Supplementary Homework Exercises for Section 11.9: Calculus with Power Series

Exercises

Answer each of the following questions.

S1. Find a power series representation of the given function and determine the corresponding radius and interval of convergence.

(a)
$$f(x) = \frac{3}{1 - x^4}$$

(b)
$$f(x) = \frac{x}{9+x^2}$$

S2. Find a power series representation of the given function and determine the corresponding radius of convergence (you do *not* need to find the interval of convergence). In most cases, you will need to use differentiation or integration of a power series to obtain your answer.

(a)
$$f(x) = \frac{1}{(1+x)^2}$$

(b)
$$f(x) = \ln(1+x)$$

(c)
$$f(x) = \frac{x^3}{(x-2)^2}$$

(d)
$$f(x) = \arctan(x/3)$$