

Your Name:

Names of Any Collaborators:

Instructions

This portion of Exam 1 is worth a total of 20 points and is due at the beginning of class on **Monday, October 19**. Your total combined score on the in-class portion and take-home portion is worth ??% of your overall grade.

I expect your solutions to be *well-written, neat, and organized*. Do not turn in rough drafts. What you turn in should be the “polished” version of potentially several drafts.

Feel free to type up your final version. The \LaTeX source file of this exam is also available if you are interested in typing up your solutions using \LaTeX . I'll gladly help you do this if you'd like.

The simple rules for the exam are:

1. You may freely use any theorems that we have discussed in class, but you should make it clear where you are using a previous result and which result you are using. For example, if a sentence in your proof follows from Theorem x.yz, then you should say so.
2. Unless you prove them, you cannot use any results from the course notes that we have not yet covered.
3. You are **NOT** allowed to consult external sources when working on the exam. This includes people outside of the class, other textbooks, and online resources.
4. You are **NOT** allowed to copy someone else's work.
5. You are **NOT** allowed to let someone else copy your work.
6. You are allowed to discuss the problems with each other and critique each other's work.

I will vigorously pursue anyone suspected of breaking these rules.

You should **turn in this cover page** and all of the work that you have decided to submit. **Please write your solutions and proofs on your own paper.**

To convince me that you have read and understand the instructions, sign in the box below.

Signature:

Good luck and have fun!

Complete the following tasks. Write your solutions on your own paper and please put the problems in order.

1. (4 points) For Problem 7 on the in-class portion of the exam, you proved one of the following. Now, prove the one you didn't prove.
 - (a) Prove that the group of rigid motions of a tetrahedron is isomorphic to a subgroup of S_4 .
 - (b) Suppose $\phi : G \rightarrow H$ is a group homomorphism. We know that $\ker(\phi) \leq G$. Prove that $N_G(\ker(\phi)) = G$.
2. (4 points) For Problem 9 on the in-class portion of the exam, you proved one of the following. Now, prove the one you didn't prove.
 - (a) Let G be a group and define $\phi : G \rightarrow G$ via $\phi(g) = g^2$ for all $g \in G$. Prove that ϕ is a homomorphism iff G is abelian.
 - (b) Define the group $G = \{z \in \mathbb{C} \mid |z| < \infty\}$ where the operation is ordinary multiplication of complex numbers.* Prove that the function $\psi : G \rightarrow G$ is a surjective homomorphism but not an isomorphism.
3. (4 points each) Prove any **three** of the following.
 - (a)
 - (b)
 - (c)
 - (d)
 - (e)

*You do not need to prove that this is a group. It turns out that G is the torsion subgroup of $\mathbb{C} \setminus \{0\}$.