

Step 1: Initialize Population

• Chromosomes (7 integers, 0-2 for Facility 1, 2, 3):

• $C_1: [0, 1, 2, 0, 1, 2, 0]$

• $C_2: [1, 0, 1, 2, 0, 1, 2]$

• $C_3: [2, 1, 0, 1, 2, 0, 1]$

• $C_4: [0, 2, 1, 0, 2, 1, 0]$

• $C_5: [1, 2, 0, 1, 2, 1, 2]$

• $C_6: [2, 0, 2, 1, 0, 2, 1]$

Step 2: Calculate fitness

• Fitness $1 / (\text{total cost} + 1000 \times \text{excess hours})$

• Cost: sum of $(\text{task time} \times \text{facility cost})$

$C_1: [0, 1, 2, 0, 1, 2, 0]$

• Facility 1 (0): Tasks 1, 4, 7

• Time $5 + 7 + 9 = 21 \leq 24$

• Cost: $(5 \times 10) + (7 \times 12) + (9 \times 11) = 50 + 84 + 99 = 233$

• Facility 2 (1): Tasks 2, 5

• Time $8 + 6 = 14 \leq 30$

• Cost $(8 \times 14) + (6 \times 13) = 112 + 78 = 190$

• Facility 3 (2): Tasks 3, 6

• Time $4+3 = 7 \leq 28$

• Cost: $(4 \times 7) + (3 \times 10) = 28 + 30 = 58$

• Total cost: $233 + 190 + 158 = 481$

• Fitness: $1/481 \approx 0.002079$

C2: [1, 0, 1, 2, 0, 1, 2]

• Facility 1 (0): Task 2, 5

• Time: $8+6=14 \leq 24$

• Cost: $(8 \times 15) + (6 \times 14) = 120 + 84 = 204$

• Facility 2 (1): Task 1, 3, 6

• Time $5+4+3=12 \leq 30$

• Cost: $(5 \times 12) + (4 \times 9) + (3 \times 8) = 60 + 36 + 24 = 120$

• Facility 3 (2): Tasks 4, 7

• Time: $7+9=16 \leq 28$

• Cost: $(7 \times 13) + (9 \times 13) = 91 + 117 = 208$

• Total cost: $204 + 120 + 208 = 532$

• Fitness: $1/532 \approx 0.001880$

• Facility 3 (2): Tasks 3, 6

• Time $4+3 = 7 \leq 28$

• Cost: $(4 \times 7) + (3 \times 10) = 28 + 30 = 58$

• Total cost: $233 + 190 + 58 = 481$

• Fitness: $1/481 \approx 0.002079$

C2: [1, 0, 1, 2, 0, 1, 2]

• Facility 1 (0): Tasks 2, 5

• Time: $8+6 = 14 \leq 24$

• Cost: $(8 \times 15) + (6 \times 14) = 120 + 84 = 204$

• Facility 2 (1): Task 1, 3, 6

• Time $5+4+3 = 12 \leq 30$

• Cost: $(5 \times 12) + (4 \times 9) + (3 \times 8) = 60 + 36 + 24 = 120$

• Facility 3 (2): Tasks 4, 7

• Time: $7+9 = 16 \leq 28$

• Cost: $(7 \times 13) + (9 \times 13) = 91 + 117 = 208$

• Total cost: $204 + 120 + 208 = 532$

• Fitness: $1/532 \approx 0.001880$

$$C_3: [2, 1, 0, 1, 2, 0, 1]$$

• Facility 1(0): Task 3, 6

• Time $4+3 = 7 \leq 24$

• Cost: $(4 \times 8) + (3 \times 9) = 32 + 27 = 59$

• Facility 2(1): Task 2, 4, 7

• Time: $8+7+9 = 24 \leq 30$

• Cost: $(8 \times 14) + (7 \times 10) + (9 \times 12) = 112 + 70 + 108 = 290$

• Facility 3(2): Tasks 1, 5

• Time: $5+6 = 11 \leq 28$

• Cost: $(5 \times 9) + (6 \times 12) = 45 + 72 = 117$

• Total cost: $59 + 290 + 117 = 466$

• Fitness: $1/466 \approx 0.002146$

$$C_4: [0, 2, 1, 0, 2, 1, 0]$$

• Facility 1(0): Tasks 1, 4, 7

• Time $5+7+9 = 21 \leq 24$

• Cost: $(5 \times 10) + (7 \times 12) + (9 \times 11) = 50 + 84 + 99 = 233$

• Facility 2(1): Tasks 3, 6

• Time: $4 + 3 = 7 \leq 30$

• Cost: $(4 \times 9) + (3 \times 8) = 36 + 24 = 60$

• Facility 3(2): Tasks 2, 5

• Time: $8 + 6 = 14 \leq 28$

• Cost: $(8 \times 16) + (6 \times 12) = 128 + 72 = 200$

• Total cost: $233 + 60 + 200 = 493$

• Fitness: $1/493 \approx 0.002028$

$C_5: [1, 2, 0, 1, 2, 1, 2]$

• Facility 1(0): Task 3

• Time: $4 \leq 24$

• Cost: $(4 \times 8) = 32$

• Facility 2(1): Task 1, 4, 6

• Time: $5 + 7 + 3 = 15 \leq 30$

• Cost: $(5 \times 12) + (7 \times 10) + (3 \times 8) = 60 + 70 + 24 = 154$

• Facility 3(2): Tasks 2, 5, 7

• Time : $8 + 6 + 9 = 23 \leq 28$

• Cost : $(8 \times 16) + (6 \times 12) + (9 \times 13) = 128 + 72 + 117 = 317$

• Total cost : $32 + 154 + 317 = 503$

• Fitness : $1/503 \approx 0.001988$

$C_6 : [2, 0, 2, 1, 0, 2, 1]$

• Facility 1(0): Tasks 2, 5

• Time : $8 + 6 = 14 \leq 24$

• Cost : $(8 \times 15) + (6 \times 14) = 120 + 84 = 204$

• Facility 2(1): Tasks 4, 7

• Time : $7 + 9 = 16 \leq 30$

• Cost : $(7 \times 10) + (9 \times 12) = 70 + 108 = 178$

• Facility 3(2): Tasks 1, 3, 6

• Time : $5 + 4 + 3 = 12 \leq 28$

• Cost : $(5 \times 9) + (4 \times 7) + (3 \times 10) = 45 + 28 + 30 = 103$

Total cost : $204 + 178 + 103 = 485$

Fitness : $1/485 \approx 0.002062$

Step 3: Selection (Roulette Wheel)

• Total fitness: $0.002079 + 0.001880 + 0.002146 + 0.002028 + 0.001988 + 0.002062 \approx 0.012183$

• Probabilities:

- $C_1: 0.002079 / 0.012183 \approx 0.171$
- $C_2: 0.001880 / 0.012183 \approx 0.154$
- $C_3: 0.002146 / 0.012183 \approx 0.176$
- $C_4: 0.002028 / 0.012183 \approx 0.166$
- $C_5: 0.001988 / 0.012183 \approx 0.163$
- $C_6: 0.002062 / 0.012183 \approx 0.169$

• Pairs (random picks):

- Pair 1: C_3, C_1
- Pair 2: C_6, C_4
- Pair 3: C_1, C_2

Step 4: Crossover (80%)

- Pair 1: $C_3[2, 1, 0, 1, 2, 0, 1], C_1[0, 1, 2, 0, 1, 2, 0]$

random = 0.6

• Point 4

• Child: $[2, 1, 0, 1, 1, 2, 0]$

• Child: $[0, 1, 2, 0, 2, 0, 1]$

Pair 2: $C_6 [2, 0, 2, 1, 0, 2, 1]$, $C_4 [0, 2, 1, 0, 2, 1, 0]$,
random = 0.5

Pair 4

Child 3: $[2, 0, 2, 1, 2, 1, 0]$

Child 4: $[0, 2, 1, 0, 0, 2, 1]$

Pair 3: $C_1 [0, 1, 2, 0, 1, 2, 0]$, $C_2 [1, 0, 1, 2, 0, 1, 2]$,

random = 0.9

No crossover: keep C_1, C_2

Step 5: Mutation (20%)

Child 1: $[2, 1, 0, 1, 1, 2, 0]$

Gene 3 (random = 0.15): Swap with gene 6 $\rightarrow [2, 1, 2, 1, 1, 0, 0]$

Child 1: $[2, 1, 0, 1, 1, 2, 0]$

Gene 3 (random = 0.15): Swap with gene

Child 3: $[2, 0, 2, 1, 2, 1, 0]$

Gene 5 (random = 0.1): Swap with gene 2 $\rightarrow [2, 0, 2, 1, 1, 2, 2, 0]$

Others: no mutations (random > 0.2)

Step 6: New Population

- Child 1 : $[2, 1, 2, 1, 1, 0, 0]$
- Child 2 : $[0, 1, 2, 0, 2, 0, 1]$
- Child 3 : $[2, 0, 1, 1, 2, 2, 0]$
- Child 4 : $[0, 2, 1, 0, 0, 2, 1]$
- C_1 : $[0, 1, 2, 0, 1, 2, 0]$
- C_2 : $[1, 0, 1, 2, 0, 1, 2]$

Repeat from Steps 3 to 6 until convergence
Convergence