

Teacher's section

hw = learned function

for linear regression

$$hw(x) = w_1 * x + w_0$$

Quadratic

$$hw(x) = w_2 * x^2 + w_1 * x + w_0$$

$$d(f_1(w) + f_2(w) + f_3(w) + \dots) / dw$$

Finding values of  $w_1, w_2$  that minimize loss can be done using gradient descent as well

$$y = \text{foo}(x, w_1, w_2, w_3, \dots)$$

or

$$y = \text{foo}(x_1, x_2, x_3, \dots, x_4, \dots, w_1, w_2, w_3, w_4, \dots)$$

for complicated functions like this use gradient descent to find the values of  $w_1, w_2, w_3, \dots$  that minimize loss

loss = sum over all of your data points

$$\sum (y - hw(x_1, x_2, x_3, \dots))^2$$

Gradient descent

Loss function  $\text{loss}(w_1, w_2, w_3, w_4, \dots)$

$$\text{loss}(w_1, w_2, w_3, w_4, \dots) = \sum_{\text{data points}} (h(w_1, w_2, w_3, \dots, x_1, x_2, x_3, \dots) - y)^2$$

Gradient of loss function

$$\text{gradient}(\text{loss}(w_1, w_2, w_3, w_4, \dots)) \Rightarrow$$

$$\{\delta w_1, \delta w_2, \delta w_3, \dots\} = v$$

step w values in direction of vector  $v$

$$w_1' = w_1 + \alpha * \delta w_1$$

$$w_2' = w_2 + \alpha * \delta w_2$$

$$w_3' = w_3 + \alpha * \delta w_3$$

For linear example

$$y = x * w_1 + w_0$$

$$\text{loss} = \sum_j (y_j - h_w(x))^2$$

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{
  d(loss)/dw0=sum_j(y_j-h_w(x_j))
  d(loss)/dw1=sum_j(j-h_w(x_j))*x_j

  gradient = {d(loss)/dw0, d(loss)/dw1}
  ={sum_j(y_j -hw(x_j)), sum_j(y_j-hw(x_j)*x_j)}

  w0'=w0+alpha*sum_j(y_j -hw(x_j))

  w1'=w1+alpha*sum_j(y_j -hw(x_j)*x_j)

  w0=w0'
  w1=w1'

}repeat until it converges

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## Linear classification

Data points consists of parameter values along with a classification type

Parameters  $\{x_1, x_2, \dots\}$

Type - what you are trying to classify by

In example data set would be

$(x_1, x_2, \text{type})$

Example classify football players based on their height and weight

$x_1 = \text{height}$

$x_2 = \text{weight}$

$\text{type} = \{\text{wider receivers, blocker}\}$

Data

$\{5'6", 350 \text{ lbs, blocker}\}$

$\{6'4, 280 \text{ lbs, wide receiver}\}$

$\{5'7", 380, \text{blocker}\}$

$\{6'2", 270 \text{ lbs, wide receiver}\}$

Find a function that classifies a player as a wider receiver or blocker based on their weight and height

$f(\text{weight, height}) = \{\text{blocker/wide\_receiver}\}$

Idea: find a function for which all elements above are of one type and all elements below are the other type

If  $w_1 * \text{weight} + w_2 * \text{height} > w_0 \Rightarrow \text{wide receiver}$

If  $w_1 * \text{weight} + w_2 * \text{height} \leq w_0 \Rightarrow \text{blocker}$

$w_1 * \text{weight} + w_2 * \text{height} - w_0 > 0 \Rightarrow \text{wide receiver}$

$w_1 * \text{weight} + w_2 * \text{height} - w_0 \leq 0 \Rightarrow \text{blocker}$

What are values for  $w_0$ ,  $w_1$  and  $w_2$

Learn these values from data

In slide, find lines that separate points into black points and white point

find values  $w_0$ ,  $w_1$ ,  $w_2$

Define loss function that quantifies how well function does at dividing points into groups

Simple function: just count the number of points on wrong side of line

More complicated function: Take into consideration distance between points on wrong side of line and line.