

SYNCHRONOUS MOTOR LAB

EEE3091F: Lab Report



Prepared By:

Ronak Mehta - MHTRON001

Lab Session #: 3A

Faculty of Engineering and the Built Environment

09th May 2019

AIM

To determine the operating characteristics of a synchronous machine connected to Infinite Bus bars, to measure the parameters of the equivalent circuit and to use this circuit to verify the motor performance.

DATA

Watt meter multiplication factor = X20

VAR meter multiplication factor = X30

Table 1: Effect of Field current

I _{ac} [A]	V _{ac} [V]	Power[W]	Power factor	I _f [A]	I _{drive} [A]	Rotor angle	VARs	VAR flow direction	Lead/Lag
5.0	228	120	0.099	8.5	0.7	88.0°	1200	+ve	Lag
2.5	229	80	0.139	6.8	0.7	87.5°	570	+ve	Lag
0.0	229	40*	0.555	5.4	0.7	89.0°	60*	Neutral	Neutral
2.5	229	100	0.173	3.6	0.7	88.0°	570	-ve	Lead
5.0	229	140	0.119	1.9	0.7	89.0°	1170	-ve	Lead

*Should be zero but there is an offset

Table 2: Effect of Mechanical Power Flow

I _{ac} [A]	V _{ac} [V]	Power[W]	Power factor	I _f [A]	I _{drive} [A]	Rotor angle	VARs	VAR flow direction	Lead/Lag
2.0	229	400	0.976	5.3	0.70	102°	90	-ve	Lead
1.0	229	160	0.936	5.3	0.65	96°	60	-ve	Lead
0.0	229	20	1.000	5.25	0.60	90°	0	Neutral	Neutral
1.0	229	140	0.978	5.2	0.60	86°	30	+ve	Lag
2.0	227	400	0.997	5.2	0.35	78°	30*	+ve	Lag

*There seems to be an issue as the value should have been around 90 VARs

Table 3: Exercise

I _{ac} [A]	V _{ac} [V]	Power[W]	Power factor	I _f [A]	I _{drive} [A]	Rotor angle	VARs	VAR flow direction	Lead/Lag
2.15	229	300	0.8	6.4	0.65	98°	225	+ve	Lag

Calculations for Exercise:

$$Pf = \cos(\arctan(\text{VAR}/W))$$

$$0.8 = \cos(\arctan(\text{VAR}/W))$$

$$\tan(\arccos(0.8)) = \text{VAR}/W$$

$$0.75 = \text{VAR}/W$$

If W = 300:

$$\text{VAR} = 0.75 \times 300 = 225$$

Table 4: Effect of Field Current

I_f [A]	V_{ac} [V]	Speed [rpm]
5.22	230	3040
4	188	3040
3	139	3040
2	99	3040
0	0	3040

Table 5: Short circuit test

I_f [A]	I_{ac} [A]	Speed [rpm]
4.9	7.25	2950
4	6.20	2980
3	4.55	2995
2	2.95	3000
0	0	3000

Stator Resistance:

$$A = 0.828 \, \Omega$$

$$B = 0.937 \, \Omega$$

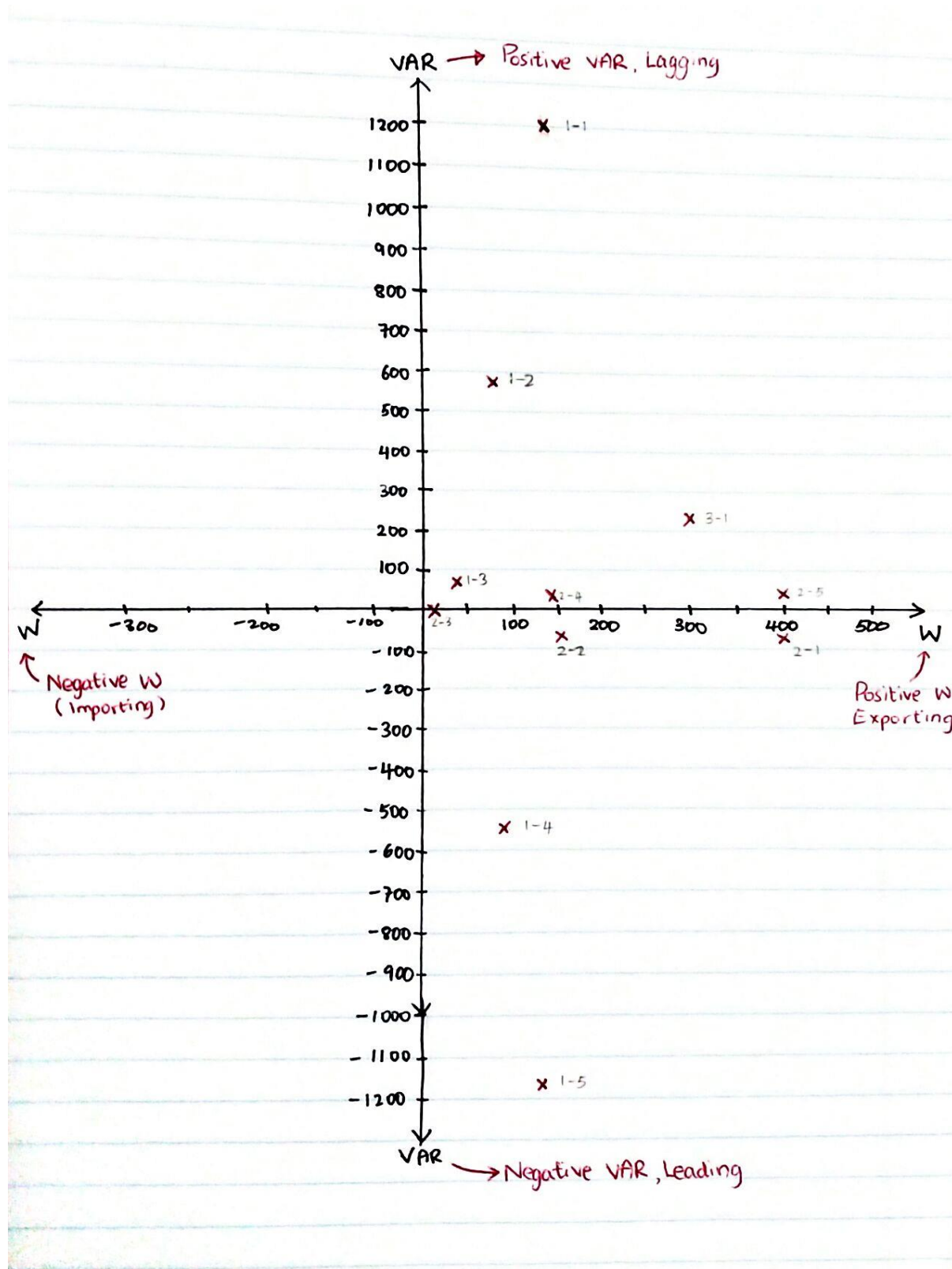
$$C = 0.870 \, \Omega$$

$$\text{Average} = 0.878 \, \Omega$$

Hence, Stator resistance, **$R = 0.878 \, \Omega$**

RESULTS

Question 1:



Question 2:

Given that the supply has a frequency of 50Hz and the machine is 2-pole, the theoretical synchronous speed is:

$$N_s = (120 \cdot f) / p = (120 \cdot 50) / 2 = \underline{3000 \text{ rpm}}$$

From tables 4 and 5, we see that the maximum speed is 3040rpm.

$$\text{Then maximum error} = \frac{3040 - 3000}{3000} \cdot 100\% = \underline{1.33\%}$$

This agrees well within the accuracy of the tachogenerator which is $\pm 1.5\%$

Question 3:

By adjusting I_f , it is possible to get more than one identical value for I_{ac} . This is possible because the machine can supply reactive power (act as an inductor) or absorb reactive power (act as a capacitor). As a result, we get similar I_{ac} values for different I_f values since the direction of VARs get changed. This can be seen in tables 1 and 2.

Question 4:

This machine is known as a synchronous condenser and is operated in a borderline condition between a motor and a generator with no mechanical load to fulfill this condition. It can compensate either a lagging or a leading power factor by absorbing or supplying reactive power to the line. This enhances power-line voltage regulation.

Question 5:

When the machine was supplying VARs to the system, the rotor angle was lagging.

Question 6:

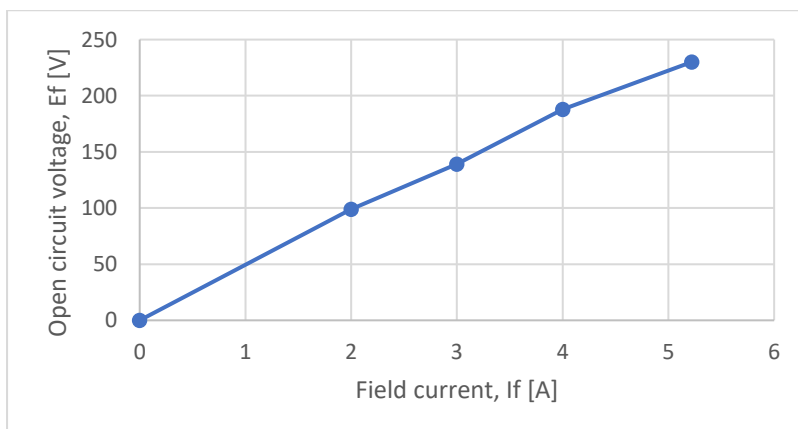


Figure 1: Open circuit voltage vs. Field current

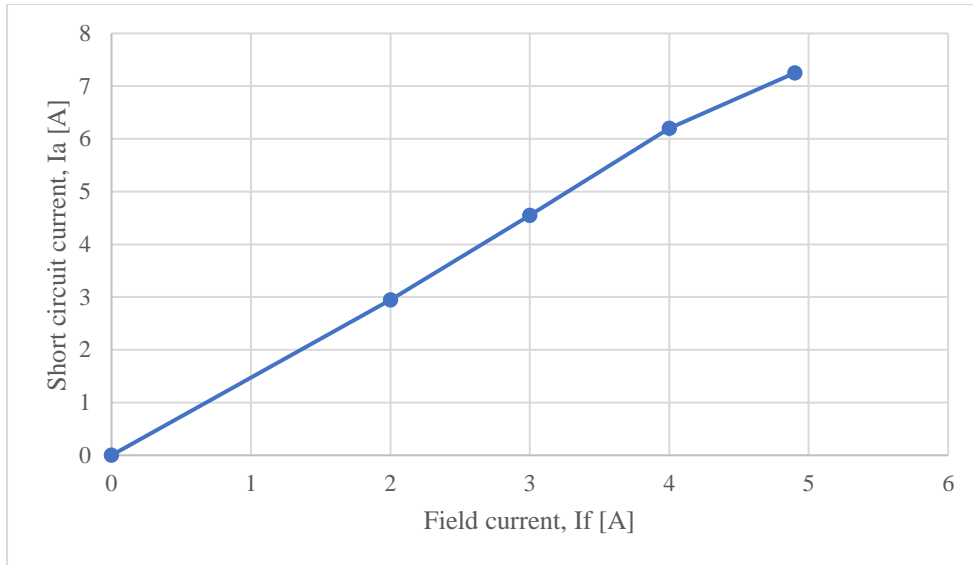


Figure 2: Short circuit current vs. Field current

Using $E_f = I_a \sqrt{X_s^2 + R^2}$, where $R = 0.878\Omega$

E_f [V]	I_a [A]	$(X_s)^2$ [Ω^2]	X_s [Ω]	I_f [A]
230	7.25	1005.65	31.71199	5
188	6.2	918.688	30.30987	4
139	4.55	932.498	30.53683	3
99	2.95	1125.457	33.54783	2
0	0	0	0	0

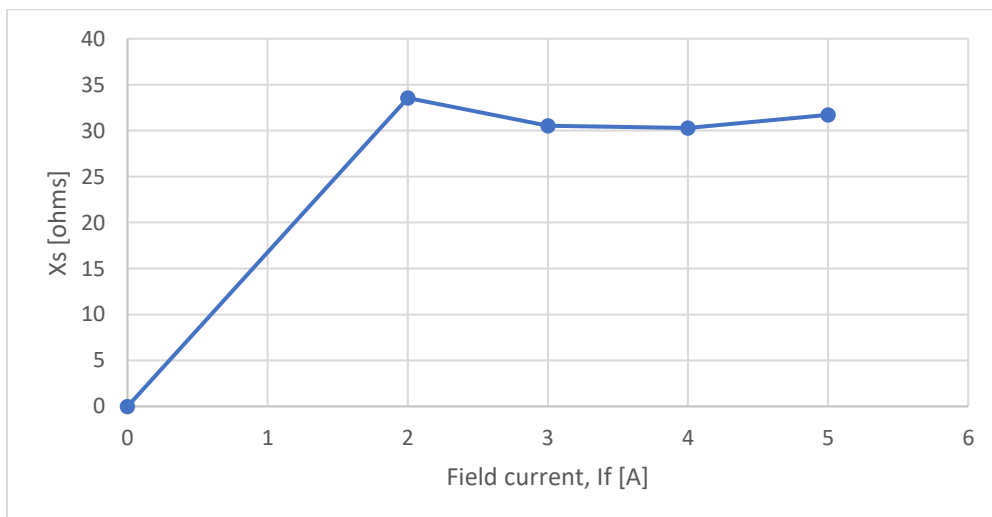


Figure 3: X_s vs. Field current

- X_s departs from a linear curve because the machine is driven into saturation.

$$X_s(\text{rated}) = \sqrt{\left(\frac{E_f \text{ airgap}}{I_{ac}}\right)^2 - R^2}$$

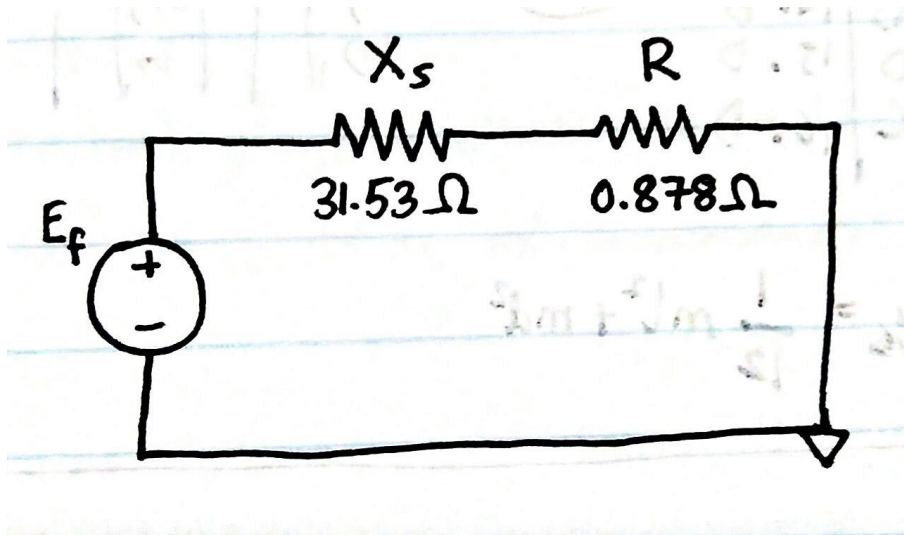
$$X_s(\text{rated}) = \sqrt{\left(\frac{270}{7.7}\right)^2 - 0.878^2} = 35.05 \Omega$$

- $X_s(\text{rated}) = 35.05 \Omega$
- Average X_s from graph = 31.53Ω

$$X_s \text{ as a percentage of the rated basis} = \left(\frac{31.53}{35.05}\right) * 100\% = \underline{\underline{89.96\%}}$$

$$\text{Stator resistance as a percentage} = 0.878 * 100\% = \underline{\underline{87.8\%}}$$

Equivalent Circuit Diagram:



Question 7:

$$\vec{E}_f = \vec{I}_a R_a + j \vec{I}_a X_s + \vec{V}_t$$

$$|\vec{E}_f| = \sqrt{(I_a R_a)^2 + (I_a X_s)^2 + (V_t)^2}$$

where:

$$I_a = 2.15 \text{ A}, R_a = 0.878 \Omega, X_s = 31.53 \Omega, V_t = 229 \text{ V}$$

$$\therefore |\vec{E}_f| = \underline{238.83}$$

$$I_a^* = \frac{|\vec{E}_f| \angle (\theta_s - \delta) - V_t \angle \theta_s}{|Z_s|}$$

$$|I_a^* Z_s| = E_f \cos(\theta_s - \delta) + E_f \sin(\theta_s - \delta) - V_t$$

$$(2.15)(\sqrt{(31.53)^2 + (0.878)^2}) = 238.83 [\cos(\theta_s - \delta) + \sin(\theta_s - \delta)] - 229$$

$$\cos(\theta_s - \delta) + \sin(\theta_s - \delta) = 1.243$$

$$\text{let } \alpha = \theta_s - \delta$$

$$\cos \alpha + \sin \alpha = 1.243$$

$$\cos \alpha + \sin \alpha = 1.243$$

$$\sqrt{(1 - \sin^2 \alpha)} + \sin \alpha = 1.243$$

$$2 \sin^2 \alpha - 2.486 \sin \alpha + 0.545 = 0$$

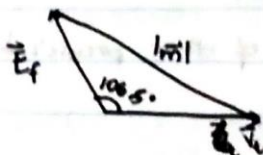
$$\sin \alpha = 0.2842 \quad \text{or } \sin \alpha = 0.9588$$

$$\alpha = 16.51^\circ$$

$$\text{but } \alpha = \theta_s - \delta$$

$$\delta = \theta_s - \alpha = 90 - (-16.51)$$

$$\text{Rotor Angle } \rightarrow \underline{\delta = 106.51^\circ}$$



$$|\vec{m}|^2 = (E_f)^2 + (V_t)^2 - 2(E_f)(V_t) \cos 106.51^\circ$$

$$|\vec{m}| = 374.89$$

$$|\vec{m}| \cos \beta = V_t$$

$$V_t = 374.89 \cos \beta = 229$$

$$\beta = 52.35^\circ$$

$$\theta = 90 - \beta = 90 - 52.35^\circ$$

$$\theta = 37.65^\circ$$

$$\underline{\text{PF} = \cos \theta = 0.79}$$

Thus, the measured power factor and rotor angle agree with the calculated value expressed as a percentage of the measured value in the following way:

$$\text{Active Power} = s \cdot \cos\theta = 380 \cdot \cos(37.65) = \mathbf{300.9W}$$

$$\text{Reactive Power} = s \cdot \sin\theta = 380 \cdot \sin(37.65) = \mathbf{232.1 VAR}$$

- % error in Rotor angle = $\frac{106.5 - 98}{98} * 100\% = 8.67\%$
- % error in PF = $\frac{0.8 - 0.79}{0.8} * 100\% = 1.25\%$
- % error in Reactive Power = $\frac{232.1 - 225}{225} * 100\% = 3.16\%$
- % error in Active Power = $\frac{300.9 - 300}{300} * 100\% = 0.3\%$

Hence:

$$\text{Power factor} = \mathbf{0.79 \pm 1.25\%}$$

$$\text{Reactive Power} = \mathbf{(232.10 \pm 3.16\%) VARs}$$

$$\text{Real Power} = \mathbf{(300.9 \pm 0.3\%) Watts}$$