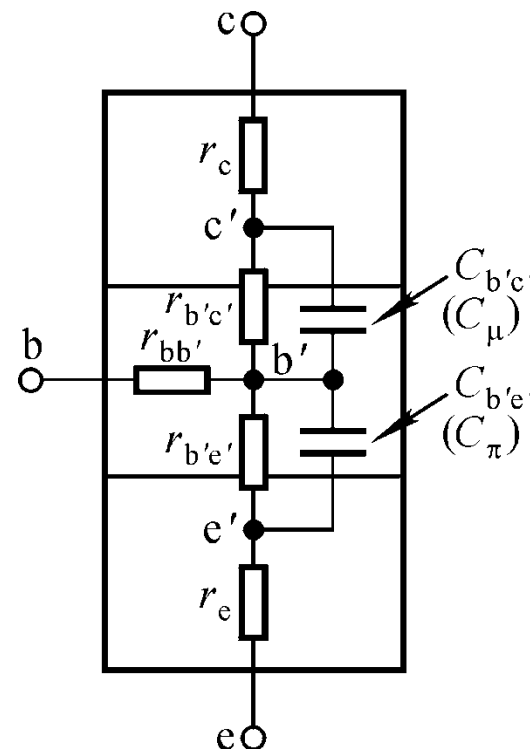
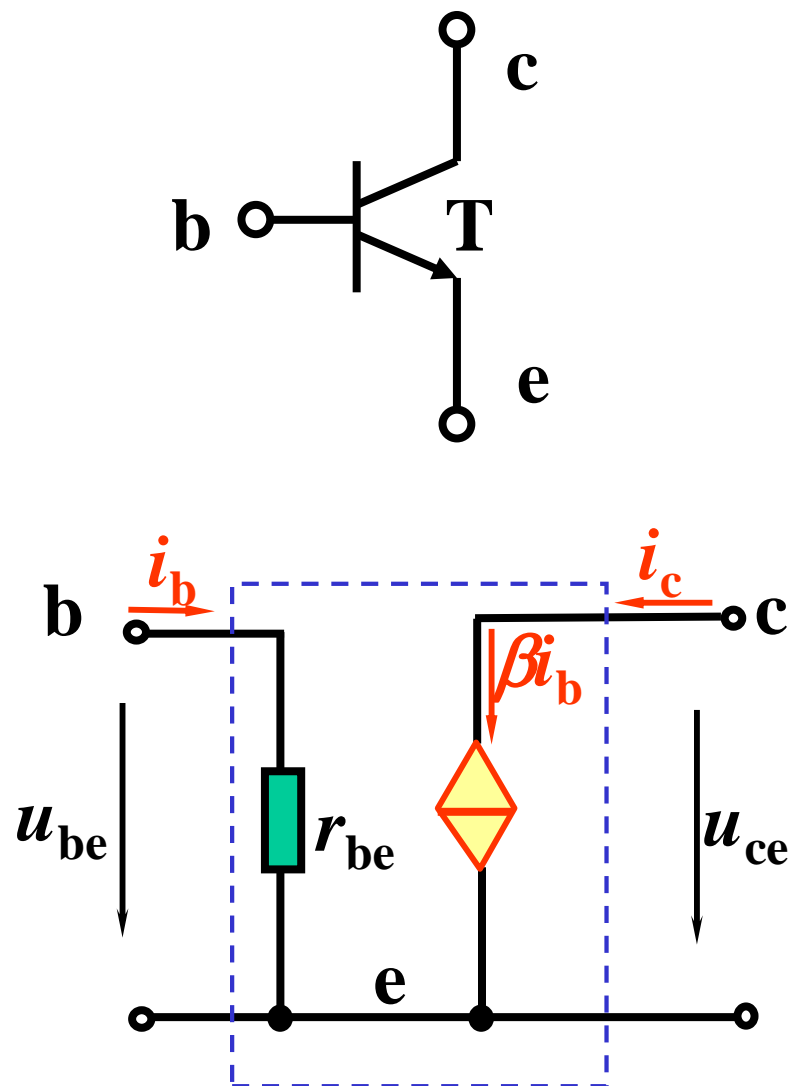
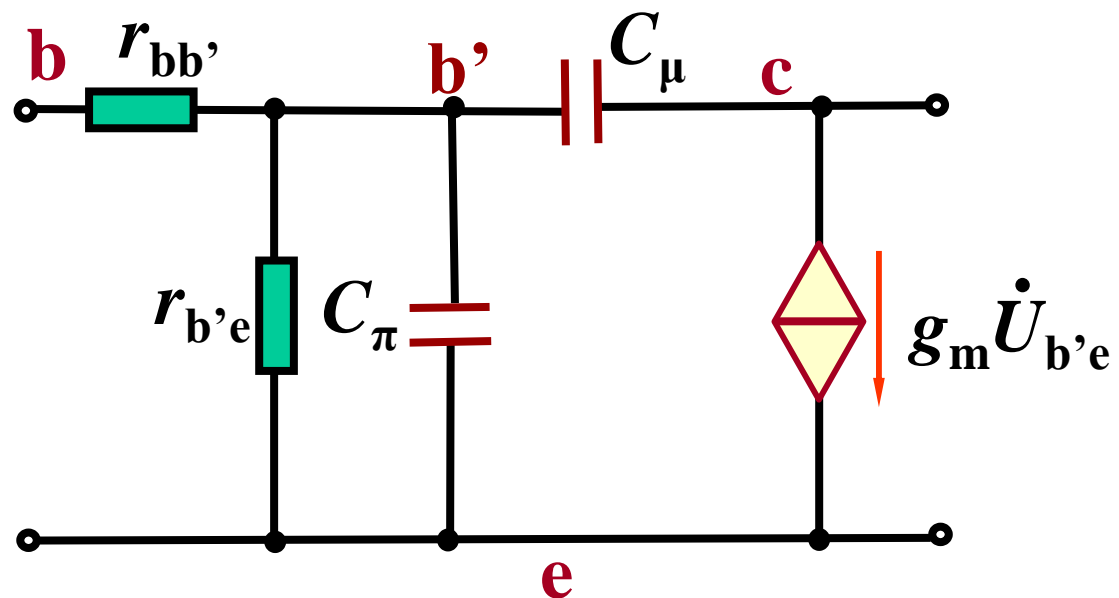
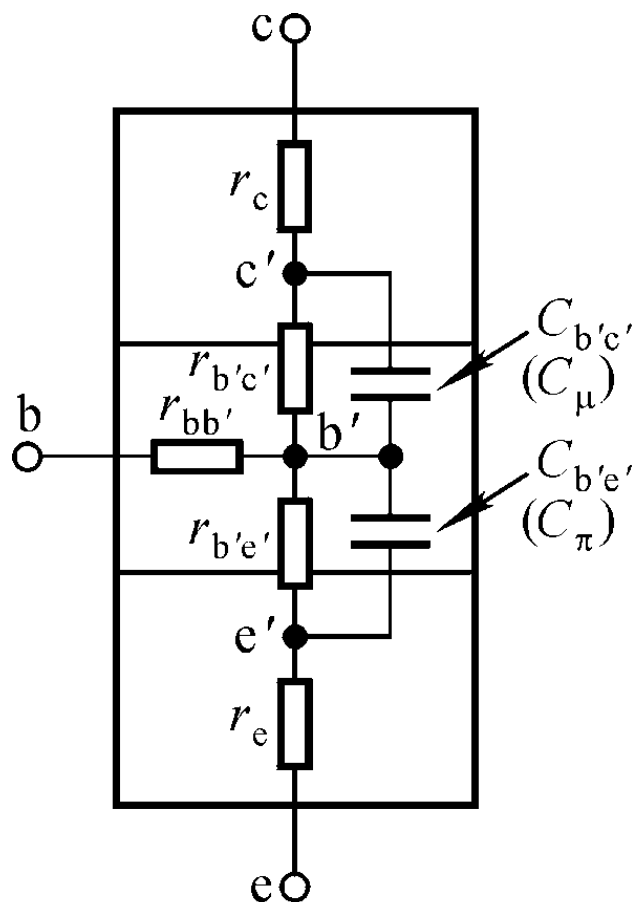


## 4.2 晶体管的高频等效模型



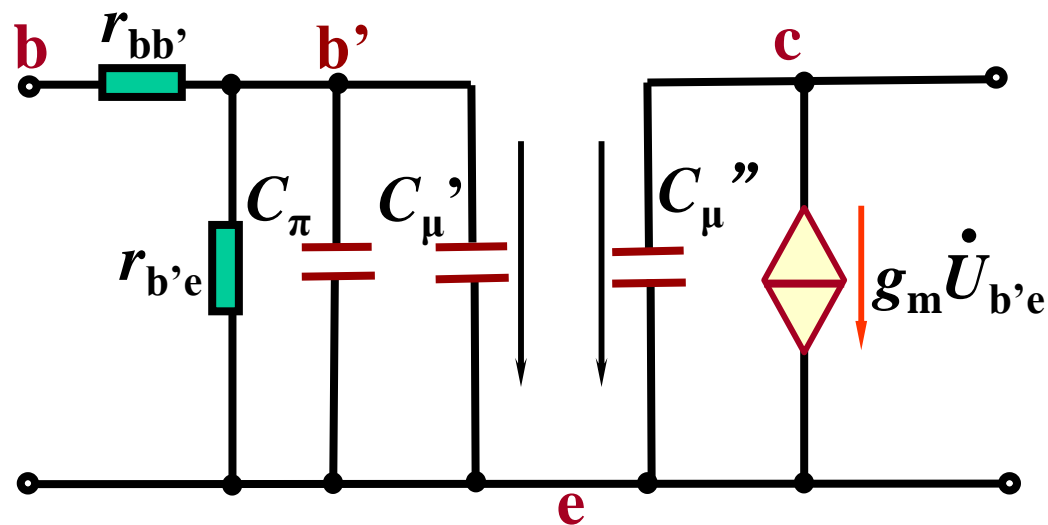
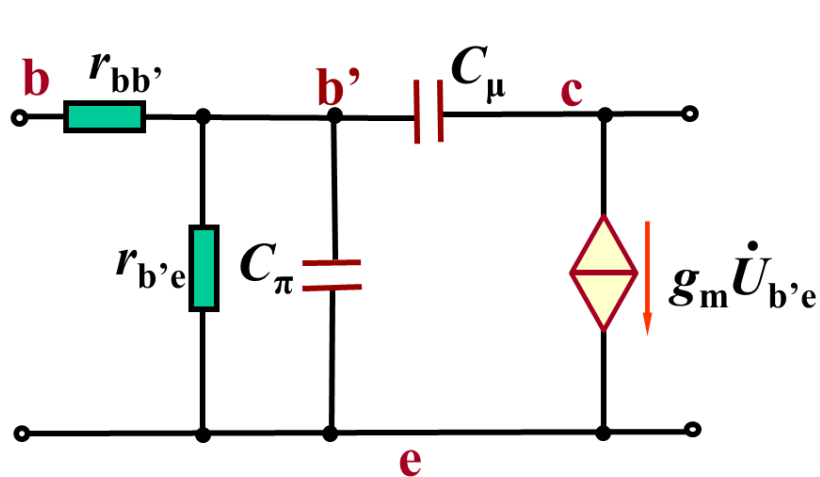
## 4.2 晶体管的高频等效模型



$g_m$ 为跨导，不随信号频率的变化而变化

$$r_{be} = r_{bb'} + (1 + \beta) \frac{U_T}{I_E} = r_{bb'} + r_{b'e}$$

## 4.2 晶体管的高频等效模型



$$\frac{\dot{U}_{b'e}}{1} = \frac{\dot{U}_{b'e} - \dot{U}_{ce}}{1}$$

$$\frac{1}{j\omega C_{\mu}'} = \frac{1}{j\omega C_{\mu}}$$

$$\text{令 } K = \frac{\dot{U}_{ce}}{\dot{U}_{b'e}}$$

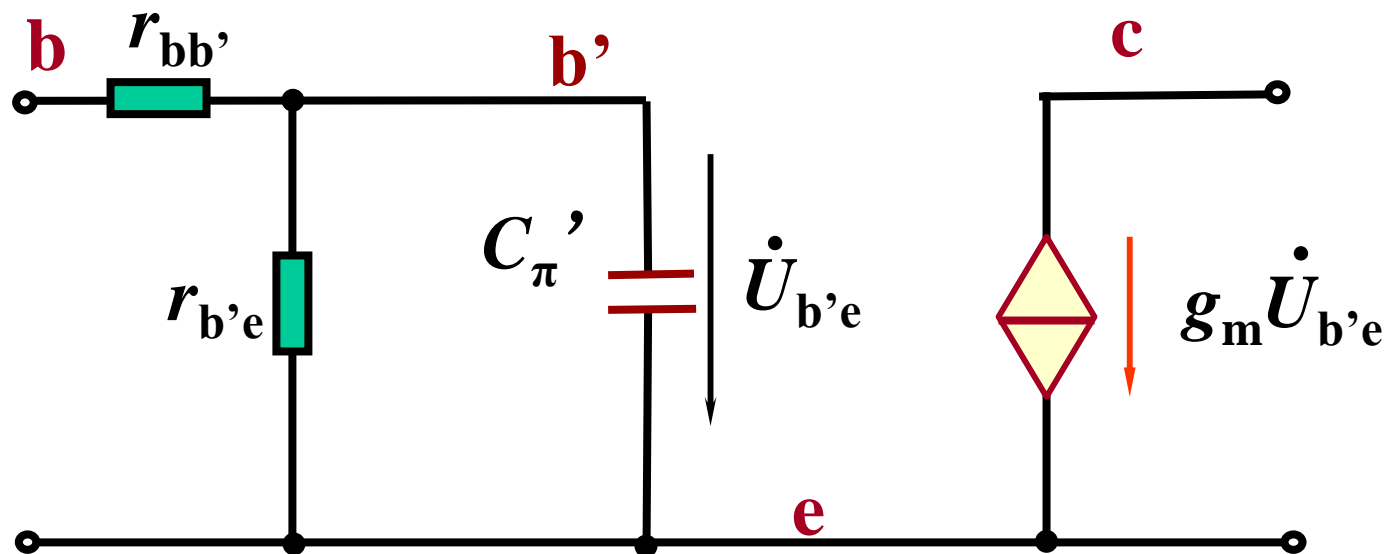
$$C_{\mu}' = (1 - K)C_{\mu} \quad \text{密勒效应}$$

$$C_{\mu}(\dot{U}_{b'e} - \dot{U}_{ce}) = C_{\mu}'\dot{U}_{b'e}$$

$$C_{\mu}'' = \frac{K - 1}{K}C_{\mu} \quad \text{电容小, 容抗大可忽略}$$

## 4.2 晶体管的高频等效模型

### 高频下简化三极管等效电路



$r_{bb'}$  查手册

$$r_{b'e} = (1 + \beta_0) \frac{U_T}{I_{EQ}}$$

$$C_{\pi}' = C_{\pi} + C_{\mu}'$$

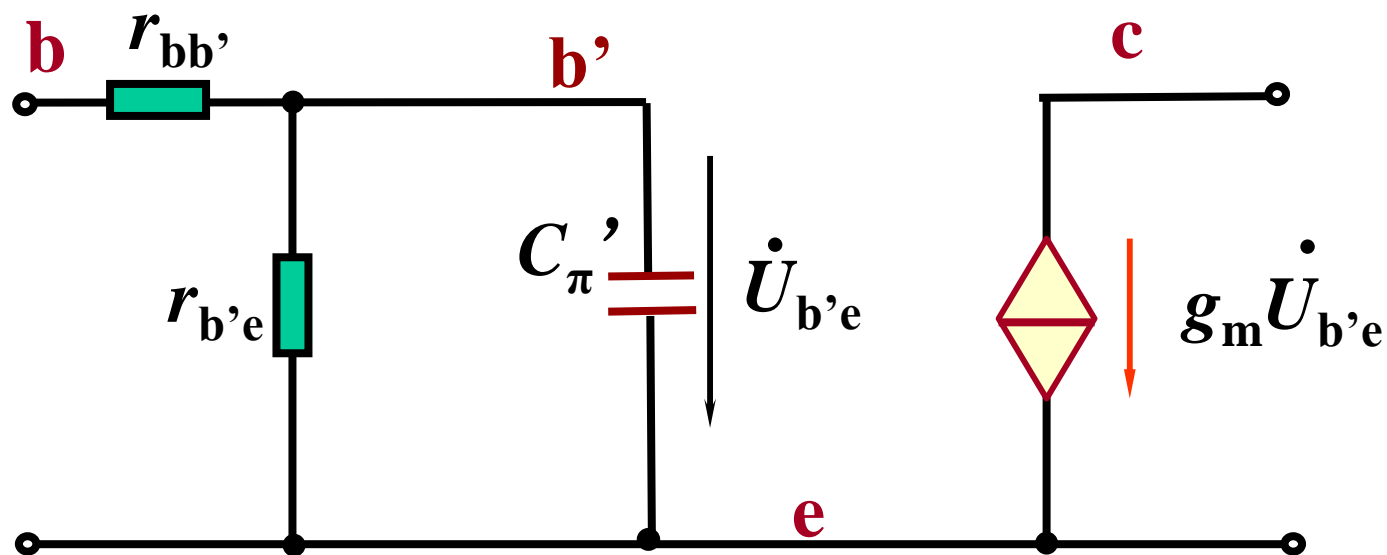
$$C_{\mu}' = (1 - K) C_{\mu}$$

$C_{\mu}$  近似为  $C_{Ob}$ : 查手册

$C_{\pi}, g_m$  ?

## 4.2 晶体管的高频等效模型

$g_m$  的求解

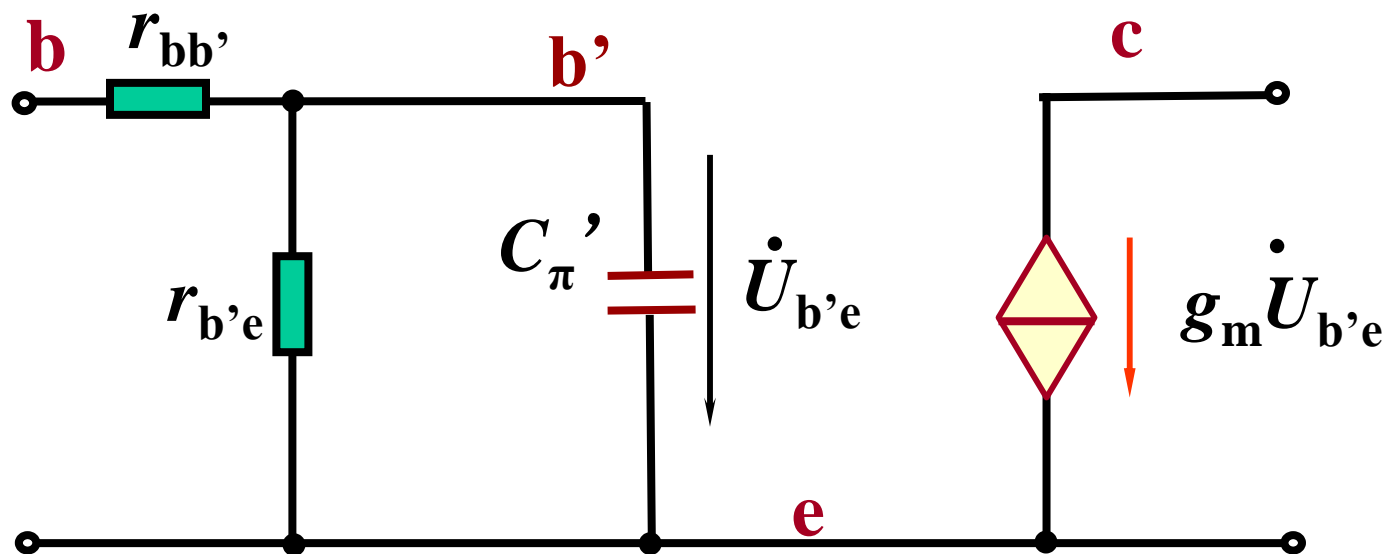


低频段  $\beta_0 \dot{I}_b = g_m \dot{U}_{b'e}$

$$g_m = \beta_0 \frac{\dot{I}_b}{\dot{U}_{b'e}} = \beta_0 \frac{1}{r_{b'e}} = \frac{\beta_0}{(1 + \beta_0) \frac{U_T}{I_E}} \approx \frac{I_E}{U_T}$$

## 4.2 晶体管的高频等效模型

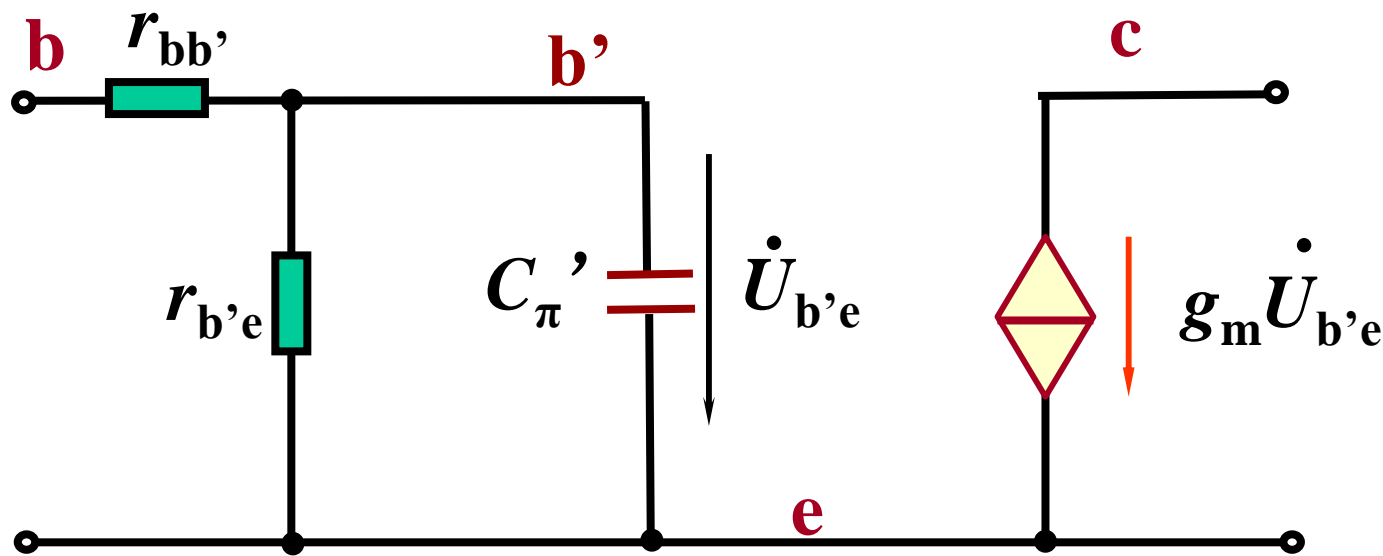
$C_\pi$  的求解



高频段 求  $\beta(f)$  , 然后求  $C_\pi$

根据定义  $\beta(f) = \frac{\dot{I}_c}{\dot{I}_b} \bigg|_{U_{CE}=\text{常数}} \Rightarrow \dot{U}_{ce}=0$

## 4.2 晶体管的高频等效模型



$$\beta(f) = \frac{\dot{I}_c}{\dot{I}_b} = \frac{g_m \dot{U}_{b'e}}{\frac{\dot{U}_{b'e}}{r_{b'e}} + \frac{\dot{U}_{b'e}}{\frac{1}{j\omega C_{\pi}'}}} = \frac{g_m r_{b'e}}{1 + j\omega r_{b'e} C_{\pi}'} = \frac{\beta_0}{1 + j\omega r_{b'e} C_{\pi}'}$$

令

$$f_{\beta} = \frac{1}{2\pi r_{b'e} C_{\pi}'}, \quad \beta(f) = \frac{\beta_0}{1 + j\omega r_{b'e} C_{\pi}'} = \frac{\beta_0}{1 + j\frac{\omega}{\omega_{\beta}}} = \frac{\beta_0}{1 + j\frac{f}{f_{\beta}}}$$

## 4.2 晶体管的高频等效模型

$$\beta(f) = \frac{\beta_0}{1 + j \frac{f}{f_\beta}}$$

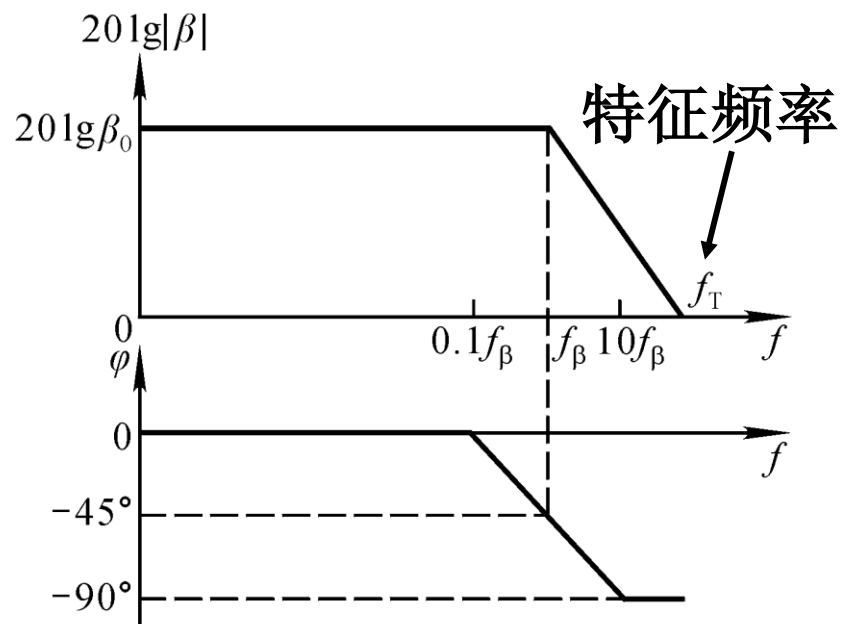
$$f_\beta = \frac{1}{2\pi r_{be} C_\pi} \quad \text{共射截止频率 手册}$$

当  $f=0$  时  $\beta = \beta_0$   $\varphi=0$

当  $f = f_\beta$  时

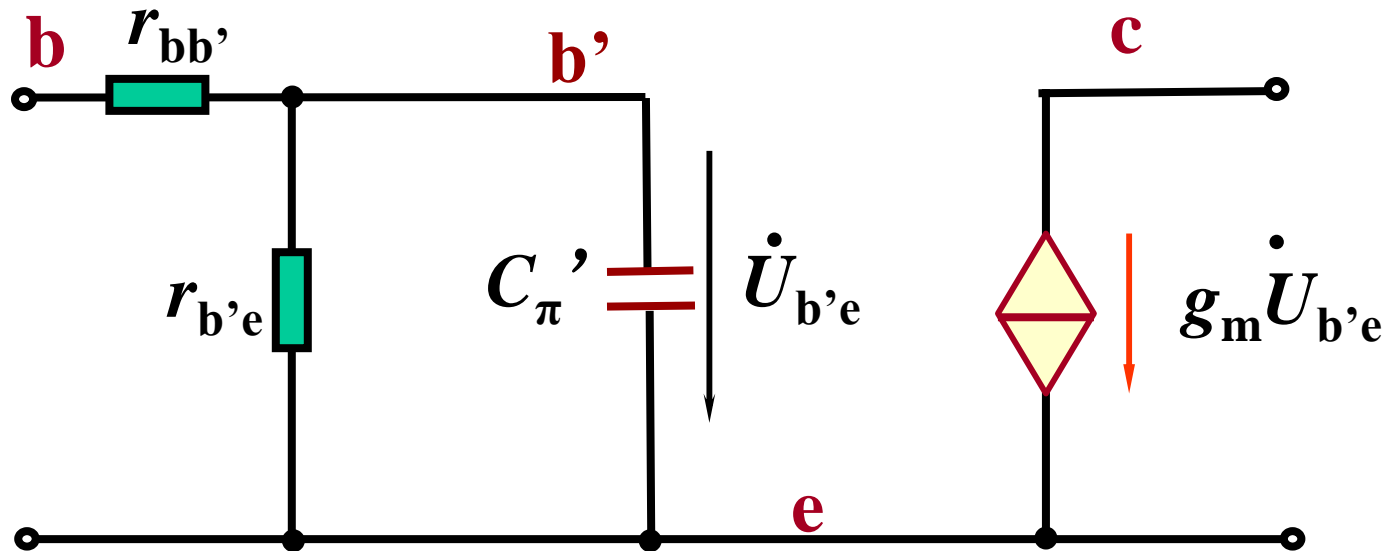
$$\beta = \frac{1}{\sqrt{2}} \beta_0 \approx 0.707 \beta_0 \quad \varphi = 45^\circ$$

当  $f \gg f_\beta$  时  $\beta \rightarrow 0$   $\varphi \rightarrow 90^\circ$





## 4.2 晶体管的高频等效模型



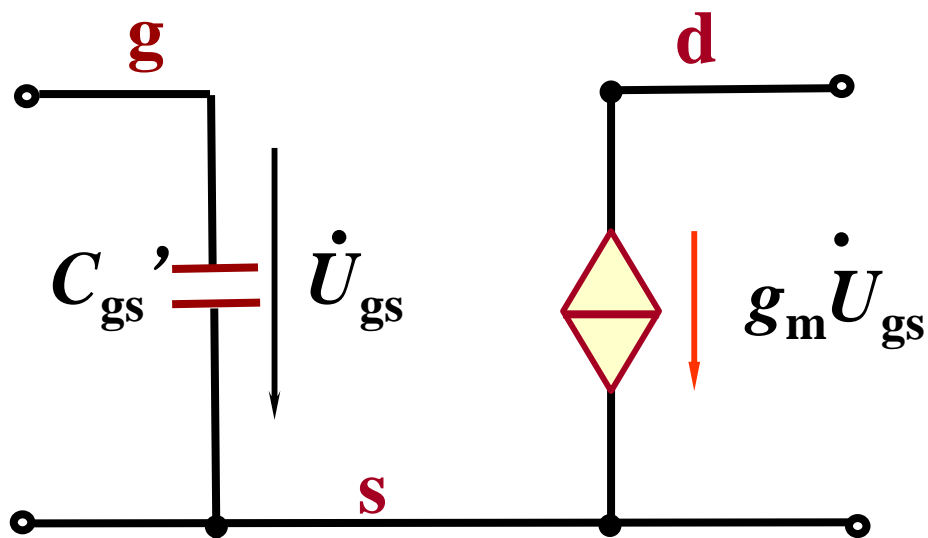
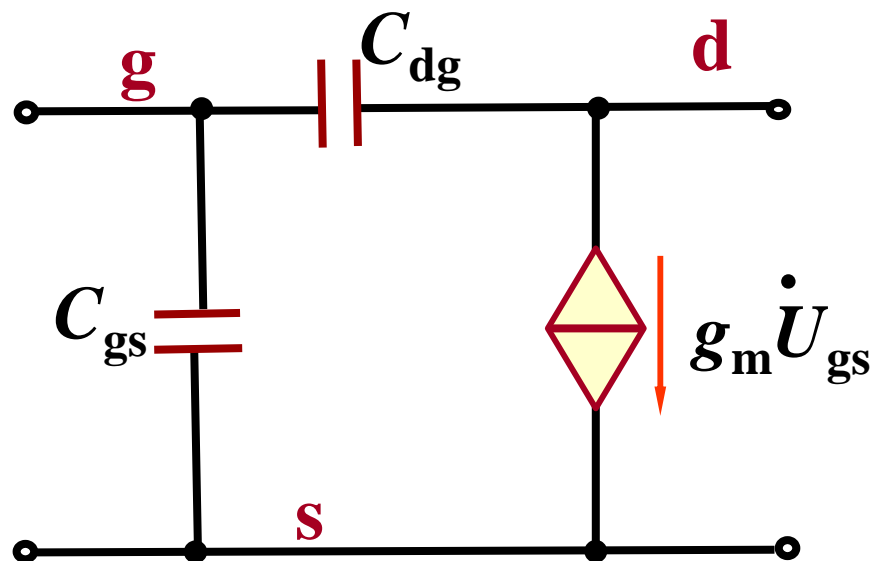
$$f_{\beta} = \frac{1}{2\pi r_{b'e} C_{\pi}'}$$

$$C_{\pi}' = C_{\pi} + C_{\mu}'$$

$$C_{\mu}' = C_{\mu} (1 - K) \quad K = \frac{\dot{U}_{ce}}{\dot{U}_{b'e}} \quad \dot{U}_{ce} = 0 \Rightarrow K = 0 \Rightarrow C_{\mu}' = C_{\mu}$$

$$f_{\beta} = \frac{1}{2\pi r_{b'e} (C_{\pi} + C_{\mu})}$$

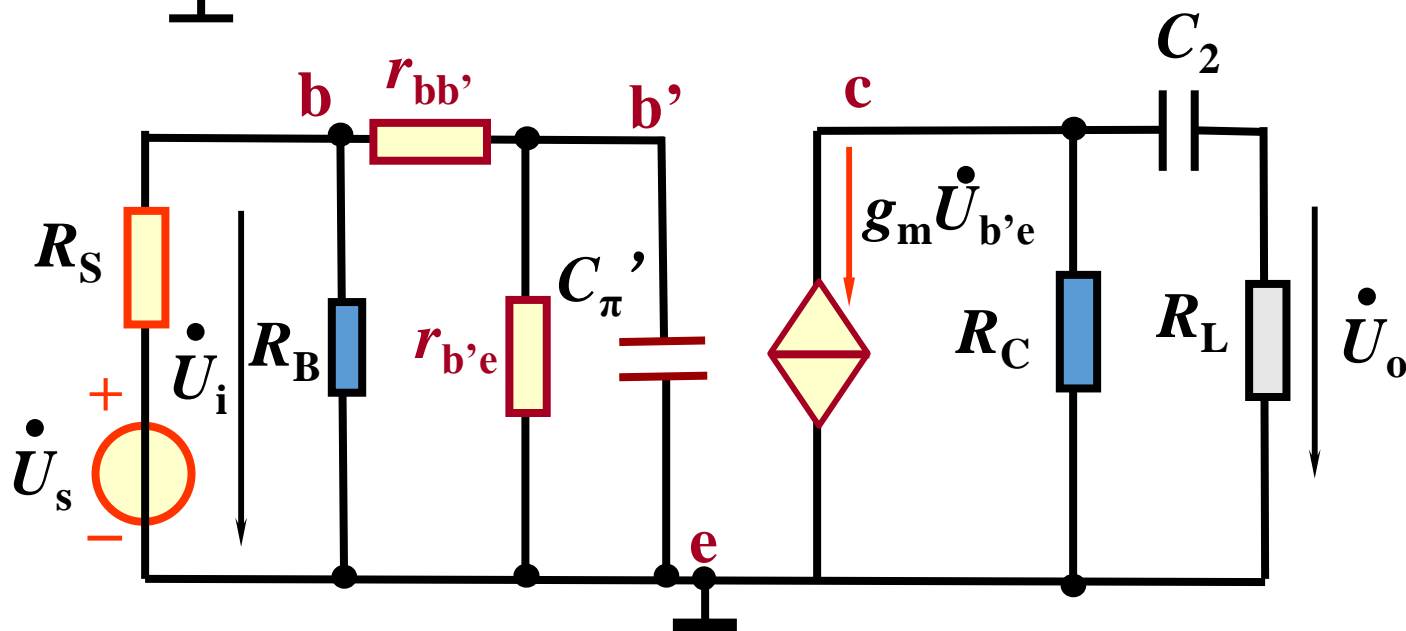
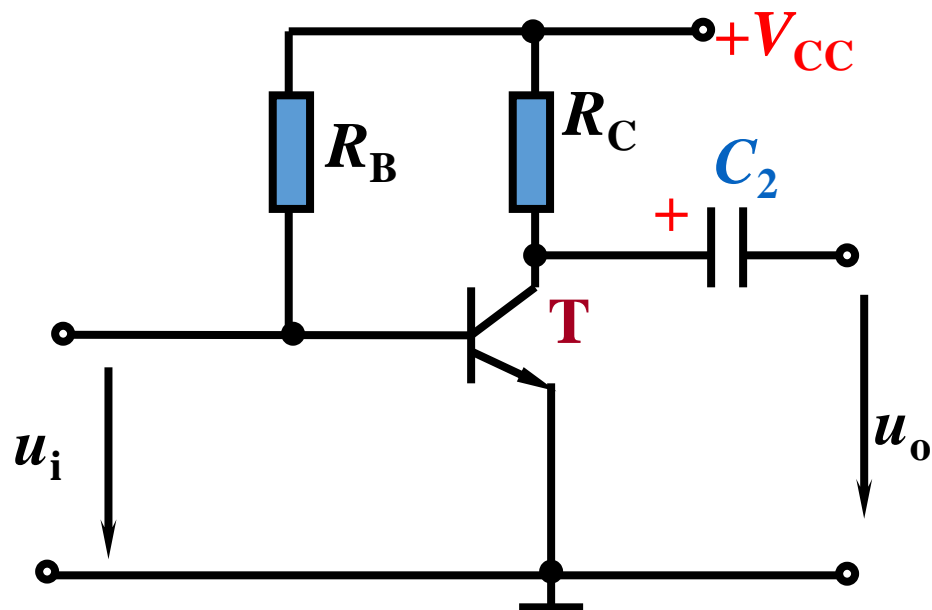
## 4.3 场效应管的高频等效模型



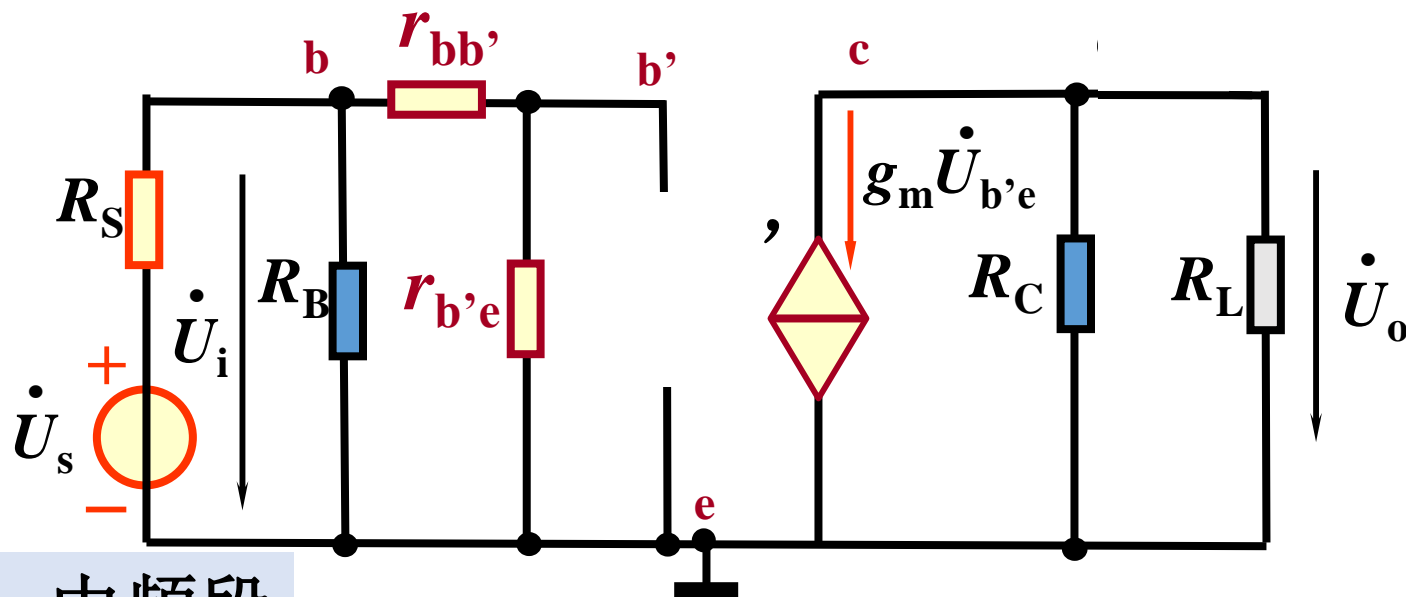
$$K \approx -g_m R_L'$$

$$C_{gs}' = C_{gs} + (1 - K)C_{gd}$$

## 4.4 单管放大电路的频率响应



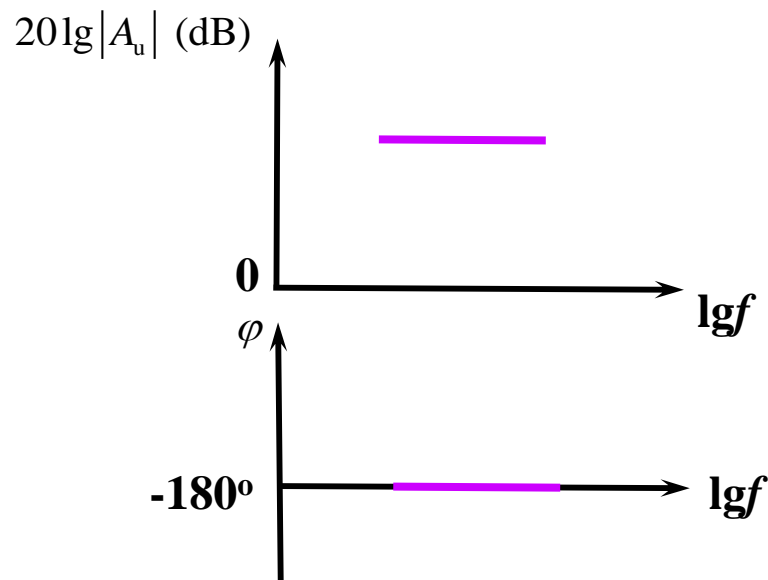
# 4.4 单管放大电路的频率响应



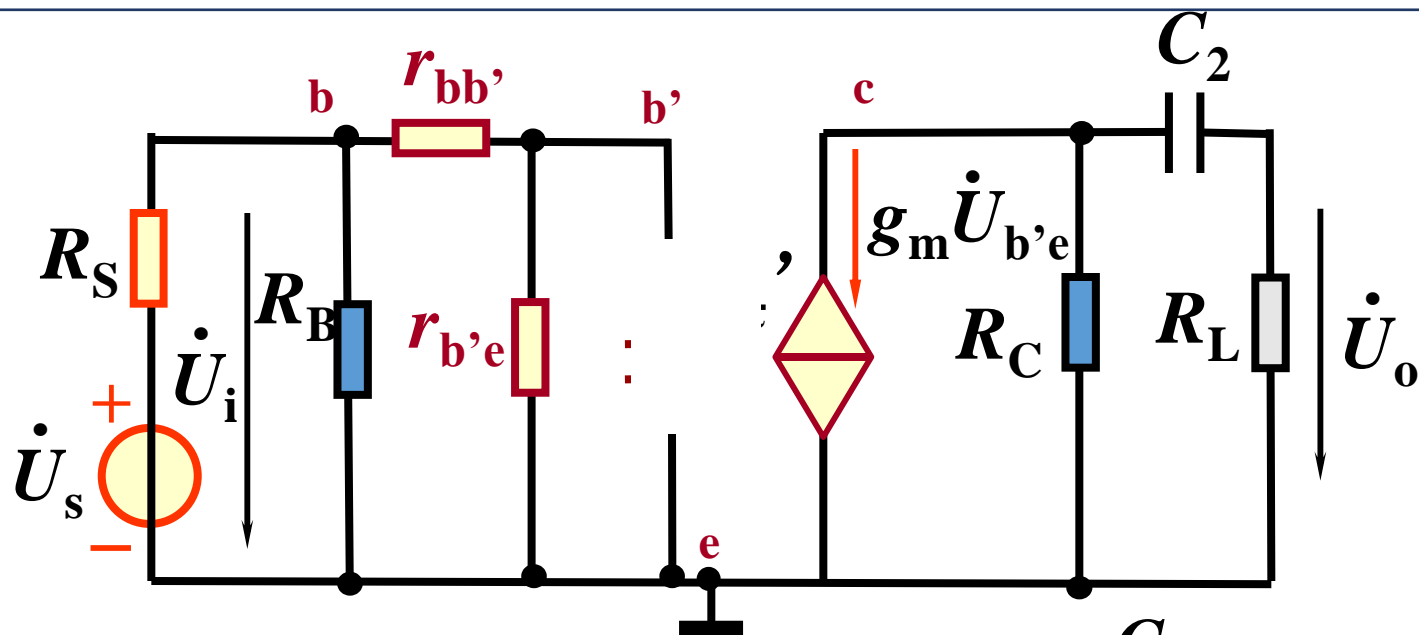
## 一、中频段

$$A_{um} = \frac{\dot{U}_o}{\dot{U}_i} = \frac{-g_m \dot{U}_{b'e} (R_C // R_L)}{\dot{U}_{b'e} \left( \frac{r_{be}}{r_{b'e}} \right)}$$

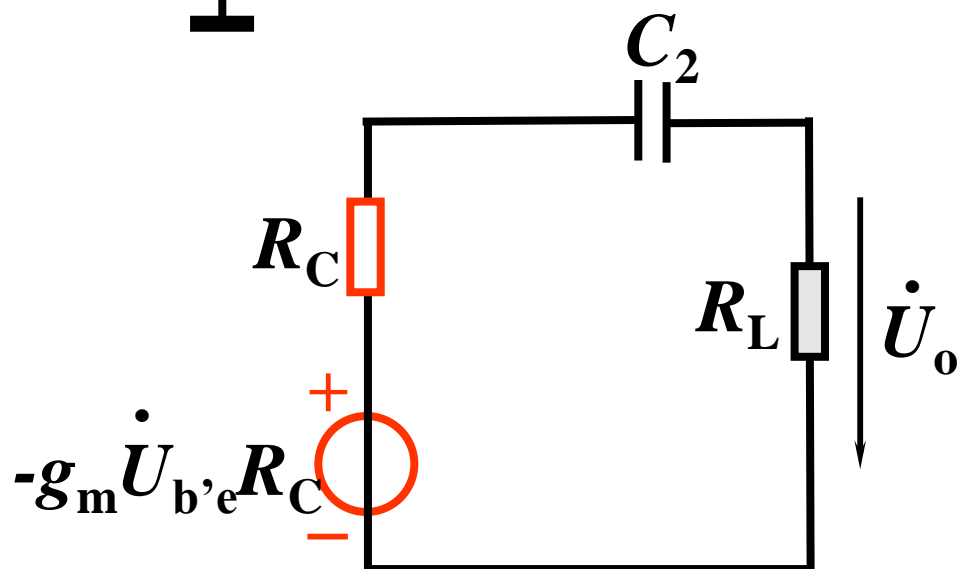
$$= -g_m \frac{r_{b'e} R_C // R_L}{r_{be}} = -\beta_0 \frac{R_C // R_L}{r_{be}}$$



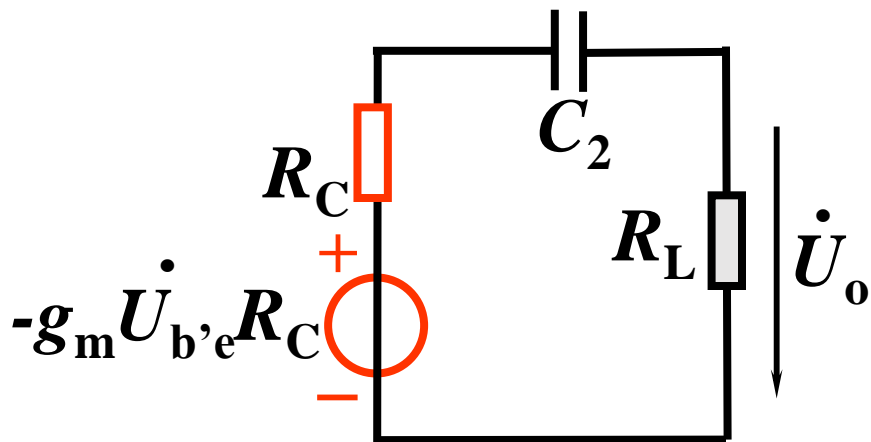
# 4.4 单管放大电路的频率响应



## 二、低频段



# 4.4 单管放大电路的频率响应



$$\begin{aligned}\dot{U}_o &= -g_m \dot{U}_{b'e} R_C \frac{R_L}{R_C + R_L + \frac{1}{j\omega C_2}} \\ &= -g_m \frac{r_{be}}{r_{be}} \frac{R_C R_L}{R_C + R_L + \frac{1}{j\omega C_2}} \dot{U}_i \\ &= -g_m \frac{r_{be}}{r_{be}} \frac{R_C // R_L}{1 + \frac{1}{j\omega C_2 (R_C + R_L)}} \dot{U}_i\end{aligned}$$

$$A_{uL} = -g_m \frac{r_{be}}{r_{be}} \frac{R_C // R_L}{1 + \frac{1}{j\omega C_2 (R_C + R_L)}}$$

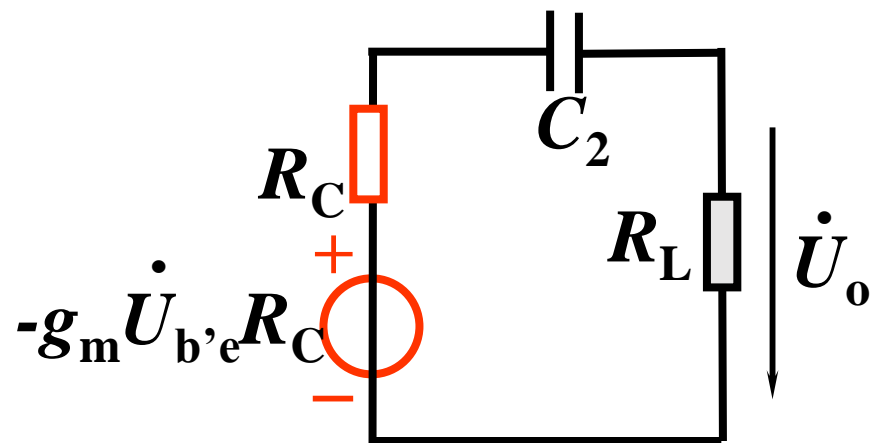
$$A_{um} = \frac{\dot{U}_o}{\dot{U}_i} = -g_m \frac{r_{be}}{r_{be}} \frac{R_C // R_L}{1}$$

$$A_{uL} = \frac{A_{um}}{1 + \frac{1}{j\omega C_2 (R_C + R_L)}}$$

$$\text{令 } f_L = \frac{1}{2\pi (R_C + R_L) C_2}$$

$$A_{uL} = A_{um} \bullet \frac{j \frac{f}{f_L}}{1 + j \frac{f}{f_L}}$$

# 4.4 单管放大电路的频率响应



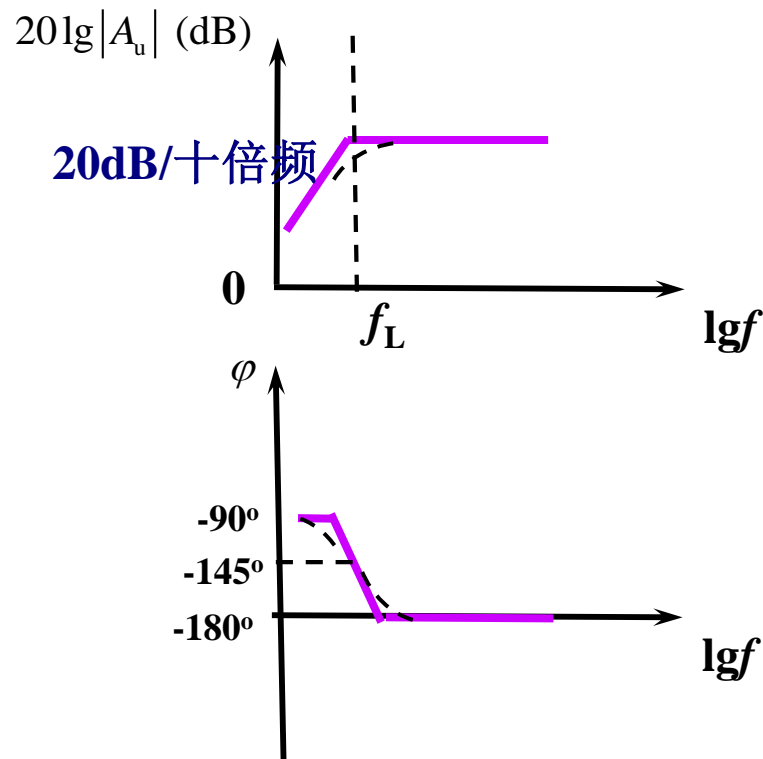
$$A_{uL} = A_{um} \cdot \frac{j \frac{f}{f_L}}{1 + j \frac{f}{f_L}}$$

$$f_L = \frac{1}{2\pi(R_C + R_L)C_2}$$

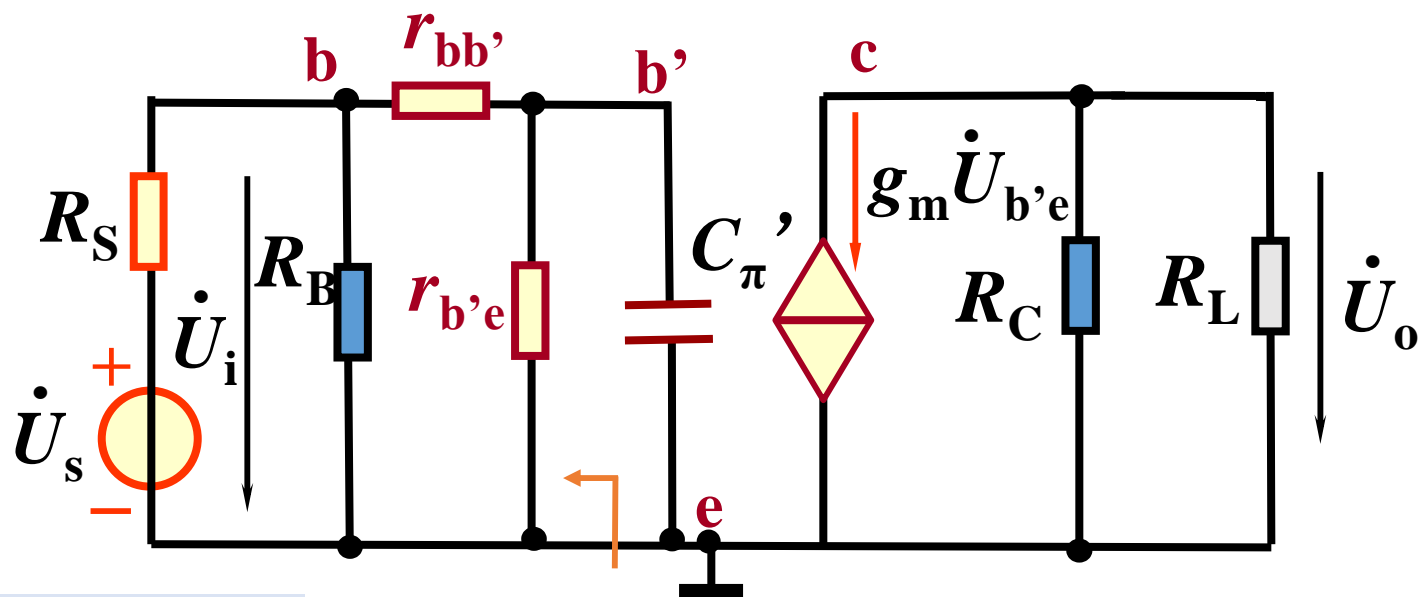
$$|A_{uL}| = |A_{um}| \cdot \frac{\frac{f}{f_L}}{\sqrt{1 + (\frac{f}{f_L})^2}}$$

$$\varphi = -180^\circ + 90^\circ - \arctg \frac{f}{f_L}$$

附加相移

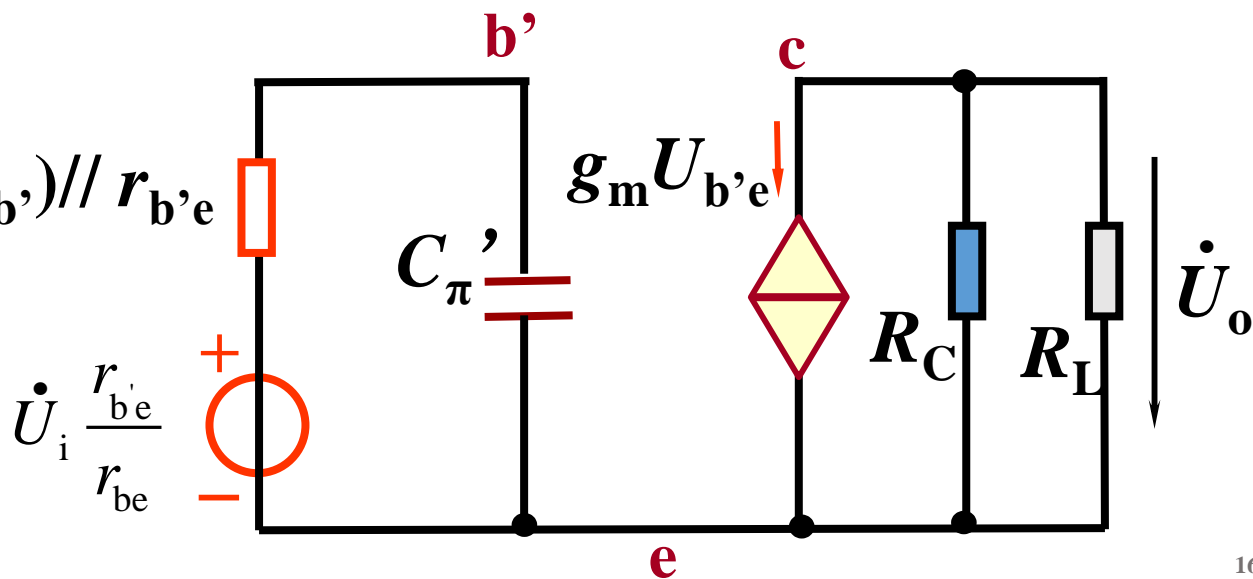


# 4.4 单管放大电路的频率响应



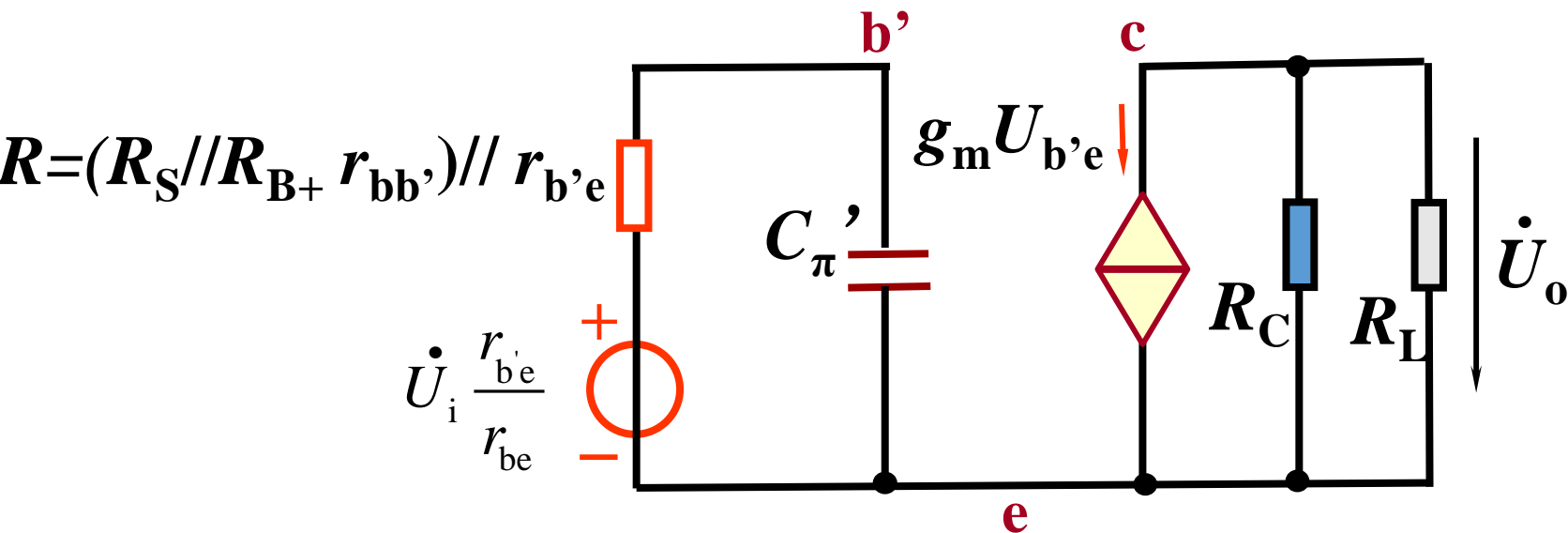
## 三、高频段

$$R = (R_S // R_{B+} r_{bb'}) // r_{b'e}$$





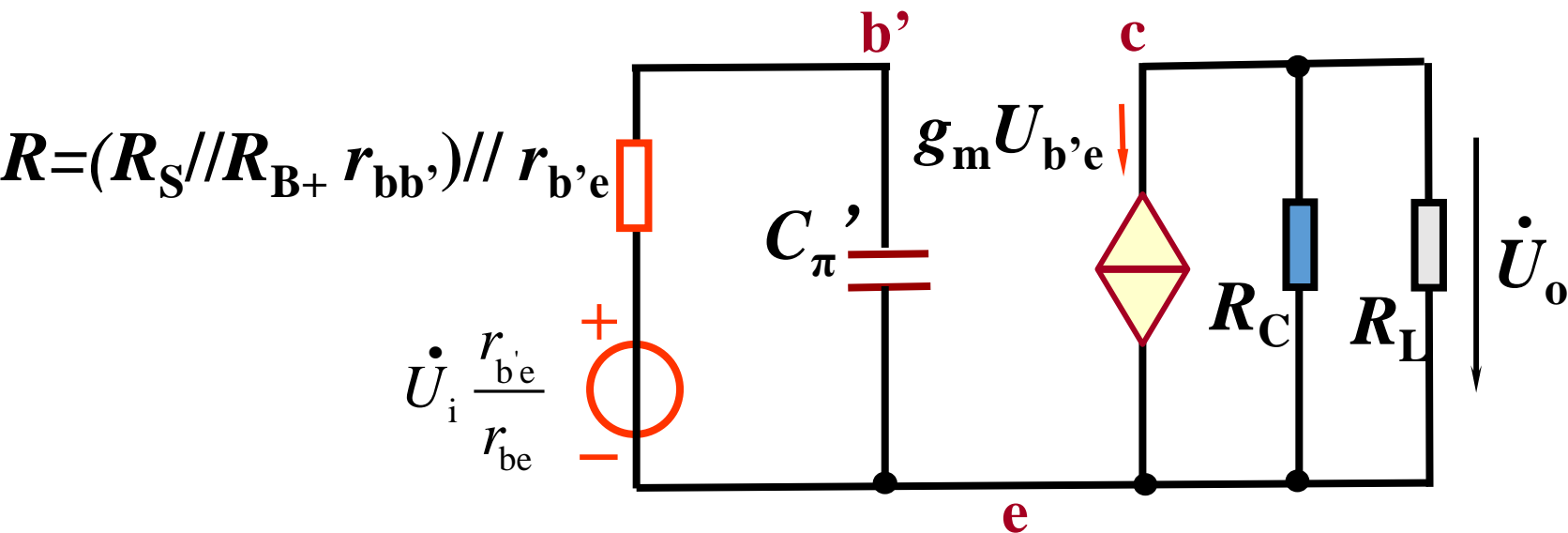
# 4.4 单管放大电路的频率响应



$$\dot{U}_o = -g_m \dot{U}_{b'e} (R_C // R_L):$$

$$A_{uH} = \frac{\dot{U}_o}{\dot{U}_i} = -g_m \frac{r_{b'e}}{r_{be}} \cdot \frac{1}{R + \frac{1}{j\omega C_{\pi}'}} \cdot (R_C // R_L)$$

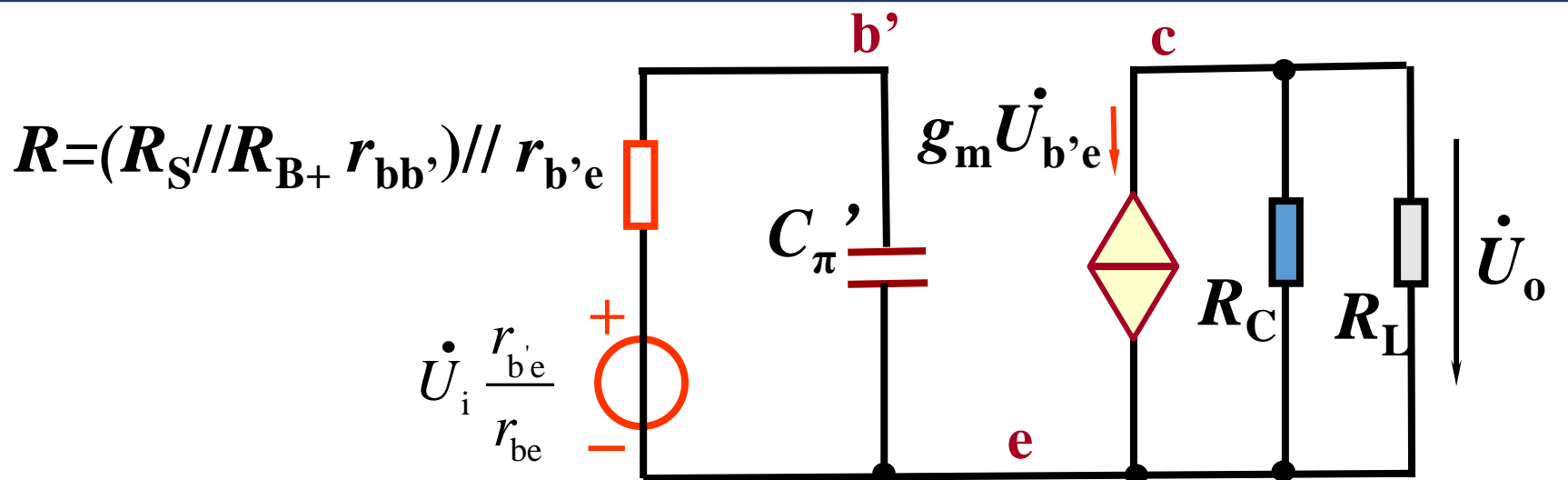
# 4.4 单管放大电路的频率响应



$$A_{uH} = \frac{\dot{U}_o}{\dot{U}_i} = -g_m \frac{r_{b'e}}{r_{be}} \cdot \frac{1}{R + \frac{1}{j\omega C_{\pi}'}} \cdot (R_C // R_L) \quad \text{令} \quad f_H = \frac{1}{2\pi R C_{\pi}'}$$

$$A_{uH} = \frac{\dot{U}_o}{\dot{U}_i} = A_{um} \frac{1}{1 + j\omega R C_{\pi}'} = A_{um} \frac{1}{1 + j \frac{f}{f_H}}$$

# 4.4 单管放大电路的频率响应

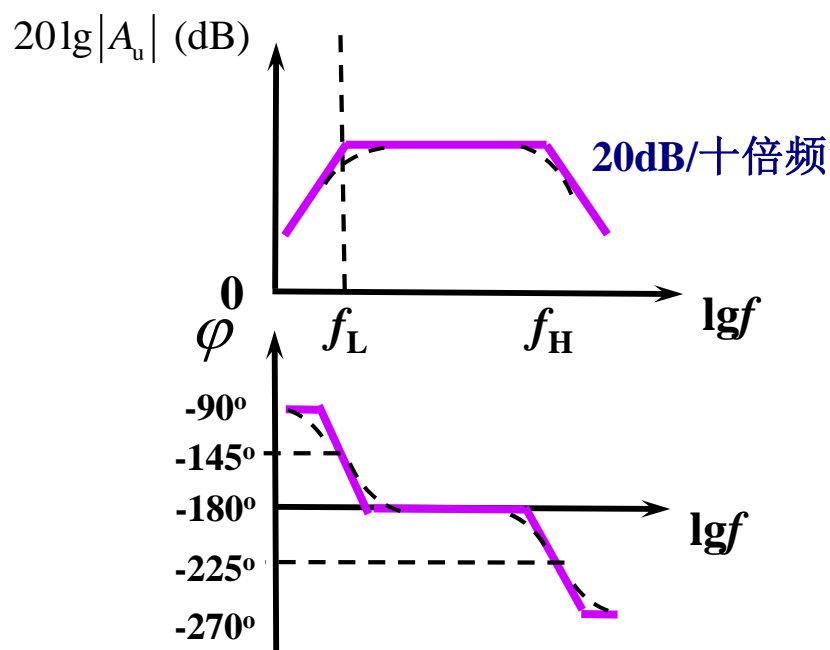


$$A_{uH} = \frac{\dot{U}_o}{\dot{U}_i} = A_{um} \frac{1}{1 + j \frac{f}{f_H}}$$

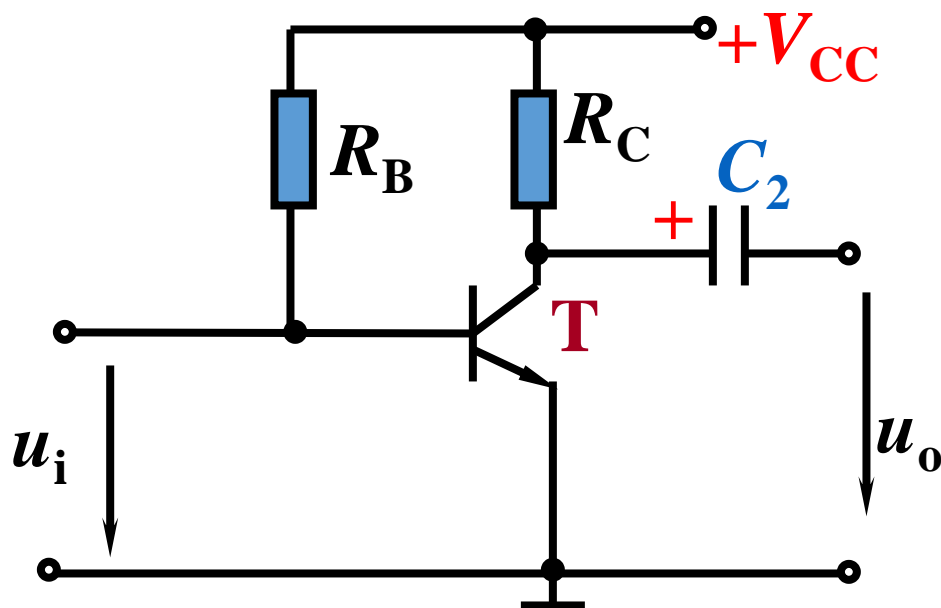
$$f_H = \frac{1}{2\pi R C_{\pi}'}$$

$$\varphi = -180^\circ - \arctg \frac{f}{f_L}$$

附加相移



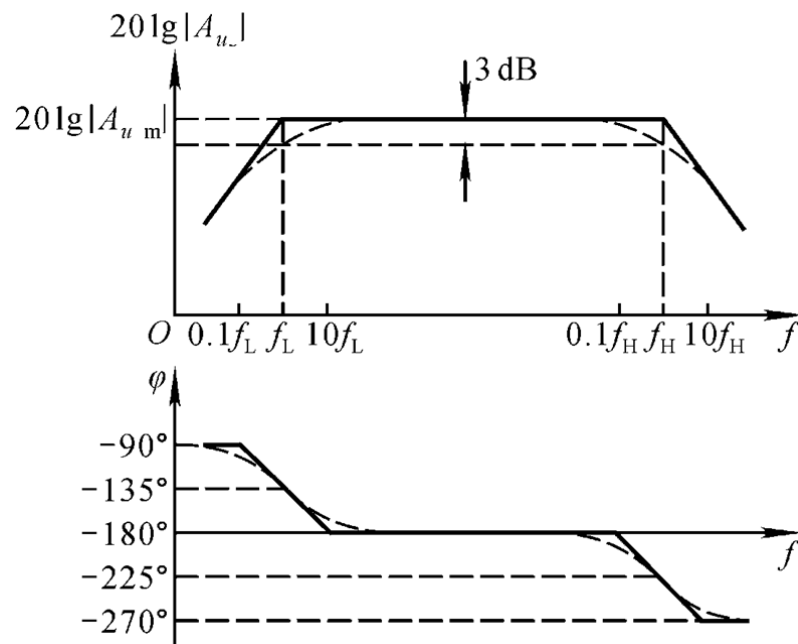
# 4.4 单管放大电路的频率响应



外加耦合电容影响  
低频特性，极间电  
容影响高频特性

$$f_H = \frac{1}{2\pi R C_{\pi}}, \quad f_L = \frac{1}{2\pi (R_C + R_L) C_2}$$

$$f_{BW} = f_H - f_L$$



# 4.4 单管放大电路的频率响应

## 全频段放大倍数

$$A_u = \frac{\dot{U}_o}{\dot{U}_i}$$
$$= A_{um} \frac{j \frac{f}{f_L}}{(1 + j \frac{f}{f_L})(1 + j \frac{f}{f_H})}$$

