

$$\frac{x}{\text{hyp}} = \frac{x}{5} = \cos \theta$$

$$x = 5 \cos \theta$$

$$y = 5 \sin \theta$$

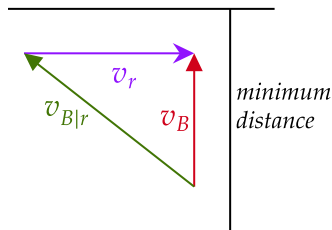
$$v_{B|r} = 5 \cos \theta \hat{i} + 5 \sin \theta \hat{j}$$

$$v_{B|r} = v_B - v_r$$

$$v_B = v_{B|r} + v_r$$

$$v_B = 5 \cos \theta \hat{i} + 5 \sin \theta \hat{j} + 3\hat{i}$$

$$v_B = (3 + 5 \cos \theta) \hat{i} + 5 \sin \theta \hat{j}$$



Assuming the boat attempts to traverse over a minimum distance (takes a straight line)

- Take $\theta =$ to be in the j direction
- Boat is travelling vertical
- i component = 0

$$3 + 5 \cos \theta = 0$$

$$5 \cos \theta = -3$$

$$\cos \theta = \frac{-3}{5}$$

$$\theta = \cos^{-1}\left(\frac{-3}{5}\right) = 127^\circ$$

$$\sin 127 = \sqrt{1 - \cos^2 127}$$

$$\approx 4/5$$

$$v_B = 5 \sin \theta = 5 \cdot \frac{4}{5}$$

$$v_B = 4\hat{j}$$

$$|v_B| = 4 \text{ m/s}$$

Thus it takes :

$$\frac{500}{4} = 125 \text{ seconds to cross}$$

Part A

$$\text{Recall } \sin^2 \theta + \cos^2 \theta = 1$$

$$= \sin^2 \theta = 1 - \cos^2 \theta$$

$$= \sin \theta = \sqrt{1 - \cos^2 \theta}$$

$$v_B = 3 + 5 \cos \theta \hat{i} + 5 \sin \theta \hat{j}$$

$$r_B = t v_B$$

$$r_B = v_B = (3 + 5 \cos \theta) t \hat{i} + 5 \sin \theta t \hat{j}$$

We want to cross a vertical distance of 500m and have y velocity of $5 \sin \theta t \hat{j}$

$$500 = 5 \sin \theta t$$

$$t = \frac{500}{5 \sin \theta} = \frac{100}{\sin \theta}$$

If we cross vertically (optimal)

$$t = \frac{100}{\sin 90} = \frac{100}{1} = 100 \text{ s}$$

Finding how much we drifted optimally

– sub in 100 s for t in i component

$$(3 + 5 \cos(90))t = (3 + 5(0))(100)$$

$$= (3)(100) = 300 \text{ m horizontally}$$

Part B