

Cálculo II

Integral Iterada

$$a = \int_0^2 \int_0^{z^2} \int_0^{y-z} (2x - y) dx dy dz$$

Integração (1)

$$\int_0^2 \int_0^{z^2} \int_0^{y-z} (2x - y) dx dy dz = \int_0^2 \int_0^{z^2} (x^2 - xy) \Big|_0^{y-z} dy dz$$

$$\int_0^2 \int_0^{z^2} \left((y-z)^2 - (y-z) - y \right) dy dz$$

$$\int_0^2 \int_0^{z^2} (-yz + z^2) dy dz$$

Integração (2)

$$\int_0^2 \int_0^{z^2} (-yz + z^2) dy dz = \int_0^2 \left(-\frac{y^2}{2} z + z^2 y \right) \Big|_0^{z^2} dz$$

$$\int_0^2 \left(-\frac{z^5}{2} + z^4 \right) dz$$

Coca-Cola

Integração ②

$$\int_0^2 \left(-\frac{z^5}{2} + z^4 \right) dz = \left(-\frac{z^6}{12} + \frac{z^5}{5} \right) \Big|_0^2$$

$$\left(-\frac{16}{3} + \frac{32}{5} \right) = \frac{16}{15}$$

$$\int_0^2 \int_0^{z^2} \int_0^{y-z} (2x-y) dx dy dz = \frac{16}{15}$$

$$b - \int_0^1 \int_y^{2y} \int_0^{x+y} (6xy) dz dx dy$$

$$\int_0^{x+y} 6xy dx = 3y (x+y)^2$$

$$\int_0^1 \int_y^{2y} 3y (x+y)^2 dy dz$$

$$\int_y^{2y} 3y (x+y)^2 dy = \frac{45y^4}{4} + 14xy^3 + \frac{9x^2y^2}{2}$$

$$\int_0^1 \left(\frac{45y^4}{4} + 14xy^3 + \frac{9x^2y^2}{2} \right) dz$$

$$\int_0^1 \int_y^{2y} \int_0^{x+y} (6xy) dz dx dy = 14y^3x + \frac{45y^4}{4} + \frac{9y^2x^2}{2}$$