

# Vectors Assignment-1

Section 12th Math- Exercise 12.10.4.1

1. Find  $\left| \vec{a} \times \vec{b} \right|$  if  $\vec{a} = \hat{i} - 7\hat{j} + 7\hat{k}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$

**Solution:**

The given two vectors are  $\vec{a} = \hat{i} - 7\hat{j} + 7\hat{k}$  and  $\vec{b} = 3\hat{i} - 2\hat{j} + 2\hat{k}$   
Let

$$\vec{a} = \begin{pmatrix} A_1 \\ A_2 \\ A_3 \end{pmatrix} \quad \vec{b} = \begin{pmatrix} B_1 \\ B_2 \\ B_3 \end{pmatrix} \quad (1)$$

The cross product of vectors  $\vec{a}$  and  $\vec{b}$  is given as

$$\left| \vec{a} \times \vec{b} \right| = \begin{vmatrix} \vec{A}_1 & \vec{B}_1 \\ \vec{A}_2 & \vec{B}_2 \\ \vec{A}_3 & \vec{B}_3 \end{vmatrix} = \begin{vmatrix} 1 & 3 \\ -7 & -2 \\ 7 & 2 \end{vmatrix} \quad (2)$$

$$\left| A_1 \quad B_1 \right| = \begin{vmatrix} -7 & -2 \\ 7 & 2 \end{vmatrix} = -14 + 14 = 0 \quad (3)$$

$$(4)$$

$$\left| A_2 \quad B_2 \right| = \begin{vmatrix} 1 & 3 \\ 7 & 2 \end{vmatrix} = 2 - 21 = -19 \quad (5)$$

$$(6)$$

$$\left| A_3 \quad B_3 \right| = \begin{vmatrix} 1 & 3 \\ -7 & -2 \end{vmatrix} = -2 + 21 = 19 \quad (7)$$

$$(8)$$

$$(9)$$

$$\left| \vec{a} \times \vec{b} \right| = \sqrt{(-19^2) + (19)^2} \tag{10}$$

$$= \sqrt{2} \times 19 \tag{11}$$

$$= 19\sqrt{2} \tag{12}$$