

Objective: Implementation and analysis of 0-1Knapsack

0-1 Knapsack

Given weights and values of n items, put these items in a knapsack of capacity W to get the maximum total value in the knapsack. In other words, given two integer arrays $val[0..n-1]$ and $wt[0..n-1]$ which represent values and weights associated with n items respectively. Also given an integer W which represents knapsack capacity, find out the maximum value subset of $val[]$ such that sum of the weights of this subset is smaller than or equal to W . You cannot break an item, either pick the complete item or don't pick it (0-1 property).

Code:

```
def KnapSack(W, wt, val, n):
    K = [[0 for x in range(W + 1)] for x in range(n + 1)]

    for i in range(n + 1):
        for w in range(W + 1):
            if i == 0 or w == 0:
                K[i][w] = 0
            elif wt[i - 1] <= w:
                K[i][w] = max(val[i - 1] + K[i - 1][w - wt[i - 1]], K[i - 1][w])
            else:
                K[i][w] = K[i - 1][w]

    return K[n][W]

val = [60, 100, 120]
wt = [10, 20, 30]
W = 50
n = len(val)
print(KnapSack(W, wt, val, n))
```

The screenshot shows an IDE window titled "DAA Lab - 14_0-1 Knapsack Problem.py". The code defines a function `KnapSack(W, wt, val, n)` that calculates the maximum value for a knapsack of capacity `W` using items with weights `wt` and values `val`. The function uses a 2D array `K` for dynamic programming. The main code sets `val = [60, 100, 120]`, `wt = [10, 20, 30]`, and `W = 50`, then prints the result of `KnapSack(W, wt, val, n)`. The output of the program is displayed in the Run console as `220`.

```
def KnapSack(W, wt, val, n):
    K = [[0 for x in range(W + 1)] for x in range(n + 1)]

    for i in range(n + 1):
        for w in range(W + 1):
            if i == 0 or w == 0:
                K[i][w] = 0
            elif wt[i - 1] <= w:
                K[i][w] = max(val[i - 1] + K[i - 1][w - wt[i - 1]], K[i - 1][w])
            else:
                K[i][w] = K[i - 1][w]

    return K[n][W]

val = [60, 100, 120]
wt = [10, 20, 30]
W = 50
n = len(val)
print(KnapSack(W, wt, val, n))
```

Output:

220

This screenshot shows the same IDE window as above, but with the Run console expanded. It displays the command used to run the program: `C:\Users\Hp\anaconda3\python.exe "C:/Users/Hp/OneDrive/Desktop/Pdhai Stuff/Vth Sem/DAA Lab/14_0-1 Knapsack Problem.py"`. The output of the program is `220`, and the console also shows "Process finished with exit code 0".

Time Complexity: $O(N*W)$.

where 'N' is the number of weight element and 'W' is capacity. As for every weight element we traverse through all weight capacities $1 \leq w \leq W$.

Auxiliary Space: $O(N*W)$.

The use of 2-D array of size 'N*W'.