

Space complexity - It is defined as the amount of space and memory required by an algorithm to solve the problem.

$$S(P) = C + SP(\text{instance})$$

$S(P)$ = Space complexity
 C = fixed part

$SP(\text{instance}) \rightarrow$ variable part

Example.

(1) Algorithm abc (a, b, c)

{
 }
 }

return $a + b + b^*c + (a + b + c) / (a + b) + 4.0$

for every instance 3 words are required to store variable : a, b & c

\therefore Space complexity = 3

(2) Algorithm Sum (a[], n)

{

$S = 0;$
 for ($i = 1$ to n)
 $S = S + a[i];$
 return S;

}

space complexity = $n + 3$

To store $a[]$ = n words
 To store n = 1 word
 To store i & S = 2 words

There are three notations
O - Notation (upper bound)
 Ω - Notation

O - Notation (upper bound)
 $f(n) = O(g(n))$

In this $f(n)$ lies on or below $cg(n)$
where c is positive constant

Big O gives us formal way of expressing
upper bound.

Ω - Notation (lower bound)
 $f(n) = \Omega(g(n))$

In this $f(n)$ lies on or above $cg(n)$
where c is positive constant

Omega gives us a formal way of
expressing lower bound.

Θ - Notation (Same order)
 $f(n) = \Theta(g(n))$

In this $f(n)$ lies between $c_1 g(n)$
and $c_2 g(n)$ where c_1 and c_2 are
positive constant.

The theta notation is more precise
than both the big O(n) and
Omega notation.