

Group Scheduling for Block Diagonal Digital Precoder in Multi-user MIMO System

Guanchong Niu and Man-On Pun[†]

School of Science and Engineering

The Chinese University of Hong Kong, Shenzhen

Shenzhen, Guangdong, China, 518172

Abstract—Beam division multiple access (BDMA) has recently been proposed for massive multiple-input multiple-output (MIMO) systems by simultaneously transmitting multiple users' data streams via different beams. In our previous work, single-path propagation channel model has been investigated by opportunistically selecting users to suppress the multiuser interference. Similarly, for multipath channel model, the different paths of each user can be chosen opportunistically. Furthermore, the block diagonal precoding is proposed and the number of RF chains can be significantly reduced by applying the Time Division Duplex(TDD) or switches. Simulation results confirm the effectiveness of proposed block diagonal precoding algorithm.

I. INTRODUCTION

To meet the ever-increasing demand of higher user data rates, it is envisioned that the next-generation cellular systems will be equipped with massive antenna arrays [1]. Capitalizing on the large number of antennas at the base-station (BS), beam division multiple access (BDMA) has recently been proposed to transmit multiple users' data streams via different beams [2], [3]. In contrast to the more conventional multiple access schemes such as Code Division Multiple Access (CDMA) or Orthogonal Frequency Multiple Division Access (OFDMA) that multiplex users in code, time and frequency domains, BDMA separates users in the beam space by transmitting data to different users in orthogonal beam directions. In [2], BDMA was first proposed to decompose the multiuser multiple-input multiple-output (MU-MIMO) system into multiple single-user MIMO channels by multiplexing multiple users' data onto non-overlapping beams. More recently, joint user scheduling and beam selection for BDMA was formulated under the Lyapunov-drift optimization framework before the optimal user-beam scheduling policy was derived in a closed form [3].

In the meantime, hybrid digital and analog beamforming has also been developed for millimeter wave (mmWave) massive MIMO transmissions by dividing the precoding process into two steps, namely analog and digital precoding [4], [5]. More specifically, the transmitted signals are first precoded digitally using a smaller number of radio frequency (RF) chains followed by the analog precoding implemented with a much larger number of low-cost phase shifters. As a result, the hybrid analog-digital precoding architecture requires significantly less RF chains as compared to the fully digital precoding in which every available antenna element is supported by one RF chain.

However, the number of RF chains is lower bounded by the transmitted the number of data streams. In our proposed system, the users are grouped to several clusters. We assume the symbol

duration is much larger than time delay thus the received symbols of different users are same and the channel gain is constant. Compared to serve each cluster separately, the interference will increase since each user has to decode received signal from other clusters. Leveraging the scheduling of users, we can firstly use analog precoding to eliminate the inter-cluster interference between cluster and then implement digital precoding to suppress the intra-cluster interference. The simulation results show that our proposed algorithm can efficiently reduce the number of RF chains without introducing large intra-cluster interference.

Notation: Vectors and matrices are denoted by boldface letters. \mathbf{A}^T and \mathbf{A}^H denote transpose and conjugate transpose of \mathbf{A} , respectively. \mathbf{A}^\dagger being the pseudo inverse of \mathbf{A} while $\|\mathbf{A}\|$ and $|\mathbf{A}|$ stand for the Frobenius norm and determinant of \mathbf{A} , respectively. $\mathbf{A}(i, j)$ denotes the i row, j column element of \mathbf{A} ; $|\mathcal{I}|$ is the cardinality of the enclosed set \mathcal{I} ; Finally, $\mathbb{E}[\cdot]$ and $\Re\{\cdot\}$ denote the expectation and real part of a random variable.

II. SYSTEM MODEL

There are N_{tot} users under considered base station, and N_U of them will be selected to serve. We consider a multi-user mmWave MIMO system shown in Fig. ??, in which a transmitter equipped with N_{RF} RF chains and N_T antennas transmits N_U data streams to N_U receivers with N_R receive antennas. Following the same assumption commonly employed in the literature [6], we assume only one data stream is designated to each scheduled receiver. We use $\mathbf{s}(n)$ to denote the n -th block of N_U data to be transmitted with $\mathbb{E}[\mathbf{s}\mathbf{s}^H] = \frac{1}{N_U}\mathbf{I}_{N_U}$. In the sequel, we concentrate on a single block and omit the temporal index n for notational simplicity.

A. problem formulation

precoded signal:

$$\mathbf{x} = \mathbf{V}\mathbf{F}\mathbf{s} \quad (1)$$

received signal:

$$\mathbf{y}_u = \underbrace{\mathbf{H}_u \mathbf{V} \mathbf{f}_u s_u}_{\text{Desired Signal}} + \underbrace{\mathbf{H}_u \mathbf{V} \sum_{\substack{i=1 \\ i \neq u}}^{N_U} \mathbf{f}_i s_i}_{\text{Interference}} + \underbrace{\mathbf{n}_u}_{\text{Noise}} \quad (2)$$

decoded signal:

$$\hat{s}_u = \mathbf{w}_u^H \mathbf{H}_u \mathbf{V} \mathbf{f}_u s_u + \mathbf{w}_u^H \tilde{\mathbf{n}}_u, \quad (3)$$

where,

$$\tilde{\mathbf{n}}_u = \mathbf{H}_u \mathbf{V} \sum_{\substack{i=1 \\ i \neq u}}^{N_U} \mathbf{f}_i s_i + \mathbf{n}_u. \quad (4)$$

let

$$\mathbf{g}_u^H = \mathbf{w}_u^H \mathbf{H}_u \mathbf{V}. \quad (5)$$

data rate:

$$R_u = \log \left(1 + \frac{P}{N_U} |\mathbf{g}_u^H \mathbf{f}_u|^2 \left(\frac{P}{N_U} \sum_{\substack{i=1 \\ i \neq u}}^{N_U} |\mathbf{g}_u^H \mathbf{f}_i|^2 + \sigma^2 \right)^{-1} \right). \quad (6)$$

average rate:

$$R_{avg} = \frac{1}{KN_U} \sum_{k=1}^K \sum_{u=1}^{N_U} R_u. \quad (7)$$

Problem:

$$\begin{aligned} P1 : & \max_{\mathbf{V}, \mathbf{F}} R_{avg} \\ s.t. & C1 : \text{tr}(\mathbf{V}\mathbf{V}^H) \leq 1, \\ & C2 : \text{tr}(\mathbf{F}\mathbf{F}^H) \leq 1, \\ & C3 : N_{RF} \leq \bar{N}_{RF}, \end{aligned} \quad (8)$$

B. Channel Model

As shown in [7], the mmWave wireless channel can be well modeled by the Saleh-Valenzuela model. Following the same approach developed in [8], we assume that each scatter only contributes one single propagation path. As a result, the u -th user's channel model can be modeled as:

$$\mathbf{H}_u = \sqrt{\frac{N_T N_R}{L_u}} \sum_{l=1}^{L_u} \alpha_{u,l} \cdot \mathbf{a}_R(\phi_{u,l}^r, \theta_{u,l}^r) \cdot \mathbf{a}_T^H(\phi_{u,l}^t, \theta_{u,l}^t), \quad (9)$$

where L_u is the number of scatters of the u -th user's channel. Furthermore, $\alpha_{u,l}$, $\theta_{u,l}^r/\phi_{u,l}^r$ and $\theta_{u,l}^t/\phi_{u,l}^t$ are the complex path gain, azimuth/elevation angles of arrival(AoA) and azimuth/elevation angles of departure(AoD) of the l -th path of the u -th user, respectively. Finally, \mathbf{a} is the array response vector. For an uniform planar array (UPA) of size $P \times Q$ considered in this work, the array response vector \mathbf{a} is given by [8]

$$\mathbf{a}(\phi, \theta) = \frac{1}{\sqrt{N_T}} \begin{bmatrix} 1, e^{jkd(\sin \phi \sin \theta + \cos \theta)}, \dots, \\ e^{jkd(p \sin \phi \sin \theta + q \cos \theta)}, \dots, \\ e^{jkd((P-1) \sin \phi \sin \theta + (Q-1) \cos \theta)} \end{bmatrix}^T, \quad (10)$$

where $k = \frac{2\pi}{\lambda}$ is the wavenumber while d is the distance between two adjacent antennas.

III. PROPOSED BLOCK HYBRID BEAMFORMING

A. When $N_U \leq \bar{N}_{RF}$, ZF precoder

ZF precoder stuff goes here.

B. When $N_U > \bar{N}_{RF}$, Block Diagonal Digital Precoder

Divide users into K clusters.

$$\mathbf{s} = [\mathbf{s}_1^T, \mathbf{s}_2^T, \dots, \mathbf{s}_K^T]^T, \quad \mathbf{s}_k \in \mathcal{C}^{M_j \times 1} \quad (11)$$

K digital precoders for K clusters:

$$\mathbf{F} = [\mathbf{F}_1, \mathbf{F}_2, \dots, \mathbf{F}_K], \quad \mathbf{F}_k \in \mathcal{C}^{N_T \times M_k} \quad (12)$$

K analog precoders for K clusters:

$$\mathbf{V} = [\mathbf{V}_1, \mathbf{V}_2, \dots, \mathbf{V}_K], \quad \mathbf{V}_k \in \mathcal{C}^{N_T \times M_k} \quad (13)$$

precoded signal of k -th cluster:

$$\mathbf{x}_k = \mathbf{V}_k \mathbf{F}_k \mathbf{s}_k \quad (14)$$

radiated signal is equal to the sum of all precoded signals:

$$\mathbf{x} = \sum_{k=1}^K \mathbf{V}_k \mathbf{F}_k \mathbf{s}_k = \mathbf{V} \mathbf{F} \mathbf{s} \quad (15)$$

where,

$$\mathbf{F} = \begin{bmatrix} \mathbf{F}_1 & \dots & \mathbf{0} & \mathbf{0} \\ \vdots & \mathbf{F}_2 & \vdots & \vdots \\ \mathbf{0} & \dots & \ddots & \mathbf{0} \\ \mathbf{0} & \dots & \mathbf{0} & \mathbf{F}_K \end{bmatrix}, \mathbf{V} = \begin{bmatrix} \mathbf{V}_1 & \dots & \mathbf{0} & \mathbf{0} \\ \vdots & \mathbf{V}_2 & \vdots & \vdots \\ \mathbf{0} & \dots & \ddots & \mathbf{0} \\ \mathbf{0} & \dots & \mathbf{0} & \mathbf{V}_K \end{bmatrix} \quad (16)$$

received signal of u -th user in k -th cluster:

$$\begin{aligned} \mathbf{y}_{ku} &= \underbrace{\mathbf{H}_{ku} \mathbf{V}_k \mathbf{F}_k \mathbf{s}_{ku}}_{\text{Desired Signal}} + \underbrace{\mathbf{H}_{ku} \mathbf{V}_k \sum_{\substack{i=1 \\ i \neq u}}^{M_K} \mathbf{f}_{ki} s_{ki}}_{\text{Intra-cluster Interference}} \\ &+ \underbrace{\mathbf{H}_{ku} \sum_{\substack{j=1 \\ j \neq k}}^K \mathbf{V}_j \mathbf{F}_j \mathbf{s}_j}_{\text{Inter-cluster Interference}} + \underbrace{\mathbf{n}_{ku}}_{\text{Noise}} \end{aligned} \quad (17)$$

decoded signal

$$\hat{\mathbf{s}}_{ku} = \mathbf{w}_{ku}^H \mathbf{H}_{ku} \mathbf{V}_k \mathbf{F}_k \mathbf{s}_{ku} + \mathbf{w}_{ku}^H \tilde{\mathbf{n}}_{ku}, \quad (18)$$

$$\tilde{\mathbf{n}}_{ku} = \mathbf{H}_{ku} \mathbf{V}_k \sum_{\substack{i=1 \\ i \neq u}}^{M_K} \mathbf{f}_{ki} s_{ki} + \mathbf{H}_{ku} \sum_{\substack{j=1 \\ j \neq k}}^K \mathbf{V}_j \mathbf{F}_j \mathbf{s}_j + \underbrace{\mathbf{n}_{ku}}_{\text{Noise}} \quad (19)$$

let

$$\mathbf{g}_{ku}^H = \mathbf{w}_{ku}^H \mathbf{H}_{ku} \mathbf{V}_k. \quad (20)$$

$$\mathbf{t}_{ku,j}^H = \mathbf{w}_{ku}^H \mathbf{H}_{ku} \mathbf{V}_j. \quad (21)$$

data rate:

$$R_{ku} = \log \left(1 + \frac{\frac{P}{N_U} |\mathbf{g}_{ku}^H \mathbf{f}_{ku}|^2}{\sum_{\substack{i=1 \\ i \neq u}}^{M_K} |\mathbf{g}_{ku}^H \mathbf{f}_{ki}|^2 + \sum_{\substack{j=1 \\ j \neq k}}^K \|\mathbf{t}_{ku,j}^H \mathbf{F}_j\|^2 + \sigma^2} \right). \quad (22)$$

Problem is equivalently convert to:

$$\begin{aligned}
P2: \quad & \max_{\mathbf{V}, \mathbf{F}} R_{avg} \\
s.t. \quad & C1, C2, \\
& C4: \mathbf{F} = \text{diag}\{\mathcal{F}_k\}, \mathcal{F}_k \in \mathcal{C}^{N_T \times M_k}, \\
& C5: \mathbf{V} = \text{diag}\{\mathcal{V}_k\}, \mathcal{V}_k \in \mathcal{C}^{N_T \times M_k}, \\
& C6: \max\{M_k\}_{k=1}^K \leq \bar{N}_{RF},
\end{aligned} \quad (23)$$

we can solve the above problem by...

IV. USER CLUSTERING AND POWER ALLOCATION

A. Heuristic user clustering

Algorithm 1 Greedy scheduling algorithm for PAPR-aware hybrid beamforming

Input:

All user index set: \mathcal{X}
Selected user index set : $\mathcal{I}_k = \emptyset, k = 1, 2, \dots, K$
Number of clusters: K
Analog precoder solved by Eq. (??): $\mathbf{V} = [\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_{N_U}]$

Procedures:

Initialization: Assign the user index x corresponding to the largest channel gain $|\alpha|$ to \mathcal{I}_1 , i.e. $\mathcal{I}_1 \leftarrow x$ and $\mathcal{X} \setminus x$,

$\mathbf{V}_{else} = [\mathbf{v}_1]$

for x in \mathcal{X} **do**

$p(x) =$

end for

while $|\mathcal{I}| < N_U$ **do**

$\mathbf{A} = [\mathbf{a}_T(\phi_{i_1}^t, \theta_{i_1}^t), \mathbf{a}_T(\phi_{i_2}^t, \theta_{i_2}^t), \dots, \mathbf{a}_T(\phi_{i_{|\mathcal{I}|}}^t, \theta_{i_{|\mathcal{I}|}}^t)]$

Compute the projection space: $\mathbf{P}_A = \mathbf{A}\mathbf{A}^\dagger$

for x in \mathcal{X} **do**

$p(x) = \|\mathbf{P}_A \cdot \mathbf{a}_T(\phi_x^t, \theta_x^t)\|^2$

end for

Find the user index x^* with the minimum $p(x)$

Update $\mathcal{I} \leftarrow x^*$ and $\mathcal{X} \setminus x^*$

end while

B. Power Allocation for SIR

In this section, we will discuss the power allocation of multi-user MIMO system. For high signal-to-noise(SNR) ratio scenario, the noise can be ignored. The powers for users are represented as $\mathbf{p} = [p_1, p_2, \dots, p_{N_U}]$.

The SIR of u -th user is set to be

$$\begin{aligned}
\gamma_u &= \frac{p_u |\mathbf{g}_u^H \mathbf{f}_{ZF,u}^*|^2}{\sum_{i \neq u}^{N_U} p_i |\mathbf{g}_u^H \mathbf{f}_{ZF,i}^*|^2} \\
&= \frac{p_u |\mathbf{g}_u^H \mathbf{f}_{ZF,u}^*|^2}{\sum_{i=1}^{N_U} p_i |\mathbf{g}_u^H \mathbf{f}_{ZF,i}^*|^2 - p_u |\mathbf{g}_u^H \mathbf{f}_{ZF,u}^*|^2}
\end{aligned} \quad (24)$$

Considering the balanced SIR theory

$$\gamma_u = \gamma, u = 1, 2, \dots, N_U \quad (25)$$

the transmitted power can be minimized by eigenvalue problem

$$\mathbf{G}\mathbf{p} = \frac{\gamma + 1}{\gamma} \mathbf{p} \quad (26)$$

where

$$\mathbf{G} = \begin{bmatrix} 1 & T_2/T_1 & \dots & T_{N_U}/T_1 \\ T_1/T_2 & 1 & \dots & T_{N_U}/T_2 \\ \dots & \dots & \dots & \dots \\ T_1/T_{N_U} & T_2/T_{N_U} & \dots & 1 \end{bmatrix} \quad (27)$$

and

$$T_u = |\mathbf{g}_u^H \mathbf{f}_{ZF,u}^*|^2 \quad (28)$$

This problem can be easily solved by

$$\gamma = \frac{1}{\lambda_{max}(\mathbf{G}) - 1} \quad (29)$$

As the elements of \mathbf{G} are positive, from the *Perron Frobenius Theorem*, we know there must exist at least one positive eigenvector and thus the power is solved.

REFERENCES

- [1] F. Boccardi, R. W. Heath, A. Lozano, T. L. Marzetta, and P. Popovski, "Five disruptive technology directions for 5G," *IEEE Communications Magazine*, vol. 52, no. 2, pp. 74–80, 2014.
- [2] C. Sun, X. Gao, S. Jin, M. Matthaiou, Z. Ding, and C. Xiao, "Beam Division Multiple Access Transmission for massive MIMO communications," *IEEE Transactions on Communications*, vol. 63, no. 6, pp. 2170–2184, June 2015.
- [3] Z. Jiang, S. Chen, S. Zhou, and Z. Niu, "Joint user scheduling and beam selection optimization for beam-based massive MIMO downlinks," *IEEE Transactions on Wireless Communications*, vol. 17, no. 4, pp. 2190–2204, April 2018.
- [4] S. Han, I. Chih-Lin, Z. Xu, and C. Rowell, "Large-scale antenna systems with hybrid analog and digital beamforming for millimeter wave 5G," *IEEE Communications Magazine*, vol. 53, no. 1, pp. 186–194, 2015.
- [5] O. El Ayach, S. Rajagopal, S. Abu-Surra, Z. Pi, and R. W. Heath, "Spatially sparse precoding in millimeter wave MIMO systems," *IEEE Transactions on Wireless Communications*, vol. 13, no. 3, pp. 1499–1513, 2014.
- [6] A. Alkhateeb, G. Leus, and R. W. Heath, "Limited feedback hybrid precoding for multi-user millimeter wave systems," *IEEE Transactions on Wireless Communications*, vol. 14, no. 11, pp. 6481–6494, 2015.
- [7] T. S. Rappaport, R. W. Heath Jr, R. C. Daniels, and J. N. Murdock, *Millimeter wave wireless communications*. Pearson Education, 2014.
- [8] A. Alkhateeb, O. El Ayach, G. Leus, and R. W. Heath, "Channel estimation and hybrid precoding for millimeter wave cellular systems," *IEEE Journal of Selected Topics in Signal Processing*, vol. 8, no. 5, pp. 831–846, 2014.