

If  $x$  is an even integer and  $y$  is an odd integer, then  $x + y$  is an odd integer.

If  $x$  is an even integer and  $y$  is any other integer, then  $xy$  is an even integer.

For all integers  $x$  and  $y$ , if  $xy$  is even then either  $x$  is even or  $y$  is even.

If  $x$  and  $y$  are odd integers, then  $x + y$  is an even integer.

For every integer  $n$  (positive, negative, or zero), if  $n$  is an odd integer then  $n^3$  is an odd integer.

For every integer  $n$  (positive, negative, or zero), if  $n$  is a multiple of 4 then  $n^2 - 1$  is a multiple of 4.

For all real numbers  $a$  and  $b$ , if  $a \neq 0$  and  $b \neq 0$  then  $ab \neq 0$ .