Extra homework 6

1. Using Taylor series, prove that the forward difference (f(x+h) - f(x))/h approximates the derivative f'(x) with an error of order h (first order approximation), i.e.

$$f'(x) = \frac{f(x+h) - f(x)}{h} + O(h),$$

and that the centered difference (f(x+h) - f(x-h))/2h approximates the derivative f'(x) with an error of order h^2 (second order approximation), i.e.

$$f'(x) = \frac{f(x+h) - f(x-h)}{2h} + O(h^2).$$

[Python] Choose a function f, a point x and compute f'(x). By taking a range of small values h, show that the errors when approximating f'(x) with the finite differences above are proportional to h and h^2 , respectively.

These questions are extra. You will get bonus points for solving them.