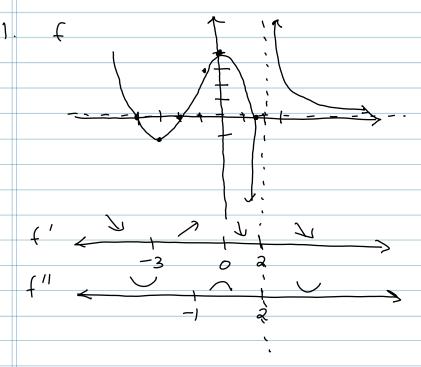
Solus to Exam 3



$$f(x) = 5 x^{2/3} + x^{5/3}$$

(a)
$$f'(x) = \frac{10}{3}x^{-1/3} + \frac{5}{3}x^{2/3}$$

 $0 = \frac{10 + 5x}{3x^{1/3}} \xrightarrow{x=0}$

3.
$$f(x) = \frac{x^5}{20} + \frac{-x^4}{6} + \frac{x^3}{6} + 5x + 1$$

$$f'(x) = \frac{5x^4}{20} - \frac{4x^3}{6} + \frac{3x^2}{6} + 5$$

$$f''(x) = x^3 - \lambda x^2 + x$$

$$0 = x (x^{2} - 2x + 1)$$

$$= x ((x-1)(x-1))$$

$$= x = 1$$

$$f(x) = \frac{5x^3 - 2x^2 - 1}{x^2 - 4}$$

V.a.

$$\times = \pm \lambda$$

hia.

none

curvilinear:

$$y = 5x - \lambda$$

$$x^{2} - y = 5x^{3} - \lambda x^{2} - 1$$

$$-5x^{3} + \lambda 0x$$

$$-\lambda x^{2} + \lambda 0x - 1$$

$$+\lambda x^{2} + \lambda 0x - 1$$

(a)
$$A = xy^{2}$$

$$x+y=24$$

$$y=24-x$$

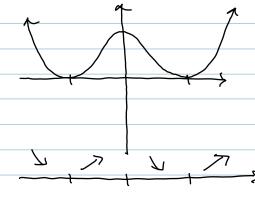
So, A = x (24-x) or 24x-x2

(c)
$$A' = 24 - 2x$$

 $0 = 24 - 2x$
 $x = 12$

2 but not in feasible dom

$$A(14) = 14(24-14) = 140$$
 $\leftarrow larger$
 $A(20) = 20(24-20) = 80$



Ь

7. (a)
$$\int \frac{4 + x^3}{x^4} dx$$

$$= \int 4x^{-d} + x dx$$

$$=\frac{4x^{-1}}{-1}+\frac{x^{2}}{2}+C$$

$$= \sqrt{\frac{-4}{x} + \frac{x^{2}}{2}} + C$$

=
$$\int \sec x + \tan x + \sec^2 x \, dx$$

= $\int \sec x + \tan x + C$

8.
$$\int_{0}^{\pi} \cos^{2} x \, dx$$

$$= \frac{1}{4} \left[\frac{1}{2} + 0 + \frac{1}{2} + \right]$$

9.
$$\int_{0}^{2} x^{k} dx = \lim_{N \to \infty} \sum_{i=1}^{N} f(X_{i}^{*}) \Delta x$$

$$=\lim_{n\to\infty}\sum_{i=1}^{n}\left\{\left(\frac{2i}{n}\right)\cdot\frac{2}{n}\right\}$$

$$=\lim_{n\to\infty}\frac{1}{\sum_{i=1}^{n}\frac{4i^{2}}{n^{2}}}\cdot\frac{2}{n}$$

$$=\lim_{N\to\infty}\frac{8}{N^3}\sum_{i=1}^{N}i\lambda$$

$$=\lim_{N\to\infty}\frac{8}{N^3}\cdot n(N+1)(2n+1)$$

$$=$$
 $\begin{bmatrix} 8\\ 3 \end{bmatrix}$

$$1(x) = x_3$$

$$g(x) = |x|$$

11. (Bonus) Let p(t) be position ton. Then p(t) is cont and diff. By MVT, there exists (E [0,2] s.t.

$$\rho'(c) = \rho(a) - \rho(o)$$

$$=\frac{158-0}{2}$$

So, there was @ least one moment in time (that's () when driver was speeding.