



Reasoning and Querying with Knowledge Graphs

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Lecturer in Artificial Intelligence

Before we start...

GitHub Repository

https://github.com/city-knowledge-graphs/phd-course



Agenda

Four sessions split into two days

– Morning sessions:

- Theory: 9:00-10:30

- Break 15 min

- Hands-on: 10:45-12:15

Lunch break (1hour)

– Afternoon sessions:

- Theory: 13:15-14:45

- Break 15 min

- Hands-on: 15:00-16:30

Course Organization

- Introduction to Knowledge Graphs
 - ✓ Lab: Creation of a small knowledge graph and ontology.
- 2. Reasoning and Querying with Knowledge Graphs
 - Lab: First steps with the SPARQL query language.
- 3. Matching: KG-to-KG and CSV-to-KG
 - Lab: Creation of a (simple) matching system.
- 4. Knowledge Graphs and Language Models
 - Lab: Ontology Embeddings with OWL2Vec*.

PART I: SPARQL Query Language for RDF-based KGs

SPARQL by Example

SPARQL

- SPARQL Protocol And RDF Query Language
- Standard language to query graph data represented as RDF triples
- W3C Recommendations
 - SPARQL 1.0: W3C Recommendation 15 January 2008
 - SPARQL 1.1: W3C Recommendation 21 March 2013

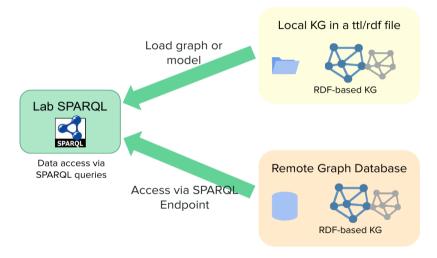
SPARQL

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- Standard language to query graph data represented as RDF triples
- W3C Recommendations
 - SPARQL 1.0: W3C Recommendation 15 January 2008
 - SPARQL 1.1: W3C Recommendation 21 March 2013
- Documentation:
 - Syntax and semantics of the SPARQL query language for RDF:

```
http://www.w3.org/TR/rdf-sparql-query/
https://www.w3.org/TR/sparql11-overview/
```

- Examples: https://www.w3.org/2008/09/sparql-by-example/

SPARQL: local and remote KG access



SPARQL Examples (i)

- Based on DBpedia: RDF version of Wikipedia with information about actors, movies, etc.: https://dbpedia.org/
- Web interface for SPARQL writing: http://dbpedia.org/sparql

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People called "Johnny Depp"

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT DISTINCT ?jd WHERE {
    ?jd foaf:name "Johnny Depp"@en .
}
```

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PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
SELECT DISTINCT ?jd WHERE {
     ?jd foaf:name "Johnny Depp"@en .
```

Answer:

```
?id
<a href="http://dbpedia.org/resource/Johnny_Depp">http://dbpedia.org/resource/Johnny_Depp></a>
```

SPARQL Examples (ii)

Films starring "Johnny Depp"

```
PREFIX foaf: <http://xmlns.com/foaf/0.1/>
PREFIX dbo: <http://dbpedia.org/ontology/>
SELECT ?m WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
}
```

(*) dbo:starring comes from the https://dbpedia.org/ontology/

SPARQL Examples (ii)

Films starring "Johnny Depp"

Answer:

```
?m
<a href="http://dbpedia.org/resource/Dead_Man">
<a href="http://dbpedia.org/resource/Edward_Scissorhands">http://dbpedia.org/resource/Arizona_Dream</a> ...
```

(*) dbo:starring comes from the https://dbpedia.org/ontology/

SPARQL Examples (iii)

Names of people who co-starred with "Johnny Depp"

```
SELECT DISTINCT ?costar WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
}
```

SPARQL Examples (iii)

Names of people who co-starred with "Johnny Depp"

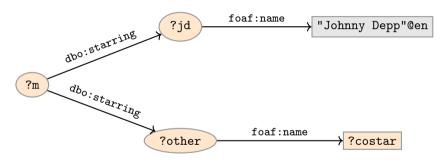
```
SELECT DISTINCT ?costar WHERE {
   ?jd foaf:name "Johnny Depp"@en .
   ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
   ?other foaf:name ?costar .
```

Answer:

```
?costar
   "Al Pacino"@en
"Antonio Banderas"@en
  "Johnny Depp"@en
 "Marlon Brando"@en
```

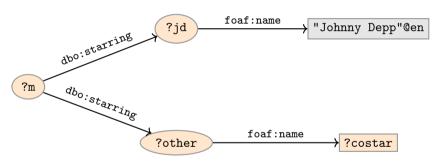
Graph Patterns

The previous SPARQL query as a graph:



Graph Patterns

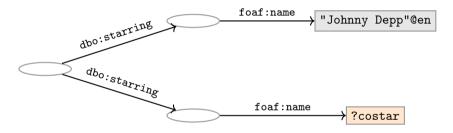
The previous SPARQL query as a graph:



Pattern matching: assign values to variables to make this a sub-graph of the RDF graph!

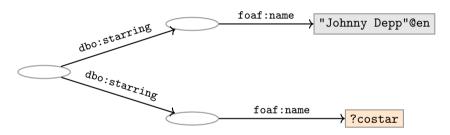
Graph with blank nodes

Variables not SELECTED can equivalently be blank:



Graph with blank nodes

Variables not SELECTED can equivalently be blank:



Pattern matching: a function that assigns values (*i.e.*, resource, a blank node, or a literal) to variables and blank nodes to make this a sub-graph of the RDF graph!

SPARQL Systematically

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
PREFIX dbo: <a href="http://dbpedia.org/ontology/">http://dbpedia.org/ontology/>
SELECT DISTINCT ?costar
WHERE {
     ?jd foaf:name "Johnny Depp"@en .
     ?m dbo:starring ?jd .
     ?m dbo:starring ?other .
     ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
I.TMTT 10
```

Prologue: prefix definitions

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
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    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10
```

Results: (1) query type (SELECT, ASK, CONSTRUCT, DESCRIBE), (2) remove duplicates (DISTINCT, REDUCED), (3) variable list.

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
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SELECT DISTINCT ?costar
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     FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
```

Query pattern: graph pattern to be matched

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LIMIT 10
```

Solution modifiers: ORDER BY, LIMIT, OFFSET

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ORDER BY ?costar
LIMIT 10
```

Types of Queries (i)

SELECT Compute table of bindings for variables

```
SELECT DISTINCT ?a ?b WHERE {
   [ dbo:starring ?a ;
     dbo:starring ?b ]
}
```

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```
SELECT DISTINCT ?a ?b WHERE {
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}
```

CONSTRUCT Use bindings to construct a new RDF graph

```
CONSTRUCT {
    ?a foaf:knows ?b .
} WHERE {
    [ dbo:starring ?a ;
     dbo:starring ?b ]
}
```

Types of Queries (ii)

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SPARQL Systematically: Solution Modifiers

Solution Sequences and Modifiers

- Permitted to SELECT queries only
- SELECT treats solutions as a sequence (solution sequence)
- Query patterns generate an unordered collection of solutions
- Sequence modifiers can modify the solution sequence (not the solution itself). Applied in this order:
 - Order
 - Projection
 - Distinct
 - Reduced
 - Offset
 - Limit

ORDER BY

- Used to sort the solution sequence in a given way:
- SELECT ... WHERE ... ORDER BY ...
- ASC for ascending order (default) and DESC for descending order

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- E.g.

```
SELECT ?city ?pop WHERE {
   ?city dbo:country ?country ;
        dbo:populationUrban ?pop .
} ORDER BY ?country DESC(?pop)
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- SELECT ... WHERE ... ORDER BY ...
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- E.g.

```
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    ?city dbo:country ?country ;
        dbo:populationUrban ?pop .
} ORDER BY ?country DESC(?pop)
```

- Standard defines sorting conventions for literals, URIs, etc.
- Not all "sorting" variables are required to appear in the SELECTION.

ORDER BY (Example)

```
SELECT DISTINCT ?costar
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
}
ORDER BY ?costar
```

Projection, DISTINCT, REDUCED

- Projection (i.e., SELECTED variables) means that only some variables are part of the solution
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 - Done with SELECT DISTINCT ?x ?y WHERE {?x dbo:starring ?y. }
 - A solution is a duplicate if it assigns the same RDF terms to all variables as another solution.
- REDUCED allows to remove some or all duplicate solutions
 - Done with SELECT REDUCED ?x ?y WHERE {?x dbo:starring ?y . }
 - Motivation: Can be expensive to find and remove all duplicates
 - Behaviour left to the SPARQL engine.

OFFSET and LIMIT

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- OFFSET: position/index of the first returned result
- Useful for paging through a large set of solutions

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- For example, solutions number 51 to 60:
 SELECT ?x ?y WHERE {?x dbo:starring ?y .} ORDER BY ?x
 LIMIT 10 OFFSET 50

OFFSET and LIMIT

- I IMIT: limits the number of results.
- OFFSET: position/index of the first returned result
- Useful for paging through a large set of solutions
- For example, solutions number 51 to 60: SELECT ?x ?v WHERE {?x dbo:starring ?v .} ORDER BY ?x LIMIT 10 OFFSET 50
- LIMIT and OFFSET can be used separately
- OFFSET not meaningful without ORDER BY.

OFFSET and LIMIT (Example)

```
SELECT DISTINCT ?costar
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar ...
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10 OFFSET 50
```

SPARQL Systematically: Query Graph Patterns

Query patterns

- Types of graph patterns for the query pattern (WHERE clause):
 - ✓ Basic Graph Patterns (BGP)
 - Filters or Constraints (FILTER)
 - Optional Graph Patterns (OPTIONAL)
 - Union Graph Patterns (UNION, Matching Alternatives)
 - Graph Graph Patterns (RDF Datasets)

Filters (i)

- A set of triple patterns may include constraints or filters
- Reduces matches of surrounding group where filter applies
- Example:

```
SELECT ?x
WHERE {
    ?x a dbo:Place ;
       dbo:populationUrban ?pop .
    FILTER (?pop > 1000000)
}
```

Filters (ii)

– Example:

```
SELECT DISTINCT ?costar
FROM <a href="http://dbpedia_dataset">http://dbpedia_dataset</a>
WHERE {
    ?jd foaf:name "Johnny Depp"@en .
    ?m dbo:starring ?jd .
    ?m dbo:starring ?other .
    ?other foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
LIMIT 10 OFFSET 50
```

Filters: Functions and Operators

- Usual binary operators: | |, &&, =, !=, <, >, <=, >=, +, -, *, /.
- Usual unary operators: !, +, -.
- Unary tests: bound(?var), isURI(?var), isBlank(?var), isLiteral(?var).
- Accessors: str(?var), lang(?var), datatype(?var), year(?date), xsd:integer(?value)
- regex is used to match a variable with a regular expression. Always use with str(?var). E.g.: regex(str(?costar), "Alpacino").

More details in specification: http://www.w3.org/TR/rdf-sparql-query/

OPTIONAL Patterns

 Allows a match to leave some variables unbound (e.g. no data is available). e.g.,:

```
WHERE {
    ?x a dbo:Person ;
      foaf:name ?name .
    OPTIONAL {
      ?x dbo:birthDate ?date .
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    }
}
```

- ?x and ?name bound in every match, ?date is bound if available.
- Groups can contain several optional parts, evaluated separately

OPTIONAL Patterns: with FILTER

```
- Example:
    WHERE {
      ?x a dbo:Person :
         foaf:name ?name ...
      OPTIONAL {
        ?x dbo:birthDate ?date .
        FILTER (?date > "1980-01-01T00:00:00"^^xsd:dateTime)
```

 - ?x and ?name bound in every match, ?date is bound if available and from 1980 onwards.

Matching Alternatives (UNION)

- A UNION pattern matches if any of some alternatives matches
- E.g.

```
SELECT DISTINCT ?writer
WHERE
  ?s rdf:type dbo:Book .
    ?s dbo:author ?writer .
  UNION
    ?s dbo:writer ?writer .
```

'Graph' Graph Patterns (RDF datasets)

- SPARQL queries are executed against an RDF dataset
- An RDF dataset comprises
 - One default graph (unnamed) graph. Target for this course.
 - Zero or more named graphs identified by an URI

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- SPARQL queries are executed against an RDF dataset
- An RDF dataset comprises
 - One default graph (unnamed) graph. Target for this course.
 - Zero or more named graphs identified by an URI
- FROM and FROM NAMED keywords allows to select an RDF dataset
- Keyword GRAPH makes the named graphs the active graph for pattern matching

SPARQL 1.1

SPARQL 1.1: new features

- The new features in SPARQL 1.1 QUERY language:
 - Assignments and Expressions
 - Aggregates
 - Subqueries
 - Negation (new syntax)
 - Property paths

SPARQL 1.1: new features

- The new features in SPARQL 1.1 QUERY language:
 - Assignments and Expressions
 - Aggregates
 - Subqueries
 - Negation (new syntax)
 - Property paths
- Specification for:
 - SPARQL 1.1 UPDATE Language
 - SPARQL 1.1 Federated Queries
 - SPARQL 1.1 Entailment Regimes

Assignment and Expressions

- The value of an expression can be assigned/bound to a new variable
- Can be used in SELECT, BIND or GROUP BY clauses: (expression AS ?var)

Expressions in SELECT clause

```
SELECT ?city (xsd:integer(?pop)/xsd:float(?area) AS ?density)
{
    ?city dbo:populationTotal ?pop .
    ?city dbo:PopulatedPlace/areaTotal ?area .
    ?city dbo:country dbr:United_Kingdom .
    FILTER (xsd:float(?area)>0.0)
}
```

Aggregates: Grouping and Filtering

- Solutions can optionally be grouped according to one or more expressions.
- To specify the group, use GROUP BY.
- If GROUP BY is not used, then only one (implicit) group

Aggregates: Grouping and Filtering

- Solutions can optionally be grouped according to one or more expressions.
- To specify the group, use GROUP BY.
- If GROUP BY is not used, then only one (implicit) group
- To filter solutions resulting from grouping, use HAVING.
- HAVING operates over grouped solution sets, in the same way that FILTER operates over un-grouped ones.

Aggregates: Example

Actors with more than 15 movies

Aggregates: Example

Actors with more than 15 movies

† Only expressions consisting of aggregates and constants may be projected, together with variables in GROUP, BY

Aggregates: common functions

- Count counts the number of times a variable has been bound.
- Sum sums numerical values of bound variables.
- Avg finds the average of numerical values of bound variables.
- Min finds the minimum of the numerical values of bound variables.
- Max finds the maximum of the numerical values of bound variables.

† Aggregates assume CWA and UNA

Subqueries

- A way to embed SPARQL queries within other queries
- Subqueries are evaluated first and the results are projected to the outer query.

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```
SELECT ?country ?pop (round(?pop/?worldpop*1000)/10 AS ?percentage) WHERE {
  ?country rdf:type dbo:Country .
  ?country dbo:populationTotal ?pop .
   SELECT (sum(?p) AS ?worldpop) WHERE {
      ?c rdf:type dbo:Country .
      ?c dbo:populationTotal ?p .}
   ORDER BY desc(?pop)
```

Subqueries

- A way to embed SPARQL gueries within other gueries
- Subgueries are evaluated first and the results are projected to the outer query.

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SELECT ?country ?pop (round(?pop/?worldpop*1000)/10 AS ?percentage) WHERE {
  ?country rdf:type dbo:Country .
  ?country dbo:populationTotal ?pop .
   SELECT (sum(?p) AS ?worldpop) WHERE {
      ?c rdf:type dbo:Country .
      ?c dbo:populationTotal ?p .}
   ORDER BY desc(?pop)
```

† Note that the *Sum()* aggregation is done over all the elements (single default group).

Negation in SPARQL 1.1: MINUS and FILTER NOT EXISTS

Two ways to do negation. *e.g.*, retrieve people without a name:

```
SELECT DISTINCT * WHERE {
    ?person a foaf:Person .
    MINUS { ?person foaf:name ?name }
}

SELECT DISTINCT * WHERE {
    ?person a foaf:Person .
    FILTER NOT EXISTS { ?person foaf:name ?name }
}
```

Property paths: basic motivation

- Some queries get needlessly large.
- SPARQL 1.1 define a small language to defined paths.
- Examples:
 - city:ernesto foaf:knows+ ?friend to extract all friends of friends.
 - foaf:maker dc:creator instead of UNION.
 - Friend's names, { _:me foaf:knows/foaf:name ?friendsname }.
 - Sum several items:

```
SELECT (sum(?cost) AS ?total) { :order :hasItem/:price ?cost }
```

Property paths: example

```
PREFIX foaf: <a href="http://xmlns.com/foaf/0.1/">http://xmlns.com/foaf/0.1/>
              <http://dbpedia.org/ontology/>
PREFIX dbo:
SELECT DISTINCT ?costar
WHERE {
    ?m dbo:starring/foaf:name "Johnny Depp"@en .
    ?m dbo:starring/foaf:name ?costar .
    FILTER (STR(?costar)!="Johnny Depp")
ORDER BY ?costar
```

†Similar to blank node syntax.

Property paths: syntax

Syntax Form	Matches
iri	An (property) IRI. A path of length one.
^elt	Inverse path (object to subject).
elt1 / elt2	A sequence path of elt1 followed by elt2.
elt1 elt2	A alternative path of elt1 or elt2 (all possibilities are tried).
elt*	Seq. of zero or more matches of elt.
elt+	Seq. of one or more matches of elt.
elt?	Zero or one matches of elt.
!iri or !(iri1 irin)	Negated property set.
!^iri or !(^irii ^irin)	Negation of inverse path.
!(iri ₁ iri _j ^iri _{j+1} ^iri _n)	Negated combination of forward and inverese properties.
(elt)	A group path elt, brackets control precedence.

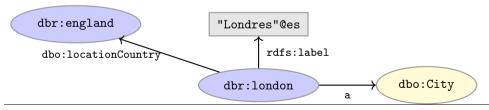
^{*} elt is a path element, which may itself be composed of path constructs (see Syntax form).

SPARQL Summary

SPARQL Summary (i)

Return all Cities:

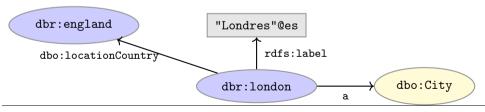
```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?city WHERE {
     ?city rdf:type dbo:City .
}
```



SPARQL Summary (i)

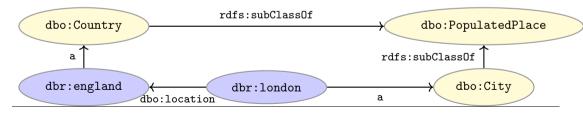
Return all Cities: Query Result= {dbr:london}

```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?city WHERE {
     ?city rdf:type dbo:City .
}
```



SPARQL Summary (ii)

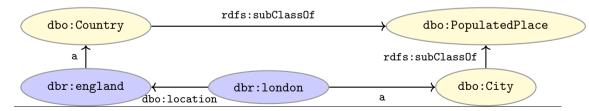
Return all Populated Places:



SPARQL Summary (ii)

Return all Populated Places: Query Result= {}

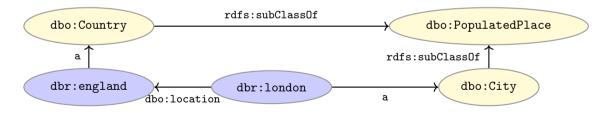
```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?place WHERE {
     ?place rdf:type dbo:PopulatedPlace .
}
```



PART II: Reasoning with Knowledge Graphs

Implicit Knowledge in KGs: Entailment

- Given a set of triples \mathcal{G} (i.e., a Graph), can we entail a triple t ($\mathcal{G} \models t$)?
- Can we entail the triple: dbr:london rdf:type dbo:PopulatedPlace and add it to the graph below? (Graph expansion via reasoning).
- Similarly for dbr:england



- Interpretations might be conceived as potential "realities" or "worlds".
- Interpretations assign values to elements.
 - (The **intuitions** behind set-theory are **formally represented**.)

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- Interpretations assign values to elements.
 - (The intuitions behind set-theory are formally represented.)
- Given an interpretation $\mathcal I$ and a set of triples $\mathcal G$
- $-\mathcal{G}$ is valid in \mathcal{I} (written $\mathcal{I} \models \mathcal{G}$), iff $\mathcal{I} \models t$ for all $t \in \mathcal{G}$.
- Then \mathcal{I} is also called a **model** of \mathcal{G} .

- The following interpretation \mathcal{I} is a model of our example \mathcal{G} :
 - $dbo:City^{\mathcal{I}} = \{dbr:london\}$
 - $dbo:Country^{\mathcal{I}} = \{dbr:england\}$
 - dbo:PopulatedPlace $^{\mathcal{I}} = \{dbr:london, dbr:england\}$
 - dbo:location $^{\mathcal{I}} = \{ \langle dbr:london, dbr:england \rangle \}$

- The following interpretation \mathcal{I} is a model of our example \mathcal{G} :
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 - $dbo: Country^{\mathcal{I}} = \{dbr: england\}$
 - $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
 - dbo:location^{\mathcal{I}} = { $\langle dbr:london, dbr:england \rangle$ }
- $-\mathcal{I} \models \mathcal{G}$ (is a model of \mathcal{G}) as the following holds:
 - dbo:City $^{\mathcal{I}} \subseteq$ dbo:PopulatedPlace $^{\mathcal{I}}$
 - dbo:Country $^{\mathcal{I}} \subset dbo:PopulatedPlace^{\mathcal{I}}$
 - dbr:london $^{\mathcal{I}} \in dbo:City^{\mathcal{I}}$

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?

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- Does 𝒢 ⊨ t ?
 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
 - $-\mathcal{I} \models t$.
 - (Yes, in this case too.)

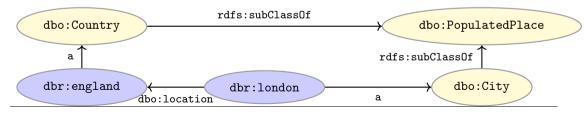
- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
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 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
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 - (Yes, in this case too.)
- Does $\mathcal{G} \models t_2$ (t_2 =dbr:london rdf:type dbo:Country)?

- -t = dbr:london rdf:type dbo:PopulatedPlace
- Does $\mathcal{I} \models t$?
 - Yes: $dbo:PopulatedPlace^{\mathcal{I}} = \{dbr:london, dbr:england\}$
- − Does $\mathcal{G} \models t$?
 - if and only if
 - For any interpretation \mathcal{I} with $\mathcal{I} \models \mathcal{G}$
 - $-\mathcal{I} \models t$.
 - (Yes, in this case too.)
- Does $\mathcal{G} \models t_2$ (t_2 =dbr:london rdf:type dbo:Country)?
 - No: Our \mathcal{I} is a counter example. $\mathcal{I} \models \mathcal{G}$ but $\mathcal{I} \not\models t_2$

SPARQL Example: with entailment

Return all Populated places:

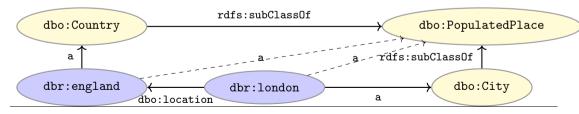
```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?place WHERE {
     ?place rdf:type dbo:PopulatedPlace .
}
```



SPARQL Example: with entailment

Return all Populated places: Query Result= {dbr:england, dbr:london}

```
PREFIX dbo: <http://dbpedia.org/ontology/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
SELECT DISTINCT ?place WHERE {
    ?place rdf:type dbo:PopulatedPlace .
}
```



Model-Theoretic Semantics in practice

- Model-theoretic semantics yields an unambigous notion of entailment.
- In principle, all interpretations need to be considered.
- However there are infinitely many such interpretations,
- An algorithm should terminate in finite time.

Foundations of Semantic Web Technologies. Chapter 3.

Syntactic methods for Entailment

Syntactic Reasoning

- From the computation point of view, we need means to decide entailment syntactically.
- Syntactic methods operate
 - only on the form of a statement, that is on its concrete grammatical structure (i.e., triples),
 - without recurring to interpretations.
- Syntactic methods should justify that their so-called operational semantics are expected with respect to model-theoretic semantics.

OWL 2 Reasoning Algorithms (i)

- Reasoning in OWL 2 is typically based on (Hyper)Tableau Reasoning Algorithms (tableau = truth tree)
- Algorithm tries to construct an abstraction of a model.

OWL 2 Reasoning Algorithms (i)

- Reasoning in OWL 2 is typically based on (Hyper)Tableau Reasoning Algorithms (tableau = truth tree)
- Algorithm tries to construct an abstraction of a model.
- State-of-the-art algorithms:
 - e.g., HermiT (default option in Protégé).

OWL 2 Reasoning Algorithms (ii)

- ✓ OWL 2 Reasoners are optimised for TBox tasks.
- Effective with many realistic ontologies.
- ABox reasoning tasks are untractable with relatively small KGs.
- Decidability is open when querying OWL-based KGs with SPARQL.
- There are some tricks to make it work, but complexity is still high.
- The main problem is that one cannot just expand the (knowledge) graph and then execute a SPARQL query
- Solution: OWL 2 Profiles

Computational properties: https://www.w3.org/TR/ow12-profiles/#Computational_Properties Seminars by Prof. Ian Horrocks: http://www.cs.ox.ac.uk/people/ian.horrocks/Seminars/seminars.html

OWL 1, OWL 2 (profiles) and RDFS

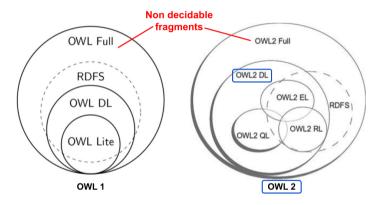
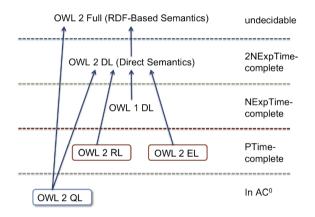


Image adapted from Olivier Cure and Guillaume Blin. RDF Database Systems (Chapter 3). 2015. Elsevier.

Data Complexity in OWL 2 and Profiles



https://www.w3.org/TR/owl2-profiles/

OWL 2 Profiles summary

- OWL 2 has various profiles that correspond to different DLs.
- These profiles have very interesting computational properties.

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 - OWL 2 QL:
 - Specifically designed for efficient database integration.
 - OWL 2 EL:
 - A lightweight language with polynomial time reasoning.
 - OWL 2 RL:
 - Designed for compatibility with rule-based inference tools.
 - Efficient reasoning with large datasets.

OWL QL Profile

- ✓ Required language so that queries can be rewritten using the TBox.
- ✓ Used in Ontology Based Data Access (OBDA) where SPARQL queries are translated to SQL

Not supported, simplified:

- disjunction
- universal quantification, cardinalities, and functional roles
- X = (SameIndividual)
- enumerations (closed classes)
- subproperties of chains, transitivity
- reduced list of datatypes

OWL EL Profile

- Standard reasoning tasks in P time
- Very good for large ontologies.
- ✓ Used in many biomedical ontologies (e.g., SNOMED CT).
- ✓ Reasoning can be performed via saturation (i.e., inference rules).

Not supported features, simplified:

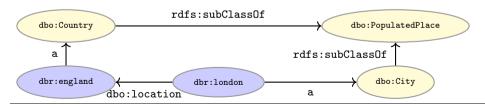
- \nearrow negation (but $C \sqcap D \sqsubseteq \bot$ possible)
- disjunction
- universal quantification and cardinalities
- inverse roles and some role characteristics
- reduced list of datatypes

OWL 2 RL Profile

- Y Puts syntactic constraints in the way in which constructs are used (i.e., syntactic subset of OWL 2).
- Imposes a reduced list of allowed datatypes.
- ✓ OWL 2 RL axioms can be directly translated into datalog rules.
- Enables desirable computational properties using rule-based reasoning engines.

Reasoning in the OWL QL Profile

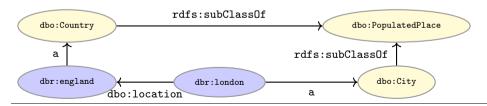
- Reasoning is performed via backward chaining (e.g., rewriting of a given query Q into Q' via the ontology axioms, instead of expanding the graph). For example:



Reasoning in the OWL QL Profile

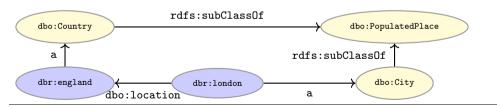
- Reasoning is performed via backward chaining (e.g., rewriting of a given query Q into Q' via the ontology axioms, instead of expanding the graph). For example:

```
Q: SELECT DISTINCT ?place WHERE {?place rdf:type dbo:PopulatedPlace . }
```



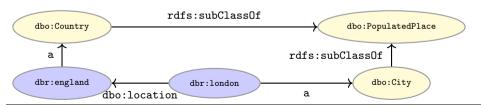
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Inference rules

Inference rules (i)

- Inference rules (also known as deduction rules or derivation rules) is an option to describe syntactic solutions.
- The general form of an inference rule is:

$$\frac{P_1,\ldots,P_n}{P}$$

- the P_i are **premises** (body)
- and P is the **conclusion** (head).
- An inference rule may have,
 - any number of premises (typically one or two),
 - but only one conclusion.

Inference rules (ii)

- Recall that syllogisms (i.e., inference) can be traced back to Aristotle
- Example:

All human are mortal
Socrates is a human
Therefore, Socrates is mortal

Inference rules (iii)

- The whole set of inference rules given for a logic is called **deduction** calculus.
- ⊢ is the inference relation, while ⊨ was the entailment relation using model theoretic semantics.
 - − We write $\Gamma \vdash P$ if we can deduce P from the premises Γ .

Inference rules (iii)

- The whole set of inference rules given for a logic is called **deduction** calculus.
- ⊢ is the inference relation, while ⊨ was the entailment relation using model theoretic semantics.
 - − We write $\Gamma \vdash P$ if we can deduce P from the premises Γ .
- In our example:
 - the **premises** Γ are a **set of triples** (*i.e.*, a (sub)graph \mathcal{G}),
 - the conclusion P is a new triple t
 - After applying the rules to \mathcal{G} we will get an **expanded graph** \mathcal{G}'

RDFS Inference Rules

RDFS supports several rules. Organized into three groups:

1. Type propagation:

- "London is a City, all Cities are populated places, so. . . "

2. Property propagation:

- "London is the capital of England, anything that is capital of a country is also located in that country, so..."

3. Domain and range propagation:

- "Everything that has a capital is a country, so England is a..."
- "Everything that is a capital is a city, so London is a..."

Type propagation

- Members of superclasses:

(*) rdfs9, rdfs10, rdfs11 are the names of the inference rules in the W3C standard. A, B are classes; x is an instance.

Type propagation

– Members of superclasses:

– Reflexivity of sub-class relation:

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Type propagation

Members of superclasses:

Reflexivity of sub-class relation:

Transitivity of sub-class relation:

(*) rdfs9. rdfs10. rdfs11 are the names of the inference rules in the W3C standard. A. B are classes: x is an instance.

Type propagation: Examples

– Members of superclasses:

```
:City rdfs:subClassOf :PopulatedPlace . :london rdf:type :City . rdfs9
                :london rdf:type :PopulatedPlace .
```

Reflexivity of sub-class relation:

```
:City rdf:type rdfs:Class .
:City rdfs:subClassOf :City .
```

Transitivity of sub-class relation:

```
:City rdfs:subClassOf :PopulatedPlace . :PopulatedPlace rdfs:subClassOf :Place .
                                                                                    rdfs11
                          :City rdfs:subClassOf :Place .
```

Property Propagation

- Transitivity:

```
P rdfs:subPropertyOf Q . Q rdfs:subPropertyOf R . rdfs5
             P rdfs:subPropertvOf R .
```

(*) P, Q are properties; u, v are instances.

Property Propagation

- Transitivity:

- Reflexivity:

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Property Propagation

- Transitivity:

- Reflexivity:

– Property transfer:

(*) P, Q are properties; u, v are instances.

Property Propagation: Examples

- Transitivity:

```
:has_writer rdfs:subPropertyOf :has_author . :has_author rdfs:subPropertyOf :has_creator . rdfs:subPropertyOf :has_creator .
```

- Reflexivity:

```
:has_writer rdf:type rdf:Property .
:has_writer rdfs:subPropertyOf :has_writer .
```

– Property transfer:

```
:has_author rdfs:subPropertyOf :has_creator . :Hamlet :has_author :Shakespeare . rdfs
```

Domain and range propagation

Typing triggered by the use of properties.

- Domain propagation:

(*) P, Q are properties; x, y are instances.

Domain and range propagation

Typing triggered by the use of properties.

- Domain propagation:

- Range propagation:

(*) P, Q are properties; x, y are instances.

Domain and Range Propagation: Examples

Domain propagation:

```
:capitalOf rdfs:domain :City . :london :capitalOf :england .
                   :london rdf:type :City .
```

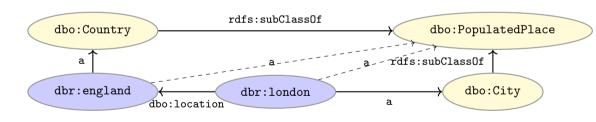
– Range propagation:

```
:capitalOf rdfs:range :Country . :london :capitalOf :england . rdfs3
                  :england rdf:type :Country .
```

RDFS inference rules in our example

```
dbo:City rdfs:subClassOf dbo:PopulatedPlace . dbr:london rdf:type dbo:City . dbr:london rdf:type dbo:PopulatedPace . rdfs9
```

```
dbo:Country rdfs:subClassOf dbo:PopulatedPlace . dbr:england rdf:type dbo:Country . dbr:england rdf:type dbo:PopulatedPlace . r
```



Inference rules in the OWL EL Profile

- Reasoning can be performed via saturation[†] (i.e., inference rules).
- For example:

† Using a saturation-based approach over an OWL 2 ontology is not possible.

ELK reasoner (also available as Protégé plugin): https://github.com/liveontologies/elk-reasoner/wiki

Inference rules in the OWL 2 RL Profile

Reasoning via full materialisation of the graph, similarly to RDFS inference rules. e.g.,:

 See W3C specification for further inference rules in OWL 2 RL in addition to the RDFS ones.

W3C: https://www.w3.org/TR/ow12-profiles/#Reasoning_in_OWL_2_RL_and_RDF_Graphs_using_Rules GraphDB: https://graphdb.ontotext.com/documentation/standard/reasoning.html

OWL 2 Important Practical Examples

Open World Assumptions

Closed World Assumption (CWA)

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

Open World Assumptions

Closed World Assumption (CWA)

- Complete knowledge.
- Any statement that is not known to be true is false. (*)
- Typical semantics for database systems.

Open World Assumption (**OWA**)

- Potential incomplete knowledge.
- (*) does not hold.
- Typical semantics for logic-based systems (including OWL).

Name Assumptions

Unique Name Assumption (UNA)

- Different names **always** denote different things.
 - $\mathsf{E.g.}, \, a^{\mathcal{I}} \neq b^{\mathcal{I}}.$
 - common in relational databases.

Name Assumptions

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Non-unique Name Assumption (NUNA)

- Different names need not denote different things. As in OWL.
 - dbpedia: $Person^{\mathcal{I}} = foaf: Person^{\mathcal{I}}$.
 - wikidata:ernesto $^{\mathcal{I}}$ = city:ernesto $^{\mathcal{I}}$

Name Assumptions

Unique Name Assumption (UNA)

- Different names always denote different things.
 - E.g., $a^{\mathcal{I}} \neq b^{\mathcal{I}}$.
 - common in relational databases.

Non-unique Name Assumption (NUNA)

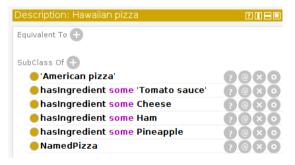
- Different names need not denote different things. As in OWL.
 - dbpedia: $Person^{\mathcal{I}} = foaf : Person^{\mathcal{I}}$.
 - wikidata:ernesto^{\mathcal{I}} = city:ernesto^{\mathcal{I}}

Equal names (e.g., URIs) always denote the same "thing".

- E.g., cannot have city:ernesto^{\mathcal{I}} \neq city:ernesto^{\mathcal{I}}.

Necessary conditions and primitive classes

Hawaiian pizza **implies** having pineapple as ingredient (among others); but not the other way round.



Sufficient conditions and defined classes

Meat pizza **implies** having meat as ingredient (and being pizza).

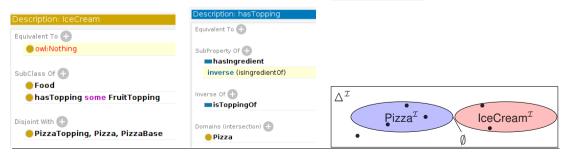
A pizza with meat as ingredient **implies** being a meat pizza.

Hawaiian pizzas have ham as ingredient and thus they are meat pizzas.



Detecting modelling errors

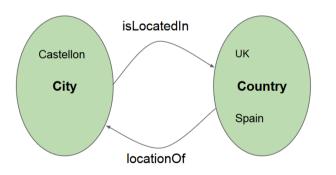
- Ice cream implies having fruit as topping
- Ice cream is disjoint with Pizza
- The domain of has topping is pizza, that is, having any topping implies being a pizza.
- Domain is a type of <u>sufficient condition</u>, global scope for the property.

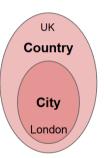


Common mistakes: part-of VS subclass-of (i)

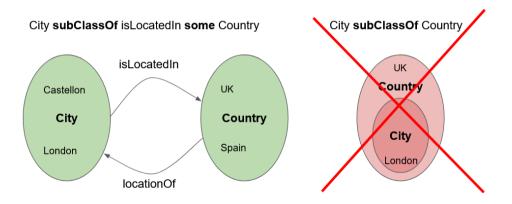
City subClassOf isLocatedIn some Country

City subClassOf Country



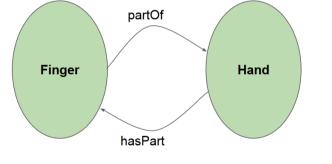


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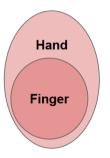


Common mistakes: part-of VS subclass-of (ii)

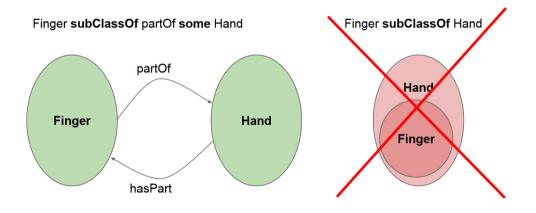
Finger subClassOf partOf some Hand



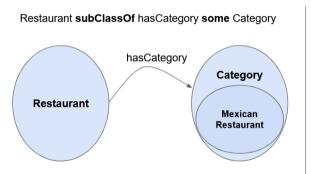
Finger subClassOf Hand



Common mistakes: part-of VS subclass-of (ii)



Common mistakes: part-of VS subclass-of (iii)

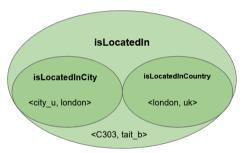


Mexican_Restaurant **subClassOf** Restaurant

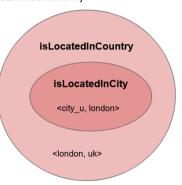


Common mistakes: property hierarchy

isLocatedInCity **subPropertyOf** isLocatedIn isLocatedInCountry **subPropertyOf** isLocatedIn

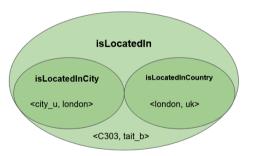


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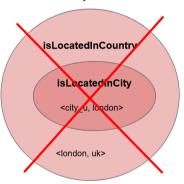


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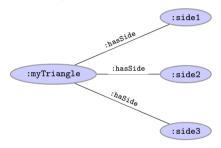


isLocatedInCity **subPropertyOf** isLocatedinCountry



OWL 2 and Open World Assumption

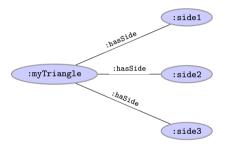
- :Triangle EquivalentTo :hasSide exactly 3 :Side



- is :myTriangle a :Triangle?

OWL 2 and Open World Assumption

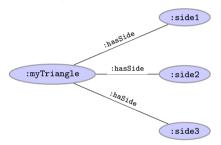
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- is :myTriangle a :Triangle? I don't know because of OWA and NUNA.

OWL 2 and Open World Assumption

- :Triangle EquivalentTo :hasSide exactly 3 :Side



- is :myTriangle a :Triangle? I don't know because of OWA and NUNA.
- Solution: deductive reasoning complemented with SPARQL queries (in this case with aggregates) → SPARQL assumes a CWA.

Graph Database Solutions

How to store Graph models?

- Relational model
 - Single table with 3 columns (source, edge, target)
 - Property tables (one table per type of entity, e.g., Person, Module)
 - Binary tables (one table per relationship, e.g., source, target)

M. Wylot and others. RDF Data Storage and Query Processing Schemes. ACM Computing Surveys 2018

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 - Single table with 3 columns (source, edge, target)
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 - Binary tables (one table per relationship, e.g., source, target)
- Graph-based databases (NoSQL)

M. Wylot and others. RDF Data Storage and Query Processing Schemes. ACM Computing Surveys 2018

Graph database solutions

- Scale to large Knowledge Graphs.
- Sophisticated indexing structures.
- Optimised reasoning.
- Fast query performance.
- Server solution in production.

State-of-the-art solutions

Dimensions:

- Free version.
- Compliance with Semantic Web standards.
- Reasoning capabilities.
- In-memory or In-disk.
- Documentation and installation requirements.
- Additional features.

A Survey of RDF Stores & SPARQL Engines for Querying Knowledge Graphs. arXiv:2102.13027 2021 (Appendix A)

Semantic Web standards

- The World Wide Web Consortium (W3C) is an international community that develops open standards to ensure the long-term growth of the Web: https://www.w3.org/
- On the Web and beyond.

– Why standards?

- broader industry (and academic) agreement,
- interoperability across organizations and applications,
- avoids vendor lock-in of a particular (exchange or query) format.

Apache Jena TDB

- Free solution.
- Provides a native (in-disk) RDF store.
- In combination with Jena Fuseki to provide SPARQL Endpoint support.
- Supports reasoning as in Jena, but not direct support for OWL 2 nor the OWL 2 profiles.

https://jena.apache.org/documentation/tdb/

OpenLink Virtuoso

- Provides the SPARQL endpoint for DBpedia.
- Open source and commercial versions.
- Object-oriented database model.
- ✓ Native graph model storage provider for Jena and RDF4J.
- Custom inference rules. Partial support for OWL 2.

https://virtuoso.openlinksw.com/

http://vos.openlinksw.com/owiki/wiki/VOS

Blazegraph

- Provides the SPARQL Endpoint for Wikidata.
- Free and open source.
- Both in-memory and disk-oriented storage.
- Only supports OWL 1 Lite reasoning.
- Blazegraph team now working for Amazon.

https://blazegraph.com/

AllegroGraph

- Free and commercial licenses.
- Support for OWL 2 RL materialization.
- Client interface in several languages.
- Can be used to query both documents and graph data (via SPARQL).

https://allegrograph.com/

Neo4j

- Open source graph database.
- Based on the Property Graph Model.
- Cypher as graph query language (no native SPARQL support).
- Support via a plugin for RDF, RDFS and OWL vocabularies.
- X Basic inferencing support.
- Support for Analytics.
- Interfaces in many languages.

https://neo4i.com/

GraphDB (formerly OWLIM)

- Free and commercial versions.
- Very easy to install and use.
- ✓ Powerful reasoning features: including OWL 2 QL and RL profiles.
- Supports SHACL validation.
- Includes text indexing via lucene.
- Powered the early Linked Data services at the BBC.

https://www.ontotext.com/products/graphdb/

RDFox

- Commercial system. Free academic license on request.
- Support for materialization-based datalog reasoning (including OWL 2 RL and SWRL rules).
- Supports SHACL validation.
- In-memory RDF engine.
- ✓ Access via Java API or remotely via REST API or SPARQL Endpoint.
- Limitation on the size of the memory.

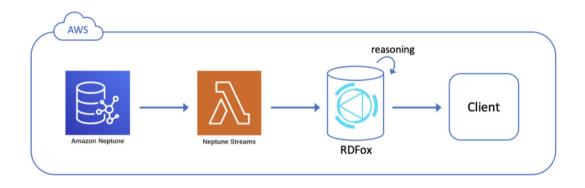
https://www.oxfordsemantic.tech/product

Amazon Neptune

- Cloud-based only solution.
- Blazegraph is now part of Amazon Neptune.
- On-Demand pricing.
- Native inferencing is not yet supported.
- Keep an eye on future development!

https://aws.amazon.com/neptune/

Amazon Neptune + RDFox



Amazon Neptune and RDFox: https://aws.amazon.com/blogs/database/use-semantic-reasoning-to-infer-new-facts-from-your-rdf-graph-by-integrating-rdfox-with-amazon-neptune/

Graph database/Triplestore benchmarking

- Oracle Database 12c: 1.08 Trillion triples
- AnzoGraph DB: 1.06 Trillion triples
- AllegroGraph: 1.0 Trillion triples
- Virtuoso: 94.2 Billion Triples
- Stardog: 50 Billion triples
- **RDFox**: 19.47 Billion triples
- GraphDB: 17 Billion triples
- Apache Jena TBD: 16.7 billion triples.

```
Numbers may not be up-to-date: https://www.w3.org/wiki/LargeTripleStores
https://medium.com/wallscope/comparison-of-linked-data-triplestores-a-new-contender-c62ae04901d3
https://medium.com/wallscope/comparing-linked-data-triplestores-ebfac8c3ad4f
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Laboratory: Hands-on SPARQL

SPARQL: local and remote KG access

