



Engines, Energy and Environment Group



**POLITECNICO
DI TORINO**

Dipartimento
Energia

Fuel Consumption, CO₂ and NO_x Emissions of a Passenger Car over the NEDC and WLTC driving cycles

Engine Emission Control – Automotive Engineering

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07-10-2019

Rules for the Report



- You should not re-discover the wheel:
 - The report should include the main **equations, hypothesis, numeric results and images**
 - The introduction of this presentation **must not** be included in the report with different words.
- Pay attention
 - to the shape of the pictures:
 - Axis/Fonts dimensions
 - Dimension of the lines
 - Table of numeric results ➔ significant digits
- The reports should be uploaded **at least 5 working days before the exam**



03EXGNE - Propulsori termici

Crediti: 10 cfu
Periodo: 1-1

Precedenze:
Esclusioni:

Avvisi / Materiale / Forum / Studenti / Elaborati

Consegna Elaborati (?)

In fase di scaricamento, al nome dei file verrà aggiunto un prefisso composto da "anno accademico"_"cognome studente"_"username studente": (esempio: "2016_ROSSI_S123456_nome_originale.zip")

E' stata introdotta la possibilità per lo studente di richiedere la cancellazione dei propri elaborati. Tali file compariranno nell'elenco sottostante barrati e contrassegnati dal simbolo ☒, in fase di download verrà inoltre loro aggiunto il prefisso "deleted_".

Nessun file inserito per questo incarico (227890)

[Accedi all'Archivio](#) [Accedi all'Archivio Elaborati zip](#)

Agenda



- Introduction
- Goal of the Exercise
- Vehicle Model Building
- Model Limits
- CO₂ Legislation Targets
- Post-Processing

Agenda



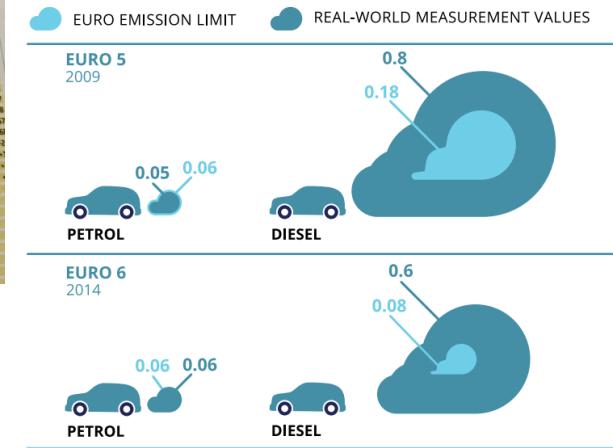
- Introduction**
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Real vs Declared Emissions/Fuel Consumption

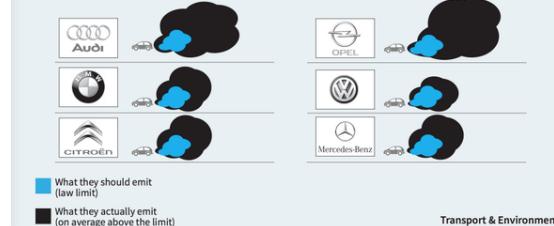


Comparison of NO_x emissions and standards

Nitrogen oxide emissions (in g/km)



Above and beyond the safe limit



THE FUEL ECONOMY GAP

Ten of the biggest miles per gallon differences

Car tested	Official mpg	'True mpg'	Difference
Kia Picanto 1.0 2	67.3	41.2	26.1
Ford Focus Estate 1.6 TDCi 115 Titanium	67.3	42.3	25
Peugeot 3008 Hybrid4 104g	70.6	46	24.6
Ford Focus 1.6 TDCi 115 Zetec	67.3	43.1	24.2
Volkswagen Golf 1.6 TDI 105 Bluemotion	74.3	51.8	22.5
Hyundai i30 1.6 CRDi Active	76.3	54.4	21.9
Mini 1.6D Cooper	74.3	52.5	21.8
Nissan Micra 1.2 DIG-S Shiro	65.7	44.1	21.6
VW Jetta 1.6 TDI 105 Bluemotion Technology S	67.3	48.4	18.9
Toyota Prius 1.8 VVT-i T Spirit (before facelift)	70.6	52.2	18.4

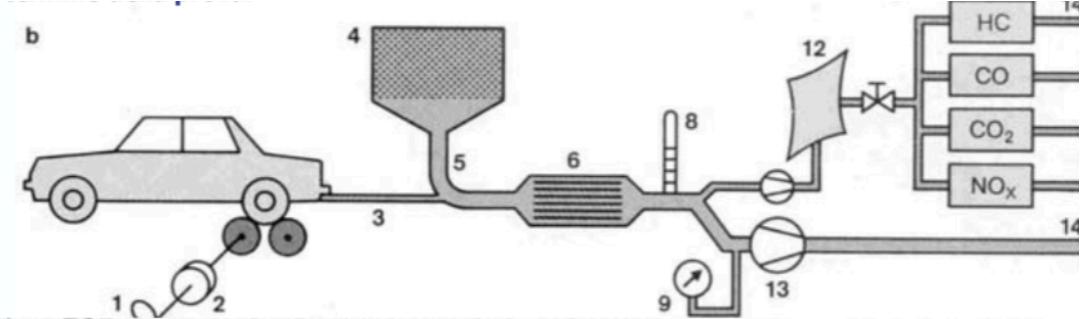
Source: What Car?

Luciano Rolando

Fuel Consumption, CO₂ and NO_x Emissions of a Passenger Car over the NEDC and WLTC driving cycles

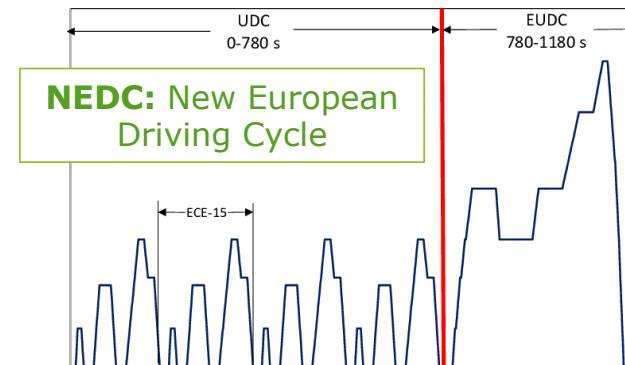
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Test Bench Measurements



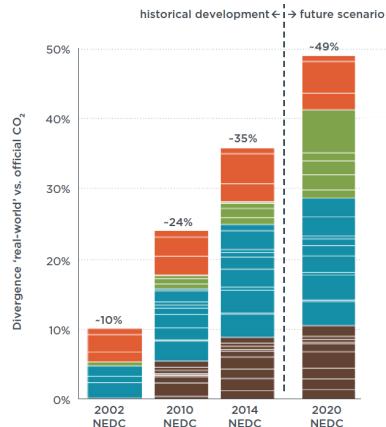
b) per ECE, Giappone, Svezia, Svizzera, Australia, Messico (qui con compressore rotativo).
1 Freno, 2 massa volanica, 3 gas di scarico, 4 filtro aria, 5 aria di diluizione, 6 radiatore, 7 venturimetro di prelievo, 8 temperatura gas, 9 pressione, 10 venturimetro, 11 elettroventilatore, 12 contenitore di raccolta, 13 compressore rotativo, 14 allo scarico.

Constant Speed Pattern → it is expected to represent real world driving conditions

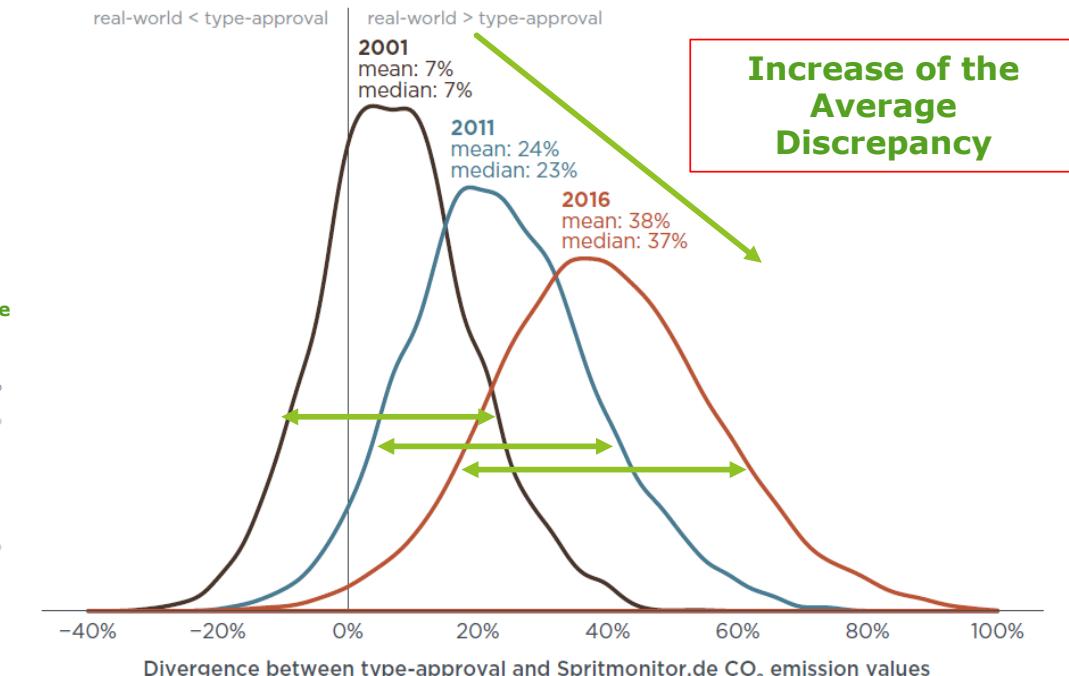
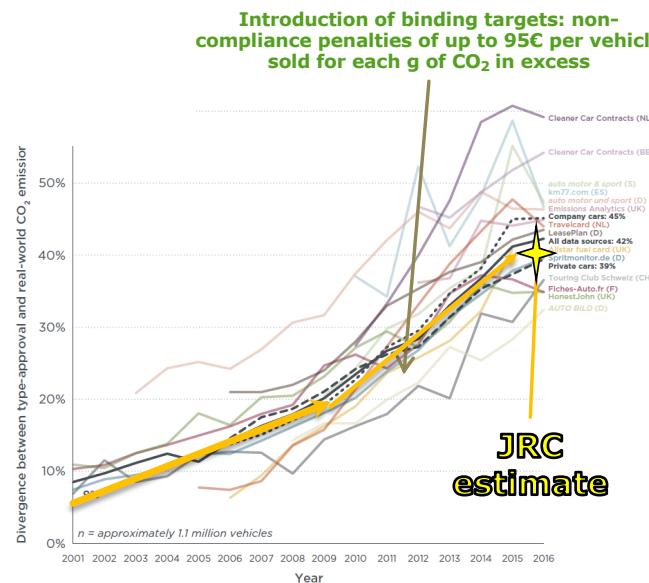


NEDC vs Real World - Discrepancy

Increasing Gap between Type Approval and average real-world CO₂



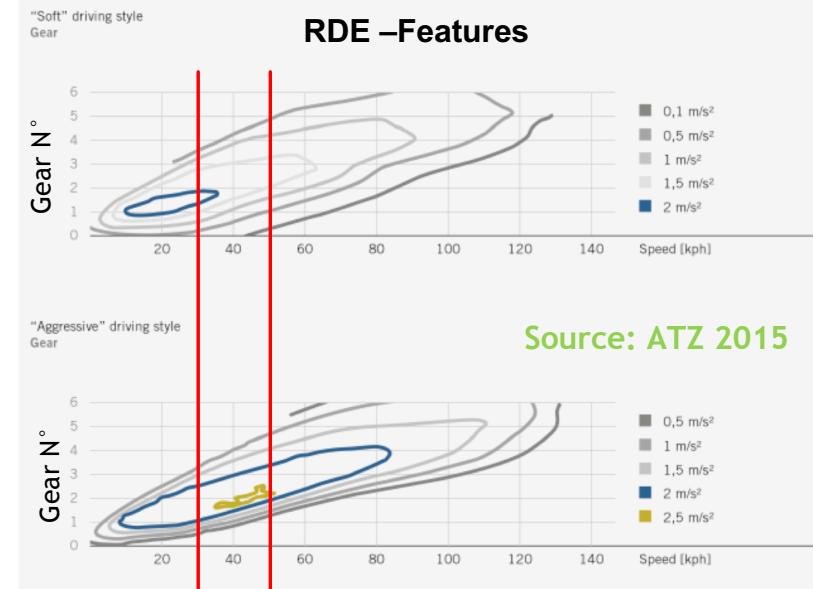
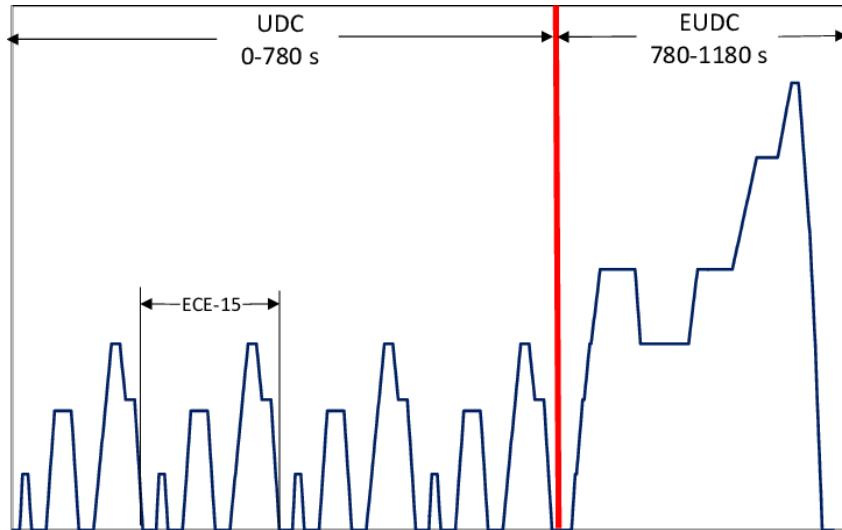
Source: ICCT 2015



real-world individual variability increasing with time

Source: ICCT 2016

NEDC vs Real World - Discrepancy



Characteristics	Unit	ECE 15	EUDC	NEDC†
Distance	km	0.9941	6.9549	10.9314
Total time	s	195	400	1180
Idle (standing) time	s	57	39	267
Average speed (incl. stops)	km/h	18.35	62.59	33.35
Average driving speed (excl. stops)	km/h	25.93	69.36	43.10
Maximum speed	km/h	50	120	120
Average acceleration ¹	m/s ²	0.599	0.354	0.506
Maximum acceleration ¹	m/s ²	1.042	0.833	1.042

† Four repetitions of ECE 15 followed by one EUDC
1 Calculated using central difference method

NEDC Avg. Spd



NEDC vs Real World - Discrepancy

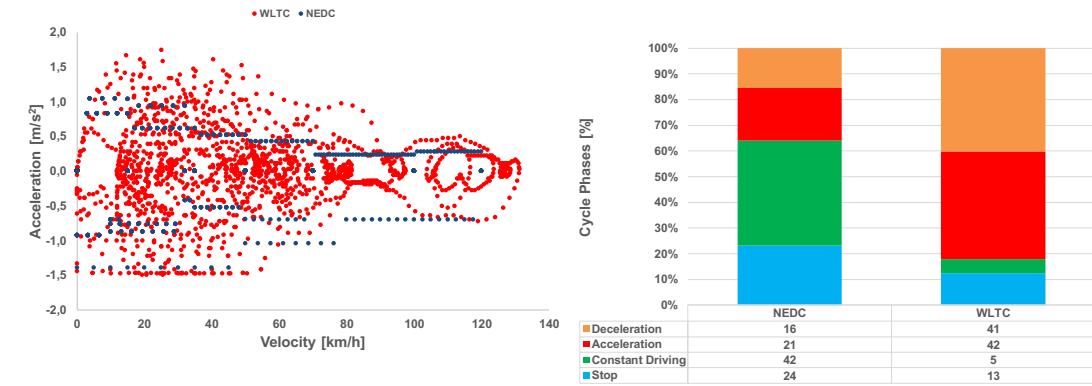
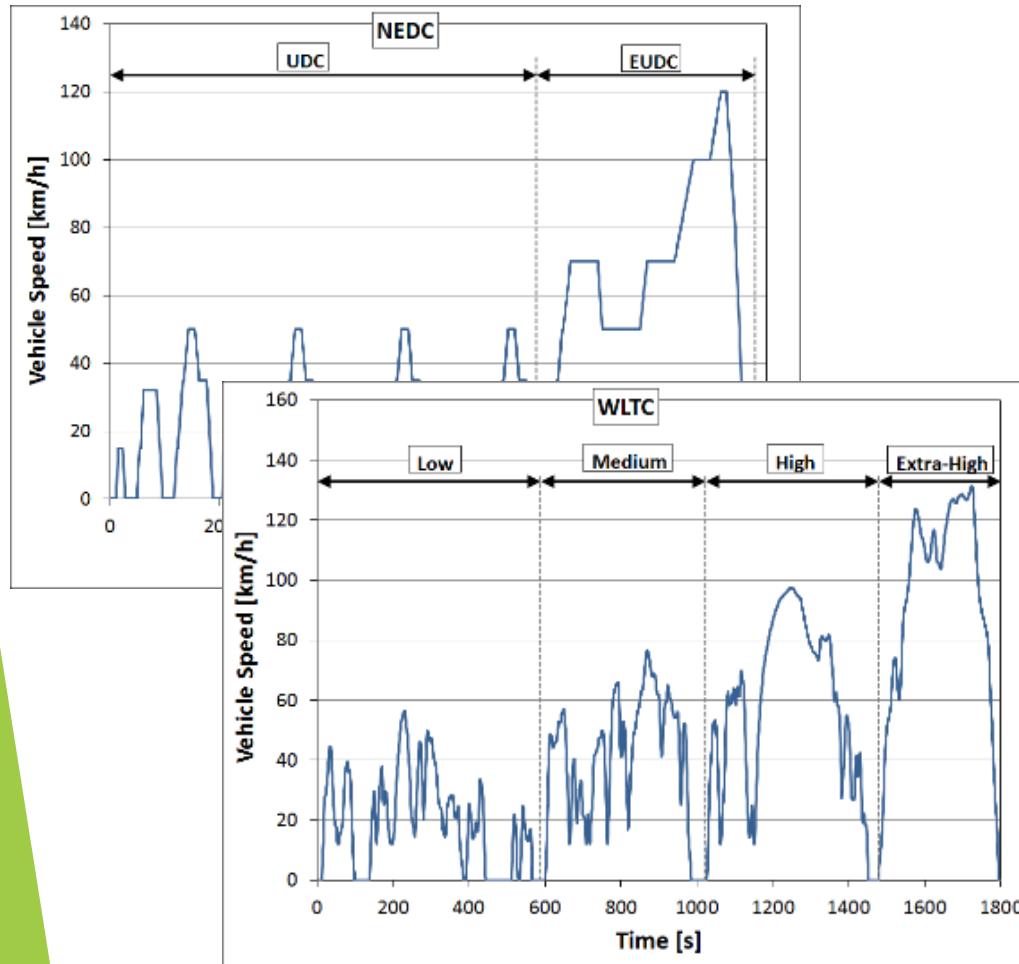


The lack of correlation with

1. Real world driving, which is due to more aggressive driving.
2. *Real world vehicle masses*
3. Road incline;
4. Environmental conditions.

and different driving patterns, e.g. accelerations/decelerations

NEDC → WLTP



NEDC → WLTP

Category	Item	in NEDC	in WLTP	Impact on CO ₂
Road Load Determination	Vehicle test mass	Present	Modified	↑
	Tire selection	Present	Modified	↑
	Tire pressure	Present	Modified	↑
	Tire tread depth	Present	Modified	↑
	Calculation of resistance forces	Present	Corrected	↑
	Inertia of rotating parts	Absent	Introduced	↑
Laboratory test	Driving cycle	Present	Modified	±
	Test temperature	Present	Modified	↑
	Vehicle inertia	Present	Modified	↑
	Preconditioning	Present	Modified	↑
	Gear Shift strategy	Present	Modified	↓
Post-processing test results	SOC correction	Absent	Introduced	↑
	Correction of speed and distance	Absent	Under discussion	±
Declared value	Declaration of CO ₂ emissions	Present	Modified	↑

$$TM_{EU} = UM + 100$$

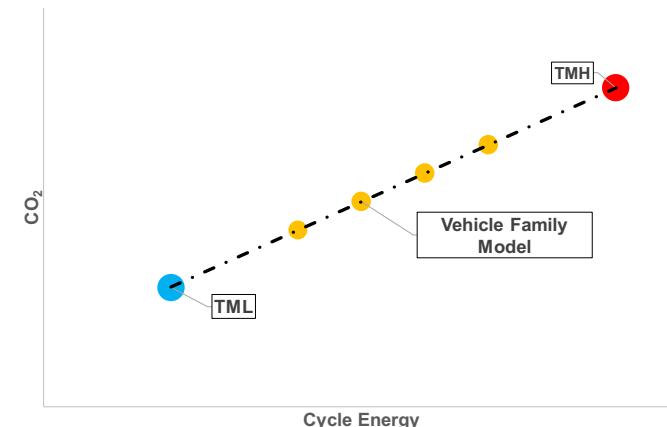
$$TM_H = UM + OM + 100 + 0,15 * (LM - UM - OM - 100)$$

Where:

- UM is the curb mass of the vehicle
- OM is the mass of optional equipment
- LM is the technically permissible laden mass

WLTC features

- Higher vehicle test mass (optional equipment)
- Higher & realistic road loads



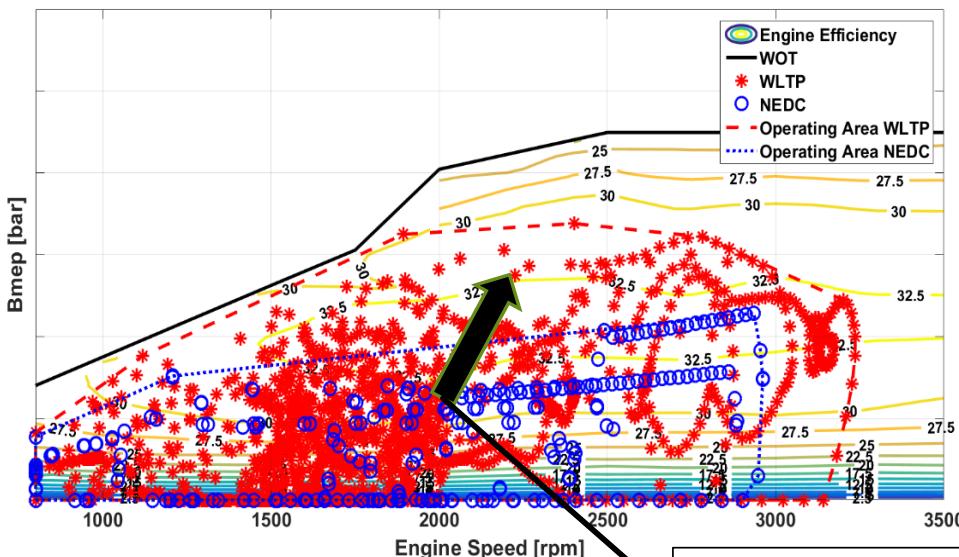
In particular 2 tests are considered:

- The **Test Mass Low** (TML) requires the lowest amount of energy to drive the test cycle, which has no optional equipment, lowest rolling resistance and least aerodynamic drag
- The **Test Mass High** (TMH) is equipped with all the optional equipment and it has the highest rolling resistance and the aerodynamic drag.

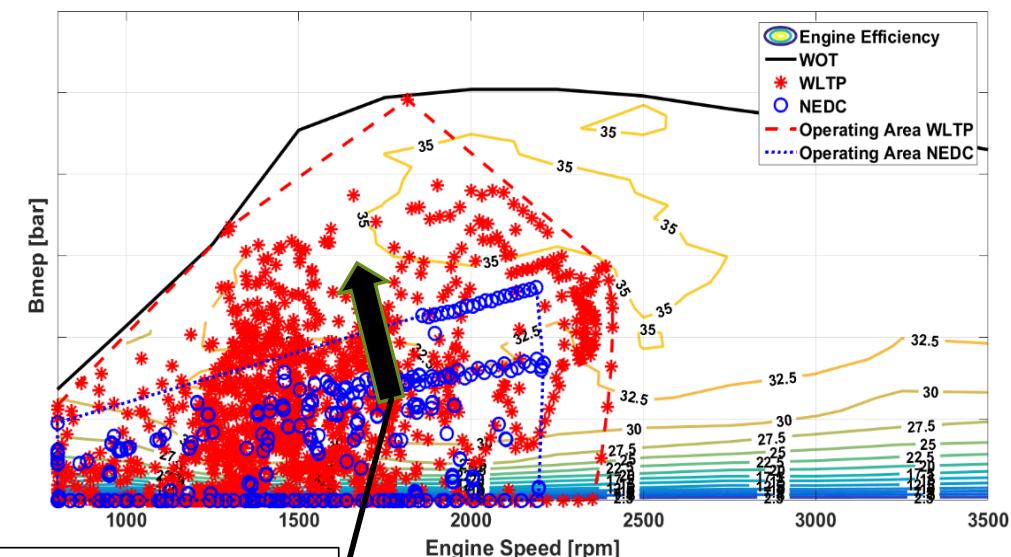
NEDC → WLTP

	Vehicle 1 (SI)	Vehicle 2 (CI)
NEDC	149 g/km	120 g/km
WLTP	164 g/km	149 g/km
Δ	+10%	+24%

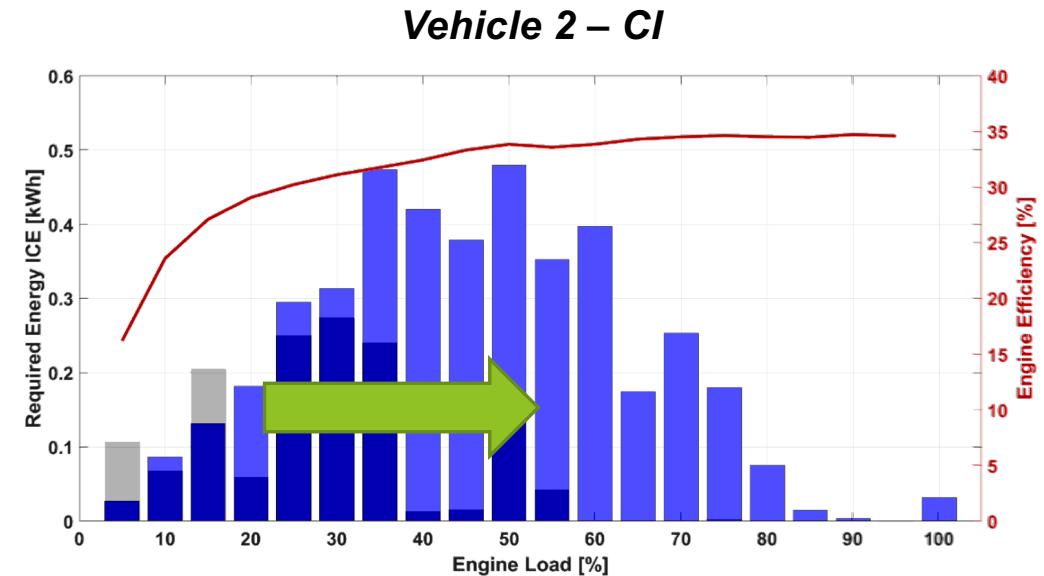
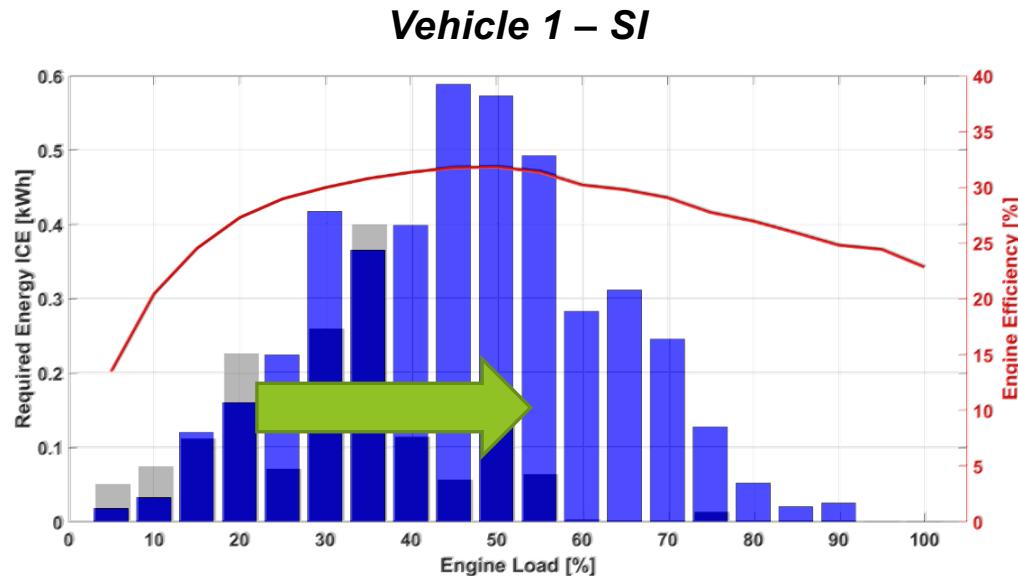
Vehicle 1 – SI



Shift of the engine operating points
towards higher efficiency regions

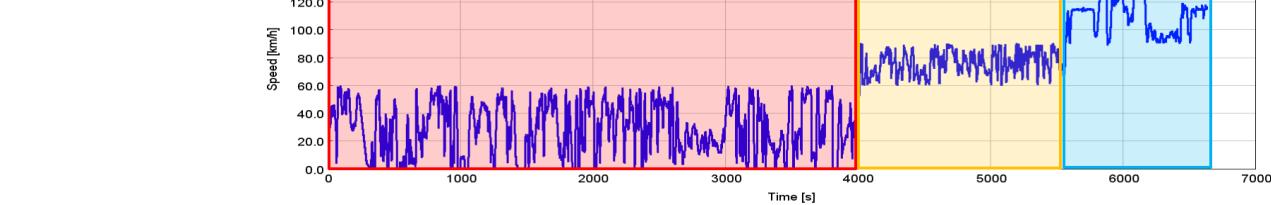
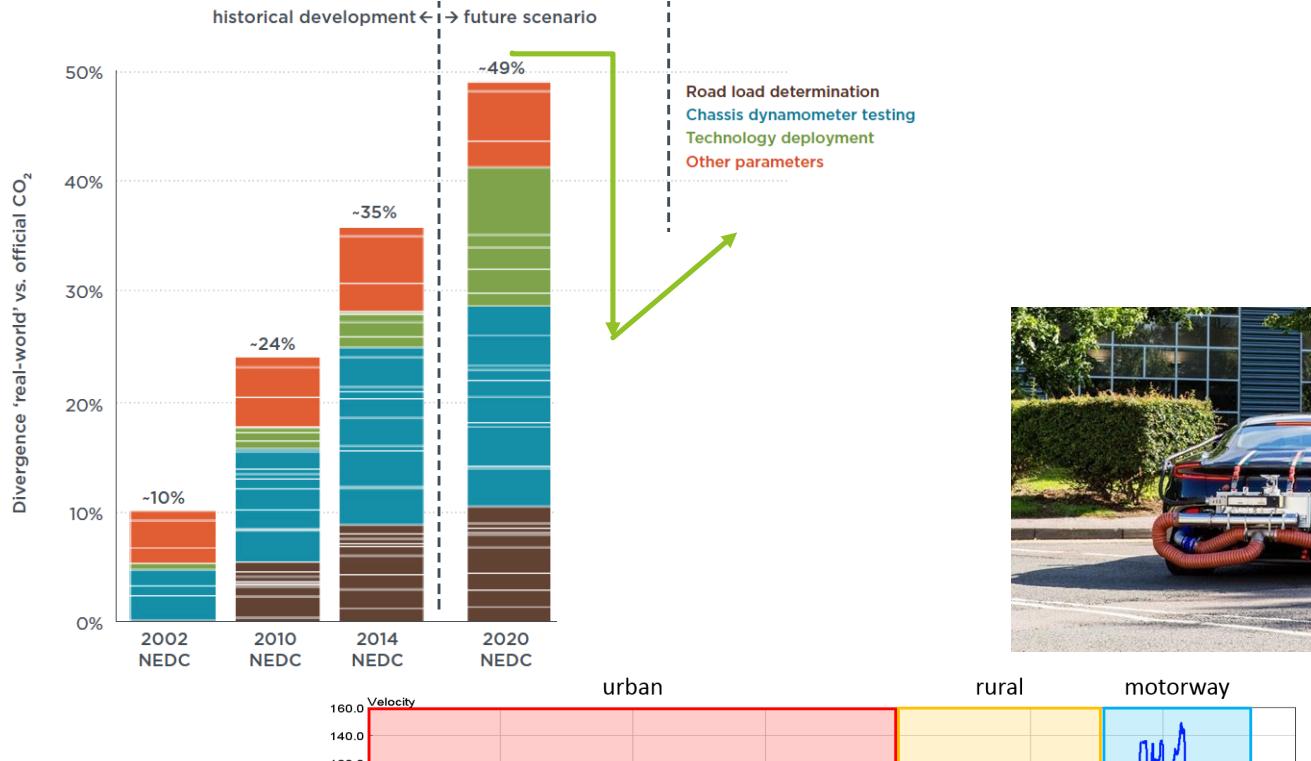


NEDC vs WLTP – Energy Bins



- Along the **NEDC** cycle a significant fraction of energy is provided by the two powertrains under poor efficiency conditions
- On **WLTP** the centre of gravity of the energy distribution is moved toward to the maximum efficiency area

NEDC → Real Driving Emissions



- RDE imply need of:
- Statistical constraints on the speed pattern.
 - Correction coefficients for ambient conditions

Agenda



- Introduction
- **Goal of the Exercise**
- Vehicle Model Building
- Model Limits
- CO2 Legislation Targets
- Post-Processing

Goal of the Exercise



- The goal of this practice exercise is the evaluation, **through numerical simulations** of fuel consumption, CO₂ and NO_x emissions over two type approval driving cycles:
 - The **New European Driving Cycle** (NEDC);
 - The **Worldwide Harmonized Light-duty Test Cycle** (WLTC);
- Two Euro 4 B-Segment vehicles, equipped with a **5 gears Manual Transmission** (MT) and a **1.3 liter Diesel engine** and characterized by different masses and Road Loads (RLs), are the test cases used to assess the impact of **NEDC** and **WLTC** cycles on fuel consumption and pollutants emissions;



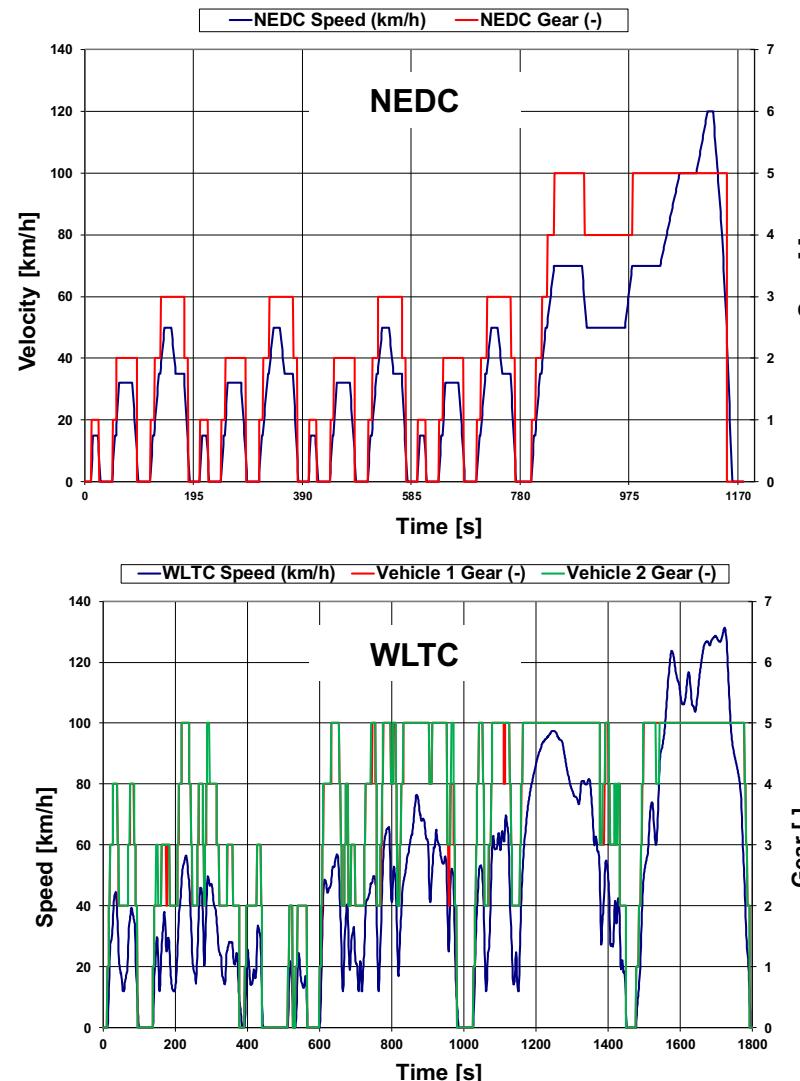
Fiat Idea



Fiat Punto

Test Conditions

- The **NEDC** and the **WLTC** cycles impose different test conditions:
 - The **WLTC** is characterized by higher speeds, steeper accelerations, less idling time compared to the **NEDC**;
 - The **WLTC** cycle should be tested considering higher **test mass**, **RLs** compared to the **NEDC**;
 - In case of **MT** the **WLTC** cycle request a specific gearshift profile, designed as function of the vehicle characteristics (engine, gear ratios, etc..) and test conditions (**mass** and **RLs**), while the **NEDC** uses a unique gearshift pattern.
- Therefore, for the two vehicles the test conditions and the gearshift patterns for the two driving cycles are provided.



NEDC		
Test Conditions	Idea	Punto
Mass [kg]	1168	1063
F0 [N]	124,7	114,2
F1 [N/(km/h)]	0	0
F2 [N/(km/h) ²]	0,0364	0,0344

WLTC		
Test Conditions	Idea	Punto
Mass [kg]	1360	1210
F0 [N]	186	166
F1 [N/(km/h)]	0	0
F2 [N/(km/h) ²]	0,0419	0,039

Agenda



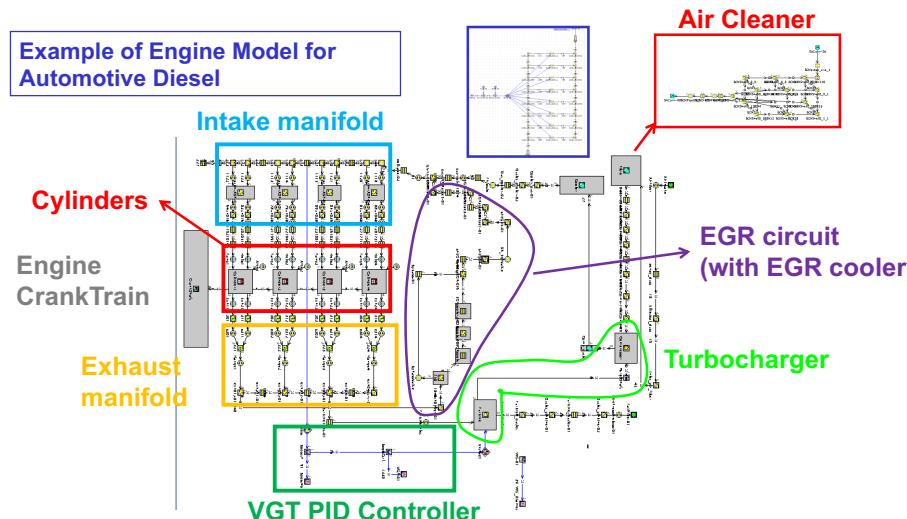
- Introduction
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- **Vehicle Model Building**
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Modeling Approaches 1/2

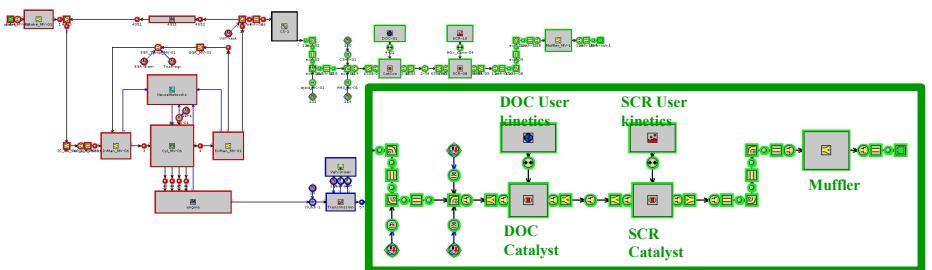
Dynamic Approach:

Not only the longitudinal vehicle dynamics equation is solved to determine the engine speed and the torque demand, but also the internal combustion engine behaviour during transients is modelled by means of detailed 0D or 1D fluid-dynamic models. For instance, for an internal combustion engine, the intake and exhaust systems can be represented as a network of ducts connected by junctions that represent either physical joints between the ducts, such as area changes or volumes, or subsystems such as the engine cylinder.

- The solution of the equations governing the conservation of mass, momentum and energy of the flow for each element of the network can then be obtained using a finite difference technique.
- In this way, even highly dynamic events, such as abrupt vehicle accelerations during tip-in manoeuvres can be properly and reliably simulated with a reasonable accuracy



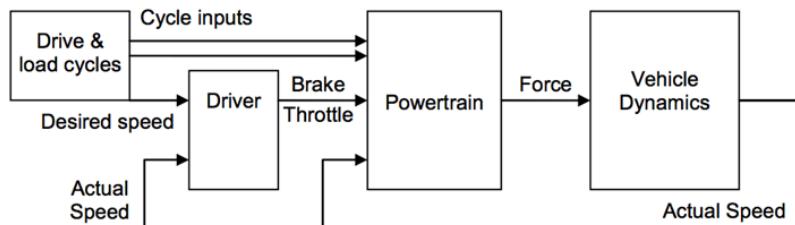
Example: Aftertreatment Models



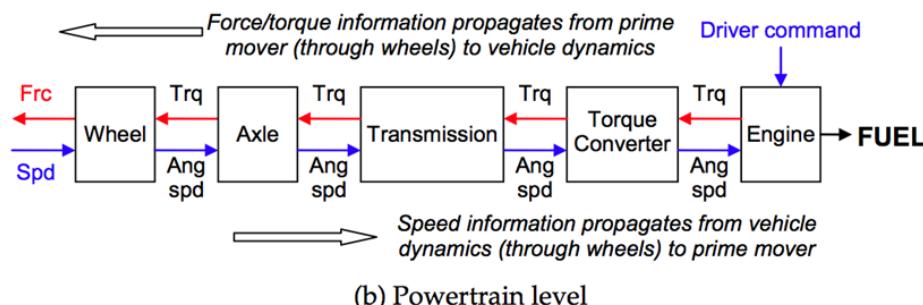
Modeling Approaches 2/2

Quasi Static Approach:

a driver model (typically a PID) compares the target vehicle speed with the actual speed and generates a power demand profile in order to follow the target vehicle speed profile, by solving the longitudinal vehicle dynamics equation as shown.

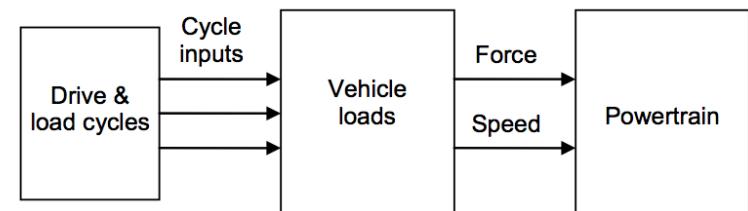


(a) Vehicle level

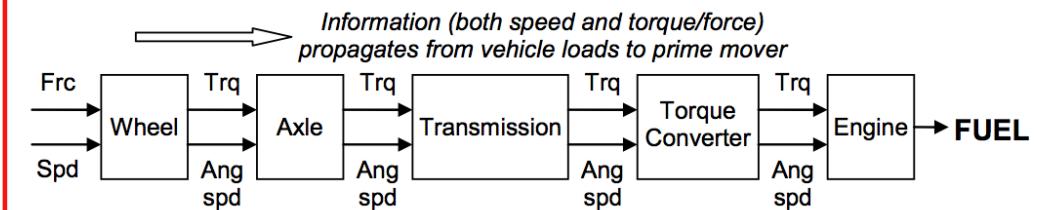


The kinematic approach:

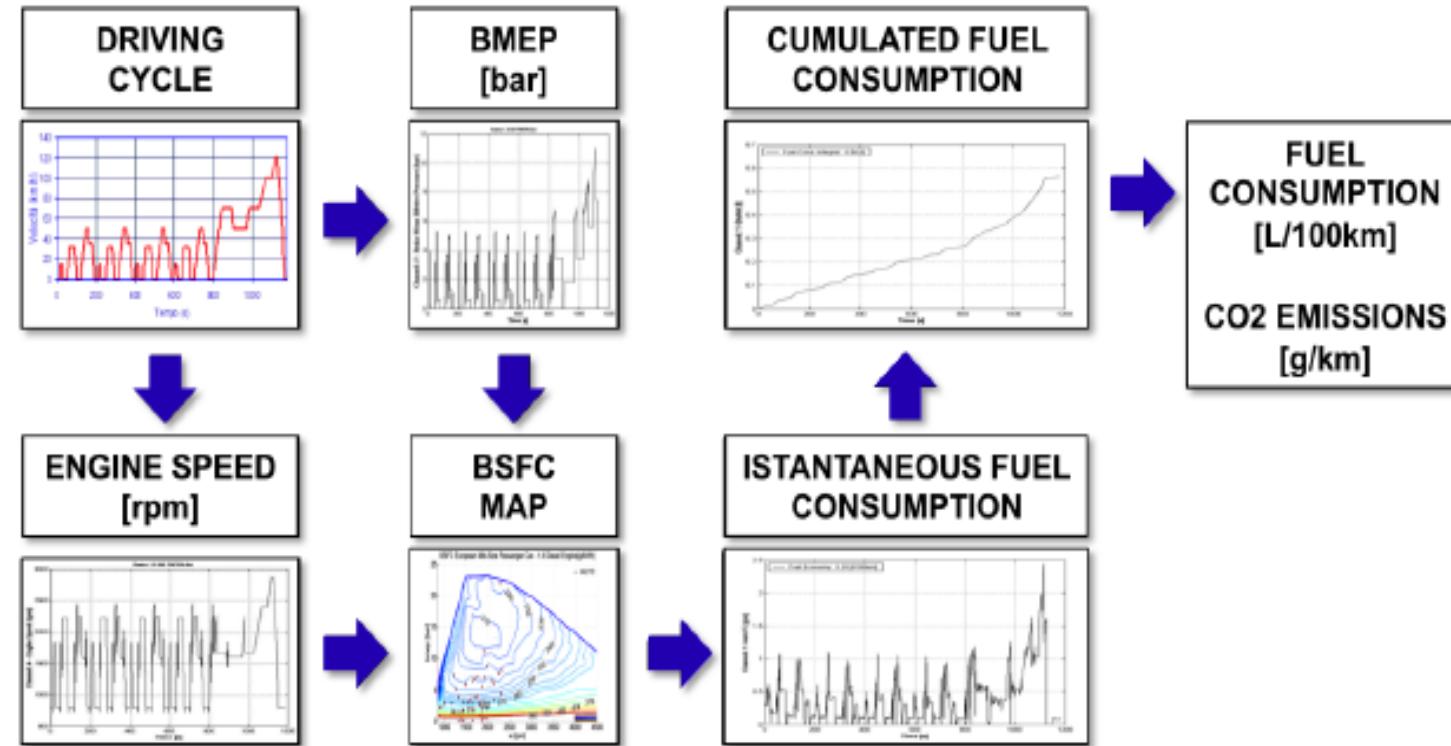
it is based on a backward methodology where the input variables are the speed of the vehicle and the grade angle of the road. The engine speed can therefore be easily determined from simple kinematic relationships.



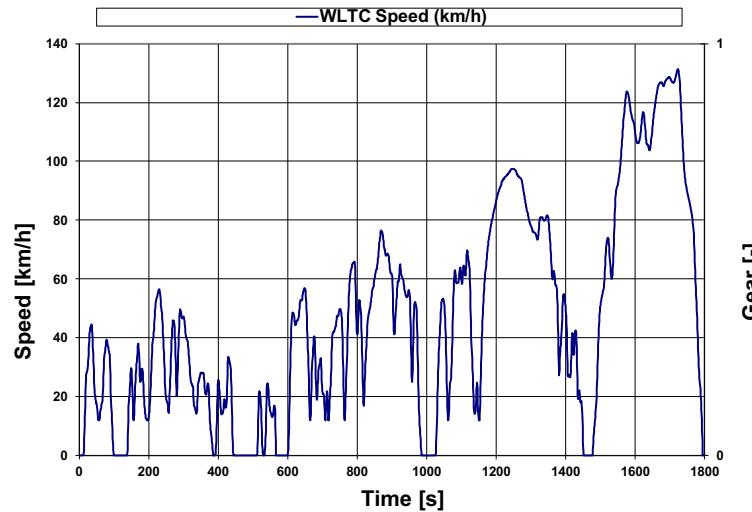
(a) Vehicle level



Vehicle Model



Calculation of the engine speed and BMEP



$$rpm[rpm] = \frac{v \left[\frac{Km}{h} \right] * 60}{2 * \pi * R_0[m] * 3,6} * \tau_p * \tau_{marcia}$$

The engine speed should be limited to the idle speed equal to 800 rpm

$$F_{res} = F_0 + F_1 * v + F_2 * v^2$$

$$P_m \eta_T [kW] = F_{res} * v + m_{tras} * \frac{dv}{dt} * v$$

$$bmepl[bar] = 1200 \frac{P_m[kW]}{rpm * V[dm^3]}$$

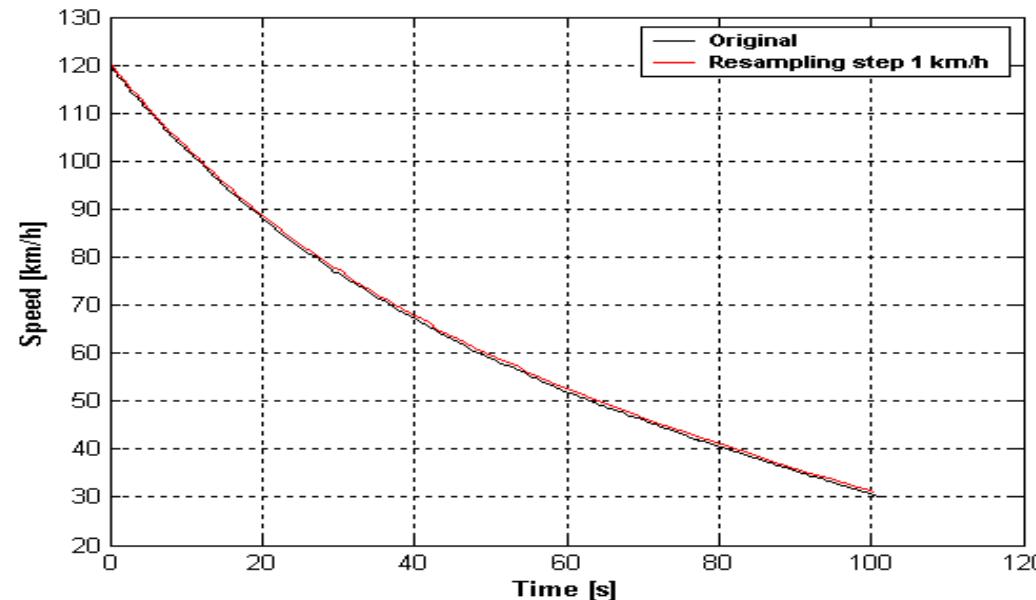
The BMEP should be equal to 0 when the power is negative

- F_{res} is the resistive force;
- F_0, F_1 and F_2 are the Coast Down coefficients;
- M_{tras} the apparent mass of the vehicle;
- v is the vehicle speed;
- η_t is the efficiency of the transmission;
- P_m is the engine power;
- τ_p is the final drive ratio;
- τ_{marcia} is the gear ratio;
- V is the engine displacement

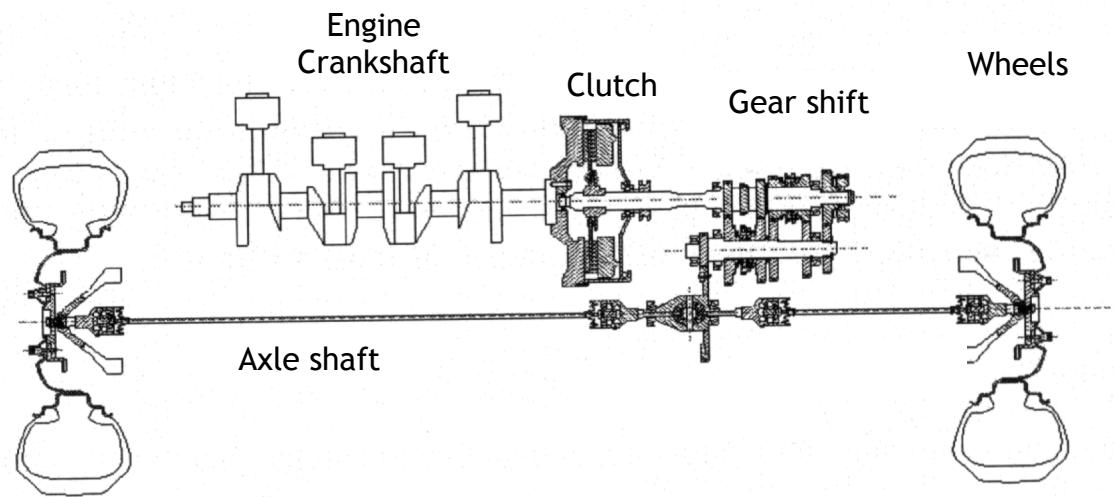
Coast Down Coefficient



$$-m_{tras} \frac{dv}{dt} = F_0 + F_1 v + F_2 v^2$$

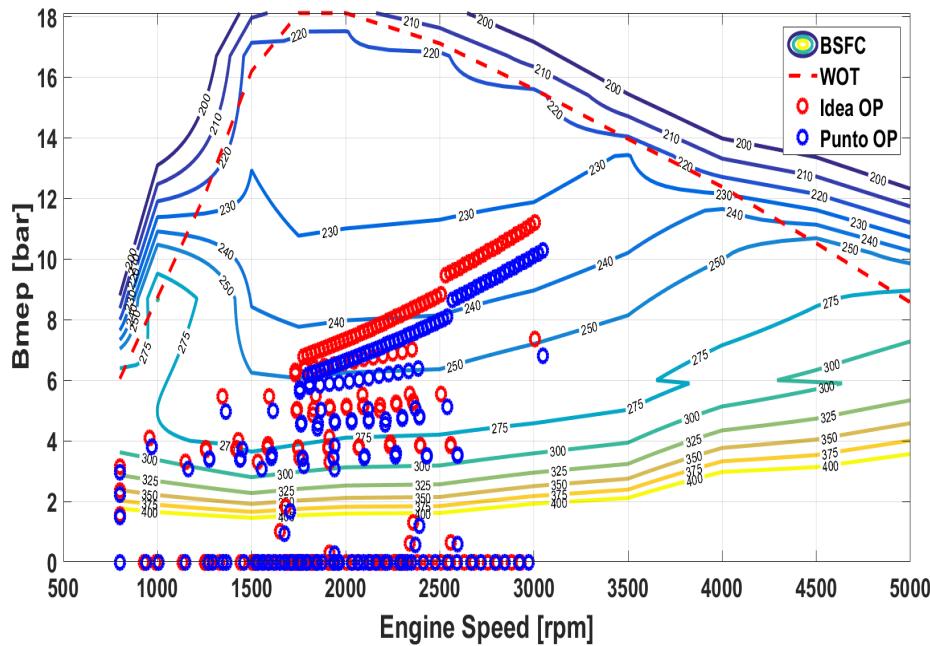


Apparent Mass

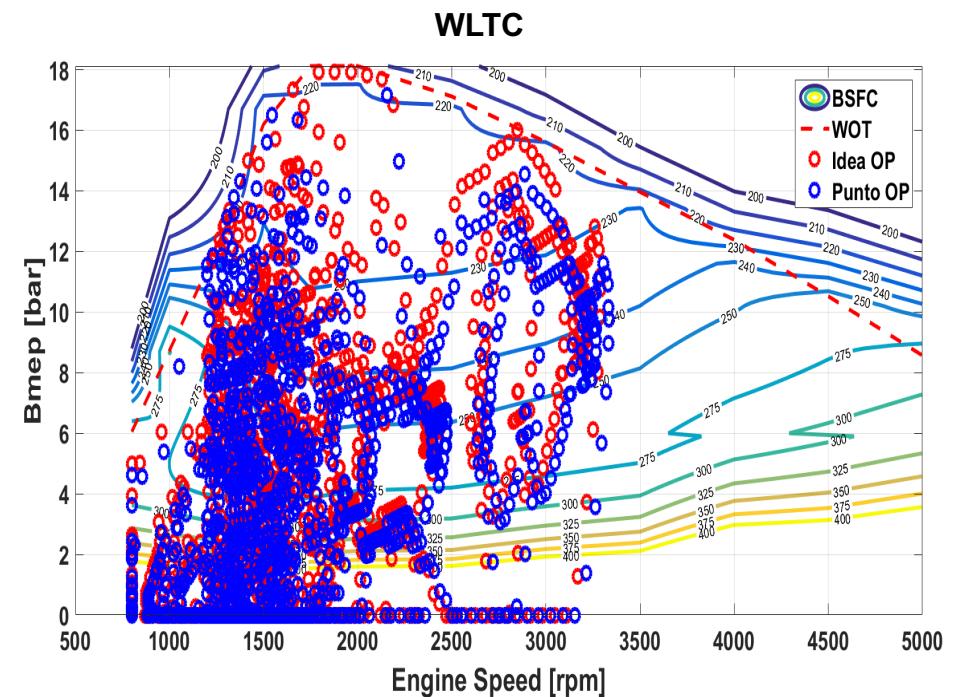


$$m_{\text{apparent}} \cong m_{\text{vehicle}} + J_{\text{wheel}} \frac{1}{r^2} + J_{\text{eng}} \frac{\tau_{\text{gear}}^2 \tau_{\text{final}}^2}{r^2}$$

Calculation of the engine speed and BMEP



NEDC



Calculation of the engine speed and BMEP

The calculation of operating points (Engine speed, BMEP) requests the data import in Matlab of the vehicle speed and gear profiles

1. Create an M-File: [edit cycle_simulation.m](#)
2. Get data and text from Excel spreadsheet, using the command `xlsread`:

```
nedc = xlsread(NEDC_WLTP_data.xlsx,'NEDC')
```

nedc =		
	1.0e+003 *	
0	0	0
0.00010	0	0
0.00020	0	0
0.00030	0	0
0.00040	0	0
0.00050	0	0
0.00060	0	0
0.00070	0	0
0.00080	0	0
0.00090	0	0
0.00100	0	0
0.00110	0	0
0.0120	0.0037	0.0010
0.0130	0.0075	0.0010
0.0140	0.0112	0.0010
0.0150	0.0150	0.0010

Calculation of the engine speed and BMEP

3. Get columns time, speed, gear

```
time = nedc(:,1); speed = nedc(:,2); gear = nedc(:,3)
```

4. Define the variables necessary for the calculations:

```
mass = 1168;
```

```
ratio_l = 3.563;
```

```
eta_l = 0.94;
```

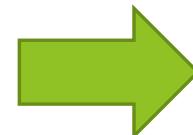
```
F0 = 124.7;
```

```
...
```

5. Choice of the gear ratio:

```
for i=1:length(speed)
```

```
    if gear(i)==0
        ratio=0
        eta=0;
    elseif gear(i)==1
        ratio=ratio_l;
        eta=eta_l;
    elseif ...
        ...
    end
```



6. Calculation of the Engine Speed

```
rpm(i) = speed(i)*60/2/pi/r_wheel/3.6*ratio_fin*ratio;
```

```
if rpm(i)<rpm_idle
```

```
    rpm(i)=rpm_idle;
```

```
end
```

To avoid down speeding
below idling speed

7. Calculation of the BMEP:

```
fres(i) = F0+F1*speed(i)+F2*speed(i)^2; % Resistive Force [N]
```

```
m_trasl(i) = mass+J_wheel/r_wheel^2+J_eng/r_wheel^2*ratio^2*ratio_fin^2; %  
Apparent Mass [kg]
```

```
acc(i) = (speed(i)-speed(i-1))/(time(i)-time(i-1)); % Vehicle Acceleration [m/s²]
```

```
pwr(i) = (fres(i)+m_trasl(i)*acc(i))*speed(i); % Vehicle Motive Power
```

```
btep(i) = 1200*pwr(i)/(rpm(i)*Vtot*eta_l); % Engine BMEP [bar]
```

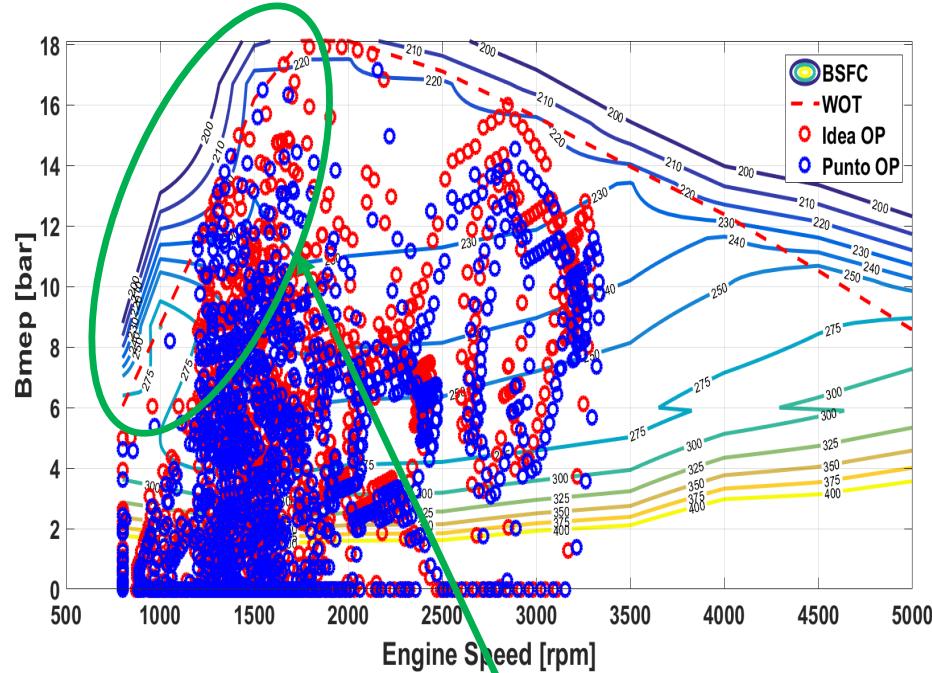
```
If btep(i) < 0
```

```
    btep(i) = 0; % BMEP correction when vehicle motive power is  
negative
```

```
else
```

```
end
```

Calculation of the engine speed and BMEP

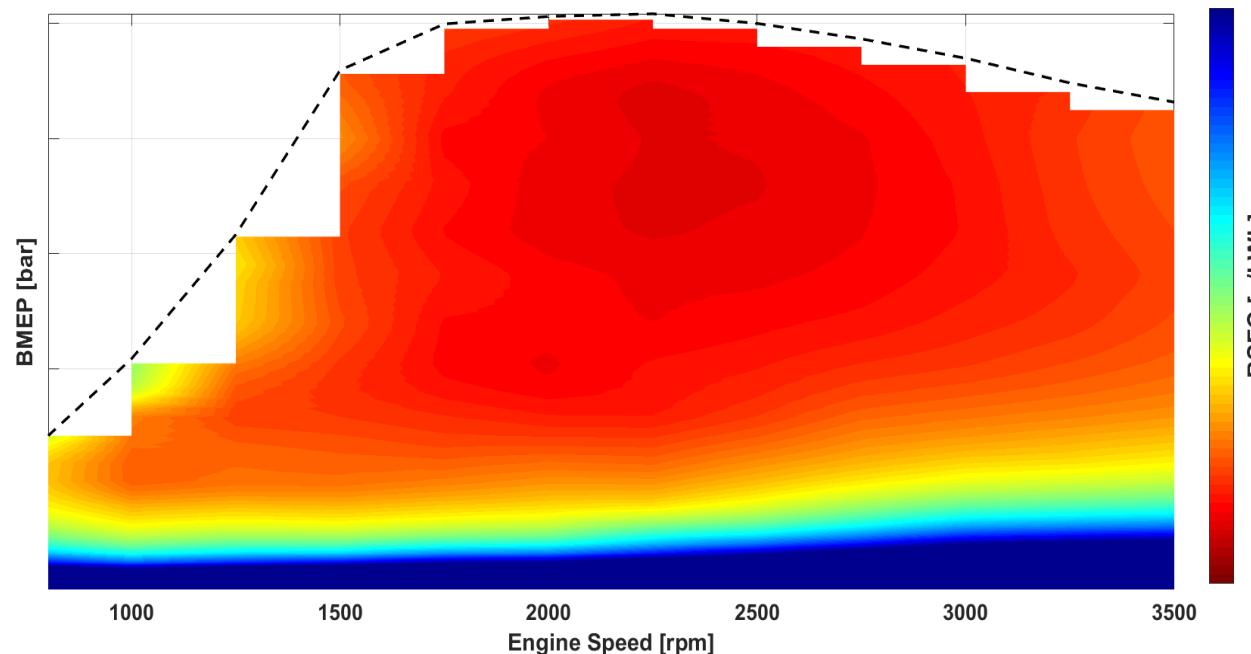


Along the **WLTC** cycle the internal combustion engine could operate along the Full Load Curve → **It is necessary to limit the engine power using the Full Load Curve**

Calculation of the fuel consumption/NOx emissions



The engine fuel consumption and the NO_x emissions are evaluated using performance maps, experimentally measured under steady state conditions



Example of engine fuel consumption map

Calculation of the fuel consumption/NOx emissions

1. Get fuel consumption map

```

pq=dlmread('fuel_cons_kg_h_vesr_matlab.pqm','t');
rpm_pq=pq(1,2:end);
bmep_pq=pq(2:end,1);
fc_pq=pq(2:end,2:end); % [kg/h]

```

2. Interpolation to calculate the engine fuel rate

```
fc(i) = interp2(rpm_pq,bmep_pq,fc_pq,rpm(i),bmep(i));
```

CAUTION: The performance map is not defined for speed <850 rpm e BMEP<0.5 bar ! In these conditions the idle fuel consumption or other hypothesis should be applied

3. NO_x rate

```

nox_map = dlmread('nox_g_h.txt','t');
rpm_nox = nox_map(1,2:end);
nox_pq = nox_map(2:end,1);
nox_pq = nox_map(2:end,2:end); % [g/h]
nox(i) = interp2(rpm_nox,bmep_nox,nox_pq,rpm(i),bmep(i));

```

CAUTION: The performance map is not defined for speed <1000 rpm e BMEP<1 bar! Hypothesis should be applied

4. Cumulative fuel consumption

```
fc_tot = fc_tot + fc(i)*( time(i)-time(i-1) )/3.6; [g]
```

Alternative function: fc_tot = cumtrapz(time [s], fc [kg/h])/3.6 [g]

5. Cumulative NOx emissions

```
nox_tot = nox_tot+nox(i)*(time(i)-time(i-1))/3600; [g]
```

Alternative function: nox_tot = cumtrapz(time [s], nox [g/h])/3600 [g]

6. Distance travelled

```
km_tot = km_tot + speed(i)*( time(i)-time(i-1) )/3600;
```

Alternative function: km_tot = cumtrapz(time [s], speed [km/h])/3600 [km]

7. Fuel Economy

```
I_100km = fc_tot/fuel_dens/km_tot*100;
```

8. NO_x Emissions

```
nox_spec = nox_tot/km_tot;
```

9. CO₂ Emissions

$$m_{CO_2} [g / km] = \frac{\rho_f [kg/l]}{0.0315} \cdot V [l / 100km]$$



Calculation of the CO₂ Emissions

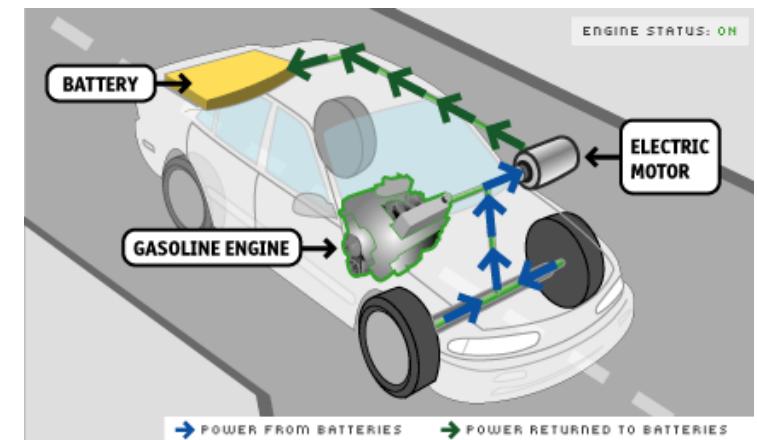
$$n_f = n_{CO_2} + n_{CO} + n_{HC} \quad \rightarrow \quad m_f = n_f \mu_f = \left(\frac{m_{CO_2}}{\mu_{CO_2}} + \frac{m_{CO}}{\mu_{CO}} + \frac{m_{HC}}{\mu_{HC}} \right) \mu_f$$

≈ 0

$$\rightarrow \quad m_{CO_2} \approx m_f \frac{\mu_{CO_2}}{\mu_f} \quad \rightarrow \quad m_{CO_2} [g/km] = \frac{\rho_f [kg/dm^3]}{0.0315} \cdot V [l/100km]$$

Evaluation of the mechanical energy demand and of the maximum energy recovered through regenerative braking

- The cycle energy demand is an important parameter for a meaningful comparison between different driving cycles and test conditions;
- The mechanical energy demand is computed by integrating the positive motive power as function of time (resistive force + inertias);
- The regenerative braking is an energy recovery mechanism which converts the kinetic energy during the braking phases into electrical energy through a electric generator, which is stored inside battery, instead of dissipating it through mechanical brakes;
- The energy stored inside the battery can be used for electric drive (mild/strong hybrid vehicles) or to supply auxiliary components (cockpit, infotainment, etc..) for micro hybrid applications (48V);
- The application of regenerative braking is becoming popular between manufacturers to improve vehicle fuel economy;
- The goal of this practice exercise is the evaluation of the maximum energy that can be recovered along the driving cycle;
- The energy recovered along the cycle can be computed by integrating the negative motive power as function of time.



¹Source: <https://www.quora.com/What-is-the-difference-between-conventional-braking-and-regenerative-braking-in-automobiles> (Accessed on 10/05/2017)

Evaluation of the mechanical energy demand and of the maximum energy recovered through regenerative braking



1. Mechanical energy demand

```
if pwr(i)>0  
    pwr_pos(i) = pwr(i);  
else  
    pwr_pos(i) = 0;  
end  
  
mechanical_energy(i) = mechanical_energy(i-1) + pwr_pos(i)*(time(i)-time(i-1)) % [J]  
...  
specific_mechanical_energy = mechanical_energy/(1000*km_tot) % [kJ/km]
```

2. Maximum energy recovered through regenerative braking

```
if pwr(i)<0  
    pwr_neg(i) = pwr(i);  
else  
    pwr_neg(i) = 0;  
end  
  
brake_energy(i) = brake_energy(i-1) + pwr_neg(i)*(time(i)-time(i-1)) % [J]  
...  
specific_brake_energy = brake_energy/(1000*km_tot) % [kJ/km]
```

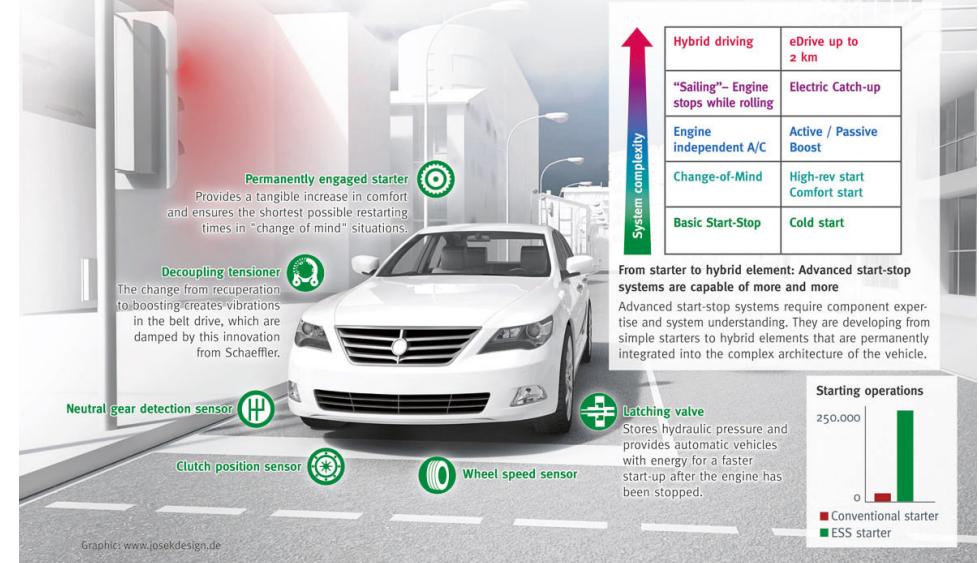
Additional features: Cut-Off and Stop-Start



- **The fuel cut-off is a particular control strategy available with electronic injection systems, which disables the fuel injection when the accelerator pedal is released;**
- The cut-off is enabled when the engine speed is above a specific threshold ($1000 \leq \text{speed threshold} \geq 1400 \text{ rpm}$) to guarantee a smooth deceleration of the vehicle;
- **The Stop-Start system is used automatically shuts down the internal combustion engine to reduce the amount of time the engine spends idling, reducing fuel consumption and pollutants emissions;**
- On MT vehicles, the Stop-Start is activated by pressing the clutch and moving the gear to neutral position when the vehicle is stopped (brake pedal pressed);
- The engine Stop-Start is disabled when the driver releases the clutch pedal;
- The possibility to enable the Stop-Start is also influenced by the coolant temperature (if the engine coolant temperature is below $40/50^\circ\text{C}$ the stop-start is disabled to accelerate the engine and after-treatment warm-up).

UNDERSTANDING START-STOP SYSTEMS

Start-stop systems are on the verge of being integrated into all automobiles worldwide. Schaeffler's comprehensive and ever-expanding product range offers numerous engine start-stop (ESS) solutions.



Stop-start technology²

²Source: <http://www.car-engineer.com/stop-and-start-system-for-automatic-transmissions> (Accessed on 10/05/2017)



Additional features: Cut-Off and Stop-Start

1. Fuel Cut-Off

```
if pwr(i) < 0 & rpm > 1000  
    fc(i) = 0;  
elseif  
    ...  
end
```

CAUTION: The same procedure should be applied to NOx emissions!

2. Stop-Start

```
if speed(i) <= 0 & ratio <= 0  
    fc(i) = 0;  
elseif  
    ...  
end
```

CAUTION: The same procedure should be applied to NOx emissions!

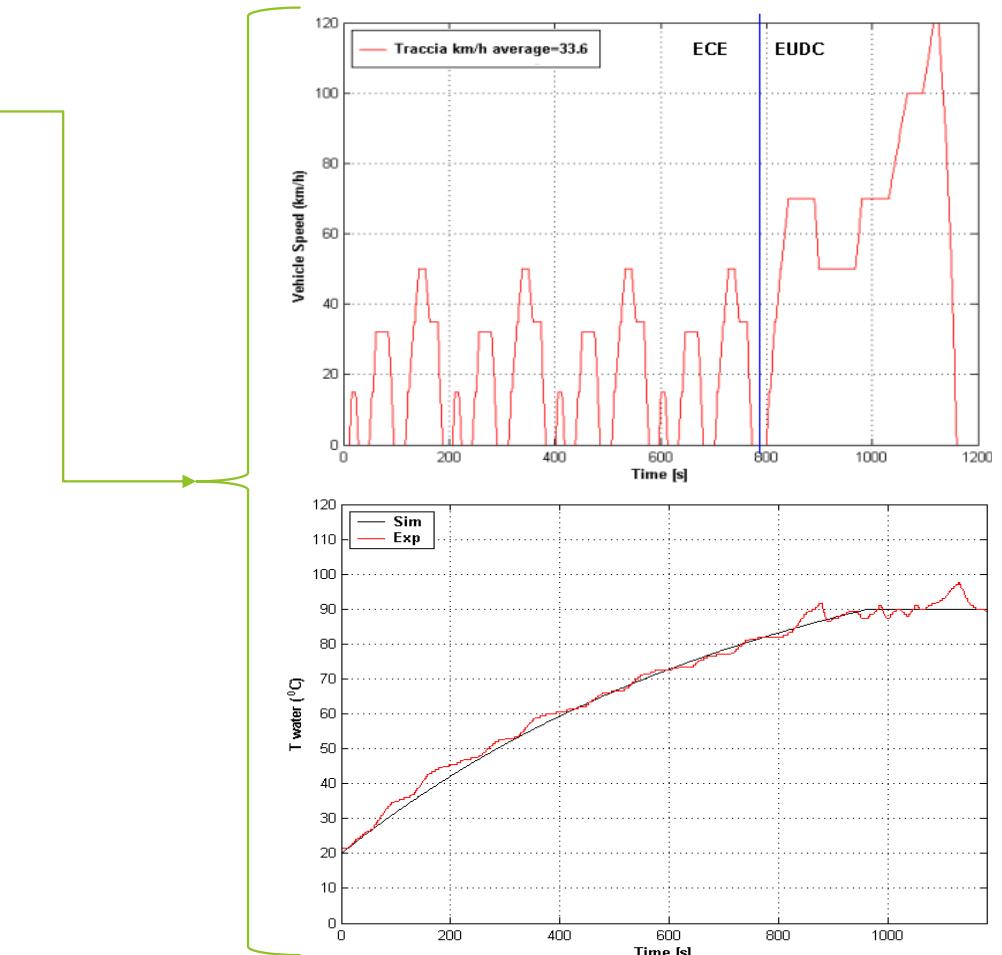
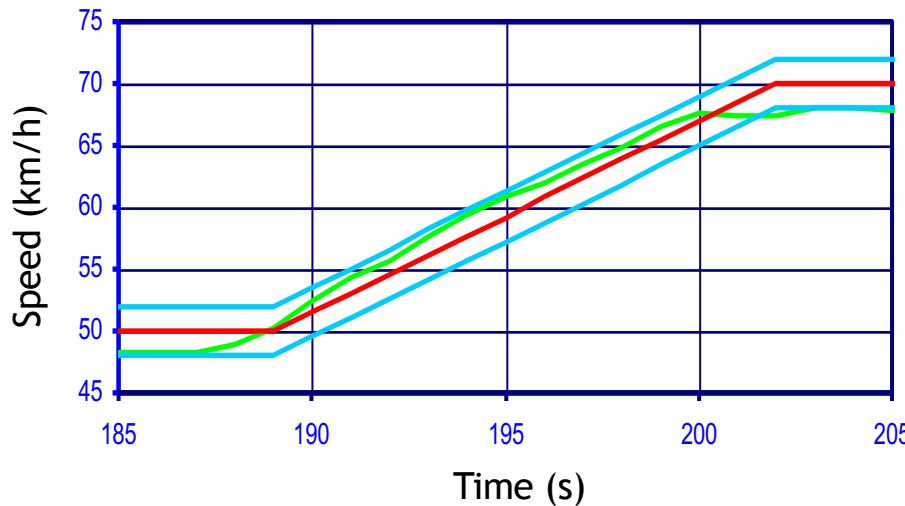
Agenda



- Introduction
- Goal of the Exercise
- Vehicle Model Building
- **Model Limits**
- CO2 Legislation Targets
- Post-Processing

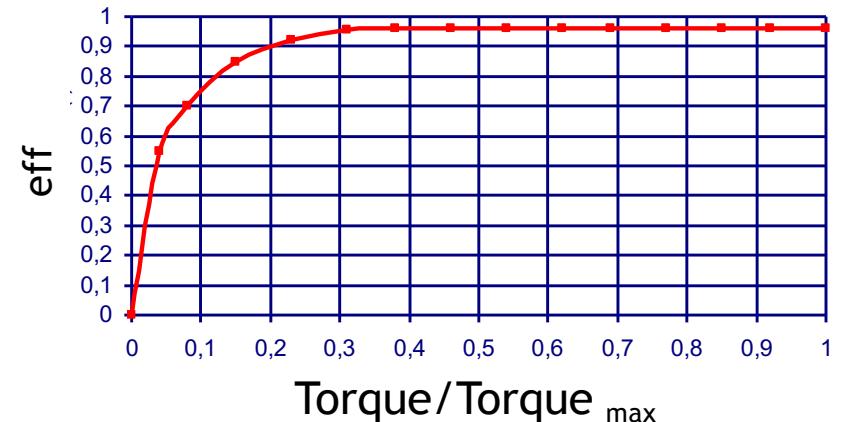
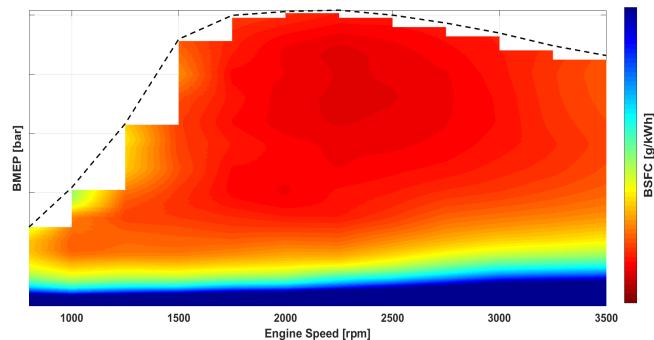
Model Limits

1. Thermal transient during warm-up not taken into account.
2. Real vehicle speed profile not simulated.



Model Limits

3. Transmission efficiency variations with load not taken into account
4. Transient conditions not taken into account: driving cycle simulated as a sequence of steady state conditions.



Although with some limitations, the analysis allows a number of issues to be evaluated, such as for instance:

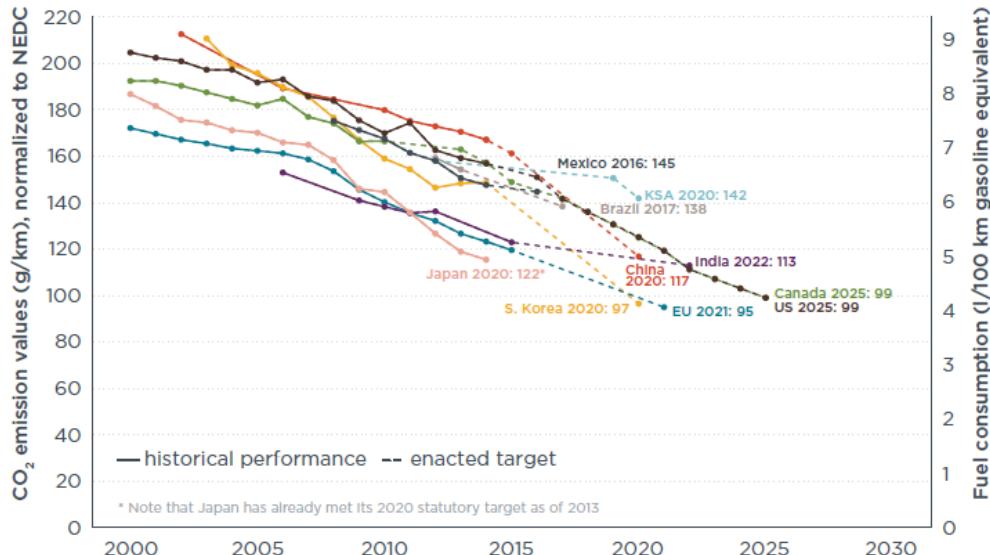
- effects on fuel consumption of variations of gear ratios, coast down, vehicle mass
- effects of fuel cut-off, start&stop

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CO₂ Legislation Targets

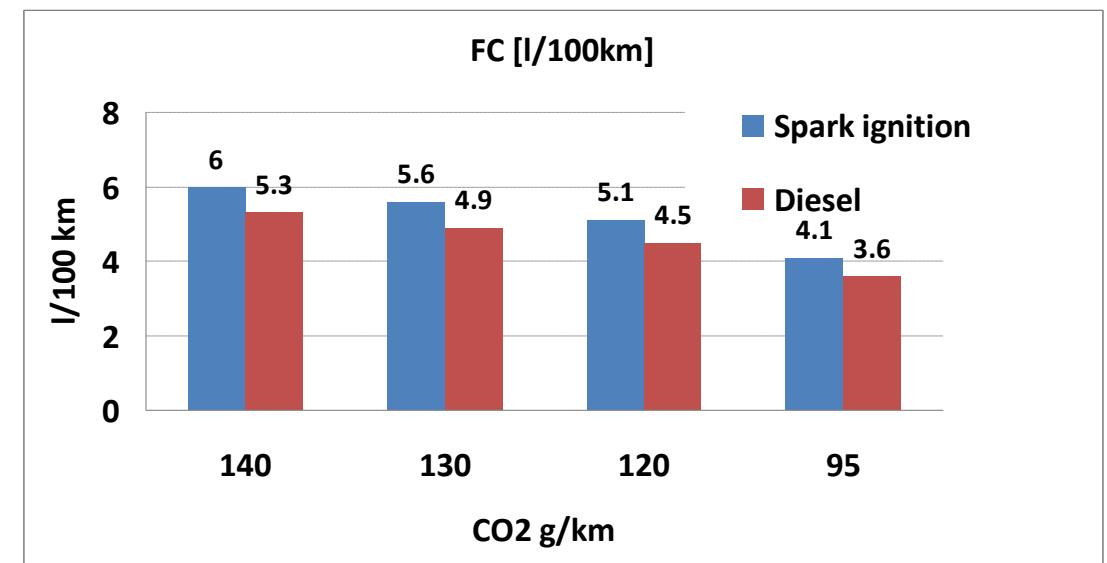


But... what does 130 grams of CO₂ per km mean ?

So the question is: can these targets be reached with current technologies?

For typical gasoline and diesel fuels, the following conversion factors from carbon balance apply to convert from CO₂ g/km to liters/100 km :

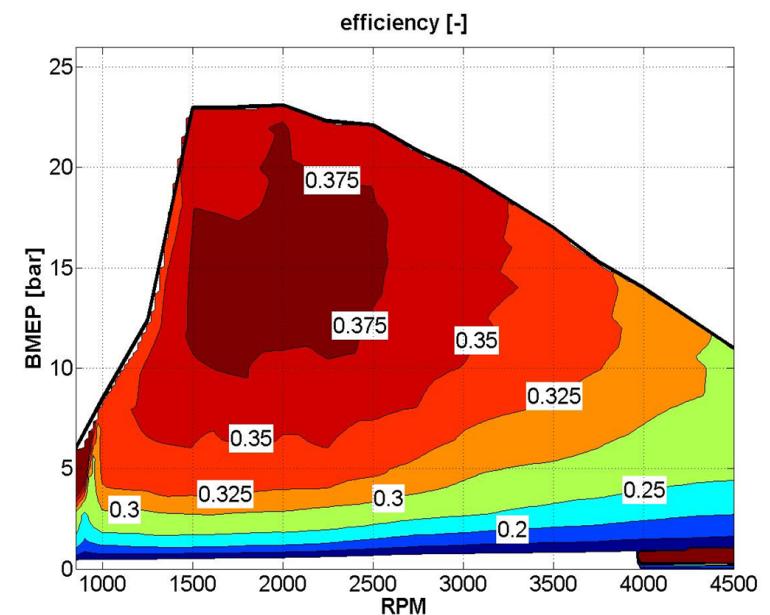
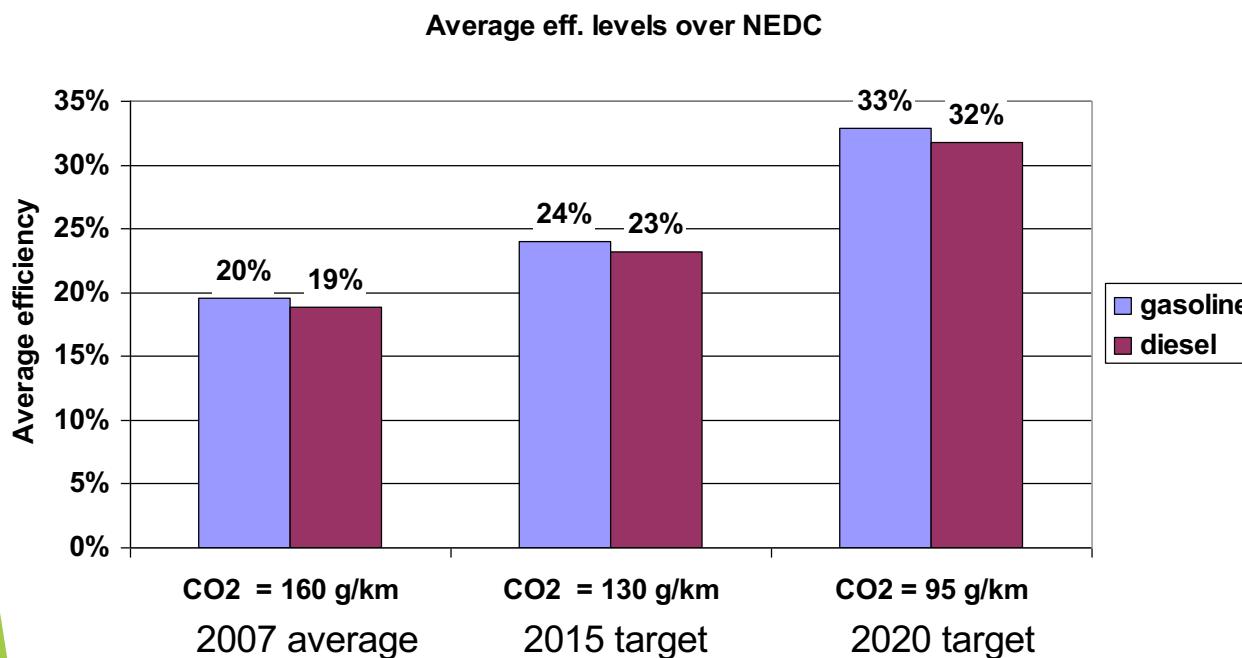
$$V_f [l/100km] \cong \frac{0.0315 \cdot m_{CO_2} [g / km]}{\text{fuel_density} [kg / l]}$$



CO₂ Legislation Targets

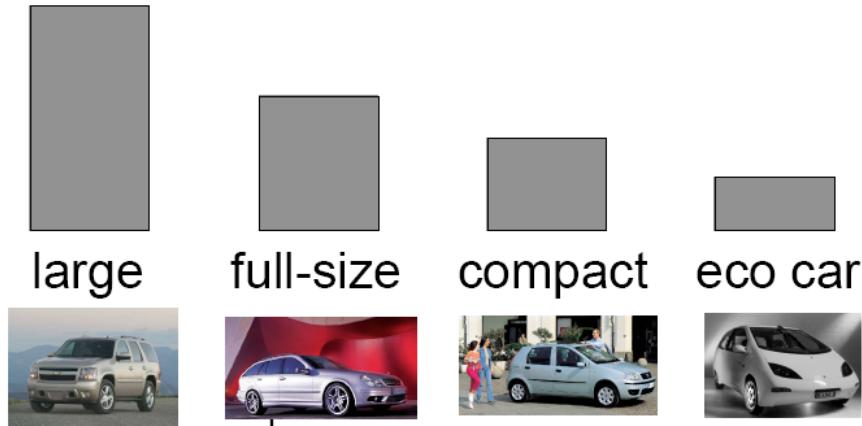


If future CO₂ target are to be met with powertrain improvements only (i.e. no possible tires or drag reduction should be taken in to account) for the “average” European passenger car the following average efficiencies values will be required, that, at least for gasoline engines, appear far beyond current system capabilities.



CO₂ Legislation Targets

Mechanical Energy Demand

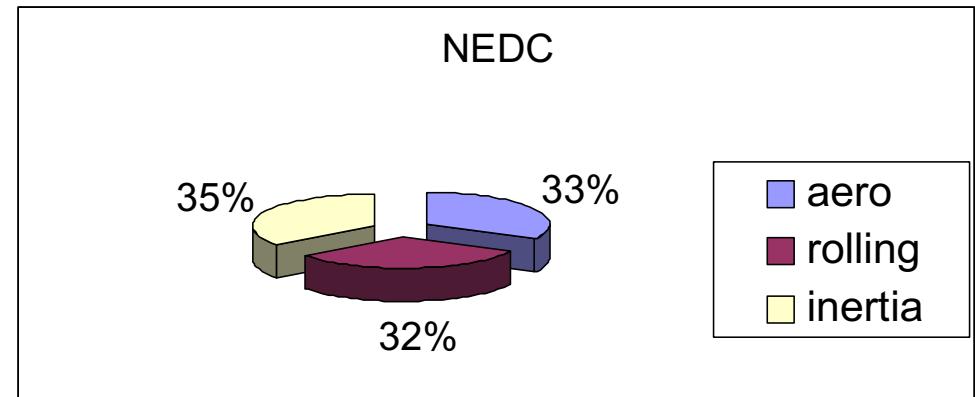


For the “average” European passenger car

(1280 kg mass, c_{roll} 0.012, $Cx^*A = 0.7 \text{ m}^2$)

Energy requested for NEDC is about **40 MJ/100km**

(or about 110 Wh/km)



10% reduction in:

- Aero → 3.3% red. En. Req.
- Rolling → 3.2% red. En. Req.
- Mass → 6.7% red. En. Req.

[1] Guzzella L.: “Control of IC Engine Systems”, 8th International Conference on Engines for Automobile, SAE – ICE 2007

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Post processing

1. Example: engine speed VS time plot

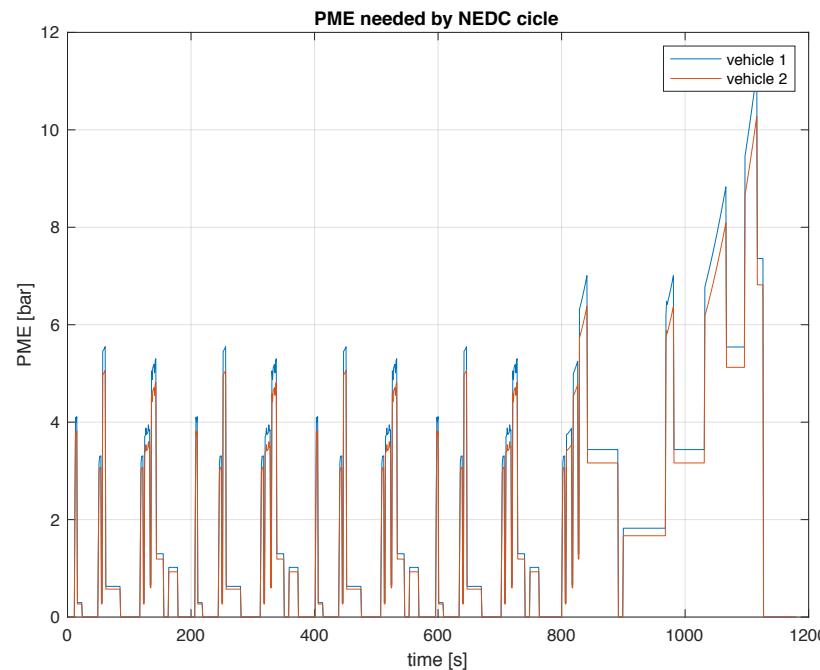
```
plot(time,rpm)
```

```
grid on % Insert a grid on the plot
```

```
xlabel('Time [s]') % Insert the label on the X-Axle
```

```
ylabel('Engine Speed [rpm]') % Insert the label on the Y-Axle
```

NOTE: The same script can be applied to engine BMEP, instantaneous fuel consumption, NOx instantaneous emissions, etc..



Post processing – Operating Map Creation

1. Calculation of the BSFC map → it should be performed starting from the experimental fuel consumption map
 1. Calculation of the power corresponding to fuel consumption data: $P=bmep_{pq} \cdot rpm_{pq} \cdot V / 1200$; % [kW] **CAUTION:** the matrix product should be performed in order to obtain a matrix with the same dimension of fc_{pq} → Where: $bmep_{pq}$ and rpm_{pq} are obtained from the first column of the experimental map of fuel consumption respectively; **ATTENTION:** $bmep_{pq} \cdot rpm_{pq}$ will return an error.
 2. $Bsfc = fc_{pq} ./ P * 1000$; % [g/kWh] → point to point ratio of the fuel consumption and of the power
2. Definition of the WOT performance
 1. $rpm_{max} = [800; 1000; \dots; 5000]$; → values of speed corresponding to WOT BMEP → could be either manually defined or loaded from excel
 2. $bmep_{max} = [6.05; 8.73; \dots; 8.57]$; → values WOT BMEP → could be either manually defined or loaded from excel
3. Limiting of the BSFC values to the WOT curve
 1. $bmep_{wot} = interp1(rpm_{max}, bmep_{max}, rpm_{pq}, 'linear', 'extrap')$; → calculation of the maximum BMEP corresponding to the speed set points of the fuel consumption map
 2. $bmep_{mtx} = repmat(bmep_{wot}, length(bmep_{pq}), 1)$; → → matrix of max bmep index
 3. $bmep_{pq_mtx} = repmat(bmep_{pq}, 1, length(rpm_{pq}))$; → matrix of bmep index to be compared with the $bmep_{mtx}$ matrix
 4. $bsfc(bmep_{pq_mtx} > bmep_{mtx}) = NaN$; → all the bsfc point featuring a BMEP higher than the WOT values will be set to NaN

Post processing – Operating Map Creation

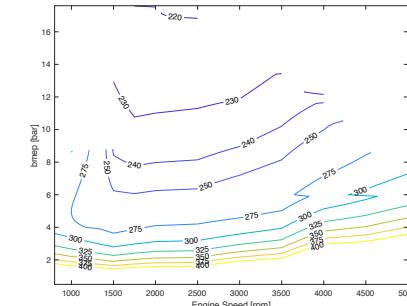
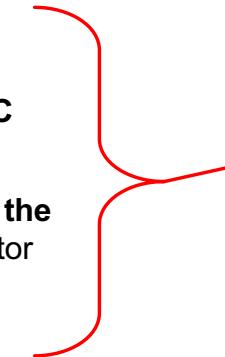


1. Creation of BSFC Contour

`V = [200 210 220 230 240 250 275 300 325 350 375 400];` → array with the BSFC values represented on the map → decided by the user

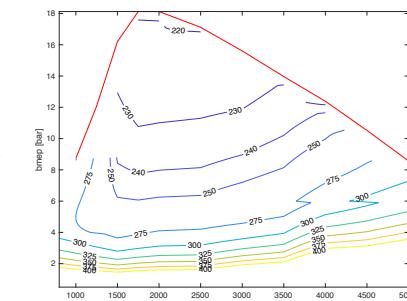
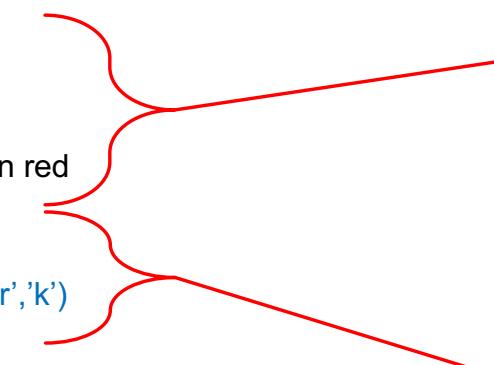
`figure, [c,h] = contour(rpm_pq,bmep_pq,bsfc,V)` → Matlab command for creating the iso-level plot → it requires x-index: rpm_pq – y-index: bmep_pq – z-values: bsfc – vector of iso-level curves to be represented

`clabel(c,h)` → Add the labels to the iso-BSFC curves



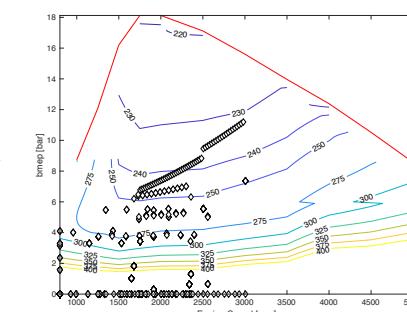
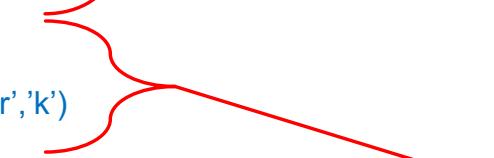
4. Add Full Load curve on the BSFC map plot

1. `hold all` → Enable to add new curves on the same figure
2. `plot(rpm_max,bmep_max,'r')` → plot of the WOT profile in red



5. Add engine operating point on the map

1. `plot(rpm,bmep,'d','MarkerFaceColor','w','MarkerEdgeColor','k')`



Appendix 1

- How to define a matrix:

```
Command Window
>> a= [1 2 3; 4 5 6]

a =
    1     2     3
    4     5     6
```

- Simple Operation between Vector or Matrix

- Sum: +
- Difference: -
- Array multiply (it should be performed only between matrixes with the same dimension): *

a=[3 4] b=[5 6]

>> a.*b

ans =

15 24

Appendix 2

- Matrix multiply:

`a=[3 4] b=[5; 6]`

```
>> a*b          >> b*a

ans =           ans =
               39           15    20
               18           18    24
```

- Array Operations

- Array divide: `.`
- Matrix divide: `/`
- Array Power: `.^`
- Matrix Power: `^`
- Transpose: `'`

- Write `;` at the end of each line to suppress the output in the command window

Iterations: **for cycle**

```
for i=1:15
    ...
    ...
end
```

Appendix 3

- Conditionally executed statements: **if**

```
if a==b  
    ...  
    ...  
else  
    ...  
    ...  
end
```

- Interpolation (table lookup): **interp2**

Z = interp2(x_map,y_map,z_map,X,Y)

