

MA2287: Complex Analysis Exam Notes

Robert Davidson

Contents

1	Question 1:	3
1.1	Sketch the region in the complex plane determined by the inequality	3
1.2	Determine all solutions to roots of unity	3
1.3	Determine and sketch the image under the mapping	3
1.4	Find z where the function is 0	3
1.5	Calculate principal value $\text{Log}(z)$	3
1.6	Prove the following	3

1 Question 1:

1.1 Sketch the region in the complex plane determined by the inequality

- $|z - 4| > 3|z + 4|$ (2023 (1.a))
- $\{z \in \mathbb{C} : |2z - 1| < 2|2z - i|\}$ (2022 (1.a))

1.2 Determine all solutions to roots of unity

- $z^6 - 1 = 0$ and factorize $z^6 - 1$ as a product of linear and quadratic factors (2023 (1.b))

1.3 Determine and sketch the image under the mapping

- $w = e^z, \{z \in \mathbb{C} : \pi/4 \leq \text{Im}(z) \leq \pi/2\}$ (2023 (1.c))

1.4 Find z where the function is 0

- $\cos(z) = \frac{e^{iz} + e^{-iz}}{2}$ (2023 (1.d))

1.5 Calculate principal value $\text{Log}(z)$

1.6 Prove the following