

## Supplementary Homework Exercises for Section 4.11: Hyperbolic Functions (part 1)

### Exercises

Complete the following exercises.

S1. Prove that  $\sinh(x + y) = \sinh x \cosh y + \cosh x \sinh y$ .

S2. Differentiate each of the following.

(a)  $f(x) = \sinh(x^2)$

(b)  $g(x) = \operatorname{sech}(x) \tanh(x)$

(c)  $y = \sinh^{-1}(2x)$

S3. Integrate each of the following.

(a)  $\int \frac{\sinh x}{\cosh^2 x} dx$

(b)  $\int e^{\tanh x} \operatorname{sech}^2 x dx$

(c)  $\int \frac{\operatorname{sech} \sqrt{x} \tanh \sqrt{x}}{\sqrt{x}} dx$