

Calculo

$$a. f(x,y) = y^4 + 5xy^3$$

$$\frac{\partial f}{\partial x} = 5y^3$$

$$\frac{\partial f}{\partial y} = 4y^3 + 3(5x)y^2 = 4y^3 + 15xy^2$$

$$b. f(x,y) = x^2y - 3y^4$$

$$\frac{\partial f}{\partial x} = 2xy$$

$$\frac{\partial f}{\partial y} = x^2 - 12y^3$$

$$c. z = \ln(x+t^2)$$

$$\frac{\partial z}{\partial x} = \frac{1}{x+t^2} \cdot \frac{d}{dx} = \frac{1}{x+t^2} \cdot 1 = \frac{1}{x+t^2}$$

$$\frac{\partial z}{\partial y} = \frac{1}{x+t^2} \cdot \frac{d}{dx} (x+t^2) = \frac{1}{x+t^2} \cdot 2t = \frac{2t}{x+t^2}$$

$$d = z = x \cdot \sin(xy)$$

$$\frac{dz}{dx} = \frac{d}{dx} (x) \sin(xy) + x \cdot \frac{d}{dx} (\sin xy)$$

$$\sin(xy) + xy \cdot \cos(xy) =$$

$$\frac{dz}{dy} = \pi \cdot x \cdot \cos(xy) = x^2 \cos(\pi y) =$$