Solution to Exercise 11.2.44

$$S = \int_{0}^{\pi} \sqrt{\left(\frac{dy}{dt}\right)^{2} + \left(\frac{dx}{dt}\right)^{2}} dt$$

$$= \int_0^{\pi} \sqrt{(-3\sin t + 3\sin 3t)^2 + (3\cos t - 3\cos 3t)^2} dt$$

$$= \int_{0}^{\pi} \sqrt{9 \sin^{2} t - 18 \sin^{2} 3t + 9 \cos^{2} t}$$
 dt
$$-18 \cos t \cos 3t + 9 \cos^{2} 3t$$

$$= \int_0^{\pi} \sqrt{18 - 18 \left(\sinh \sin(t+2t) - \cosh \cos(t+2t) \right)} dt$$

=
$$\frac{1}{3\sqrt{2}}\int_{0}^{\pi} \sqrt{1-\sin t \left(\sinh \cos 2t + \cosh \sin 2t \right)} dt$$

 $\frac{1}{3\sqrt{2}}\int_{0}^{\pi} -\cos t \left(\cosh \cos 2t - \sinh t \sinh 2t \right)$

$$= 243$$

$$3\sqrt{2}$$

$$\int_{0}^{\pi} \sqrt{1 - \cos 2t \left(\sin^{2}t + \cos^{2}t \right)} dt$$

$$= 2043 \qquad \left(\begin{array}{c} T \sqrt{1-\cos 2t} & \text{cl} + \\ 3\sqrt{2} & \end{array} \right)$$

$$= 248$$

$$312$$

$$= 243 \cdot 12$$

$$= 246$$

$$= 246$$

$$= -\cos \pi - (-\cos \pi)$$

$$= 246$$

$$= -(-1) + 17$$

$$= -246$$

$$= -246$$

$$= -246$$

$$= -246$$

$$= -(-1) + 17$$

$$= -246$$

$$= -(-1) + 17$$