

Resizing Array Computations

Stack: resizing-array implementation

- Q. How to grow array?
- A. If array is full, create a new array of **twice** the size, and copy items.

↙ "repeated doubling"

Array accesses to insert first $N = 2^i$ items. $N + (2 + 4 + 8 + \dots + N) \sim 3N$



1 array access
per push



k array accesses to double to size k

(ignoring cost to create new array)

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- Q. How to grow array?
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- Array accesses to insert first $N = 2^i$ items. $N + (2 + 4 + 8 + \dots + N) = 3N - 2$

\uparrow
 1 array access
per push

\uparrow
 k array accesses to double to size k
(ignoring cost to create new array)

- Array accesses to insert first $N = 2^i$ items. $N + (4 + 8 + 16 + \dots + 2N) = 5N - 4$

\uparrow
 1 array access
per push

\uparrow
 k array accesses to double to size k
(including cost to create new array)

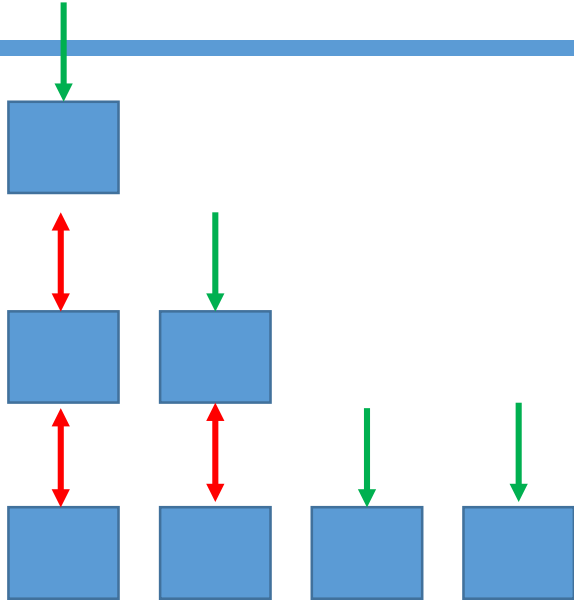
For these computations, N must be a power of 2



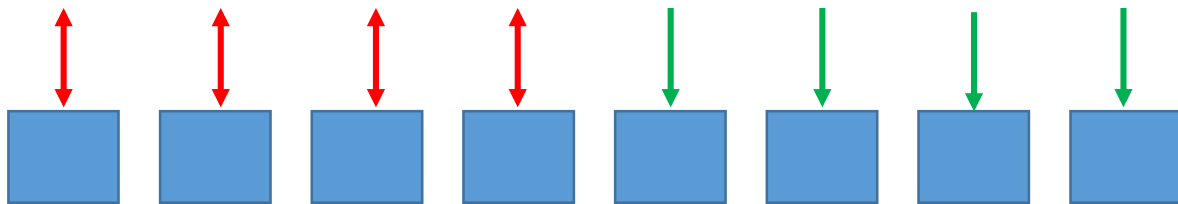
Assumptions

- What to count
 - In Resize()
 - For cost including creation of array ($5N+4$) - when creating the new array of size – $2 * \text{current length}$
 - Add capacity to accesses
 - When moving an item from the old (small) array to the new (larger) array
 - Add two to accesses (one for the read from old and one for write to new)
 - In push()
 - Add one for each item pushed
- What not to count
 - The first creation of the array
 - Equation starts with empty array

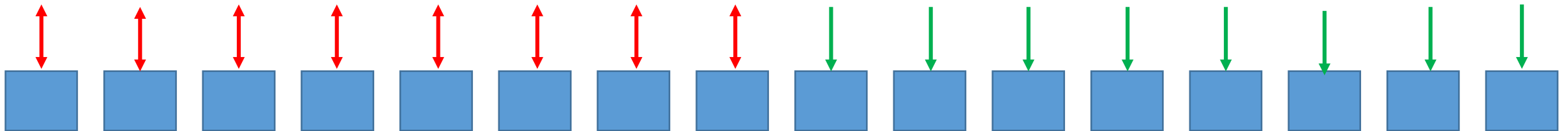
$$N + (2 + 4 + 8 + \dots + N) = 3N - 2: N = 16, 3N - 2 = 46$$



16 pushes (inserts)
 reads/writes to move from old array to new array
 $2+4+8+16=30$
 Total = 46



From code: accesses without initialization is 46



$$N + (4 + 8 + 16 + \dots + 2N) = 5N - 4: N = 16, 5N - 4 = 76$$

