0=autoscale)  |
| PHASE_REFERENCE     |       | long   | 0          | phase reference number (to link with other time-dependent elements)                        |
| STANDING_WAVE       |       | short  | 0          | If nonzero, then cavity is standing wave.  |
| VOLTAGE_WAVEFORM    |       | STRING | NULL       | <filename>=<x>+<y> form specification of input file giving voltage waveform factor vs time |
| VOLTAGE_PERIODIC    |       | short  | 0          | If non-zero, voltage waveform is periodic with period given by time span.                  |
| ALIGN_WAVEFORMS     |       | short  | 0          | If non-zero, waveforms' t=0 is aligned with first bunch arrival time.                      |
| VOLTAGE_NOISE       |       | double | 0.0        | Rms fractional noise level for voltage.  |
| PHASE_NOISE         | $DEG$ | double | 0.0        | Rms noise level for phase.   |
| GROUP_VOLTAGE_NOISE |       | double | 0.0        | Rms fractional noise level for voltage linked to group.                                    |
| GROUP_PHASE_NOISE   | $DEG$ | double | 0.0        | Rms noise level for phase linked to group.   |
| VOLTAGE_NOISE_GROUP |       | long   | 0          | Group number for voltage noise.  |

## RFDF continued

A simple traveling or standing wave deflecting RF cavity.

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| PHASE_NOISE_GROUP   |       | long   | 0       | Group number for phase noise.  |
| START_PASS          |       | long   | -1      | If non-negative, pass on which to start modeling cavity.   |
| END_PASS            |       | long   | -1      | If non-negative, pass on which to end modeling cavity.   |
| DRIFT_MATRIX        |       | short  | 0       | If non-zero, calculations involving matrices assume this element is a drift space.   |
| DX                  | $M$   | double | 0.0     | misalignment   |
| DY                  | $M$   | double | 0.0     | misalignment   |
| DZ                  | $M$   | double | 0.0     | misalignment   |
| MAGNETIC_DEFLECTION |       | short  | 0       | If non-zero, deflection is assumed to be performed by a magnetic field, rather than electric field (default).  |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This cavity provides a transverse deflection that is constant as a function of transverse coordinates. It is probably the best model for a real cavity, because real cavities contain a mixture of TM- and TE-like modes that result in a uniform deflection.

For simplicity of use, the deflection is specified as a voltage, even though it originates in a magnetic field. The magnetic field is

$$B = B_0 \hat{y} \cos \omega t \quad (122)$$

The corresponding electric field is obtained from Faraday's law (MKS units)

$$\left( \nabla \times \vec{E} \right)_y = - \left( \frac{\partial \vec{B}}{\partial t} \right)_y. \quad (123)$$

Assuming  $E_x = E_y = 0$ , we have

$$E_z = B_0 \omega x \sin \omega t. \quad (124)$$

The change in momenta (in units of  $mc$ ) in passing through a slice of length  $\Delta L$  is

$$\Delta p_x = \frac{q B_0 \Delta L}{mc} \cos \omega t \quad (125)$$

$$\Delta p_y = 0 \quad (126)$$

$$\Delta p_z = \frac{q B_0 \omega x \Delta L}{mc^2} \sin \omega t \quad (127)$$

If we want to think in terms of a deflecting voltage, we can re-write this as

$$\Delta p_x = \frac{qV}{mc^2} \cos \omega t \quad (128)$$

$$\Delta p_y = 0 \quad (129)$$

$$\Delta p_z = \frac{qV}{mc^2} kx \sin \omega t, \quad (130)$$

where  $k = \omega/c$ .

**Explanation of <filename>=<x>+<y> format:** Several elements in **elegant** make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is **waveform.sdds=t+A**, then it means that columns **t** and **A** will be taken from file **waveform.sdds**. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## RFMODE

### 10.84 RFMODE—A simulation of a beam-driven TM monopole mode of an RF cavity.

A simulation of a beam-driven TM monopole mode of an RF cavity.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name     | Units      | Type   | Default | Description  |
|--------------------|------------|--------|---------|--|
| RA                 | $\Omega m$ | double | 0.0     | shunt impedance, $R_a = \sqrt{2}/P$  |
| RS                 | $\Omega m$ | double | 0.0     | shunt impedance ( $R_s = R_a/2$ )  |
| Q                  |            | double | 0.0     | cavity Q   |
| FREQ               | $Hz$       | double | 0.0     | Resonant frequency of the cavity mode  |
| CHARGE             | $C$        | double | 0.0     | beam charge (or use CHARGE element)  |
| INITIAL_V          | $V$        | double | 0.0     | initial beam-loading voltage   |
| INITIAL_PHASE      | $RAD$      | double | 0.0     | initial beam-loading phase   |
| INITIAL_T          | $S$        | double | 0.0     | time at which INITIAL_V and INITIAL_PHASE held   |
| BETA               |            | double | 0.0     | normalized load impedance  |
| BIN_SIZE           | $S$        | double | 0.0     | bin size for current histogram (use 0 for autosize)  |
| N_BINS             |            | long   | 20      | number of bins for current histogram   |
| INTERPOLATE        |            | long   | 0       | if non-zero, interpolate voltage within bins   |
| PRELOAD            |            | long   | 0       | preload cavity with steady-state field   |
| PRELOAD_CHARGE     | $C$        | double | 0.0     | beam charge used for preloading calculations   |
| PRELOAD_FACTOR     |            | double | 1       | multiply preloaded field by this value   |
| PRELOAD_HARMONIC   |            | long   | 0       | If detuning from harmonic is greater than half the revolution frequency, automatic determination of the rf harmonic will fail. Give the harmonic explicitly with this parameter. |
| RIGID_UNTIL_PASS   |            | long   | 0       | don't affect the beam until this pass  |
| DETUNED_UNTIL_PASS |            | long   | 0       | cavity is completely detuned until this pass   |



## RFMODE continued

A simulation of a beam-driven TM monopole mode of an RF cavity.

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| SAMPLE_INTERVAL     |       | long   | 1       | passes between samples to RECORD file  |
| FLUSH_INTERVAL      |       | long   | 1000    | samples between flushing output to RECORD file   |
| RECORD              |       | STRING | NULL    | output file for cavity fields  |
| SINGLE_PASS         |       | long   | 0       | if nonzero, don't accumulate field from pass to pass   |
| PASS_INTERVAL       |       | long   | 1       | interval in passes at which to apply PASS_INTERVAL times the field (may increase speed)  |
| FREQ_WAVEFORM       |       | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving frequency/f0 vs time, where f0 is the frequency given with the FREQ parameter       |
| Q_WAVEFORM          |       | STRING | NULL    | <filename>=<x>+<y> form specification of input file giving qualityFactor/Q0 vs time, where Q0 is the quality factor given the the Q parameter. |
| RAMP_PASSES         |       | long   | 0       | Number of passes over which to linearly ramp up the impedance to full strength.  |
| BINLESS             |       | long   | 0       | If nonzero, use algorithm that doesn't requiring binning. Best for few particles, widely spaced.   |
| RESET_FOR_EACH_STEP |       | long   | 1       | If nonzero, voltage and phase are reset for each simulation step.  |
| LONG_RANGE_ONLY     |       | long   | 0       | If nonzero, induced voltage from present turn does not affect bunch. Results are not self-consistent!  |

## RFMODE continued

A simulation of a beam-driven TM monopole mode of an RF cavity.

| Parameter Name           | Units | Type   | Default | Description  |
|--------------------------|-------|--------|---------|--|
| ALLOW_UNBINNED_PARTICLES |       | long   | 0       | If nonzero, will keep running even if some particles fall outside the binning region. Use with caution!  |
| N_CAVITIES               |       | long   | 1       | effect is multiplied by this number, simulating N identical cavities   |
| BUNCHED_BEAM_MODE        |       | long   | 1       | If 1, then do calculations bunch-by-bunch. If >1, use pseudo bunches.  |
| BUNCH_INTERVAL           | $S$   | double | 0.0     | For pseudo-bunch mode, time between bunches.   |
| DRIVE_FREQUENCY          | $Hz$  | double | 0.0     | drive frequency from generator. If zero, no generator voltage is applied.  |
| V_SETPOINT               | $V$   | double | 0.0     | setpoint for total cavity voltage  |
| PHASE_SETPOINT           | $DEG$ | double | 0.0     | setpoint for total cavity phase  |
| UPDATE_INTERVAL          |       | long   | 1       | update interval of feedback in units of rf period  |
| READ_OFFSET              |       | long   | 0       | Offset in buckets of point at which voltage and phase are read for feedback relative to the first bunch passage. A positive value corresponds to reading before bunch passage. |
| ADJUSTMENT_START         |       | long   | 0       | Pass on which to begin adjustment of the effective voltage setpoint.   |
| ADJUSTMENT_END           |       | long   | 0       | Pass on which to stop adjustment of the effective voltage setpoint.  |
| ADJUSTMENT_INTERVAL      |       | long   | 100     | Interval in passes between adjustment of the effective voltage setpoint.   |

## RFMODE continued

A simulation of a beam-driven TM monopole mode of an RF cavity.

| Parameter Name      | Units | Type   | Default | Description   |
|---------------------|-------|--------|---------|---|
| ADJUSTMENT_FRACTION |       | double | 0.0     | Fraction of voltage setpoint error taken out on each adjustment step                      |
| AMPLITUDE_FILTER    |       | STRING | NULL    | IIR filter specification for amplitude feedback   |
| PHASE_FILTER        |       | STRING | NULL    | IIR filter specification for phase feedback   |
| IN_PHASE_FILTER     |       | STRING | NULL    | IIR filter specification for in-phase component feedback                                  |
| QUADRATURE_FILTER   |       | STRING | NULL    | IIR filter specification for quadrature component feedback                                |
| FEEDBACK_RECORD     |       | STRING | NULL    | output file for feedback data   |
| MUTE_GENERATOR      |       | long   | -1      | If nonnegative, gives the pass on which to mute the generator. This simulates an rf trip. |
| NOISE_ALPHA_GEN     |       | STRING | NULL    | <filename>=<x>+<y> specifying alpha(t) for generator noise.                               |
| NOISE_PHI_GEN       |       | STRING | NULL    | <filename>=<x>+<y> specifying dphi(t) for generator noise, in radians.                    |
| NOISE_ALPHA_V       |       | STRING | NULL    | <filename>=<x>+<y> specifying alpha(t) for voltage noise.                                 |
| NOISE_PHI_V         |       | STRING | NULL    | <filename>=<x>+<y> specifying dphi(t) for voltage noise, in radians.                      |
| NOISE_I_GEN         |       | STRING | NULL    | <filename>=<x>+<y> specifying ni(t) for in-phase generator noise.                         |
| NOISE_Q_GEN         |       | STRING | NULL    | <filename>=<x>+<y> specifying nq(t) for quadrature generator noise.                       |

## RFMODE continued

A simulation of a beam-driven TM monopole mode of an RF cavity.

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| NOISE_I_V      |       | STRING | NULL    | <filename>=<x>+<y><br>specifying ei(t) for in-phase<br>voltage noise.   |
| NOISE_Q_V      |       | STRING | NULL    | <filename>=<x>+<y><br>specifying eq(t) for quadra-<br>ture voltage noise.   |
| GROUP          |       | string | NULL    | Optionally used to assign an<br>element to a group, with a<br>user-defined name. Group<br>names will appear in the pa-<br>rameter output file in the col-<br>umn ElementGroup |

This element simulates a beam-driven monopole mode cavity using the fundamental theorem of beam loading and phasor rotation. In addition, a generator-driven field may be included using a feedback system [44].

Note on phase conventions: the phase convention for the `PHASE_SETPoint` parameter of `RFMODE` is the same as for the `PHASE` parameter of `RFCA`. However, in the output files from `RFMODE`, i.e., the files requested with the `RECORD` and `FEEDBACK_RECORD` parameters, a different convention is used, which differs by  $-90$  degrees from the `PHASE_SETPoint` parameter.

The feedback implementation uses either amplitude and phase feedback or else in-phase and quadrature feedback. Figure 3 shows the model used for the feedback system. More information is available in [44]. Feedback is active when a non-zero value is given for `DRIVE_FREQUENCY` and when either `AMPLITUDE_FILTER` and `PHASE_FILTER` or else `IN_PHASE_FILTER` and `QUADRATURE_FILTER` are given.

The feedback loop reads the cavity state and acts on the generator at a fixed interval (in buckets) of `UPDATE_INTERVAL`. The timing of this activity is aligned to the arrival time of the first bunch in the `RFMODE` element. By default (`READ_OFFSET=0`), the timing is such that the state is read just before the next arrival of that bunch; in particular, it is 180 degrees ahead of that arrival. If bunches are equally spaced by, say  $N_b$  buckets, the `UPDATE_INTERVAL` parameter should ideally be  $mN_b$ , where  $m > 0$  is an integer. This ensures that the state is read at a fixed timing relative to the bunches.

The rf feedback feature makes use of the voltage amplitude measured when there is no bunch present. The `RECORD` file shows the voltage seen by the beam, computed by averaging over the voltage for each particle. These may deviate by values from a few percent to of order ten percent, depending on the loss factor for the cavity and the number of bunches; this is caused by the fact that the rate at which an intense bunch removes energy from the cavity will typically, albeit briefly, exceed the power from the generator. To reduce the impact of this effect, one may use the `ADJUSTMENT_FRACTION`, `ADJUSTMENT_START`, and `ADJUSTMENT_INTERVAL` parameters to modify the voltage setpoint. If `ADJUSTMENT_FRACTION` is non-zero, then for every `ADJUSTMENT_INTERVALth` pass after the `ADJUSTMENT_STARTth` pass, the voltage setpoint will be adjusted based on a comparison of the bunch-averaged voltage to the user's setpoint. E.g., if the bunch-averaged voltage is 100 V

too low and ADJUSTMENT\_FRACTION is 0.1, the voltage setpoint will be raised by 10 V. Users should note that if ADJUSTMENT\_FRACTION is too large or ADJUSTMENT\_INTERVAL is too small, the system may be unstable.

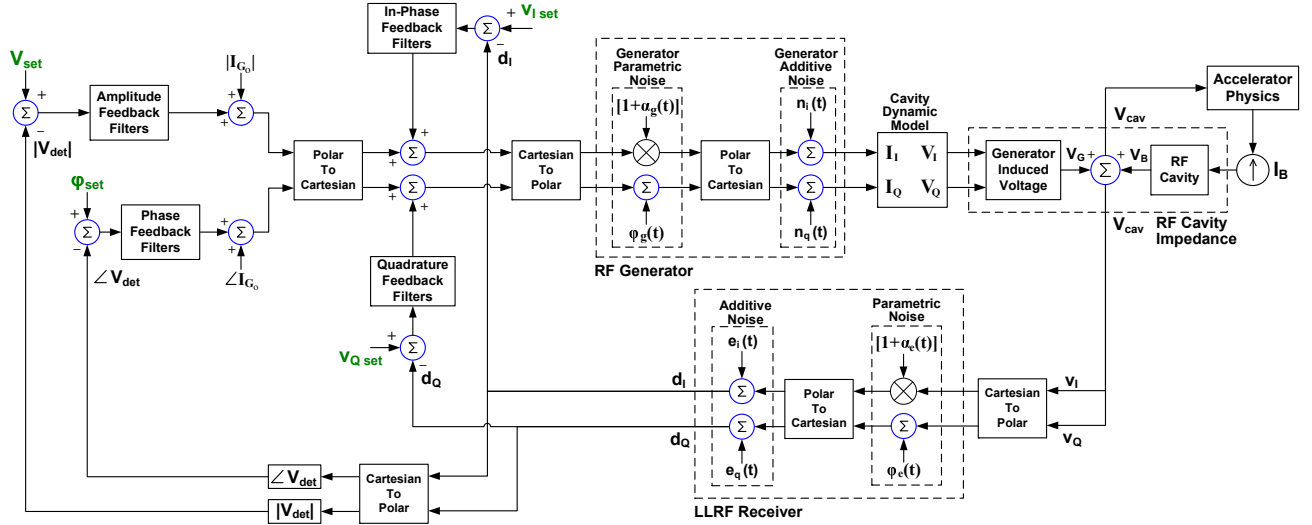


Figure 3: Rf feedback model used by the RFMODE element.

Normally, the field dumped in the cavity by one particle affects trailing particles in the same turn. However, if one is also using a WAKE or ZLONGIT element to simulate the short-range wake of the cavity, this would be double-counting. In that case, one can use LONG\_RANGE\_ONLY=1 to suppress the same-turn effects of the RFMODE element.

Two output files are available: the RECORD file includes bunch-by-bunch data on the beam-induced fields and the total cavity fields. The FEEDBACK\_RECORD file includes tick-by-tick data from the feedback system simulation; *writing this file this can significantly impact performance*.

NB: when BUNCHED\_BEAM\_MODE is set to a value other than 1, in order to obtain the effect of several bunches while tracking only one bunch, the total charge set with the TOTAL parameter of the CHARGE element should equal the charge in a single bunch, not the entire beam. However, when BUNCHED\_BEAM\_MODE=1 (allowing an indeterminant number of bunches to be actually present), then TOTAL should be the total for all bunches together.

**Explanation of <filename>=<x>+<y> format:** Several elements in elegant make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is waveform.sdds=t+A, then it means that columns t and A will be taken from file waveform.sdds. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## RFTM110

**10.85 RFTM110—Tracks through a TM110-mode (deflecting) rf cavity with all magnetic and electric field components. NOT RECOMMENDED—See below.**

Tracks through a TM110-mode (deflecting) rf cavity with all magnetic and electric field components.  
NOT RECOMMENDED—See below.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units      | Type   | Default    | Description  |
|---------------------|------------|--------|------------|--|
| PHASE               | <i>DEG</i> | double | 0.0        | phase  |
| TILT                | <i>RAD</i> | double | 0.0        | rotation about longitudinal axis   |
| FREQUENCY           | <i>HZ</i>  | double | 2856000000 | frequency  |
| VOLTAGE             | <i>V</i>   | double | 0.0        | peak deflecting voltage  |
| PHASE_REFERENCE     |            | long   | 0          | phase reference number (to link with other time-dependent elements)  |
| VOLTAGE_WAVEFORM    |            | STRING | NULL       | <filename>=<x>+<y> form specification of input file giving voltage waveform factor vs time   |
| VOLTAGE_PERIODIC    |            | short  | 0          | If non-zero, voltage waveform is periodic with period given by time span.  |
| ALIGN_WAVEFORMS     |            | short  | 0          | If non-zero, waveforms' t=0 is aligned with first bunch arrival time.  |
| VOLTAGE_NOISE       |            | double | 0.0        | Rms fractional noise level for voltage.  |
| PHASE_NOISE         | <i>DEG</i> | double | 0.0        | Rms noise level for phase.   |
| GROUP_VOLTAGE_NOISE |            | double | 0.0        | Rms fractional noise level for voltage linked to group.  |
| GROUP_PHASE_NOISE   | <i>DEG</i> | double | 0.0        | Rms noise level for phase linked to group.   |
| VOLTAGE_NOISE_GROUP |            | long   | 0          | Group number for voltage noise.  |
| PHASE_NOISE_GROUP   |            | long   | 0          | Group number for phase noise.  |
| START_PASS          |            | long   | -1         | If non-negative, pass on which to start modeling cavity.   |
| END_PASS            |            | long   | -1         | If non-negative, pass on which to end modeling cavity.   |
| GROUP               |            | string | NULL       | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

**NB:** Although this element is correct insofar as it uses the fields for a pure TM<sub>110</sub> mode, it is recommended that the **RFDF** element be used instead. In a real deflecting cavity with entrance and exit tubes, the deflecting mode is a hybrid TE/TM mode, in which the deflection has no dependence on the radial coordinate.

To derive the field expansion, we start with some results from Jackson[17], section 8.7. The

longitudinal electric field for a TM mode is just

$$E_z = -2iE_0\Psi(\rho, \phi) \cos\left(\frac{p\pi z}{d}\right) e^{-i\omega t}, \quad (131)$$

where  $p$  is an integer,  $d$  is the length of the cavity, and we use cylindrical coordinates  $(\rho, \phi, z)$ . The factor of  $-2i$  represents a choice of sign and phase convention. We are interested in the TM<sub>110</sub> mode, so we set  $p = 0$ . In this case, we have

$$E_x = E_y = 0 \quad (132)$$

and (using CGS units)

$$\vec{H} = -2iE_0 \frac{i\epsilon\omega}{ck^2} \hat{z} \times \nabla \Psi e^{-i\omega t}. \quad (133)$$

For a cylindrical cavity, the function  $\Psi$  for the  $m = 1$  aximuthal mode is

$$\Psi(\rho, \phi) = J_1(k\rho) \cos \phi, \quad (134)$$

where  $k = x_{11}/R$ ,  $x_{11}$  is the first zero of  $J_1(x)$ , and  $R$  is the cavity radius. We don't need to know the cavity radius, since  $k = \omega/c$ , where  $\omega$  is the resonant frequency. By choosing  $\cos \phi$  for the aximuthal dependence, we'll get a magnetic field primarily in the vertical direction.

In MKS units, the magnetic field is

$$\vec{B} = \frac{2E_0}{kc} e^{-i\omega t} \left( \hat{\rho} \frac{J_1(k\rho)}{\rho} \sin \phi + \hat{\phi} \cos \phi \frac{\partial J_1(k\rho)}{\partial \rho} \right). \quad (135)$$

Using `mathematica`, we expanded these expressions to sixth order in  $k * \rho$ . Here, we present only the expressions to second order. Taking the real parts only, we now have

$$E_z \approx E_0 k \rho \cos \phi \sin \omega t \quad (136)$$

$$cB_\rho \approx E_0 \left( 1 - \frac{k^2 \rho^2}{8} \right) \sin \phi \cos \omega t \quad (137)$$

$$cB_\phi \approx E_0 \left( 1 - \frac{3k^2 \rho^2}{8} \right) \cos \phi \cos \omega t \quad (138)$$

The Cartesian components of  $\vec{B}$  can be computed easily

$$cB_x = cB_\rho \cos \phi - cB_\phi \sin \phi \quad (139)$$

$$= \frac{E_0}{4} \rho^2 k^2 \cos \phi \sin \phi \cos \omega t \quad (140)$$

$$cB_y = cB_\rho \sin \phi + cB_\phi \cos \phi \quad (141)$$

$$= E_0 \left( 1 - \frac{k^2 \rho^2 (2 \cos^2 \phi + 1)}{8} \right) \cos \omega t \quad (142)$$

The Lorentz force on an electron is  $F = -eE_z \hat{z} - ec\vec{\beta} \times \vec{B}$ , giving

$$F_x/e = \beta_z cB_y \quad (143)$$

$$F_y/e = -\beta_z cB_x \quad (144)$$

$$F_z/e = -E_z - \beta_x cB_y + \beta_y cB_x \quad (145)$$



We see that for  $\rho \rightarrow 0$ , we have  $E_z = 0$ ,  $B_x = 0$ , and

$$cB_y = E_0 \cos \omega t. \quad (146)$$

Hence, for  $\omega t = 0$  and  $E_0 > 0$  we have  $F_x > 0$ . This explains our choice of sign and phase convention above. Indeed, owing to the factor of 2, we have a peak deflection of  $eE_0L/E$ , where  $L$  is the cavity length and  $E$  the beam energy. Thus, if  $V = E_0L$  is specified in volts, and the beam energy expressed in electron volts, the deflection is simply the ratio of the two. As a result, we've chosen to parametrize the deflection strength simply by referring to the “deflecting voltage,”  $V$ .

**Explanation of <filename>=<x>+<y> format:** Several elements in `elegant` make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is `waveform.sdds=t+A`, then it means that columns `t` and `A` will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## RFTMEZO

### 10.86 RFTMEZO—A TM-mode RF cavity specified by the on-axis Ez field.

A TM-mode RF cavity specified by the on-axis Ez field.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name   | Units      | Type   | Default    | Description   |
|------------------|------------|--------|------------|---|
| L                | <i>M</i>   | double | 0.0        | length  |
| FREQUENCY        | <i>HZ</i>  | double | 2856000000 | frequency   |
| PHASE            | <i>RAD</i> | double | 0.0        | phase   |
| EZ_PEAK          | <i>V</i>   | double | 0.0        | Peak on-axis longitudinal electric field  |
| TIME_OFFSET      | <i>S</i>   | double | 0.0        | time offset (adds to phase)   |
| PHASE_REFERENCE  |            | long   | 0          | phase reference number (to link to other time-dependent elements)   |
| DX               | <i>M</i>   | double | 0.0        | misalignment  |
| DY               | <i>M</i>   | double | 0.0        | misalignment  |
| DZ               | <i>M</i>   | double | 0.0        | misalignment  |
| ETILT            | <i>RAD</i> | double | 0.0        | misalignment  |
| EYAW             | <i>RAD</i> | double | 0.0        | misalignment  |
| EPITCH           | <i>RAD</i> | double | 0.0        | misalignment  |
| N_STEPS          |            | long   | 100        | number of steps (for nonadaptive integration)   |
| RADIAL_ORDER     |            | short  | 1          | highest order in off-axis expansion   |
| CHANGE_P0        |            | short  | 0          | does element change central momentum?   |
| INPUTFILE        |            | STRING | NULL       | file containing Ez vs z at r=0  |
| ZCOLUMN          |            | STRING | NULL       | column containing z values  |
| EZCOLUMN         |            | STRING | NULL       | column containing Ez values   |
| SOLENOID_FILE    |            | STRING | NULL       | file containing map of Bz and Br vs z and r. Each page contains values for a single r.  |
| SOLENOID_ZCOLUMN |            | STRING | NULL       | column containing z values for solenoid map.  |
| SOLENOID_RCOLUMN |            | STRING | NULL       | column containing r values for solenoid map. If omitted, data is assumed to be for r=0 and an on-axis expansion is performed. |

# RFTMEZO continued

A TM-mode RF cavity specified by the on-axis Ez field.

| Parameter Name    | Units      | Type   | Default     | Description  |
|-------------------|------------|--------|-------------|--|
| SOLENOID_BZCOLUMN |            | STRING | NULL        | column containing Bz values for solenoid map.  |
| SOLENOID_BRCOLUMN |            | STRING | NULL        | column containing Br values for solenoid map. If omitted, data is assumed to be for r=0 and an on-axis expansion is performed.                             |
| SOLENOID_FACTOR   |            | double | 1           | factor by which to multiply solenoid fields.   |
| SOLENOID_DX       | <i>M</i>   | double | 0.0         | misalignment   |
| SOLENOID_DY       | <i>M</i>   | double | 0.0         | misalignment   |
| SOLENOID_DZ       | <i>M</i>   | double | 0.0         | misalignment   |
| SOLENOID_ETILT    | <i>RAD</i> | double | 0.0         | misalignment   |
| SOLENOID_EYAW     | <i>RAD</i> | double | 0.0         | misalignment   |
| SOLENOID_EPITCH   | <i>RAD</i> | double | 0.0         | misalignment   |
| BX_STRAY          |            | double | 0.0         | Uniform stray horizontal field   |
| BY_STRAY          |            | double | 0.0         | Uniform stray vertical field   |
| ACCURACY          |            | double | 0.0001      | integration accuracy   |
| METHOD            |            | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL          |            | STRING | t,median    | {t p},{median min max ave first light}<br>(e.g., "t,median")   |
| FIELD_TEST_FILE   |            | STRING | NULL        | filename for output of test fields (r=0)   |
| GROUP             |            | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## RIMULT

### 10.87 RIMULT—Multiplies radiation integrals by a given factor. Use to compute emittance for collection of various types of cells.

Multiplies radiation integrals by a given factor. Use to compute emittance for collection of various types of cells.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| FACTOR         |       | double | 1       | factor   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## RMDF

### 10.88 RMDF—A linearly-ramped electric field deflector, using an approximate analytical solution FOR LOW ENERGY PARTICLES.

A linearly-ramped electric field deflector, using an approximate analytical solution FOR LOW ENERGY PARTICLES.

Parallel capable? : no

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| L               | $M$   | double | 0.0     | length   |
| TILT            | $RAD$ | double | 0.0     | rotation about longitudinal axis   |
| RAMP_TIME       | $S$   | double | 1e-09   | length of ramp   |
| VOLTAGE         | $V$   | double | 0.0     | full voltage   |
| GAP             | $M$   | double | 0.01    | gap between plates   |
| TIME_OFFSET     | $S$   | double | 0.0     | time offset of ramp start  |
| N_SECTIONS      |       | long   | 10      | number of sections   |
| PHASE_REFERENCE |       | long   | 0       | phase reference number (to link with other time-dependent elements)  |
| DX              | $M$   | double | 0.0     | misalignment   |
| DY              | $M$   | double | 0.0     | misalignment   |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## ROTATE

### 10.89 ROTATE—An element that rotates the beam about the longitudinal axis.

An element that rotates the beam about the longitudinal axis.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis   |
| EXCLUDE_FLOOR  |            | short  | 0       | if non-zero, does not affect the floor coordinates   |
| EXCLUDE_OPTICS |            | short  | 0       | if non-zero, does not affect the optics (i.e., transfer matrix is unit matrix)   |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The sign convention for the TILT parameter is confusing on this element. In particular, a positive TILT rotates the beam counter-clockwise about the longitudinal axis. This is the opposite sense to rotations of elements, where a positive TILT rotates the element clockwise about the longitudinal axis.

Hence, if one wanted to rotate a series of elements by 0.1 rad, one could do the following:

```
ROT1: ROTATE,TILT=0.1
ROT2: ROTATE,TILT=-0.1
BL: line=(ROT1,...,ROT2)
```

The TILT value for ROT1 is the same (including the sign) as the individual TILT values one would give to all the elements represented by ....

## SAMPLE

### 10.90 SAMPLE—An element that reduces the number of particles in the beam by interval-based or random sampling.

An element that reduces the number of particles in the beam by interval-based or random sampling.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| FRACTION       |       | double | 1       | fraction to keep   |
| INTERVAL       |       | long   | 1       | interval between sampled particles   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## SBEN

### 10.91 SBEN—A sector dipole implemented as a matrix, up to 2nd order. Use CSBEND for symplectic tracking.

A sector dipole implemented as a matrix, up to 2nd order. Use CSBEND for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default | Description   |
|----------------|---------|--------|---------|---|
| L              | $M$     | double | 0.0     | arc length  |
| ANGLE          | $RAD$   | double | 0.0     | bend angle  |
| K1             | $1/M^2$ | double | 0.0     | geometric focusing strength                           |
| E1             | $RAD$   | double | 0.0     | entrance edge angle                                   |
| E2             | $RAD$   | double | 0.0     | exit edge angle                                       |
| TILT           | $RAD$   | double | 0.0     | rotation about incoming longitudinal axis             |
| K2             | $1/M^3$ | double | 0.0     | geometric sextupole strength                          |
| H1             | $1/M$   | double | 0.0     | entrance pole-face curvature                          |
| H2             | $1/M$   | double | 0.0     | exit pole-face curvature                              |
| HGAP           | $M$     | double | 0.0     | half-gap between poles                                |
| FINT           |         | double | 0.5     | edge-field integral                                   |
| DX             | $M$     | double | 0.0     | misalignment of entrance                              |
| DY             | $M$     | double | 0.0     | misalignment of entrance                              |
| DZ             | $M$     | double | 0.0     | misalignment of entrance                              |
| FSE            |         | double | 0.0     | fractional strength error of all components           |
| FSE_DIPOLE     |         | double | 0.0     | fractional strength error of dipole component         |
| FSE_QUADRUPOLE |         | double | 0.0     | fractional strength error of quadrupole component     |
| ETILT          | $RAD$   | double | 0.0     | error rotation about incoming longitudinal axis       |
| EDGE1_EFFECTS  |         | short  | 1       | include entrance edge effects?                        |
| EDGE2_EFFECTS  |         | short  | 1       | include exit edge effects?                            |
| ORDER          |         | short  | 0       | matrix order  |
| EDGE_ORDER     |         | short  | 0       | edge matrix order                                     |
| TRANSPORT      |         | short  | 0       | use (incorrect) TRANSPORT equations for T436 of edge? |
| USE_BN         |         | short  | 0       | use B1 and B2 instead of K1 and K2 values?            |
| B1             | $1/M$   | double | 0.0     | $K1 = B1/\rho$ , where $\rho$ is bend radius          |



## SBEN continued

A sector dipole implemented as a matrix, up to 2nd order. Use CSBEND for symplectic tracking.

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| B2             | $1/M^2$ | double | 0.0     | $K2 = B2/\rho$   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Some confusion may exist about the edge angles, particularly the signs. For a sector magnet, we have of course  $E1=E2=0$ . For a symmetric rectangular magnet,  $E1=E2=ANGLE/2$ . If  $ANGLE$  is negative, then so are  $E1$  and  $E2$ . To understand this, imagine a rectangular magnet with positive  $ANGLE$ . If the magnet is flipped over, then  $ANGLE$  becomes negative, as does the bending radius  $\rho$ . Hence, to keep the focal length of the edge  $1/f = -\tan E_i/\rho$  constant, we must also change the sign of  $E_i$ .

When adding errors, care should be taken to choose the right parameters. The **FSE** and **ETILT** parameters are used for assigning errors to the strength and alignment relative to the ideal values given by  $ANGLE$  and  $TILT$ . One can also assign errors to  $ANGLE$  and  $TILT$ , but this has a different meaning: in this case, one is assigning errors to the survey itself. The reference beam path changes, so there is no orbit/trajectory error. The most common thing is to assign errors to **FSE** and **ETILT**. Note that when adding errors to **FSE**, the error is assumed to come from the power supply, which means that multipole strengths also change.

*Special note about splitting dipoles:* when dipoles are long, it is common to want to split them into several pieces, to get a better look at the interior optics. When doing this, care must be exercised not to change the optics. **elegant** has some special features that are designed to reduce or manage potential problems. At issue is the need to turn off edge effects between the portions of the same dipole.

First, one can simply use the **divide\_elements** command to set up the splitting. Using this command, **elegant** takes care of everything.

Second, one can use a series of dipoles *with the same name*. In this case, **elegant** automatically turns off interior edge effects. This is true when the dipole elements directly follow one another or are separated by a **MARK** element.

Third, one can use a series of dipoles with different names. In this case, you must also use the **EDGE1\_EFFECTS** and **EDGE2\_EFFECTS** parameters to turn off interior edge effects.

## SCATTER

### 10.92 SCATTER—A scattering element to add gaussian random numbers to particle coordinates.

A scattering element to add gaussian random numbers to particle coordinates.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| X              | $M$   | double | 0.0     | rms scattering level for x   |
| XP             |       | double | 0.0     | rms scattering level for x'  |
| Y              | $M$   | double | 0.0     | rms scattering level for y   |
| YP             |       | double | 0.0     | rms scattering level for y'  |
| DP             |       | double | 0.0     | rms scattering level for (p-pCentral)/pCentral   |
| PROBABILITY    |       | double | 1       | Probability that any particle will be selected for scattering.   |
| STARTONPASS    |       | long   | 0       | Pass number to start on.   |
| ENDONPASS      |       | long   | -1      | Pass number to end on (inclusive). Ignored if negative.  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## SCMULT

### 10.93 SCSMULT—Tracks through a zero length multipole to simulate space charge effects

Tracks through a zero length multipole to simulate space charge effects

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

Important notes:

- This element is not designed for space charge calculations in guns or linacs. It is only intended for simulating space charge in rings.
- If inserting SCSMULT elements using `insert_sceffects`, see the manual page for `insert_sceffects` for other caveats and pitfalls.

This element simulates transverse space charge (SC) kicks using K.Y. Ng's formula [24].

The linear SC force is given by:

$$\begin{aligned}\Delta x' &= \frac{K_{sc} L e^{-z^2/(2\sigma_z^2)}}{\sqrt{2\pi}\sigma_z} \frac{x}{\sigma_x(\sigma_x + \sigma_y)} \\ \Delta y' &= \frac{K_{sc} L e^{-z^2/(2\sigma_z^2)}}{\sqrt{2\pi}\sigma_z} \frac{y}{\sigma_y(\sigma_x + \sigma_y)}\end{aligned}\quad (147)$$

where  $K_{sc} = \frac{2Nr_e}{\gamma^3\beta^2}$ ,  $L$  is the integrating length,  $\sigma_{x,y,z}$  are rms beam size.

The non-linear SC force is given by:

$$\begin{aligned}\Delta x' &= \frac{K_{sc} L e^{-z^2/(2\sigma_z^2)}}{2\sigma_z \sqrt{\sigma_x^2 - \sigma_y^2}} \text{Im} \left[ w \left( \frac{x + iy}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) - e^{-\frac{x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2}} w \left( \frac{x \frac{\sigma_y}{\sigma_x} + iy \frac{\sigma_x}{\sigma_y}}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) \right] \\ \Delta y' &= \frac{K_{sc} L e^{-z^2/(2\sigma_z^2)}}{2\sigma_z \sqrt{\sigma_x^2 - \sigma_y^2}} \text{Re} \left[ w \left( \frac{x + iy}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) - e^{-\frac{x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2}} w \left( \frac{x \frac{\sigma_y}{\sigma_x} + iy \frac{\sigma_x}{\sigma_y}}{\sqrt{2(\sigma_x^2 - \sigma_y^2)}} \right) \right]\end{aligned}\quad (148)$$

where  $w(z)$  is the complex error function

$$w(z) = e^{-z^2} \left[ 1 + \frac{2i}{\sqrt{\pi}} \int_0^z e^{\zeta^2} d\zeta \right] \quad (149)$$

Equation 148 appear to diverge when  $\sigma_x = \sigma_y$ . In fact, this is not true, because the expressions inside the square brackets will provide zero too at  $\sigma_x = \sigma_y$  to cancel the poles outside. In our code, we calculate this equation at  $1.01\sigma_x$  and  $0.99\sigma_x$ , and average the total effects.

To invoke the calculation, one must use set up command “insert\_sceffects” proceed “run\_setup” and “Twiss\_output” command proceed “track”.

## SCRAPER

**10.94 SCRAPER**—A collimating element that sticks into the beam from one side only. The directions 0, 1, 2, and 3 are from +x, +y, -x, and -y, respectively.

A collimating element that sticks into the beam from one side only. The directions 0, 1, 2, and 3 are from +x, +y, -x, and -y, respectively.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name         | Units    | Type   | Default | Description  |
|------------------------|----------|--------|---------|--|
| L                      | $M$      | double | 0.0     | length   |
| XO                     | $M$      | double | 0.0     | radiation length   |
| ENERGY_DECAY           |          | long   | 0       | If nonzero, then particles will lose energy due to material using a simple exponential model.  |
| ENERGY_STRAGGLE        |          | long   | 0       | Use simple-minded energy straggling model coupled with ENERGY_DECAY=1?   |
| NUCLEAR_BREMSSTRAHLUNG |          | long   | 0       | Model energy loss to nuclear bremsstrahlung? If enabled, set ENERGY_DECAY=0 to disable simpler model.  |
| ELECTRON_RECOIL        |          | long   | 0       | If non-zero, electron recoil during Coulomb scattering is included (results in energy change).   |
| Z                      |          | long   | 0       | Atomic number  |
| A                      | $AMU$    | double | 0.0     | Atomic mass  |
| RHO                    | $KG/M^3$ | double | 0.0     | Density  |
| PLIMIT                 |          | double | 0.05    | Probability cutoff for each slice  |
| POSITION               | $M$      | double | 0.0     | position of edge   |
| DX                     | $M$      | double | 0.0     | misalignment   |
| DY                     | $M$      | double | 0.0     | misalignment   |
| INSERT_FROM            |          | STRING | NULL    | direction from which inserted (+x, -x, x, +y, -y, y)   |
| DIRECTION              |          | long   | -1      | Deprecated. use INSERT_FROM.   |
| GROUP                  |          | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The method used for material modeling is the same as that used for the **MATTER** element.

The **DIRECTION** parameter is deprecated and the more versatile **INSERT\_FROM** parameter should be used instead. The values for the latter determine from which side the scraper is inserted. E.g., **INSERT\_FROM="-x", POSITION=0.005** means the scraper is inserted from the negative x side and extends from  $x = -\infty$  to  $x = 0.005m$ .

**INSERT\_FROM="x"** or **INSERT\_FROM="y"** means the scraper is inserted from both sides, in which case the interpretation of the position is different. E.g., **INSERT\_FROM="x", POSITION=0.005** means that only the region  $x : [-0.005, 0.005]m$  is clear.

## SCRIPT

### 10.95 SCRIPT—An element that allows transforming the beam using an external script.

An element that allows transforming the beam using an external script.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| L              | $M$   | double | 0.0     | Length to be used for matrix-based operations such as twiss parameter computation.  |
| COMMAND        |       | STRING | NULL    | SDDS-compliant command to apply to the beam. Use the sequence %i to represent the input filename and %o to represent the output filename. |
| USE_CSH        |       | short  | 1       | Use C-shell for execution (may be slower)?  |
| VERBOSITY      |       | short  | 0       | Set the verbosity level.  |
| RPN_PARAMETERS |       | short  | 0       | If nonzero, then parameters from the script output file are loaded into RPN variables.  |
| START_PASS     |       | long   | -1      | Start script action on this pass. Before that, behaves like a drift space.  |
| END_PASS       |       | long   | -1      | End script action after this pass. Before that, behaves like a drift space.   |
| PASS_INTERVAL  |       | long   | -1      | Execute script only every Nth pass following START_PASS, including START_PASS. Otherwise, behaves like a drift space.                     |
| ON_PASS        |       | long   | -1      | Perform script action only on this pass, overriding other pass controls. Other than that, behaves like a drift space.                     |
| DIRECTORY      |       | STRING | NULL    | Directory in which to place input and output files. If blank, the present working directory is used.                                      |
| ROOTNAME       |       | STRING | NULL    | Rootname for use in naming input and output files. %s may be used to represent the run rootname.  |

## SCRIPT continued

An element that allows transforming the beam using an external script.

| Parameter Name            | Units | Type   | Default | Description   |
|---------------------------|-------|--------|---------|---|
| INPUT_EXTENSION           |       | STRING | in      | Extension for the script input file.  |
| OUTPUT_EXTENSION          |       | STRING | out     | Extension for the script output file.   |
| KEEP_FILES                |       | short  | 0       | If nonzero, then script input and output files are not deleted after use. By default, they are deleted.                               |
| DRIFT_MATRIX              |       | short  | 0       | If nonzero, then for non-tracking calculations the element is treated as a drift space.   |
| USE_PARTICLE_ID           |       | short  | 1       | If nonzero, then the output file will supply particle IDs. Otherwise, particles are renumbered.                                       |
| NO_NEW_PARTICLES          |       | short  | 1       | If nonzero, then no new particles will be added in the script output file.  |
| DETERMINE_LOSSES_FROM_PID |       | short  | 1       | If nonzero and if USE_PARTICLE_ID is nonzero, then particleID data from script output is used to determine which particles were lost. |
| SOFT_FAILURE              |       | short  | 1       | If output file does not exist or can't be read, consider all particles lost.  |
| NP0                       |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np0   |
| NP1                       |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np1   |
| NP2                       |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np2   |



## SCRIPT continued

An element that allows transforming the beam using an external script.

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| NP3            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np3 |
| NP4            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np4 |
| NP5            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np5 |
| NP6            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np6 |
| NP7            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np7 |
| NP8            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np8 |
| NP9            |       | double | 0.0     | User-defined numerical parameter for command substitution for sequence %np9 |
| SP0            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp0    |
| SP1            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp1    |
| SP2            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp2    |
| SP3            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp3    |
| SP4            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp4    |

## SCRIPT continued

An element that allows transforming the beam using an external script.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| SP5            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp5   |
| SP6            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp6   |
| SP7            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp7   |
| SP8            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp8   |
| SP9            |       | STRING | NULL    | User-defined string parameter for command substitution for sequence %sp9   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows expanding **elegant** by using external scripts (or programs) as elements in a beamline. Here are requirements for the script:

- It must be executable from the commandline.
- It must read the initial particle distribution from an SDDS file. This file will have the usual columns that an **elegant** phase-space output file has, along with the parameter **Charge** giving the beam charge in Coulombs. The file will contain a single data page.
- It must write the final particle distribution to an SDDS file. This file should have all of the columns and parameters that appear in the initial distribution file. Additional columns and parameters will be ignored, as will all pages but the first.
- The **Charge** parameter in the file is used to determine the total beam charge; the script must ensure that this parameter is set correctly; when particles are lost or created, simply copying or retaining the value from the input file will not be correct. Normally, the charge per particle is constant in simulations. Hence, if **elegant** sees a change in charge per particle after the **SCRIPT** element, it issues a warning.

The **SCRIPT** element works best if the script accepts commandline arguments. In this case, the **COMMAND** parameter is used to provide a template for creating a command to run the script. The **COMMAND** string may contain the following substitutable fields:

1. `%i` — Will be replaced by the name of the input file to the script. (**elegant** writes the initial particle distribution to this file.)
2. `%o` — Will be replaced by the name of the output file from the script. (**elegant** expects the script to write the final particle distribution to this file.)
3. `%p` — Will be replaced by the pass number, which starts from 0.
4. `%np0, %np1, ..., %np9` — Will be replaced by the value of Numerical Parameter 0, 1, ..., 9. This can be used to pass to the script values that are parameters of the element definition. For example, if one wanted to vary parameters or add errors to the parameter, one would use this facility.
5. `%sp0, %sp1, ..., %sp9` — Will be replaced by the value of String Parameter 0, 1, ..., 9. This can be used to pass to the script values that are parameters of the element definition.

In some cases, one may wish to keep the input file delivered to the **SCRIPT** as well as the output file returned by it. This is facilitated by using the **ROOTNAME** parameter, which allows specifying the rootname for these files, as well as the **INPUT\_EXTENSION** and **OUTPUT\_EXTENSION** parameters. The **ROOTNAME** parameter may contain a simple string, but may also contain several sustainable fields:

- `%s` — The global rootname, which may be given by the **rootname** parameter in the **run\_setup** command.
- `%p` — The pass index.
- `%ld` — The occurrence number of the element.

Here's an example of a **SCRIPT COMMAND**:

```
myScript -input %i -output %o -accuracy %np0 -type %sp0
```

In this example, the script **myScript** takes four commandline arguments, giving the names of the input and output files, an accuracy requirement, and a type specifier. By default, **elegant** will choose unique, temporary filenames to use in communicating with the script. The actual command when executed might be something like

```
myScript -input tmp391929.1 -output tmp391929.2 -accuracy 1.5e-6 -type scraper
```

where for this example I've assumed **NP0=1.5e-6** and **SP0='scraper'**.

If you have a program (e.g., a FORTRAN program) that does not accept commandline arguments, you can easily wrap it in a Tcl/Tk simple script to handle this. Alternatively, you can force **elegant** to use specified files for communicating with such a script. This is done using the **ROOTNAME**, **INPUT\_EXTENSION**, and **OUTPUT\_EXTENSION** parameters. So if your program was **crass** and it expected its input (output) in files **crass.in** (**crass.out**), then you'd use

```
S1: script,command='crass',rootname='crass',input_extension='in',&
output_extension='out'
```

For purposes of computing concatenated transport matrices, Twiss parameters, response matrices, etc., **elegant** will perform initial tracking through the **SCRIPT** element using an ensemble of 25 particles. If this is not desirable, then set the parameter **DRIFT\_MATRIX** to a non-zero value. This will force **elegant** to treat the element as a drift space for any calculations that involve transport

matrices. Examples of where one might want to use this feature would be a **SCRIPT** that involves randomization (e.g., scattering), particle loss, or particle creation.

If non-zero, the **RPN\_PARAMETERS** parameter directs **elegant** to load all numerical SDDS parameter values from the script output file into **rpn** variables, where they may be used for optimization. This provides the user the ability to perform script-based analysis of particle distributions and then optimize the results of that analysis. (Typically in this case the script does not actually transform the particle coordinates, but simply copies them from the input file to the output file.) The names of the variables are of the form *ElementName#N.ParameterName*, where *N* is the occurrence number of the script element (usually 1 if there is only one instance).

## SEXT

### 10.96 SEXT—A sextupole implemented as a matrix, up to 3rd order. Use KSEXT for symplectic tracking.

A sextupole implemented as a matrix, up to 3rd order. Use KSEXT for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| K2             | $1/M^3$ | double | 0.0     | geometric strength   |
| K1             | $1/M^2$ | double | 0.0     | geometric quadrupole strength error. See notes below!  |
| J1             | $1/M^2$ | double | 0.0     | geometric skew quadrupole strength error. See notes below!   |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| DX             | $M$     | double | 0.0     | misalignment   |
| DY             | $M$     | double | 0.0     | misalignment   |
| DZ             | $M$     | double | 0.0     | misalignment   |
| FSE            |         | double | 0.0     | fractional strength error  |
| FFRINGE        |         | double | 0.0     | Length occupied by linear fringe regions as fraction hard-edge length L.   |
| ORDER          |         | short  | 0       | matrix order   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a sextupole using a matrix, up to third order.

The K1 and J1 parameters allow introducing normal and skew quadrupole **error** terms. The matrix expressions assume that these are weak effects and high accuracy should not be expected if this is not true. If K1 is significant, then use of the KQUSE element is preferred.

## SHRFDF

### 10.97 SHRFDF—Simulation through space harmonics of zero length deflecting cavity.

Simulation through space harmonics of zero length deflecting cavity.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| FACTOR         |            | double | 1       | A factor by which to multiply all components.          |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis                       |
| PERIOD_LENGTH  | <i>M</i>   | double | 0.0     | cavity period length, or cell length                   |
| PERIOD_PHASE   | <i>RAD</i> | double | 0.0     | cavity period phase advance, or so-called working mode |
| V0             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=0                |
| V1             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=1                |
| V2             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=2                |
| V3             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=3                |
| V4             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=4                |
| V5             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=5                |
| V6             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=6                |
| V7             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=7                |
| V8             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=8                |
| V9             | <i>V</i>   | double | 0.0     | effective voltage of space harmonic n=9                |
| PHASE0         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=0                            |
| PHASE1         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=1                            |
| PHASE2         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=2                            |
| PHASE3         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=3                            |
| PHASE4         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=4                            |
| PHASE5         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=5                            |
| PHASE6         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=6                            |
| PHASE7         | <i>HZ</i>  | double | 0.0     | Phase of space harmonic n=7                            |

## SHRFDF continued

Simulation through space harmonics of zero length deflecting cavity.

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| PHASE8          | $HZ$  | double | 0.0     | Phase of space harmonic n=8  |
| PHASE9          | $HZ$  | double | 0.0     | Phase of space harmonic n=9  |
| PHASE_REFERENCE |       | long   | 0       | phase reference number<br>(to link with other time-dependent elements)   |
| GROUP           |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates an rf deflector with specified space harmonic parameters (voltage, phase). The thin kicks from the fundamental deflecting mode are the same as for the element RFDF. The thin kicks from the space harmonics ( $n \geq 1$ ) are [55]

$$\begin{aligned}\Delta P_x &= -\frac{\partial(\mathbf{H}-H_0)}{\partial x} \\ &= \sum_{n=1}^{\infty} -q\bar{V}_n \cdot \sin(k_n z + \phi_n) \cdot \left(\frac{1}{2}\alpha_n + \frac{1}{16}\alpha_n^3 \cdot (3x^2 + y^2)\right)\end{aligned}\tag{150}$$

$$\begin{aligned}\Delta P_z &= -\frac{\partial(\mathbf{H}-H_0)}{\partial z} \\ &= \sum_{n=1}^{\infty} -q\bar{V}_n \cdot k_n \cdot \cos(k_n z + \phi_n) \cdot \left(\frac{1}{2}\alpha_n \cdot x + \frac{1}{16}\alpha_n^3 \cdot (x^2 + y^2) \cdot x\right)\end{aligned}\tag{151}$$

The wave numbers  $k_n$  and  $\alpha_n$  are listed below.

$$k_n = \frac{\varphi_0 + 2\pi n}{d}\tag{152}$$

$$\alpha_n^2 + k_n^2 = k_0^2\tag{153}$$

where  $k_n$  is wave number of  $n^{th}$  space harmonic,  $n$  an integer number,  $\varphi_0$  the phase advance per cavity period,  $d$  the cavity period length,  $\alpha_n$  the wave number in the radial direction,  $m$  wave number (per  $2\pi$ ) in the angular direction.

## SLICE

### 10.98 SLICE—Performs slice-by-slice analysis of the beam for output to a file.

Performs slice-by-slice analysis of the beam for output to a file.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| N_SLICES            |       | long   | 10      | number of slices   |
| START_PID           |       | long   | -1      | starting particleID for particles to dump  |
| END_PID             |       | long   | -1      | ending particleID for particles to dump  |
| INTERVAL            |       | long   | 1       | interval for data output (in turns)  |
| START_PASS          |       | long   | 0       | pass on which to start   |
| END_PASS            |       | long   | -1      | pass on which to end (inclusive). Ignored if negative.   |
| FILENAME            |       | STRING |         | output filename, possibly incomplete (see below)   |
| LABEL               |       | STRING |         | output label   |
| INDEX_OFFSET        |       | long   | 0       | Offset for file indices for sequential file naming.  |
| REFERENCE_FREQUENCY |       | double | -1      | If non-zero, the indicated frequency is used to define the bucket center for purposes of computing time offsets.   |
| DISABLE             |       | short  | 0       | If nonzero, no output will be generated.   |
| USE_DISCONNECT      |       | short  | 0       | If nonzero, files are disconnected between each write operation. May be useful for parallel operation. Ignored otherwise.                                  |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

NB: This element has very poor parallel efficiency. Hence, the **START\_PASS**, **END\_PASS**, and **INTERVAL** options should be used to limit the frequency of computations to the minimum needed.



## SOLE

### 10.99 SOLE—A solenoid implemented as a matrix, up to 2nd order.

A solenoid implemented as a matrix, up to 2nd order.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| KS             | $RAD/M$ | double | 0.0     | geometric strength, -<br>Bs/(B*Rho)  |
| B              | $T$     | double | 0.0     | field strength (used if KS is zero)  |
| DX             | $M$     | double | 0.0     | misalignment   |
| DY             | $M$     | double | 0.0     | misalignment   |
| DZ             | $M$     | double | 0.0     | misalignment   |
| ORDER          |         | short  | 0       | matrix order   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## SPEEDBUMP

### 10.100 SPEEDBUMP—Simulates a semi-circular protuberance from one or both walls of the chamber.

Simulates a semi-circular protuberance from one or both walls of the chamber.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | insertion length   |
| CHORD          | $M$   | double | 0.0     | z length of speed bump   |
| DZCENTER       | $M$   | double | 0.0     | z center displacement of speed bump relative to middle of object   |
| HEIGHT         | $M$   | double | 0.0     | height above the surrounding chamber   |
| POSITION       | $M$   | double | 0.0     | position of peak relative to ideal trajectory  |
| DX             | $M$   | double | 0.0     | horizontal misalignment  |
| DY             | $M$   | double | 0.0     | vertical misalignment  |
| INSERT.FROM    |       | STRING | NULL    | direction from which inserted (x, +x, -x, y, +y, -y)   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a commonplace type of aperture restriction, consisting of a bump on one or both sides of a chamber. The parameters of the speedbump are illustrated in Fig. 4 It may be useful to know that the radius  $R$  of the cylinder from which the speedbump is made is

$$R = \frac{C^2 + 4h^2}{8h}, \quad (154)$$

where  $C$  is the chord length and  $h$  is the bump height. Solving for  $h$ , we have

$$h = R - \sqrt{R^2 - \left(\frac{C}{2}\right)^2}. \quad (155)$$

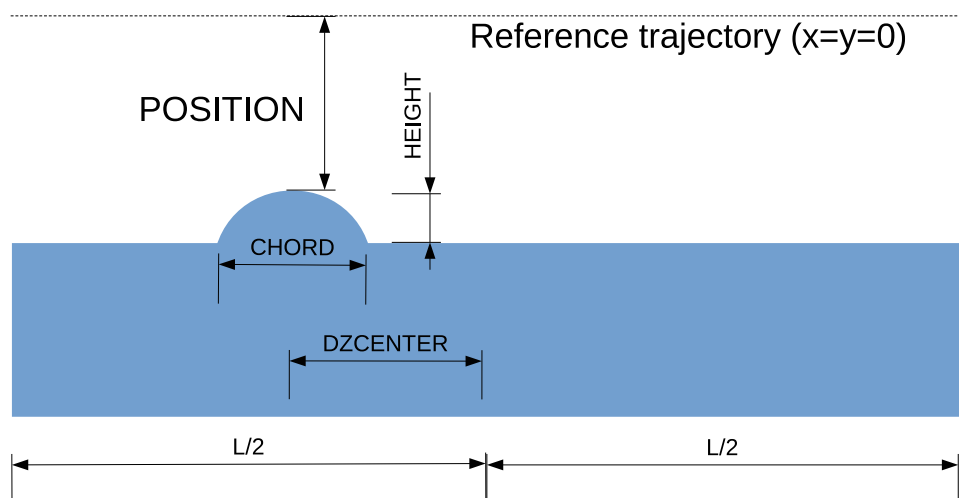


Figure 4: Illustration of the parameters used in specifying a speedbump.

## SREFFECTS

### 10.101 SREFFECTS—Lumped simulation of synchrotron radiation effects (damping and quantum excitation) for rings.

Lumped simulation of synchrotron radiation effects (damping and quantum excitation) for rings.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units   | Type   | Default | Description  |
|-----------------|---------|--------|---------|--|
| JX              |         | double | 1       | x damping partition number   |
| JY              |         | double | 1       | y damping partition number   |
| JDELTA          |         | double | 2       | momentum damping partition number  |
| EXREF           | $m$     | double | 0.0     | reference equilibrium x emittance  |
| EYREF           | $m$     | double | 0.0     | reference equilibrium y emittance  |
| SDELTAREF       |         | double | 0.0     | reference equilibrium fractional momentum spread   |
| DDELTAREF       |         | double | 0.0     | reference fractional momentum change per turn due to SR (negative value)   |
| PREF            | $m_e c$ | double | 0.0     | reference momentum (to which other reference values pertain)   |
| COUPLING        |         | double | 0.0     | x-y coupling   |
| FRACTION        |         | double | 1       | fraction of implied SR effect to simulate with each instance   |
| DAMPING         |         | long   | 1       | include damping, less rf effects?  |
| QEXCITATION     |         | long   | 1       | include quantum excitation?  |
| LOSSES          |         | long   | 1       | include average losses?  |
| CUTOFF          |         | double | 100     | cutoff (in sigmas) for gaussian random numbers   |
| INCLUDE_OFFSETS |         | long   | 1       | include orbit offsets in tracking (see below)?   |
| GROUP           |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is intended for storage ring modeling only and provides a fast alternative to element-by-element modeling of synchrotron radiation. It should be used with care because the

results will not necessarily be self-consistent. This is particularly an issue when there is dispersion at the location of the **SREFFECTS** element.

There are several types of storage ring simulation in which one may want to use this element:

- Simulation of instabilities or other dynamics where radiation damping or quantum excitation is important.
- Simulation of dynamics with an rf cavity when the synchronous phase is significantly different from 180 degrees, so that average radiation losses must be included.
- Computation of dynamic and momentum aperture in the presence of radiation damping.

The major parameters (**JX**, **JY**, **EXREF**, **SDELTAREF**, **DDELTAREF**, and **PREF**) can be supplied explicitly by the user, or filled in by **elegant** if the **twiss\_output** command is given with **radiation\_integrals=1**.

In explicit initialization, the user supplies the quantities **EXREF**, **EYREF**, **SDELTAREF**, **DDELTAREF**, and **PREF**. These are, respectively, the reference values for the x-plane emittance, y-plane emittance, fractional momentum spread, energy loss per turn, and momentum. The first four values pertain to the reference momentum. **JX**, **JY**, and **JDELTA** may also be given, although the defaults work for typical lattices.

In automatic initialization, the user turns on the radiation integral feature in **twiss\_output**, causing **elegant** to automatically compute the above quantities. This will occur only if **PREF=0**. The **COUPLING** parameter can be used to change the partitioning of quantum excitation between the horizontal and vertical planes. Because the radiation integrals computation in **twiss\_output** pertains to the horizontal plane only, the user must supply either **EYREF** or **COUPLING** if non-zero vertical emittance is desired.

The user may elect to turn off some aspects of the synchrotron radiation model. These should be changed from the default values with care!

- **DAMPING** — Default is 1. If set to 0, then no radiation damping effects will be included. More precisely, it is equivalent to setting **JX=JY=JDELTA=1**. Damping still occurs at any rf cavities (since **elegant** works in trace space).
- **QEXCITATION** — Default is 1. If set to 0, then no quantum excitation effects are included, which is to say that all particles will experience the same perturbation.
- **LOSSES** — Default is 1. If set to 0, no average energy losses are included.

*There are a number of caveats that must be observed when using this element.*

1. If there is dispersion at the location of the **SREFFECTS** element, the closed orbit will change because of the average momentum change, but it will disagree with tracking results. The reason is that in tracking **SREFFECTS** must displace the beam to the new equilibrium orbit, because otherwise there will be additional betatron motion excited and the wrong equilibrium emittance will be obtained. (Since the **SREFFECTS** element is already adding the betatron motion excitation for the entire ring, **elegant** is forced to offset each particle by  $\Delta\delta\vec{\eta}$  to suppress any additional excitation.)

This issue can be resolved by placing the **SREFFECTS** element next to the rf cavity and setting **INCLUDE\_OFFSETS=0**. Since the average momentum change is zero from the two elements, no additional betatron motion will be generated. Optionally, one can also use many **SREFFECTS** elements at equivalent locations in the lattice, which will decrease the magnitude of the effect.

2. When used for dynamic aperture and momentum aperture determination, one should set `QEXCITATION=0`. Putting the rf cavity (if any) right next to the `SREFFECTS` element is a good idea to avoid spurious excitation of betatron motion.
3. Nothing prevents including this element in a lattice when doing frequency map analysis, although it probably doesn't make any sense. Only the average energy loss per turn will be included. Again, putting an rf cavity right after `SREFFECTS` is a good idea.
4. In versions 19.0 and later, `elegant` includes the effect of `SREFFECTS` on the closed orbit. This presents a dilemma when automatic initialization is used, because in order to perform automatic initialization, `elegant` has to compute the optics functions. However, it must determine the closed orbit to compute the optics functions. The solution to this is for the user to pre-compute the twiss parameters and radiation integrals using `twiss_output` with `output_at_each_step=0`. The user is free to subsequently give `twiss_output` with `output_at_each_step=1` to obtain the results on the closed orbit.
5. Computation of Twiss parameters does not fully include the effects of synchrotron radiation losses when these are imposed using `SREFFECTS` elements. If `PREF=0` (automatic initialization), these effects are completely missing. If `PREF` is non-zero, then `elegant` will use the `DDELTAREF` parameter to compute the energy offset from the element, and thus its effect on the beam trajectory.

## STRAY

### 10.102 STRAY—A stray field element with local and global components. Global components are defined relative to the initial beamline direction.

A stray field element with local and global components. Global components are defined relative to the initial beamline direction.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| LBX            | $T$   | double | 0.0     | local Bx   |
| LBY            | $T$   | double | 0.0     | local By   |
| GBX            | $T$   | double | 0.0     | global Bx  |
| GBY            | $T$   | double | 0.0     | global By  |
| GBZ            | $T$   | double | 0.0     | global Bz  |
| ORDER          |       | long   | 0       | matrix order   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates stray fields. These fields are considered perturbations, in that they change the trajectory (or orbit), but not the floor coordinates. Local stray fields (LBX and LBY) are referenced to the local coordinate system. Global stray fields (GBX, GBY, GBZ) are referenced to the global coordinate system, which coincides with the local coordinate system only at the start of the beamline (unless there is no bending, in which case the two systems are identical).

## TAPERAPC

### 10.103 TAPERAPC—A tapered aperture that is a section of a circular cylinder.

A tapered aperture that is a section of a circular cylinder.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| RSTART         | <i>M</i>    | double | 0.0     | radius at the start  |
| REND           | <i>M</i>    | double | 0.0     | radius at the end  |
| DX             | <i>M</i>    | double | 0.0     | misalignment   |
| DY             | <i>M</i>    | double | 0.0     | misalignment   |
| STICKY         | <i>NULL</i> | short  | 0       | final aperture holds downstream until next TAPERAPC, TAPERAPE, TAPERAPR, or MAXAMP   |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |



## TAPERAPE

### 10.104 TAPERAPE—A tapered elliptical aperture.

A tapered elliptical aperture.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| ASTART         | <i>M</i>    | double | 0.0     | horizontal semi-axis at the start  |
| AEND           | <i>M</i>    | double | 0.0     | horizontal semi-axis at the end  |
| BSTART         | <i>M</i>    | double | 0.0     | vertical semi-axis at the start  |
| BEND           | <i>M</i>    | double | 0.0     | vertical semi-axis at the end  |
| DX             | <i>M</i>    | double | 0.0     | misalignment   |
| DY             | <i>M</i>    | double | 0.0     | misalignment   |
| TILT           | <i>RAD</i>  | double | 0.0     | misalignment   |
| RESOLUTION     | <i>M</i>    | double | 1e-06   | z resolution of finding intersection   |
| XEXPONENT      | <i>NULL</i> | short  | 2       | super-elliptical exponent (even number)  |
| YEXPONENT      | <i>NULL</i> | short  | 2       | super-elliptical exponent (even number)  |
| STICKY         | <i>NULL</i> | short  | 0       | final aperture holds downstream until next TAPERAPC, TAPERAPE, TAPERAPR, or MAXAMP   |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TAPERAPR

### 10.105 TAPERAPR—A tapered rectangular aperture.

A tapered rectangular aperture.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units       | Type   | Default | Description  |
|----------------|-------------|--------|---------|--|
| L              | <i>M</i>    | double | 0.0     | length   |
| XSTART         | <i>M</i>    | double | 0.0     | horizontal half-aperture at the start  |
| XEND           | <i>M</i>    | double | 0.0     | horizontal half-aperture at the end  |
| YSTART         | <i>M</i>    | double | 0.0     | vertical half-aperture at the start  |
| YEND           | <i>M</i>    | double | 0.0     | vertical half-aperture at the end  |
| DX             | <i>M</i>    | double | 0.0     | misalignment   |
| DY             | <i>M</i>    | double | 0.0     | misalignment   |
| TILT           | <i>RAD</i>  | double | 0.0     | misalignment   |
| STICKY         | <i>NULL</i> | short  | 0       | final aperture holds downstream until next TAPER-APC, TAPER-APC, TAPER-APC, or MAXAMP  |
| GROUP          |             | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TFBDRIVER

### 10.106 TFBDRIVER—Driver for a turn-by-turn feedback loop

Driver for a turn-by-turn feedback loop

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description   |
|-----------------|-------|--------|---------|---|
| ID              |       | STRING | NULL    | System identifier   |
| STRENGTH        |       | double | 0.0     | Strength factor   |
| KICK_LIMIT      |       | double | 0.0     | Limit on applied kick, nominally in radians.  |
| FREQUENCY       | $Hz$  | double | 0.0     | Resonant frequency of the unloaded kicker cavity.   |
| DRIVE_FREQUENCY | $Hz$  | double | 0.0     | Drive frequency. If zero, defaults to resonant frequency of the loaded cavity.                                      |
| CLOCK_FREQUENCY | $Hz$  | double | 0.0     | Clock frequency used for timing of the changes to generator current. Typically the rf or bunch frequency is used.   |
| CLOCK_OFFSET    | $s$   | double | 0.0     | Offset of the generator current change relative to clock tick. Clock tick is nominally aligned to the bunch center. |
| PHASE           | $Deg$ | double | 0.0     | Phase of the applied voltage relative to the bunch center, with 0 being on-crest.x2                                 |
| RAOVERQ         | $Ohm$ | double | 0.0     | Shunt impedance, $R_a/Q = V^2 / (P * Q)$ .  |
| QLOADED         |       | double | 0.0     | Loaded Q of the cavity.   |
| OUTPUT_FILE     |       | STRING | NULL    | File for logging filter output and driver output  |
| DELAY           |       | long   | 0       | Delay (in turns)  |
| A0              |       | double | 1       | Filter coefficient  |
| A1              |       | double | 0.0     | Filter coefficient  |
| A2              |       | double | 0.0     | Filter coefficient  |
| A3              |       | double | 0.0     | Filter coefficient  |
| A4              |       | double | 0.0     | Filter coefficient  |
| A5              |       | double | 0.0     | Filter coefficient  |
| A6              |       | double | 0.0     | Filter coefficient  |
| A7              |       | double | 0.0     | Filter coefficient  |

## TFBDRIVER continued

Driver for a turn-by-turn feedback loop

| Parameter Name  | Units | Type   | Default | Description  |
|-----------------|-------|--------|---------|--|
| A8              |       | double | 0.0     | Filter coefficient   |
| A9              |       | double | 0.0     | Filter coefficient   |
| A10             |       | double | 0.0     | Filter coefficient   |
| A11             |       | double | 0.0     | Filter coefficient   |
| A12             |       | double | 0.0     | Filter coefficient   |
| A13             |       | double | 0.0     | Filter coefficient   |
| A14             |       | double | 0.0     | Filter coefficient   |
| A15             |       | double | 0.0     | Filter coefficient   |
| A16             |       | double | 0.0     | Filter coefficient   |
| A17             |       | double | 0.0     | Filter coefficient   |
| A18             |       | double | 0.0     | Filter coefficient   |
| A19             |       | double | 0.0     | Filter coefficient   |
| A20             |       | double | 0.0     | Filter coefficient   |
| A21             |       | double | 0.0     | Filter coefficient   |
| A22             |       | double | 0.0     | Filter coefficient   |
| A23             |       | double | 0.0     | Filter coefficient   |
| A24             |       | double | 0.0     | Filter coefficient   |
| A25             |       | double | 0.0     | Filter coefficient   |
| A26             |       | double | 0.0     | Filter coefficient   |
| A27             |       | double | 0.0     | Filter coefficient   |
| A28             |       | double | 0.0     | Filter coefficient   |
| A29             |       | double | 0.0     | Filter coefficient   |
| UPDATE_INTERVAL |       | long   | 0       | Interval in units of pickup update interval for sampling pickup data and updating filter output. |
| OUTPUT_INTERVAL |       | long   | 1024    | Number of samples to buffer between writing output file updates.                                 |
| START_PASS      |       | long   | -1      | If positive, first pass on which to drive beam.  |
| END_PASS        |       | long   | -1      | If positive, last pass on which to drive beam.   |
| LONGITUDINAL    |       | short  | 0       | If non-zero, kick is in the longitudinal plane. KICK_LIMIT is in fractional momentum deviation.  |

## TFBDRIVER continued

Driver for a turn-by-turn feedback loop

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| BUNCHED_BEAM_MODE |       | short  | 1       | If non-zero, run in bunched beam mode.   |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is used together with the TFBPICKUP element to simulate a digital turn-by-turn feedback system. Each TFBDRIVER element must have a unique identification string assigned to it using the ID parameter. The same identifier must be used on a TFBPICKUP element. This is the pickup from which the driver gets its signal. Each pickup may feed more than one driver, but a driver can use only one pickup.

A 30-term FIR filter can be defined using the A0 through A29 parameters. The output of the filter is simply  $\sum_{i=0}^{29} a_i P_i$ , where  $P_i$  is the pickup filter output from  $i * U$  turns ago, where  $U$  is the UPDATE\_INTERVAL value specified for the pickup. The output of the filter is optionally delayed by the number of update intervals given by the DELAY parameter.

To some extent, the DELAY is redundant. For example, the filter  $a_0 = 0, a_1 = 1$  with a delay of 0 is equivalent to  $a_0 = 1, a_1 = 0$  with a delay of 1. However, for long delays or delays combined with many-term filters, the DELAY feature must be used.

The output of the filter is multiplied by the STRENGTH parameter to get the kick to apply to the beam. The KICK\_LIMIT parameter provides a very basic way to simulate saturation of the kicker output.

The plane that the TFBDRIVER kicks is determined by the PLANE parameter on the corresponding TFBPICKUP element, and additionally by the LONGITUDINAL parameter, as described in Table 3

| TFBPICKUP<br>PLANE | TFBDRIVER<br>LONGITUDINAL | coordinate<br>kicked | note                               |
|--------------------|---------------------------|----------------------|------------------------------------|
| x                  | 0                         | $x'$                 |                                    |
| x                  | 1                         | $\delta$             | pickup should have $\eta_x \neq 0$ |
| y                  | 0                         | $y'$                 |                                    |
| y                  | 1                         | $\delta$             | pickup should have $\eta_y \neq 0$ |
| delta              | 0                         | -                    | invalid                            |
| delta              | 1                         | $\delta$             |                                    |

Table 3: Correspondence between PLANE parameter of TFBPICKUP, LONGITUDINAL parameter of TFBDRIVER, and action of feedback loop.

Note: The OUTPUT\_FILE will produce a file with missing data at the end of the buffer if the OUTPUT\_INTERVAL parameter is not a divisor of the number of passes.

The FREQUENCY and PHASE parameters may be used to specify the resonant frequency of the driving cavity and its phase relative to the center of the bunch. If the frequency is not specified,

the kicker is assumed to kick all particles in a bunch by the same amount.

For longitudinal feedback only, a more sophisticated approach is available using a circuit model developed by T. Berenc (APS) may be employed to simulate driving the cavity resonance. To invoke this, the user must provide the loaded  $Q$  of the cavity using the **QLOADED** parameter, the  $(R_a/Q)$  using **RAOVERQ**, and the resonant frequency of the unloaded cavity using **FREQUENCY**. Optionally, the drive frequency may be specified using **DRIVE\_FREQUENCY**; it defaults to the unloaded resonant frequency.

Typically one should choose the resonant frequency to be  $(n \pm \frac{1}{4})f_b$ , where  $f_b$  is the bunch frequency and  $n$  is an integer. This will ensure that the kick to one bunch from the residual voltage from the previous bunch (both beam-loading and generator terms), is approximately minimized. Checking the **ResidualVoltage** column in the output file to confirm this is advised.

In addition to the resonant and drive frequencies, one must specify a clock frequency with **CLOCK\_FREQUENCY** and a clock offset with **CLOCK\_OFFSET**. The clock used to determine when the drive current changes, which happens at regular intervals. The clock offset is used to ensure that the change does not occur during passage of the bunch. If the clock offset is too small and the bunch length too long, this will happen and results in an error. The phase shift that results from the clock offset is automatically compensated.

Beam loading is not included in the model, but can be superimposed by inserting an **RFMODE** element with matching parameters.

See Section 7.2.14 of *Handbook of Accelerator Physics and Engineering* (Chao and Tigner, eds.) for a discussion of feedback systems.

## TFBPICKUP

### 10.107 TFBPICKUP—Pickup for a turn-by-turn feedback loop

Pickup for a turn-by-turn feedback loop

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default | Description   |
|-----------------|-------|--------|---------|---|
| ID              |       | STRING | NULL    | System identifier   |
| PLANE           |       | STRING | x       | "x", "y", "delta", or "phase"                                   |
| RMS_NOISE       | $M$   | double | 0.0     | RMS noise to add to position readings.                          |
| A0              |       | double | 0.0     | Filter coefficient  |
| A1              |       | double | 0.0     | Filter coefficient  |
| A2              |       | double | 0.0     | Filter coefficient  |
| A3              |       | double | 0.0     | Filter coefficient  |
| A4              |       | double | 0.0     | Filter coefficient  |
| A5              |       | double | 0.0     | Filter coefficient  |
| A6              |       | double | 0.0     | Filter coefficient  |
| A7              |       | double | 0.0     | Filter coefficient  |
| A8              |       | double | 0.0     | Filter coefficient  |
| A9              |       | double | 0.0     | Filter coefficient  |
| A10             |       | double | 0.0     | Filter coefficient  |
| A11             |       | double | 0.0     | Filter coefficient  |
| A12             |       | double | 0.0     | Filter coefficient  |
| A13             |       | double | 0.0     | Filter coefficient  |
| A14             |       | double | 0.0     | Filter coefficient  |
| A15             |       | double | 0.0     | Filter coefficient  |
| A16             |       | double | 0.0     | Filter coefficient  |
| A17             |       | double | 0.0     | Filter coefficient  |
| A18             |       | double | 0.0     | Filter coefficient  |
| A19             |       | double | 0.0     | Filter coefficient  |
| A20             |       | double | 0.0     | Filter coefficient  |
| A21             |       | double | 0.0     | Filter coefficient  |
| A22             |       | double | 0.0     | Filter coefficient  |
| A23             |       | double | 0.0     | Filter coefficient  |
| A24             |       | double | 0.0     | Filter coefficient  |
| A25             |       | double | 0.0     | Filter coefficient  |
| A26             |       | double | 0.0     | Filter coefficient  |
| A27             |       | double | 0.0     | Filter coefficient  |
| A28             |       | double | 0.0     | Filter coefficient  |
| A29             |       | double | 0.0     | Filter coefficient  |
| UPDATE_INTERVAL |       | long   | 0       | Interval in turns for sampling data and updating filter output. |

## TFBPICKUP continued

Pickup for a turn-by-turn feedback loop

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| START_PASS          |       | long   | -1      | If positive, first pass on which to perform computations.  |
| END_PASS            |       | long   | -1      | If positive, last pass on which to perform computations.   |
| REFERENCE_FREQUENCY |       | double | 0.0     | Reference frequency for computing phase offsets.   |
| DX                  | $M$   | double | 0.0     | Horizontal offset (subtracted from pickup signal).   |
| DY                  | $M$   | double | 0.0     | Vertical offset (subtracted from pickup signal)  |
| BUNCHED_BEAM_MODE   |       | short  | 1       | If non-zero, run in bunched beam mode.   |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element is used together with the TFBDRIVER element to simulate a digital turn-by-turn feedback system. Each TFBPICKUP element must have a unique identification string assigned to it using the ID parameter. This is used to identify which drivers get signals from the pickup.

A 30-term FIR filter can be defined using the A0 through A29 parameters. The input to the filter is the turn-by-turn beam centroid at the pickup location. The output of the filter is simply  $\sum_{i=0}^{29} a_i C_i$ , where  $C_i$  is the centroid from  $i * U$  turns ago, where  $U$  is the value specified by the UPDATE\_INTERVAL parameter. Note that  $\sum_{i=0}^{29} a_i$  should generally be zero. Otherwise, the system will attempt to correct the DC orbit. The output of the filter is the input to the driver element(s).

The PLANE parameter can take four values: “x”, “y”, “delta”, and “phase”, specifying what centroid property of the beam is measured by the pickup. The “delta”-mode pickup is nonphysical, but could have applications to simulations where is not convenient to put a pickup in a high-dispersion area.

See Section 7.2.14 of *Handbook of Accelerator Physics and Engineering* (Chao and Tigner, eds.) for a discussion of feedback systems.



# TMCF

## **10.108 TMCF—A numerically-integrated accelerating TM RF cavity with spatially-constant fields.**

A numerically-integrated accelerating TM RF cavity with spatially-constant fields.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| L               | $M$   | double | 0.0         | length   |
| FREQUENCY       | $HZ$  | double | 2856000000  | frequency  |
| PHASE           | $S$   | double | 0.0         | phase  |
| TIME_OFFSET     | $S$   | double | 0.0         | time offset (adds to phase)  |
| RADIAL_OFFSET   | $M$   | double | 1           | not recommended  |
| TILT            | $RAD$ | double | 0.0         | rotation about longitudinal axis   |
| ER              | $V$   | double | 0.0         | radial electric field  |
| BPHI            | $T$   | double | 0.0         | azimuthal magnetic field   |
| EZ              | $V$   | double | 0.0         | longitudinal electric field  |
| ACCURACY        |       | double | 0.0001      | integration accuracy   |
| X_MAX           | $M$   | double | 0.0         | x half-aperture  |
| Y_MAX           | $M$   | double | 0.0         | y half-aperture  |
| DX              | $M$   | double | 0.0         | misalignment   |
| DY              | $M$   | double | 0.0         | misalignment   |
| PHASE_REFERENCE |       | long   | 0           | phase reference number (to link with other time-dependent elements)  |
| N_STEPS         |       | long   | 100         | number of steps (for nonadaptive integration)  |
| METHOD          |       | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL        |       | STRING | t,median    | {t p},{median min max ave first light}<br>(e.g., "t,median")   |
| GROUP           |       | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TRCOUNT

### 10.109 TRCOUNT—An element that defines the point from which transmission calculations are made.

An element that defines the point from which transmission calculations are made.

Parallel capable? : no

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| DUMMY          |       | long   | 0       |  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TRFMODE

### 10.110 TRFMODE—A simulation of a beam-driven TM dipole mode of an RF cavity.

A simulation of a beam-driven TM dipole mode of an RF cavity.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name      | Units        | Type   | Default | Description  |
|---------------------|--------------|--------|---------|--|
| RA                  | $\Omega m/m$ | double | 0.0     | shunt impedance, $R_a = V^2/P$   |
| RS                  | $\Omega m/m$ | double | 0.0     | shunt impedance ( $R_s = R_a/2$ )  |
| Q                   |              | double | 0.0     | cavity Q   |
| FREQ                | $Hz$         | double | 0.0     | frequency  |
| CHARGE              | $C$          | double | 0.0     | beam charge (or use CHARGE element)  |
| BETA                |              | double | 0.0     | normalized load impedance  |
| BIN_SIZE            | $S$          | double | 0.0     | bin size for current histogram (use 0 for autosize)  |
| N_BINS              |              | long   | 20      | number of bins for current histogram   |
| INTERPOLATE         |              | long   | 0       | if non-zero, interpolate voltage within bins   |
| PLANE               |              | STRING | both    | x, y, or both  |
| SAMPLE_INTERVAL     |              | long   | 1       | passes between output to RECORD file   |
| PER_PARTICLE_OUTPUT |              | long   | 0       | If non-zero, then in BINLESS mode, provides per-particle output of RECORD data.                  |
| RECORD              |              | STRING | NULL    | output file for cavity data  |
| SINGLE_PASS         |              | long   | 0       | if nonzero, don't accumulate field from pass to pass   |
| RIGID_UNTIL_PASS    |              | long   | 0       | don't affect the beam until this pass  |
| DX                  | $M$          | double | 0.0     | misalignment   |
| DY                  | $M$          | double | 0.0     | misalignment   |
| XFACTOR             |              | double | 1       | factor by which to multiply shunt impedances   |
| YFACTOR             |              | double | 1       | factor by which to multiply shunt impedances   |
| RAMP_PASSES         |              | long   | 0       | Number of passes over which to linearly ramp up the impedance to full strength.                  |
| BINLESS             |              | long   | 0       | If nonzero, use algorithm that doesn't requiring binning. Best for few particles, widely spaced. |

## TRFMODE continued

A simulation of a beam-driven TM dipole mode of an RF cavity.

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| RESET_FOR_EACH_STEP |       | long   | 1       | If nonzero, voltage and phase are reset for each simulation step.  |
| LONG_RANGE_ONLY     |       | long   | 0       | If nonzero, induced voltage from present turn does not affect bunch. Short range wake should be included via TRWAKE or ZTRANSVERSE element.                |
| N_CAVITIES          |       | long   | 1       | effect is multiplied by this number, simulating N identical cavities   |
| BUNCHED_BEAM_MODE   |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a beam-driven dipole mode cavity using the fundamental theorem of beam loading and phasor rotation.

Normally, the field dumped in the cavity by one particle affects trailing particles in the same turn. However, if one is also using a TRWAKE or ZTRANSVSE element to simulate the short-range wake of the cavity, this would be double-counting. In that case, one can use LONG\_RANGE\_ONLY=1 to suppress the same-turn effects of the RFMODE element.

## TRWAKE

### 10.111 TRWAKE—Transverse wake specified as a function of time lag behind the particle.

Transverse wake specified as a function of time lag behind the particle.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name   | Units | Type   | Default | Description  |
|------------------|-------|--------|---------|--|
| INPUTFILE        |       | STRING | NULL    | name of file giving Green functions                    |
| TCOLUMN          |       | STRING | NULL    | column in INPUTFILE containing time data               |
| WXCOLUMN         |       | STRING | NULL    | column in INPUTFILE containing x Green function        |
| WYCOLUMN         |       | STRING | NULL    | column in INPUTFILE containing y Green function        |
| CHARGE           | $C$   | double | 0.0     | beam charge (or use CHARGE element)                    |
| FACTOR           |       | double | 1       | factor by which to multiply both wakes                 |
| XFACTOR          |       | double | 1       | factor by which to multiply x wake                     |
| YFACTOR          |       | double | 1       | factor by which to multiply y wake                     |
| N_BINS           |       | long   | 0       | number of bins for current histogram                   |
| INTERPOLATE      |       | long   | 0       | interpolate wake?                                      |
| SMOOTHING        |       | long   | 0       | Use Savitzky-Golay filter to smooth current histogram? |
| SG_HALFWIDTH     |       | long   | 4       | Savitzky-Golay filter half-width for smoothing         |
| SG_ORDER         |       | long   | 1       | Savitzky-Golay filter order for smoothing              |
| DX               | $M$   | double | 0.0     | misalignment   |
| DY               | $M$   | double | 0.0     | misalignment   |
| TILT             | $RAD$ | double | 0.0     | rotation about longitudinal axis                       |
| X_DRIVE_EXPONENT |       | long   | 1       | Exponent applied to x coordinates of drive particles   |
| Y_DRIVE_EXPONENT |       | long   | 1       | Exponent applied to y coordinates of drive particles   |
| X_PROBE_EXPONENT |       | long   | 0       | Exponent applied to x coordinates of probe particles   |
| Y_PROBE_EXPONENT |       | long   | 0       | Exponent applied to y coordinates of probe particles   |

## TRWAKE continued

Transverse wake specified as a function of time lag behind the particle.

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| RAMP_PASSES       |       | long   | 0       | Number of passes over which to linearly ramp up the wake to full strength.   |
| BUNCHED_BEAM_MODE |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| ACAUSAL_ALLOWED   |       | long   | 0       | If non-zero, then an acausal wake is allowed.  |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The input file for this element gives the transverse-wake Green functions,  $W_x(t)$  and  $W_y(t)$ , versus time behind the particle. The units of the wakes are V/C/m, so this element simulates the integrated wake of some structure (e.g., a cell or series of cells). If you have, for example, the wake for a cell and you need the wake for N cells, then you may use the **FACTOR** parameter to make the appropriate multiplication. The values of the time coordinate should begin at 0 and be equi-spaced, and be expressed in seconds. A positive value of time represents the distance behind the exciting particle. Time values must be equally spaced.

The sign convention for  $W_q$  ( $q$  being  $x$  or  $y$ ) is as follows: a particle with  $q > 0$  will impart a positive kick ( $\Delta q' > 0$ ) to a trailing particle following  $t$  seconds behind if  $W_q(t) > 0$ . A physical wake function should be zero at  $t = 0$  and also be initially positive as  $t$  increases from 0. Causality requires that  $W_q(t) = 0$  for  $t < 0$ . Acausal wakes are supported, provided the user sets **ACAUSAL\_ALLOWED=0**. The data file must contain a value of  $W(t)$  at  $t = 0$ , and should have equal spans of time to the negative and positive side of  $t = 0$ .

Use of the **CHARGE** parameter on the **TRWAKE** element is disparaged. It is preferred to use the **CHARGE** element as part of your beamline to define the charge.

Setting the **N\_BINS** parameter to 0 is recommended. This results in auto-scaling of the number of bins to accomodate the beam. The bin size is fixed by the spacing of the time points in the wake.

The default degree of smoothing (**SG\_HALFWIDTH=4**) may be excessive. It is suggested that users vary this parameter to verify that results are reliable if smoothing is employed (**SMOOTHING=1**).

The **XFACTOR** and **YFACTOR** parameters can be used to adjust the strength of the wakes if the location at which you place the **TRWAKE** element has different beta functions than the location at which the object that causes the wake actually resides.

The **X\_DRIVE\_EXPONENT** and **Y\_DRIVE\_EXPONENT** parameters can be used to change the dependence of the wake on the  $x$  and  $y$  coordinates, respectively, of the particles. Normally, these have the value 1, which corresponds to an ordinary dipole wake in a symmetric chamber.

If you have an asymmetric chamber, then you will have a transverse wake kick even if the beam is centered. (Of course, you'll need a 3-D wake code like GdfidL or MAFIA to compute this wake.) This part of the transverse wake is modeled by setting **X\_DRIVE\_EXPONENT=0** and

`Y_DRIVE_EXPONENT=0`. It will result in an orbit distortion, but conceivably could have other effects, such as emittance dilution. In this case, the units for the x and y wake must be  $V/C$ . A negative value of the wake corresponds to a kick toward negative x (or y).

In addition, a quadrupole wake can be modeled by setting `X_DRIVE_EXPONENT=0`, `Y_DRIVE_EXPONENT=0`, `X_PROBE_EXPONENT=1`, and `Y_PROBE_EXPONENT=1`. The kick to a particle now depends on *it's* displacement, not on the displacement of the leading particles. In this case, the units for the wakes must be  $V/C/m$ .

Bunched-mode application of the short-range wake is possible using specially-prepared input beams. See Section 6 for details. The use of bunched mode for any particular `TRWAKE` element is controlled using the `BUNCHED_BEAM_MODE` parameter

## TSCATTER

### 10.112 TSCATTER—An element to simulate Touschek scattering.

An element to simulate Touschek scattering.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| DUMMY          |       | long   | 0       |  |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |



## TUBEND

### 10.113 TUBEND—A special rectangular bend element for top-up backtracking.

A special rectangular bend element for top-up backtracking.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units      | Type   | Default | Description  |
|----------------|------------|--------|---------|--|
| L              | <i>M</i>   | double | 0.0     | arc length   |
| ANGLE          | <i>RAD</i> | double | 0.0     | bend angle   |
| FSE            |            | double | 0.0     | fractional strength error  |
| OFFSET         |            | double | 0.0     | horizontal offset of magnet center from arc center   |
| MAGNET_WIDTH   |            | double | 0.0     | horizontal width of the magnet pole  |
| MAGNET_ANGLE   |            | double | 0.0     | angle that the magnet was designed for   |
| GROUP          |            | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TWISS

### 10.114 TWISS—Sets Twiss parameter values.

Sets Twiss parameter values.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description   |
|----------------|-------|--------|---------|---|
| BETAX          | $M$   | double | 1       | horizontal beta function  |
| ALPHAX         |       | double | 0.0     | horizontal alpha function   |
| ETAX           | $M$   | double | 0.0     | horizontal eta function   |
| ETAXP          |       | double | 0.0     | slope of horizontal eta function  |
| BETAY          | $M$   | double | 1       | vertical beta function  |
| ALPHAY         |       | double | 0.0     | vertical alpha function   |
| ETAY           | $M$   | double | 0.0     | vertical eta function   |
| ETAYP          |       | double | 0.0     | slope of vertical eta function  |
| FROM_BEAM      |       | short  | 0       | compute transformation from tracked beam properties instead of Twiss parameters?      |
| FROM_0VALUES   |       | short  | 0       | if non-zero, transformation is from the "0" values provided in the element definition |
| COMPUTE_ONCE   |       | short  | 0       | compute transformation only for first beam or lattice functions?                      |
| APPLY_ONCE     |       | short  | 1       | apply correction only on first pass through for each beam?                            |
| VERBOSE        |       | short  | 0       | if non-zero, print extra information about transformations                            |
| DISABLE        |       | short  | 0       | if non-zero, element is ignored   |
| BETAX0         | $M$   | double | 1       | initial horizontal beta function (if FROM_0VALUES nonzero)                            |
| ALPHAX0        |       | double | 0.0     | initial horizontal alpha function (if FROM_0VALUES nonzero)                           |
| ETAX0          | $M$   | double | 0.0     | initial horizontal eta function (if FROM_0VALUES nonzero)                             |

## TWISS continued

Sets Twiss parameter values.

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| ETAXP0         |       | double | 0.0     | initial slope of horizontal eta function (if FROM_0VALUES nonzero)   |
| BETAY0         | $M$   | double | 1       | initial vertical beta function (if FROM_0VALUES nonzero)   |
| ALPHAY0        |       | double | 0.0     | initial vertical alpha function (if FROM_0VALUES nonzero)  |
| ETAY0          | $M$   | double | 0.0     | initial vertical eta function (if FROM_0VALUES nonzero)  |
| ETAYP0         |       | double | 0.0     | initial slope of vertical eta function (if FROM_0VALUES nonzero)   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows transformation of the twiss parameters of a beam with a first-order matrix. The matrix is computed in various ways based on initial and final twiss parameters. Depending on how you set it up, the final twiss parameters for your beam may not be the twiss parameters you specify.

The twiss parameter values BETAX, BETAY, etc. specified in the element definition specify the target values of the transformation. To completely specify the transformation, one must know the initial values as well.

### Lattice-Function-Based Transformation

If FROM\_BEAM is zero, which is the default, then the initial values are taken from the incoming lattice functions computed by `twiss_output`. This provides a way to transform the lattice functions between two parts of a transport line without designing intervening optics. A beam that is matched at the beginning of the transport line will remain matched. A beam that is mismatched at the beginning of the transport line *will not* be matched after the TWISS element.

By default, each time the twiss parameters are recomputed, the transformation is updated to maintain the desired lattice functions at the exit of the TWISS element. Setting COMPUTE\_ONCE to a non-zero value specifies that `elegant` should compute the transformation matrix only once, i.e., for the first set of computed lattice functions.

By default, the transformation is applied to the beam only the first time it passes the element. Setting APPLY\_ONCE to a zero will result in application of the transformation at each pass.

### Beam-Ellipse-Based Transformation

If FROM\_BEAM is non-zero, then the initial values for the transformation are computed from a beam. This provides a way to transform the beam ellipse to the desired twiss parameters irrespective of the lattice. The results from `twiss_output` will not necessarily be matched downstream of this

element. Only if the beam ellipse and lattice ellipse are the same will this occur.

By default, each time a new beam is generated, the transformation will be updated to maintain the desired beam ellipse at the exit of the `TWISS` element. Setting `COMPUTE_ONCE` to a non-zero value specifies that `elegant` should compute the transformation matrix only once, i.e., for the first beam it sees.

By default, the transformation is applied to the beam only the first time it passes the element. Setting `APPLY_ONCE` to a zero will result in application of the transformation at each pass. This would make sense, for example, if the `TWISS` element was filling in for a section of a ring. It wouldn't make sense if the `TWISS` element was being used to match the beam from a transport line to a ring.

## TWLA

### 10.115 TWLA—A numerically-integrated first-space-harmonic traveling-wave linear accelerator.

A numerically-integrated first-space-harmonic traveling-wave linear accelerator.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| L               | $M$   | double | 0.0         | length   |
| FREQUENCY       | $HZ$  | double | 2856000000  | frequency  |
| PHASE           | $RAD$ | double | 0.0         | phase  |
| TIME_OFFSET     | $S$   | double | 0.0         | time offset (adds to phase)  |
| EZ              | $V/M$ | double | 0.0         | electric field   |
| B_SOLENOID      | $T$   | double | 0.0         | solenoid field   |
| ACCURACY        |       | double | 0.0001      | integration accuracy   |
| X_MAX           | $M$   | double | 0.0         | x half-aperture  |
| Y_MAX           | $M$   | double | 0.0         | y half-aperture  |
| DX              | $M$   | double | 0.0         | misalignment   |
| DY              | $M$   | double | 0.0         | misalignment   |
| BETA_WAVE       |       | double | 1           | (phase velocity)/c   |
| ALPHA           | $1/M$ | double | 0.0         | field attenuation factor   |
| PHASE_REFERENCE |       | long   | 0           | phase reference number (to link with other time-dependent elements)  |
| N_STEPS         |       | long   | 100         | number of steps (for nonadaptive integration)  |
| FOCUSSING       |       | long   | 1           | include focusing effects?  |
| METHOD          |       | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL        |       | STRING | t,median    | {t p},{median min max ave first light} (e.g., "t,median")  |
| CHANGE_P0       |       | long   | 0           | does element change central momentum?  |
| SUM_BN2         |       | double | 0.0         | sum of squares of amplitudes of $n \neq 0$ space harmonics   |
| GROUP           |       | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TWMTA

### 10.116 TWMTA—A numerically-integrated traveling-wave muffin-tin accelerator.

A numerically-integrated traveling-wave muffin-tin accelerator.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| L               | $M$   | double | 0.0         | length   |
| FREQUENCY       | $HZ$  | double | 2856000000  | frequency  |
| PHASE           | $RAD$ | double | 0.0         | phase  |
| EZ              | $V/M$ | double | 0.0         | electric field   |
| ACCURACY        |       | double | 0.0001      | integration accuracy   |
| X_MAX           | $M$   | double | 0.0         | x half-aperture  |
| Y_MAX           | $M$   | double | 0.0         | y half-aperture  |
| DX              | $M$   | double | 0.0         | misalignment   |
| DY              | $M$   | double | 0.0         | misalignment   |
| KX              | $1/M$ | double | 0.0         | horizontal wave number   |
| BETA_WAVE       |       | double | 1           | (phase velocity)/c   |
| BSOL            |       | double | 0.0         | solenoid field   |
| ALPHA           | $1/M$ | double | 0.0         | field attenuation factor   |
| PHASE_REFERENCE |       | long   | 0           | phase reference number<br>(to link with other time-dependent elements)   |
| N_STEPS         |       | long   | 100         | number of kicks  |
| METHOD          |       | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL        |       | STRING | t,median    | {t p},{median min max ave first light}<br>(e.g., "t,median")   |
| GROUP           |       | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## TWPL

### 10.117 TWPL—A numerically-integrated traveling-wave stripline deflector.

A numerically-integrated traveling-wave stripline deflector.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name  | Units      | Type   | Default     | Description  |
|-----------------|------------|--------|-------------|--|
| L               | <i>M</i>   | double | 0.0         | length   |
| RAMP_TIME       | <i>S</i>   | double | 1e-09       | time to ramp to full strenth   |
| TIME_OFFSET     | <i>S</i>   | double | 0.0         | offset of ramp-start time  |
| VOLTAGE         | <i>V</i>   | double | 0.0         | maximum voltage between plates due to ramp   |
| GAP             | <i>M</i>   | double | 0.01        | gap between plates   |
| STATIC_VOLTAGE  | <i>V</i>   | double | 0.0         | static component of voltage  |
| TILT            | <i>RAD</i> | double | 0.0         | rotation about longitudinal axis   |
| ACCURACY        |            | double | 0.0001      | integration accuracy   |
| X_MAX           | <i>M</i>   | double | 0.0         | x half-aperture  |
| Y_MAX           | <i>M</i>   | double | 0.0         | y half-aperture  |
| DX              | <i>M</i>   | double | 0.0         | misalignment   |
| DY              | <i>M</i>   | double | 0.0         | misalignment   |
| PHASE_REFERENCE |            | long   | 0           | phase reference number (to link with other time-dependent elements)  |
| N_STEPS         |            | long   | 100         | number of steps (for nonadaptive integration)  |
| METHOD          |            | STRING | runge-kutta | integration method (runge-kutta, bulirsch-stoer, non-adaptive runge-kutta, modified midpoint)  |
| FIDUCIAL        |            | STRING | t,median    | {t p},{median min max ave first light}<br>(e.g., "t,median")   |
| GROUP           |            | string | NULL        | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## UKICKMAP

### 10.118 UKICKMAP—An undulator kick map (e.g., using data from RADIA).

An undulator kick map (e.g., using data from RADIA).

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes

| Parameter Name | Units      | Type   | Default | Description   |
|----------------|------------|--------|---------|---|
| L              | <i>M</i>   | double | 0.0     | length  |
| TILT           | <i>RAD</i> | double | 0.0     | rotation about longitudinal axis  |
| DX             | <i>M</i>   | double | 0.0     | misalignment  |
| DY             | <i>M</i>   | double | 0.0     | misalignment  |
| DZ             | <i>M</i>   | double | 0.0     | misalignment  |
| FIELD_FACTOR   |            | double | 1       | Factor by which to multiply the magnetic fields.  |
| XY_FACTOR      |            | double | 1       | Factor by which to multiply the x and y values in the input file.   |
| YAW            |            | double | 0.0     | Yaw angle of the device. Meaningful only if N_KICKS is not 1.   |
| INPUT_FILE     |            | STRING | NULL    | Name of SDDS file with undulator kickmap data.  |
| N_KICKS        |            | long   | 1       | Number of kicks into which to split the element.  |
| PERIODS        |            | long   | 0       | Number of periods (for radiation integral computations only).   |
| KREF           |            | double | 0.0     | Reference value of undulator parameter. $K=KREF*FIELD\_FACTOR$ is used for radiation integral calculations only assuming $period=L/PERIODS$ . |
| KACTUAL        |            | double | 0.0     | Value of undulator parameter, used for radiation integral calculations only assuming $period=L/PERIODS$ .                                     |
| SYNCH_RAD      |            | short  | 0       | include classical, single-particle synchrotron radiation?   |
| ISR            |            | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?  |



## UKICKMAP continued

An undulator kick map (e.g., using data from RADIA).

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| YAW_END           |       | short  | 0       | -1=Entrance, 0=Center, 1=Exit  |
| SINGLE_PERIOD_MAP |       | short  | 0       | if non-zero, the map file is for a single period. L still pertains to the full device. Set N_KICKS to the number of periods.                               |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element provides simulation of undulators using kick maps [27]. A script (`km2sdds`) is provided with the `elegant` distribution to translate RADIA [28] output into SDDS for use by `elegant`.

The input file has the following columns:

- **x** — Horizontal position in meters.
- **y** — Vertical position in meters.
- **xpFactor** — Horizontal kick factor  $C_x$  in  $T^2m^2$ . This factor is defined by equation (5a) in [27]. In particular,  $\Delta x' = C_x/H^2$ , where  $H$  is the beam rigidity in  $T^2m^2$ .
- **ypFactor** — Vertical kick factor  $C_y$  in  $T^2m^2$ . This factor is defined by equation (5b) in [27]. In particular,  $\Delta y' = C_y/H^2$ , where  $H$  is the beam rigidity in  $T^2m^2$ .

The values of **x** and **y** must be laid out on a grid of equispaced points. It is assumed that the data is ordered such that **x** varies fastest. This can be accomplished with the command

```
% sddsort -column=y,increasing -column=x,increasing input1.sdds input2.sdds
```

where `input1.sdds` is the original (unordered) file and `input2.sdds` is the new file, which would be used with UKICKMAP.

The data file is assumed to result from integration through a full device. If instead it results from integration through just a single period of a full device, one should set the `SINGLE_PERIOD_MAP` parameter to 1 and `N_KICKS` equal to the number of periods. (One can also use the `FIELD_FACTOR` parameter to get the same result, but this is confusing and is discouraged.)

`elegant` performs radiation integral computations for UKICKMAP and can also include radiation effects in tracking. This feature has limitations, namely, that the radiation integral computations assume the device is horizontally deflecting. However, in tracking, no such assumption is made. To obtain synchrotron radiation integral effects (e.g., in output from `twiss_output`), the `KREF` and `PERIODS` parameters must be given. Care must be taken when using the `FIELD_FACTOR` parameter

in this case, particularly if it is adjusted to account for using a single-period kickmap multiple times. To obtain synchrotron radiation effects in tracking, the `SYNCH_RAD` and/or `ISR` flags must additionally be used.

N.B.: at present this element is *not* included in beam moments computations via the `moments_output` command (the `CWIGGLER` element is an option for that).

The `YAW` and `YAW_END` parameters can be used in the simulation of canted IDs. Normally, steering magnets are used to create an angle between the devices. The devices are thus oriented in the reference coordinate system, meaning the beam tranverses the IDs at an angle. If it is desirable to align the IDs to the beam, the IDs can be yawed. A positive yaw will tilt the ID so that it is colinear with a beam that has been kicked by a positive horizontal steering angle. The `YAW_END` parameter defines which end of the ID is held fixed when the yaw is applied.

This element was requested by W. Guo (BNL), who also assisted with the implementation and debugging.

## VKICK

### 10.119 VKICK—A vertical steering dipole implemented as a matrix, up to 2nd order. Use EVKICK for symplectic tracking.

A vertical steering dipole implemented as a matrix, up to 2nd order. Use EVKICK for symplectic tracking.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| L              | $M$     | double | 0.0     | length   |
| KICK           | $RAD$   | double | 0.0     | kick strength  |
| TILT           | $RAD$   | double | 0.0     | rotation about longitudinal axis   |
| B2             | $1/M^2$ | double | 0.0     | normalized sextupole strength<br>(kick = KICK*(1+B2*y <sup>2</sup> ))  |
| CALIBRATION    |         | double | 1       | strength multiplier  |
| EDGE_EFFECTS   |         | short  | 0       | include edge effects?  |
| ORDER          |         | short  | 0       | matrix order   |
| STEERING       |         | short  | 1       | use for steering?  |
| SYNCH_RAD      |         | short  | 0       | include classical, single-particle synchrotron radiation?  |
| ISR            |         | short  | 0       | include incoherent synchrotron radiation (quantum excitation)?   |
| LERAD          |         | double | 0.0     | if L=0, use this length for radiation computations   |
| GROUP          |         | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## VMON

### 10.120 VMON—A vertical position monitor, accepting a rpn equation for the readout as a function of the actual position (y).

A vertical position monitor, accepting a rpn equation for the readout as a function of the actual position (y).

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name | Units    | Type   | Default | Description  |
|----------------|----------|--------|---------|--|
| L              | <i>M</i> | double | 0.0     | length   |
| DX             | <i>M</i> | double | 0.0     | misalignment   |
| DY             | <i>M</i> | double | 0.0     | misalignment   |
| WEIGHT         |          | double | 1       | weight in correction   |
| TILT           |          | double | 0.0     | rotation about longitudinal axis   |
| CALIBRATION    |          | double | 1       | calibration factor for readout   |
| SETPOINT       | <i>M</i> | double | 0.0     | steering setpoint  |
| ORDER          |          | short  | 0       | matrix order   |
| READOUT        |          | STRING | NULL    | rpn expression for readout (actual position supplied in variable y)  |
| CO_FITPOINT    |          | short  | 0       | If nonzero, then closed orbit value is placed in variable <name>#<occurrence>.yco  |
| GROUP          |          | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

## WAKE

### 10.121 WAKE—Longitudinal wake specified as a function of time lag behind the particle.

Longitudinal wake specified as a function of time lag behind the particle.

Parallel capable? : yes

GPU capable? : yes

Back-tracking capable? : yes

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| INPUTFILE         |       | STRING | NULL    | name of file giving Green function   |
| TCOLUMN           |       | STRING | NULL    | column in INPUTFILE containing time data   |
| WCOLUMN           |       | STRING | NULL    | column in INPUTFILE containing Green function  |
| CHARGE            | $C$   | double | 0.0     | beam charge (or use CHARGE element)  |
| FACTOR            | $C$   | double | 1       | factor by which to multiply wake   |
| N_BINS            |       | long   | 0       | number of bins for current histogram   |
| INTERPOLATE       |       | long   | 0       | interpolate wake?  |
| SMOOTHING         |       | long   | 0       | Use Savitzky-Golay filter to smooth current histogram?   |
| SG_HALFWIDTH      |       | long   | 4       | Savitzky-Golay filter half-width for smoothing   |
| SG_ORDER          |       | long   | 1       | Savitzky-Golay filter order for smoothing  |
| CHANGE_P0         |       | long   | 0       | change central momentum?   |
| ALLOW_LONG_BEAM   |       | long   | 0       | allow beam longer than wake data?  |
| RAMP_PASSES       |       | long   | 0       | Number of passes over which to linearly ramp up the wake to full strength.   |
| BUNCHED_BEAM_MODE |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| ACAUSAL_ALLOWED   |       | long   | 0       | If non-zero, then an acausal wake is allowed.  |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The input file for this element gives the longitudinal Green function,  $W(t)$  versus time behind the particle. The units of the wake are V/C, so this element simulates the integrated wake of some structure (e.g., a cell or series of cells). If you have, for example, the wake for a cell and you need the wake for N cells, then you may use the **FACTOR** parameter to make the appropriate multiplication. The values of the time coordinate should begin at 0 and be equi-spaced, and be expressed in seconds. A positive value of time represents the distance behind the exciting particle.

A positive value of  $W(t)$  results in energy *loss*. A physical wake function should be positive at  $t = 0$ . Causality requires that  $W(t) = 0$  for  $t < 0$ . Acausal wakes are supported, provided the user

sets `ACAUSAL_ALLOWED=0`. The data file must contain a value of  $W(t)$  at  $t = 0$ , and should have equal spans of time to the negative and positive side of  $t = 0$ .

Use of the `CHARGE` parameter on the `WAKE` element is disparaged. It is preferred to use the `CHARGE` element as part of your beamline to define the charge.

Setting the `N_BINS` parameter to 0 is recommended. This results in auto-scaling of the number of bins to accomodate the beam. The bin size is fixed by the spacing of the time points in the wake.

The default degree of smoothing (`SG_HALFWIDTH=4`) may be excessive. It is suggested that users vary this parameter to verify that results are reliable if smoothing is employed (`SMOOTHING=1`).

The algorithm for the wake element is as follows:

1. Compute the arrival time of each particle at the wake element. This is necessary because **elegant** uses the longitudinal coordinate  $s = \beta ct$ .
2. Find the mean, minimum, and maximum arrival times ( $t_{mean}$ ,  $t_{min}$ , and  $t_{max}$ , respectively). If  $t_{max} - t_{min}$  is greater than the duration of the wakefield data, then **elegant** either exits (default) or issues a warning (if `ALLOW_LONG_BEAM` is nonzero). In the latter case, that part of the beam that is furthest from  $t_{mean}$  is ignored for computation of the wake.
3. If the user has specified a fixed number of bins (not recommended), then **elegant** centers those bins on  $t_{mean}$ . Otherwise, the binning range encompasses  $t_{min} - \Delta t$  to  $t_{max} + \Delta t$ , where  $\Delta t$  is the spacing of data in the wake file.
4. Create the arrival time histogram. If any particles are outside the histogram range, issue a warning.
5. If `SMOOTHING` is nonzero, smooth the arrival time histogram.
6. Convolve the arrival time histogram with the wake function.
7. Multiply the resultant wake by the charge and any user-defined factor.
8. Apply the energy changes for each particle. This is done in such a way that the transverse momentum are conserved.
9. If `CHANGE_P0` is nonzero, change the reference momentum of the beamline to match the average momentum of the beam.

Bunched-mode application of the short-range wake is possible using specially-prepared input beams. See Section 6 for details. The use of bunched mode for any particular `WAKE` element is controlled using the `BUNCHED_BEAM_MODE` parameter.

## WATCH

**10.122 WATCH—A beam property/motion monitor—allowed modes are centroid, parameter, coordinate, and fft.**

A beam property/motion monitor—allowed modes are centroid, parameter, coordinate, and fft.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : yes



| Parameter Name  | Units | Type   | Default     | Description  |
|-----------------|-------|--------|-------------|--|
| FRACTION        |       | double | 1           | fraction of particles to dump (coordinate mode)  |
| START_PID       |       | long   | -1          | starting particleID for particles to dump  |
| END_PID         |       | long   | -1          | ending particleID for particles to dump  |
| INTERVAL        |       | long   | 1           | interval for data output (in turns)  |
| START_PASS      |       | long   | 0           | pass on which to start   |
| END_PASS        |       | long   | -1          | pass on which to end (inclusive). Ignored if negative.   |
| FILENAME        |       | STRING |             | output filename, possibly incomplete (see below)   |
| LABEL           |       | STRING |             | output label   |
| MODE            |       | STRING | coordinates | coordinate, parameter, centroid, or fft. For fft mode, you may add a space and a qualifier giving the window type: hanning (default), parzen, welch, or uniform. |
| X_DATA          |       | short  | 1           | include x data in coordinate mode?   |
| Y_DATA          |       | short  | 1           | include y data in coordinate mode?   |
| LONGIT_DATA     |       | short  | 1           | include longitudinal data in coordinate mode?  |
| EXCLUDE_SLOPES  |       | short  | 0           | exclude slopes in coordinate mode?   |
| FLUSH_INTERVAL  |       | long   | 100         | file flushing interval (parameter or centroid mode)  |
| SPARSE_INTERVAL |       | long   | 1           | interval for particle output (coordinate mode)   |
| DISABLE         |       | short  | 0           | If nonzero, no output will be generated.   |
| USE_DISCONNECT  |       | short  | 0           | If nonzero, files are disconnected between each write operation. May be useful for parallel operation. Ignored otherwise.  |

## WATCH continued

A beam property/motion monitor—allowed modes are centroid, parameter, coordinate, and fft.

| Parameter Name      | Units | Type   | Default | Description  |
|---------------------|-------|--------|---------|--|
| INDEX_OFFSET        |       | long   | 0       | Offset for file indices for sequential file naming.  |
| REFERENCE_FREQUENCY |       | double | -1      | If non-zero, the indicated frequency is used to define the bucket center for purposes of computing time offsets.   |
| GROUP               |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

The output filename may be an incomplete filename. In the case of the WATCH point element, this means it may contain one instance of the string format specification “%s” and one occurrence of an integer format specification (e.g., “%03ld”). **elegant** will replace the format with the rootname (see **run\_setup**) and the latter with the element’s occurrence number. For example, suppose you had a repetitive lattice defined as follows:

```
W1: WATCH,FILENAME=' '%s-%03ld.w1' '
Q1: QUAD,L=0.1,K1=1
D: DRIFT,L=1
Q2: QUAD,L=0.1,K1=-1
CELL: LINE=(W1,Q1,D,2*Q2,D,Q1)
BL: LINE=(100*CELL)
```

The element W1 appears 100 times. Each instance will result in a new file being produced. Successive instances have names like “*rootname-001.w1*”, “*rootname-002.w1*”, “*rootname-003.w1*”, and so on up to “*rootname-100.w1*”. (If instead of “%03ld” you used “%ld”, the names would be “*rootname-1.w1*”, “*rootname-2.w1*”, etc. up to “*rootname-100.w1*”. This is generally not as convenient as the names don’t sort into occurrence order.)

The files can easily be plotted together, as in

```
% sddsplot -column=t,p *-???.w1 -graph=dot -separate
```

They may also be combined into a single file, as in

```
% sddscombine *-???.w1 all.w1
```

In passing, note that if W1 was defined as

```
W1: WATCH,FILENAME=' '%s.w1' '
```

or

```
W1: WATCH,FILENAME=' 'output.w1' '
```

only a single file would be produced, containing output from the last instance only.

Notes:

1. Confusion sometimes occurs about some of the quantities related to the **s** coordinate in this file when in parameter mode. Please see Section 4 above.
2. This element can adversely affect parallel efficiency. Use of the **START\_PASS**, **END\_PASS**, **INTERVAL**, and **FLUSH\_INTERVAL** options can help reduce the impact. Also, particle output is the most expensive, by far.

## WIGGLER

### 10.123 WIGGLER—A wiggler or undulator for damping or excitation of the beam.

A wiggler or undulator for damping or excitation of the beam.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units | Type   | Default | Description  |
|----------------|-------|--------|---------|--|
| L              | $M$   | double | 0.0     | length   |
| RADIUS         | $M$   | double | 0.0     | Peak bending radius. Ignored if K or B is non-negative.  |
| K              |       | double | 0.0     | Dimensionless strength parameter.  |
| B              | $T$   | double | 0.0     | Peak vertical magnetic field. Ignored if K is non-negative   |
| DX             |       | double | 0.0     | Misalignment.  |
| DY             |       | double | 0.0     | Misalignment.  |
| DZ             |       | double | 0.0     | Misalignment.  |
| TILT           |       | double | 0.0     | Rotation about beam axis.  |
| POLES          |       | long   | 0       | Number of wiggler poles  |
| FOCUSING       |       | short  | 1       | If 0, turn off vertical focusing (this is unphysical!)   |
| GROUP          |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element simulates a wiggler or undulator. There are two aspects to the simulation: the effect on radiation integrals and the vertical focusing. Both are included as of release 15.2 of elegant.

If the number of poles should be an odd integer, we include half-strength end poles to match the dispersion, but only for the radiation integral calculation. For the focusing, we assume all the poles are full strength (i.e., a pure sinusoidal variation). If the number of poles is an even integer, no special end poles are required, but we make the unphysical assumption that the field at the entrance (exit) of the device jumps instantaneously from 0 (full field) to full field (0).

The radiation integrals were computed analytically using Mathematica, including the variation of the horizontal beta function and dispersion. For an odd number of poles, half-strength end-poles are assumed in order to match the dispersion of the wiggler. For an even number of poles, half-length end poles are assumed (i.e., we start and end in the middle of a pole), for the same reason.

The vertical focusing is implemented as a distributed quadrupole-like term (affecting only the vertical, unlike a true quadrupole). The strength of the quadrupole is (see Wiedemann, *Particle*

*Accelerator Physics II*, section 2.3.2)

$$K_1 = \frac{1}{2\rho^2}, \quad (156)$$

where  $\rho$  is the bending radius at the center of a pole. The undulator is focusing in the vertical plane.

The wiggler field strength may be specified either as a peak bending radius  $\rho$  (RADIUS parameter) or using the dimensionless strength parameter  $K$  (K parameter). These are related by

$$K = \frac{\gamma\lambda_u}{2\pi\rho}, \quad (157)$$

where  $\gamma$  is the relativistic factor for the beam and  $\lambda_u$  is the period length.

## ZLONGIT

### **10.124 ZLONGIT—A simulation of a single-pass broad-band or functionally specified longitudinal impedance.**

A simulation of a single-pass broad-band or functionally specified longitudinal impedance.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units    | Type   | Default             | Description   |
|----------------|----------|--------|---------------------|---|
| CHARGE         | $C$      | double | 0.0                 | beam charge (or use CHARGE element)   |
| BROAD_BAND     |          | long   | 0                   | broad-band impedance?   |
| RA             | $\Omega$ | double | 0.0                 | shunt impedance, $R_a = V^2/P$  |
| RS             | $\Omega$ | double | 0.0                 | shunt impedance ( $R_s = R_a/2$ )   |
| Q              |          | double | 0.0                 | cavity Q  |
| FREQ           | $Hz$     | double | 0.0                 | frequency<br>(BROAD_BAND=1)   |
| ZREAL          |          | STRING | NULL                | <filename>=<x>+<y> form<br>specification of input file giving<br>real part of impedance vs f<br>(BROAD_BAND=0)      |
| ZIMAG          |          | STRING | NULL                | <filename>=<x>+<y><br>form specification of input file<br>giving imaginary part of impedance<br>vs f (BROAD_BAND=0) |
| BIN_SIZE       | $S$      | double | 0.0                 | bin size for current histogram<br>(use 0 for autosize)  |
| N_BINS         |          | long   | 128                 | number of bins for current histogram  |
| MAX_N_BINS     |          | long   | 0                   | Maximum number of bins for<br>current histogram   |
| WAKES          |          | STRING | NULL                | filename for output of wake   |
| WAKE_INTERVAL  |          | long   | 1                   | interval in passes at which to<br>output wake   |
| WAKE_START     |          | long   | 0                   | pass at which to start to output<br>wake  |
| WAKE_END       |          | long   | 9223372036854775807 | pass at which to stop to output<br>wake   |
| AREA_WEIGHT    |          | long   | 0                   | use area-weighting in assigning<br>charge to histogram?   |
| INTERPOLATE    |          | long   | 0                   | interpolate wake?   |
| SMOOTHING      |          | long   | 0                   | Use Savitzky-Golay filter to<br>smooth current histogram?   |
| SG_ORDER       |          | long   | 1                   | Savitzky-Golay filter order for<br>smoothing  |
| SG_HALFWIDTH   |          | long   | 4                   | Savitzky-Golay filter<br>halfwidth for smoothing  |

## ZLONGIT continued

A simulation of a single-pass broad-band or functionally specified longitudinal impedance.

| Parameter Name         | Units | Type   | Default | Description  |
|------------------------|-------|--------|---------|--|
| REVERSE_TIME_ORDER     |       | long   | 0       | Reverse time-order of particles for wake computation?  |
| FACTOR                 |       | double | 1       | Factor by which to multiply impedance.   |
| START_ON_PASS          |       | long   | 0       | The pass on which the impedance effects start.   |
| RAMP_PASSES            |       | long   | 0       | Number of passes over which to linearly ramp up the impedance to full strength.  |
| HIGH_FREQUENCY_CUTOFF0 |       | double | -1      | Frequency at which smoothing filter begins. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize).        |
| HIGH_FREQUENCY_CUTOFF1 |       | double | -1      | Frequency at which smoothing filter is 0. If not given, defaults to HIGH_FREQUENCY_CUTOFF0.  |
| BUNCHED_BEAM_MODE      |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| ALLOW_LONG_BEAM        |       | long   | 0       | Allow beam longer than covered by impedance data?  |
| GROUP                  |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows simulation of a longitudinal impedance using a “broad-band” resonator or an impedance function specified in a file. The impedance is defined as the Fourier transform of the wake function

$$Z(\omega) = \int_{-\infty}^{+\infty} e^{-i\omega t} W(t) dt \quad (158)$$

where  $i = \sqrt{-1}$ ,  $W(t) = 0$  for  $t < 0$ , and  $W(t)$  has units of  $V/C$ .

For a resonator impedance, the functional form is

$$Z(\omega) = \frac{R_s}{1 + iQ(\frac{\omega}{\omega_r} - \frac{\omega_r}{\omega})}, \quad (159)$$

where  $R_s$  is the shunt impedance in *Ohms*,  $Q$  is the quality factor, and  $\omega_r$  is the resonant frequency.

When providing an impedance in a file, the user must be careful to conform to these conventions. In addition, the units of the frequency column must be Hz, while the units of the impedance components must be Ohms. At present, **elegant** does not check the units for correctness.



Other notes:

1. The frequency data required from the input file is *not*  $\omega$ , but rather  $f = \omega/(2\pi)$ .
2. The default smoothing setting (`SG_HALFWIDTH=4`), may apply too much smoothing. It is recommended that the user vary this parameter if smoothing is employed.
3. Using the broad-brand resonator model can often result in a very large number of bins being used, as **elegant** will try to resolve the resonance peak and achieve the desired bin spacing. This can result in poor performance, particularly for the parallel version.
4. Wake output is available only in the serial version.

Bunched-mode application of the impedance is possible using specially-prepared input beams. See Section 6 for details. The use of bunched mode for any particular **ZLONGIT** element is controlled using the `BUNCHED_BEAM_MODE` parameter.

**Explanation of <filename>=<x>+<y> format:** Several elements in **elegant** make use of data from external files to provide input waveforms. The external files are SDDS files, which may have many columns. In order to provide a convenient way to specify both the filename and the columns to use, we frequently employ <filename>=<x>+<y> format for the parameter value. For example, if the parameter value is `waveform.sdds=t+A`, then it means that columns **t** and **A** will be taken from file `waveform.sdds`. The first column is always the independent variable (e.g., time, position, or frequency), while the second column is the dependent quantity.

## ZTRANSVERSE

### 10.125 ZTRANSVERSE—A simulation of a single-pass broad-band or functionally-specified transverse impedance.

A simulation of a single-pass broad-band or functionally-specified transverse impedance.

Parallel capable? : yes

GPU capable? : no

Back-tracking capable? : no

| Parameter Name | Units   | Type   | Default | Description  |
|----------------|---------|--------|---------|--|
| CHARGE         | $C$     | double | 0.0     | beam charge (or use CHARGE element)                            |
| BROAD_BAND     |         | long   | 0       | broad-band impedance?  |
| RS             | $Ohm/m$ | double | 0.0     | shunt impedance<br>( $R_s = R_a/2 = V^2/(2 \cdot P)$ )         |
| Q              |         | double | 0.0     | cavity Q   |
| FREQ           | $Hz$    | double | 0.0     | frequency<br>(BROAD_BAND=1)                                    |
| INPUTFILE      |         | STRING | NULL    | name of file giving impedance<br>(BROAD_BAND=0)                |
| FREQCOLUMN     |         | STRING | NULL    | column in INPUTFILE containing frequency                       |
| ZXREAL         |         | STRING | NULL    | column in INPUTFILE containing real impedance for x plane      |
| ZXIMAG         |         | STRING | NULL    | column in INPUTFILE containing imaginary impedance for x plane |
| ZYREAL         |         | STRING | NULL    | column in INPUTFILE containing real impedance for y plane      |
| ZYIMAG         |         | STRING | NULL    | column in INPUTFILE containing imaginary impedance for y plane |
| BIN_SIZE       | $S$     | double | 0.0     | bin size for current histogram<br>(use 0 for autosize)         |
| INTERPOLATE    |         | long   | 0       | interpolate wake?  |
| N_BINS         |         | long   | 128     | number of bins for current histogram                           |
| MAX_N_BINS     |         | long   | 0       | Maximum number of bins for current histogram                   |
| SMOOTHING      |         | long   | 0       | Use Savitzky-Golay filter to smooth current histogram?         |
| SG_ORDER       |         | long   | 1       | Savitzky-Golay filter order for smoothing                      |
| SG_HALFWIDTH   |         | long   | 4       | Savitzky-Golay filter halfwidth for smoothing                  |

## ZTRANSVERSE continued

A simulation of a single-pass broad-band or functionally-specified transverse impedance.

| Parameter Name         | Units    | Type   | Default             | Description   |
|------------------------|----------|--------|---------------------|---|
| DX                     | <i>M</i> | double | 0.0                 | misalignment  |
| DY                     | <i>M</i> | double | 0.0                 | misalignment  |
| FACTOR                 |          | double | 1                   | Factor by which to multiply x and y impedances.   |
| XFACTOR                |          | double | 1                   | Factor by which to multiply x impedance.  |
| YFACTOR                |          | double | 1                   | Factor by which to multiply y impedance.  |
| WAKES                  |          | STRING | NULL                | filename for output of wake   |
| WAKE_INTERVAL          |          | long   | 1                   | interval in passes at which to output wake  |
| WAKE_START             |          | long   | 0                   | pass at which to start to output wake   |
| WAKE_END               |          | long   | 9223372036854775807 | pass at which to stop to output wake  |
| START_ON_PASS          |          | long   | 0                   | The pass on which the impedance effects start.  |
| RAMP_PASSES            |          | long   | 0                   | Number of passes over which to linearly ramp up the impedance to full strength.   |
| HIGH_FREQUENCY_CUTOFF0 |          | double | -1                  | Frequency at which smoothing filter begins. If not positive, no frequency filter smoothing is done. Frequency is in units of Nyquist (0.5/binsize). |
| HIGH_FREQUENCY_CUTOFF1 |          | double | -1                  | Frequency at which smoothing filter is 0. If not given, defaults to HIGH_FREQUENCY_CUTOFF0  |
| X_DRIVE_EXPONENT       |          | long   | 1                   | Exponent applied to x coordinates of drive particles  |
| Y_DRIVE_EXPONENT       |          | long   | 1                   | Exponent applied to y coordinates of drive particles  |
| X_PROBE_EXPONENT       |          | long   | 0                   | Exponent applied to x coordinates of probe particles  |

## ZTRANSVERSE continued

A simulation of a single-pass broad-band or functionally-specified transverse impedance.

| Parameter Name    | Units | Type   | Default | Description  |
|-------------------|-------|--------|---------|--|
| Y_PROBE_EXPONENT  |       | long   | 0       | Exponent applied to y coordinates of probe particles   |
| BUNCHED_BEAM_MODE |       | long   | 1       | If non-zero, then do calculations bunch-by-bunch.  |
| ALLOW_LONG_BEAM   |       | long   | 0       | Allow beam longer than covered by impedance data?  |
| GROUP             |       | string | NULL    | Optionally used to assign an element to a group, with a user-defined name. Group names will appear in the parameter output file in the column ElementGroup |

This element allows simulation of a transverse impedance using a “broad-band” resonator or an impedance function specified in a file. The impedance is defined as the Fourier transform of the wake function

$$Z(\omega) = \int_{-\infty}^{+\infty} e^{-i\omega t} W(t) dt \quad (160)$$

where  $i = \sqrt{-1}$ ,  $W(t) = 0$  for  $t < 0$ , and  $W(t)$  has units of  $V/C/m$ . Note that there is no factor of  $i$  in front of the integral. Thus, in **elegant** the transverse impedance is simply the Fourier transform of the wake. This makes it easy to convert data from a program like ABCI into the wake formalism using **sddsfft**.

For a resonator impedance, the functional form is

$$Z(\omega) = \frac{-i\omega_r}{\omega} \frac{R_s}{1 + iQ(\frac{\omega}{\omega_r} - \frac{\omega_r}{\omega})}, \quad (161)$$

where  $R_s$  is the shunt impedance in *Ohms/m*,  $Q$  is the quality factor, and  $\omega_r$  is the resonant frequency.

When providing an impedance in a file, the user must be careful to conform to these conventions. In addition, the units of the frequency column must be Hz, while the units of the impedance components must be Ohms/m. At present, **elegant** does not check the units for correctness.

Other notes:

1. The frequency data required from the input file is *not*  $\omega$ , but rather  $f = \omega/(2\pi)$ .
2. The default smoothing setting (**SG\_HALFWIDTH=4**), may apply too much smoothing. It is recommended that the user vary this parameter if smoothing is employed.
3. Using the broad-band resonator model can often result in a very large number of bins being used, as **elegant** will try to resolve the resonance peak and achieve the desired bin spacing. This can result in poor performance, particularly for the parallel version.
4. Wake output is available only in the serial version.

Bunched-mode application of the impedance is possible using specially-prepared input beams. See Section 6 for details. The use of bunched mode for any particular `ZTRANSVERSE` element is controlled using the `BUNCHED_BEAM_MODE` parameter.

## 11 Examples

Example runs and post-processing files are available in a separate tar file. The examples are intended to demonstrate program capabilities with minimal work on the user's part. However, they don't pretend to cover all the capabilities.

Each demo is (typically) invoked using a command (usually a C-shell script) that can both run **elegant** and post-process the output. The post-processing is often handled by a lower-level script that is called from the demo script. These lower-level scripts are good models for the creation of customized scripts for user applications.

The examples are organized into a number of directories and subdirectories. In each area, the user will find a "Notebook" file (a simple ASCII file) that describes the example and how to run it.

Many examples for storage ring simulations reside in the **PAR** subdirectory. The PAR (Particle Accumulator Ring) is a small storage ring in the APS injector that is good for quick examples because of its size.

Here's a helpful tip in searching the examples on UNIX/LINUX systems: suppose one wants to find an example of the **frequency\_map** command. One can search all the elegant command files very quickly with this command:

```
find . -name '*.ele' | xargs fgrep frequency_map
```

Similarly, to find all examples that use CSBEND elements, one could use

```
find . -name '*.lte' | xargs fgrep -i csbend
```

- **acceptance** — Use of the acceptance feature when tracking collections of particles.
  - **energyScan1** — Tracking a FODO line with various apertures, with variation of the initial momentum offset.
  - **fodoScan1** — Tracking a FODO line with various apertures, with scanning of the quadrupole strengths.
  - **transportLineAcceptance** — Determine transverse and momentum acceptance of a transport line using tracking. Example by M. Borland (ANL).
- **alphaMagnet** — Optimization of the strength of an alpha magnet to compress the beam from a thermionic rf gun.
- **APSRing** — Examples for the APS storage ring
  - **beamMoments** — 6D beam moments calculation with errors
  - **ibsAndTouschekLifetime** — Compute touschek lifetime with IBS-inflated emittances
  - **ibsVsEnergy** — Compute IBS as a function of energy.
  - **ionEffects1** — Basic simulation of ion effects.
- **beamBasedAlignment** — Determines quadrupole offsets based on simulated beam-based alignment procedure.
- **beamBreakup** — Example of simulating beam-driven deflecting rf mode in a simple linac.
- **bendErrors** — Analysis of the effect of errors on the matrix elements for a four-dipole bunch compression chicane.
- **boosterRamp** — Examples of simulating ramping in a booster.
  - **elementByElement** — Example of simulating ramping in a booster, using the NSLS-II booster lattice (R. Fliller).
  - **ILMATRIX** — Example of ramping using ILMATRIX for faster tracking.
- **bpmOffsets1** — Example of loading BPM offsets from an external file and then correcting the orbit with those offsets.
- **bunchCompression** — Examples of using a four-dipole chicane for bunch compression.
  - **bunchComp** — Four examples revolving around a four-dipole chicane bunch compressor. Simulations include basic compression, sensitivity to timing, phase, and beam energy.
  - **bunchCompJitter** — Simulation of a linac with a bunch compressor, including phase and voltage errors in the linac.
  - **bunchCompJitter2** — Simulation of a linac with a bunch compressor, including phase and voltage errors in the linac. In this case, the errors are generated externally.
  - **bunchCompLSC** — Inclusion of longitudinal space charge in simulation of a linac with a bunch compressor.
  - **bunchCompOptimize** — Example of using tracking to optimize a linac and bunch compressor including a 4th-harmonic linearizer.

- **chromaticAmplitudes** — Example of minimizing chromatic amplitude functions in a simple beamline.
- **chromaticResponse** — Example of computing the chromatic transfer functions  $R_{16}(s)$  and  $R_{26}(s)$  as described in P. Emma and R. Brinkmann, SLAC-PUB-7554.
- **constructOrbitBump1** — Illustration of how to make an orbit bump using BPM offsets and the orbit correction algorithm.
- **coupling** — Examples of coupling calculation and correction.
  - **couplingCorrection1** — Scripts to perform coupling correction for the APS ring, emulating what is done in APS operations. These scripts are now part of the elegant distribution.
  - **couplingCorrection2** — Example of using cross-plane response matrix and vertical dispersion to correct the coupling.
- **customBeamDistributions** — Examples of making custom beam distributions for tracking with elegant.
  - **doubleBeam1** — Example of how to make a double-gaussian time distribution using two runs. The resultant beam would be used in a subsequent run using the `sdds_beam` command.
  - **example1** — Gaussian energy distribution, linearly-ramped time distribution, and uniform transverse distributions.
  - **parabolic** — Gaussian longitudinal distribution combined with parabolic transverse distributions.
- **cwiggler** — Examples of using the CWIGGLER element.
  - **cwig+kickmap** — Example of simulating a simple wiggler with CWIGGLER, making a kickmap from trackings, then validating the kickmap.
  - **cwiggler1** — A simple example of dynamic aperture with a set of sinusoidal wigglers, using the CWIGGLER element.
  - **cwiggler2** — An simple example of dynamic aperture with a set of two-component horizontal wigglers, using the CWIGGLER element.
- **DATuneScan** — Performs a scan of the tunes in a storage ring and determines the variation in dynamic aperture.
- **defeatLinkage** — Example of how to defeat the automatic link between the gradient and other multipoles in a dipole and the strength of the dipole itself.
- **ellipseComparison** — Example of comparing beam ellipse from tracking to ellipse implied by the twiss parameters.
- **emitProc** — Various applications of the program `sddsemitproc`, which processes quad-scan emittance measurements.
  - **emitProc1** — Simple example with constant measurement errors.



- `emitProc2` — Measurement errors are supplied in the data file.
  - `emitProc3` — Includes the presence of dispersion, with constant measurement errors.
  - `emitProc4` — Quadrupole scan values are supplied from an external source.
  - `emitProc5` — Includes acceleration as part of the beamline.
- `fiducialization` — Examples for fiducialization of a beamline.
  - `fiducial1` — Example of fiducialization with a fiducial bunch and a perturbed bunch. The system in question is a linac with 50 structures, a four dipole chicane, then 50 more structures
- `full457MeV` — Tracking of the APS linac with a PC gun beam, up to the entrance of the LEUTL undulator.
- `GENESIS2.0` — Example of running SDDS-compliant GENESIS 1.3 with output from elegant for LCLS.
- `geneticOptimizer1` — Illustration of using the geneticOptimizer script together with elegant.
- `ILMatrixFromTracking` — Determination of the values for ILMATRIX based on analysis of tracking data.
- `injRingMatch` — Matching of a transport line to a storage ring.
  - `injRingMatch1` — Illustration of finding the periodic solution for a ring, then matching a transport line to that solution.
  - `injRingMatch2` — Illustration of finding the periodic solution for a ring, then matching a transport line to that solution. In this case, a single run is used.
  - `movingElements` — Example of matching a transport line to a ring with movable quadrupoles but fixed total length.
- `LCLS` — LCLS-I tracking example from P. Emma, November 2007.
  - `wakes` —
- `linacDispersion1` — Example of determining the initial dispersion error in a linac.
- `LongitudinalSpaceCharge` — Examples related to longitudinal space charge.
  - `LSC0scillationExample` — Example of longitudinal space charge oscillations in a drift space.
- `lsrMdltr` — Various examples of using the LSRMDLTR (Laser Modulator) element
  - `example1` — Simple example using LCLS-I-like parameters
  - `example2` — Includes a time-profile on the laser.
  - `example3` — Simulation of laser slicing for a storage ring.
- `matching` — Various examples of lattice matching and optimization.

- **beamSizeMatch1** — Example of adjusting the initial beam parameters to match the measured beam sizes at a set of diagnostics.
- **betaMatching** — A simple two-stage matching example.
- **IDCompensation** — Example of compensating for insertion device focusing effects.
- **linacMatching1** — Example of three-part matching of a linac with a bunch compressor.
- **linearize2** — Example of reducing nonlinearities in phase space using the REMCOR element to remove linear correlations first.
- **matchMeasuredBetas** — Optimization of lattice quadrupoles to create a model that reproduces measured beta functions.
- **matchTwoEnergies** — Example of matching beams with two different initial energies in a linac. The beams are affected by common quadrupoles, but also by quadrupoles unique to each beam.
- **multiPartMatching1** — Complex example of multi-part matching for a linac with several splice points.
- **multiPartMatching2** — Example of storage ring matching with three types of cells.
- **spectrometer1** — Optimizes a simple spectrometer to maximize energy resolution.
- **MBALatticeDAWithErrors** — Example of performing DA vs momentum offset tracking when the lattice has strong sextupoles that make the orbit difficult to correct.
- **multibunchCollectiveEffects** — Examples of multi-bunch collective effects for APS storage ring and other cases.
  - **APS-24Bunch-CBI** — Includes main and harmonic cavities, beamloading, rf feedback, beam feedback, and short-range impedance.
  - **ILMatrixFromTracking** — Example of using tracking to set up the ILMATRIX element for fast tracking. This is useful for increasing the speed of collective effects simulations.
  - **linacBunchTrain1** — Includes main linac cavities, dipole HOMs, and monopole HOMs for a simple linac, showing beam breakup.
- **multiStepErrors1** — Example of multi-step addition and correction of errors for a storage ring.
- **NSLS-II-GirderMisalignment** — Simulation of girder misalignment for NSLS-II, by S. Kramer (BNL) and M. Borland (ANL).
- **outboardTrajCorr** — Examples of using the response matrix computed by elegant to perform trajectory correction with a script.
  - **outboardTrajCorr1** — Compares trajectory correction inside elegant to correction performed with an external script.
  - **outboardTrajCorr2** — Compares trajectory correction inside elegant to correction performed with an external script. Includes BPM offsets.
- **PAR** — Numerous examples using the small APS Particle Accumulator Ring.
  - **accumulate** — Simulates adding particles to an already-stored beam.

- **alphaExpansion** — Example of computing momentum compaction ( $\alpha$ ) to higher order using tracking.
- **broadBandImpedance** — Example of using ZLONGIT, ILMATRIX, and SREFFECTS to simulate a broad-band impedance in a storage ring.
- **bunchLengthening** — Simulation of a passive bunch-lengthening cavity using the RF-MODE element.
- **chromCorrection** — Simple chromaticity correction with two families. Also illustrates saving and loading correction results.
- **chromTracking** — Illustration of using tracking to determine variation of tune with momentum.
- **chromTracking2** — Similar to chromTracking, but includes determination of the momentum dependence of the beta functions.
- **CSR** — Example of tracking with APS Particle Accumulator Ring with a Coherent Synchrotron Radiation impedance.
- **DANormSigma** — Determination of dynamic aperture in terms of beam size.
- **daOpt** — Example of optimization of dynamic acceptance.
- **dynamicAperture** — Determination of dynamic aperture for a series of momentum errors.
- **dynamicApertureWithSynchMotion** — Example of dynamic aperture with radiation damping and synchrotron motion.
- **ejectionOptimization** — Tuning of a multi-turn extraction system using several kickers.
- **elasticScatteringTracking** — Tracking to determine elastic scattering lifetime and loss distribution.
- **emittanceOptimization** — Direct optimization of the emittance using linear optics tuning.
- **fineDynamicAperture** — High-resolution dynamic aperture including a map of where particles are lost.
- **fixedLVsRegularOrbit** — Illustration of the difference between orbits computed with fixed path length (fixed rf frequency) and fixed beam energy (variable rf frequency).
- **frequencyMap** — Example of frequency map analysis
- **frequencyMap-x-delta** — Example of frequency map analysis for (x,  $\delta$ )
- **gasScatteringLifetime** — Simple computation of gas scattering lifetime using a fixed pressure and gas mixture.
- **gasScatteringLifetimePresFile** — Computation of gas scattering lifetime using a file giving the pressure around the ring.
- **ILMatrixScan** — Set up ILMATRIX element, then scan the tune.
- **inelasticScatteringTracking** — Tracking to determine inelastic scattering lifetime and loss distribution.
- **moments** — Computes 6D beam moments with coupling errors.
- **momentumAperture** — Computes the s-dependent momentum aperture without errors.

- `offMomentumDA` — Another computation of off-momentum dynamic aperture
  - `offMomentumTwiss` — Computation of off-momentum twiss parameters.
  - `offMomentumTwiss2` — Computation of off-momentum twiss parameters vs s.
  - `quadScan` — Computation of twiss parameters as quadrupoles are varied according to an external table.
  - `randomMultipoles` — Dynamic aperture including random multipole errors in the quadrupoles and sextupoles.
  - `synchrotronTune` — Simple example of tracking with synchrotron motion.
  - `tracking` — Visualization of motion in x-x' and y-y' phase space.
  - `trajOrbitCorrect` — Correct the first-turn trajectory, then correct the orbit.
  - `TSWATracking` — Uses tracking and post-processing to determine tune variation with amplitude.
  - `tuneExcitation` — Use a swept kick to excite the horizontal tune, observing excitation of the synchrotron tune as well.
  - `tuneOptimization` — Correct the tunes and chromaticities.
  - `twissCalculation` — Simple calculation of the twiss parameters
  - `twoCavityMoments` — Calculation of 6D beam moments in the presence of main and harmonic rf cavities.
- `parallel` — Various runs illustrating a few features of the parallel version.
    - DA — Dynamic aperture calculation.
    - FMA — Frequency map analysis.
    - LMA — Local momentum aperture calculation.
  - `pepperPot` — Examples of using the PEPPER\_POT element
    - `basic` — Basic example of simulating a pepper-pot plate.
    - `pepperPotScan` — Example of simulating a pepper-pot plate with emittance analysis.
  - `periodicTwissRFCA` — Demonstration that one can't have periodic beta functions in a FODO cell array with linac structures.
  - `pulsedSextInjection` — Illustration of optimizing the sextupoles of pulsed sextupole kickers for injection into a storage ring.
  - `rampTunesWithBeam` — Example of ramping tunes while tracking beam. In this case, we ramp the tunes across the difference coupling resonance.
  - `rfDeflectingCavity` — A simple example of using a traveling wave rf deflector (RFDF).
  - `RFTMEZ0` — Tracking through a TM-mode rf cavity based on an off-axis expansion starting from  $E_z(z)$  at  $r=0$ .
  - `scanParameters` — Examples of scanning parameters of beamline elements.

- `scanParameters1` — Scan two quadrupoles together.
  - `scanParameters2` — Scan the phase of an rf cavity and look at synchrotron oscillations.
- `scriptElement` — Examples of using the SCRIPT element
  - `elegantShower` — Use of the SCRIPT element to execute the electron-gamma shower simulation code SHOWER as part of an elegant run.
  - `mergeBeams` — Using the SCRIPT element to merge several beams into a simulation that already has a beam.
  - `slitArray` — Simulation of an array of slits using the SCRIPT element.
- `sddsoptimizeExample` — Example of using the program sddsoptimize to optimize the results of elegant simulations. In this example, we vary a strength fudge factor for a set of quadrupoles in a transport line in order to attempt to match measured H and V response matrices.
- `serverExample` — Example of using elegant in server mode to update lattice functions when magnet strengths change.
- `SPEAR3` — Various examples using an early SPEAR3 lattice
  - `dynamicAperture` — Compute DA for several error seeds, including multipole errors.
  - `latticeErrors` — Compute variation in lattice functions with errors, including correction of the orbit, tunes, and chromaticities.
- `staticPlusDynamicErrors` — Example of combining static and dynamic errors in one simulation.
- `storageRingRfNoise` — Example of including rf phase and amplitude noise in a tracking simulation.
- `transportLineHigherOrderDispersion` — Determine higher-order dispersion in a transport line using tracking.
- `twissDerivatives` — Example of how to compute slopes of beta, alpha, and dispersion as a function of initial momentum for a transport line.
- `twoBunchPhasing` — Example of putting two bunches through a linac with the linac phased to the first bunch.
- `varyPlotExample` — Example of varying a beamline parameter and computing beam properties, then plotting those properties vs s.
- `wakesAndImpedances` — Examples of wakes and impedances.
  - `transverse1` — Compare use of transverse wake and impedance methods for a damped oscillator.

## 12 The `rpn` Calculator

The program `rpn` is a Reverse Polish Notation programmable scientific calculator written in C. It is incorporated as a subprogram into `elegant`, and a number of the SDDS programs. It also exists as a command-line program, `rpn1`, which executes its command-line arguments as `rpn` operations and prints the result before exiting. Use of `rpn` in any of these modes is extremely straightforward. Use of the program in its stand-alone form is the best way to gain familiarity with it. Once one has entered `rpn`, entering “help” will produce a list of the available operators with brief summaries of their function. Also, the `rpn` definitions file `rpn.defns`, distributed with `elegant`, gives examples of most `rpn` operation types.

Like all RPN calculators, `rpn` uses stacks. In particular, it has a numeric stack, a logical stack, and a string stack. Items are pushed onto the numeric stack whenever a number-token is entered, or whenever an operation concludes that has a number as its result; items are popped from this stack by operations that require numeric arguments. Items are pushed onto the logical stack whenever a logical expression is evaluated; they are popped from this stack by use of logical operations that require logical arguments (e.g., logical ANDing), or by conditional branch instructions. Items enclosed in double quotes are pushed onto the string stack; items are popped from this stack by use of operations that require string arguments (e.g., formatted printing).

`rpn` supports user-defined memories and functions. To create a user-defined memory, one simply stores a value into the name, as in “1 sto unity”; the memory is created automatically when `rpn` detects that it does not already exist. To create a user-defined function, enter the “udf” command; `rpn` will prompt for the function name and the text that forms the function body. To invoke a UDF, simply type the name.

A file containing `rpn` commands can be executed by pushing the filename onto the string stack and invoking the “@” operator. `rpn` supports more general file I/O through the use of functions that mimic the standard C I/O routines. Files are identified by integer unit numbers, with units 0 and 1 being permanently assigned to the terminal input and terminal output, respectively.

## 13 Change Log

### 13.1 Highlights of What's New in Version 2019.3.0

Here is a summary of what's changed since release 2019.2.1. Historical change logs are collected in Section 13.

#### 13.1.1 Bug Fixes for Elements

- The matrix for the **SBEN** element was incorrect when the length was negative (which is needed for back-tracking). A. Zholents (ANL) and Y. Park (UCLA) helped identify the problem.
- The integrator used for the **CSBEND** element with the expanded Hamiltonian (**EXPAND\_HAMILTONIAN=1**) was very inaccurate and yielded poor results unless **N\_KICKS** was large. This problem, pointed out by Z. Duan (IHEP), was fixed.
- The interpolation used for **UKICKMAP** would previously produce invalid values for particles near the upper ( $y > 0$ ) and left ( $x > 0$ ) edges of the grid. In essence, the interpolation assumed the kickmap was periodic in  $x$  and  $y$ .

#### 13.1.2 Bug Fixes for Commands

- DA trimming (to make the **xClipped** and **yClipped** columns, as well as the **Area** parameter) was not working properly in the parallel version for full-plane runs. This was fixed. In addition, the algorithm was improved for both the serial and parallel versions to iterate the trimming until it converges.
- The multi-gaussian and multi-lorentzian feature of the **ion\_effects** command, added in the last release, proved unreliable, as reported by B. Podobedov (BNL). Several improvements and bug fixes were implemented that should improve matters.

#### 13.1.3 New and Modified Elements

- The **SHRFDF** element was added, which models a deflecting rf cavity using a space harmonic expansion. This was implemented by Y.P. Sun (APS). See [55] for details.
- The **LSCDRIFT** element, which models longitudinal space charge, can now have its effective length set automatically to correspond to the length of the upstream element.

#### 13.1.4 New and Modified Commands

- The **run\_setup** command has a new parameter, **back\_tracking**, which allows invoking a limited back-tracking capability. See the entry for **run\_setup** for more details. This is an experimental feature and users are encouraged to report problems to the forum.
- The **ion\_effects** command was improved in several ways:
  - The default distribution fitting parameters were modified to give improved convergence
  - The default distribution fitting criterion is now the sum of the maximum fractional absolute deviation over the histogram and the absolute fractional deviation of the ion charge. This makes it less likely that overfitting will result in large spikes in the distribution.

- The new `ion_histogram_max_bins` parameter allows restricting the maximum number of bins.
  - The new `ion_histogram_min_per_bin` parameter allows setting a requirement on the minimum number of macro ions per bin.
  - The new `freeze_ions_until_pass` and `freeze_electrons_until_pass` parameters allow “freezing” the motion of the ions and electrons until a specified pass number. This is useful for diagnostic purposes.
  - The new `pressure_factor` parameter allows multiplying all the pressure profiles by a common factor.
- The `matrix_output` command can now print the full matrix in a form accepted by Mathematica.

### 13.1.5 Changes Specific to the MPI Parallel Version

- Some apparent MPI-related issues were resolved for the `ion_effects` command.

### 13.1.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.1.7 Changes to Related Programs and Files

- The `touschekLifetime` program now reports the value of `deltaLimit` in the output file, whether that value is given explicitly or computed via the rf voltage.
- Added the program `sdds5x5sigmaproc`, which computes the 5x5 sigma matrix (i.e., all elements except those related to the time coordinates) from a quadrupole scan.

## 13.2 Highlights of What’s New in Version 2019.2.1

Here is a summary of what’s changed since release 2019.1.1.

### 13.2.1 Bug Fixes for Elements

- Fixed a bug in tracking-based matrix computation for `CCBEND` that would result in the program hanging under some circumstances.
- Fixed a bug in the implementation of the expanded Hamiltonian for `MULT` elements.
- Fixed a bug in the `BMXYZ` element that caused a crash when multiple such elements were used.
- If `COUPLING` and `EYREF` were both non-zero for an `SREFFECTS` element, the `EYREF` value would be ignored, which is potentially confusing. This issue is now flagged as an error. B. Podobodov (BNL) brought the issue to our attention.



### 13.2.2 Bug Fixes for Commands

- The `correct` command, which performs trajectory or orbit correction, would fail to output corrector data for both planes in some cases. This was fixed.
- The `correct` command, also had a bug in reporting the “uncorrected” trajectory in the trajectory output file. Instead of giving the uncorrected trajectory, it was giving the trajectory after the penultimate correction iteration. This was reported by forum user shancai.
- The memory-efficiency of bucket assignments, invoked when using `use_bunched_mode` in `sdds_beam`, was improved, preventing crashes in some extreme cases for the serial version.

### 13.2.3 New and Modified Elements

- Added the `APCONTOUR` element, which provides an aperture or obstruction defined by an  $(x, y)$  contour in an SDDS file.
- Added the `TAPERAPC` element, which provides a tapered circular aperture.
- Added the `TAPERAPE` element, which provides a tapered elliptical aperture.
- Added the `TAPERAPR` element, which provides a tapered rectangular aperture.
- `RFMODE` now allows ignoring particles that are outside the binning region, using the `ALLOW_UNBINNED_PARTICLES` parameter.
- The required format for `MATR` (matrix from a text file) has changed slightly, as described on the manual page. The element also has a new parameter, `FRACTION` that allows interpolating the matrix elements with the identity matrix as one endpoint.

### 13.2.4 New and Modified Commands

- The `ion_effects` command now supports calculation of ion fields using a bi-gaussian distribution (sum of two gaussians) or bi-lorentzian distribution (sum of two lorentzians), as well as tri-gaussian and tri-lorentzian distributions. This which allows modeling the core and tails of the distribution more accurately. A number of parameters were added for control of fitting and output. J. Calvey (ANL) and R. Lindberg (ANL) co-developed this improvement.
- The `sdds_beam` command now offers control of which bunch is used for fiducialization of rf systems. It defaults to the first bunch (`#0`), which is a change from the previous (and frequently confusing) behavior of fiducializing to the entire beam.
- The `aperture_search` command now allows full-plane computations, i.e., computations covering both  $y \geq 0$  and  $y < 0$ .

### 13.2.5 Changes Specific to the MPI Parallel Version

- None

### 13.2.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.2.7 Changes to Related Programs and Files

- The `touschekLifetime` program now reports the value of `deltaLimit` in the output file, whether that value is given explicitly or computed via the rf voltage.
- Added the program `sdds5x5sigmaproc`, which computes the 5x5 sigma matrix (i.e., all elements except those related to the time coordinates) from a quadrupole scan.

## 13.3 Highlights of What's New in Version 2019.1.1

Note that following release 35.1.0, version numbers changed to the form *year.release.minor*, where *year* is the four-digit year, *release* is the consecutive release number for the year, and *minor* is for internal APS use.

Here is a summary of what's changed since release 35.1.0. Historical change logs are collected in Section 13.

### 13.3.1 Bug Fixes for Elements

- The `BMXYZ` element previously would inject particles at  $z = 0$  by default, which is usually not the desired behavior. Now, it injects at the start of the field map by default. The new `INJECT_AT_Z0` parameter can be used to recover the old behavior. In addition, drift spaces are now automatically included to compensate for differences between the length of the field map and the user-defined insertion length.

### 13.3.2 Bug Fixes for Commands

- The `load_parameters` command with `change_defined_values=0` did not work correctly when combined with `insert_elements` or `replace_elements`. This was reported by G. Penn (LBNL).
- The `insert_elements` command would sometimes fail to insert all the intended elements when `insert_before=1` when insertion between consecutive elements was required. This was reported by G. Penn (LBNL).

### 13.3.3 New and Modified Elements

- The `BOFFAXE` element was added. It allows integrating through a magnetic field defined by an off-axis expansion from on-axis gradients.
- Transfer matrices are now automatically computed for `BMXYZ` and `BGGEXP` elements.
- The `CSBEND`, `SBEND`, and `CCBEND` elements now support separate fractional strength errors (FSE) for the dipole and quadrupole terms.
- The `HKPOLY` element now supports an alternative, more general form for the drift Hamiltonian.
- The `UKICKMAP` element now has a flag to indicate that the kickmap is for a single period of an insertion device, which makes it easier to configure. It also has a new parameter, `KACTUAL`, for giving the  $K$  value independent of the field factor (which is applied to the kickmap).

### 13.3.4 New and Modified Commands

- The `global_settings` command now allows setting the default step sizes for tracking-based determination of element-by-element matrices using the new `tracking_matrix_step_size` parameter. The default values are the same as those used by the `analyze_map` command.
- The `analyze_map` command now allows changing the number of points in each dimension and the maximum fit order.
- the `correct_tunes` command now allows specifying a list of quadrupoles to be excluded from the tune knob.

### 13.3.5 Changes Specific to the MPI Parallel Version

- Fixed a bug that resulted in crashing of tracking-based matrix computation for certain numbers of processors.
- Fixed a bug in parallel hybrid simplex optimization, which would cause optimization to terminate prematurely if one processor encountered an invalid condition (e.g., undefined tunes).

### 13.3.6 Changes Specific to the GPU Version

The GPU version continues to be an alpha release and contains bugs. Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.3.7 Changes to Related Programs and Files

- None.

## 13.4 Highlights of What's New in Version 35.1.0

Here is a summary of what's changed since release 35.0.1. Historical change logs are collected in Section 13.

### 13.4.1 Bug Fixes for Elements

- The matrix for misaligned FMULT elements was incorrect. The misalignment was applied twice.
- The edge effects for KQUAD were broken for tracking only in version 35.0.1. This was fixed.

### 13.4.2 Bug Fixes for Commands

- The filter parameters (`start_occurence`, `end_occurence`, `s_start`, `s_end`, `after`, and `before`) of the `steering_element` command now work better when multiple such commands are given. In particular, overlapping intervals are detected and non-overlapping intervals are correctly implemented.

### 13.4.3 New and Modified Elements

- The HKPOLY element was added. It allows imparting kicks to the beam according to a Hamiltonians that are polynomial functions of  $(x, y)$  and  $(qx, qy)$ . R. Lindberg (APS) helped develop the concept for this element.

### 13.4.4 New and Modified Commands

- The `correct` command has a new parameter, `force_alternation` that forces orbit or trajectory correction to continue with x/y alternation regardless of whether one plane appears to have converged.
- The `set_reference_particle_output` command was added. It allows defining a reference set of particle coordinates to which tracked coordinates will be compared for purposes of optimization.
- The `optimization_setup` command now allows setting the interval (in terms of function evaluations) between checks of the interrupt semaphore file. Previously, the file was checked only at the end of a simplex pass.

### 13.4.5 Changes Specific to the MPI Parallel Version

- None.

### 13.4.6 Changes Specific to the GPU Version

The GPU version continues to be an alpha release and contains bugs. Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.4.7 Changes to Related Programs and Files

- None.

## 13.5 Highlights of What's New in Version 35.0.1

Here is a summary of what's changed since release 34.4.0.

### 13.5.1 Bug Fixes for Elements

- The order of edge transformations for the CCBEND element was revised to make more physical sense.
- A bug was fixed in the expressions for integral-based fringe field effects in QUAD and KQUAD. The bug resulted in very small inconsistencies between the matrices when  $K_1 \rightarrow -K_1$ .
- Some small errors were found and fixed in the linear fringe treatment for the KQUAD and QUAD elements. Thanks to X. Huang (SLAC) for pointing out the problem.
- A bug was fixed in the NIBEND element that resulted in incorrect edge effects for `ANGLE<0`. This bug was apparently introduced in release 33.0.

- The `SCRAPER` element was not respecting changes to the `DIRECTION` or `INSERT_FROM` parameters made outside the lattice definition (e.g., using `alter_elements` or `load_parameters`). In addition, the interpretation of the `INSERT_FROM='x'` and `INSERT_FROM='y'` was incorrect, since these were supposed to correspond to a scraper inserted from both sides. Both problems were reported by forum user `Youssef`.
- The `SPEEDBUMP` element was not respecting changes to the `DIRECTION` or `INSERT_FROM` parameters made outside the lattice definition (e.g., using `alter_elements` or `load_parameters`).
- The `RFCA` element would bomb if no particles per present on a processor and `CHANGE_T=1`. This was found upon investigating a problem reported by G. Penn (ALS).
- The transport matrix for `BGGEXP` was being computed only to first order, which resulted in erroneous values for chromaticity, for example. This was reported by R. Linbderg (APS).
- When `CSRDRIFT` elements were divided using the `divide_elements` command or `element_divisions` parameter of the `run_setup` command, the length was saved incorrectly to the `parameters` file (requested from `run_setup`). This was reported by Pau Gonzalez.

### 13.5.2 Bug Fixes for Commands

- None.

### 13.5.3 New and Modified Elements

- The `CCBEND` element now has a `YAW` parameter that permits changing the entrance and exit angles in a coordinated fashion. It also supports the `FINT1`, `FINT2`, and `HGAP` parameters for soft-fringe effects, as well as explicit multipoles from octupole to 18-pole (in addition to the existing support for systematic multipole errors). The multipoles at the entrance and exit can now be specified separately, using the `EDGE1_MULTIPOLES` and `EDGE2_MULTIPOLES` parameters.
- The `FMULT` element, which provides a general multipole with content specified by an SDDS file, now affects matrix-based computations (e.g., twiss parameters, chromaticities, and transfer matrix).
- The `KSEXT` element now provides a parameter for a normal quadrupole error, in addition to the existing skew quadrupole error. The utility of this was pointed out by Y.-P. Sun (APS) and X. Huang (SLAC).
- The `BRANCH` element now provides periodic branching, which permits modeling a periodic bypass, for example. This improvement was triggered by a question from forum user `simone.dimitri`.
- The `global_settings` command now has user overriding of default values, which means that whenever the user changes a value, it becomes the new default for any subsequent instances of the command in that run.
- The `RFMODE` element has additional features that help refine the agreement between the voltage obtained by rf feedback and the effective voltage seen by the beam.
- The `WAKE` and `TRWAKE` elements now accept acausal wakes, provided the user explicitly allows it with the `ACAUSAL_ALLOWED` parameter. This feature will be requested by R. Lindberg (APS).

- The LSRMDLTR and CWIGGLER elements now include *experimental* capabilities providing a transverse gradient in undulators or wigglers. In both cases, hard-to-correct residual trajectory and dispersion effects are seen, which are not yet understood. For this reason, these features are considered experimental.

#### 13.5.4 New and Modified Commands

- The `matrix_output` command has two new parameters
  - `print_element_data` controls whether the element data is printed in addition to the matrices.
  - `printout_format` allows controlling the format of the printed elements.
- The `analyze_map` command has a new parameter, `printout_format`, allows controlling the format of the printed elements.
- The `correct_tunes` command has a new parameter, `update_orbit`, which allows controlling whether the orbit is updated during correction. The need for this arose from a problem encountered by I. Agapov (DESY).
- The `chromaticity` command has a new parameter, `update_orbit`, which allows controlling whether the orbit is updated during correction.
- The tracking used for matrix determination for elements, such as CCBEND, BGGEXP, and others, that rely on this, now takes advantage of parallel resources if `Pelegant` is used. This feature can be controlled using the newly-added `parallel_tracking_based_matrices` control in `global_settings`. The `global_settings` command also now offers the ability to control the number of points per phase space dimension that are used in matrix fitting, via the `tracking_matrix_points` parameter. The default value of this parameter has been set to 9—an increase from the minimalist value of 5 used in previous versions—in order to improve accuracy. Forum posts by J. Björklund Svensson (MAX-Lab) helped spur work on these features.
- The `insert_sceffects` command now supports averaging of beam size data turn-by-turn to reduce noise in transverse space charge simulation in rings, via the new `averaging_factor` parameter. This was suggested by V. Kornilov (GSI).

#### 13.5.5 Changes Specific to the MPI Parallel Version

- None.

#### 13.5.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.5.7 Changes to Related Programs and Files

- The `FTABLE` method for integration through 3D magnetic field maps now works in the `abrat` program via the `-ftable` commandline option. Previously, the control existed but resulted in no transformation of particles taking place.
- The program `abrat` now supports interpolation among multiple 2D field maps, which can be used, for example, to find the operating point in a magnet for which the field scales differently with current in different regions.
- For the `longitCalcs` script, the calculation of rf bucket height sometimes failed when a harmonic voltage was present; this was fixed. Also, the option to run without the GUI and put all results in a file was added.
- The `makeWigglerFromBends` script now includes the ability to add a gradient and specify the beam energy.
- A new program, `sdds4x4sigmaproc` is included that allows processing beam moments measurements from a quadrupole scan in a transport line to determine the 4x4 sigma matrix.

## 13.6 Highlights of What's New in Version 34.4.0

Here is a summary of what's changed since release 34.3.0.

### 13.6.1 Bug Fixes for Elements

- The `FTABLE` method for integration through 3D magnetic field maps now works in the `BRAT` element via the `USE_FTABLE` control. Previously, the control existed but resulted in no transformation of particles taking place.
- The `YAW` and `PITCH` parameters of the `LTHINLENS` and `LMIRROR` elements were overwriting the `TILT` parameters of the same elements.
- The `B7` and `B8` parameters of the `CSRCSBEND` elements were overwriting the `B6` parameter of the same element.

### 13.6.2 Bug Fixes for Commands

- The `share_tracking_based_matrices` feature, controlled by the `global_settings` command, now works correctly. This can provide a considerable increase in performance when tracking-based matrices are required for many beamline elements.
- The `insert_sceffects` command and `SCMULT` element, used for space-charge simulation in rings, had a bug that caused the sign of the tune shift to be wrong for protons and positrons. This was reported by forum user `hongjin`.

### 13.6.3 New and Modified Elements

- `MARK` elements with `FITPOINT=1` now create `psix` and `psiy` symbols for use in optimization, in addition to `nux` and `nuy`. This may be more intuitive for some users, as pointed out by forum user `jgarland`.

- When used for longitudinal feedback, the `TFBDRIVER` element now includes simulation of the feedback cavity resonance and driving circuit, using a circuit model developed by T. Berenc (APS).
- When K. Hwang’s fringe model is used for the `CSBEND` element, automatic adjustment of the `FSE` value can optionally be invoked in order to null out trajectory errors that result from the fringe fields extending outside the magnet. This is obtained by setting `FSE_CORRECTION=1`.
- The `TRACKING_MATRIX` parameter of `CSBEND` can now be used to control the order of the tracking-based matrix, with a limit of third order. This provides an alternative to the 2nd-order analytical matrix.
- The `CSBEND` element now supports separate edge integral values for the entrance and exit fringes, using the `FINT1` and `FINT2` parameters. If not given, the `FINT` parameter is used as before.
- The `CSBEND` and `CSRCSBEND` elements now support a new symplectic edge effects mode, based on the linear approach of K. L. Brown. It is similar to the existing, non-symplectic default mode, but in most cases users won’t see a difference.
- The `CSBEND`, `KQUAD`, `KSEXT`, `KOCT`, `KQUSE`, and `MULT` elements now support use of the expanded (to leading order) Hamiltonian by setting the `EXPAND_HAMILTONIAN` flag to 1. Note that no significant reduction in run time is observed with the expanded Hamiltonian.

#### 13.6.4 New and Modified Commands

- None.

#### 13.6.5 Changes Specific to the MPI Parallel Version

- None.

#### 13.6.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

#### 13.6.7 Changes to Related Programs and Files

- The `FTABLE` method for integration through 3D magnetic field maps now works in the `abrat` program via the `-ftable` commandline option. Previously, the control existed but resulted in no transformation of particles taking place.
- The program `abrat` now places the vertex, entry, and exit points (which are provided by the user) in the trajectory output file.

### 13.7 Highlights of What’s New in Version 34.3.0, June 14, 2018

Here is a summary of what’s changed since release 34.2.0.



### 13.7.1 Bug Fixes for Elements

- The CCBEND element had incorrect signs for the odd-order systematic multipoles when the bending angle was negative. There was also an issue with incorrect ordering of edge effects and coordinate transformations. R. Lindberg (APS) helped identify these problems.
- The KQUAD element had an issue with the order of the submatrices used for linear edge effects when tracking. This would cause small tune errors in tracking compared to the results of `twiss_output`.

### 13.7.2 Bug Fixes for Commands

- The beta-function scaling resulting from the `twiss_scaling=1` setting for the `elastic_scattering` command was incorrect. Although the tracking results would be correct, this made it more difficult to optimize run time.
- The `rf_setup` command now handles  $\alpha_c < 0$ , a deficiency that was reported by P. Piot (NIU/FNAL). It also now uses  $\eta = \alpha_c - 1/\gamma^2$  instead of  $\alpha_c$ , though this rarely makes a significant difference.
- The computation of exact normalized emittances, requested with the `global_settings` command, had several issues that were fixed. First, the values assigned to the horizontal and vertical corrected and uncorrected emittances were permuted. Second, in the serial version, the corrected emittances (with dispersive terms removed) were computed incorrectly. This would impact the `sigma` and `final` files from the `run_setup` command. J. Björklund Svensson (MAX-Lab) reported problems that helped find these bugs.

### 13.7.3 New and Modified Elements

- CCBEND has a new parameter, `EDGE_ORDER`, that allows controlling the order of edge kicks.
- BRANCH has a new parameter, `DEFAULT_TO_ELSE`, which allows determining how the element behaves when tracking for closed orbits and the like.

### 13.7.4 New and Modified Commands

- The `configuration` command-line argument was added, which allows specifying a configuration file to be read before processing the input file. This file can also be specified with the `ELEGANT_CONFIGURATION` environment variable.
- The `floor_coordinates` command now creates additional columns in the output file, giving data on the next element in the lattice. Given that data is only provided at the end of elements, this provides an easier way to determine information at the start of elements.
- The `insert_elements` command now has a parameter, `insert_before`, that allows controlling whether elements are inserted before or after (default) the specified locations.
- The `elastic_scattering` command now includes data that indicates warning conditions in the file specified by `log_file`.

### 13.7.5 Changes Specific to the MPI Parallel Version

- Read buffering was re-enabled for parallel I/O to avoid performance problems on GPFS file systems. Write buffering is still disabled, since this seems to prevent data corruption on some file systems. Users may wish to configure this for their file system using the new `ELEGANT_CONFIGURATION` environment variable.

### 13.7.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.7.7 Changes to Related Programs and Files

- The scripts `elasticScatteringAnalysis` and `inelasticScatteringAnalysis`—which are used to analyze data from the `elastic_scattering` and `inelastic_scattering` commands—were replaced with compiled programs of the same name, giving a large reduction in run time.
- The script `longitCalcs`, which does rf calculations using an output file from `twiss_output`, now supports a commandline mode that is convenient for use in other scripts.
- The script `computeQuadFringeIntegrals` was added. It computes the fringe integrals and effective length for a quadrupole from gradient vs z data, producing a file suitable for configuring KQUAD elements.
- A bug was fixed in `elegant2astra` that would affect results for particles that are not highly relativistic. Forum user Biaobin reported the bug and provided the fix.
- A bug was fixed in `smoothDist6s` that resulted in strange longitudinal phase space when the average value of `t` was very large compared to the spread in `t`. Forum user Marcello reported the bug.

## 13.8 Highlights of What's New in Version 34.2.0, March 22, 2018

Here is a summary of what's changed since release 34.1. Historical change logs are collected in Section 13.

### 13.8.1 Bug Fixes for Elements

- None.

### 13.8.2 Bug Fixes for Commands

- The `frequency_map` command was incorrectly computing the diffusion rate as

$$d_r = \frac{\log_{10}(\Delta\nu_x^2 + \Delta\nu_y^2)}{N}, \quad (162)$$

instead of

$$d_r = \log_{10}\left(\frac{\Delta\nu_x^2 + \Delta\nu_y^2}{N}\right), \quad (163)$$

- The `coupled_twiss_output` command would sometimes crash when `calculate_3d_coupling=0`.

### 13.8.3 New and Modified Elements

- None.

### 13.8.4 New and Modified Commands

- The `global_settings` command has two new fields, `mpi_io_force_file_sync` and `usleep_mpi_io_kludge`, which can be used to solved MPI I/O problems that appear on some file systems. Z. Pan (LBNL) brought the problems to our attention.
- The `floor_coodinates` command now ignores `MAXAMP` elements when computing combined vertex points of strings of dipoles.
- The `coupled_twiss_output` command did not compute the tunes of the two modes, as pointed out by G. Wei (TJNAF). This was addressed with assistance from V. Sajaev (APS).

### 13.8.5 Changes Specific to the GPU Version

The GPU version continues to be an alpha release and contains bugs. Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.8.6 Changes to Related Programs and Files

- The program `sddsbrightness` now correctly includes the effect of  $J_x$  and  $J_y$  on the x and y emittances when the `-coupling` option is used.
- Added the script `parmela2elegant`, to convert PARMELA beam data (ASCII format) to a form acceptable by `elegant`.
- Fixed error in the atomic mass of  $\text{CO}_2$  in the script `ionTrapping`.

## 13.9 Highlights of What's New in Version 34.1.0, 27 February 2018

Here is a summary of what's changed since release 34.0. Historical change logs are collected in Section 13.

### 13.9.1 Bug Fixes for Elements

- Restored the long-deprecated `DIRECTION` parameter for the `SCRAPER` element, as a convenience.
- Fixed a problem that caused the `SCRIPT` element to sometimes hang up in `Pelegant` if some processors did not have any particles after loading data from the script output file.
- The `UKICKMAP` element would sometimes fail to add synchrotron radiation effects during tracking even if asked; this would happen, for example, if there was no `twiss_output` or `matrix_output` command.

- The `WIGGLER`, `UKICKMAP`, `CWIGGLER`, and `GFWIGGLER` elements had an inconsistency in radiation integral computations, in that in some cases *gamma* was used when  $\beta\gamma$  was intended. The differences were very small for any practical case.
- The `BRAT` element and the `abrat` commandline program for tracking particles through 3D field distributions had an error in the initial coordinate transformation, discovered by R. Lindberg (APS). In practical use, the error seems to have had a negligible effect on results. Also, the element was treated as a drift for matrix computations; now, the matrix is determined by tracking (which can be time-consuming).
- Synchrotron radiation calculations for `KQUAD`, `KSEXT`, and `KOCT` had a bug that resulted in only the last component being computed. For example, if steering or higher multipoles were included, those would override the effect of the main field.
- Previously, when the `KQUAD` element was split (with the `divide_elements` command or `element_divisions` in the `run_setup` command), soft-edge effects would be replicated at the interior boundaries. This was fixed.
- Soft-edge effects on the `KQUAD` element were not exactly symmetric. This would, e.g., introduce a slight asymmetry into an otherwise symmetric lattice. This has been fixed.

### 13.9.2 Bug Fixes for Commands

- The `rf_setup` command could not handle  $\alpha_c < 0$ , as discovered using files provided by P. Piot (NIU/FNAL). This was fixed.
- The `analyze_map` command would crash if SDDS output was not requested. This was fixed.

### 13.9.3 New and Modified Elements

- The `CCBEND` element, which integrates symplectically in Cartesian coordinates through a straight-pole combined-function bending magnet, was added.
- The `BMXYZ` element, which integrates particles through straight-element 3D magnetic field maps, now includes misalignment parameters. Multiple `BMXYZ` elements that use the same field map will share the data internally to reduce I/O and memory requirements.
- The `EHKICK`, `EVKICK`, and `EHVKICK` elements now include the `RANDOM_MULTIPOLE_FACTOR` and `SYSTEMATIC_MULTIPOLE_FACTOR` parameters.
- The `BGGEXP` element can now handle bending magnets. The non-symplectic integrator was replaced with a new method that is more accurate. R. Lindberg (APS) did most of the work on this.

### 13.9.4 New and Modified Commands

- During tracking, particles are no longer checked against apertures after transitioning through zero-length elements that don't modify the aperture. This improves performance in lattices with many `MONI`, `MARK`, and similar elements.
- The `analyze_map` command can now output the matrix in SDDS format to second or third order, on request.

### 13.9.5 Changes Specific to the GPU Version

The GPU version continues to be an alpha release and contains bugs. Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.9.6 Changes to Related Programs and Files

- The program `sddsbrightness` now correctly includes the effect of  $J_x$  and  $J_y$  on the x and y emittances when the `-coupling` option is used.
- Added the script `parmel2elegant`, to convert PARMELA beam data (ASCII format) to a form acceptable by `elegant`.
- Fixed error in the atomic mass of CO<sub>2</sub> in the script `ionTrapping`.

## 13.10 Highlights of What's New in Version 34.0, 31 October 2017

Here is a summary of what's changed since release 33.1.1.

### 13.10.1 Bug Fixes for Elements

- A bug in the `IONEFFECTS` element was reported by J. Cavley (APS): when only one bunch was present, the electron beam coordinates were zeroed out.
- A bug in the `WATCH` element caused `elegant` to crash in `centroid` and `parameter` mode when the `WATCH` element was in a beamline branch that did not get executed on the first pass.
- In multi-step runs, the `STEERING_MULTIPOLES` input for the `EKICK`, `EHKICK`, and `EVKICK` elements was ignored except on the first step.

### 13.10.2 Bug Fixes for Commands

- A bug in the `ion_effects` command was reported by J. Cavley (APS): when only one bunch was present, the electron beam coordinates were zeroed out.
- The `center_arrival_time` feature of `sdds_beam` did not work correctly for the parallel version, as reported by Jonas Björklund.
- The `use_moments_output_values` qualifier of the `bunched_beam` command did not work for the parallel version.
- The `full_grid_output` mode of the `frequency_map` command provided incorrect results for the diffusion for particles that got lost.
- The `parameters` output file from the `run_setup` command incorrectly reported the length and angle of `CSBEND` elements when element division was invoked. This was reported by V. Sajaev (APS).
- The `amplification_factors` command now respects `link_elements` commands.
- The `tune_footprint` command now optionally runs in major action command mode. The inability to do so was pointed out by Y.-P. Sun (APS).

### 13.10.3 New and Modified Elements

- The long-deprecated `DIRECTION` parameter of the `SCRAPER` element has been removed; input files using the `SCRAPER` element will need to be updated to remove this parameter and replace it with equivalent `INSERT_FROM` parameter. One result is that the `SCRAPER` element can now support two-sided scrapers.
- Added the `SYSTEMATIC_MULTIPOLE_FACTOR`, `RANDOM_MULTIPOLE_FACTOR`, and `STEERING_MULTIPOLE_FACTOR` parameters to the `KQUAD`, `KSEXT`, and `KOCT` elements. These allow multiplying each of the indicated higher multipole contributions by a factor.
- Added `YAW` and `YAW_END` parameters to `UKICKMAP` element. It's useful in simulating canted insertion devices.
- Added the `SPEEDBUMP` element, which provides a new kind of aperture formed by a semi-circular bump protruding from one or both sides of the chamber.
- Added the `DX`, `DY`, and `DZ` misalignment parameters to the `EHKICK`, `EVKICK`, and `EKICK` elements. Also added `RANDOM_MULTIPOLES` parameter.

### 13.10.4 New and Modified Commands

- Added the `inelastic_scattering` command, which assists in computation of the inelastic gas scattering lifetime and the distribution of lost particles. This is only available in the parallel version.
- Added the `generation_interval` parameter to the `ion_effects` command to permit generation of ions only at every  $n^{th}$  bunch. This was suggested by J. Calvey (APS).
- Added the `ignore_elements` command, which allows instructing `elegant` to ignore specified elements in tracking. This can reduce overhead from “do-nothing” elements like markers and monitors.
- The `link_elements` command can now create the source element name by editing the target name.
- The `momentum_aperture` command now uses resources more efficiently for the parallel version when `output_mode=2`. In particular, it honors the user-provided minimum  $\delta$  values. In addition, the domain decomposition was revised to better equalize the workload of the processors.

### 13.10.5 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to check results against the serial or parallel versions and report issues to the developers.

- None.

### 13.10.6 Changes to Related Programs and Files

- Added the `inelasticScatteringAnalysis` script, a companion to the `inelastic_scattering` command in `Pelegant`. It allows computing the lifetime and local loss rates from inelastic gas scattering.

## 13.11 Highlights of What's New in Version 33.1.1, 25 July 2017

Here is a summary of what's changed since release 33.0.

### 13.11.1 Bug Fixes for Elements

- The `BGGEXP` element had a bug that prevented it from working when two elements used the same data file. This was fixed.
- The `BGGEXP` element refused to run if  $m = 1$  (dipole) was the main multipole, which prevented modeling wigglers. This was reported by forum user `Ji_Li` and was fixed.
- The `RFDF` element had a bug in computing the energy-dependence of the time of flight, as reported by Daniel Marx. This was fixed. The missing phase reference feature was also implemented.
- Using the third-order matrix of the `QUAD` element with `RADIAL=1` would result in a crash. This was fixed. Forum user `meisal` reported the bug.

### 13.11.2 Bug Fixes for Commands

- Fixed a bug in `load_parameters` related to the `allow_missing_elements` and `allow_missing_parameters` qualifiers. In runs with multiple `load_parameters` commands, only the last values of these parameters were used.
- Fixed a bug in saving parameters when elements are subdivided: the lengths of certain elements were incorrect in the saved file.

### 13.11.3 New and Modified Elements

- The `IONEFFECTS` element and the companion `ion_effects` command were added. These allow simulation of the interaction of the beam with residual gas ions. J. Calvey (ANL) did much of the work on these new features.
- Added `SLICE` element to provide turn-by-turn slice analysis.
- The `CSBEND` element now includes skew multipole errors up to eighth order. This involves newly-computed expressions for the fields in curvilinear coordinates, so slight numerical changes may be seen.
- The `KSEXT` and `SEXT` elements now support a skew-quad correction term. This was suggested by Z. Duan (IHEP).
- Synchrotron radiation effects were added to the `BGGEXP` element, so that radiation effects from essentially arbitrary fields can be included in both tracking and `moments_output` calculations. There are limitations as described in the manual page.
- Improvements were made to memory management for numerous elements, chiefly `CSBEND`, `CSRCSBEND`, `CWIGGLER`, `FRFMODE`, `FTRFMODE`, `RFMODE`, `SLICE`, `TFBDRIVER`, `TRFMODE`, `ZTRANSVERSE`, and `ZLONGIT`. This can dramatically decrease memory usage in some cases.
- The `TFBPICKUP` and `TFBDRIVER` elements (used for turn-by-turn feedback) now have start- and end-pass controls.

- The **MATTER** element now has start- and end-pass controls.
- To improve performance and simplify the code, the **SQRT\_ORDER** parameter on the **CSBEND**, **FMULT**, **KOCT**, **KQUAD**, **KQUSE**, and **KSEXT** elements is now nonfunctional. The default behavior (exact square roots) is unchanged.
- The **BMXYZ** element now has the option for classical synchrotron radiation. It can also check the divergence and curl of the fields to assess the quality of the field solution.
- Added the **BX** and **BY** parameters to the **BGGEXP** element, to allow imposing a uniform “external” magnetic field.
- It is now possible to interleave zero-length **LSCDRIFT** elements with **CSRCSBEND** elements with CSR fields building up through the successive **CSRCSBEND** elements. This was added following a related forum post by Aaron Fetterman.

#### 13.11.4 New and Modified Commands

- Added the **elastic\_scattering** command, which assists in computation of the elastic gas scattering lifetime and the distribution of lost particles. This is only available in the parallel version.
- Added **bpm\_output** option to the **correct** command, which provides optional output of beam position monitor readings after orbit or trajectory correction. This was suggested by V. Sajaev (APS).
- The **twiss\_output** command now records the location of the acceptance-limiting apertures in parameters **AxLocation** and **AyLocation**.
- The **track** command has a new field, **interrupt\_file**, which gives the name of a file to monitor as a semaphore to interrupt the tracking. If the file is created or updated during tracking, then tracking will terminate on completion of the next pass.

#### 13.11.5 Changes Specific to Parallel Version

- The **elastic\_scattering** command was added. It performs parallel tracking to determine the angular acceptance at a series of *s* locations. The data is intended for use with the script **elasticScatteringAnalysis**, which allows determination of the elastic gas scattering lifetime and loss distribution. This command is presently only available in **Pelegant**, due to the long runtime required.

#### 13.11.6 Changes Specific to the GPU Version

**The GPU version continues to be an alpha release and contains bugs.** Users are encouraged to test results against the serial or parallel versions.

- None.



### 13.11.7 Changes to Related Programs and Files

- The `computeGeneralizedGradients` script (used to prepare data for the `BGGEXP` element) did not work for odd multipole orders (e.g., dipole, sextupole, ...) or fields that are odd functions of  $z$ . This was reported by forum user `Ji_Li` and has been fixed, with the assistance of R. Lindberg (APS).
- The program `sddsmatchmoments` was added. It allows generating a particle distribution to match the moments from the `moments_output` command.
- The `LFBFfirSetup` script was added. It helps set up FIR filters for longitudinal turn-by-turn feedback.
- `touschekLifetime` can now use data from the `SLICE` element in `elegant` for slice-based lifetime computations.
- The script `removeBackDrifts` was added. It allows post-processing s-dependent files to remove negative drifts, which improves the appearance of plots and is needed for certain types of analysis.
- The program `sddsemitproc` now has the ability to specify the independent variable on the commandline. This was suggested by forum user `jan`.
- The `TBFfirSetup` script, which helps set up FIR filters for transverse turn-by-turn feedback, can now support filters with up to 30 terms.

## 13.12 Highlights of What's New in Version 33.0, March 3, 2017

Here is a summary of what's changed since release 32.0. Historical change logs are appended to the end of this manual.

This version includes an alpha release of GPU-enabled code. The original GPU code was developed by Tech-X corporation [51], with further work by R. Soliday (APS).

### 13.12.1 Bug Fixes for Elements

- The `SREFFECTS` element now correctly computes the equilibrium horizontal and vertical emittances when  $J_x \neq 1$ . Previously, the computation used an equation that implicitly assumes  $J_x = 1$ .
- The `MALIGN` element could cause spurious integer changes in the reported tunes if the `DZ` parameter was negative. This problem, reported by V. Sajaev (APS), was fixed.
- A memory management bug related to the systematic and random multipole data store was fixed. This in principle affected `KQUAD`, `KSEXT`, and other elements using the `SYSTEMATIC_MULTIPOLES` and `RANDOM_MULTIPOLES` features. In testing, no effect was in fact observed.

### 13.12.2 Bug Fixes for Commands

- The `correction_matrix_output` command command were ignoring the monitor calibrations (`MONI`, `HMON`, and `VMON`) values when `use_response_from_computed_orbits = 1`. This was reported by V. Sajaev (APS).

- The `steering_element` command no longer aborts even if the declared steering corrector appears not to kick the beam. This allows using unusual controls such as path length to steer the beam. This issue was pointed out by V. Sajaev (APS).
- The `load_parameters` and `save_lattice` commands incorrectly saved the edge angles and other edge-related quantities for bending magnets that were reflected. This issue was fixed. *Previously-saved parameter files should be modified (e.g., remove the edge parameters)* unless the magnets had the same parameters for the entrance and exit. This problem was reported by Y. Li (BNL).
- The `rf_setup` and `moments_output` commands will now run in a loop with `find_aperture`, `momentum_aperture`, and `frequency_map` operations, if set for per-step execution. Previously, this would only happen for the `track`, `analyze_map`, and `touschek_scatter` commands.

### 13.12.3 New and Modified Elements

- The `EKICK`, `EHKICK`, and `EVKICK` elements now support inclusion of multipole errors linked to the correction strength.
- The steering kicks and steering multipoles in the `KQUAD` element are now implemented in the body of the element, rather than at the ends.
- The `WATCH` element was improved so that the `dt` column in coordinate-logging mode and the `dCt` column in parameter- and centroid-logging modes are more useful. In particular, in normal cases these will now more reliably be centered on zero. One can also provide a reference frequency relative to which the reference time is defined. This improvement grew out of discussions with J. Calvey and T. Berenc (APS).
- The reported phases of the beam- and generator-induced parts of the voltage for the `RFMODE` element `RECORD` file are now computed using a method that should be more reliable. This improvement grew out of discussions with J. Calvey and T. Berenc (APS).
- The `RECORD` output from the `RFMODE` element now includes the phase of the net cavity voltage. This was requested by M. Venturini (LBNL).
- The `RFMODE` element now supports injection of noise into the rf source and low-level rf system. This is based on discussions with T. Berenc (APS).
- The `SCRIPT` element can now import `particleID` data from the script without attempting to use this information for lost-particle accounting. This provides better functionality when the `particleID` is used for other purposes, such as bunch membership.
- The `TFBPICKUP` and `TFBDriver` elements, used for bunch-by-bunch feedback, now allow 30-term FIR filters, up from 15 turns in earlier versions.
- The `TFBDriver` element now accepts specification of the frequency and phase of the driver cavity.
- Aperture enforcement inside `KQUAD`, `KSEXT`, `KOCT`, `KQUSE`, `CSBEND`, and `CSRCSBEND` elements has been improved. In particular, the `ELLIPTICAL`, `EXPONENT`, `YEXPONENT`, and `OPEN_SIDE` parameters of `MAXAMP` are now implemented. In addition, for the fourth-order integrator, the

apertures are no longer asserted at each integration step, but only after each slice (or “kick”, to use the misleading terminology of the element parameters).

- Added the `ALLOW_LONG_BEAM` parameter to the `ZLONGIT` and `ZTRANSVERSE` elements.

#### 13.12.4 New and Modified Commands

- The `bunched_beam` command can now be set to take the fully-coupled 6D bunch parameters from the calculations of the `moments_output` command, provided the latter is used to compute matched, equilibrium parameters. This was requested by forum user `duanz`.
- Added occurrence and positional filters for the `steering_element` command. This was requested by V. Sajaev (ANL).
- Several informational printouts for the `touschekScatter` command are no longer shown by default, but only if the `verbosity` control is set to a non-zero value. This makes short runs more efficient.
- Compared to previous versions, the lost-particle data file (`losses` file requested by the `run_setup` command) will exhibit changes in the order in which particles are recorded. This was a result of reworking the code for lost particle management.

#### 13.12.5 Changes Specific to Parallel Version

- None.

#### 13.12.6 Changes to Related Programs and Files

- The program `madto` was renamed `elegantto`, to more accurately reflect what it does. It will now translate `elegant` lattice files into MAD8 format.

### 13.13 Highlights of What’s New in Version 32.0, 5 Jan. 2017

Here is a summary of what’s changed since release 31.

#### 13.13.1 Bug Fixes for Elements

- None.

#### 13.13.2 Bug Fixes for Commands

- A bug was fixed in the `amplification_factors` command that resulted in a crash when the corrected amplification factors were requested. This was reported by S. DiMitri (ELETTRA).
- A bug was fixed for `twiss_output`, which was incorrectly reporting the quantities  $\frac{\partial \alpha_{x,y}}{\partial \delta}$  (parameters `dalphax/dp` and `dalphay/dp` in the output file) in some cases.

### 13.13.3 New and Modified Elements

- Added the **BRANCH** element, which permits branching between parts of a beamline based on the number of passes executed.
- Apertures specified using **MAXAMP** or an external aperture file (using the **aperture\_data** command) are now enforced inside **CSBEND** and **CSRCSBEND** elements. There may be small changes in, for example, momentum acceptance as a result of this, particularly when gradient dipoles are involved.
- The longitudinal location of losses inside **KQUAD** and **KSEXT** elements is now computed more accurately. Previously, it was simply the start of the element.
- Removed the non-functional **FRINGE** parameter of the **CSBEND** element.
- The **BGGEXP** (B-field Generalized Gradient Expansion) element now supports symplectic integration using an implicit method, implemented by R. Lindberg (APS).

### 13.13.4 New and Modified Commands

- Added **exclude** parameter to **chromaticity** command, allowing exclusion of some sextupoles that may match the list in the **sextupole** parameter.
- Added **alter\_at\_each\_step** and **alter\_before\_load\_parameters** parameters to the **alter\_elements** command, allowing better control of potential conflicts with **load\_parameters**.
- The random number generator seed is now permuted bitwise in order to add a greater level of apparent randomness. Thus, changing the seed by a small amount will now have a bigger effect on the sequences generated, making it easier to deliberately perform several runs with very distinct random values. This can be defeated using the **global\_settings** command by setting **inhibit\_seed\_permutation=1**. This issue was pointed out by V. Sajaev (APS).

### 13.13.5 Changes Specific to Parallel Version

- None.

### 13.13.6 Changes to Related Programs and Files

- **ionTrapping** — Added computation of the single-ion oscillation frequency.

## 13.14 Highlights of What's New in Version 31.0, 1 Oct. 2016

Here is a summary of what's changed since release 30.1.

### 13.14.1 Bug Fixes for Elements

- The **touschek\_scatter** command had a bug when random multipoles were used on **KQUAD** and **KSEXT** elements. In particular, these multipoles components were re-randomized for each **TSCATTER** element. This was discovered and fixed by A. Xiao (ANL).

- The implementation of edge effects in the **KQUAD** element was using  $x'$  and  $y'$  in place of  $q_x$  and  $q_y$ , and so was not symplectic. It also did not have the correct dependence on  $\delta$ . These issues were reported by R. Lindberg (ANL). A similar error was fixed in the implementation of edge effects for **CSBEND**; this was fixed by Y.P. Sun (ANL). Practically speaking, we haven't noticed any significant change in results.
- There was a bug in the evaluation of systematic multipoles when using the second-order integrator for **KQUAD** and **KSEXT**. The default fourth-order integrator did not have this issue.
- Higher-order path-length issues were fixed for the **BRAT** element. This issue was reported by R. Lindberg (ANL).
- The steering kick calibration factors are no longer ignored on the **KQUAD** element.
- The **BMXYZ** and **BMAPXY** elements lacked dependence on the momentum deviation  $\delta$ . This issue was reported by R. Lindberg (ANL).

#### 13.14.2 Bug Fixes for Commands

- None

#### 13.14.3 New and Modified Elements

- Added the **BGGEXP** element, which performs tracking through magnetic fields constructed from a generalized gradient expansion [50]. Although the integration is not symplectic, the fields satisfy Maxwell's equations exactly. A script, `computeGeneralizedGradients`, is provided to assist in preparing input for this element. Advice from M. Venturini (LBNL) was helpful in performing this work.
- Added separate specification of edge and body multipoles to the **KQUAD** and **KSEXT** elements.
- Added steering and steering multipoles to the **KSEXT** element.
- The **BMXYZ** element now allows independent specification of the insertion length and field map length.
- The code for the **KQUAD**, **KSEXT**, **MULT**, and **FMULT** was improved to prevent underflows that might occur in some odd cases, which would negatively affect accuracy.
- The **LSRMDLR** element now includes an option for a helical device. This was requested by forum user **zzhang** and implemented by Y.-P. Sun (ANL).
- Two additional parameters, **SampledParticles** and **SampledCharge** were added to **WATCH** files in coordinate mode. These are identical to **Particles** and **Charge**, respectively, except when the **FRACTION** parameter is  $< 1$ . In that case, the latter parameters give the values prior to sampling, while the new parameters give the parameters of the sampled fraction of the bunch. Previously, **Particles** and **Charge** changed as **FRACTION** was changed. *Note that scripts that use the **Particles** and **Charge** may need modification since the meaning has changed.* Y. Ding (SLAC) pointed out this issue.

#### 13.14.4 New and Modified Commands

- The `analyze_map` command can now report the map using canonical variables. It also has a user-controlled accuracy parameter that can be used to eliminate spurious matrix elements. R. Lindberg (ANL) helped with the development and testing.
- The `touschek_scatter` command now uses averaging of the loss rate over the interval between two `TSCATTER` elements instead of the local value at the element, which gives more accurate estimates of the distribution of scattered particles. This change requires that `TSCATTER` elements be inserted at the beginning and end of the beamline, which can be done using `add_at_end=1` and `add_at_start=1` in the `insert_elements` command. This was implemented by A. Xiao (ANL).
- The `modulate_elements` command now offers more control over verbose printouts, to help reduce the volume of uninformative printouts. It also provides user control of the buffer flushing interval for the `record` output file.
- The `insert_elements` command now has the option to insert an element at the beginning of the beamline.

#### 13.14.5 Changes Specific to Parallel Version

- None.

#### 13.14.6 Changes to Related Programs and Files

- The script `computeGeneralizedGradients` was added to assist in preparing input for the `BGGEXP` element.
- The scripts `elasticScatteringLifetime` and `bremsstrahlungLifetime` now support user-specified gas composition. The Z values for carbon and oxygen were mixed up in some places in these and related scripts, as pointed out by S. Tian (IHEP); this was fixed.
- The `ionTrapping` script now supports user-provided factors for inflating the emittance and energy spread.

### 13.15 Highlights of What's New in Version 30.1, 3 Aug. 2016

Here is a summary of what's changed since release 30.0

#### 13.15.1 Bug Fixes for Elements

- Fixed a bug in Touschek scattering simulation (`TSCATTER` element and `touschek_scatter` command) that resulted in the random multipole components of `KQUAD` and `KSEXT` elements being re-randomized for each `TSCATTER` element.

#### 13.15.2 Bug Fixes for Commands

- Fixed a bug introduced in `moments_output` computations when `CSBEND` elements were present with non-zero values of `ETILT`. Reported by V. Sajaev (ANL).

- Fixed a bug in Touschek scattering simulation (`TSCATTER` element and `touschek_scatter` command) that resulted in the random multipole components of `KQUAD` and `KSEXT` elements being re-randomized for each `TSCATTER` element.

### 13.15.3 New and Modified Elements

- Added edge multipoles to `KQUAD` element. This necessitated some rearrangement of the code, so results might be slightly different even if this feature is not invoked.
- Added I/Q mode feedback to the `RFMODE` element.

### 13.15.4 New and Modified Commands

- None.

### 13.15.5 Changes Specific to Parallel Version

- Implemented exact normalized emittance calculations for the `sigma` output file of the `run_setup` command and in `WATCH` output in `parameter` mode. J. Bjorklund pointed out the lack of calculations in the parallel version.
- Fixed bug in assignment of particle ID values when using Halton sequences in the `bunched_beam` command.

### 13.15.6 Changes to Related Programs and Files

- The program `abrat` (“Asymmetric Bend RAY tracing”) was added. It allows tracking electrons through 2- and 3-D magnetic field maps. It is a commandline version of the `BRAT` element.
- The script `ionTrapping` was added, providing simple ion trapping calculations for uniform bunch trains. J. Calvey (APS) helped with debugging.
- The script `computeSCTuneSpread` was added to allow computation of space-charge tune spread.
- The script `radiationEnvelope` now computes envelopes for central cone flux.

## 13.16 Highlights of What’s New in Version 30.0, 5 July 2016

Here is a summary of what’s changed since release 29.1:

### 13.16.1 Bug Fixes for Elements

- Fixed a memory leak in the `FTABLE` element.

### 13.16.2 Bug Fixes for Commands

- Fixed calculations of exact normalized emittance (error in equations) and implemented in parallel version. This bug impacted results in the **sigma** output file of the **run\_setup** command and in **WATCH** output in **parameter** mode. J. Bjorklund pointed out the lack of calculations in the parallel version and provided an example run that helped discover the problem with the serial version.
- The **diffusionRate** output from the **frequency\_map** command is now computed as  $\log_{10}((\Delta\nu_x^2 + \Delta\nu_y^2)/n)$  instead of  $(\log_{10}(\Delta\nu_x^2 + \Delta\nu_y^2))/n$ .
- Fixed a bug in **bunched\_beam** whereby the centroids for a shell-type beam were offset from zero. Reported by L. Emery (ANL).
- Fixed bug in **moments\_output** when bending magnets with non-zero **ETILT** are present. When this occurs, the number of slices for moments calculation is set to 1 for those elements, to avoid numerical problems with the vertical orbit.

### 13.16.3 New and Modified Elements

- Added the **LEFFECTIVE** parameter for **QUAD** and **KQUAD**, which provides a convenient way to change the effective length without changing the adjacent drift spaces. Also added the ability to turn off the linear fringe field effects while keeping the nonlinear part, and to multiply the nonlinear effects by a numerical factor.
- Added the **BMXYZ** element for straightforward integration through 3D field maps for straight elements.
- Added the **BRAT** element, which is similar to **BMXYZ** but accommodates curved elements. Elements may be asymmetric, e.g., longitudinal gradient dipoles.
- Added the **FACTOR** and **THRESHOLD** options to **FTABLE**. The former allows multiplying the fields by a user-defined factor. The latter allows specifying the magnitude of the field below which it is considered zero, which can help ensure numerical stability.
- The **FTABLE** element can accept the simple-to-create input files used by the **BMXYZ** element in addition to the original input format.
- Results that depend on the transport matrix will show small changes for elements for which the matrix is determined by tracking. The tracking-based method was modified to use a larger number of sample points, increasing the accuracy.

### 13.16.4 New and Modified Commands

- Added the **full\_grid\_output** parameter to the **frequency\_map** command, making it possible to display frequency maps using **sddscontour**.

### 13.16.5 Changes Specific to Parallel Version

- Implemented exact normalized emittance calculations for the **sigma** output file of the **run\_setup** command and in **WATCH** output in **parameter** mode. J. Bjorklund pointed out the lack of calculations in the parallel version.



- Fixed bug in assignment of particle ID values when using Halton sequences in the `bunched_beam` command.

### 13.16.6 Changes to Related Programs and Files

- The program `abrat` (“Asymmetric Bend RAY tracing”) was added. It allows tracking electrons through 2- and 3-D magnetic field maps. It is a commandline version of the `BRAT` element.
- The script `ionTrapping` was added, providing simple ion trapping calculations for uniform bunch trains. J. Calvey (APS) helped with debugging.
- The script `computeSCTuneSpread` was added to allow computation of space-charge tune spread.
- The script `radiationEnvelope` now computes envelopes for central cone flux.

## 13.17 Highlights of What’s New in Version 29.1, 3 March 2016

Here is a summary of what’s changed since release 29.0:

### 13.17.1 Bug Fixes for Elements

- Fixed bugs in `RECORD` output from `TRFMODE` element for multi-step, single-pass runs. This was fixed by A. Xiao (APS).

### 13.17.2 Bug Fixes for Commands

- The `replace_elements` command now respects quoted sequences in the new element definition.

### 13.17.3 New and Modified Elements

- `LRWAKE` now supports long-range quadrupole wakes. R. Lindberg (APS) provided helpful discussion in this implementation.
- `ILMATRIX` now supports second-order tune shift with amplitude as well as path-length dependence on amplitude.
- `TFBPICKUP` now supports horizontal and vertical offsets.
- Added logging of photon coordinates and angles to the `CSBEND` element. Works in serial mode only.
- `TRFMODE` now supports interpolation within bins, giving smoother results.

### 13.17.4 New and Modified Commands

- `alter_elements` now has a occurrence-skip parameter, which would allow for example changing every other member of a group of elements.
- `momentum_aperture` now allows specifying that `WATCH` elements remain active during momentum aperture determination.

- `frequency_map` was modified to include the path-length in the output file, which can be used to determine the dependence of the path length of the betatron amplitude.

### 13.17.5 Changes Specific to Parallel Version

- None.

### 13.17.6 Changes to Related Programs and Files

- The script `prepareTAPAs` was added, which allows processing files from `twiss_output` into a form that is accepted by the Android App TAPAs [46].
- The script `makeSummedCsrWake` was added, which allows making a CSR wake that sums up contributions from dipoles with various lengths and bending radii.
- The script `TFBFirSetup` was added, which allows generating FIR filters for turn-by-turn feedback using `TFBDRIVER` and `TFBPICKUP` elements.
- `ibsEmittance` can now perform intrabeam scattering calculations for non-gaussian longitudinal distributions.
- `computeCoherentFraction` now uses  $\lambda/4\pi$  for the radiation emittance to be consistent with `sddsbrightness`.
- `longitCalcs` now computes the bucket-half-height even when a harmonic cavity is powered.

## 13.18 Highlights of What's New in Version 29.0, 15 Jan. 2016

Here is a summary of what's changed since release 28.1:

### 13.18.1 Bug Fixes for Elements

- Fixed a bug in the `MATR` element that would crop up in multi-step runs, causing a crash or lock-up. This was reported by P. Emma (SLAC).
- Fixed a bug in the `RFMODE` element that resulted in a few percent error between the voltage seen by the beam and the feedback-regulated voltage. T. Berenc (ANL) helped resolve this.
- The output file feature was restored for the `FTRFMODE` element.
- The `TFBDRIVER` and `TFBPICKUP` feedback elements can now handle changes in the number of bunches.
- The drive limit for `TFBDRIVER` is now imposed after application of the filter, rather than before.
- The `KQUAD` element now has a valid associated transfer matrix for `RADIAL=1`. This bug was reported by forum user `libov`.

### 13.18.2 Bug Fixes for Commands

- The `touschek_scatter` command now behaves as a regular major action command, meaning that error generation, scanning, parameter loading, etc. behave as expected.
- Fixed a bug in the `correct_tunes` command that resulted in a crash when `n_iterations=0` and would also have resulted in invalid data in the log file for mixed element types. This was reported by V. Sajaev (ANL).
- Fixed a bug in the `chromaticity` command that resulted in a crash when `n_iterations=0` and would also have resulted in invalid data in the log file for mixed element types.
- Fixed a bug related to optimization of the chromatic derivative of `alpha_x`. The value provided was actually the chromatic derivative of `betax`. A related error gave incorrect results for the `use_linear_chromatic_matrix` mode of the `track` command.
- Previous versions of this manual indicated that the `find_aperture` command provided a quantity `Area` giving the dynamic aperture area for optimization. The quantity is in fact called `DaArea`. This was reported by S. Hilbrich (TU Dortmund).
- Fixed a bug in the optimization feature that resulted in the user's weighting factors being ignored. This was pointed out by A. Zholents (ANL).
- Fixed a bug in the `alter_elements` command that caused string values not to be reflected in the output file created with `save_lattice`. This was reported by T. Pulampong (SLRI/DLS).

### 13.18.3 New and Modified Elements

- Added nonlinear symplectic fringe field model to `CSBEND` and `CSRCSBEND`, based on theoretical work of K. Hwang (IU) [45]. The implementation was performed by Y. Sun (APS) with assistance from K. Hwang and M. Borland.
- Added `EKICKER`, `EHKICK`, and `EVKICK`, which provide various flavors of steering correctors using an Exact model. These may be used in place of the existing `KICKER`, `HKICK`, and `VKICK` elements. The need for this was pointed out by L. Yang (BNL).
- The `MATTER` element now supports arrays of slits. This can be used, for example, to model a double-slit spoiler for producing two pulses in an FEL.
- The `ECOL` and `RCOL` collimator elements now support an `INVERT` parameter to allow simulation of an obstruction instead of an opening.
- The output files from the `WATCH` element in centroid and parameter mode now contain the beam charge, provided that a `CHARGE` element is in the beamline.
- Elements that read multipole error files (e.g., `KQUAD` and `KSEXT`) now share data internally rather than each reading the data files separately. This provides a significant speed improvement for massively parallel execution in particular.
- The `MALIGN` element was improved to allow optionally applying misalignments to only part of the beam, based on the particle ID.
- The `RFMODE` element now has a feature that allows “muting” the rf generator on a specified pass, to simulate a trip of the rf source.

- The voltage “preloading” feature of the **RFMODE** element now works even when rf feedback is used.
- In order to eliminate problems with the parallel version, the **IBSCATTER** element no longer has a separate **CHARGE** parameter. Instead, the **CHARGE** element should be used.

#### 13.18.4 New and Modified Commands

- The **analyze\_map** command can now determine the nonlinear transport matrix up to third order based on tracking data, using the method described in [4]. Parallel tracking is used for this command in **Pelegant**. Previously, the analysis was limited to the linear matrix. Also, the terminal lattice functions and their chromatic derivatives are determined from the map for both transport lines and rings. This was requested by Y. Hao (BNL) and L. Yang (BNL).
- The **correct\_tunes** and **chromaticity** commands now include a weighting factor that results in minimization of the strength changes in the event that more than two families are provided for correction. (In the future this will be replaced with an SVD-based implementation.)
- Added to **closed\_orbit** and **correct** commands the ability to use multi-turn tracking to determine the approximate orbit. This was suggested by V. Sajaev (ANL), and is helpful when the orbit convergence is poor.
- The output in the **run\_setup** centroid file now contains the beam charge, provided that a **CHARGE** element is in the beamline.
- The **run\_control** command now includes a variable, **n\_passes\_fiducial**, that allows specifying a different number of tracking passes for fiducialization than for tracking. For ring fiducialization, this should probably always be 1.
- Most output files from **elegant** now include a parameter giving the SVN revision number of the version used to create the output.

#### 13.18.5 Changes Specific to Parallel Version

- The **analyze\_map** command, which was improved as described above, can now use parallel resources.
- A bug was fixed in the **center\_on\_orbit** feature of the **track** command. The bug caused the particles on each processor to be offset by different amounts related to the centroid of the local particles only. This was reported by M. Furseman (DLS).
- Fixed a bug in **FTABLE** introduced in version 26.0. The bug would cause the program to crash.
- Memory management was improved in the **touschek\_scatter** command, allowing a larger number of particles to be utilized.
- The **SCRIPT** element would cause a crash when **twiss\_output**, **matrix\_output**, or similar commands were included but when tracking was required to determine the transfer matrix of the element. This was fixed.
- Tracking instigated via the **track** command is now more forgiving of uneven particle losses among cores. In particular, the program should no longer crash if one core has lost all of its particles or all of the particles in a particular bunch.

- The `stop_tracking_particle_limit` feature of the `track` command now works in the parallel version.
- Instead of exiting, the parallel version now simply ignores the `slice_anlysis` command.

### 13.18.6 Changes to Related Programs and Files

- The script `reorganizeMmap` was added to convert momentum aperture data from `Pelegant` in `output_mode=1` into the same form as produced by `elegant`. This was a result of correspondence with S. Tian (IHEP).
- A bug was fixed in `elegant2astra` that resulting in slightly erroneous values for the longitudinal coordinate.
- The `beamLifetimeCalc` can now perform approximate Touschek lifetime calculations for polarized beams. This was added by A. Xiao (ANL) following an inquiry from forum user `marlibgin`.

## 13.19 Highlights of What's New in Version 28.1.0, 23 July 2015

Here is a summary of what's changed since release 28.0:

### 13.19.1 Bug Fixes for Elements

- The `ROTATE` element was not affecting the floor coordinates. This was found and fixed by A. Xiao (APS).
- The `END_PASS` parameter on `SCATTER` now works as expect, after removal of a one-pass offset.

### 13.19.2 Bug Fixes for Commands

- A bug was fixed that caused a crash when a 1-line aperture search was performed. This was reported by Guohui Wei (JLab).

### 13.19.3 New and Modified Elements

- The `TFBDriver` element now has the ability to measure the beam phase for use in longitudinal feedback. Previously, only momentum-based input was available for longitudinal feedback.

### 13.19.4 New and Modified Commands

- The `ramp_elements` and `modulate_elements` commands now have the ability to write a record of their output values.
- The `run_setup` command now has options, intended primarily for developers, to turn on memory usage and executing time monitoring during tracking.
- The units given for loss rate the output files from `touschek_scatter` were incorrect and were fixed. Results were not affected. (A. Xiao, ANL)

- The `tune_footprint` command was improved in several ways. It is now possible to ignore half-integer resonances. The upper and lower bounds of the chromatic tune footprints are now available for optimization. It's now possible to turn off either chromatic or amplitude tune footprint determination.
- The `optimization_setup` command allows suppressing particle tracking in order to improve performance in some unusual cases.
- The `correct_tunes` command can now utilize any element that has the K1 parameter.
- The `chromaticity` command can now utilize any element that has the K2 parameter.

### 13.19.5 Changes for Parallel Version Only

- Fixed a bug that affected tracking when orbit correction was used, `start_from_centroid=1`, and particle distribution was not random across processors.
- Warnings about  $\rho > 10^6$  m are now issued by the parallel version, as for the serial version.
- Memory usage logging to WATCH output files now sums the memory across all cores, rather than just the master core.
- A memory leak was fixed in the ZTRANSVERSE element that sometimes caused the program to crash. This was reported by R. Lindberg (ANL).
- The output of the beam charge in the ZLONGIT wake output file was corrected; previously, it only showed the charge on one core.
- The `frequency_map` command now provides an estimate of the time needed to complete.

### 13.19.6 Changes to Related Programs and Files

- The program `sdds bunchingfactor` is now part of the distribution.

## 13.20 Highlights of What's New in Version 28.0.0, 18 June 2015

Here is a summary of what's changed since release 27.1.0:

### 13.20.1 Bug Fixes for Elements

- The WATCH element was improved so that the `dCt` column (in parameter or coordinate mode) and `dt` column (in coordinate mode) no longer exhibit fictitious drift due to precision limitations in simulations of rings with many turns.
- For numerical reasons, any CSBEND with  $\rho > 10^6$  m is replaced with another element. In the past, an EDRIFT was used, which would produce incorrect results if the element had non-zero  $K_1$  or  $K_2$ . This was fixed.

### 13.20.2 Bug Fixes for Commands

- None.

### 13.20.3 New and Modified Elements

- The `TFBPICKUP` and `TFBDRIVER` elements, which provide a turn-by-turn feedback capability, now support multi-bunch feedback. In addition, support was added for longitudinal feedback as well as sample/update intervals greater than one turn.
- The `CSRDRIFT` element can now also include longitudinal space charge, using the algorithm from the `LSCDRIFT` element.
- The `CSBEND` element has a new feature that allows suppression of spurious trajectory offsets that result from limitations of the symplectic integration routine. This feature is controlled using the `REFERENCE_CORRECTION` parameter.
- The input of multipole errors for `KQUAD` and `KSEXT` elements was modified so that the input columns have more transparent names. Previously, the names caused some confusion. Files that worked with previous versions are still accepted.
- The `MARK` element with `FITPOINT=1` now stores the emittances of the three modes as `e1m`, `e2m`, and `e3m` for optimization if `moments_output` is invoked. This deficiency was pointed out by forum user marlibgin.

### 13.20.4 New and Modified Commands

- The `transmute_elements` command now does a better job of copying common parameters between the old and new element types. In the past, only the length was preserved. A. Zholents (ANL) reported this issue.
- The `floor_coordinates` command has a new parameter, `store_vertices`, which allows requesting that dipole vertex points be stored for use in optimization.
- The `twiss_output` command now stores the acceptances `Ax` and `Ay` for use in optimization.

### 13.20.5 Changes for Parallel Version Only

- None

### 13.20.6 Changes to Related Programs and Files

- None.

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