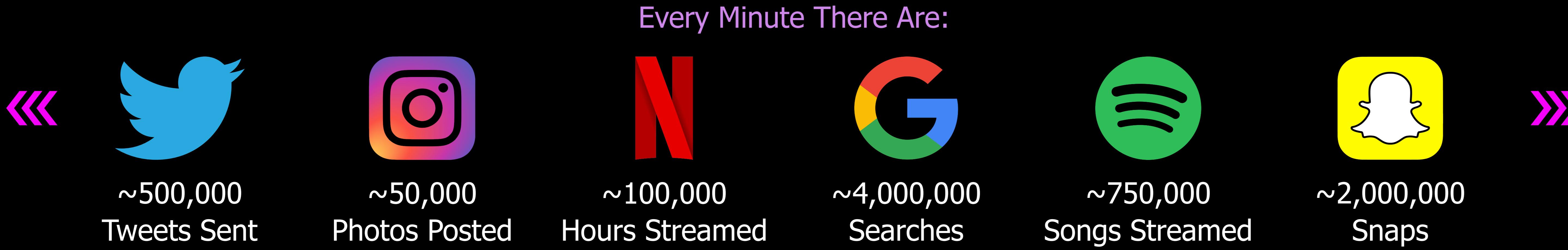




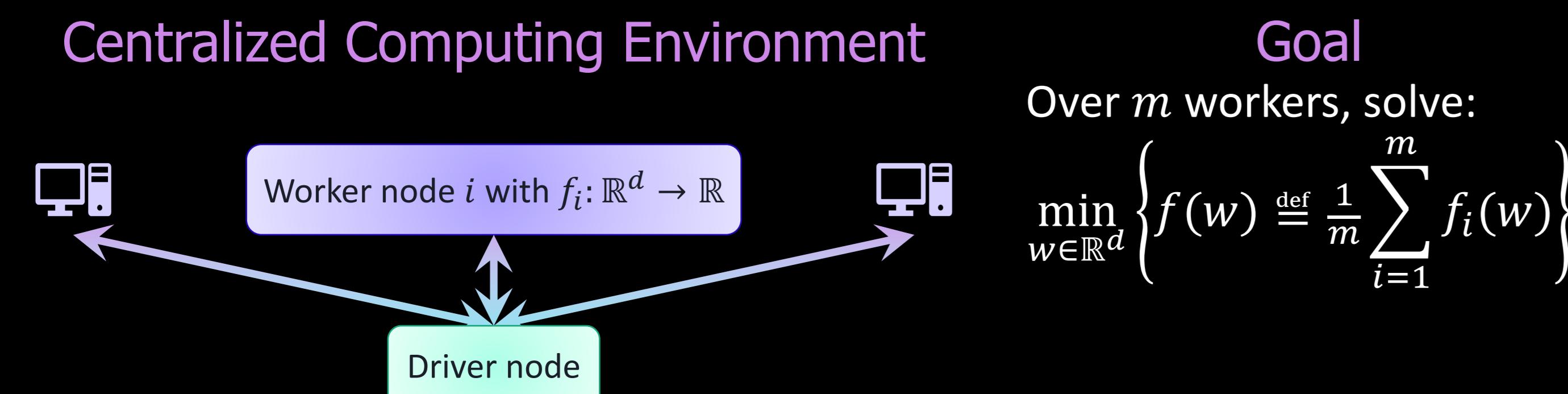
# DINGO: Distributed Newton-Type Method for Gradient-Norm Optimization

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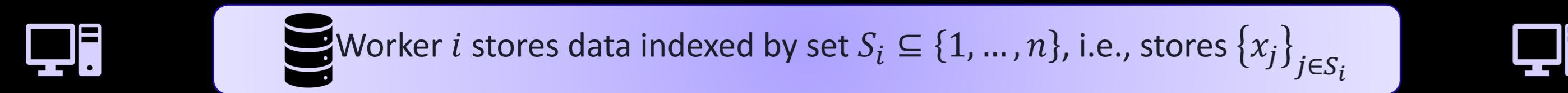


## The Problem



## Use Case: Big Data Regimes

Distributively Working With a Very Large Dataset  $\{x_i\}_{i=1}^n$



## Why use Second-Order Methods?

Second-order methods employ curvature (Hessian matrix) information to transform the gradient so that it is a more suitable direction to follow.

Benefits	
Perform more computations per iteration	
May take full advantage of available distributed computational resources	

Benefits	
May require significantly less communication costs	

## Our Method: DINGO

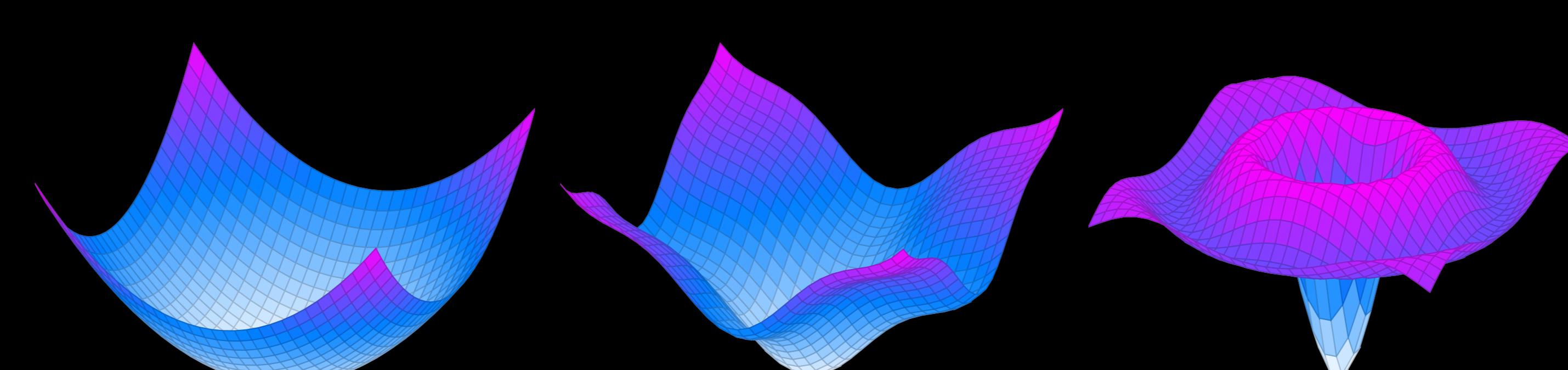
Derived by optimization of the gradient's norm as a surrogate function, i.e.,

$$\min_{w \in \mathbb{R}^d} \left\{ \frac{1}{2} \|\nabla f(w)\|^2 = \frac{1}{2m^2} \left\| \sum_{i=1}^m \nabla f_i(w) \right\|^2 \right\}.$$

DINGO is for “Distributed Newton-type method for Gradient-norm Optimization”. DINGO is particularly suitable for invex objectives. A strict linear-rate reduction in the gradient norm is always guaranteed.

## Related Work

Method	Applicable to Non-Convex Functions	Arbitrary Data Distribution	Arbitrary Form of $f_i$	Simple Sub-Problems	Not Sensitive to Hyper-Parameters
GIANT	✗	✗	✗	✓	✓
DiSCO	✗	✓	✓	✓	✓
DANE	✓	✓	✓	✗	✗
InexactDANE	✓	✓	✓	✗	✗
AIDE	✓	✓	✓	✗	✗
DINGO	✓	✓	✓	✓	✓



### Convex

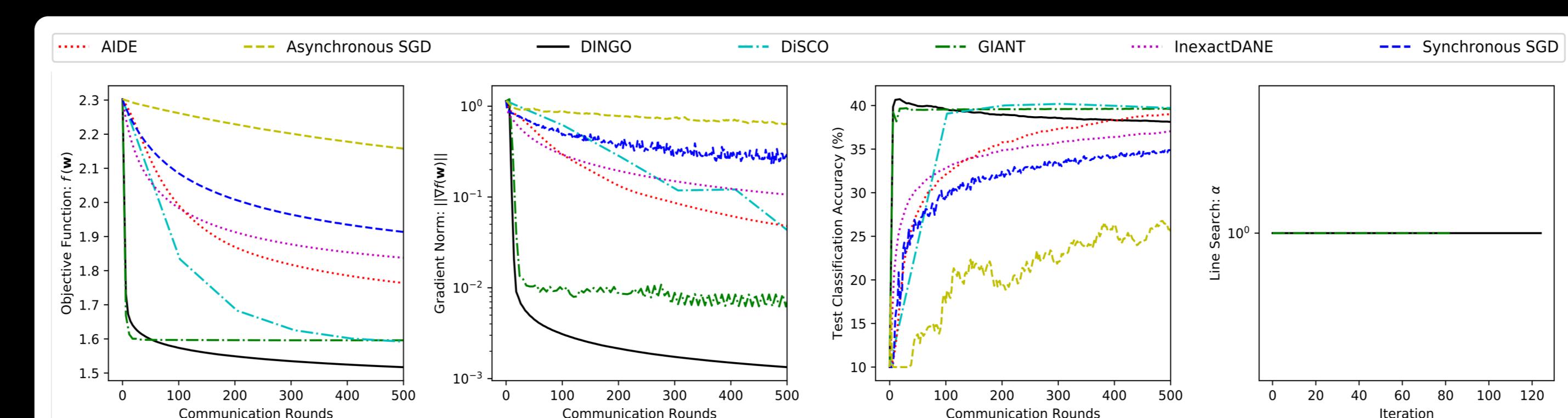
- Hessian is positive semidefinite.
- Local minima are global minima.

### Invex

- Hessian can be indefinite and singular.
- Local minima are global minima.

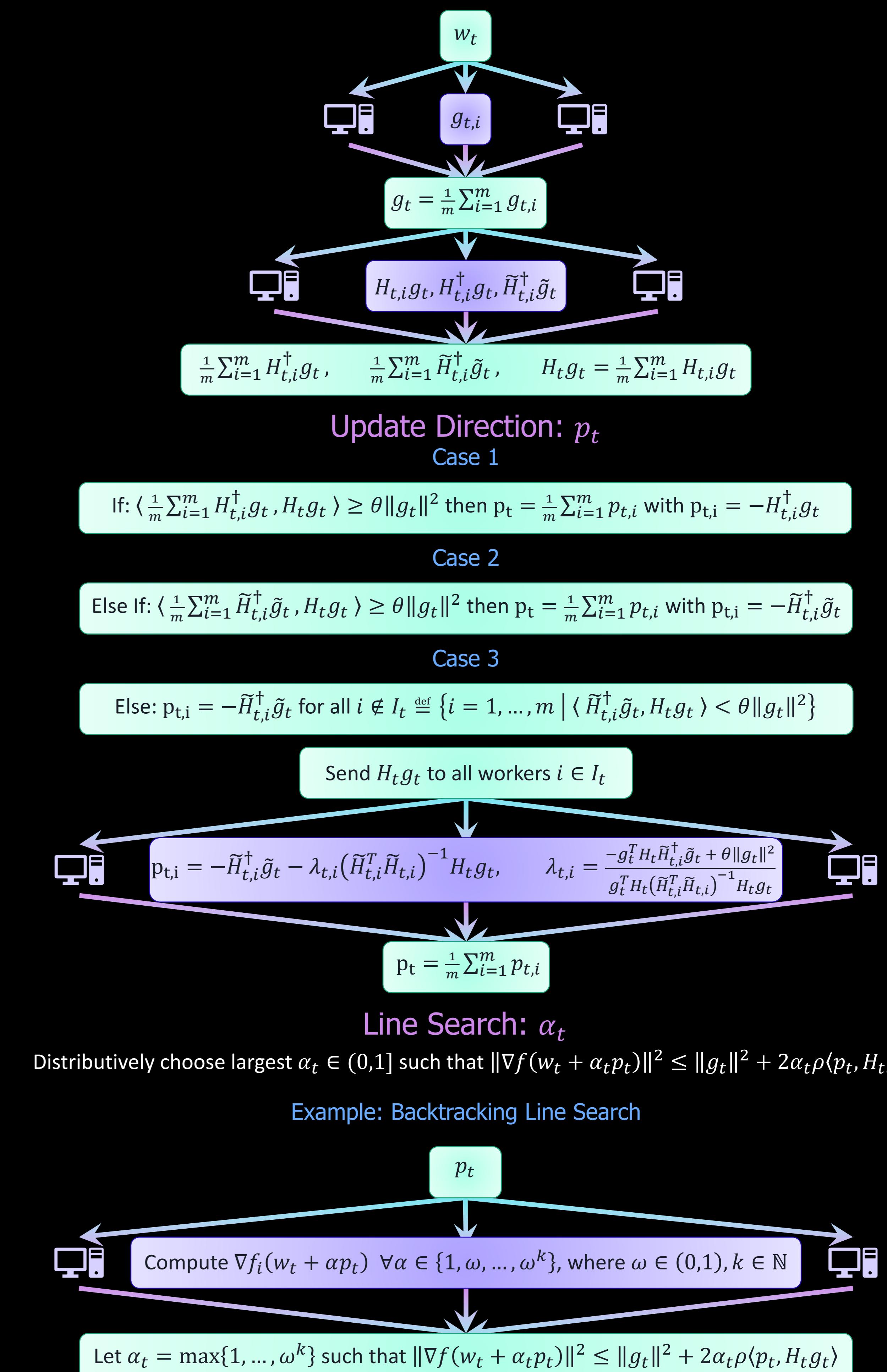
### Non-Convex

- Hessian can be indefinite and singular.
- Not all local minima are global minima.



Softmax regression, with regularization, problem on the CIFAR10 dataset.

## Each Iteration of DINGO



### Update

$$w_{t+1} = w_t + α_t p_t$$

The constants  $θ, φ > 0$  and  $ρ ∈ (0, 1)$  are hyper-parameters. The vector  $w_t ∈ ℝ^d$  denotes the point at iteration  $t$ . For notational convenience, we denote  $g_{t,i} \stackrel{\text{def}}{=} ∇f_i(w_t)$ ,  $H_{t,i} \stackrel{\text{def}}{=} ∇^2 f_i(w_t)$ ,  $H_t \stackrel{\text{def}}{=} ∇^2 f(w_t)$ . We also let  $\tilde{H}_{t,i} \stackrel{\text{def}}{=} [H_{t,i} \ I] ∈ ℝ^{2d × d}$ ,  $\tilde{g}_t \stackrel{\text{def}}{=} [g_t \ 0] ∈ ℝ^{2d}$ , where  $I$  is the identity matrix and  $0$  is the zero vector. Green and purple rectangles represent the driver node and worker nodes, respectively.