

1.3 BAGS, QUEUES, AND STACKS



<http://algs4.cs.princeton.edu>

- ▶ *stacks*
- ▶ *resizing arrays*
- ▶ *queues*
- ▶ *generics*
- ▶ *iterators*
- ▶ *applications*



Do some review before labs start

Extra credit – 2 points to lab grade

- Using the stack class from Java, write a program that will push 20 random integers (between 1 and 100) onto the stack
- Print the stack
- Pop the top integer and print that integer
- Print the stack again
- Print the result of checking if 50 is in the stack
- Print the result of checking if the stack is empty
- After popping all the numbers off of the stack, print the average of the numbers
 - Will not include the top number because it was already popped
- Run it a few times to make sure you are getting a different average each time
- DUE: 9/6 at 10am
- Competition – used 14 lines of executable code



Iterable Collections

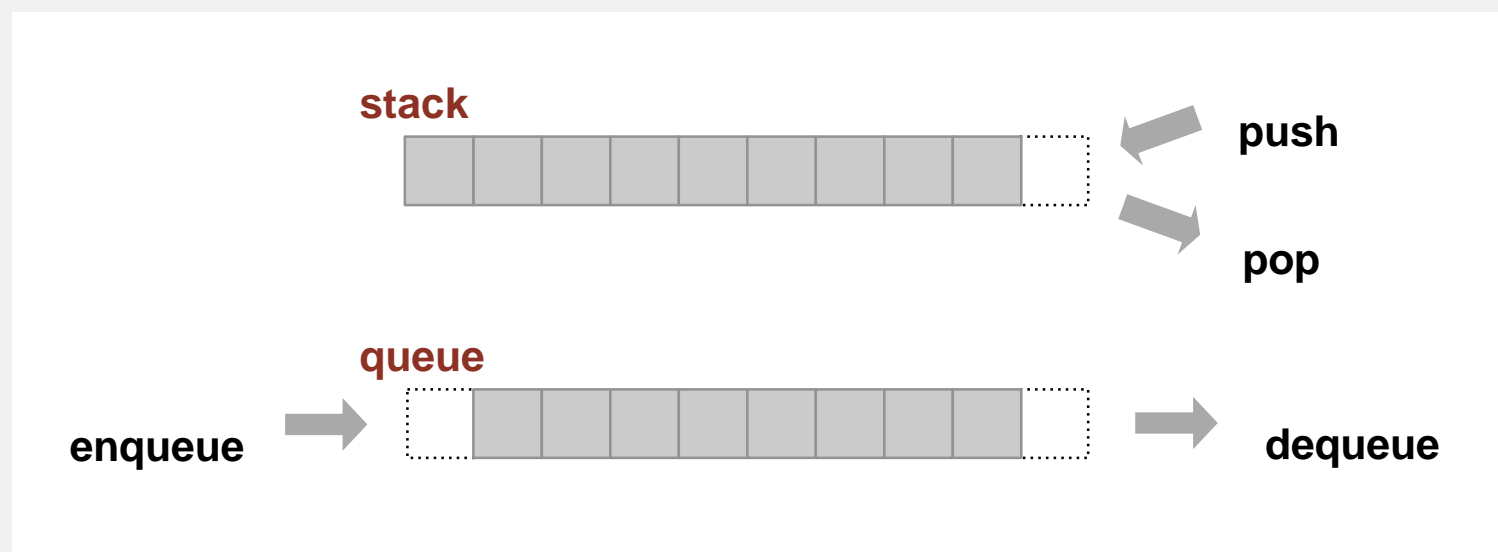
- class Bag implements iterable<Item>
 - The internal elements of the class that implements an iterable allows moving through the elements (using a for-each loop)

```
public static void main(String[] args) {  
    List list = new ArrayList();  
    list.add("one");  
    list.add("two");  
    list.add("three");  
  
    for(Object o : list){  
        System.out.println(o.toString());  
    }  
}
```

Stacks and queues

Fundamental data types.

- Value: collection of objects.
- Operations: **insert**, **remove**, **iterate**, test if empty.
- Intent is clear when we insert.
- Which item do we remove?



Stack.
Queue.

**HOW DOES EACH DATA STRUCTURE STORE DATA?
WHAT IS THAT CALLED?**

Client, implementation, interface

Separate interface and implementation.

Ex: stack, queue, bag, priority queue, symbol table, union-find,

Benefits.

- Client can't know details of implementation \Rightarrow client has many implementation from which to choose.
- Implementation can't know details of client needs \Rightarrow many clients can re-use the same implementation.
- **Design:** creates modular, reusable libraries.
- **Performance:** use optimized implementation where it matters.

Client: program using operations defined in interface.

Implementation: actual code implementing operations.

Interface: description of data type, basic operations.

1.3 BAGS, QUEUES, AND STACKS

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Stack API

Warmup API. Stack of strings data type.

```
public class StackOfStrings
```

```
    StackOfStrings()
```

create an empty stack

```
    void push(String item)
```

insert a new string onto stack

```
    String pop()
```

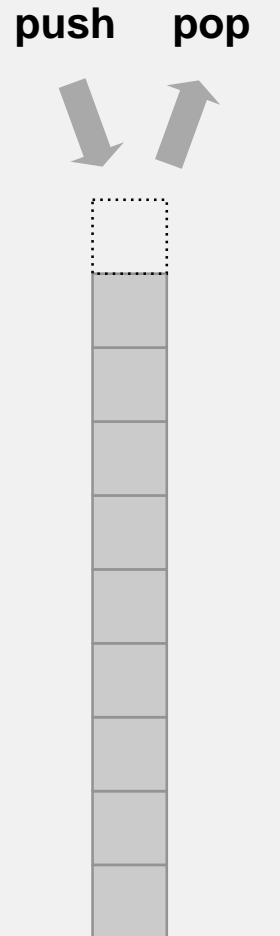
*remove and return the string
most recently added*

```
    boolean isEmpty()
```

is the stack empty?

```
    int size()
```

number of strings on the stack



StackOfStrings.java

LOOK AT THE CODE AND TELL ME HOW IT IS IMPLEMENTED

Sample client

Warmup client. Reverse sequence of strings from standard input.

- Read string and push onto stack.
- Pop string and print.

```
% more tinyTale.txt
```

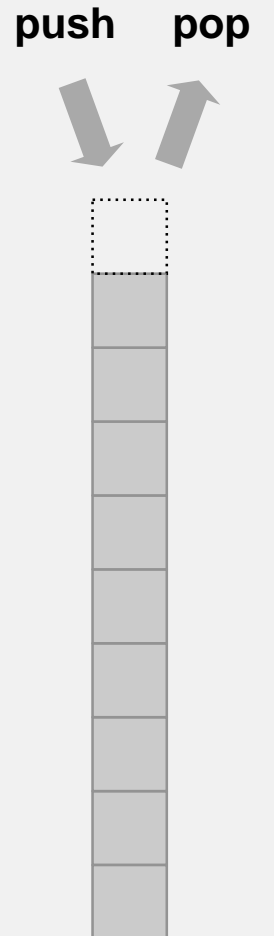
```
it was the best of times ...
```

```
% java ReverseStrings < tinyTale.txt
```

```
... times of best the was it
```

```
[ignoring newlines]
```

ReverseStrings.java
StackOfStrings.java



Stack test client

Read strings from standard input.

- If string equals "-", pop string from stack and print.
- Otherwise, push string onto stack.

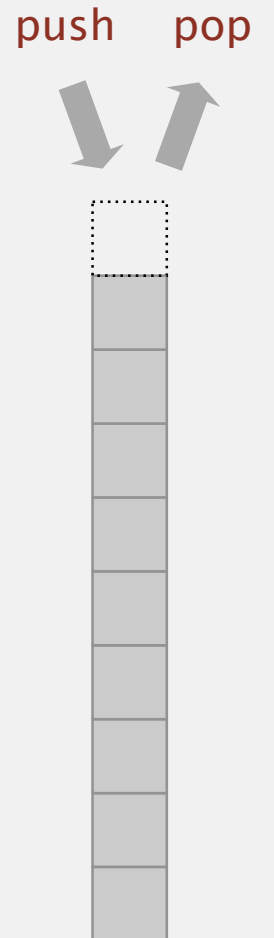
```
% more tobe.txt
```

```
to be or not to - be - -
```

```
% java StackOfStringsApps < tobe.txt
```

```
to be not
```

```
Left on stack: or be to
```

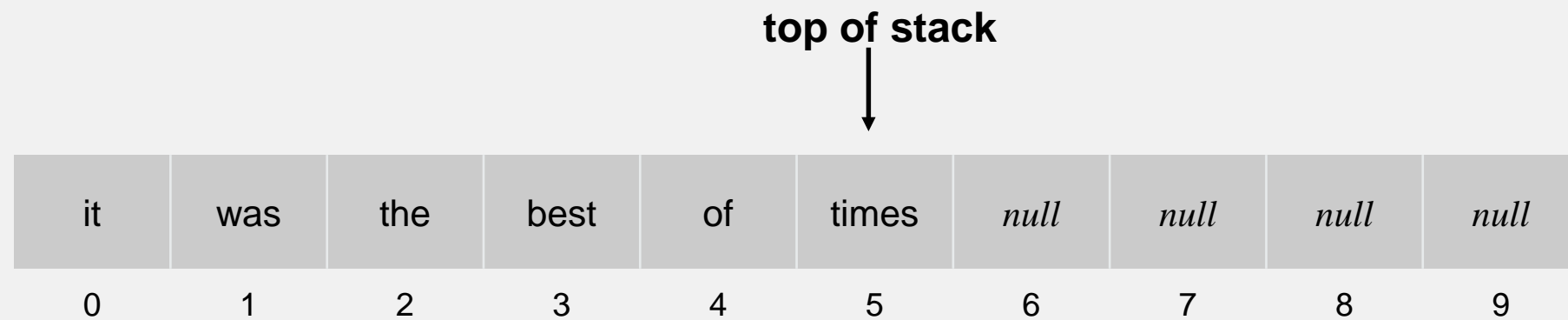


```
StackOfStringsApp.java  
StackOfStrings.java
```

How to implement a fixed-capacity stack with an array?

A. Can't be done efficiently with an array.

B.

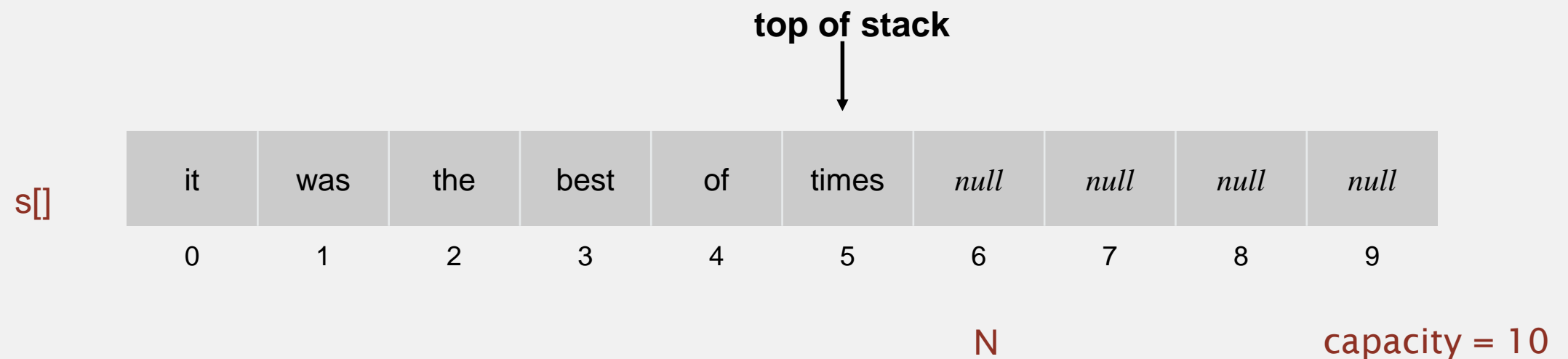


C.



Fixed-capacity stack: array implementation

- Use array $s[]$ to store N items on stack.
- $\text{push}()$: add new item at $s[N]$.
- $\text{pop}()$: remove item from $s[N-1]$.



Defect. Stack overflows when N exceeds capacity. [stay tuned]

Stack considerations

Overflow and underflow.

- Underflow: throw exception if pop from an empty stack.
- Overflow: use resizing array for array implementation. [stay tuned]

Null items. We allow null items to be inserted.

Loitering. Holding a reference to an object when it is no longer needed.

```
public String pop()
{ return s[--N]; }
```

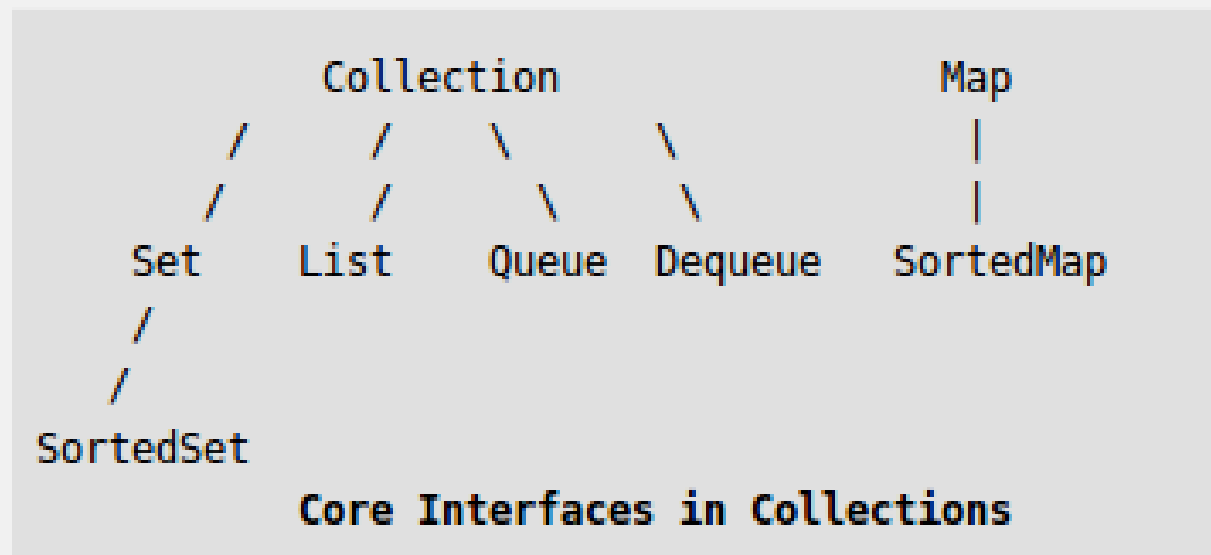
loitering

```
public String pop()
{
    String item = s[--N];
    s[N] = null;
    return item;
}
```

**this version avoids "loitering":
garbage collector can reclaim memory for an
object only if no outstanding references**

Linked List

Linked List implements the list interface



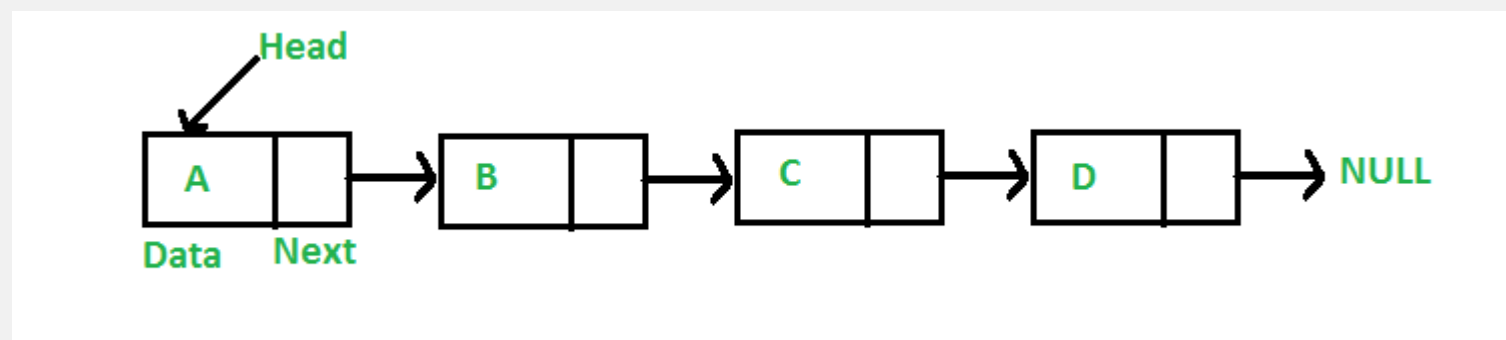
List interface calls for:

void add(int index, Object O)

boolean addAll(int index, Collection c)

Object remove(int index): Object get(int index)

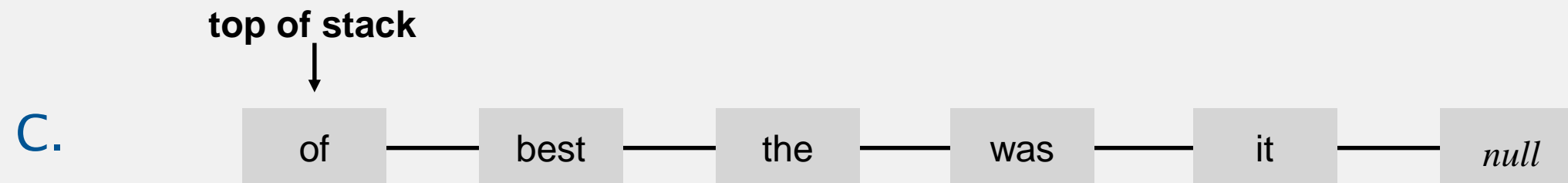
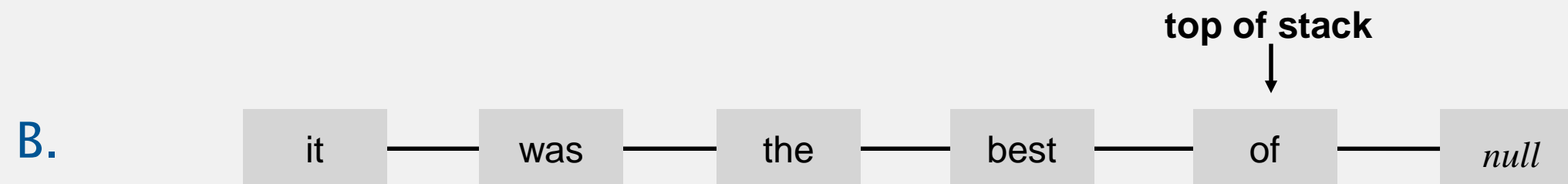
Object set(int index, Object new)



Taken from [geeksforgeeks.org](https://www.geeksforgeeks.org)

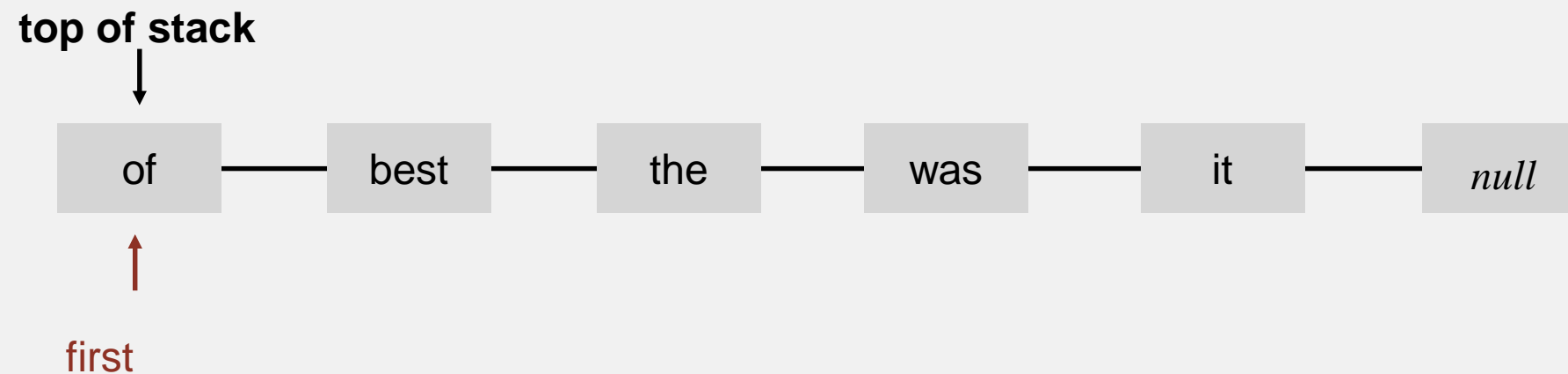
How to implement a stack with a linked list?

A. Can't be done efficiently with a singly-linked list.



Stack: linked-list implementation

- Maintain pointer *first* to first node in a singly-linked list.
- Push new item before *first*.
- Pop item from *first*.



Stack pop: linked-list implementation

inner class

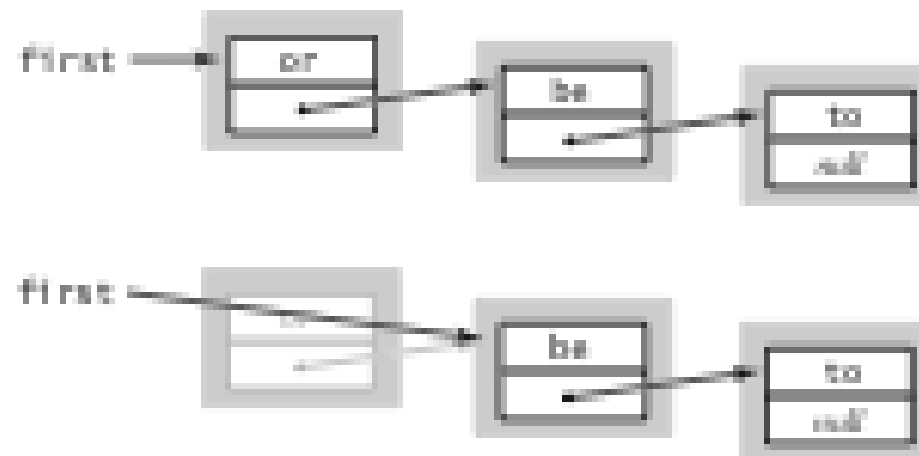
```
private class Node
{
    String item;
    Node next;
}
```

save item to return

```
String item = first.item;
```

delete first node

```
first = first.next;
```



return saved item

```
return item;
```

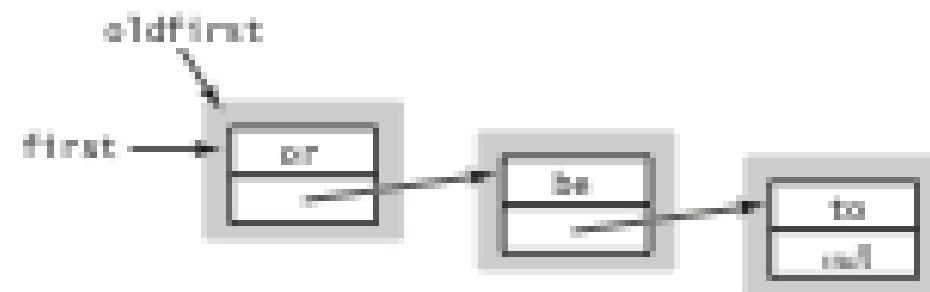

Stack push: linked-list implementation

inner class

```
private class Node
{
    String item;
    Node next;
}
```

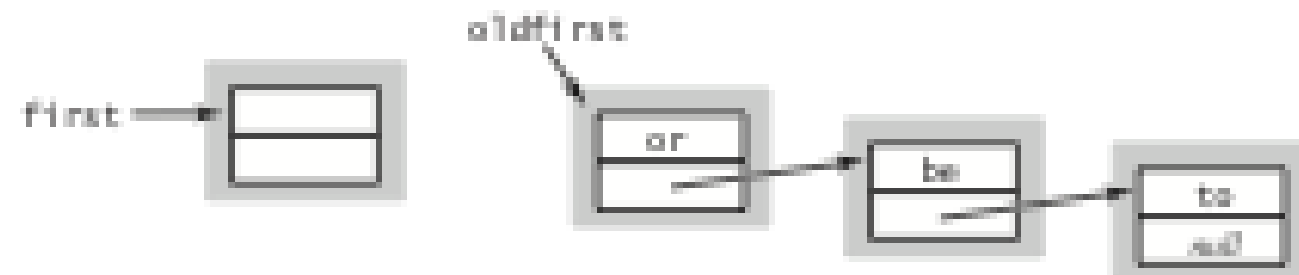
save a link to the list

```
Node oldfirst = first;
```



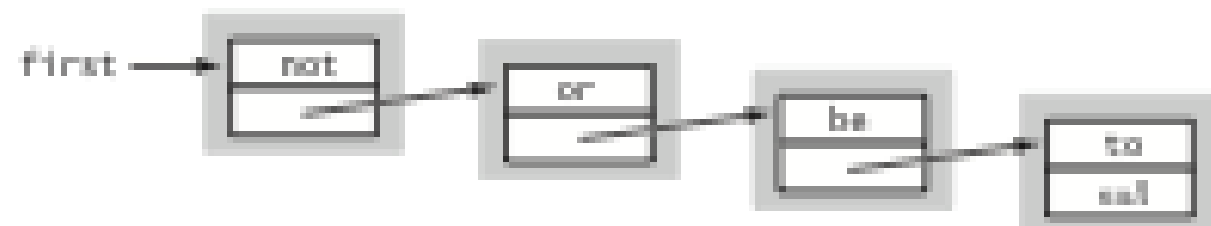
create a new node for the beginning

```
first = new Node();
```



set the instance variables in the new node

```
first.item = "not";
first.next = oldfirst;
```



Stack: linked-list implementation in Java

ListStack.java
StackOfStringsApp.java

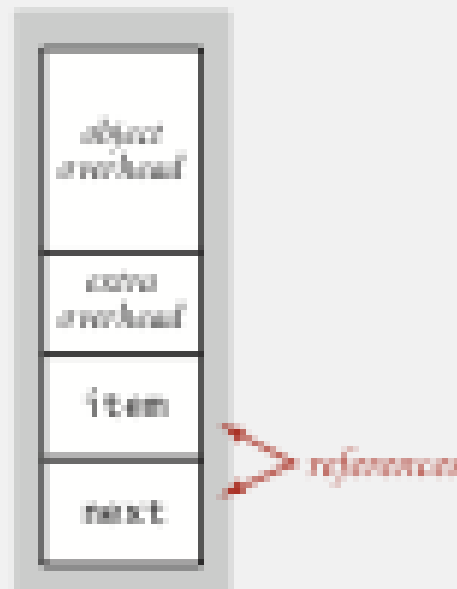
Stack: linked-list implementation performance

Proposition. Every operation takes constant time in the worst case.

Proposition. A stack with N items uses $\sim 40 N$ bytes.

inner class

```
private class Node
{
    String item;
    Node next;
}
```



16 bytes (object overhead)

8 bytes (inner class extra overhead)

8 bytes (reference to String)

8 bytes (reference to Node)

40 bytes per stack node

Remark. This accounts for the memory for the stack
(but not the memory for strings themselves, which the client owns).

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Stack: resizing-array implementation

Problem. Requiring client to provide capacity does not implement API!

Q. How to grow and shrink array?

First try.

- `push()`: increase size of array `s[]` by 1.
- `pop()`: decrease size of array `s[]` by 1.

Too expensive.

- Need to copy all items to a new array, for each operation.
 - Array accesses to insert first N items = $N + (2 + 4 + \dots + 2(N-1)) \sim N^2$.
- infeasible for large N ↓
- ↑ ↑
- 1 array access 2(k-1) array accesses to expand to size k
per push (ignoring cost to create new array)

Challenge. Ensure that array resizing happens infrequently.

Stack: resizing-array implementation

Q. How to grow array?

A. If array is full, create a new array of **twice** the size, and copy items.

"repeated doubling"



Array accesses to insert first $N = 2^i$ items. $N + (2 + 4 + 8 + \dots + N) \sim 3N$.

↑
1 array access
per push

↑
k array accesses to double to size k
(ignoring cost to create new array)

LAB QUESTION

Stack: resizing-array implementation

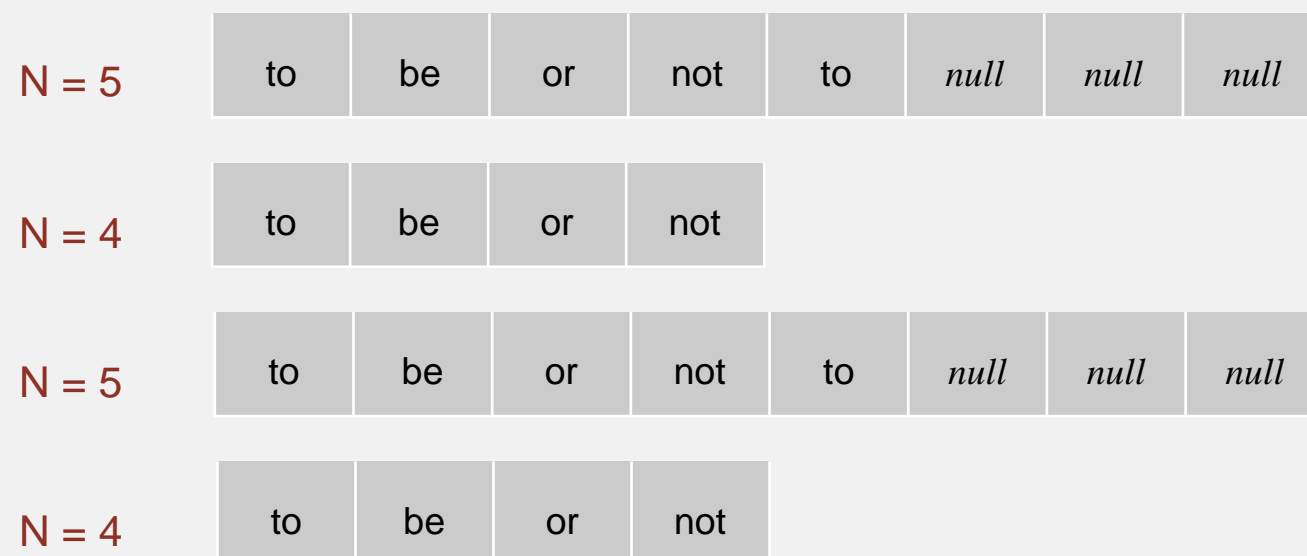
Q. How to shrink array?

First try.

- `push()`: double size of array `s[]` when array is full.
- `pop()`: halve size of array `s[]` when array is **one-half full**.

Too expensive in worst case.

- Consider push-pop-push-pop-... sequence when array is full.
- Each operation takes time proportional to N .



Stack: resizing-array implementation

Q. How to shrink array?

Efficient solution.

- push(): double size of array `s[]` when array is full.
- pop(): halve size of array `s[]` when array is **one-quarter full**.

```
public String pop() {  
    String item = s[--N];  
    s[N] = null;  
    if (N > 0 && N == s.length/4) resize(s.length/2);  
    return item;  
}
```

Invariant. Array is between 25% and 100% full.

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Queue API

```
public class Queue
```

```
    Queue()
```

create an empty queue

```
    void enqueue(Item item)
```

insert a new item onto queue

```
    Item dequeue()
```

*remove and return the string
least recently added*

```
    boolean isEmpty()
```

is the queue empty?

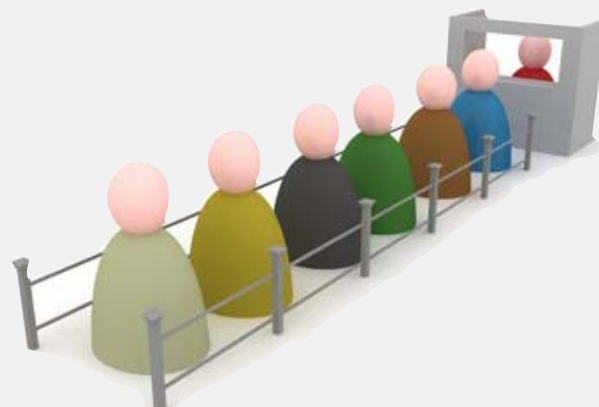
```
    int size()
```

number of items on the queue

enqueue

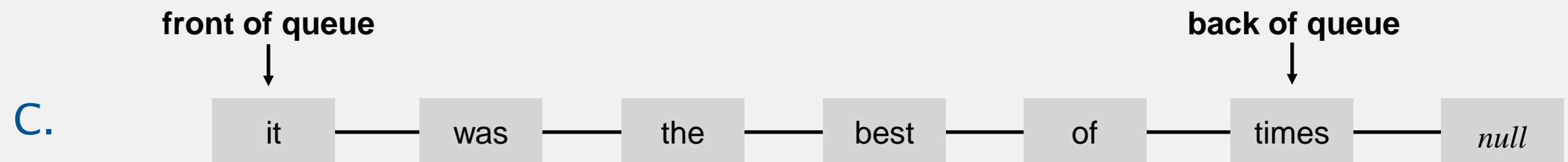
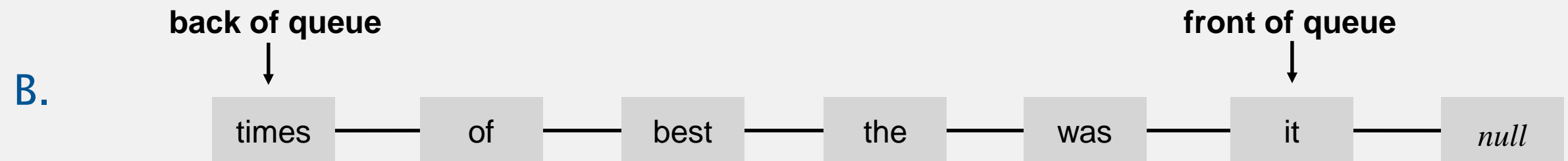


dequeue



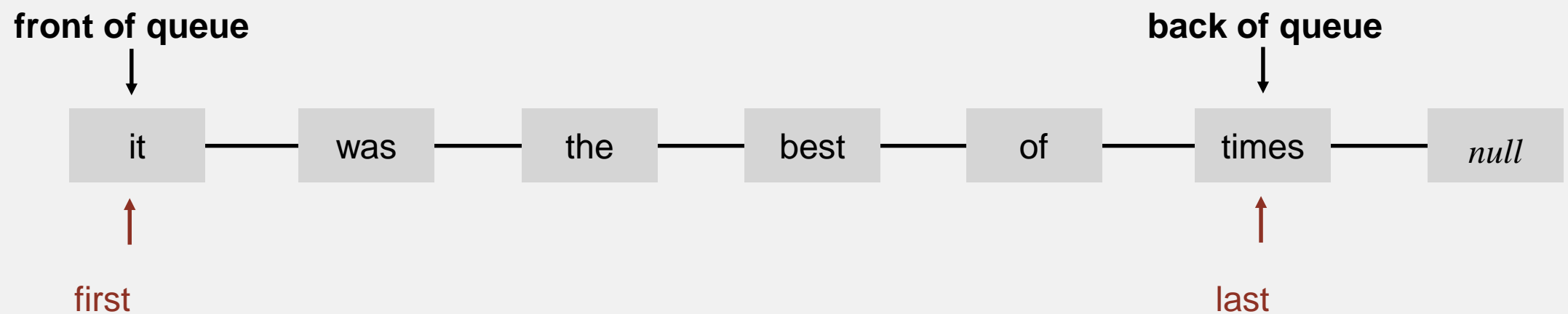
How to implement a queue with a linked list?

A. Can't be done efficiently with a singly-linked list.



Queue: linked-list implementation

- Maintain one pointer *first* to first node in a singly-linked list.
- Maintain another pointer *last* to last node.
- Dequeue from *first*.
- Enqueue after *last*.



Queue dequeue: linked-list implementation

inner class

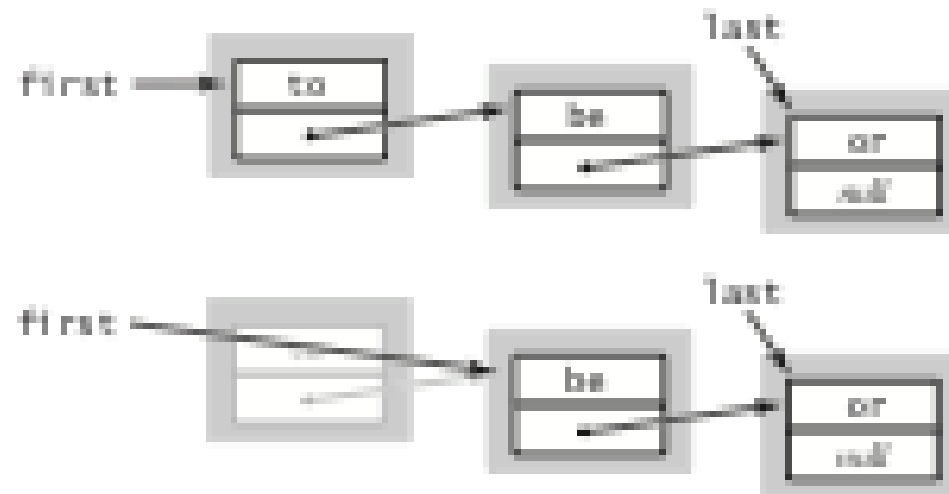
```
private class Node
{
    String item;
    Node next;
}
```

~~save item to return~~

```
String item = first.item;
```

~~delete first node~~

```
first = first.next;
```



~~return saved item~~

```
return item;
```

Remark. Identical code to linked-list stack pop().

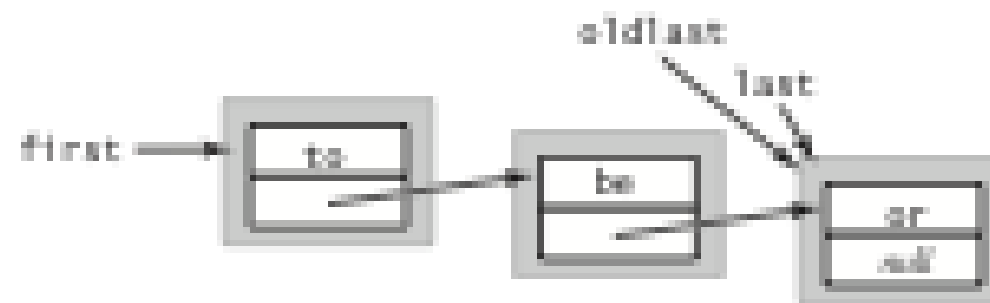
Queue enqueue: linked-list implementation

inner class

```
private class Node
{
    String item;
    Node next;
}
```

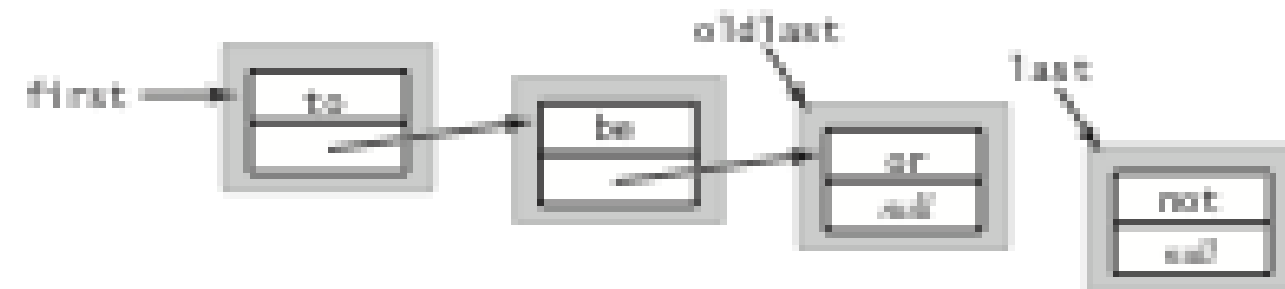
save a link to the last node

```
Node oldlast = last;
```



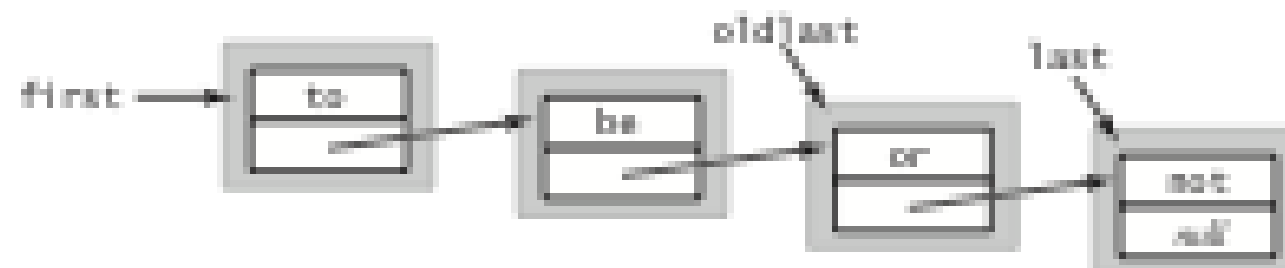
create a new node for the end

```
last = new Node();
last.item = "not";
```



link the new node to the end of the list

```
oldlast.next = last;
```



How to implement a fixed-capacity queue with an array?

A. Can't be done efficiently with an array.

