

数学作业纸

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第1-1次作业

1-1 瞬时:
解: ① $\sin(\omega t + \beta z) = \cos(\omega t + \beta z - \frac{\pi}{2})$

复振幅:

$$\dot{U}(z) = e^{j\beta z - j\frac{\pi}{2}}$$

② 瞬时:

$$\sin \beta z \sin \omega t = -\frac{1}{2} [\cos(\beta z + \omega t) - \cos(\beta z - \omega t)]$$

复振幅:

$$\dot{U}(z) = -\frac{1}{2} [e^{j\beta z} - e^{-j\beta z}]$$

③ 瞬时:

$$e^{-\alpha z} \cos(\omega t - \beta z)$$

复振幅

$$\dot{U}(z) = e^{-\alpha z} \cdot e^{-j\beta z}$$

④ 瞬时:

$$\vec{E}(z, t) = \vec{E}_R \cos \omega t - \vec{E}_I \sin \omega t$$

$$\vec{E} = \vec{E}_R + j\vec{E}_I$$

1-2

解: ① $\dot{U}(z) = (1+j)e^{j\beta z}$

$$u(z, t) = \cos(\omega t + \beta z) - \sin(\omega t + \beta z)$$

$$\textcircled{2} \dot{U}(z) = j \sin \beta z$$

$$= \frac{1}{2} (e^{j\beta z} - e^{-j\beta z})$$

$$= \frac{1}{2} [\cos(\omega t + \beta z) - \cos(\beta z - \omega t)]$$

$$\textcircled{3} \dot{U}(z) = e^{\alpha z} e^{j\beta z}$$

$$u(z, t) = e^{\alpha z} \cdot \cos(\omega t + \beta z)$$

$$\textcircled{4} \vec{E} = \hat{i}_x (5+3j) + \hat{i}_y (2+3j)$$

$$(5\hat{i}_x + 2\hat{i}_y) \cos \omega t + j(3\hat{i}_x + 3\hat{i}_y) \sin \omega t$$

$$(5\hat{i}_x + 2\hat{i}_y) \cos \omega t - (3\hat{i}_x + 3\hat{i}_y) \sin \omega t$$

1-3

$$\textcircled{1} \text{角: } \vec{E} = (\hat{i}_x + \hat{i}_z) E_0 \cos(\omega t + \beta y)$$

$$\vec{E} = (\hat{i}_x + \hat{i}_z) E_0 \cos(\omega t + \beta y)$$

$$\vec{E} = (\hat{i}_x + \hat{i}_z) E_0 e^{j\beta y}$$

传播方向: -y 方向



$$\vec{H} = \frac{1}{\eta_0} \hat{i}_k \times \vec{E}$$

$$= \frac{E_0}{\eta_0} (\hat{i}_z - \hat{i}_x) e^{j\beta y}$$

线极化波.

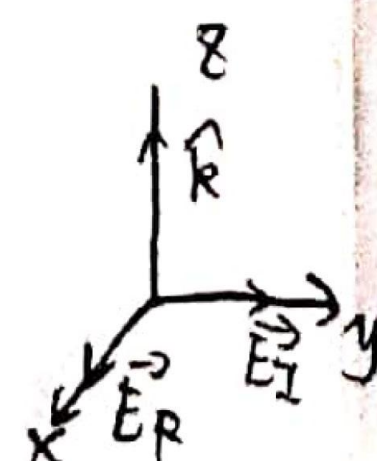
$$\textcircled{2} \text{解: } \vec{E} = \hat{i}_x E_0 \cos(\omega t - \beta z) - \hat{i}_y E_0 \sin(\omega t - \beta z)$$

$$\vec{E} = (\hat{i}_x + j\hat{i}_y) E_0 e^{-j\beta z}$$

传播方向: +z 方向

$$\vec{H} = \frac{1}{\eta_0} (-\hat{i}_z) \times \vec{E}$$

$$= \frac{E_0}{\eta_0} (\hat{i}_y - j\hat{i}_x) e^{-j\beta z}$$



左旋

$$|\vec{E}_R| = |\vec{E}_I| \quad \vec{E}_R \cdot \vec{E}_I = 0$$

左旋圆极波



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