MTH 201: Calculus - Module 1B

The concept of the limit (AC 1.2)

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Agenda

Review of Daily Prep

Polling for today

Go to www.mentimeter.com and enter code 32 04 90 Or go to https://www.menti.com/4d48wn64k6

Q+A

Limits using algebra

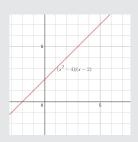
Finding limits using algebra

Alert

Finding a limit of a function at a point, is not always the same thing as evaluating the function at that point.

Example

$$\lim_{x \to 2} \frac{x^2 - 4}{x - 2} = 4$$



But $\frac{x^2-4}{x-2}$ evaluated at x=2 is undefined (0/0).

Using algebra first

Pro Tip

Always try to simplify the algebra first.

Example

$$\lim_{x \to 2} \frac{x^2 - 4}{x - 2} = \lim_{x \to 2} \frac{(x - 2)(x + 2)}{x - 2}$$
$$= \lim_{x \to 2} (x + 2)$$

As x gets closer to 2, x + 2 gets closer to 4.

Therefore $\lim_{x\to 2} \frac{x^2-4}{x-2} = 4$.

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Practice with the concept

Go to:

http://gvsu.edu/s/1pq

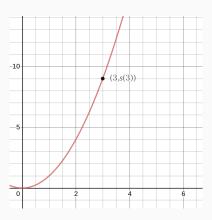
Find the value of the limit using algebra simplification first. Spoiler: The answer is 12.

Instantaneous velocity using

limits

Average velocity

Consider a moving object whose position function is given by $s(t) = t^2$ where t is time in seconds, s is position in meters.



Finding average and instantaneous velocity

The average velocity on the small time interval from t = 3 to t = 3 + h is

$$\frac{s(3+h)-s(3)}{(3+h)-3}=\frac{s(3+h)-s(3)}{h}$$

On Mentimeter: If we wanted to find the *instantaneous velocity* at t=3, how would we modify this?

Working out the velocity

We get the instantaneous velocity at t=3 by taking the average velocity expression and evaluating its limit as $h \to 0$:

$$IV_{t=3} = \lim_{h \to 0} \frac{s(3+h) - s(3)}{h}$$

But we can now work out the value with algebra! Work with your partner to do this:

Spoiler: The answer is 6 meters/second.

Getting the instantaneous velocity

$$IV_{t=3} = \lim_{h \to 0} \frac{s(3+h) - s(3)}{h}$$

$$= \lim_{h \to 0} \frac{(3+h)^2 - 9}{h}$$

$$= \lim_{h \to 0} \frac{9 + 6h + h^2 - 9}{h}$$

$$= \lim_{h \to 0} \frac{6h + h^2}{h}$$

$$= \lim_{h \to 0} \frac{h(6+h)}{h}$$

$$= \lim_{h \to 0} (6+h)$$

$$= 6 \text{ meters/second}$$

What to do next

Coming up next

- Online followup activities: Due 11:59pm ET, Friday 9/11 (Link to be posted and in email)
- Daily Prep for Module 2A: Due 11:59pm ET, Sunday 9/13 (Blackboard)
- WeBWorK 1B: Due 11:59pm ET, Sunday 9/13 (WeBWorK)

Continue to check email and announcements every day — ask questions and give help on CampusWire too.