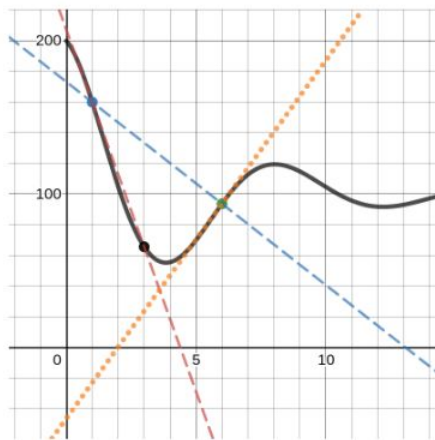


The second derivative

MTH 201 – Module 3B part 2

Retrieval practice

Which of the following quantities is/are negative in this picture? Select all that apply.



The average rate of change in s on $[1, 3]$

The average rate of change in s on $[1, 6]$

The instantaneous rate of change in s at $t = 6$

There's not enough information present to decide

(Select this option if none of the above is true)



The derivative $f'(a)$ tells you

The instantaneous rate of change in $f(x)$ at $x = a$

The slope of the tangent line touching the graph of $f(x)$ at $x = a$

The slope of the secant line connecting $x = 0$ and $x = a$ on the graph of $f(x)$

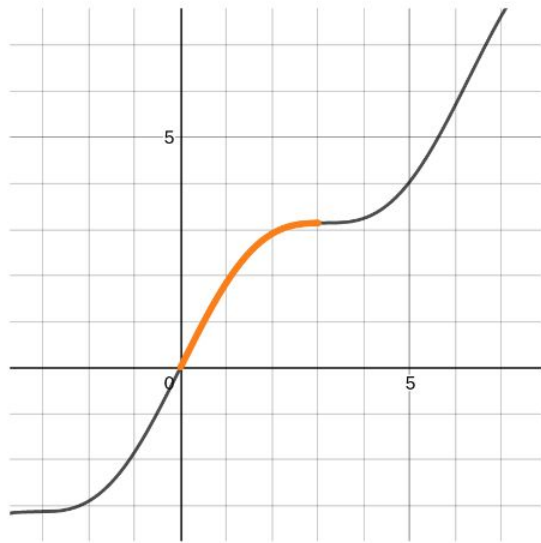
Both (a) and (b)



To

0

On the section of the graph of $y = f(x)$ from 0 to 2 (colored orange),



f is increasing and concave up

f is increasing and concave down

f is decreasing and concave up

f is decreasing and concave down



Concave Up, Decreasing



Concave Up, Increasing



Concave Down, Decreasing



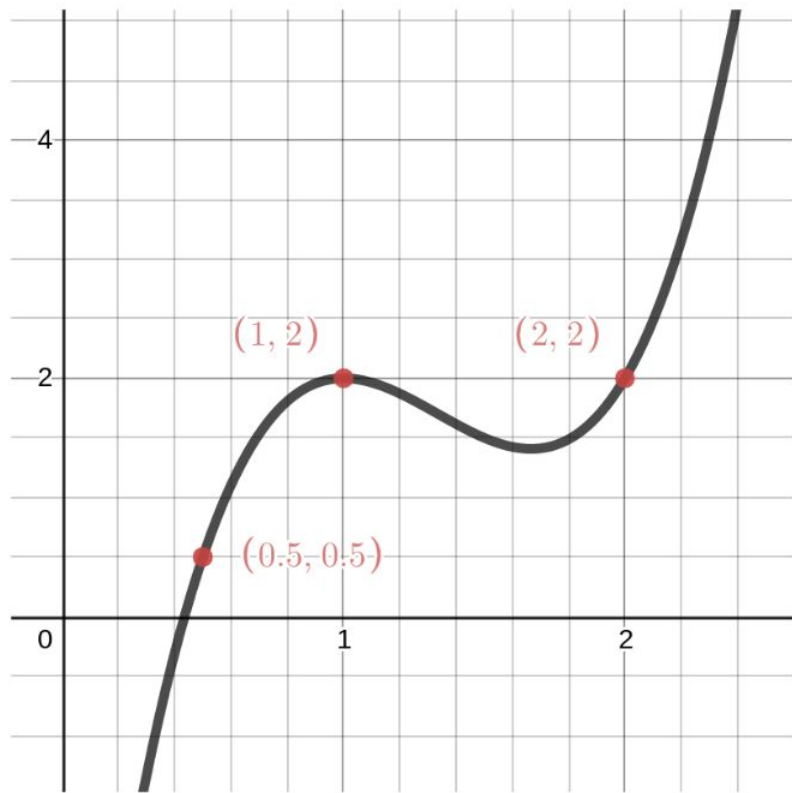
Concave Down, Increasing





Connecting this to the second
derivative

The graph of $y = g(x)$ is shown. At the point $(0.5, 0.5)$,



$$g' > 0 \text{ and } g'' > 0$$

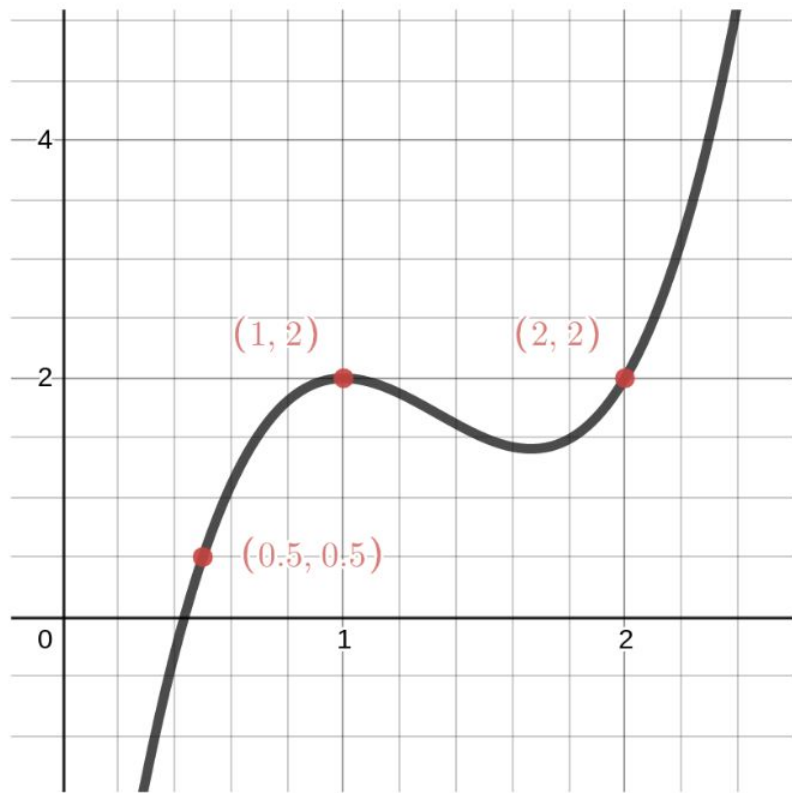
$$g' > 0 \text{ and } g'' < 0$$

$$g' < 0 \text{ and } g'' > 0$$

$$g' < 0 \text{ and } g'' < 0$$



The graph of $y = g(x)$ is shown. At the point $(2, 2)$,



$$g' > 0 \text{ and } g'' > 0$$

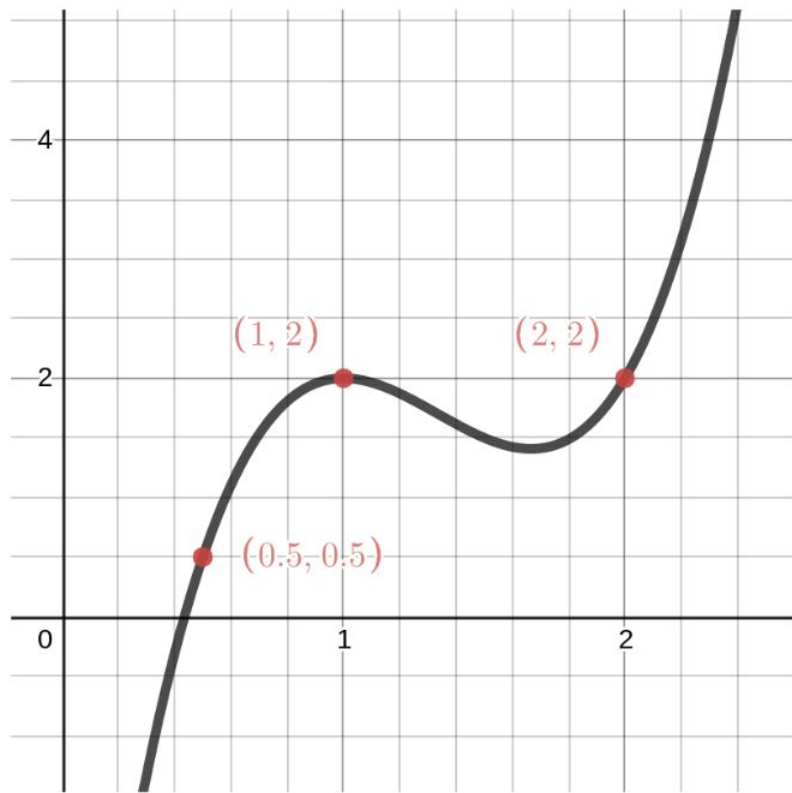
$$g' > 0 \text{ and } g'' < 0$$

$$g' < 0 \text{ and } g'' > 0$$

$$g' < 0 \text{ and } g'' < 0$$



The graph of $y = g(x)$ is shown. Based on the graph,



$$g''(1) = 0$$

$$g''(1) < 0$$

$$g''(1) > 0$$

None of the above



The second derivative $f''(x)$ of a function $f(x)$ is...

→ The derivative of $f'(x)$

→ The rate at which $f'(x)$ is changing

Concave up \rightarrow

Rate of change is increasing \rightarrow

$f'(x)$ is increasing \rightarrow

$f''(x)$ is positive

Concave down \rightarrow

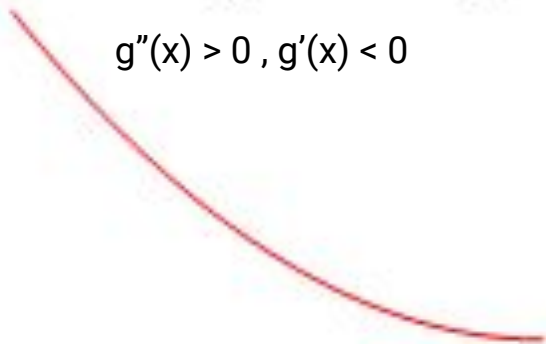
Rate of change is decreasing \rightarrow

$f'(x)$ is decreasing \rightarrow

$f''(x)$ is negative

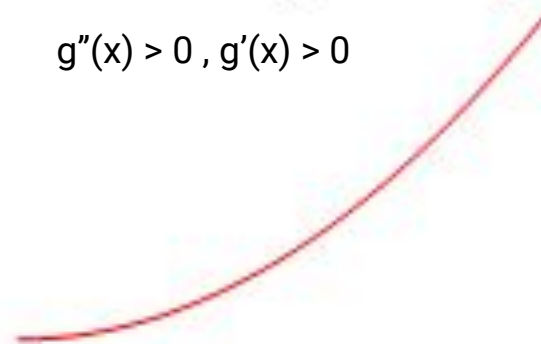
Concave Up, Decreasing

$$g''(x) > 0, g'(x) < 0$$



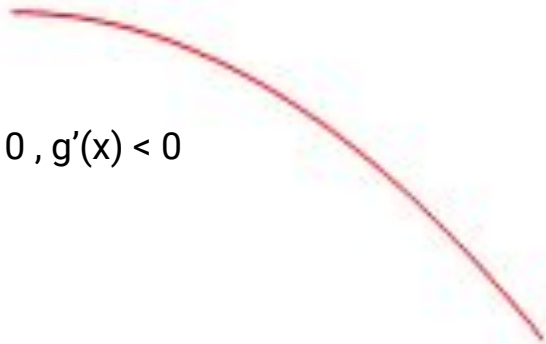
Concave Up, Increasing

$$g''(x) > 0, g'(x) > 0$$



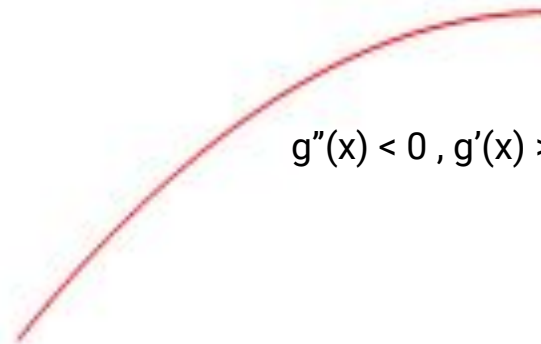
Concave Down, Decreasing

$$g''(x) < 0, g'(x) < 0$$



Concave Down, Increasing

$$g''(x) < 0, g'(x) > 0$$



Connecting this to position and velocity

- Suppose $s(t)$ tells you the position of a moving thing at time t .
- We already know $s'(t)$ tells you **velocity**.
- $s''(t)$ would tell you the *rate of change* in velocity
- What does it look/feel like when you change velocities?
<https://youtu.be/j13qLByE4hw?t=31>
- $s''(t)$ tells you **acceleration**.



Desmos activity: Concavity and the second derivative

Feedback:

<http://gvsu.edu/s/1zJ>