Group Scheduling for Block Diagonal Digital Precoder in Multi-user MIMO System

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Abstract—Beam division multiple access (BDMA) has recently been proposed for massive multiple-input multiple-output (MIMO) systems by simultaneously transmitting multiple users' data streams via different beams. In our previous work, single-path propagation channel model has been investigated by opportunistically selecting users to suppress the multiuser interference. Similarly, for multipath channel model, the different paths of each user can be chosen opportunistically. Furthermore, the block diagonal precoding is proposed and the number of RF chains can be significantly reduced by applying the Time Division Duplex(TDD) or switches. Simulation results confirm the effectiveness of proposed block diagonal precoding algorithm.

I. INTRODUCTION

To meet the ever-increasing demand of higher user data rates, it is envisioned that the next-generation cellular systems will be equipped with massive antenna arrays [1]. Capitalizing on the large number of antennas at the base-station (BS), beam division multiple access (BDMA) has recently been proposed to transmit multiple users' data streams via different beams [2], [3]. In contrast to the more conventional multiple access schemes such as Code Division Multiple Access (CDMA) or Orthogonal Frequency Multiple Division Access (OFDMA) that multiplex users in code, time and frequency domains, BDMA separates users in the beam space by transmitting data to different users in orthogonal beam directions. In [2], BDMA was first proposed to decompose the multiuser multiple-input multiple-output (MU-MIMO) system into multiple single-user MIMO channels by multiplexing multiple users' data onto non-overlapping beams. More recently, joint user scheduling and beam selection for BDMA was formulated under the Lyapunov-drift optimization framework before the optimal user-beam scheduling policy was derived in a closed form [3].

In the meantime, hyrbid digital and analog beamforming has also been developed for millimeter wave (mmWave) massive MIMO transmissions by dividing the procoding process into two steps, namely analog and digital precoding [4], [5]. More specifically, the transmitted signals are first precoded digitally using a smaller number of radio frequency (RF) chains followed by the analog precoding implemented with a much larger number of low-cost phase shifters. As a result, the hybrid analog-digital precoding architecture requires significantly less RF chains as

compared to the fully digital precoding in which every available antenna element is supported by one RF chain.

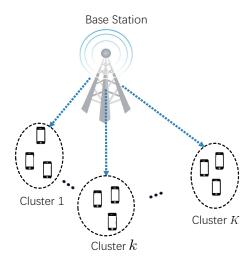


Fig. 1. Group scheduling to reduce the number of RF chains and eliminate the intra-cluster interference

However, the minimal number of RF chains is constrained by the transmitted data stream. In our proposed system, the users are grouped to several clusters and then communicate with base station in turn. We assume the symbol duration is much larger than time delay thus the received symbols of different users are same. Compared to serve each cluster separately, the interference will increase since each user has to decode received signal from other clusters. Thanks to the scheduling of users, we can firstly use analog precoding to eliminate the intra-cluster interference between cluster and then implement digital precoding to suppress the inner-cluster interference. The simulation results show that our proposed algorithm can efficiently reduce the number of RF chains without introducing large intra-cluster interference.

Notation: Vectors and matrices are denoted by boldface letters. \boldsymbol{A}^T and \boldsymbol{A}^H denote transpose and conjugate transpose of \boldsymbol{A} , respectively. \boldsymbol{A}^\dagger being the pseudo inverse of \boldsymbol{A} while $||\boldsymbol{A}||$ and $|\boldsymbol{A}|$ stand for the Frobenius norm and determinant of \boldsymbol{A} , respectively. $\boldsymbol{A}(i,j)$ denotes the i row, j column element of \boldsymbol{A} ; $|\mathcal{I}|$ is the cardinality of the enclosed set \mathcal{I} ; Finally, $\mathbb{E}[\cdot]$ and $\Re\{\cdot\}$ denote the expectation and real part of a random variable.

This work was supported, in part, by the CUHKSZ President's Fund under Grant No. PF.01.000211 and Shenzhen Science and Technology Innovation Committee under Grant No. ZDSYS20170725140921348.

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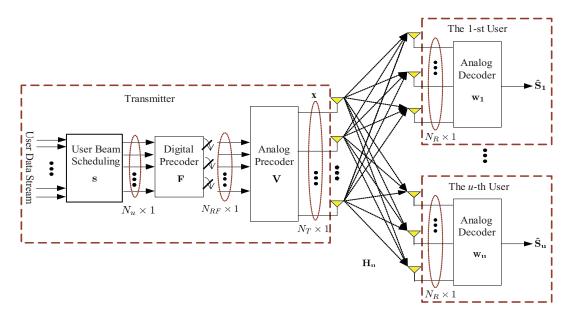


Fig. 2. Block diagram of the hybrid precoding system under consideration

II. SYSTEM MODEL

We consider a multi-user mmWave MIMO system shown in Fig. 2, in which a transmitter equipped with N_{RF} RF chains and N_T antennas transmits N_U data streams to N_U receivers with N_R receive antennas. Following the same assumption commonly employed in the literature [6], we assume only one data stream is designated to each scheduled receiver. We use s(n) to denote the n-th block of N_U data to be transmitted with $\mathbb{E}\left[ss^H\right] = \frac{1}{N_U} I_{N_U}$. In the sequel, we concentrate on a single block and omit the temporal index n for notational simplicity.

The hybrid precoding system first multiplies s with the digital precoding matrix $F = [f_1, \cdots, f_u, \cdots f_{N_U}]$ with f_u of dimension $N_{RF} \times 1$ being the digital beamforming vector for the u-th user, $u = 1, 2, \cdots, N_U$. After that, the output signal will be multiplied by the analog precoding matrix $V = [v_1, \cdots, v_i, \cdots, v_{N_{RF}}]$ with v_i of dimension $N_T \times 1$ being the i-th analog beamforming vector for $i = 1, 2, \cdots, N_{RF}$. The resulting precoded signal x of dimension $N_T \times 1$ can be expressed as

$$x = V \cdot F \cdot s = V \sum_{u=1}^{N_U} f_u s_u \tag{1}$$

The precoded signal \boldsymbol{x} is then broadcast to N_U users. The signal received by the u-th user is given by

$$y_{u} = H_{u}x + n_{u}$$

$$= \underbrace{H_{u}Vf_{u}s_{u}}_{\text{Desired Signal}} + \underbrace{H_{u}V\sum_{\substack{i=1\\i\neq u}}^{N_{U}}f_{i}s_{i}}_{\text{Noise}} + \underbrace{n_{u}}_{\text{Noise}}, \quad (2)$$

where $H_u \in \mathbb{C}^{N_R \times N_T}$ is the MIMO channel matrix between the transmitter and the *u*-th receiver [5]. Furthermore, n_u is complex

additive white Gaussian noise with zero mean and variance equal to σ^2 .

Assuming the receivers are all low-cost terminals that perform analog beamforming only in decoding, the decoded signal by the u-th user denoted by \hat{s}_u is given by

$$\hat{s}_u = \boldsymbol{w}_u^H \boldsymbol{H}_u \boldsymbol{V} \boldsymbol{f}_u \boldsymbol{s} + \boldsymbol{w}_u^H \tilde{\boldsymbol{n}}_u, \tag{3}$$

where w_u of dimension $N_T \times 1$ is the analog beamforming vector employed by the u-th receiver with the power constraint of $|w_u|^2 = 1$ and

$$ilde{m{n}}_u = m{H}_u m{V} \sum_{\substack{i=1 \ i
eq u}}^{N_U} m{f}_i s_i + m{n}_u. ag{4}$$

Note that the first term in Eq. (3) stands for the desired signal while the second term is the sum of its own receiver noise and interference from other users.

A. Channel Model

As shown in [7], the mmWave wireless channel can be well modeled by the Saleh-Valenzuela model. Following the same approach developed in [8], we assume that each scatter only contributes one single propagation path. As a result, the u-th user's channel model can been modeled as:

$$\boldsymbol{H}_{u} = \sqrt{\frac{N_{T}N_{R}}{L_{u}}} \sum_{l=1}^{L_{u}} \alpha_{u,l} \cdot \boldsymbol{a}_{R}(\phi_{u,l}^{r}, \theta_{u,l}^{r}) \cdot \boldsymbol{a}_{T}^{H}(\phi_{u,l}^{t}, \theta_{u,l}^{t}), \quad (5)$$

where L_u is the number of scatters of the u-th user's channel. Furthermore, $\alpha_{u,l}$, $\theta^r_{u,l}/\phi^r_{u,l}$ and $\theta^t_{u,l}/\phi^t_{u,l}$ are the complex path gain, azimuth/elevation angles of arrival(AoA) and azimuth/elevation angles of departure(AoD) of the l-th path of the u-th user, respectively. Finally, a is the array response vector. For an

uniform planar array (UPA) of size $P \times Q$ considered in this work, the array response vector a is given by [8]

$$\mathbf{a}(\phi,\theta) = \frac{1}{\sqrt{N_T}} \left[1, e^{jkd(\sin\phi\sin\theta + \cos\theta)}, \cdots, e^{jkd(p\sin\phi\sin\theta + q\cos\theta)}, \cdots, e^{jkd((P-1)\sin\phi\sin\theta + (Q-1)\cos\theta)} \right]^T,$$
(6)

where $k = \frac{2\pi}{\lambda}$ is the wavenumber while d is the distance between two adjacent antennas.

B. Grouping for Users Under Base Station

For simplicity, the group users are divided uniformly and then the users under a base station can be divided into K clusters with $N_K = N_U/K$ in each cluster. Thus, the digital precoder is given

$$\boldsymbol{F} = \begin{bmatrix} \boldsymbol{F}_1 & \boldsymbol{F}_2 & \cdots & \boldsymbol{F}_K \end{bmatrix} \tag{7}$$

Where

$$\boldsymbol{F}_k = \begin{bmatrix} \boldsymbol{f}_{11} & \boldsymbol{f}_{12} & \cdots & \boldsymbol{f}_{1N_K} \end{bmatrix} \tag{8}$$

means the column vectors of digital precoder in k-th cluster.

The signal received by u-th user in k-th cluster is given by

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where $s_u k$ is the u-th signal for u-th user in k-th cluster. Compared to Eq. (2), there is nothing special but the interference term is separated as inner-cluster and intra-cluster interference corresponding to the user scheduling.

C. Problem Formulation

For notational simplicity, we denote by g_u^H the effective array gain of the u-th user in k-th group with

$$\boldsymbol{g}_u^H = \boldsymbol{w}_u^H \boldsymbol{H}_u \boldsymbol{V}. \tag{10}$$

Then, the channel capacity of the u-th user in k-th cluster is given by

$$R_{uk} = \log \begin{pmatrix} \hat{\boldsymbol{s}} = \boldsymbol{G} \cdot \boldsymbol{F} \cdot \boldsymbol{s} + \boldsymbol{\xi}, & (17) \\ \frac{\frac{P}{N_U} |\boldsymbol{g}_u^H \boldsymbol{f}_{uk}|^2}{\sum_{\substack{i=1\\i\neq u}}^{N_K} |\boldsymbol{g}_u^H \boldsymbol{f}_{ik}|^2 + \sum_{\substack{j\neq k}}^{K} \sum_{t=1}^{K} |\boldsymbol{g}_u^H \boldsymbol{f}_{tj}|^2 + \sigma^2 \end{pmatrix} + 1$$
where $\boldsymbol{G} = [\boldsymbol{g}_1, \boldsymbol{g}_2, \cdots, \boldsymbol{g}_{N_U}]^H$ is of dimension $N_U \times N_{RF}$ and $\boldsymbol{\xi} = [\boldsymbol{w}_1^H \tilde{\boldsymbol{n}}_1, \boldsymbol{w}_2^H \tilde{\boldsymbol{n}}_2, \cdots, \boldsymbol{w}_{N_U}^H \tilde{\boldsymbol{n}}_{N_U}]^T$. [8] proposed a zero-forcing approach to solve Eq. (13) by setting
$$\boldsymbol{F}_{ZF} = \boldsymbol{G}^{\dagger} = \boldsymbol{G}^H (\boldsymbol{G} \boldsymbol{G}^H)^{-1}, \qquad (18)$$
with $N_{RF} \geq N_U$.

Subsequently, the system sum-rate capacity that is a function of V and F can be computed as

$$R_{tot} = \sum_{k=1}^{K} \sum_{u=1}^{N_K} R_{uk}.$$
 (12)

In order to reduce the number of RF chains by switches as shown in Fig. 2, the digital precoding matrix is required to transfer as block diagonal matrix by grouping.

Finally, the optimal design of the digital and analog precoding matrices can be formulated as

$$\{\boldsymbol{V}^*, \boldsymbol{F}^*\} = \underset{\tilde{\boldsymbol{V}}, \tilde{\boldsymbol{F}}}{\arg \max} R_{tot} \left(\tilde{\boldsymbol{V}}, \tilde{\boldsymbol{F}}\right)$$

$$s.t. \quad ||\tilde{\boldsymbol{V}}\tilde{\boldsymbol{f}}_u||^2 = 1, \quad u = 1, 2, \cdots, N_U$$

$$\boldsymbol{F}_{ij} = 0, \quad \forall i \neq j.$$

$$(13)$$

where $F_{ij} \in \mathbb{C}^{N_K \times N_K}$ is the block matrix of F.

III. BLOCK DIAGONAL DIGITAL PRECODER

In the proposed system, we are aiming to use analog beamforming to eliminate the intra-cluster interference and digital precoding to eliminate the inner-cluster interference. Based on this idea, the digital precoder matrix can be simplified as block diagonal matrix and the number of RF chains can be reduced to N_K . The precoding process in transmitter can be separated as analog precoding and digital precoding.

A. Analog Precoding

With the assumption for infinite transmitter antennas in channel model Eq. (5)

$$\lim_{N \to +\infty} \boldsymbol{a}_{T}^{H}(\phi_{i,l}^{t}, \theta_{i,l}^{t}) \cdot \boldsymbol{a}_{T}(\phi_{j,p}^{t}, \theta_{j,p}^{t}) = \delta(i-j)\delta(l-p), \quad (14)$$

the analog beamforming vector of u-th user is designed to match one of the array response vector

$$\mathbf{v}_u \in \{\mathbf{a}_T(\phi_{u,l}^t, \theta_{u,l}^t)\}_{l=1}^{L_u}$$
 (15)

Although it's impractical to use infinite number of antennas, the residual interference can be minimized by selecting the beam with least interference

$$\{v_{u}\}_{u=1}^{N_{U}} = \arg\min \frac{||w_{u}H_{u}v_{u}||_{F}^{2}}{\sum_{i=1, i\neq u}^{N_{U}} ||w_{u}H_{u}v_{i}||_{F}^{2}}$$

$$s.t. \quad v_{u} \in \{a_{T}(\phi_{u,l}^{t}, \theta_{u,l}^{t})\}_{l=1}^{L_{u}}$$
(16)

Then the analog precoder of BDMA is obtained.

B. Zero-forcing for Digital Beamforming

We denote by $\hat{s} = [\hat{s}_1, \hat{s}_2, \cdots, \hat{s}_{N_U}]^T$ the estimated signal vector. Recalling Eq. (3), \hat{s} can be expressed as [8]

$$\hat{\mathbf{s}} = \mathbf{G} \cdot \mathbf{F} \cdot \mathbf{s} + \boldsymbol{\xi},\tag{17}$$

$$\mathbf{F}_{ZF} = \mathbf{G}^{\dagger} = \mathbf{G}^{H} (\mathbf{G}\mathbf{G}^{H})^{-1}, \tag{18}$$

To satisfy the power constraint, power normalization is performed on each f_u derived from $F_{ZF}=$ $[\boldsymbol{f}_{ZF,1}, \boldsymbol{f}_{ZF,2}, \cdots, \boldsymbol{f}_{ZF,N_U}]$ as

$$\mathbf{f}_{ZF,u}^* = \frac{\mathbf{f}_{ZF,u}}{||\mathbf{V} \cdot \mathbf{f}_{ZF,u}||}.$$
 (19)

In the sequel, the hybrid beamforming scheme derived from Eq. (19) is referred to as the unconstrained zero-forcing hybrid beamforming (ZFU-HBF) for benchmarking our following proposed schemes.

C. Clipping for Digital Precoder

To realize the block digital precoding matrix, one of the simplest methods is to clip the off-block diagonal matrix to be zero, *i.e.*

$$\mathbf{F}_{ij} = 0 \quad \text{for} \quad i \neq j$$
 (20)

where we set

$$\mathbf{F}_{ZF} = \begin{bmatrix} \mathbf{F}_{11} & \mathbf{F}_{12} & \cdots & \mathbf{F}_{1K} \\ \mathbf{F}_{21} & \mathbf{F}_{22} & \cdots & \mathbf{F}_{2K} \\ \cdots & \cdots & \mathbf{F}_{pj} & \cdots \\ \mathbf{F}_{K1} & \mathbf{F}_{K2} & \cdots & \mathbf{F}_{KK} \end{bmatrix}$$
(21)

Obviously, clipping method will increase the interference compared with ZFU-HBF. Next, we will introduce a group-scheduling algorithm to reduce the residual interference of clipping.

D. Group Scheduling

To minimize the interference from different clusters, the analog precoding matrix V is also divided into K parts like F

$$V = [V_1, V_2, \cdots, V_K] \tag{22}$$

where V_k is the column vectors of analog precoder in k-th cluster. Thus, the group scheduling problem is represented as

$$\{V_{k}\}_{k=1}^{K} = \arg\min \frac{||w_{u}H_{u}V_{k}||_{F}^{2}}{\sum_{i=1, i \neq k}^{N_{U}} ||w_{u}H_{u}V_{i}||_{F}^{2}}$$
s.t. $V_{k} \in \{v_{u}\}_{u=1}^{N_{U}} \quad k = 1, 2, \dots, K$ (23)

After solving Eq. (23), the analog beamforming has the following property

$$H_u V_k \approx 0 \quad \text{for} \quad v_u \notin V_k$$
 (24)

By rewriting the Intra-cluster interference term in Eq. (9)

$$H_u V \sum_{j \neq k}^K \sum_{t=1}^{N_K} f_{tj} s_{tj} \approx H_u V_k \sum_{j=1, j \neq k}^K F_{kj} s_j$$
 (25)

Then the signal received by u-th user in k-th cluster is given by

$$y_{uk} \approx H_u V_k F_{kk} s_k + H_u V_k \sum_{j=1, j \neq k}^{K} F_{kj} s_j + n_u$$
 (26)

The second term can be removed by setting

$$\mathbf{F}_{kj} = 0 \quad \text{for} \quad j \neq k, j \in (1, K) \tag{27}$$

Furthermore, since the F_{ik} , $i \neq k$ doesn't work on Eq. (26), it can be just set to zero. The problem is simplified as Eq. (3).

$$\hat{s}_{u} = \boldsymbol{w}_{u}^{H} \boldsymbol{H}_{u} \boldsymbol{V}_{k} \boldsymbol{F}_{kk} \boldsymbol{s}_{k} + \boldsymbol{w}_{u}^{H} \boldsymbol{n}_{u}, \tag{28}$$

Finally, we have the block-diagonal precoding matrix by group scheduling.

E. Convex Optimization

Another method to realize the block diagonal matrix is minimizing the interference between ZFU-HBF and block-diagonal digital precoding by convex optimization. The convex problem is formulated as

$$F_{Block}^* = \arg\min ||GF_{ZF} - GF_{Block}||_F^2$$
s.t. $[F_{Block}]_{ij} = 0$ for $j \neq k, j \in (1, K)$

IV. POWER ALLOCATION FOR SIR

In this section, we will discuss the power allocation of multiuser MIMO system. For high signal-to-noise(SNR) ratio scenario, the noise can be ignored. The powers for users are represented as $p = [p_1, p_2, \cdots, p_{N_U}]$.

The SIR of u-th user is set to be

$$\gamma_u = \frac{p_u |\mathbf{g}_u^H \mathbf{f}_{ZF,u}^*|^2}{\sum_{i \neq u}^{N_U} p_i |g_u^H \mathbf{f}_{ZF,i}^*|^2}$$
(30)

$$= \frac{p_u |\boldsymbol{g}_u^H \boldsymbol{f}_{ZF,u}^*|^2}{\sum_{i=1}^{N_U} p_i |g_u^H \boldsymbol{f}_{ZF,i}^*|^2 - p_u |g_u^H \boldsymbol{f}_{ZF,u}^*|^2}$$
(31)

Considering the balanced SIR theory

$$\gamma_u = \gamma, u = 1, 2, \cdots, N_U \tag{32}$$

the transmitted power can be minimized by eigenvalue problem

$$Gp = \frac{\gamma + 1}{\gamma}p\tag{33}$$

where

$$G = \begin{bmatrix} 1 & T_2/T_1 & \cdots & T_{N_U}/T_1 \\ T_1/T_2 & 1 & \cdots & T_{N_U}/T_2 \\ \cdots & \cdots & \cdots & \cdots \\ T_1/T_{N_U} & T_2/T_{N_U} & \cdots & 1 \end{bmatrix}$$
(34)

and

$$T_u = |g_u^H f_{ZF,u}^*|^2 (35)$$

V. SIMULATION RESULTS

In this section, we use S-V model to prove the effective of group scheduling method.

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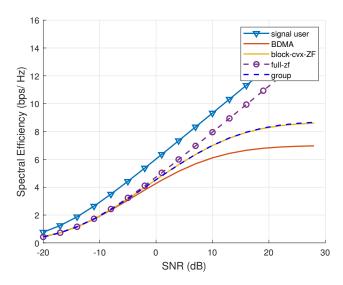


Fig. 3. 16 users with 4 paths for each user are assigned to 4 clusters.

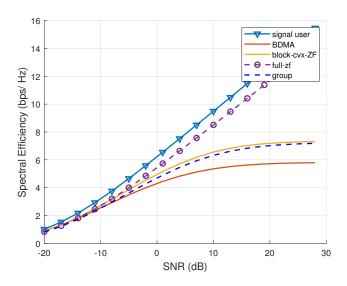


Fig. 4. 16 users with single path are assigned to 4 clusters.

VI. APPENDIX: A NUMERICAL EXAMPLE

To understand the grouping problem, a numerical example is shown below. In a system, 4 users are divided into 2 clusters which are orthogonal with each other as shown in Fig. 5. In this figure, the $\boldsymbol{H}_u, u \in (1,4)$ means the channel model with single path, given by

$$\boldsymbol{H}_{u} = \sqrt{N_{T}N_{R}} \cdot \alpha_{u} \cdot \boldsymbol{a}_{R}(\phi_{u}^{r}, \theta_{u}^{r}) \cdot \boldsymbol{a}_{T}^{H}(\phi_{u}^{t}, \theta_{u}^{t}).$$
 (36)

To maximize the channel capacity, the analog precoder can be simply designed as $V_u = a_T(\phi_u^t, \theta_u^t)$. In this scenario, $V_{1,2} = [V_1, V_2]$ is orthogonal to $V_{3,4} = [V_3, V_4]$, *i.e.*

$$\boldsymbol{V}_{1,2}^T \cdot \boldsymbol{V}_{3,4} \approx 0 \tag{37}$$

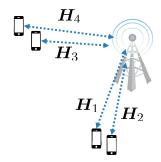


Fig. 5. There are two clusters which perpendicular to each other.

The digital precoding matrix is given by

$$\mathbf{F} = \begin{bmatrix} \mathbf{F}_{12} & \mathbf{F}_{off1} \\ \mathbf{F}_{off2} & \mathbf{F}_{34} \end{bmatrix} \tag{38}$$

where $F \in \mathbb{C}^{4\times 4}$ and $F_{12}, F_{34}, F_{off1}, F_{off2} \in \mathbb{C}^{4\times 4}$. According to Eq. (??), the received signal is

$$x = [V_{12}, V_{34}] \cdot F \cdot s$$

= $V_{12}(F_{12}s_{12} + F_{off1}s_{34}) + V_{34}(F_{off2}s_{12} + F_{34}s_{34})$ (39)

and according to Eq. (??), set u = 1

$$s_{1} = \boldsymbol{w}_{1}^{H} \boldsymbol{H}_{1} \left[\boldsymbol{V}_{12} (\boldsymbol{F}_{12} \boldsymbol{s}_{12} + \boldsymbol{F}_{off1} \boldsymbol{s}_{34}) + \boldsymbol{V}_{34} (\boldsymbol{F}_{off2} \boldsymbol{s}_{12} + \boldsymbol{F}_{34} \boldsymbol{s}_{34}) \right] + \boldsymbol{w}_{1}^{H} \boldsymbol{n}_{1}$$

$$(40)$$

As shown in Eq. (37), we have $H_1V_{34}=H_2V_{34}=0$, which means F_{off2} doesn't have any interference on s_1 . Furthermore, the f_{off1} can be simply set as zero matrix. Then s_1 and s_2 can be decoded by zero-forcing. Similarly, by setting $F_{off2}=0$, s_3 and s_4 can be decoded.