# CM30171

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# 1 Overview

This report is an explanation of the design decisions undertaken while writing a –C compiler and interpreter. The project was writtern in C and involves three

different sections of code, an interpreter, TAC compiler and MIPS compiler.

Todo bit on interpreter The TAC Compiler performs a walk over the AST at each node a section of TAC is created. The TAC is separated into blocks between each label and jump, this allows next use information to be generated in order for easy TAC optimisation.

For the MIPS the problem of delayed branching was ignored to simplify the compiler and due to time constraints I didn't get round to adding the required nops into the compiler.

# 2 Code Interpretation

# 3 Intermediate Code Generation

## 3.1 TAC Design

The three address code used in the compiler was designed to be abstract enough as too keep any machine dependent decisions out of the TAC stage. Many of the instructions are obvious such as store and mathematic operations, examples below, and they won't be explained in great detail.

```
r2 := 1

r3 := r1 / r2
```

One thing to note about the store instruction is that in the event that the store operand is defined in the scope above the current scope like x is in the following example.

```
int main()
{
  int x = 4;
  int test()
  {
    return x;
  }
  return test();
}
```

In that scenario the store command in the test function will have an extra piece of information saying that its defined in the scope one level above, so the store command will look like the following.

```
DEFINED IN 1 r2 := x
```

This information is also included when a closure is called from a narrower scope, the TAC would be as follows.

```
CALL _1 FROM SCOPE 1
```

For Functions a label instruction denotes the start and a end label for the end. After the start label the new activation frame instruction which tells the compiler to allocate space for a new activation frame with a given number of arguments, locals and tempories. Before the end there is a return instruction which contains the register with the value to return. Below is an example function in TAC.

```
_1: 
 NEW FRAME 0 arg 0 loc 1 temp DEFINED IN 1 r2 := x RETURN r2
```

### FUNCTION END

There is one type of control sequence in the language, the if else, the way this is described in TAC is using a sequence of if instructions and labels denoting the various bodies if the if and else parts. An example in –C and the corresponding TAC are below.

```
if (1 > 4) {
  return 4;
else if (2 > 1) {
  return 3;
r1 := 1
r2 := 4
r3 := 1 > 4
IF NOT r3 GOTO 1
r4 := 4
RETURN 4
GOTO 2
LABEL 1: r5 := 2
r6 := 1
r7 := 2 > 1
IF NOT r7 GOTO 3
r8 := 3
RETURN 3
LABEL 3: LABEL 2:
```

Finally there is one loop type in the language, the while loop, this is translated into a goto, an if and a label at the top and bottom of the loop body. the while condition is placed after the body. n example in  $-\mathbf{C}$  and the corresponding TAC are below.

```
int x = 0;

while (x < 5)

{

x = x + 1;

}

r1 := 0

x := r1

GOTO 1

LABEL 2: r2 := x

r3 := 1

r4 := r2 + r3

x := r4

LABEL 1: r5 := x

r6 := 5
```

```
r7 := r5 < r6
IF r7 GOTO 2
```

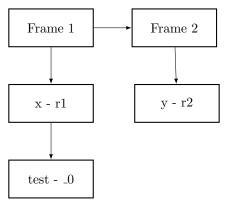
## 3.2 TAC Generation

All the TAC complilation is done in the tac\_compliler.c file. In order to generate the TAC from source code a tree walk is performed over the parse tree at each node depending on the type a set of TAC instructions are created and added to the current TAC block. If a new function is found a new TAC block is created before that part of the tree is parsed, also if a goto or label TAC instruction are created new blocks are created. When a leaf is reached a store instruction is created for the value at the leaf.

#### 3.2.1 Environment Structure

In order to keep track of the location of any local variables in the code and environment is created to store the association between token and register location. The environment is made up of frames each frame corresponds to a scope in the program and has a linked list of all locals in that scope. The frames also contain a linked list of the functions defined, these are a pair of token and label assigned to the function. For example the environment created while walking the following piece of code is shown below.

```
int main()
{
  int x = 4;
  int test()
  {
    int y = 5;
    return x * y;
  }
  return test();
}
```

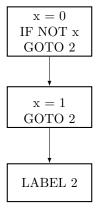


As you can see the environment holds the association between the tokens of the variables and functions with the TAC register location and the function label respectively.

## 3.2.2 TAC Blocking

The diffrent blocks of TAC code, between labels and jumps, are separated to allow easier optimisation and MIPS translation. As the AST is walked if a instruction which requires a jump (If, While, Function Call) is found a new block is created and set as the current block after the jump. Similarly if a label is created a new block is created and the label is assigned to that new block.

in order to compile the code in the same order as the TAC each block has a link to the block which was created from the code directly after it. A Simple example is given below.



This was done so that the MIPS compilation step can easily follow the sequence of TAC instructions. //TODO write about linking blocks if and when done

#### 3.2.3 Inner functions

In order to implement inner functions, functions defined inside another, in TAC the code for the function must be flattened so that there are no functions in functions in the TAC. To do this when a function definition is reached inside another the current TAC block is stored and another is created for the inner function, once the inner function's AST has finished being walked the previous block is restored as the current block and the AST tree walk continues. This gives the result of placing any inner functions after the function it was defined in.

#### 3.3 Next Use Info

## 3.4 TAC Optimisation

After the TAC generation phase has been completed the sequence of blocks is handed over to the optimisation phase. This is in the tac\_optimiser.c file. This applies constant folding, copy propagation, dead code elimination, common sub expression elimination and algebraic transformations algorithms to the TAC block repeatedly till now change can be made. Each TAC block is processed from bottom to top for each optimisation technique.

#### 3.4.1 Copy Propagation

Copy propagation looks for a store instruction, once on is found it checks the rest of the code below the store until it finds a write to the store destination. For every read of the destination before replaced the use is replaced with the stores operand. To demonstrate this copy propergation was applied to the same example as above.

#### 3.4.2 Constant Folding

The constant folding function looks for arithmetic operations and replaces them with the result where possible. This is done by looking for a operation where both operands are tokens with type constant. Below is an example using both constant folding and copy propergation.

```
r1 := 4
                                     r1 := 4
                  x := 4
                                     x := 4
                  r2 := 6
                                     r2 := 6
int x = 4;
                  y := 6
                                     y := 6
int y = 6;
                  r3 := 4
                                     r3 := 4
                  r4 := 6
                                     r4 := 6
return x + y;
                  r5 := 4 + 6
                                     r5 := 10
                                    RETURN 10
                  RETURN r5
```

#### 3.4.3 Dead Code Elimination

Dead code elimination works by analysing each instruction using and useing the next use info removes them if not needed. Firstly this is only done for registers user defined variables are live at the end of the block so an't removed. A instruction is removed if the next use is not live, its another write, or there isn't another next use. Using the same example as above and applying dead code elimination gives the following.

The function which completed the dead code elimination step does not recalculate the number of tempories in the code. So when the activation record is allocated it will be for the original number of registers, which can waste a lot of memory. This would be easy to recompute but I ran out of time.

## 3.4.4 Common Sub Expression Elimination

If two expression have the same operands and operation the later one can be replaced with a store of the destination of the first. These are found by looking for pairs of arithmatic operations, when one is found if the operation and operands are the same the second is replaced with a store. An exaple is given below usign this method in conjunction with copy propergation.

```
r1 := 4
                                     r1 := 4
                                     r2 := 6
                  r3 := r1 * r2
                                     r3 := 4 * 6
                  c := r3
                                     c := r3
int c = 4 * 6;
                  r4 := 4
                                     r4 := 4
int d = 4 * 6;
                  r5 := 6
                                     r5 := 6
                  r6 := r4 * r5
                                     r6 := r3
return c;
                  d := r6
                                     d := r3
                  r7 := c
                                     r7 := r3
                  RETURN r7
                                     RETURN r3
```

## 3.4.5 Algebraic Transformations

The final optimisation technique is to transform some algebraic expressions which will always give 1 or 0 to those values. In order to do this the optimiser looks for those specific expressions and simply replaces them with a store of either 1 or 0 depending on the expression. An example is given below using copy propagation aswell.

```
CALL _1
                                     CALL _1
                  r2 := result
                                     r2 := result
                  x := result
                                     x := result
int x = test();
                  r3 := 0
                                     r3 := 0
int a = 0 + x;
                  r4 := result
                                     r4 := result
                  r5 := 0 + result \quad r5 := result
return a;
                  a := r5
                                     a := result
                  r6 := r5
                                     r6 := result
                  RETURN r5
                                     RETURN result
```

## 4 Machine Code Generation

After the TAC cEnvironmenten generated and optimised the code is translated to MIPS assembler. This is done block by block in the order the TAC was generated. Before the user code is compiled a global MIPS block is added which allocates memory for global scope functions and sets up the environment used for variable lookup.

A decision was made to store all variables in memory and ignore the problem of register assignment, this makes the compiler simpler however reduces its performance. The files associated with this section of the compiler are compiler.c and MIPS.c.

#### 4.0.6 Functions

When a function is compiled the first thing that happens is the number of locals, temporaries and arguments are counted and a space big enough for all

these is allocated. This activation frame also contains space for the return address, previous frame and enclosing frame. These are structured as shown in the diagram below.

//TODO draw diagram

One this is created and the first 3 spaces filled the arguments are all loaded into the next spaces in the frame. Any arguments are loaded from the memory pointed by \$a0. The function code is then compiled. The final section of the code is to return to the calling code, any result is moved to \$v0 the previous frame is restored into the \$fp and the return address jumped to. Below is a simple function example in mips with annotations.

```
function1:
                                            (1)
                          move $t2 $a0
                                            (2)
                          li $a0 40
                                            (3)
                          li $v0 9
                                            (4)
                          syscall
                                            (6)
                          move $t0 $fp
                                            (5)
                          move $fp $v0
                                            (6)
                          sw $t0 \ 0($fp)
                                            (7)
                          sw $ra 4($fp)
                                            (8)
                             $a1
                                  8($fp)
                                            (9)
int times (int n, int d) lw
                             $t1 0($t2)
                                            (10)
                             \$t1
                                 12($fp)
                             $t1 4($t2)
  return n * d;
                          lw
                             $t1 16($fp)
                             $t1 12($fp)
                                            (11)
                          lw $t2 16($fp)
                          mult $t1 $t2
                          mflo $t0
                          sw $t0 20($fp)
                          lw $v0 20($fp)
                                            (12)
                          lw $t0 4($fp)
                                            (13)
                          lw fp 0(fp)
                                            (14)
                          jr $t0
                                            (15)
```

- 1. Function label
- 2. Move argument pointer into tempory register
- 3. set the number of bytes required to allocate
- 4. set the syscode for memory allocation
- 5. Move the old frame pointer into a temporary register
- 6. Save the new frame pointer
- 7. Put the previous frame pointer in the frame

- 8. Put the return adderess in the frame
- 9. The enclosing scope is passed in \$a1 so store this in the frame
- 10. for both arguments load them from the arg pointer and store in the frame
- 11. Do the function body
- 12. store the return value in \$v0
- 13. load the return address
- 14. restore the previous frame pointer
- 15. jump to the return address

#### 4.0.7 Environment

In order for the location of tokens and TAC registers to be found they are stored in an environment. The environment is made up of several frames each of which store information about a different scope in the program. Each frame holds the association between either TAC registers or tokens and there memory locations which are defined in that scope.

#### 4.0.8 Closures

In order to have closures we need to define the pair of program code and environment. The structure for a closure in MIPS is using a 8 byte object the first word is the address of the function code and the second if the address where the frame the closure was defined in is stored. When a closure is called the enclosing frame is placed in \$a1 and the program code is jumped to. Below is an example of the definition of a closure.

```
li $a0 8 Allocate 2 Words
li $v0 9
syscall
la $t1 function0 Load the address of the code
sw $t1 0($v0) Save the address in the first place
sw $fp 4($v0) Save the current frame pointer in the other
Then when the closure is called the following code is generated.
```

# 5 Testing

## 5.1 Compiler

In order to test both the TAC and MIPS compilation stages various –C programs were run though the compiler and the result they leave in the return register was checked with the expected value. In order to make this simpler a new exception handler was writtern for the spim interpreter which prints the value left in \$v0 after the user code is run. The compilation is done by using "./mycc -c FileName" and then running it in spim using "spim -exception\_file testExceptionHandler.s -file Output/test.asm". Given this here are a few example test cases there TAC and MIPS code and result value.

#### 5.1.1 Math Test - test\_math.c

```
int main()
    return 8 * 2 - 2;
DEFINE CLOSURE _0
_{-}0:
NEW FRAME 0 arg 0 loc 5 temp
RETURN 14
FUNCTION END
main:
li $a0 16
li $v0 9
svscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
svscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 32
```

```
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 14
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 14
5.1.2 Simple Test - test_simple.c
int main()
    int y;
    int x = 4;
    y = 4;
    return x + y;
}
DEFINE CLOSURE _{-}0
_{-}0:
NEW FRAME 0 arg 3 loc 4 temp
RETURN 8
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
```

```
function0:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move \ \$fp \ \$v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 8
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 8
5.1.3 If Else Test - test_if_else.c
int main()
    if (1 > 4) {
     return 4;
    else if (2 > 1) {
      return 3;
    }
    return 8;
}
DEFINE CLOSURE _{-}0
NEW FRAME 0 arg 0 loc 9 temp
r3 := 0
IF NOT r3 GOTO 1
RETURN 4
GOTO 2
LABEL 1: r7 := 1
IF NOT r7 GOTO 3
RETURN 3
LABEL 3: LABEL 2: RETURN 8
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
```

```
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
move $t2 $a0
li $a0 48
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 0
sw $t0 12($fp)
lw $t2 12($fp)
beq $t2 $zero label1
li $v0 4
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
j label2
label1:
li $t0 1
sw $t0 16($fp)
lw $t2 16($fp)
beq $t2 $zero label3
1i \$v0 3
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
label3:
label2:
li $v0 8
lw $t0 4($fp)
lw $fp 0($fp)
```

```
jr $t0
RESULT - 3
5.1.4 While Test - test_while.c
int main()
{
    int x = 0;
    while (x < 5)
     x = x + 1;
    return x;
}
DEFINE CLOSURE _{-}0
NEW FRAME 0 arg 2 loc 8 temp
x := 0
GOTO 1
LABEL 2: r4 := x + 1
x := r4
IF r7 GOTO 2
RETURN x
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function0:
```

```
move $t2 $a0
li $a0 52
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 0
sw $t0 12($fp)
j label1
label2:
lw $t1 12($fp)
li $t2 1
add $t0 $t1 $t2
sw $t0 16($fp)
lw $t0 16($fp)
sw $t0 12($fp)
label1:
lw $t1 12($fp)
li $t2 5
sltu $t0 $t1 $t2
sw $t0 20($fp)
lw $t2 20($fp)
bne $t2 $zero label2
lw $v0 12($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 5
5.1.5 Function Test - test_function.c
int test()
  return 4;
int main()
  return test();
DEFINE CLOSURE _1
DEFINE CLOSURE _0
```

```
_{-}1:
NEW FRAME 0 arg 0 loc 1 temp
RETURN 4
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 2 temp
ALLOCATE PARAMS 0
CALL _{-}1 FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 20
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function 1:
move $t2 $a0
li $a0 16
li $v0 9
syscall
move $t0 $fp
move fp v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $v0 4
```

```
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 20
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $a0 0
li $v0 9
syscall
move \$a0 \$v0
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move \$v0 \$v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 4
5.1.6 Function With Arguments Test - test_function_args.c
int times (int n, int d)
  return n * d;
int main()
  return times (3, 2);
}
DEFINE CLOSURE _1
DEFINE CLOSURE _0
_1:
NEW FRAME 2 arg 2 loc 3 temp
LOAD PARAM n
```

```
LOAD PARAM d
r3 \ := \ n \ * \ d
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 4 temp
r4 := 3
r5 := 2
ALLOCATE PARAMS 2
SAVE PARAM r4
SAVE PARAM r5
CALL _{-1} FROM SCOPE 1
RETURN result
FUNCTION END
main:
li $a0 20
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
```

```
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
lw $t2 16($fp)
mult $t1 $t2
mflo $t0
sw $t0 20($fp)
lw $v0 20($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 28
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 3
sw $t0 12($fp)
li $t0 2
sw $t0 16($fp)
li $a0 8
li $v0 9
syscall
move \$a0 \$v0
lw $t0 12($fp)
sw $t0 0($v0)
addi v0 v0 4
lw $t0 16($fp)
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
```

```
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 6
5.1.7 Inner Function Test - test_innerfunc.c
int times2(int n) {
  int times (int n, int m) {
    return n * m;
  return times (n, 2);
int main()
  return times2(3);
DEFINE CLOSURE _1
NEW FRAME 1 arg 1 loc 4 temp
LOAD PARAM n
DEFINE CLOSURE _{-}2
r4 := n
r5 := 2
ALLOCATE PARAMS 2
SAVE PARAM r4
SAVE PARAM r5
CALL _2 FROM SCOPE _0
RETURN result
FUNCTION END
DEFINE CLOSURE _0
_{-2} :
NEW FRAME 2 arg 2 loc 3 temp
LOAD PARAM n
LOAD PARAM m
r3 := n * m
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 3 temp
r7 := 3
ALLOCATE PARAMS 1
SAVE PARAM r7
```

# CALL \_1 FROM SCOPE 1 RETURN result FUNCTION END

```
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 \ 0($v0)
sw $fp 4($v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 16($fp)
lw $t0 12($fp)
sw $t0 20($fp)
li $t0 2
sw $t0 24($fp)
li $a0 8
li $v0 9
```

```
syscall
move \$a0 \$v0
lw $t0 20($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 28($fp)
function2:
move $t2 $a0
li $a0 40
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
lw $t2 16($fp)
mult $t1 $t2
mflo $t0
sw $t0 20($fp)
lw $v0 20($fp)
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
```

```
function0:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 3
sw $t0 12($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 12($fp)
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 6
5.1.8 Twice Test - test_twice.c
function twice (function f) {
  int g(int x) \{ return f(f(x)); \}
  return g;
}
void main()
  int addten(int n) {return n + 10;}
  return twice (addten)(2);
DEFINE CLOSURE _1
_1:
```

```
NEW FRAME 1 arg 1 loc 1 temp
LOAD PARAM f
DEFINE CLOSURE _2
RETURN 2
FUNCTION END
DEFINE CLOSURE _0
_{-}2:
NEW FRAME 1 arg 1 loc 5 temp
LOAD PARAM x
r1 := x
ALLOCATE PARAMS 1
SAVE PARAM r1
CALL _{-}0 FROM SCOPE 1
r2 := result
ALLOCATE PARAMS 1
SAVE PARAM r2
CALL _0 FROM SCOPE 1
RETURN result
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 6 temp
DEFINE CLOSURE _3
r8 \ := \ 3
ALLOCATE PARAMS 1
SAVE PARAM r8
CALL _1 FROM SCOPE 1
r9 := result
r10 := 2
ALLOCATE PARAMS 1
SAVE PARAM r10
CALL r9 FROM SCOPE 0
RETURN result
FUNCTION END
_3:
NEW FRAME 1 arg 1 loc 3 temp
LOAD\ PARAM\ n
r7 := n + 10
RETURN r7
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
```

```
li $a0 8
li $v0 9
svscall
la $t1 function1
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 0($v0)
sw fp 4(v0)
sw $v0 20($fp)
function2:
move $t2 $a0
li $a0 40
li $v0 9
syscall
```

```
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t0 12($fp)
sw $t0 16($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 16($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 20($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 20($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
function0:
move $t2 $a0
li $a0 36
li $v0 9
syscall
```

```
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $a0 8
li $v0 9
syscall
la $t1 function3
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
lw $t0 12($fp)
sw $t0 16($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 16($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 20($fp)
li $t0 2
sw $t0 24($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 20($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
```

```
function3:
move $t2 $a0
li $a0 32
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 \ 0($t2)
sw $t1 12($fp)
lw $t1 12($fp)
li $t2 10
add $t0 $t1 $t2
sw $t0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
RESULT - 22
{\bf 5.1.9}\quad {\bf Cplus}\ {\bf Test-cplus.c}
function cplus(int a) {
  int cplusa(int b) { return a+b; }
  return cplusa;
int main()
  return cplus (5)(2);
DEFINE CLOSURE _1
_{-}1:
NEW FRAME 1 arg 1 loc 1 temp
LOAD PARAM a
DEFINE CLOSURE _2
RETURN 2
FUNCTION END
DEFINE CLOSURE _{-}0
NEW FRAME 1 arg 1 loc 3 temp
LOAD PARAM b
DEFINED IN 1 r1 := a
```

```
r3 := r1 + b
RETURN r3
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 6 temp
r5 := 5
ALLOCATE PARAMS 1
SAVE PARAM r5
CALL _{-}1 FROM SCOPE 1
r6 := result
r7 := 2
ALLOCATE PARAMS 1
SAVE PARAM r7
CALL r6 FROM SCOPE 0
RETURN result
FUNCTION END
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
```

```
li $a0 8
li $v0 9
syscall
la \ \$t1 \ function 2
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 16($fp)
lw $v0 16($fp)
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw $fp 4($v0)
sw $v0 20($fp)
function2:
move $t2 $a0
li $a0 32
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
sw $t0 16($fp)
lw $t1 16($fp)
lw $t2 12($fp)
add $t0 $t1 $t2
sw $t0 20($fp)
lw $v0 20($fp)
lw $t0 4($fp)
lw \$fp 0(\$fp)
jr $t0
function0:
move $t2 $a0
li $a0 36
li $v0 9
```

```
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 5
sw $t0 12($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 12($fp)
sw $t0 \ 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $t0 $v0
sw $t0 16($fp)
li $t0 2
sw $t0 20($fp)
li $a0 4
li $v0 9
syscall
move $a0 $v0
lw $t0 20($fp)
sw $t0 0($v0)
addi v0 v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw fp 0(fp)
jr $t0
RESULT - 7
5.1.10 Factorial Test - test_fact.c
int fact(int n) {
    int inner_fact(int n, int a) {
```

```
if (n==0) return a;
        return inner_fact (n-1,a*n);
    return inner_fact(n,1);
}
int main()
  return fact (4);
DEFINE CLOSURE _1
NEW FRAME 1 arg 1 loc 4 temp
LOAD PARAM n
DEFINE CLOSURE _{-}2
r12 := n
r13 := 1
ALLOCATE PARAMS 2
SAVE PARAM r12
SAVE PARAM r13
CALL _{-2} FROM SCOPE _{0}
RETURN result
FUNCTION END
DEFINE CLOSURE _{-}0
_{-}2:
NEW FRAME 2 arg 2 loc 12 temp
LOAD PARAM n
LOAD PARAM a
r3 := n == 0
IF NOT r3 GOTO 1
RETURN a
LABEL 1: r7 := n - 1
r10 := a * n
ALLOCATE PARAMS 2
SAVE PARAM r7
SAVE PARAM r10
CALL _2 FROM SCOPE 1
RETURN result
FUNCTION END
_{-}0:
NEW FRAME 0 arg 0 loc 3 temp
r15 := 4
ALLOCATE PARAMS 1
SAVE PARAM r15
```

# CALL \_1 FROM SCOPE 1 RETURN result FUNCTION END

```
main:
li $a0 16
li $v0 9
syscall
move $fp $v0
sw $ra 4($fp)
li $a0 8
li $v0 9
syscall
la $t1 function1
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 12($fp)
move $a1 $fp
jal function0
lw $t0 4($fp)
jr $t0
function1:
move $t2 $a0
li $a0 36
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
li $a0 8
li $v0 9
syscall
la $t1 function2
sw $t1 0($v0)
sw $fp 4($v0)
sw $v0 16($fp)
lw $t0 12($fp)
sw $t0 20($fp)
li $t0 1
sw $t0 24($fp)
li $a0 8
li $v0 9
```

```
syscall
move \$a0 \$v0
lw $t0 20($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 16($fp)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
li $a0 8
li $v0 9
syscall
la $t1 function0
sw $t1 \ 0($v0)
sw fp 4(v0)
sw $v0 28($fp)
function2:
move $t2 $a0
li $a0 76
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
lw $t1 0($t2)
sw $t1 12($fp)
lw $t1 4($t2)
sw $t1 16($fp)
lw $t1 12($fp)
li $t2 0
sub $t0 $t1 $t2
sltu $t0 $zero $t0
xori $t0 $t0 1
sw $t0 20($fp)
lw $t2 20($fp)
beq $t2 $zero label1
lw $v0 16($fp)
```

```
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
label1:
lw $t1 12($fp)
li $t2 1
sub \$t0 \$t1 \$t2
sw $t0 24($fp)
lw $t1 16($fp)
lw $t2 12($fp)
mult $t1 $t2
mflo $t0
sw $t0 28($fp)
li $a0 8
li $v0 9
syscall
move \$a0 \$v0
lw $t0 24($fp)
sw $t0 0($v0)
addi $v0 $v0 4
lw $t0 28($fp)
sw $t0 0($v0)
addi v0 v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 16($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move $v0 $v0
lw $t0 4($fp)
lw $fp 0($fp)
jr $t0
function0:
move $t2 $a0
li $a0 24
li $v0 9
syscall
move $t0 $fp
move $fp $v0
sw $t0 \ 0($fp)
sw $ra 4($fp)
sw $a1 8($fp)
li $t0 4
sw $t0 12($fp)
li $a0 4
```

```
li $v0 9
syscall
move \$a0 \$v0
lw $t0 12($fp)
sw $t0 0($v0)
addi $v0 $v0 4
move $t7 $fp
lw $t7 8($t7)
lw $t0 \ 12($t7)
lw $t1 0($t0)
lw $a1 4($t0)
jal $t1
move \$v0 \$v0
lw $t0 4($fp)
lw \$fp 0(\$fp)
jr $t0
```

# RESULT - 24

# 6 Examples