# CM30171

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# December 6, 2016

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## 1 Overview

This report is an explanation of the design decisions undertaken while writing a –C compiler and interpreter. The project was written in C and involves three different sections of code, an interpreter, TAC compiler and MIPS compiler.

The interpreter for –C handles functions, closures, if - else statements and while loops. It uses an environment comprised of frames to store variable values in different scopes. Each variable can either be a integer or closure.

The TAC Compiler supports the same features as the interpreter. It translates the –C code into TAC blocks and performs block level optimistation to reduce the number of instructions generated. In order to perform this optimisation the next use information is calculated for each of the blocks. [1]

## 2 Code Interpretation

In order to interpret –C code the abstract syntax tree is walked, at each node the left and right children are compiled and the nodes operation is applied to them. In order to support both integer and closure return types all the functions which handle node interpretation return a union structure which either contains the integer value or a pointer to the closure. The interpreter supports variable assignment, closures, if-else and while statements I will explain each now.

#### 2.1 Variable Assignment

In order to store a value an environment structure was implemented this consists of a list of frames, one for each scope in the program, and each frame contains a list of bindings of token to union. The environment is added to each type a variable assignment is made and new frames are added each time a new scope is entered, frames are removed from the list when this scope is left.

#### 2.2 Closures & Functions

In order to store and call closures there is a closure structure this holds a pointer to the environment frame the closure was defined in and also a pointer to the start node of the AST that defines the function. Then when a closure is applied the variable is pulled out of the environment and the AST interpreted with the environment it was defined with.

The interpretation of the functions AST continues until a return node is found, at this point the hasReturned field is set. When the has returned field is set no other lines of code in the current function are executed and the function returns this value.

#### 2.3 Control Structure

There are two types of control structure in –C the if-else and while loop. In order to interpret an if - else statement the condition is interpreted and depending on if the value is non-zero or not either the right or left child.

For the while loop firstly the conditional is returned then the body, this is repeated while the conditional is non-zero.

## 3 Intermediate Code Generation

#### 3.1 TAC Design

The three address code used in the compiler was designed to be abstract enough as too keep any machine dependent decisions out of the TAC stage. Many of the instructions are obvious such as store and mathematic operations, examples below, and they won't be explained in great detail.

```
r2 := 1

r3 := r1 / r2
```

One thing to note about the store instruction is that in the event that the store operand is defined in the scope above the current scope like x is in the following example.

```
int main()
{
  int x = 4;
  int test()
  {
    return x;
  }
  return test();
}
```

In that scenario the store command in the test function will have an extra piece of information saying that its defined in the scope one level above, so the store command will look like the following.

```
DEFINED IN 1 r2 := x
```

This information is also included when a closure is called from a narrower scope, the TAC would be as follows.

#### CALL \_1 FROM SCOPE 1

For Functions a label instruction denotes the start and a end label for the end. After the start label the new activation frame instruction which tells the compiler to allocate space for a new activation frame with a given number of arguments, locals and tempories. Before the end there is a return instruction which contains the register with the value to return. Below is an example function in TAC.

```
_{-1}: NEW FRAME 0 arg 0 loc 1 temp DEFINED IN 1 r2 := x RETURN r2 FUNCTION END
```

There is one type of control sequence in the language, the if else, the way this is described in TAC is using a sequence of if instructions and labels denoting the various bodies if the if and else parts. An example in -C and the corresponding TAC are below.

```
if (1 > 4) {
   return 4;
} else if (2 > 1) {
   return 3;
}
```

```
\begin{array}{l} {\rm r1} \; := \; 1 \\ {\rm r2} \; := \; 4 \\ {\rm r3} \; := \; 1 \; > \; 4 \\ {\rm IF} \; {\rm NOT} \; {\rm r3} \; {\rm GOTO} \; 1 \\ {\rm r4} \; := \; 4 \\ {\rm REFURN} \; \; 4 \\ {\rm GOTO} \; 2 \\ {\rm LABEL} \; 1 \colon \; {\rm r5} \; := \; 2 \\ {\rm r6} \; := \; 1 \\ {\rm r7} \; := \; 2 \; > \; 1 \\ {\rm IF} \; {\rm NOT} \; {\rm r7} \; {\rm GOTO} \; 3 \\ {\rm r8} \; := \; 3 \\ {\rm REFURN} \; 3 \\ {\rm LABEL} \; 3 \colon \; {\rm LABEL} \; 2 \colon \\ \end{array}
```

Finally there is one loop type in the language, the while loop, this is translated into a goto, an if and a label at the top and bottom of the loop body. the while condition is placed after the body. n example in  $-\mathbf{C}$  and the corresponding TAC are below.

```
\begin{array}{l} \text{int } x = 0; \\ \text{while } (x < 5) \\ \{ \\ x = x + 1; \\ \} \\ \end{array} \begin{array}{l} r1 := 0 \\ x := r1 \\ \text{GOTO 1} \\ \text{LABEL 2: } r2 := x \\ r3 := 1 \\ r4 := r2 + r3 \\ x := r4 \\ \text{LABEL 1: } r5 := x \\ r6 := 5 \\ r7 := r5 < r6 \\ \text{IF } r7 \text{ GOTO 2} \end{array}
```

#### 3.1.1 List of TAC instuctions

```
x := y > z

x := y >= z

x := y <= z

LABEL x:

GOTO x

IF NOT x GOTO y

CREATE CLOSURE x

x:

ALLOCATE PARAMS x

SAVE PARAM x

NEW FRAME x arg y loc z temp

RETURN x

FUNCTION END
```

Store the result of y > z in xSStore the result of y <= z in xStore the result of y >= z in xCreate a label with the name xjump to the label with name xIf x has the value 0 jump to ydefine closure with the code label xAlso a label of value xAllocate a space for x parameters Save x in the next parameter space Allocate space for the activation frame Return the value in xA tag for the end of the function

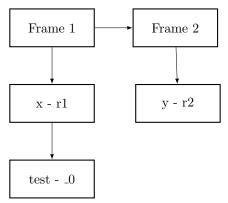
#### 3.2 TAC Generation

All the TAC complilation is done in the tac\_compliler.c file. In order to generate the TAC from source code a tree walk is performed over the parse tree at each node depending on the type a set of TAC instructions are created and added to the current TAC block. If a new function is found a new TAC block is created before that part of the tree is parsed, also if a goto or label TAC instruction are created new blocks are created. When a leaf is reached a store instruction is created for the value at the leaf.

#### 3.2.1 Environment Structure

In order to keep track of the location of any local variables in the code and environment is created to store the association between token and register location. The environment is made up of frames each frame corresponds to a scope in the program and has a linked list of all locals in that scope. The frames also contain a linked list of the functions defined, these are a pair of token and label assigned to the function. For example the environment created while walking the following piece of code is shown below.

```
int main()
{
  int x = 4;
  int test()
  {
    int y = 5;
    return x * y;
  }
  return test();
}
```

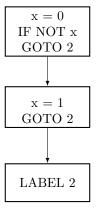


As you can see the environment holds the association between the tokens of the variables and functions with the TAC register location and the function label respectively.

#### 3.2.2 TAC Blocking

The diffrent blocks of TAC code, between labels and jumps, are separated to allow easier optimisation and MIPS translation. As the AST is walked if a instruction which requires a jump (If, While, Function Call) is found a new block is created and set as the current block after the jump. Similarly if a label is created a new block is created and the label is assigned to that new block.

in order to compile the code in the same order as the TAC each block has a link to the block which was created from the code directly after it. A Simple example is given below.



This was done so that the MIPS compilation step can easily follow the sequence of TAC instructions. //TODO write about linking blocks if and when done

#### 3.2.3 Inner functions

In order to implement inner functions, functions defined inside another, in TAC the code for the function must be flattened so that there are no functions in functions in the TAC. To do this when a function definition is reached inside another the current TAC block is stored and another is created for the inner function, once the inner function's AST has finished being walked the previous block is restored as the current block and the AST tree walk continues. This gives the result of placing any inner functions after the function it was defined in.

#### 3.3 Next Use Info

As the TAC instructions are broken down into blocks next use information can be worked out to allow optimisation. The next use info for a block is calculated by using a recursive function which looks at each instruction in term from bottom to top. A list of NEXT\_USE\_INFO structures is used, one structure for each variable used in the block. Each NEXT\_USE\_INFO structure contains a list of the uses of that variable and the associated liveness at that point. This is all done in the nextUseInfo.c file.

## 3.4 TAC Optimisation

After the TAC generation phase has been completed the sequence of blocks is handed over to the optimisation phase. This is in the tac\_optimiser.c file. This applies constant folding, copy propagation, dead code elimination, common sub expression elimination and algebraic transformations algorithms to the TAC block repeatedly till now change can be made. Each TAC block is processed from bottom to top for each optimisation technique.

#### 3.4.1 Copy Propagation

Copy propagation looks for a store instruction, once on is found it checks the rest of the code below the store until it finds a write to the store destination. For every read of the destination before replaced the use is replaced with the stores operand. To demonstrate this copy propergation was applied to the same example as above.

#### 3.4.2 Constant Folding

The constant folding function looks for arithmetic operations and replaces them with the result where possible. This is done by looking for a operation where both operands are tokens with type constant. Below is an example using both constant folding and copy propergation.

	r1 := 4	r1 := 4
	x := 4	x := 4
int $x = 4$ ;	r2 := 6	r2 := 6
int	y := 6	y := 6
$\mathbf{m} \mathbf{v} = \mathbf{v},$	r3 := 4	r3 := 4
roturn v l v	r4 := 6	r4 := 6
return x + y;	r5 := 4 + 6	r5 := 10
	RETURN r5	RETURN 10

#### 3.4.3 Dead Code Elimination

Dead code elimination works by analysing each instruction using and useing the next use info removes them if not needed. Firstly this is only done for registers user defined variables are live at the end of the block so an't removed. A instruction is removed if the next use is not live, its another write, or there isn't another next use. Using the same example as above and applying dead code elimination gives the following.

The function which completed the dead code elimination step does not recalculate the number of tempories in the code. So when the activation record is allocated it will be for the original number of registers, which can waste a lot of memory. This would be easy to recompute but I ran out of time.

#### 3.4.4 Common Sub Expression Elimination

If two expression have the same operands and operation the later one can be replaced with a store of the destination of the first. These are found by looking for pairs of arithmatic operations, when one is found if the operation and operands are the same the second is replaced with a store. An exaple is given below usign this method in conjunction with copy propergation.

```
r1 := 4
                                     r1 := 4
                                     r2 := 6
                  r3 := r1 * r2
                                     r3 := 4
                  c := r3
                                     c := r3
int c = 4 * 6;
                  r4 := 4
                                     r4 := 4
int d = 4 * 6:
                  r5 := 6
                                     r5 := 6
                  r6 := r4 * r5
                                     r6 := r3
return c;
                  d := r6
                                     d := r3
                  r7 := c
                                     r7 := r3
                  RETURN r7
                                     RETURN r3
```

#### 3.4.5 Algebraic Transformations

The final optimisation technique is to transform some algebraic expressions which will always give 1 or 0 to those values. In order to do this the optimiser looks for those specific expressions and simply replaces them with a store of either 1 or 0 depending on the expression. An example is given below using copy propagation aswell.

```
CALL _1
                                     CALL _1
                  r2 := result
                                     r2 := result
                  x := result
                                     x := result
int x = test();
                  r3 := 0
                                     r3 := 0
int a = 0 + x;
                  r4 := result
                                     r4 := result
                  r5 := 0 + result \quad r5 := result
return a;
                  a := r5
                                     a := result
                  r6 := r5
                                     r6 := result
                  RETURN r5
                                     RETURN result
```

### 4 Machine Code Generation

After the TAC is generated and optimised the code is translated to MIPS assembler. This is done block by block in the order the TAC was generated. Before the user code is compiled a global MIPS block is added which allocates memory for global scope functions and sets up the environment used for variable lookup. A decision was made to store all variables in memory and ignore the problem of register assignment, this makes the compiler simpler however reduces its performance. The files associated with this section of the compiler are compiler.c and MIPS.c.

In order for the users code to be run the main function has to be found as it was renamed by the TAC to  $_0$ . Amips main function is added at the head of the mips this contains a dynamical location of

#### 4.0.6 Functions

When a function is compiled the first thing that happens is the number of locals, temporaries and arguments are counted and a space big enough for all these is allocated. This activation frame also contains space for the return address, previous frame and enclosing frame. These are structured as shown in the diagram below.

//TODO draw diagram

One this is created and the first 3 spaces filled the arguments are all loaded into the next spaces in the frame. Any arguments are loaded from the memory pointed by \$a0. The function code is then compiled. The final section of the code is to return to the calling code, any result is moved to \$v0 the previous frame is restored into the \$fp and the return address jumped to. Below is a simple function example in mips with annotations.

```
function1:
                                             (1)
                          move $t2 $a0
                                             (2)
                          li $a0 40
                                             (3)
                          li $v0 9
                                             (4)
                          syscall
                                             (6)
                          move $t0 $fp
                                             (5)
                          move $fp $v0
                                             (6)
                          sw $t0 \ 0($fp)
                                             (7)
                          sw $ra 4($fp)
                                             (8)
                             $a1
                                  8($fp)
                                             (9)
                             $t1 0($t2)
int times (int n, int d) lw
                                             (10)
                             \$t1
                                 12($fp)
                             $t1 4($t2)
  return n * d;
                             $t1 16($fp)
                             $t1 12($fp)
                                             (11)
                          lw $t2 16($fp)
                          mult $t1 $t2
                          mflo $t0
                          sw $t0 20($fp)
                          lw $v0 20($fp)
                                             (12)
                          lw $t0 4($fp)
                                             (13)
                          lw $fp 0($fp)
                                             (14)
                          jr $t0
                                             (15)
```

- 1. Function label
- 2. Move argument pointer into tempory register
- 3. set the number of bytes required to allocate
- 4. set the syscode for memory allocation
- 5. Move the old frame pointer into a temporary register

- 6. Save the new frame pointer
- 7. Put the previous frame pointer in the frame
- 8. Put the return adderess in the frame
- 9. The enclosing scope is passed in \$a1 so store this in the frame
- 10. for both arguments load them from the arg pointer and store in the frame
- 11. Do the function body
- 12. store the return value in \$v0
- 13. load the return address
- 14. restore the previous frame pointer
- 15. jump to the return address

#### 4.0.7 Environment

In order for the location of tokens and TAC registers to be found they are stored in an environment. The environment is made up of several frames each of which store information about a different scope in the program. Each frame holds the association between either TAC registers or tokens and there memory locations which are defined in that scope.

#### 4.0.8 Closures

In order to have closures we need to define the pair of program code and environment. The structure for a closure in MIPS is using a 8 byte object the first word is the address of the function code and the second if the address where the frame the closure was defined in is stored. When a closure is called the enclosing frame is placed in \$a1 and the program code is jumped to. Below is an example of the definition of a closure.

Then when the closure is called the following code is generated.

## References

[1] Gnu basic blocks. https://gcc.gnu.org/onlinedocs/gccint/Basic-Blocks.html. Accessed: 06-12-2016.

## 5 Testing

Both the compiler and the interpretter had tests writtern for them, these are run by a python script "test.py" and were run after each change was made to check nothing had been broken. The interpreter test simply runs the code with an example and checks the output has the correct value. In order to automatically test the compiler I had to write a custom error handler script which calls the main function then prints the returned value out, with this the spim command line tool can be used to check the values returned by the mips code are correct.

## 5.1 Interpretation

The interpreter was run with various test cases, the results from some of these cases are shown below along with the result returned from the interpreter.

#### 5.1.1 Math Test - test\_math.c

```
int main()
{
    return 8 * 2 - 2;
}

RESULT - 14
5.1.2 Simple Test - test_simple.c

int main()
{
    int y;
    int x = 4;
    y = 4;
    return x + y;
}

RESULT - 8
5.1.3 If Else Test - test_if_else.c

int main()
{
    if (1 > 4) {
        return 4;
    } else if (2 > 1) {
```

```
return 3;
     return 8;
}
RESULT - 3
5.1.4 While Test - test_while.c
int main()
     int x = 0;
     while (x < 5)
       x = x + 1;
     return x;
}
RESULT - 5
{\bf 5.1.5} \quad {\bf Function \ Test - test\_function.c}
int test()
  return 4;
int main()
  return test();
RESULT - 4
{\bf 5.1.6}\quad {\bf Function\ With\ Arguments\ Test\ -\ test\_function\_args.c}
int times (int n, int d)
  return n * d;
int main()
  return times (3, 2);
RESULT - 6
{\bf 5.1.7} \quad {\bf Inner \ Function \ Test - test\_inner func.c}
```

```
int times2(int n) {
  int times (int n, int m) {
    return n * m;
  return times(n, 2);
}
int main()
  return times2(3);
RESULT - 6
5.1.8 Twice Test - test_twice.c
function twice (function f) {
  int g(int x) \{ return f(f(x)); \}
  return g;
}
void main()
  int addten(int n) {return n + 10;}
  return twice (addten)(2);
RESULT - 22
5.1.9 Cplus Test - test_cplus.c
function cplus(int a) {
  int cplusa(int b) { return a+b; }
  return cplusa;
int main()
  return cplus (5)(2);
RESULT - 7
5.1.10 Factorial Test - test_fact.c
int fact(int n) {
    int inner_fact(int n, int a) {
      if (n==0) return a;
        return inner_fact (n-1,a*n);
```

```
return inner_fact(n,1);
}
int main()
{
   return fact(4);
}
RESULT - 24
```

## 5.2 Compiler

In order to test both the TAC and MIPS compilation stages various –C programs were run though the compiler and the result they leave in the return register was checked with the expected value. In order to make this simpler a new exception handler was writtern for the spim interpreter which prints the value left in \$v0 after the user code is run. The compilation is done by using "./mycc -c FileName" and then running it in spim using "spim -exception\_file testExceptionHandler.s -file Output/test.asm". Given this here are a few example test cases there TAC and MIPS code and result value.

#### 5.2.1 Math Test - test\_math.c

```
int main()
    return 8 * 2 - 2;
}
DEFINE CLOSURE _0
_{-}0:
NEW FRAME 0 arg 0 loc 5 temp
RETURN 14
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
```

```
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 32
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 14
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 14
5.2.2 Simple Test - test_simple.c
int main()
    int y;
    int x = 4;
    y = 4;
    return x + y;
}
DEFINE CLOSURE _0
NEW FRAME 0 arg 3 loc 4 temp
RETURN 8
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
```

```
la $t1 function0
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 8
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 8
5.2.3 If Else Test - test_if_else.c
int main()
    if (1 > 4) {
      return 4;
    else if (2 > 1) {
      return 3;
    }
    return 8;
}
DEFINE CLOSURE _0
NEW FRAME 0 arg 0 loc 9 temp
r3 := 0
IF NOT r3 GOTO 1
RETURN 4
GOTO 2
LABEL 1: r7 := 1
IF NOT r7 GOTO 3
```

```
RETURN 3
LABEL 3: LABEL 2: RETURN 8
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 48
li $v0 9
syscall
move $t0 $fp
move \$fp \$v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 0
sw $t0 12($fp)
lw $t2 12($fp)
beq $t2 $zero label1
1i \$v0 4
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
j label2
label1:
li $t0 1
sw $t0 16($fp)
lw $t2 16($fp)
beq $t2 $zero label3
li $v0 3
```

```
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
label3:
label2:
li $v0 8
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 3
5.2.4 While Test - test_while.c
int main()
    int x = 0;
    while (x < 5)
     x = x + 1;
   return x;
}
DEFINE CLOSURE _{-}0
NEW FRAME 0 arg 2 loc 8 temp
x := 0
GOTO 1
x := r4
IF r7 GOTO 2
RETURN x
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
```

```
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 52
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 0
sw $t0 12($fp)
j label1
label2:
lw $t1 12($fp)
li $t2 1
add $t0 $t1 $t2
sw $t0 16($fp)
lw $t0 16($fp)
sw $t0 12($fp)
label1:
lw $t1 12($fp)
li $t2 5
sltu $t0 $t1 $t2
sw $t0 20($fp)
lw $t2 20($fp)
bne $t2 $zero label2
lw $v0 12($fp)
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 5
5.2.5 Function Test - test_function.c
int test()
  return 4;
```

```
int main()
  return test();
DEFINE CLOSURE _1
DEFINE CLOSURE _0
NEW FRAME 0 arg 0 loc 1 temp
RETURN 4
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 2 temp
ALLOCATE PARAMS 0
CALL _1 FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 20
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 16
```

```
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 4
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 20
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $a0 0
li $v0 9
syscall
move $a0 $v0
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 4
5.2.6 Function With Arguments Test - test_function_args.c
int times (int n, int d)
  return n * d;
int main()
```

```
return times (3, 2);
DEFINE CLOSURE _1
DEFINE CLOSURE _0
NEW FRAME 2 arg 2 loc 3 temp
LOAD PARAM n
LOAD PARAM d
r3 := n * d
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 4 temp
r4 := 3
r5 := 2
ALLOCATE PARAMS 2
SAVE PARAM r4
SAVE PARAM r_5
CALL _1 FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 20
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw \$fp 4(\$v0)
sw $v0 16($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
```

```
jr $t0
function1:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
lw $t2 16($fp)
mult $t1 $t2
mflo $t0
sw $t0 20($fp)
lw $v0 20($fp)
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
function 0:
move $t2 $a0
li $a0 28
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 3
sw $t0 12($fp)
li $t0 2
sw $t0 16($fp)
li $a0 8
li $v0 9
syscall
move $a0 $v0
lw $t0 12($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 16($fp)
```

```
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move \$v0 \$v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 6
5.2.7 Inner Function Test - test_innerfunc.c
int times2(int n) {
  int times (int n, int m) {
    return n * m;
  return times (n, 2);
int main()
  return times2(3);
DEFINE CLOSURE _1
NEW FRAME 1 arg 1 loc 4 temp
LOAD PARAM n
DEFINE CLOSURE _2
r4 := n
r5 := 2
ALLOCATE PARAMS 2
SAVE PARAM r4
SAVE PARAM r5
CALL _2 FROM SCOPE 0
RETURN result
FUNCTION END
DEFINE CLOSURE _0
NEW FRAME 2 arg 2 loc 3 temp
LOAD PARAM n
LOAD PARAM m
```

```
r3 := n * m
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 3 temp
r7 := 3
ALLOCATE PARAMS 1
SAVE PARAM r7
CALL _1 FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function 1:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
```

```
sw $fp 4($v0)
sw $v0 16($fp)
lw $t0 12($fp)
sw $t0 20($fp)
li $t0 2
sw $t0 24($fp)
li $a0 8
li $v0 9
syscall
move \$a0 \$v0
lw $t0 20($fp)
sw $t0 0($v0)
addi v0 v0 4
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw \$fp 4(\$v0)
sw $v0 28($fp)
function2:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
```

```
lw $t2 16($fp)
mult \$t1 \$t2
mflo $t0
sw $t0 20($fp)
lw $v0 20($fp)
lw $t0 4($fp)
lw \$fp 0(\$fp)
jr $t0
function0:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 3
sw $t0 12($fp)
li $a0 4
li $v0 9
syscall
move \$a0 \$v0
lw $t0 12($fp)
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 6
5.2.8 Twice Test - test_twice.c
function twice(function f) {
  int g(int x) \{ return f(f(x)); \}
  return g;
}
```

```
void main()
  int addten(int n) {return n + 10;}
  return twice (addten)(2);
DEFINE CLOSURE _1
_{-1} :
NEW FRAME 1 arg 1 loc 1 temp
LOAD PARAM f
DEFINE CLOSURE _2
RETURN 2
FUNCTION END
DEFINE CLOSURE _0
_{-}2:
NEW FRAME 1 arg 1 loc 5 temp
LOAD PARAM x
r1 := x
ALLOCATE PARAMS 1
SAVE PARAM r1
CALL _0 FROM SCOPE 1
r2 := result
ALLOCATE PARAMS 1
SAVE PARAM r2
CALL _{-}0 FROM SCOPE 1
RETURN result
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 6 temp
DEFINE CLOSURE _3
r8 := 3
ALLOCATE PARAMS 1
SAVE PARAM r8
CALL _1 FROM SCOPE 1
r9 := result
r10 \ := \ 2
ALLOCATE PARAMS 1
SAVE PARAM r10
CALL r9 FROM SCOPE 0
RETURN result
FUNCTION END
_3:
NEW FRAME 1 arg 1 loc 3 temp
LOAD PARAM n
r7 := n + 10
RETURN r7
```

#### FUNCTION END

```
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw \ \$fp \ 0\,(\,\$fp\,)
jr $t0
li $a0 8
li $v0 9
syscall
```

la \$t1 function0

```
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 20($fp)
function2:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t0 12($fp)
sw $t0 16($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 16($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 20($fp)
li $a0 4
li $v0 9
syscall
move \$a0 \$v0
lw $t0 20($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move \$v0 \$v0
```

```
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $a0 8
li $v0 9
syscall
la $t1 function3
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
lw $t0 12($fp)
sw $t0 16($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 16($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 20($fp)
li $t0 2
sw $t0 24($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 24($fp)
sw $t0 0($v0)
addi v0 v0 4
```

```
lw $t0 20($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
function3:
move $t2 $a0
li $a0 32
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 12($fp)
li $t2 10
add $t0 $t1 $t2
sw $t0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 22
5.2.9 Cplus Test - test_cplus.c
function cplus(int a) {
  int cplusa(int b) { return a+b; }
  return cplusa;
int main()
  return cplus (5)(2);
DEFINE CLOSURE _1
_1:
NEW FRAME 1 arg 1 loc 1 temp
LOAD PARAM a
```

```
DEFINE CLOSURE _{-2}
RETURN 2
FUNCTION END
DEFINE CLOSURE _0
_{-2} :
NEW FRAME 1 arg 1 loc 3 temp
LOAD PARAM b
DEFINED IN 1 r1 := a
r3 := r1 + b
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 6 temp
r5 := 5
ALLOCATE PARAMS 1
SAVE PARAM r5
CALL _1 FROM SCOPE 1
r6 := result
r7 := 2
ALLOCATE PARAMS 1
SAVE PARAM r7
CALL r6 FROM SCOPE 0
RETURN result
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 24
li $v0 9
```

```
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw \$fp 0(\$fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 20($fp)
function2:
move $t2 $a0
li $a0 32
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 \ 0($t2)
sw $t1 12($fp)
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
sw $t0 16($fp)
lw $t1 16($fp)
lw $t2 12($fp)
add $t0 $t1 $t2
sw $t0 20($fp)
```

```
lw $v0 20($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 5
sw $t0 12($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 12($fp)
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 16($fp)
li $t0 2
sw $t0 20($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 20($fp)
sw $t0 0($v0)
addi v0 v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
```

```
lw $fp 0($fp)
jr $t0
RESULT - 7
5.2.10 Factorial Test - test_fact.c
int fact(int n) {
    int inner_fact(int n, int a) {
      if (n==0) return a;
        return inner_fact (n-1,a*n);
    return inner_fact(n,1);
}
int main()
  return fact (4);
DEFINE CLOSURE _1
NEW FRAME 1 arg 1 loc 4 temp
LOAD PARAM n
DEFINE CLOSURE _{-}2
r12 := n
r13 \ := \ 1
ALLOCATE PARAMS 2
SAVE PARAM r12
SAVE PARAM r13
CALL _2 FROM SCOPE _0
RETURN result
FUNCTION END
DEFINE CLOSURE _0
_{-}2:
NEW FRAME 2 arg 2 loc 12 temp
LOAD PARAM n
LOAD PARAM a
r3 := n == 0
IF NOT r3 GOTO 1
RETURN a
LABEL 1: r7 := n - 1
r10 := a * n
ALLOCATE PARAMS 2
SAVE PARAM r7
SAVE PARAM r10
```

```
CALL _2 FROM SCOPE 1
RETURN result
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 3 temp
r15 \ := \ 4
ALLOCATE PARAMS 1
SAVE PARAM r15
CALL _1 FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function 1:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
```

```
sw $fp 4($v0)
sw $v0 16($fp)
lw $t0 12($fp)
sw $t0 20($fp)
li $t0 1
sw $t0 24($fp)
li $a0 8
li $v0 9
syscall
move \$a0 \$v0
lw $t0 20($fp)
sw $t0 0($v0)
addi v0 v0 4
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 28($fp)
function2:
move $t2 $a0
li $a0 76
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
```

```
li $t2 0
sub \$t0 \$t1 \$t2
sltu $t0 $zero $t0
xori $t0 $t0 1
sw $t0 20($fp)
lw $t2 20($fp)
beq $t2 $zero label1
lw $v0 16($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
label1:
lw $t1 12($fp)
li $t2 1
sub $t0 $t1 $t2
sw $t0 24($fp)
lw $t1 16($fp)
lw $t2 12($fp)
mult \$t1 \$t2
mflo $t0
sw $t0 28($fp)
li $a0 8
li $v0 9
syscall
move $a0 $v0
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 28($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 16($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
function0:
move $t2 $a0
li $a0 24
li $v0 9
syscall
```

```
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 4
sw $t0 12($fp)
li $a0 4
li $v0 9
syscall
move \$a0 \$v0
lw $t0 12($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move \$v0 \$v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 24
```

## 6 Examples