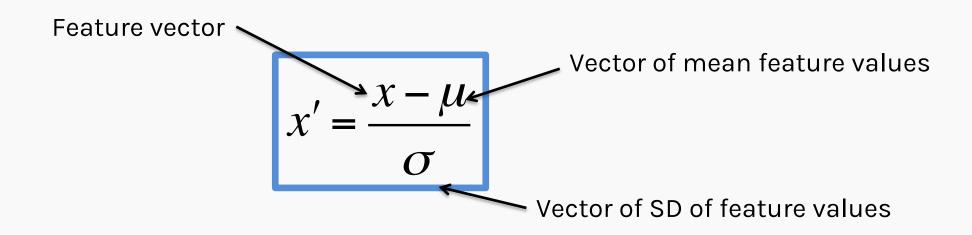
Neural Network Regularization Batch Norm

Pavlos Protopapas



Feature Normalization

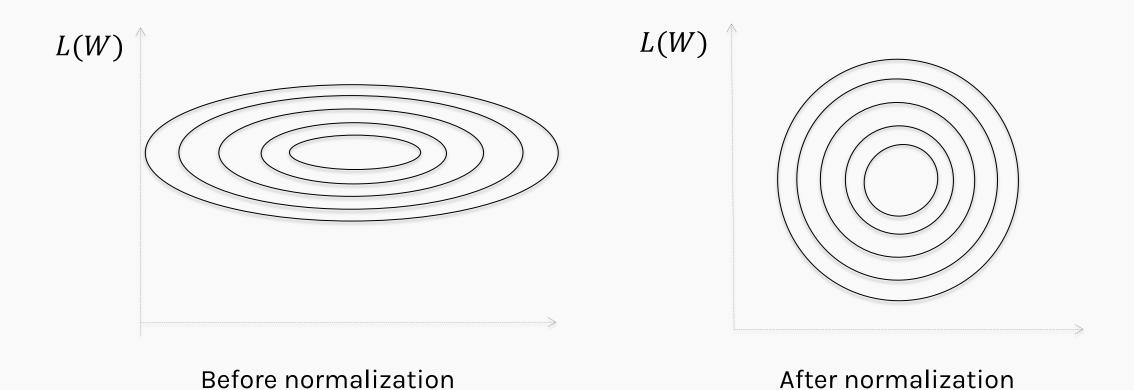
Good practice to normalize features before applying learning algorithm:



Features in same scale: mean 0 and variance 1

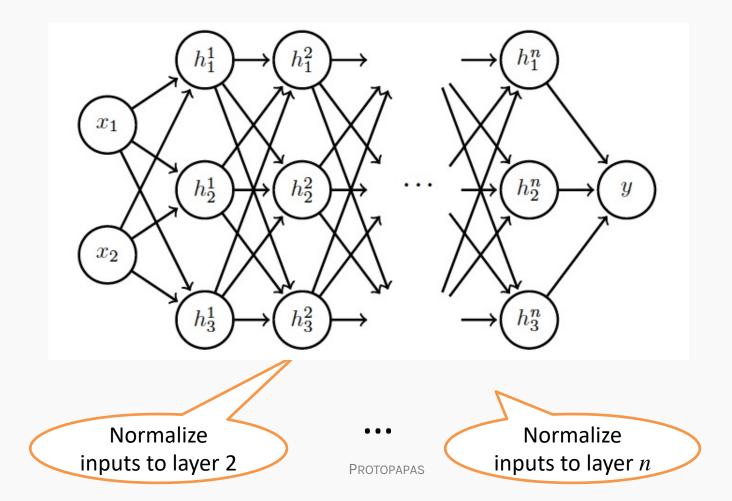
Feature Normalization

Speeds up learning



Internal Covariance Shift

Each hidden layer changes distribution of inputs to next layer: slows down learning



Training time:

Batch of activations for a layer to normalize

For a given hidden layer

$$H = \begin{bmatrix} H_{11} & \cdots & H_{1K} \\ \vdots & \ddots & \vdots \\ H_{N1} & \cdots & H_{NK} \end{bmatrix}$$

N data points in batch

5

K hidden units activations

Training time:

Batch of activations for a layer to normalize

$$H = \begin{bmatrix} H_{11} & \cdots & H_{1K} \\ \vdots & \ddots & \vdots \\ H_{N1} & \cdots & H_{NK} \end{bmatrix}$$

$$H'_{ik} = \frac{H_{ik} - \mu_k}{\sigma_k}$$

Training time:

Mini-batch of activations for a layer to normalize

$$H = \left[\begin{array}{ccc} H_{11} & \cdots & H_{1K} \\ \vdots & \ddots & \vdots \\ H_{N1} & \cdots & H_{NK} \end{array} \right] \qquad H'_{ik} = \frac{H_{ik} - \mu_k}{\sigma_k} \\ \mu_k = \frac{1}{N} \sum_i H_{ik} \qquad \text{Mean activations across mini-batch for node k.}$$

$$H'_{ik} = \frac{H_{ik} - \mu_k}{\sigma_k}$$

$$\mu_k = \frac{1}{N} \sum_i H_{ik}$$

Training time:

Mini-batch of activations for a layer to normalize

$$H = \left[egin{array}{cccc} H_{11} & \cdots & H_{1K} \ dots & \ddots & dots \ H_{N1} & \cdots & H_{NK} \end{array}
ight] \qquad H_{ik}' = rac{H_{ik} - \mu_k}{\sigma_k} \ \mu_k = rac{1}{N} \sum_i H_{ik} & ext{Mean activations across} \ \sigma_k = rac{1}{N} \sum_i (H_{ik} - \mu_k)^2 + \delta$$

$$H'_{ik} = \frac{H_{ik} - \mu_k}{\sigma_k}$$

$$\mu_k = \frac{1}{N} \sum_i H_{ik}$$

$$\sigma_k = \frac{1}{N} \sum_i (H_{ik} - \mu_k)^2 + \delta$$



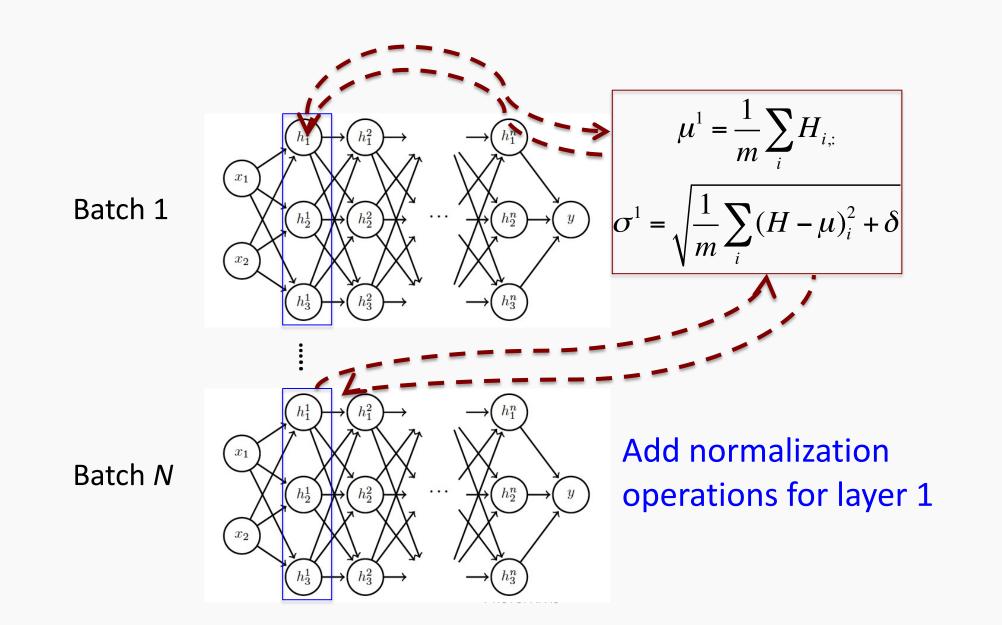
SD of each unit across minibatch

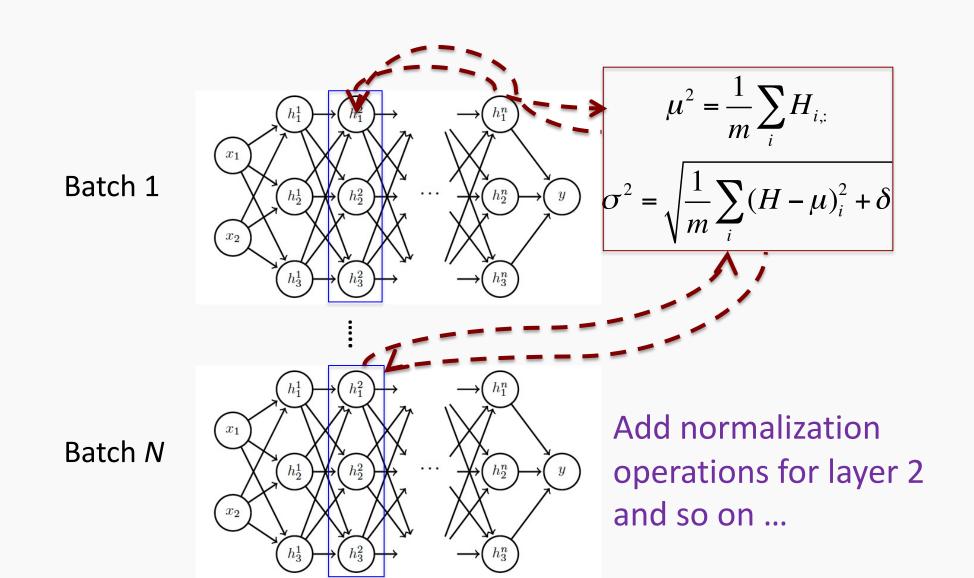
Training time:

Normalization can reduce expressive power Instead use:

$$H'_{ik} = \gamma H'_{ik} + \beta$$
Learnable parameters

Allows network to control range of normalization







We saw how batch normalization works during training, but what about evaluation phase when we do not have a complete batch!

- Store the different means and standard deviations calculated during training.
- Calculate the average mean and standard deviation.

