

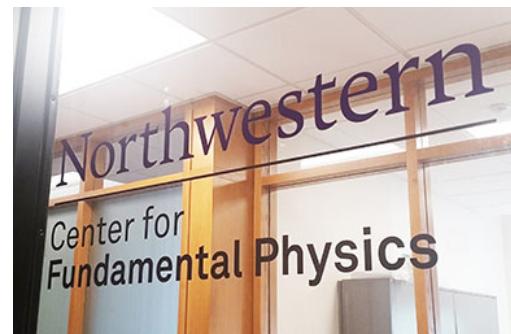
ZOMBIES: an experiment to measure nuclear anapole moments

(and more)

- Nuclear anapole moment and hadronic parity violation
- Nuclear spin-dependent parity violation (NSD-PV) in atoms & molecules:
nuclear anapole moment + semi-leptonic
- ZOMBIES approach using amplified NSD-PV effect in molecules
- Proof of principle with ^{19}F in BaF molecules
- Outlook

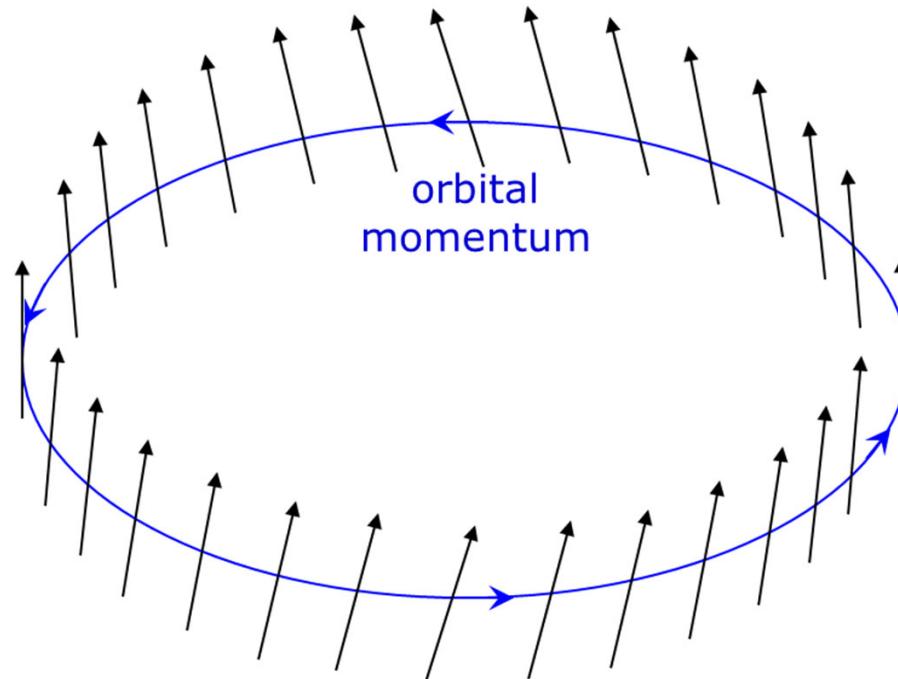
Dave DeMille

University of Chicago & Argonne National Laboratory



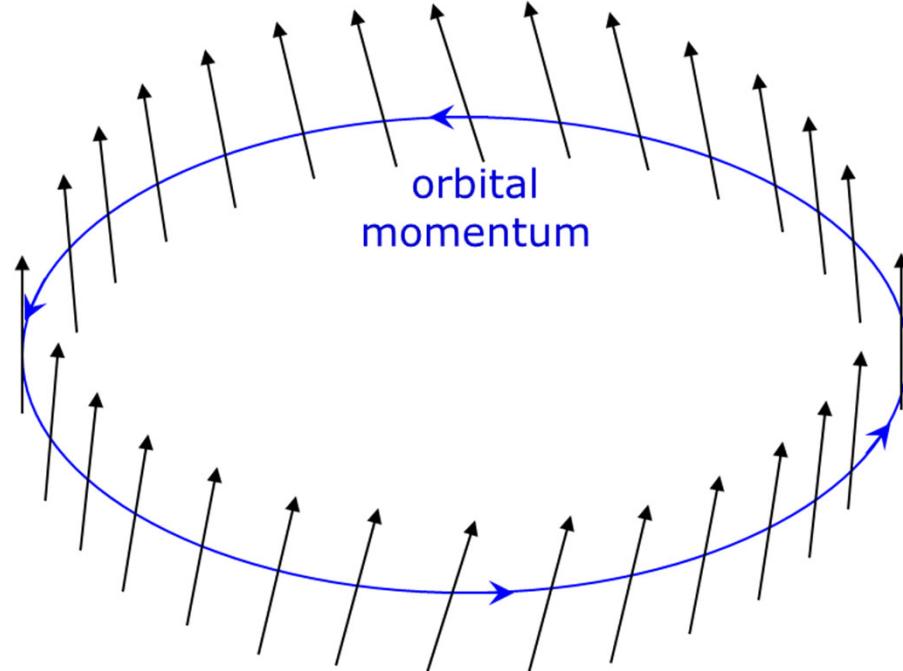
Purely hadronic PV in nucleus induces nuclear spin helix = anapole moment

$$H_{HPV} \propto \vec{\sigma}_N \cdot \vec{p}_N \Rightarrow \text{nucleon spin tilted along momentum}$$

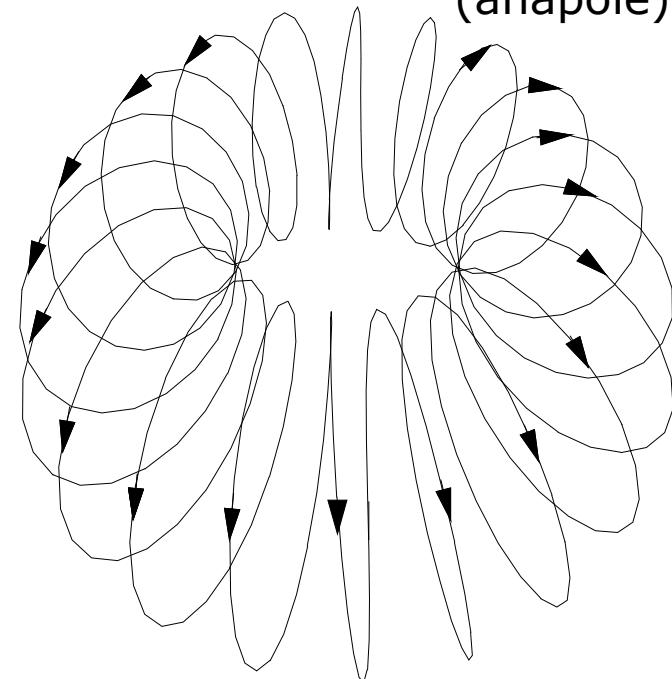
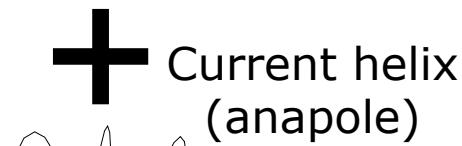
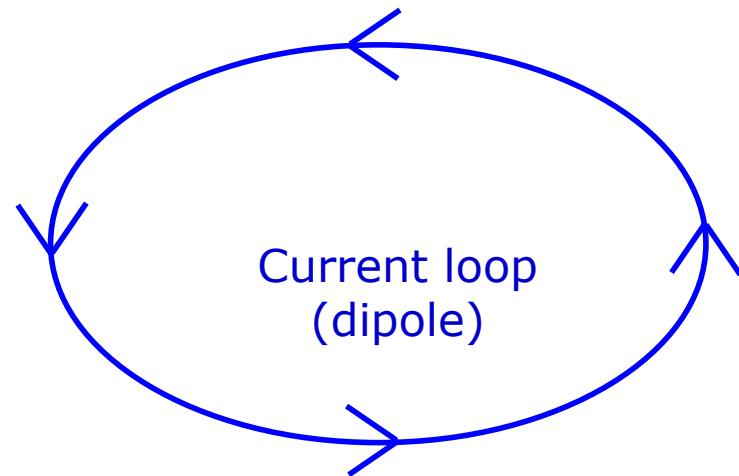


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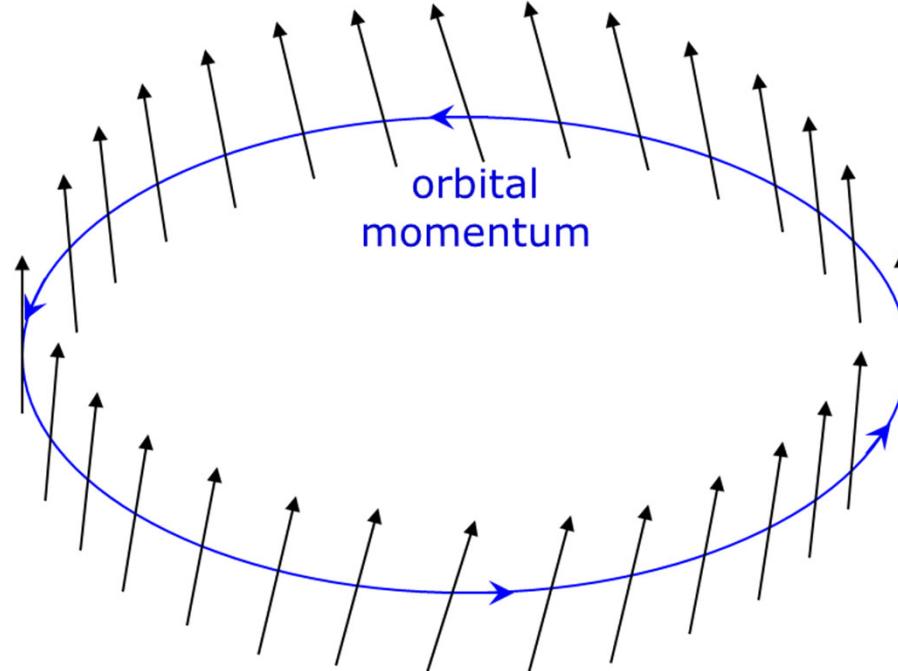


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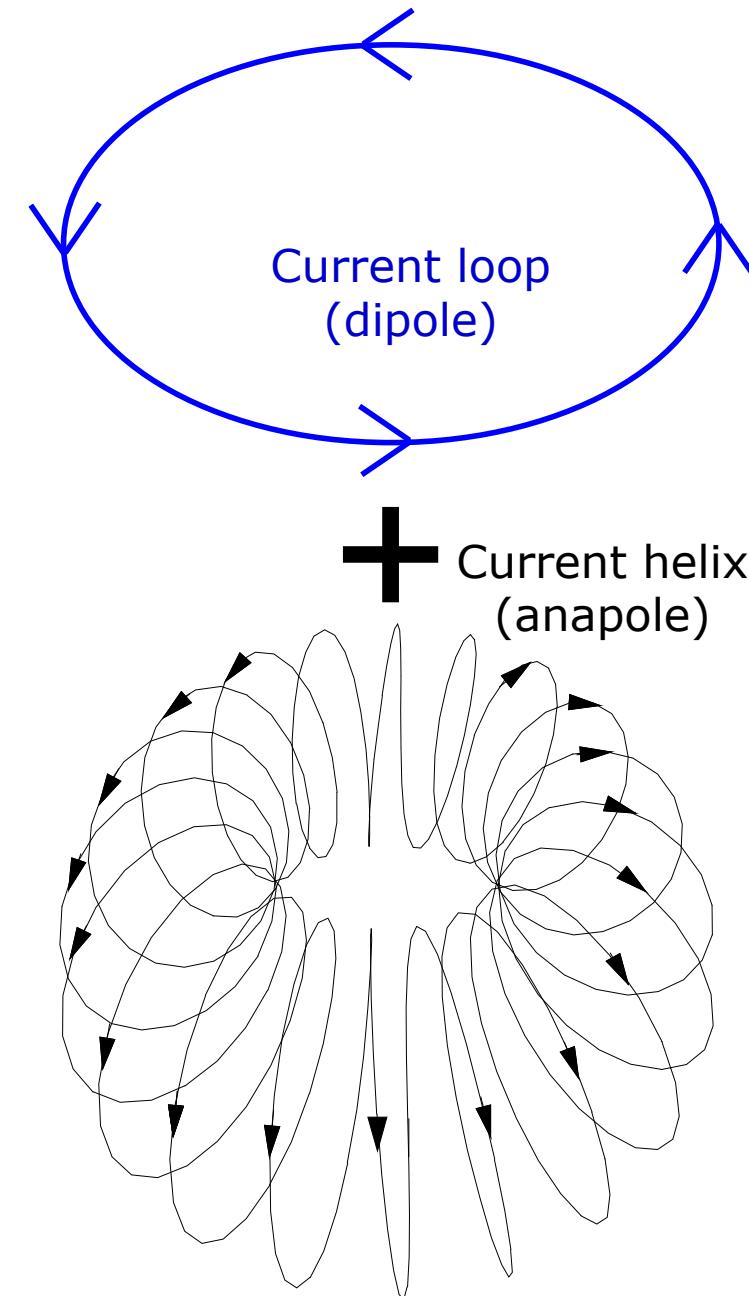


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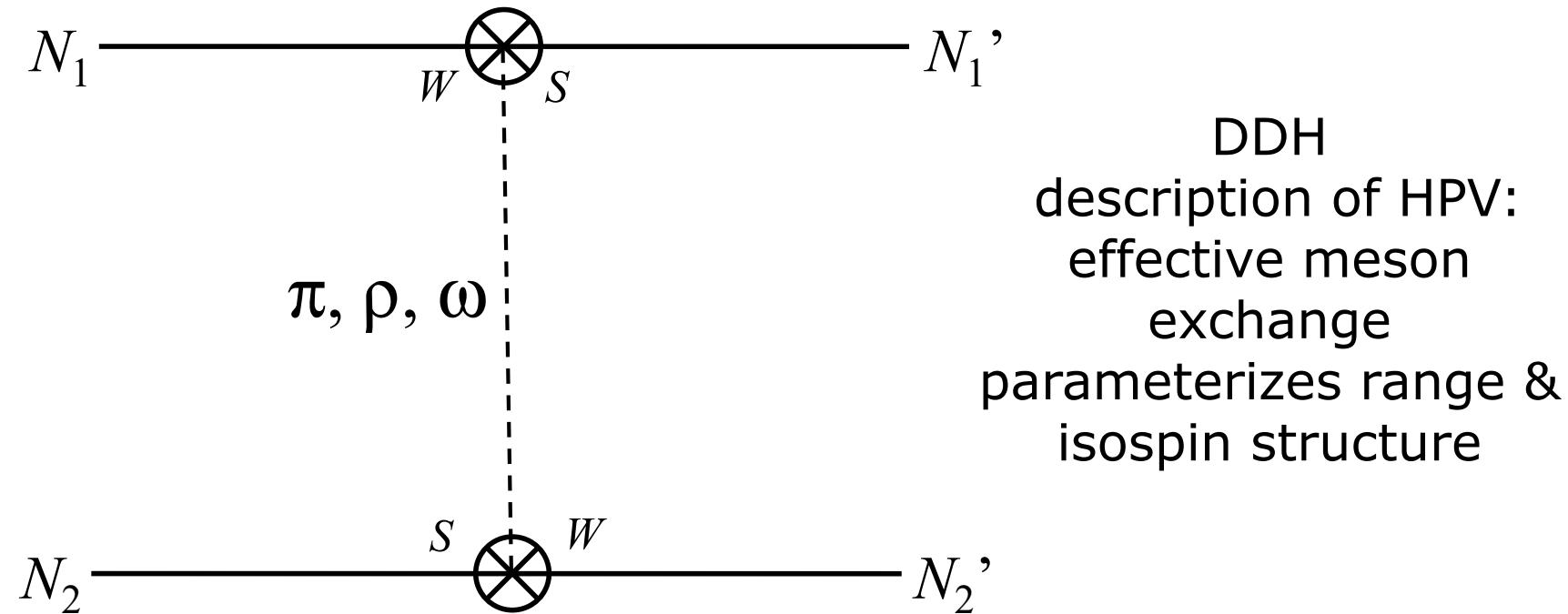


Simple model for nuclear anapole
(valence nucleon + constant-density core):

$$\vec{a} \propto g_{eff} A^{2/3} \hat{I}$$

Microscopic physics of nuclear anapole moment

Nucleon-nucleon hadronic parity-violating (HPV) interactions perturb nuclear structure:

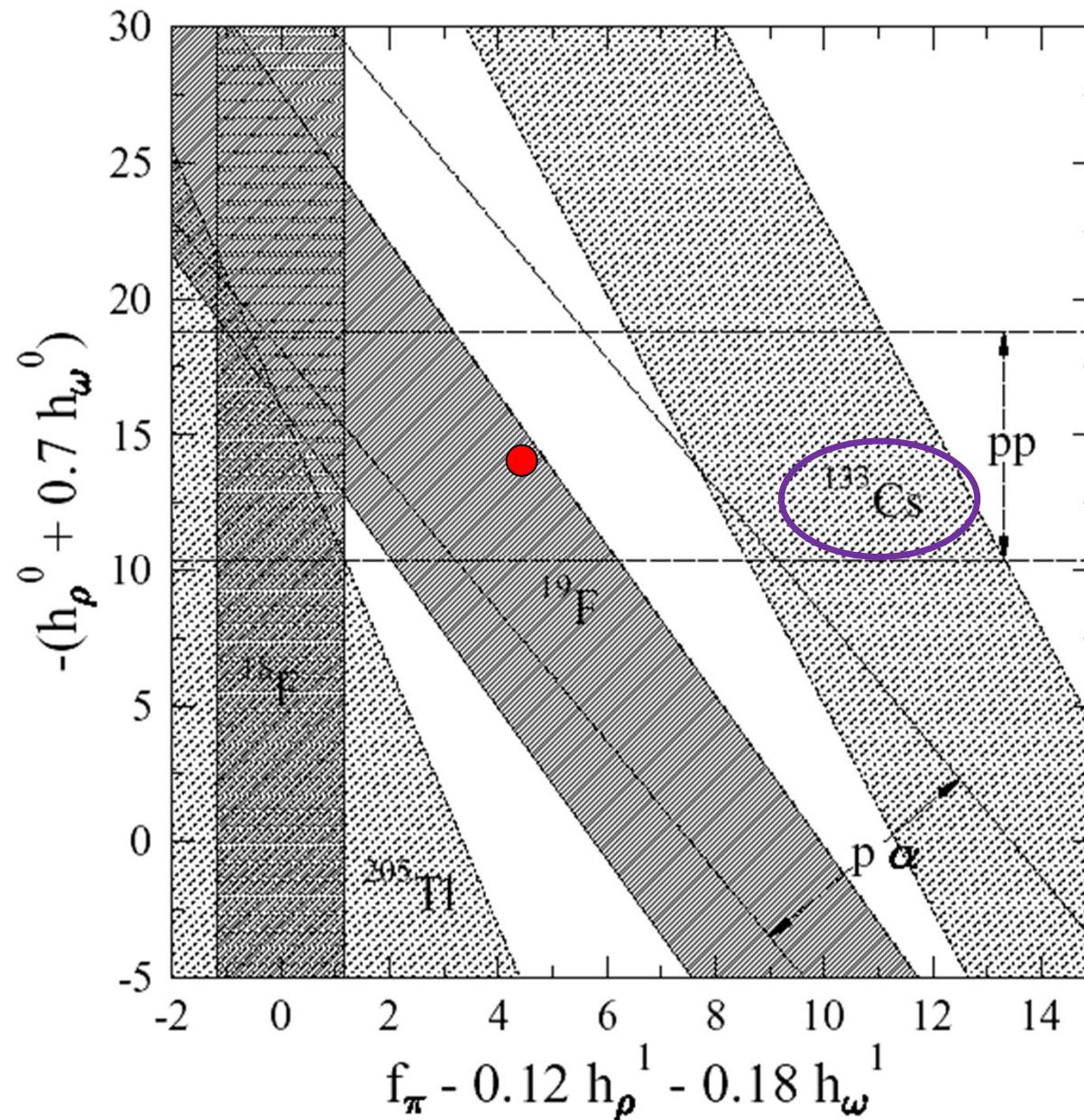


Hamiltonian for unpaired nucleon interacting with paired core gives spin-momentum correlation

$$H_{HPV} \sim G_F (\vec{\sigma}_N \cdot \vec{p}_N) \sum_i g_{\text{eff},i} F_i(\vec{r}, \vec{\tau})$$

Describe low-energy HPV with 6 dimensionless coupling constants,
each associated with different spin/isospin structure & range

HPNC measurements including anapole moments (prior to ~2018) in 2-D slice of DDH parameters

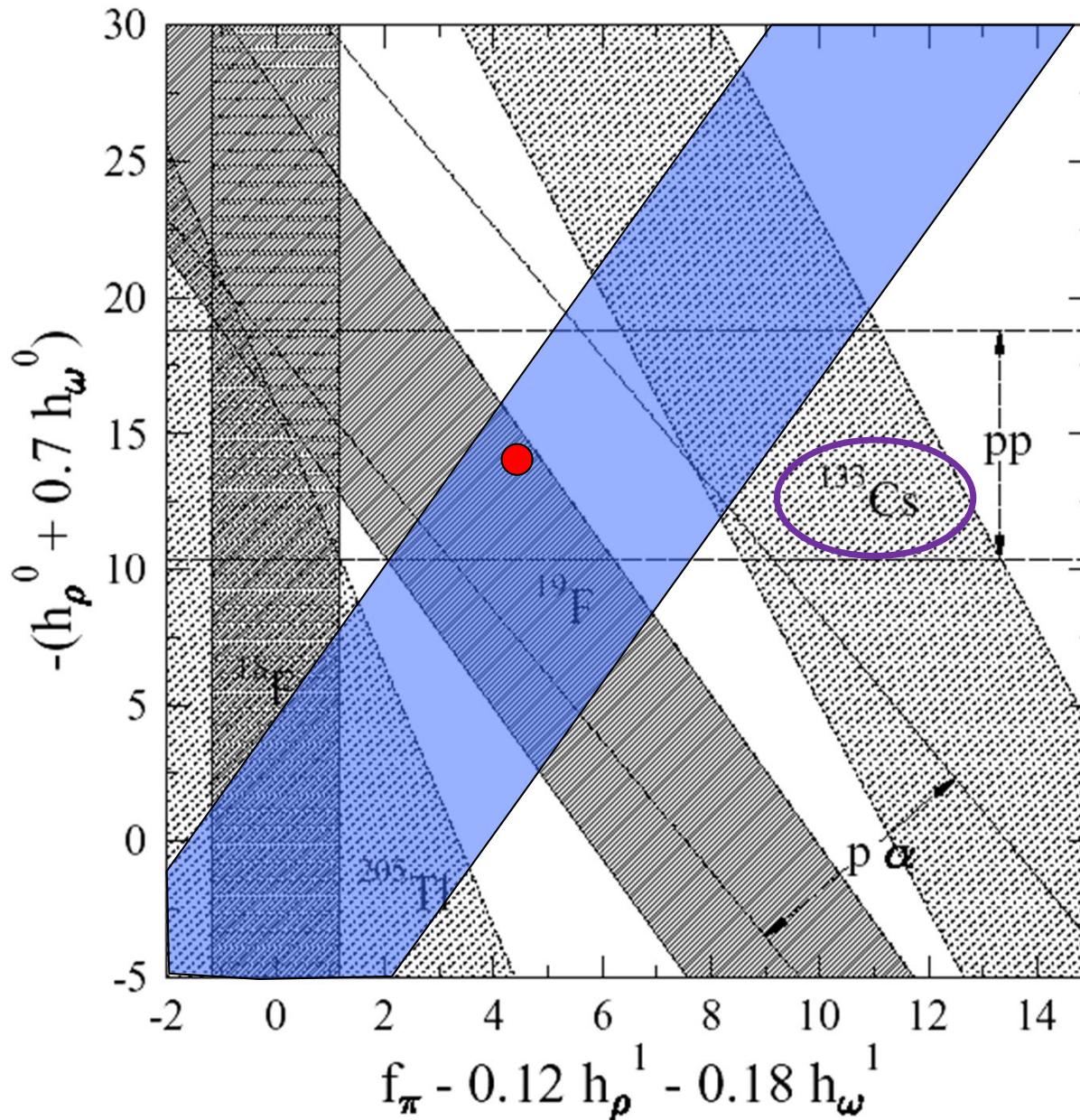


Single prior
anapole measurement
from atomic PV
in ^{133}Cs
[C. Wieman group,
JILA, 1997]

Poor agreement
with all other data
(nuclear theory
problem...?)

Assumes $\sim 30\%$
uncertainty in
nuclear structure
calculations

HPNC measurements including anapole moments (prior to ~2018) in 2-D slice of DDH parameters

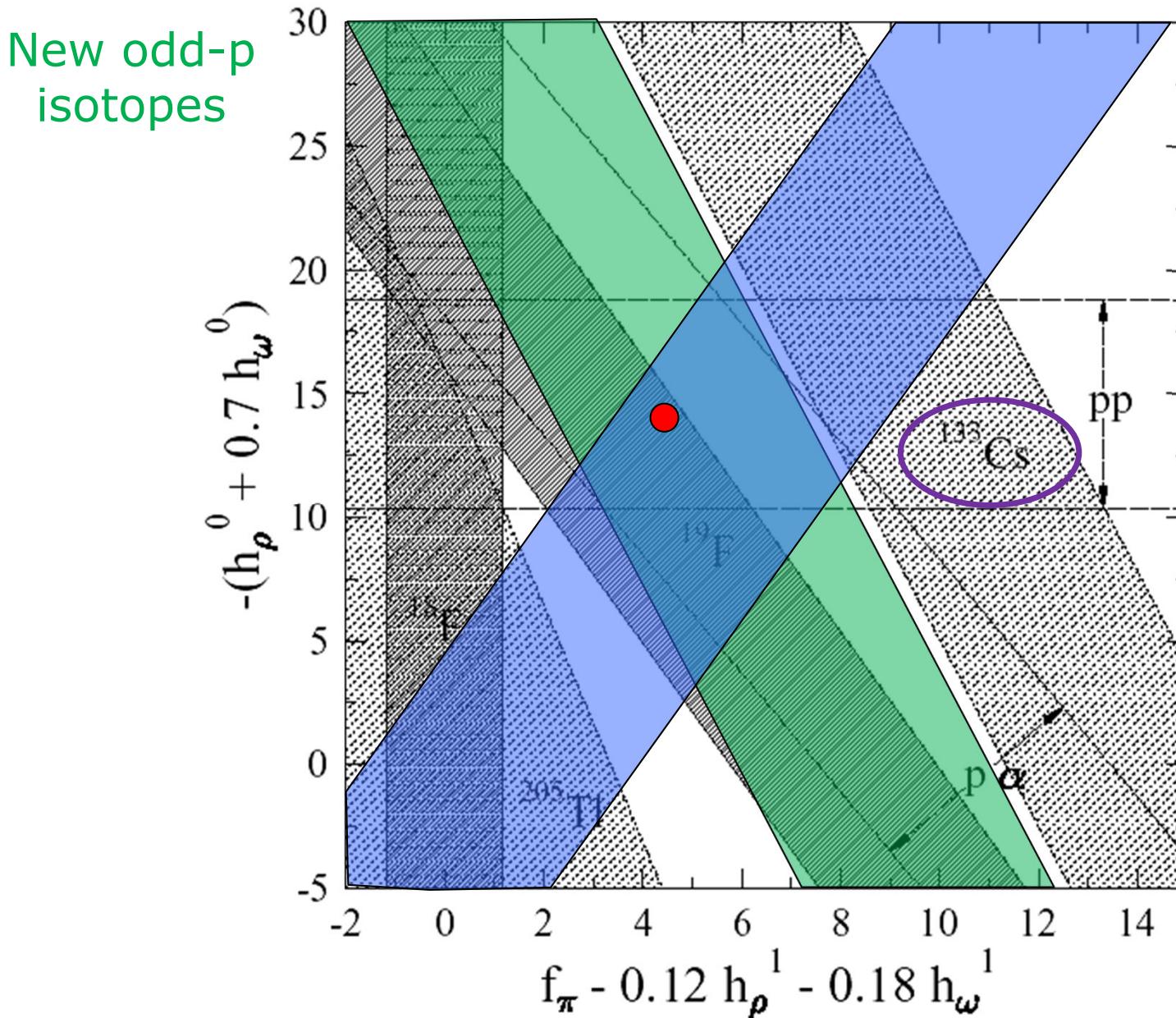


Odd-n
isotopes

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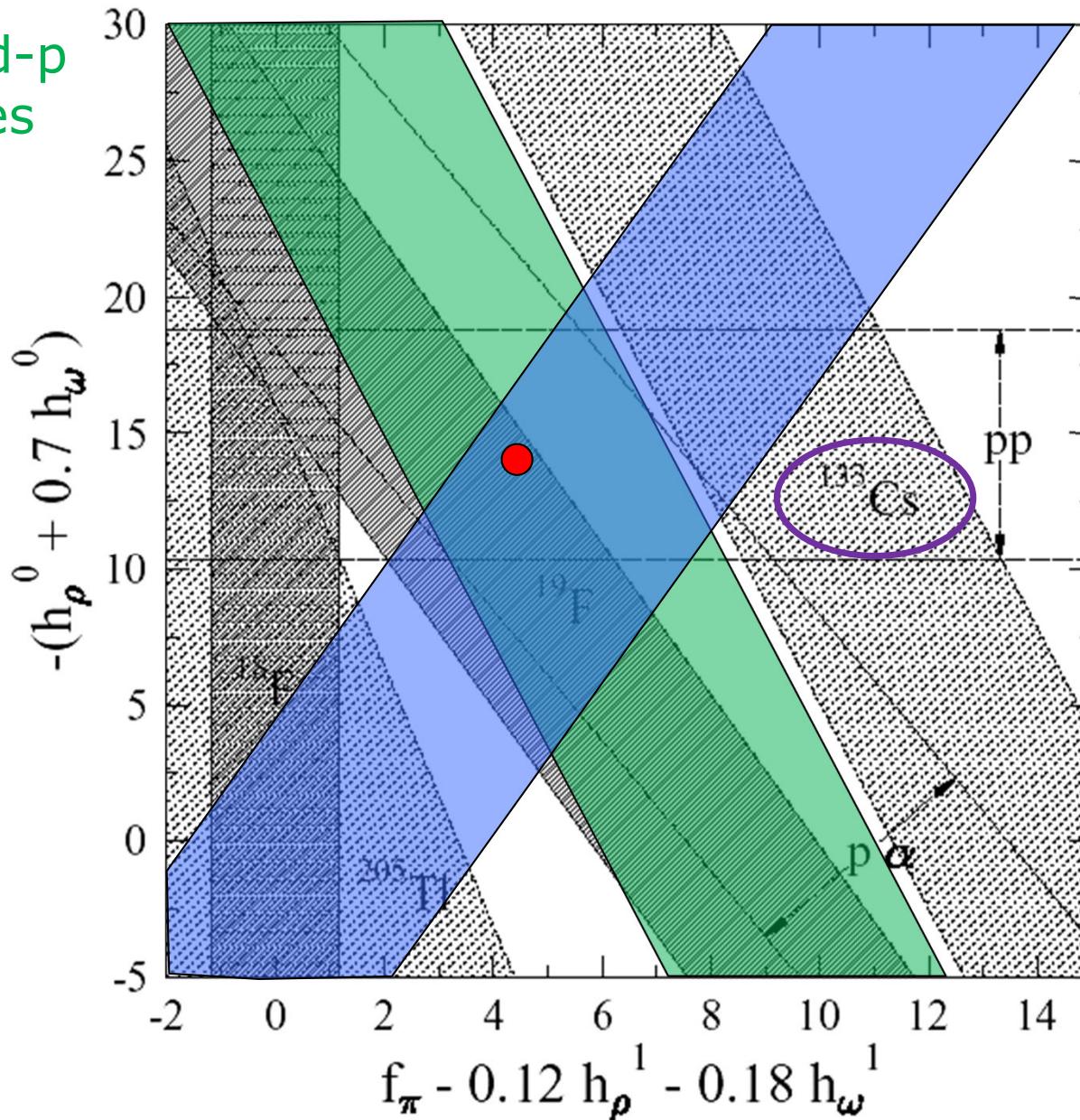


HPNC measurements including anapole moments (prior to ~2018) in 2-D slice of DDH parameters

New odd-p
isotopes

NOTE:
anapole moments not
yet evaluated in new
EFT parameterization
& large N_c analysis
of HPV

See M. Sarsour talk
this session

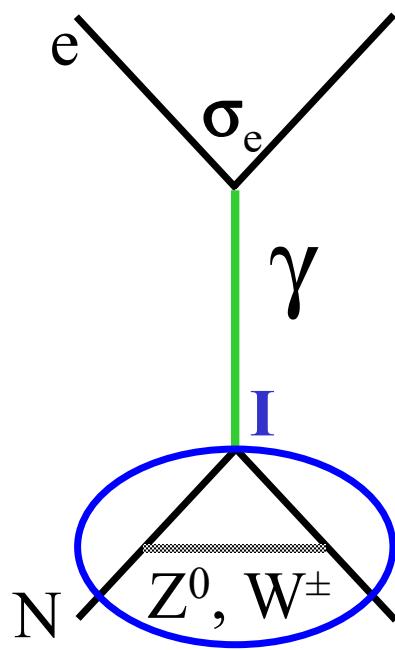


Odd-n
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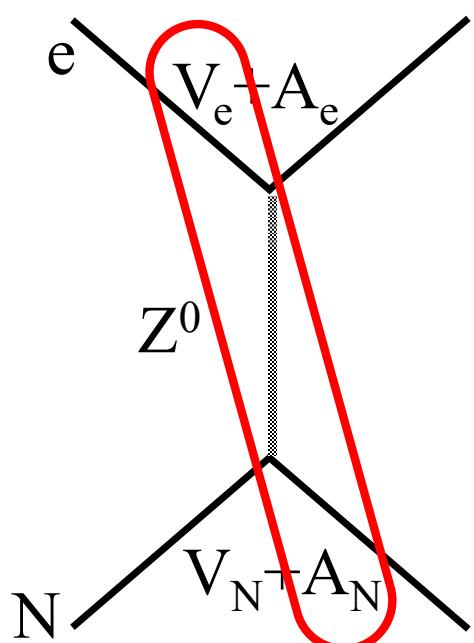
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Mechanisms for nuclear spin-dependent parity violation in atoms and molecules

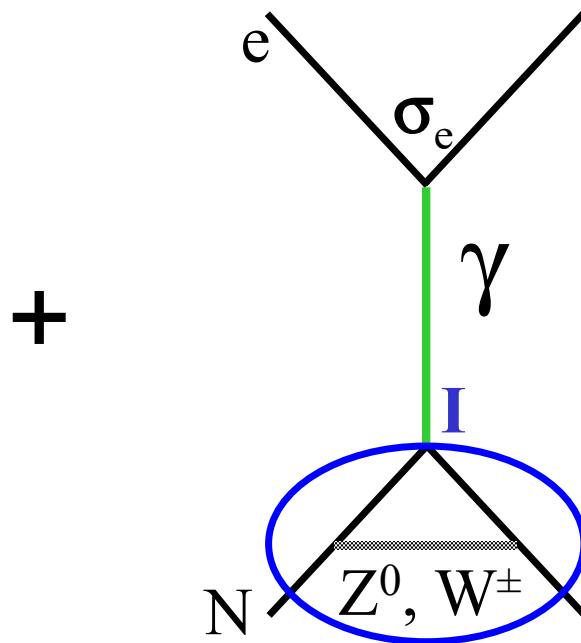


HPV interactions
inside nucleus induce
nuclear
anapole moment:
couples magnetically
to penetrating electron

Mechanisms for NSD-PV in atoms and molecules

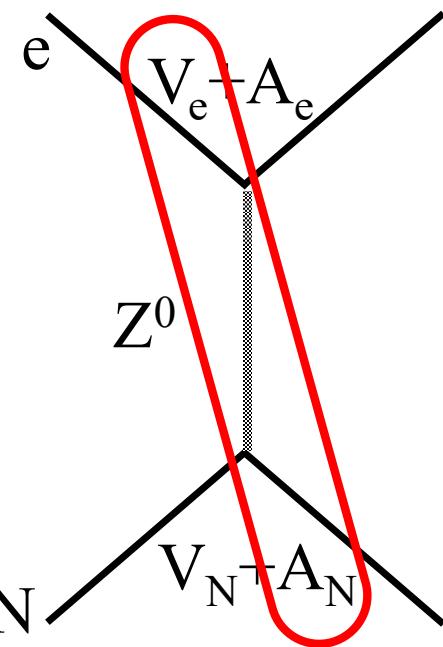


Tree-level
NSD-PV
from **suppressed**
 $V_e A_N$ term:
 C_2 subject to QCD
renormalization
similar to g_A

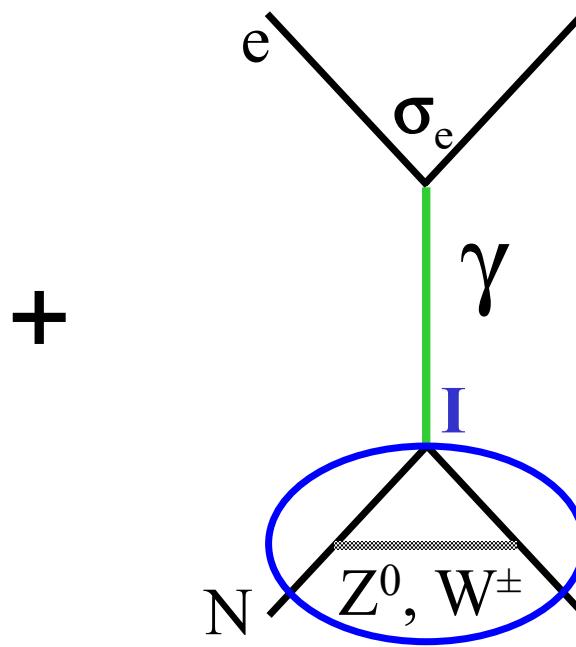


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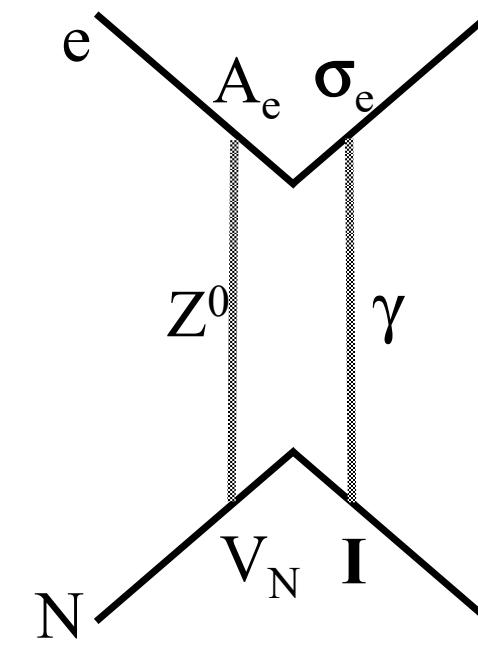
Mechanisms for NSD-PV in atoms and molecules



Tree-level
NSD-PV
from **suppressed**
 $V_e A_N$ term:
 C_2 couplings subject to
QCD renormalization
analogous to g_A



HPV interactions
inside nucleus induce
nuclear
anapole moment:
couples magnetically
to penetrating electron



Coherent sum:
weak charge Q_w
and
EM hyperfine interaction
(small, well-understood)

$$H_{NSD-PV} \propto (K'_2 + K'_a + K'_Q) G_F (\vec{\sigma} \cdot \vec{I}) (\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

3 contributions to NSD-PV in atoms/molecules: scaling with Z & A

$$H_{NSD-PV} \propto (\kappa'_2 + \kappa'_a + \kappa'_Q) G_F (\vec{\sigma} \cdot \vec{I}) (\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

$$\kappa'_{2P} = -\kappa'_{2N} \approx -.05$$

$$\kappa'_a \approx .05 g_{eff} \left(\frac{A}{50} \right)^{2/3}$$

$$(g_{eff,P} \approx 4, g_{eff,N} \lesssim 1)$$

Overall Z^2

Challenge for atomic/molecular approaches:

Signals by far easiest to detect with high Z & A

BUT

Best chance for reliable interpretation with lowest Z & A

3 contributions to atom/molecule NSD-PV: scaling with Z & A

$$H_{NSD-PV} \propto (\kappa'_2 + \kappa'_a + \kappa'_Q) G_F (\vec{\sigma} \cdot \vec{I}) (\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

$\kappa'_a \approx .05 g_{eff} \left(\frac{A}{50} \right)^{2/3}$

$(g_{eff,P} \approx 4, g_{eff,N} \lesssim 1)$

Overall Z^2

Heavy atoms/molecules \rightarrow anapole term dominates: $|\kappa'_a| > |\kappa'_2|$
(Collective enhancement causes radiative correction $>$ tree level...!)

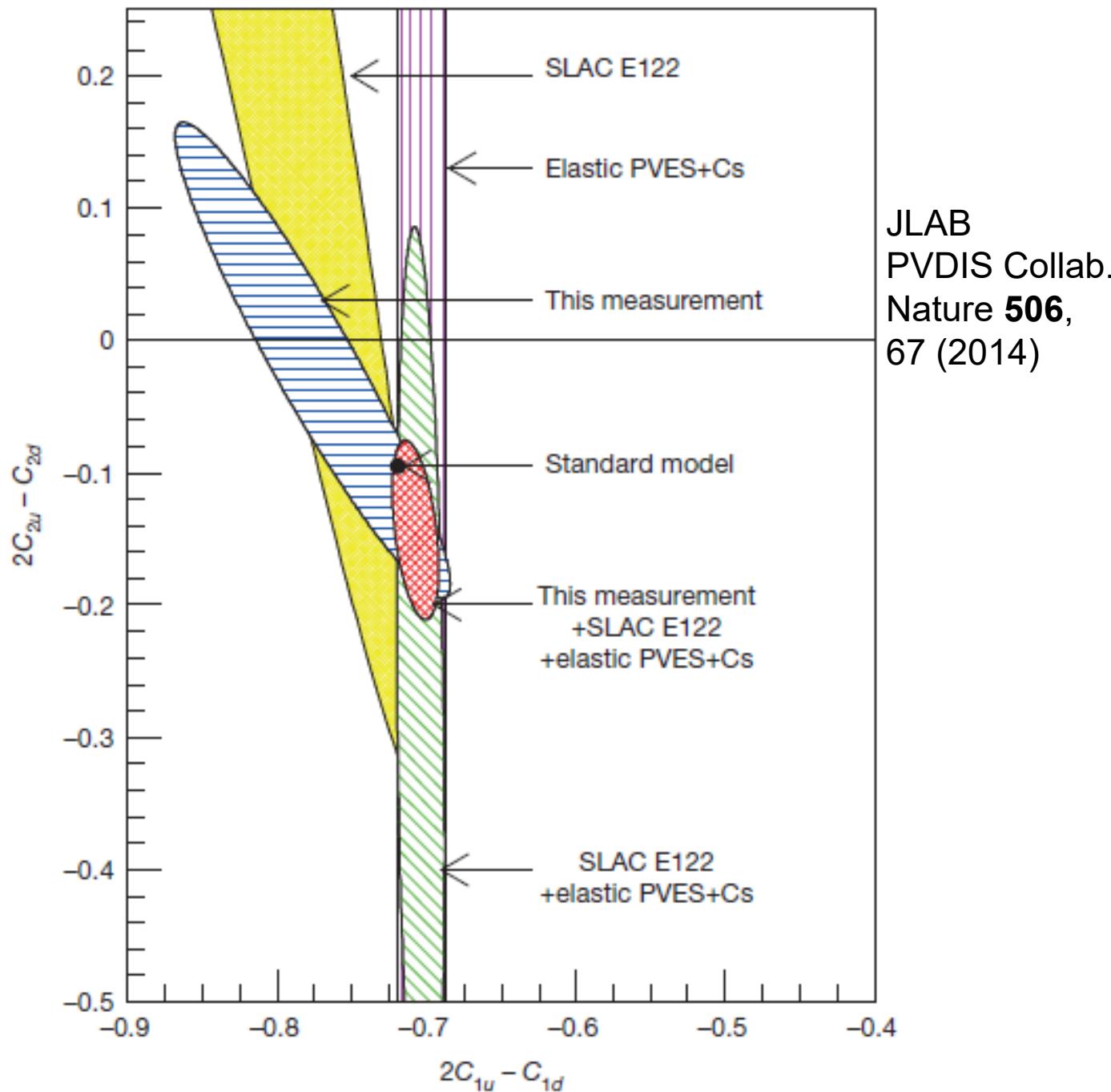
Light atoms/molecules \rightarrow tree-level Z exchange term dominates: $|\kappa'_a| > |\kappa'_2|$
 $|\kappa_a| \approx |\kappa_2|$ for $A \approx 10$ (odd proton)
 $A \approx 100$ (odd neutron)

More physics motivation for κ measurements: neutral weak currents & QCD

κ_2 : Tree-level Z^0 Exchange

- Vector electron – axial nucleon weak coupling constants (C_{2N} , C_{2P})
- Related to fundamental electron-quark couplings (C_{2u} , C_{2d}) via QCD
- Complementary to PVDIS e-p measurements at JLAB
(different linear combinations of C_2 's & nucleons vs. quarks)

See D. Adhikari talk
this session

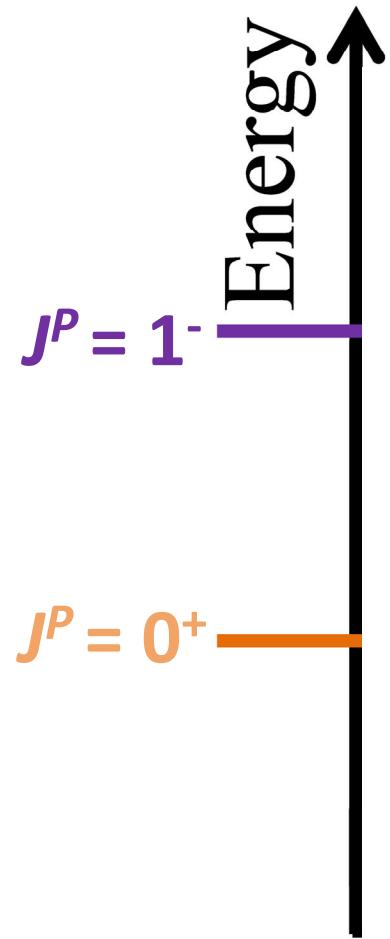


ZOMBIES overarching goal:

understand electroweak interactions in strongly-interacting environment at low q^2

- **Pure hadronic (nucleon-nucleon) parity violating interactions: still poorly understood**
 - complementary to recent few-nucleon probes (NPDGamma, polarized n on ${}^3\text{He}$, neutron spin rotation, ...)
 - sensitive to different linear combinations in multi-parameter space
 - connect to recent developments in nuclear structure calculations & HPV theory
 - rich data set for consistency checks
 - benchmark for $0\nu\beta\beta$ matrix element calculations...???
- **Nucleon-level $V_e A_h (C_{2P}, C_{2N})$ vs. Nucleus-level $V_e A_h$**
 - quenching as for g_A in charged currents...?
- **Quark-level $V_e A_h (C_{2u}, C_{2d})$ vs. nucleon-level $V_e A_h (C_{2P}, C_{2N})$ neutral current couplings ?**
 - matching as $q^2 \rightarrow 0$...?
 - potential for lattice QCD prediction & post-hoc verification?

ZOMBIES principle: amplified NSD-PV mixing in molecules w/unpaired electron

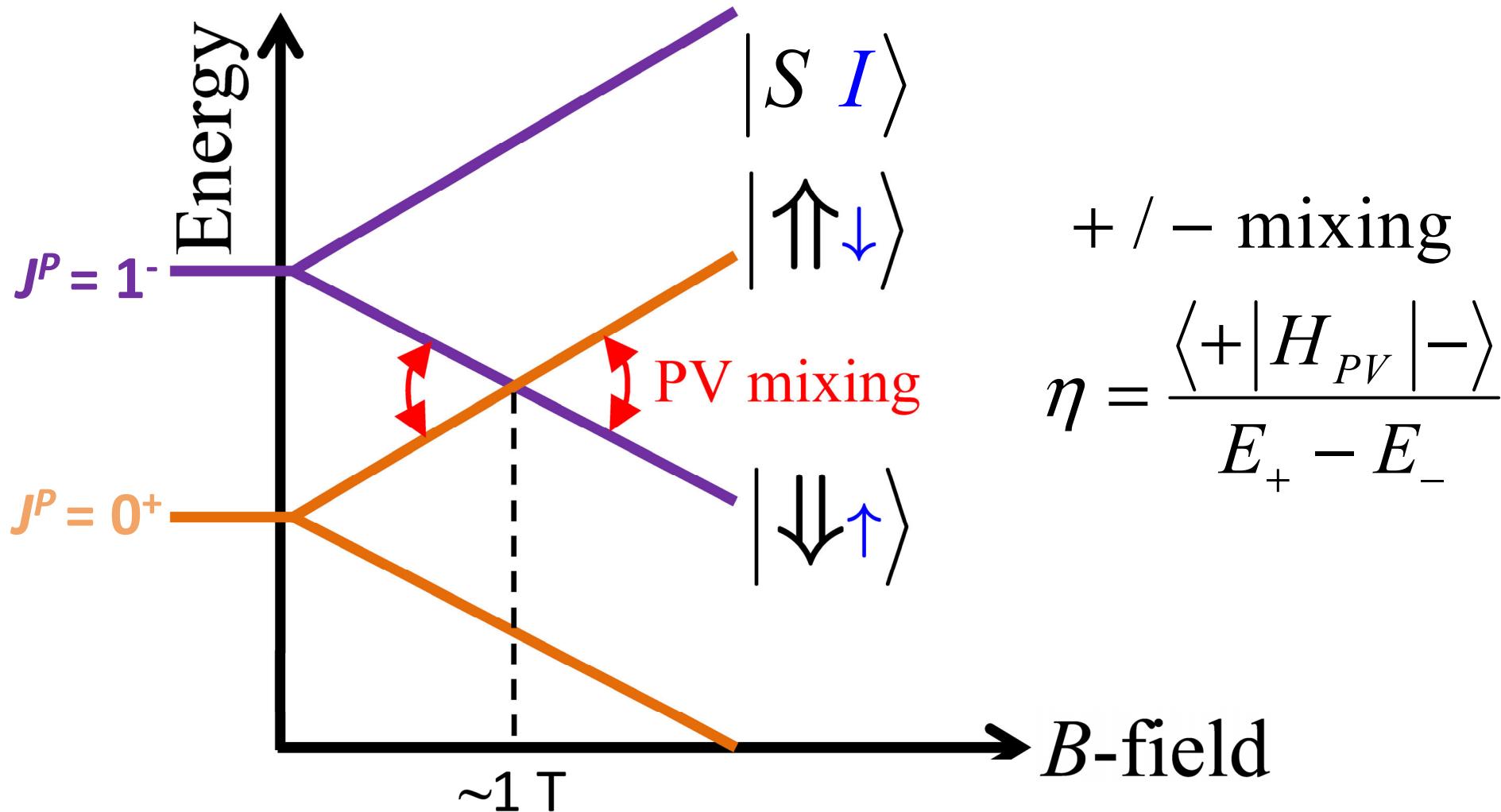


+ / - mixing

$$\eta = \frac{\langle + | H_{PV} | - \rangle}{E_+ - E_-}$$

Naturally small rotational splitting ($\sim 10^{-4}$ eV vs. ~ 1 eV in atoms)

Amplified NSD-PV mixing in molecules with one unpaired electron

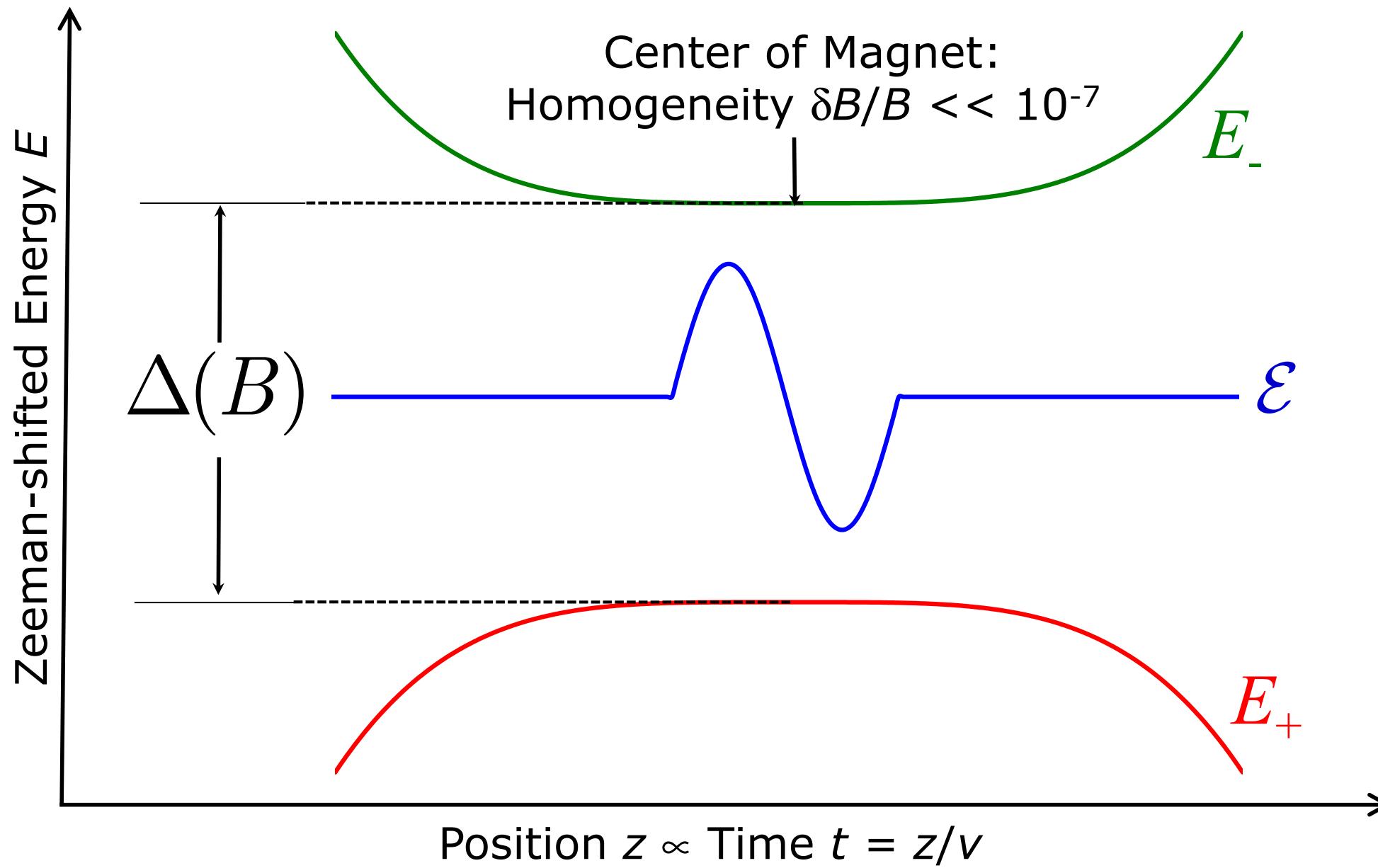


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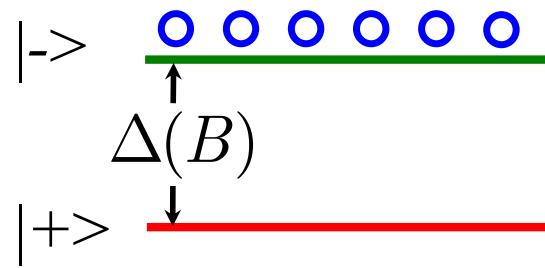
can be bridged w/Zeeman shift:

$\gtrsim 10^{11}$ enhanced PV mixing vs. classic experiments with atoms

Stark interference method:
apply oscillating \mathcal{E} -field to mix nearly-degenerate opposite-parity levels



Detecting PV in near-degenerate levels: AC Stark shift

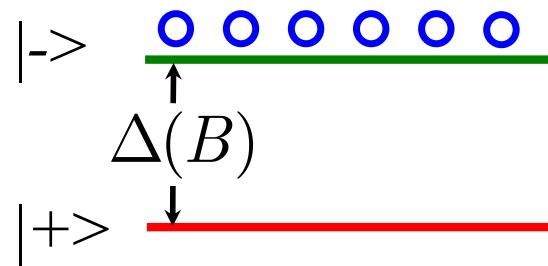


$$H = \begin{pmatrix} 0 & iW + d\mathcal{E}(t) \\ -iW + d\mathcal{E}(t) & \Delta \end{pmatrix}$$

D.D., S.B. Cahn, *et al.*
PRL 100, 023003 (2008)

Nguyen *et al.*,
PRA 56, 3453 (1997)

Detecting PV in near-degenerate levels: AC Stark shift



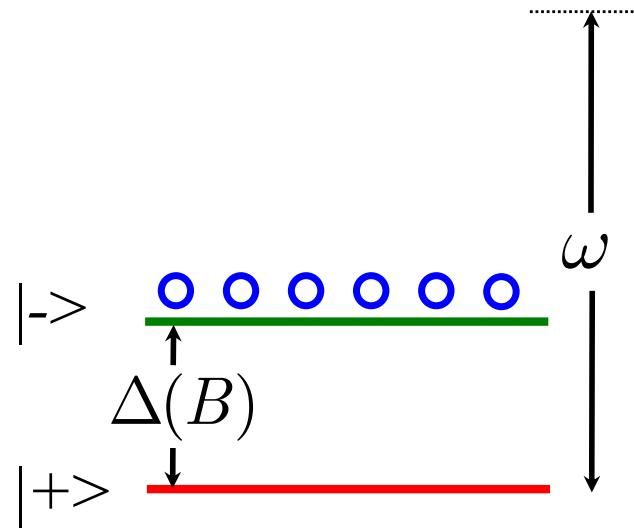
PV mixing iW encodes physics of interest

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Apply oscillating \mathcal{E} -field, 1 cycle:

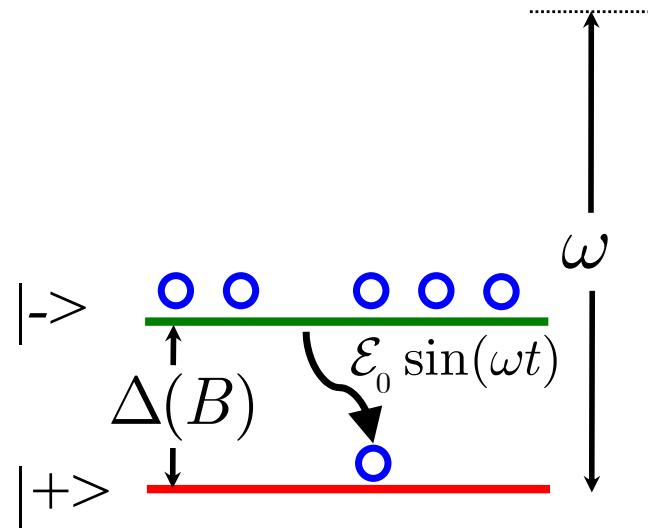
$$\mathcal{E}(t) = \mathcal{E}_0 \sin(\omega t)$$

$$\left[\begin{array}{l} \omega \gg \Delta, d\mathcal{E}_0; \\ T = 2\pi / \omega \end{array} \right]$$

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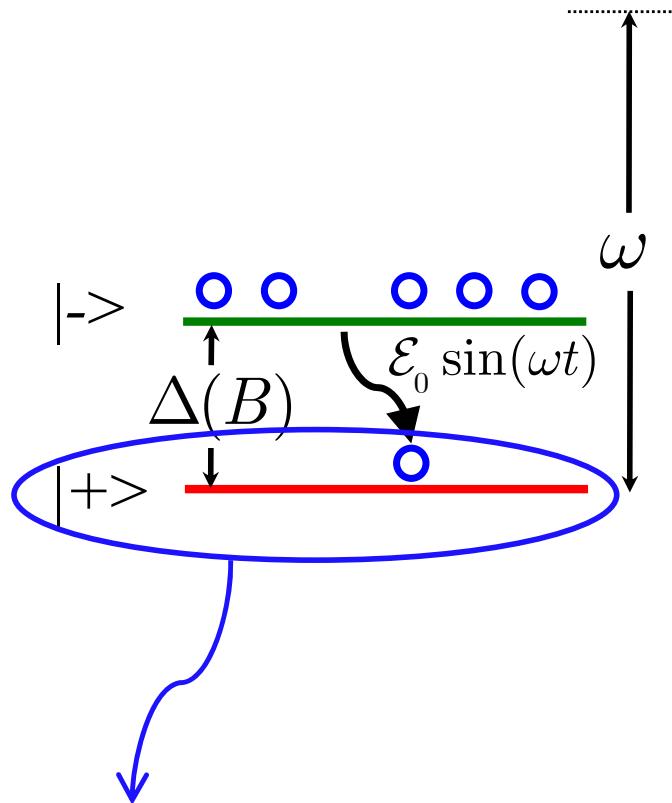
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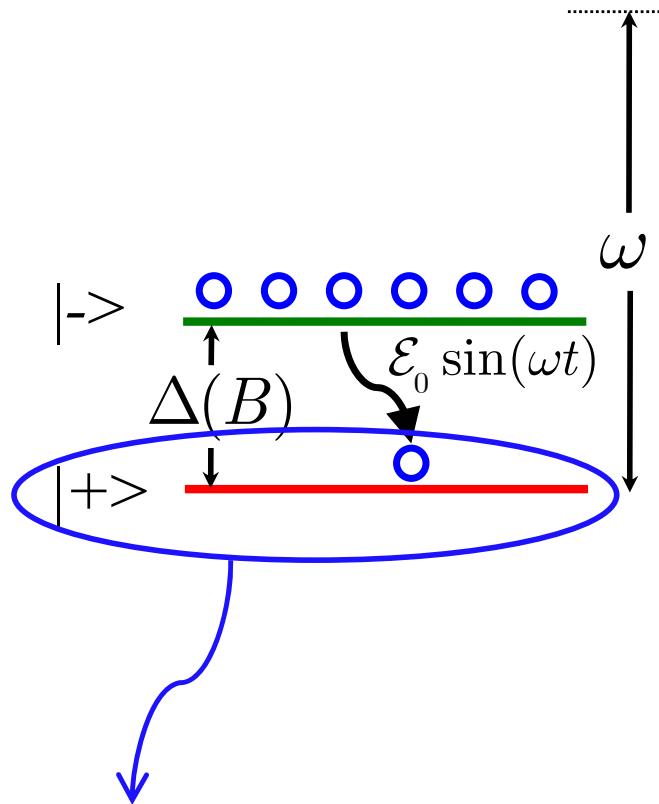
$$\left[\begin{array}{l} \omega \gg \Delta, d\mathcal{E}_0; \\ T = 2\pi / \omega \end{array} \right]$$

$$S = \left| \langle + | \psi(T) \rangle \right|^2 = 4 \sin^2 \left(\frac{\Delta T}{2} \right) \left[\left(\frac{d\mathcal{E}_0}{\omega} \right)^2 + 2 \frac{W}{\Delta} \frac{d\mathcal{E}_0}{\omega} \right]$$

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*“Large” Stark Term
Even in \mathcal{E}_0*

*Small PV Term
Odd in \mathcal{E}_0*

Signal, Asymmetry, Sensitivity

-- Measure signal $S(\mathcal{E}_0) \approx 4N_0 \sin^2\left(\frac{\Delta T}{2}\right) \left[\left(\frac{d\mathcal{E}_0}{\omega} \right)^2 + 2 \frac{W}{\Delta} \frac{d\mathcal{E}_0}{\omega} \right]$

with opposite-sign \mathcal{E} -fields $+\mathcal{E}_0, -\mathcal{E}_0$

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with opposite-sign \mathcal{E} -fields $+\mathcal{E}_0, -\mathcal{E}_0$

-- Form asymmetry to extract W in terms of known quantities :

$$\mathcal{A} = \frac{S(+\mathcal{E}_0) - S(-\mathcal{E}_0)}{S(+\mathcal{E}_0) + S(-\mathcal{E}_0)} \approx 2 \frac{W}{\Delta} \frac{\omega}{d\mathcal{E}_0}$$

Signal, Asymmetry, Sensitivity

-- Measure signal $S(\mathcal{E}_0) \approx 4N_0 \sin^2\left(\frac{\Delta T}{2}\right) \left[\left(\frac{d\mathcal{E}_0}{\omega} \right)^2 + 2 \frac{W}{\Delta} \frac{d\mathcal{E}_0}{\omega} \right]$
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Statistical Uncertainty

$$\delta W = \frac{1}{2\sqrt{2}} \frac{1}{\sqrt{N_0}} \frac{1}{T}$$

best sensitivity from
large interaction time T

Equivalent to measuring W as generic energy shift at Standard Quantum Limit

N. Fortson, PRL **70**, 2383 (1993)

Properties of NSD-PV asymmetry: example with ^{137}BaF

Typical numbers for ^{137}BaF :

$$\Delta_0 \sim 1/T \sim 2\pi \times 1 \text{ kHz}$$

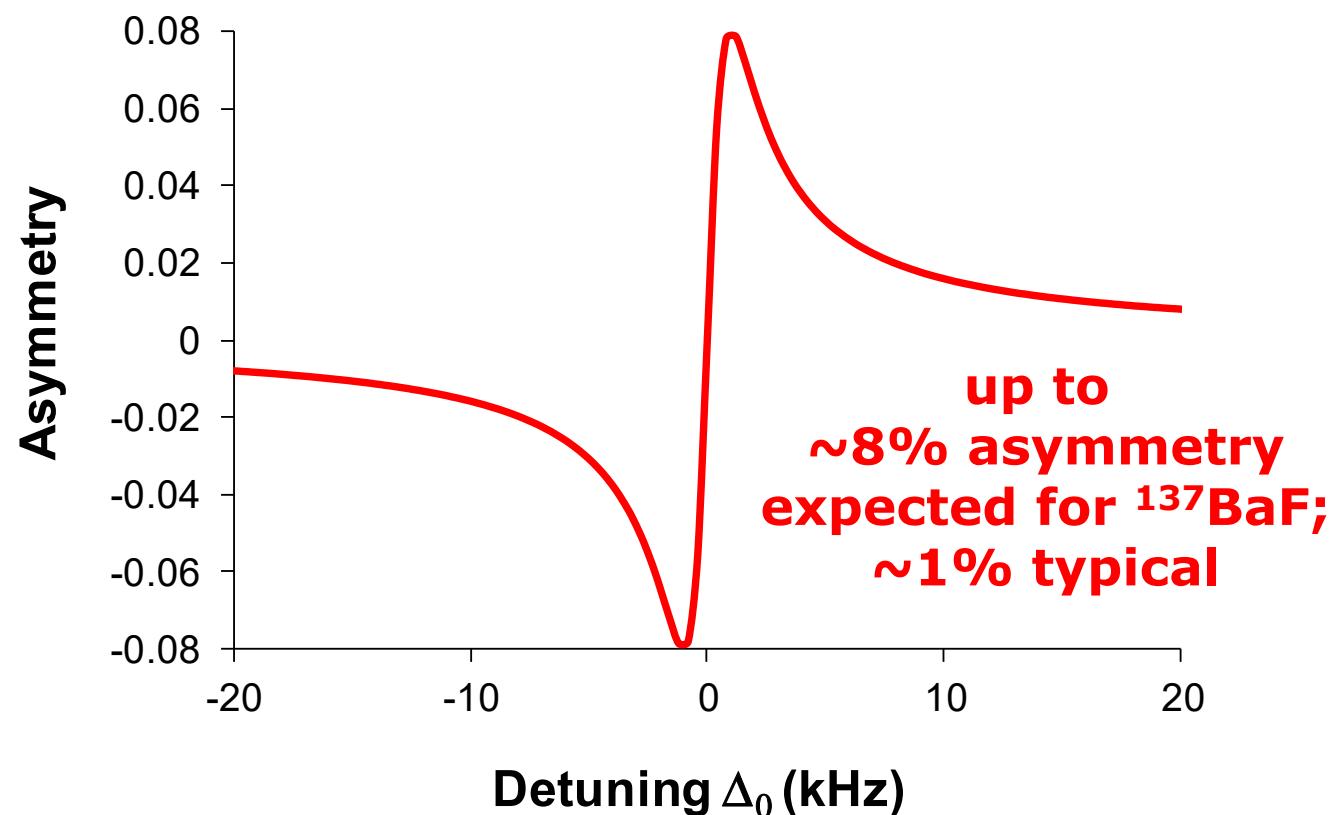
$$\omega = 2\pi \times 100 \text{ kHz}$$

$$dE_0/\omega = 0.1$$

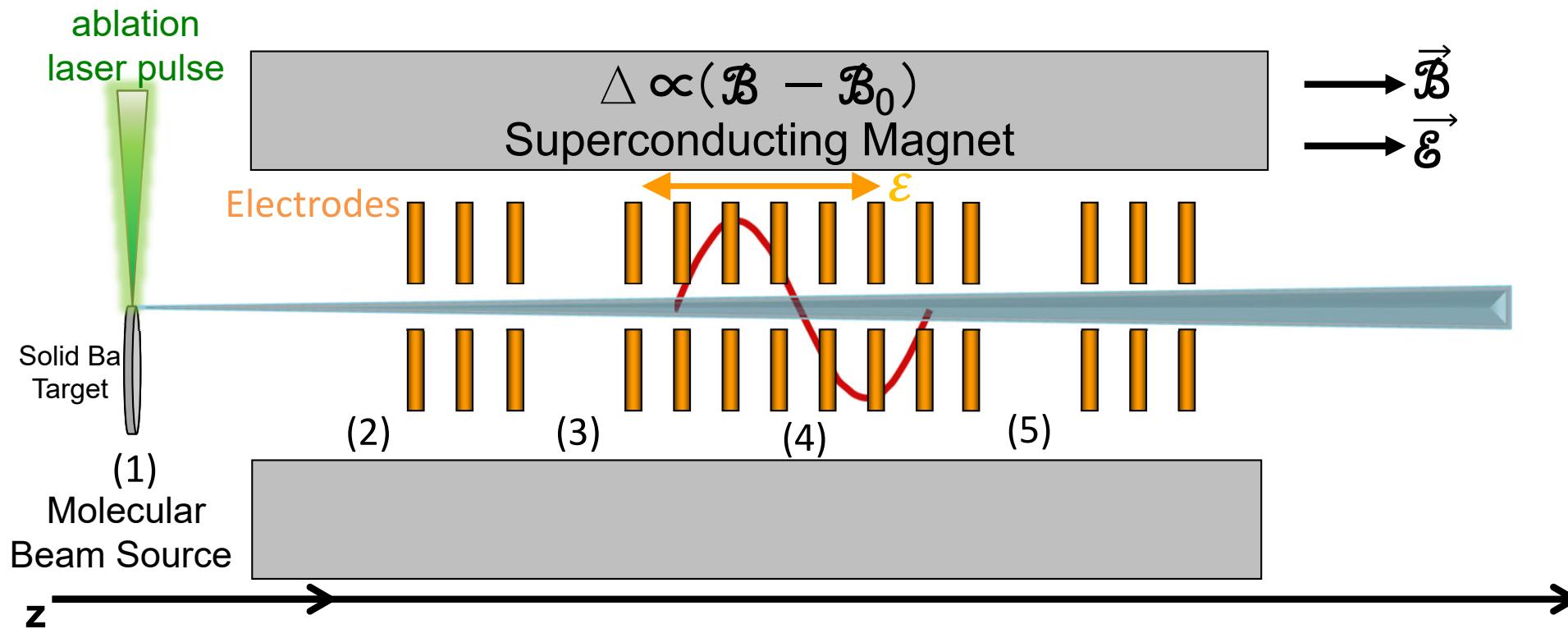
$$W = 2\pi \times 5 \text{ Hz}$$

PV Invariant

$$\left(d\vec{\mathcal{E}} / dt \right) \cdot \left(\vec{\mathcal{B}} - \vec{\mathcal{B}}_c \right)$$



ZOMBIES experimental schematic

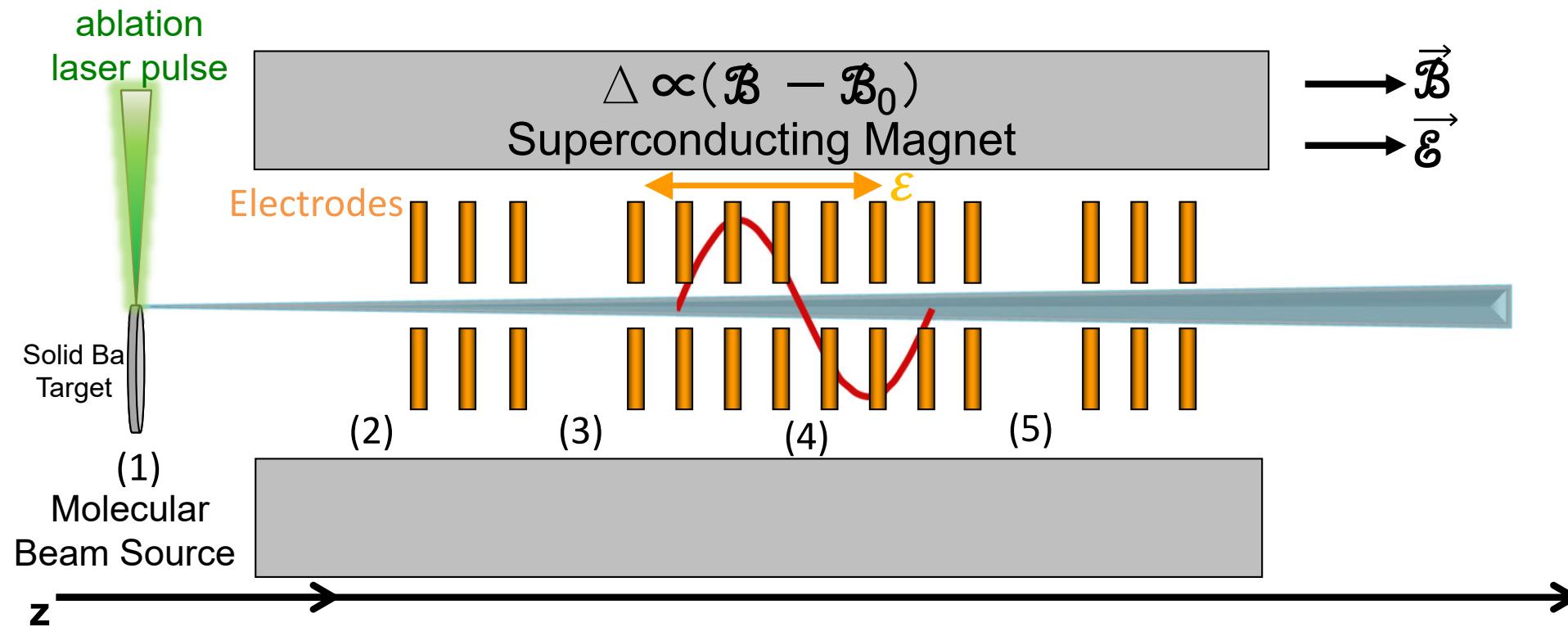


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OOOO

(1)

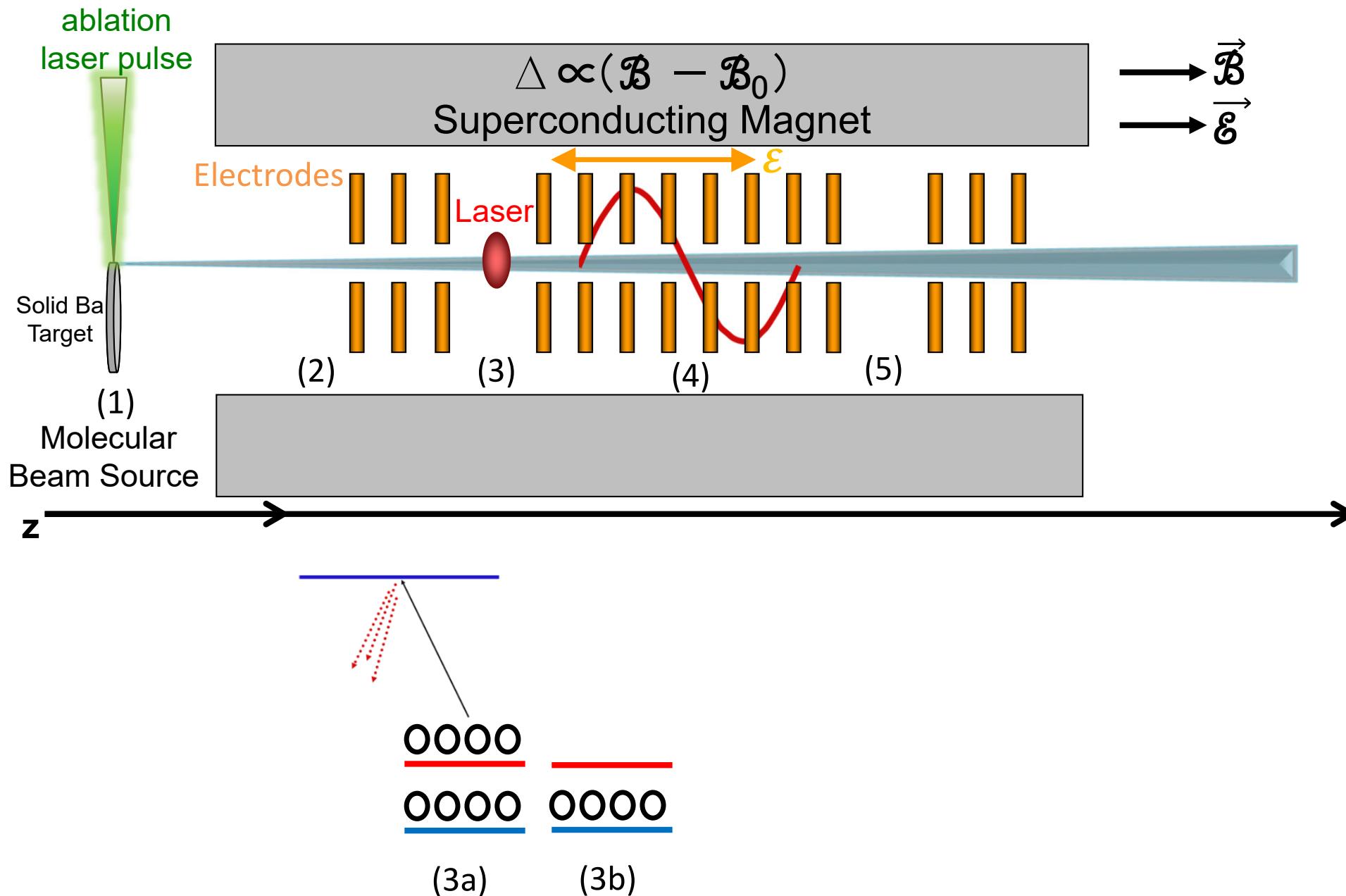
ZOMBIES experimental schematic



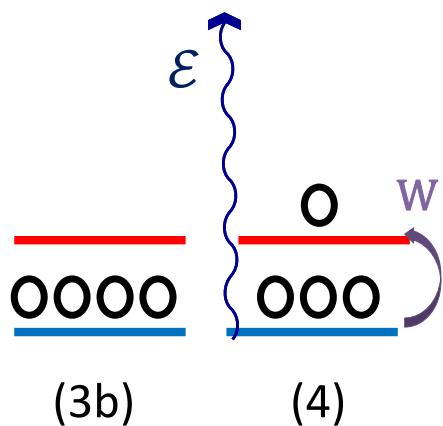
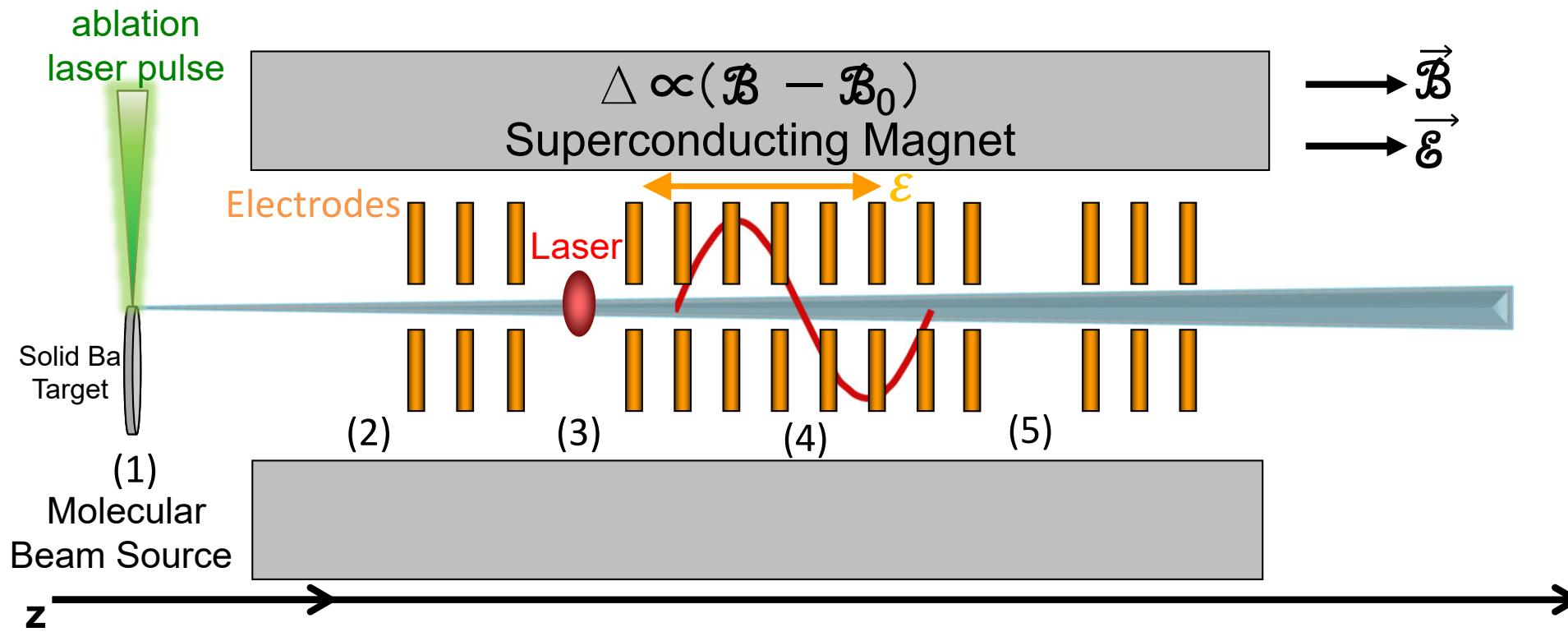
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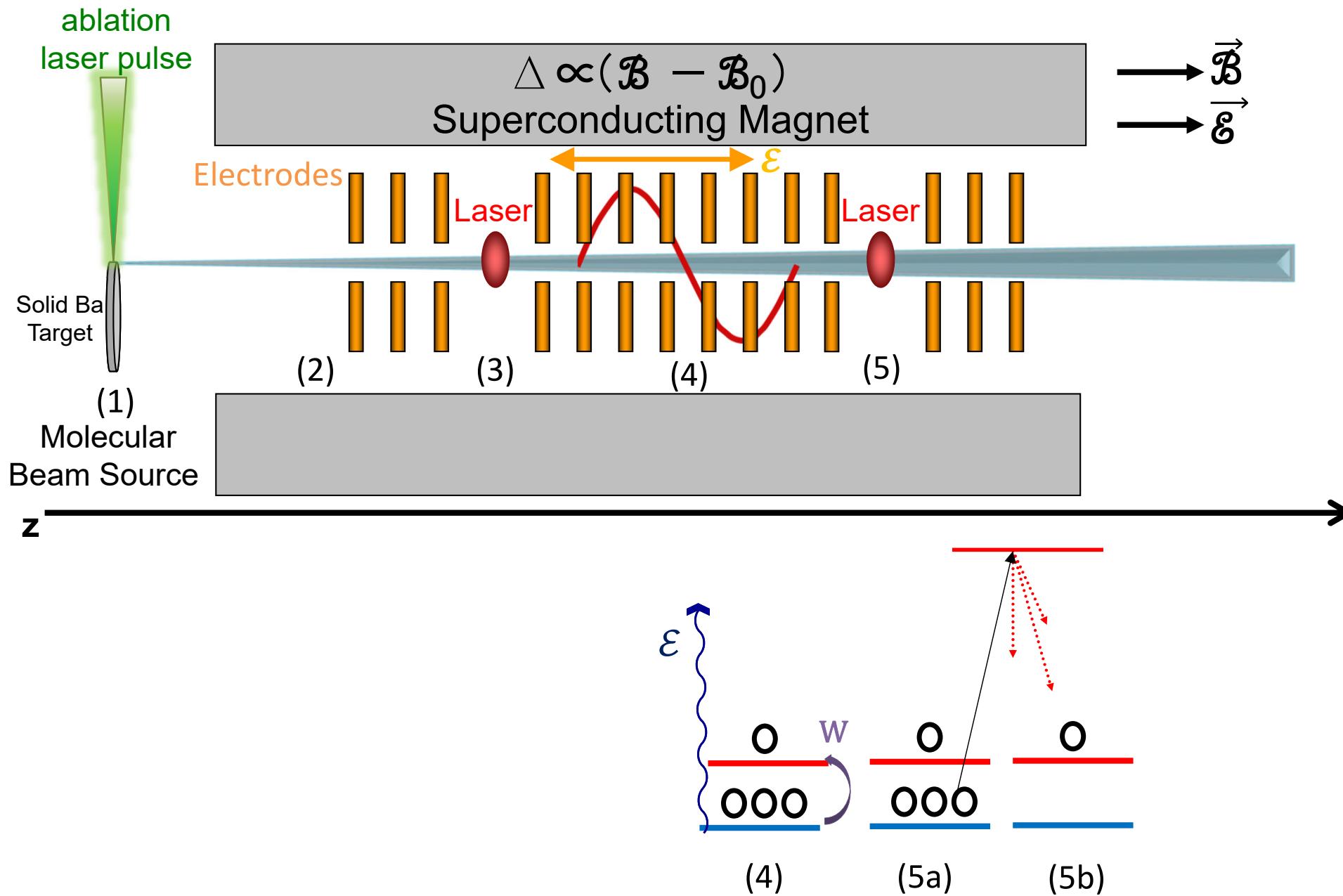
ZOMBIES experimental schematic



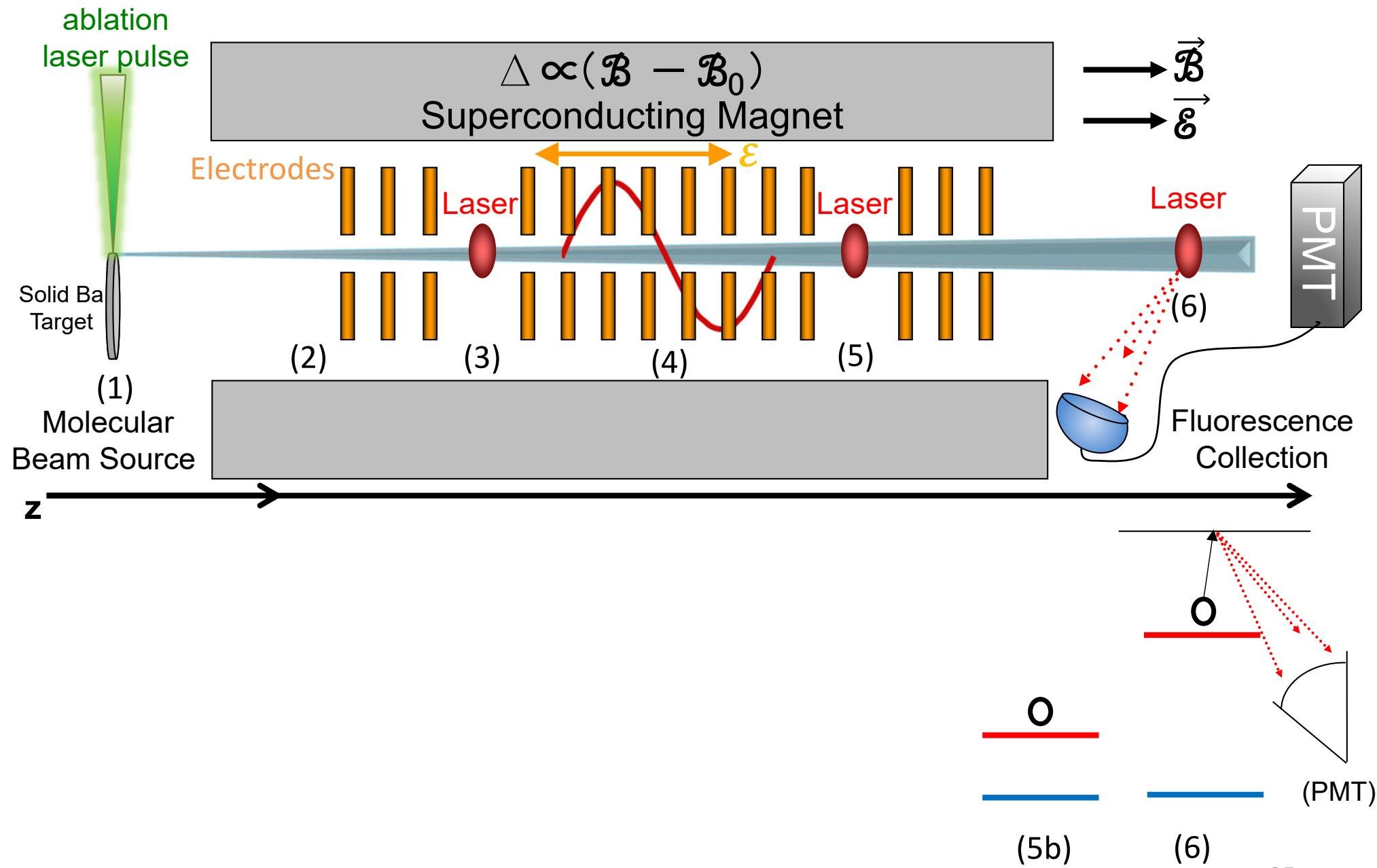
ZOMBIES experimental schematic



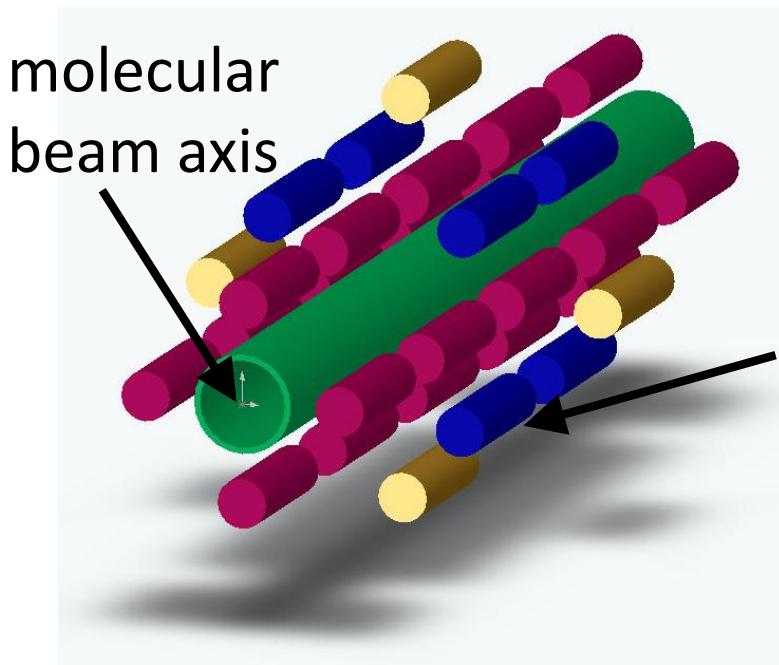
ZOMBIES experimental schematic



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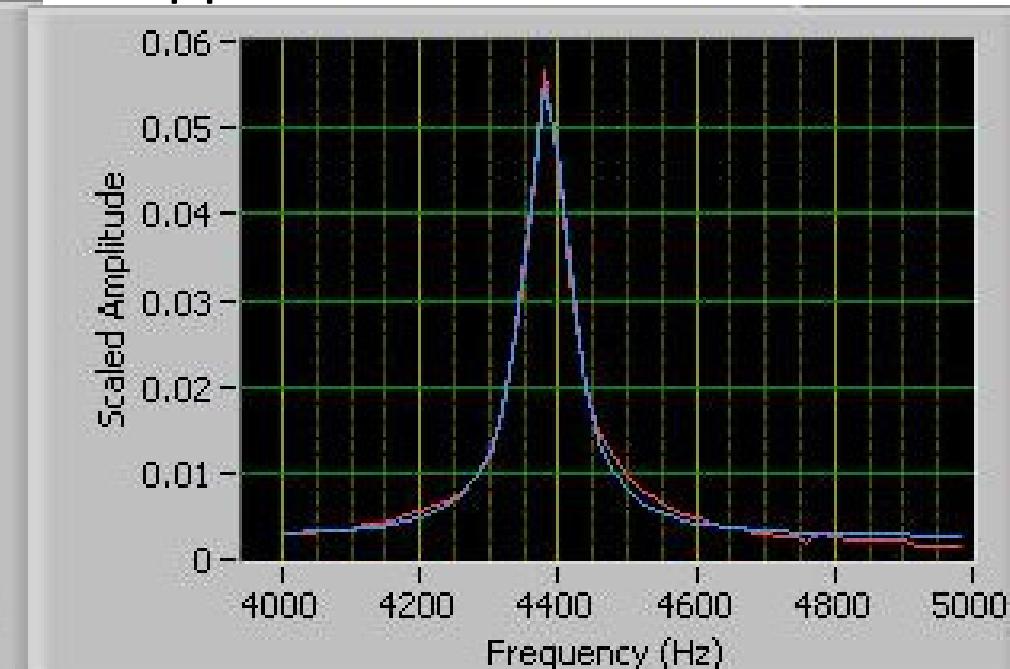
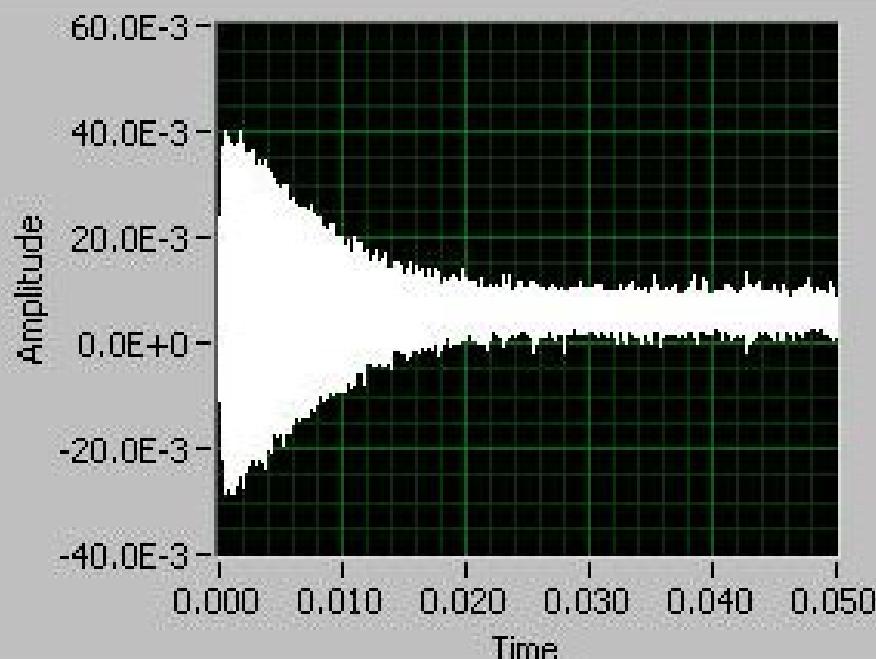
Magnetic field measurement (1st layer)



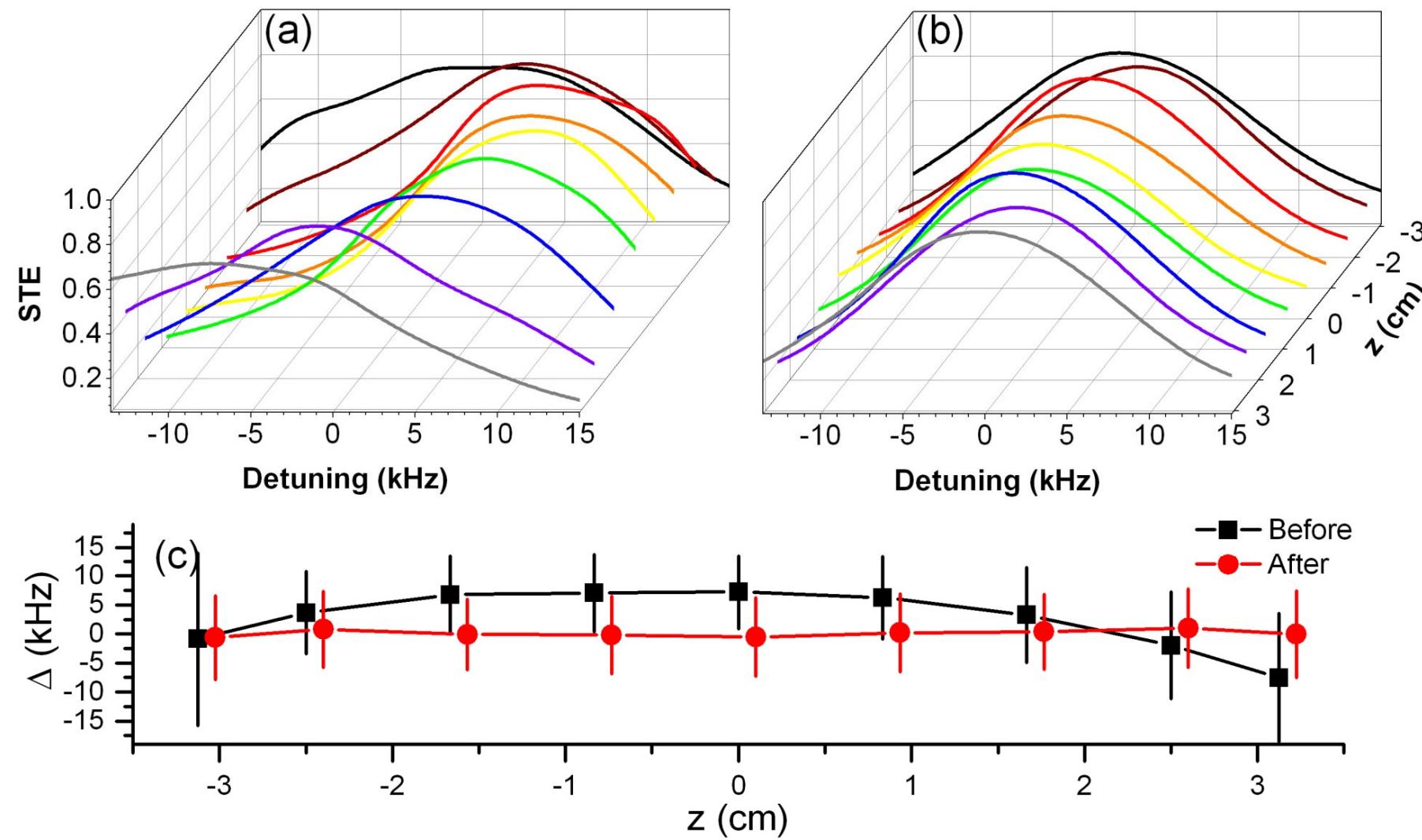
broadband probe on flex circuit



FID trace + FFT fit: $\delta B/B = 0.01$ ppm in one 60 ms shot



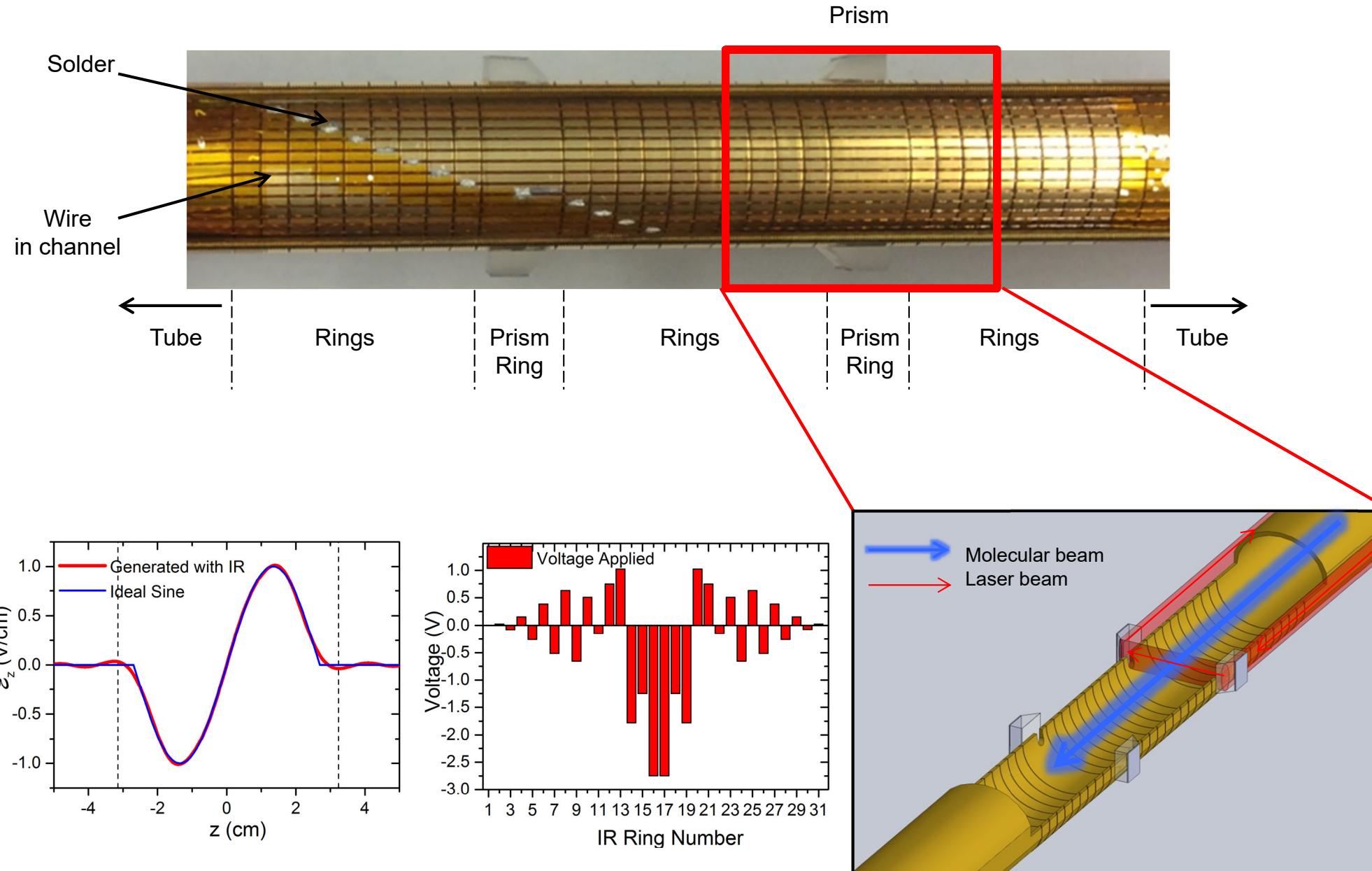
Magnetic field control (2nd layer): results with 52 shim coils



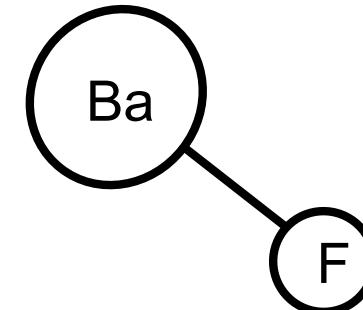
Using molecules for final measurement & shimming:
r.m.s. variation $\delta B/B < 20$ ppb [6 cm L. x 1 cm D. cylinder]

\mathcal{E} -field control

Ring electrodes create sine wave \mathcal{E} -field along **z**-axis:



ZOMBIES I: NSD-PV with BaF



Initial physics goal: NSD-PV with ^{137}BaF

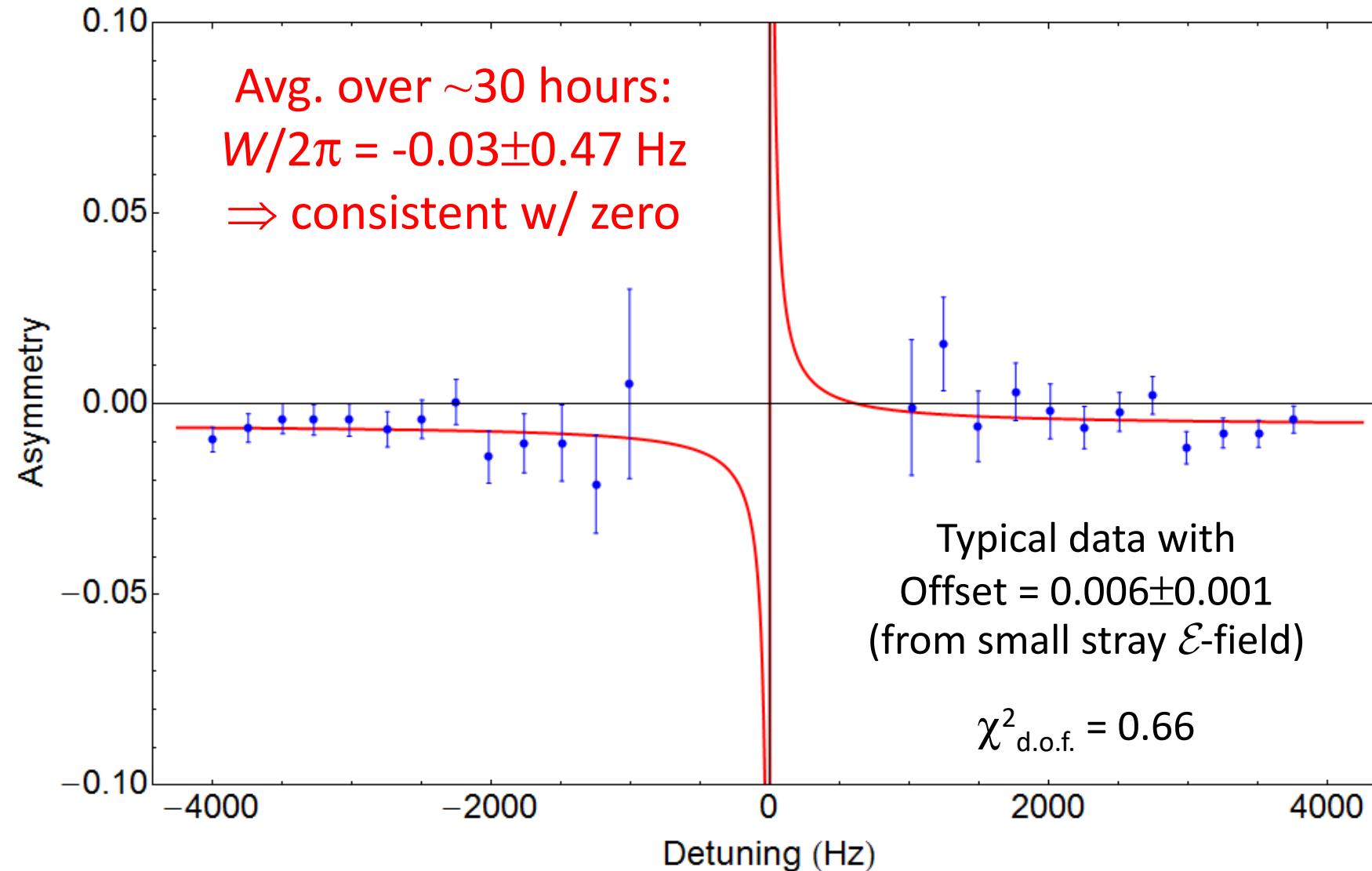
- Odd neutron (vs. ^{133}Cs w/odd proton)
- Heavy → large effect, anapole term dominates
- Large enough natural abundance 11%
- Required lasers = simple, cheap diodes

Completed: proof of principle using $^{138}\text{Ba}^{19}\text{F}$

- Larger natural abundance (~75% vs ~11% for ^{137}Ba)
- Uses same beam source, lasers, magnet, etc. as ^{137}BaF
- $W(^{138}\text{Ba}) = 0 \text{ Hz}$ (no unpaired nucleons = no NSD-PV)
 $W(^{19}\text{F}) \approx 0.002 \text{ Hz} \approx 0$ (light, small electron spin density in BaF)
- **Test for practical sensitivity & systematics with known answer**

Typical asymmetry data from proof of principle run with $^{138}\text{Ba}^{19}\text{F}$

Null signal expected for ^{19}F nucleus



Uncertainties in proof-of-principle with ^{138}BaF

Strategy

- Deliberately exaggerate possible imperfections by known, large factor
- Measure effect on the NSD-PV matrix element W from coupling to ambient imperfections in the experiment

Parameter	Shift	Systematic δW_{sys} (Hz)	Uncertainty
Bipolar \mathcal{E}_{nr} Pulses		0.12	
Unipolar \mathcal{E}_{nr} Pulses		0.16	
\mathcal{B} -Field Inhomogeneities		0.24	
$\delta\nu_{L2}$ and \mathcal{E}_{nr} at and near Gap 22	-0.04	0.21	
Total Systematic	-0.04	0.38	

Uncertainties in proof-of-principle with ^{138}BaF

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Final Error Budget with $^{138}\text{Ba}^{19}\text{F}$

Crossing	$W/(2\pi)$ (Hz)	C	d (Hz/(V/cm))	$W_{\text{mol}} = \kappa' W_P/(2\pi)$ (Hz)
A	$0.28 \pm 0.49_{\text{stat}} \pm 0.38_{\text{sys}}$	-0.41	3360	$-0.68 \pm 1.20_{\text{stat}} \pm 0.93_{\text{sys}}$
F	$0.01 \pm 0.51_{\text{stat}} \pm 0.38_{\text{sys}}$	+0.39	3530	$0.03 \pm 1.30_{\text{stat}} \pm 0.97_{\text{sys}}$
Weighted Average	-	-	-	$-0.36 \pm 0.88_{\text{stat}} \pm 0.95_{\text{sys}}$

~170 h data
~ 6×10^7 molecules total

$$W_{\text{mol}} = 2\pi \times (-0.36 \pm 1.29) \text{ Hz}$$

What does the $^{138}\text{Ba}^{19}\text{F}$ result mean?

$$W_{mol} \equiv (\kappa'_2 + \kappa'_a) W_P = 2\pi \times (-0.36 \pm 1.29) \text{ Hz}$$

Most useful comparison:

$$W_P \left(^{137}\text{Ba in BaF} \right) = 2\pi \times 160 \text{ Hz}$$

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Same experimental uncertainty in ^{137}BaF would mean

$$\delta\kappa'(^{137}\text{Ba}) = 0.008 \quad \text{vs. } \kappa'(^{137}\text{Ba})[\text{single particle + shell model}] \approx 0.07$$

~10% of predicted value

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C.S. Wood *et al.*, Science **275**, 1759 (1997)

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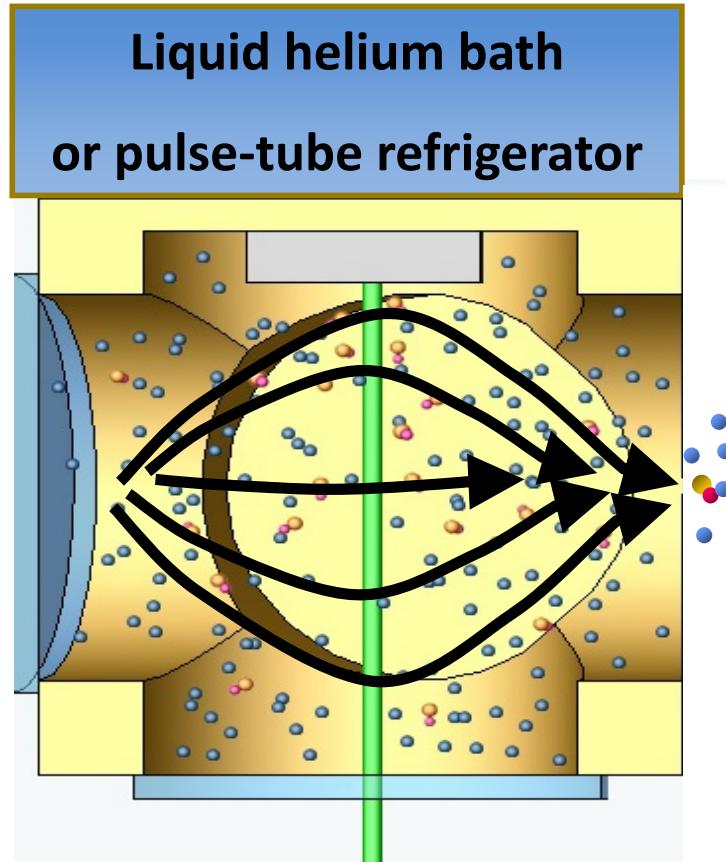
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C.S. Wood *et al.*, Science **275**, 1759 (1997)

- Unprecedented sensitivity to NSD-PV
- General technique enables measurements in broad range of nuclei

Newly added: Cryogenic Buffer Gas-cooled Beam (CBGB)

[S. Maxwell *et al.* PRL 2005; D. Patterson & J. Doyle J Chem Phys 2007;
J. Barry, DD, *et al.* PCCP 2011; N. Hutzler, DD, J. Doyle *et al.* PCCP 2011]

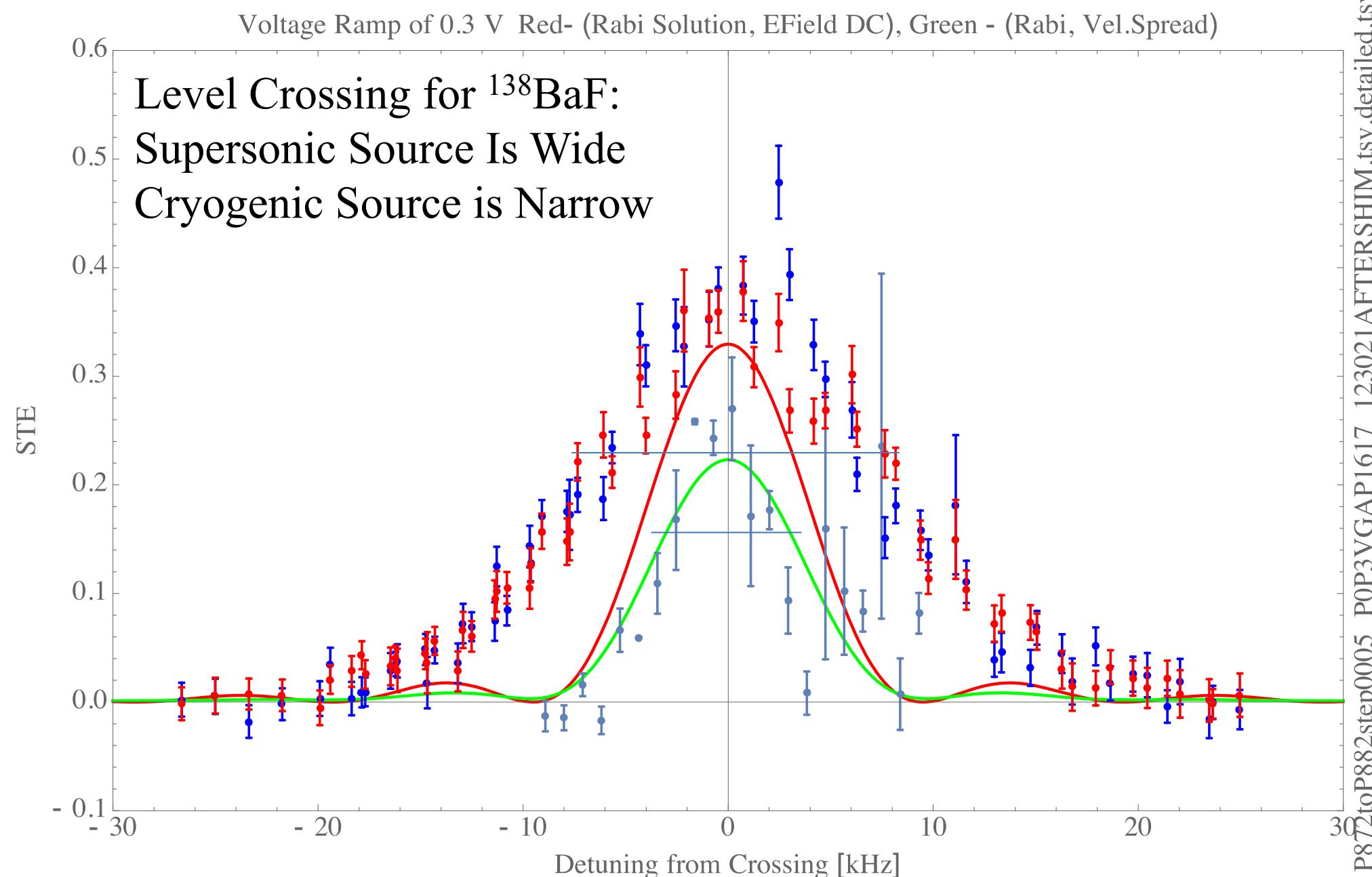


- Inject hot molecules (e.g. via laser ablation)
- Cool w/cryogenic buffer gas @ high density
- Efficient extraction to beam via “wind” in cell: $10^{-4} \rightarrow 10\%-40\%$
- “Self-collimated” by extraction dynamics
- Rotational cooling in expansion: $T \sim 1-4$ K
- Moderately slow: $v \sim 200$ m/s

Low velocity → interaction time $\sim 3\times$ larger;
Beam brightness $\sim 2\times$ larger flux observed SO FAR (but expected 10-100x....?)
Will enable magnetic focusing ⇒ $\sim 10\times$ flux

Gain in NSD-PV statistical sensitivity: 5x now, $>30\times$ anticipated

Demonstrated: Better Energy Resolution with CBGB



ZOMBIES: general-purpose technique, applicable to many isotopes

PRL 100, 023003 (2008)

PHYSICAL REVIEW LETTERS

week ending
18 JANUARY 2008

Using Molecules to Measure Nuclear Spin-Dependent Parity Violation

D. DeMille,¹ S. B. Cahn,¹ D. Murphree,¹ D. A. Rahmlow,¹ and M. G. Kozlov²

Nucleus	I	ν	ℓ	n.a. (%)	$100\kappa'_a$	$100\kappa'_2$	Species	B_e (MHz)	$\mathcal{B}_0^{(m)}$ (T)	W_P (Hz)	$\tilde{C}^{(m)}$	$W^{(m)}$ (Hz)
$^{87}\text{Sr}_{38}$	9/2	N	4	7.0	-3.6	-5.0	SrF	7515	0.62	65	-0.40	2.2
$^{91}\text{Zr}_{40}$	5/2	N	2	11.2	-3.5	-5.0	ZrN	14468	1.20	99	-0.40	3.4
$^{137}\text{Ba}_{56}$	3/2	N	2	11.2	+4.2	+3.0	BaF	6480	0.32	164	-0.44	-5.2
$^{171}\text{Yb}_{70}$	1/2	N	1	14.3	+4.1	+1.7	YbF	7246	0.33	729	-0.52	-22
$^{27}\text{Al}_{13}$	5/2	P	2	100	-11.2	+5.0	AlS	8369	0.52	10	-0.42	0.3
$^{69}\text{Ga}_{31}$	3/2	P	1	60.1	-19.6	+5.0	GaO	8217	0.49	61	-0.43	3.8
$^{81}\text{Br}_{35}$	3/2	P	1	49.3	-21.8	+5.0	MgBr	4944	0.34	18	-0.42	1.3
$^{139}\text{La}_{57}$	7/2	P	4	99.9	+34.7	-3.9	LaO	10578	0.25	222	-0.43	-29

Improved understanding of molecular structure since 2008
→ even more viable molecule species to study many different nuclei

Viable nuclei for anapole/NSD-PV measurement with ZOMBIES

- 10% measurement possible with demonstrated sensitivity, $\lesssim 100$ h data
 - Requires systematics $\sim 2\text{-}10x$ better
 - Statistics likely OK, will require systematics $\sim 100x$ better

58	59	60	61	62	63	64	65	66	67	68	69	70	71
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
90	91	92	93	94	95	96	97	98	99	100	101	102	103
Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

Beyond ZOMBIES: next-gen NSD-PV measurements with light nuclei

PRL 100, 023003 (2008)

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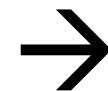
F at lower ν [31]. Alternatively, it might be possible to increase T using trapped molecular ions [32]. Such improvements, plus more spectral data for similar molecular species, could widen the list of accessible nuclei. For light molecules and nuclei, *ab initio* electronic and nuclear structure calculations may be possible at accuracies better than those envisioned here. Ultimately, the method might extend to direct measurement of κ' for ^1H and ^2H . For

See Ronald Garcia-Ruiz plenary talk
this morning

Towards measurements of symmetry-violating nuclear properties using single molecular ions in a Penning trap

J Karthein, D DeMille, J Dilling, R Garcia Ruiz, N Hutzler, P Mohapatra, Scott Moroch, Ryan Ringle, Silviu-Marian Udrescu
Bulletin of the American Physical Society 66 2021

- MUCH longer interaction time,
MUCH smaller experimental volume,
very advanced techniques w/single ions in
Penning traps



- MUCH better sensitivity (sufficient for p,d...?)
AND
ability to probe short-lived radioactive isotopes

First glimmers: reliable HPV→NSD-PV calculations in nuclei?

PHYSICAL REVIEW A **102**, 052828 (2020)

Editors' Suggestion

Nuclear spin-dependent parity-violating effects in light polyatomic molecules

Yongliang Hao ,¹ Petr Navrátil ,² Eric B. Norrgard ,³ Miroslav Iliaš ,⁴ Ephraim Eliav,⁵ Rob G. E. Timmermans ,¹ Victor V. Flambaum ,⁶ and Anastasia Borschevsky ,^{1,*}

III. NO-CORE SHELL-MODEL NUCLEAR CALCULATIONS

	⁹ Be	¹³ C	¹⁴ N	¹⁵ N	²⁵ Mg
I^π	$3/2^-$	$1/2^-$	1^+	$1/2^-$	$5/2^+$
$\mu^{\text{exp.}}$	-1.177 ^a	0.702 ^b	0.404 ^c	-0.283 ^d	-0.855 ^e
NCSM calculations					
μ	-1.05	0.44	0.37	-0.25	-0.50
κ_A	0.016	-0.028	0.036	0.088	0.035
$\langle s_{p,z} \rangle$	0.009	-0.049	-0.183	-0.148	0.06
$\langle s_{n,z} \rangle$	0.360	-0.141	-0.1815	0.004	0.30
κ_{ax}	0.035	-0.009	0.0002	0.015	0.024
κ	0.050	-0.037	0.037	0.103	0.057

- First No-Core Shell Model calculations of anapole moments and $V_e A_N$ effects
- Significant differences from single-particle SM estimates

- Magnetic moment as benchmark

present calculations, we can be optimistic that uncertainties of nuclear calculations for light nuclei can be reduced to $\sim 10\%$ once the above improvements are implemented. The NCSM

ZOMBIES Past & Present

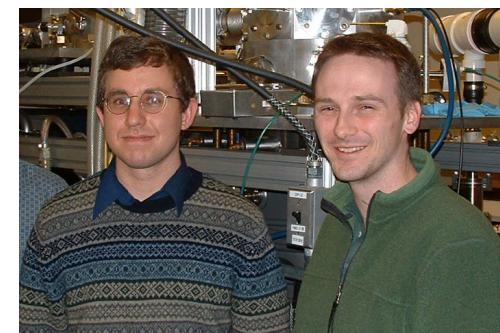
Emine Altuntas



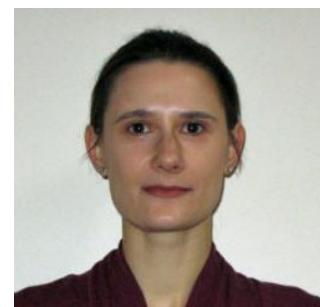
Jeffrey Ammon



David Rahmlow,
Dennis Murphree



Dr. Yulia
Gurevich



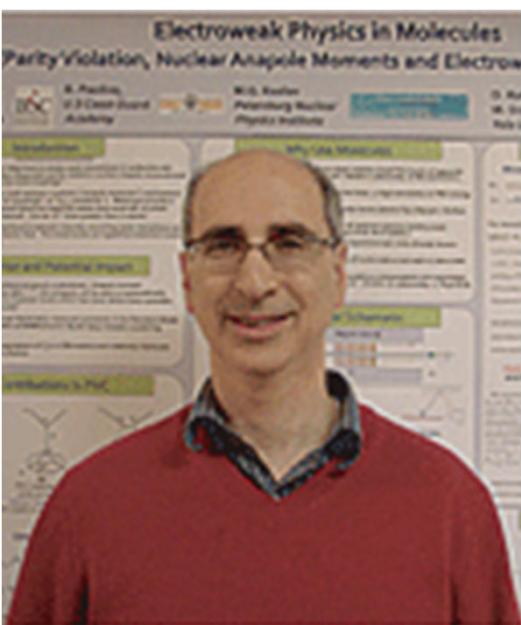
Dr. Emil
Kirilov



Dr. Max
Beyer



Sidney Cahn
(Yale)



Sidney Cahn
(Yale)

Dr. Mangesh
Bhattarai

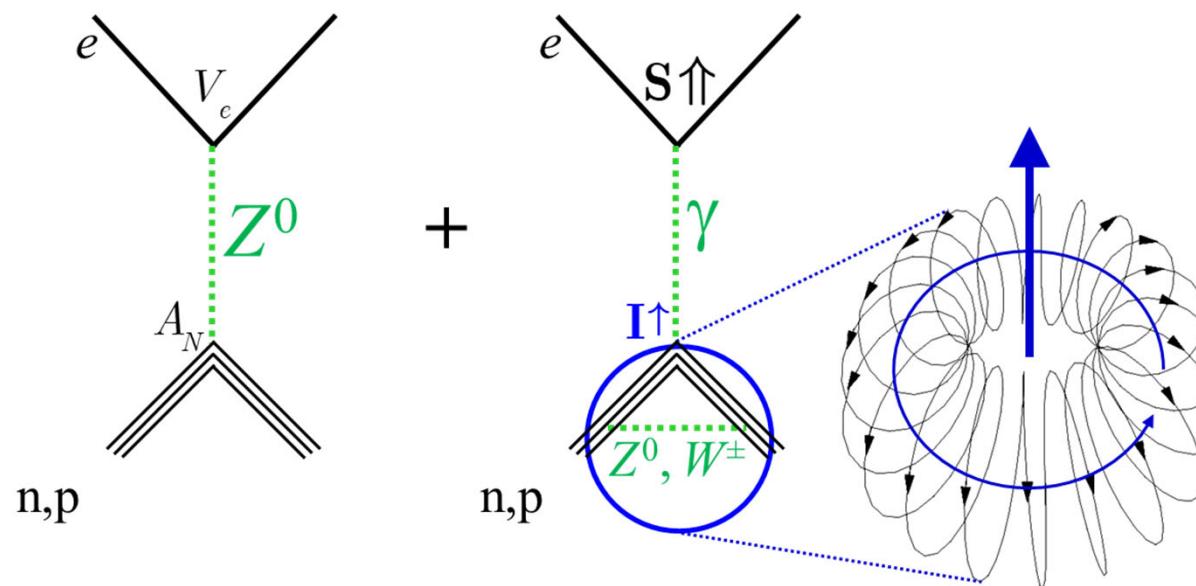


Tanvi Deshmukh



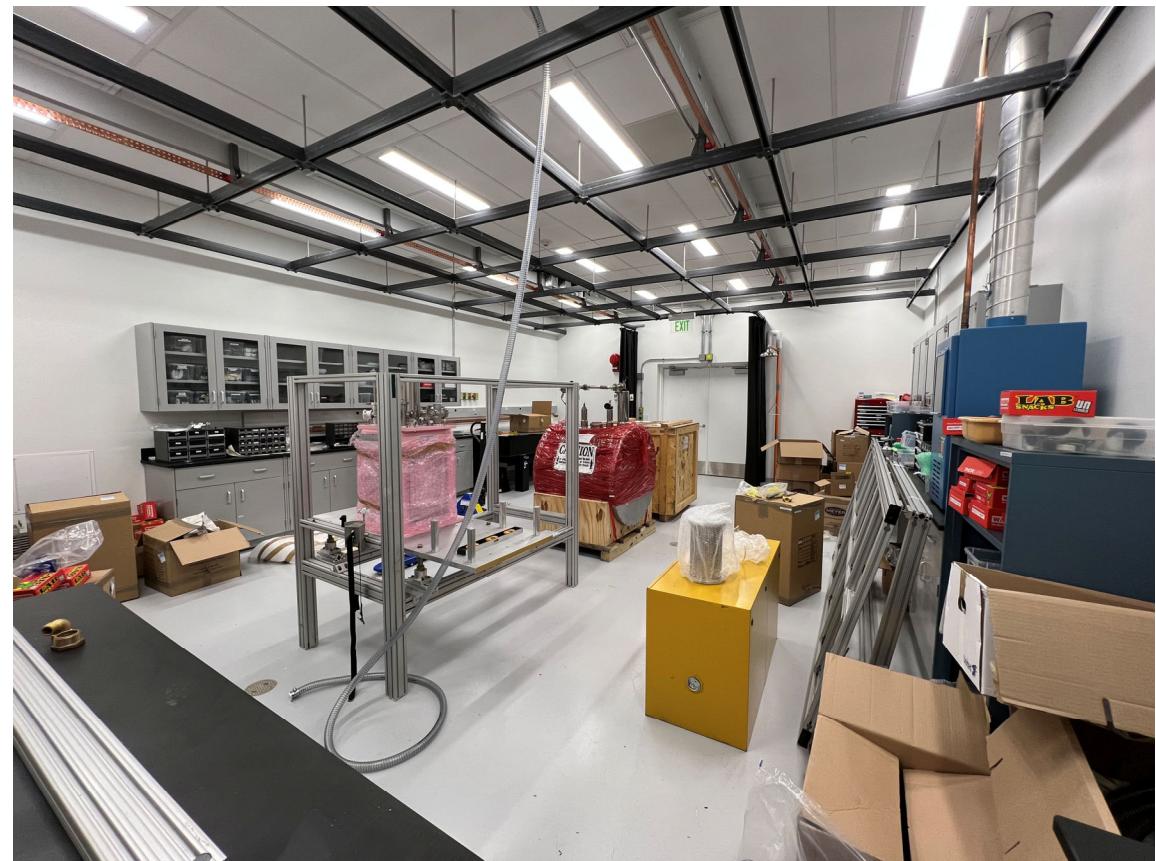
ZOMBIES: Summary & Outlook

- New era in NSD-PV: anapole + $V_e A_N$ measurements beginning
 - Sensitivity & accuracy of molecular systems likely to enable measurements on many nuclei, including lighter isotopes, with <10% uncertainty
- Complementary to other hadronic PV experiments & SoLID/PVDIS @ JLab
 - NSD-PV poised to open new window to unified understanding of hadronic PV & semileptonic neutral-current PV, in strongly-interacting environment, across wide range of scales

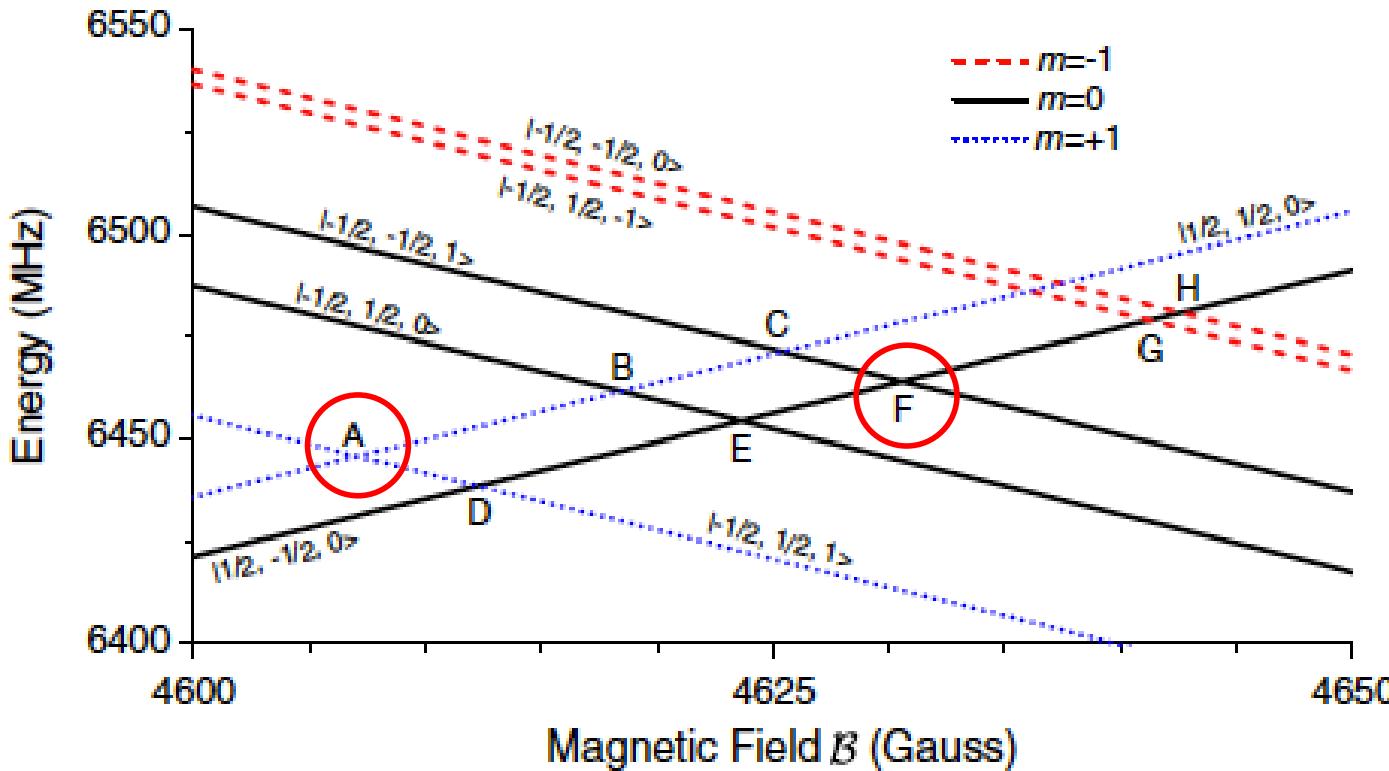


Extra Slides

ZOMBIES Re-assembly Underway at Argonne!



Different level crossings to suppress systematics



$|m_S, m_I, m_N\rangle$

S : electron spin

I : nuclear spin

N : rotation

n : molecular axis

$$W \equiv \langle +\uparrow |H_{PV}|-\downarrow \rangle$$

Measured quantity,
different for each crossing

Molecular wavefunctions:
same at all crossings,
accurately computed

$$W = W_P (K'_2 + K'_a) \left\langle (\hat{n} \times \vec{S}) \cdot \vec{I} \right\rangle$$

NSD-PV
parameters:
same at all
crossings

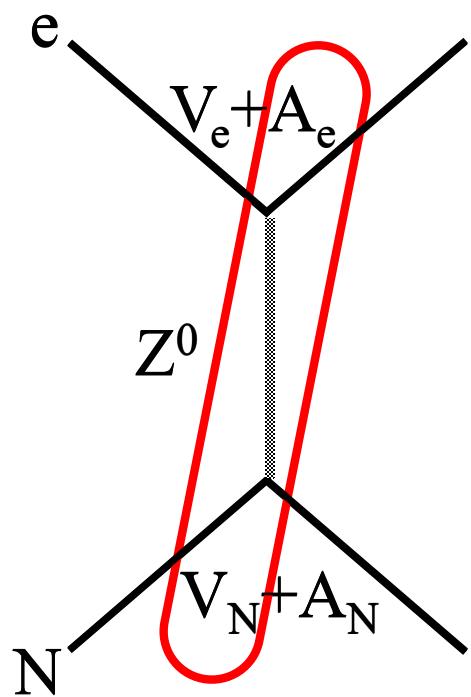
- Angular factor:
- Different for each crossing (sign & magnitude)
 - Analytically calculable

Ongoing or proposed anapole-sensitive experiments with atoms

- Mainz: ^{171}Yb , ^{173}Yb atoms (similar to JILA Cs experiment)
 - FrPNC @ TRIUMF: ^{xxx}Fr atoms (laser cooled & trapped)
 - Mainz: new ideas using NMR signals for light nuclei....?
- Mainz + ANL: use CeNTREX apparatus in different mode (AC \mathcal{E} -field)...?

Mechanisms for atomic/molecular parity violation

Axial electron-vector nucleon interaction



Coherent coupling
to all nuclei =
“weak charge”
 $Q_w = -N + (1-4\sin^2\theta_w)Z$

$A_e V_N$ interaction →
atomic Hamiltonian

$$H \propto Q_w G_F (\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

axial vector
associated with electron

short-range
Yukawa potential

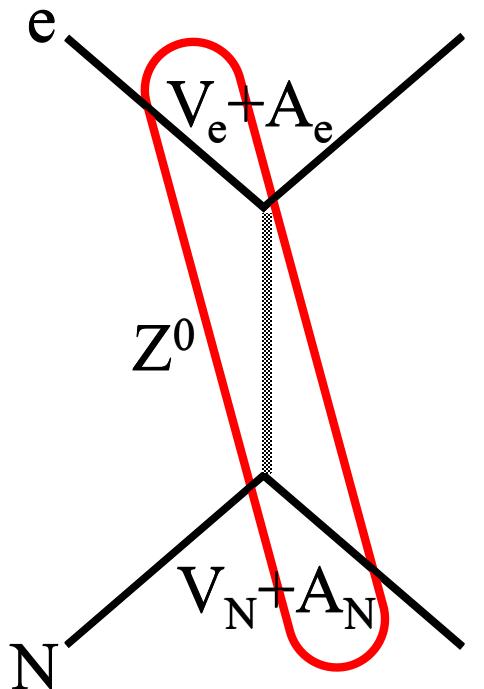
Q_w measured to 0.4%
[C. Wieman group, 1997]

& interpreted at 0.3% level
[A. Derevianko 2010,
V. Flambaum 2012, ...]

⇒ Running of $\sin^2\theta_w$ &
Limits on Z' bosons

Mechanisms for atomic/molecular parity violation

Vector electron-axial nucleon interaction



Coupling ONLY
to unpaired nucleon
coupling constant C_2

$V_e A_N$ interaction \rightarrow Hamiltonian:
$$H \propto C_2 G_F (\vec{\sigma} \cdot \vec{I})(\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

Nuclear spin I
= axial vector
associated with nucleon

C_2 numerically small:
 $V_e/A_e = (1-4\sin^2\theta_W) \sim .08$

Bottom line:

$V_e A_N / A_e V_N \sim 10^{-3}$
(for heavy atoms)

Anapole moments in DDH parameterization

Nuclear anapole moments

W. C. HAXTON, C.-P. LIU, AND M. J. RAMSEY-MUSOLF

PHYSICAL REVIEW C **65** 045502

TABLE VII. PNC observables and corresponding theoretical predictions, decomposed into the designated weak-coupling combinations.

Observable	Expt. ($\times 10^7$)	$f_\pi - 0.12h_\rho^1 - 0.18h_\omega^1$	$h_\rho^0 + 0.7h_\omega^0$	h_ρ^1	h_ρ^2	h_ω^0	h_ω^1
$A_L^{pp}(13.6)$	-0.93 ± 0.21		0.043	0.043	0.017	0.009	0.039
$A_L^{pp}(45)$	-1.57 ± 0.23		0.079	0.079	0.032	0.018	0.073
$A_L^{pp}(221)$	0.84 ± 0.34		-0.030	-0.030	-0.012	0.021	
$A_L^{pa}(46)$	-3.34 ± 0.93	-0.340	0.140	0.006		-0.039	-0.002
$P_\gamma(^{18}\text{F})$	1200 ± 3860	4385		34			-44
$A_\gamma(^{19}\text{F})$	-740 ± 190	-94.2	34.1	-1.1		-4.5	-0.1
$\langle A_1 \rangle/e, \text{ Cs}$	800 ± 140	60.7	-15.8	3.4	0.4	1.0	6.1
$\langle A_1 \rangle/e, \text{ T1}$	370 ± 390	-18.0	3.8	-1.8	-0.3	0.1	-2.0

3 contributions to NSD-PV: scaling with Z & A

$$H_{NSD-PV} \propto (\kappa'_2 + \kappa'_a + \kappa'_Q) G_F (\vec{\sigma} \cdot \vec{I}) (\vec{\sigma} \cdot \vec{p}) \delta^3(\vec{r})$$

$$\kappa'_{2P} = -\kappa'_{2N}$$

$$\approx -g_A (1 - 4 \sin^2 \theta_W)/2 \approx -.05$$

- \sim independent of A
- $\mathcal{O}(20\%)$ corrections from SU(3)_f
- $\mathcal{O}(100\%)$ expt. uncertainty
- Quenching in larger nuclei like g_A ?

Overall Z^2

$\kappa'_Q \propto A^{2/3}$ small ($< \kappa'_a/4$)
& well understood
--ignore

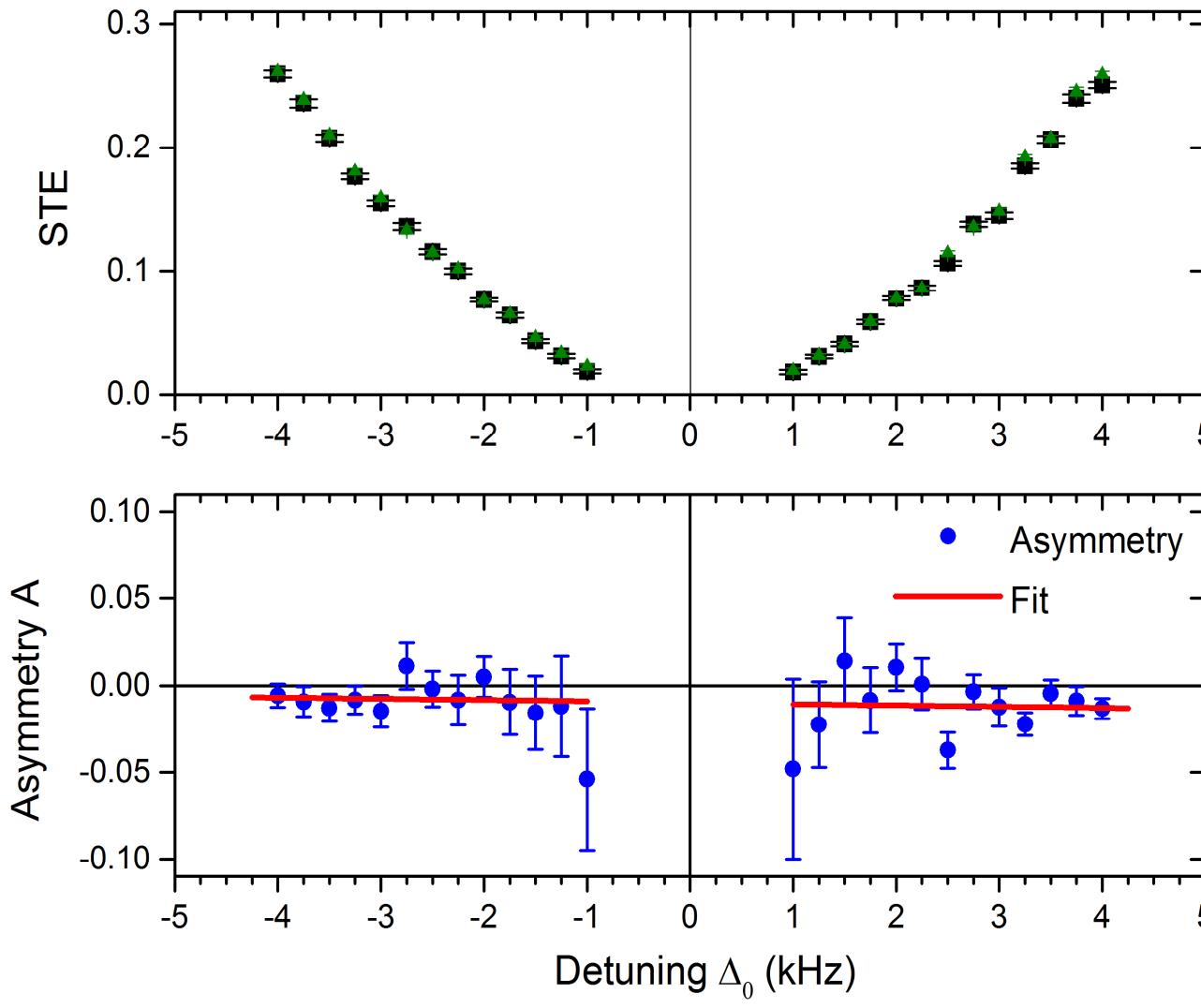
Simple shell model:
valence nucleon over closed core

$$\kappa'_a \approx \frac{9}{10} \frac{\alpha \mu}{m r_0} A^{2/3} g_{eff} \approx .05 g_{eff} \left(\frac{A}{50} \right)^{2/3}$$

$$g_{eff,p} \approx 4 - 6; g_{eff,n} \approx 0.1 - 1;$$

NSD-PV data with $^{138}\text{Ba}^{19}\text{F}$

- Measure, cancel, & remeasure \mathcal{B} -field gradients and non-reversing \mathcal{E} -fields to suppress possible systematics
 - Measure NSD-PV signal & asymmetry



$$S \propto \sin^2\left(\Delta \frac{T}{2}\right) \left(\frac{d\mathcal{E}_0}{\omega}\right)^2$$

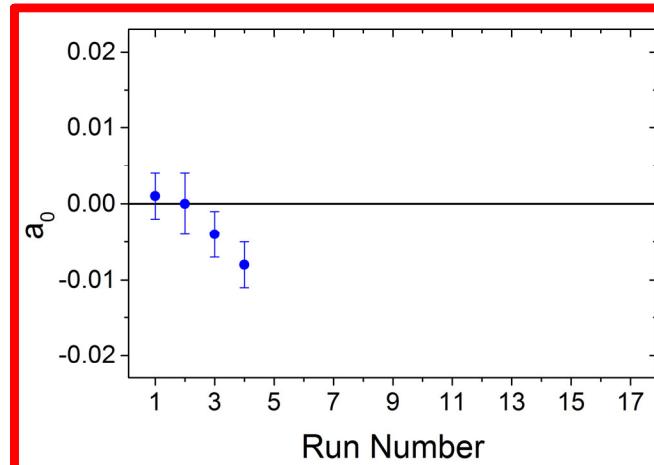
$$\mathcal{A} = \frac{S(+\mathcal{E}_0) - S(-\mathcal{E}_0)}{S(+\mathcal{E}_0) + S(-\mathcal{E}_0)}$$

Fit to function

$$\mathcal{A}_{\text{fit}}(\Delta) = 2 \frac{W_{\text{fit}}}{\Delta} \frac{\omega}{d\mathcal{E}_0} + a_0 + a_1 \Delta$$

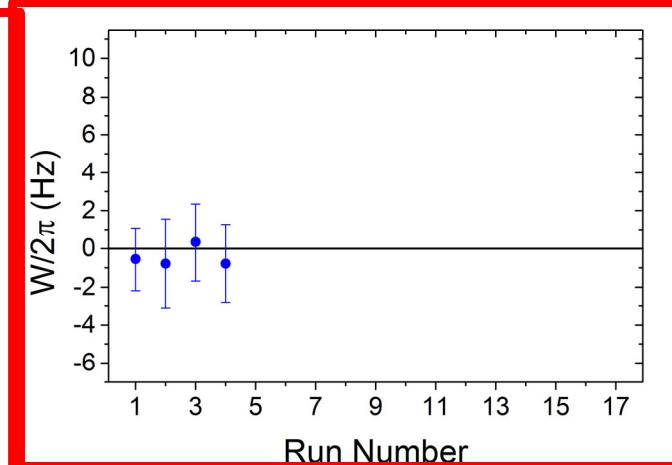
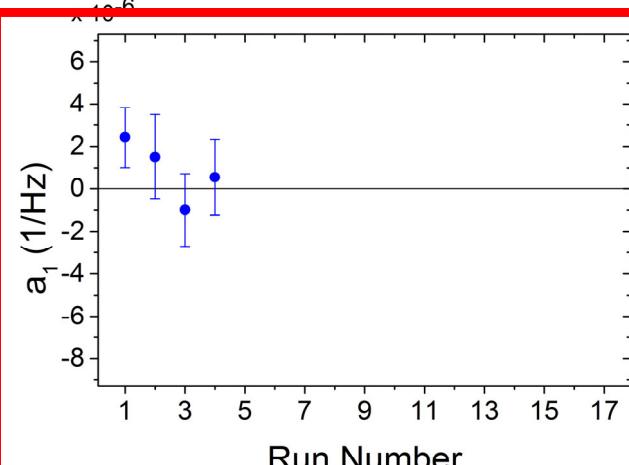
NSD-PV data with $^{138}\text{Ba}^{19}\text{F}$

from stray \mathcal{E} -fields alone

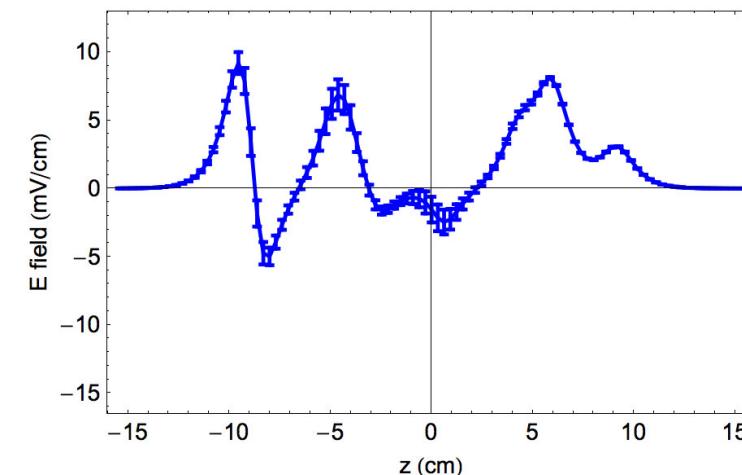


$$\text{Fit to } \mathcal{A}_{\text{fit}}(\Delta) = 2 \frac{W_{\text{fit}}}{\Delta} \frac{\omega}{d\mathcal{E}_0} + a_0 + a_1 \Delta$$

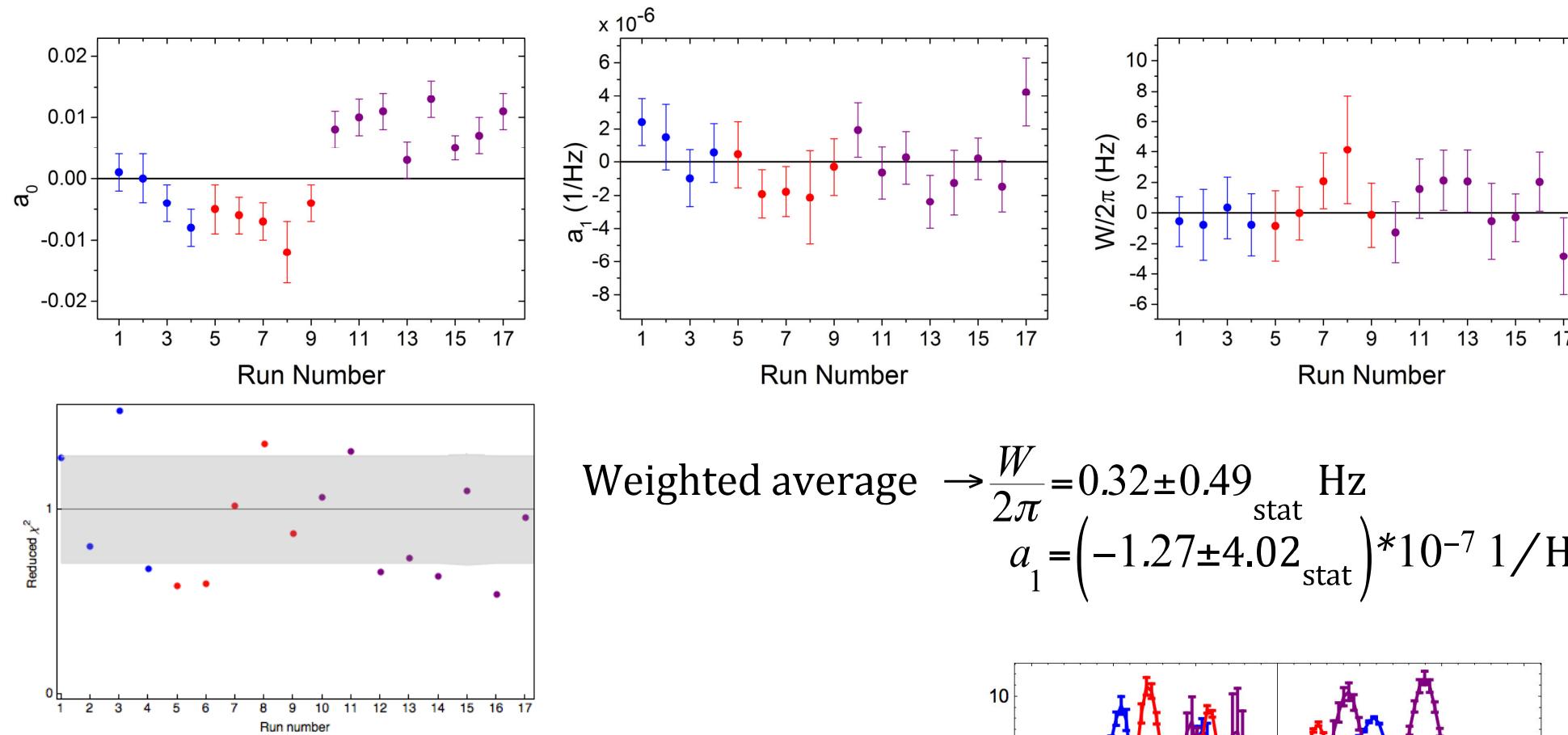
From combined
stray \mathcal{E} -fields & \mathcal{B} -field gradients



- stray \mathcal{E} -fields always below 15mV/cm

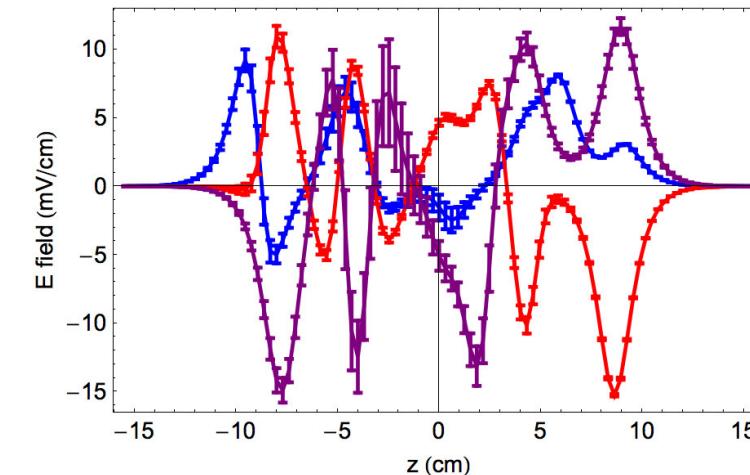


NSD-PV data with $^{138}\text{Ba}^{19}\text{F}$

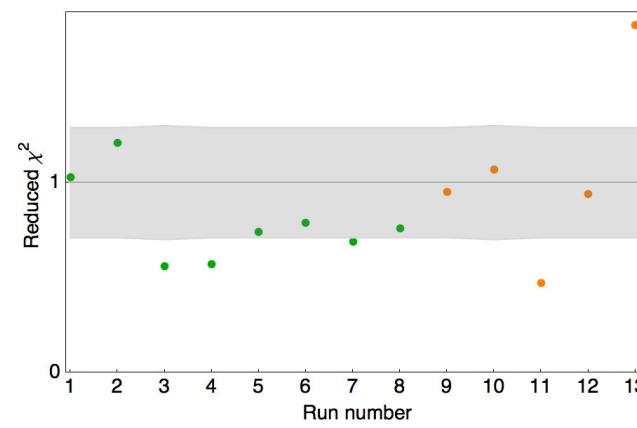
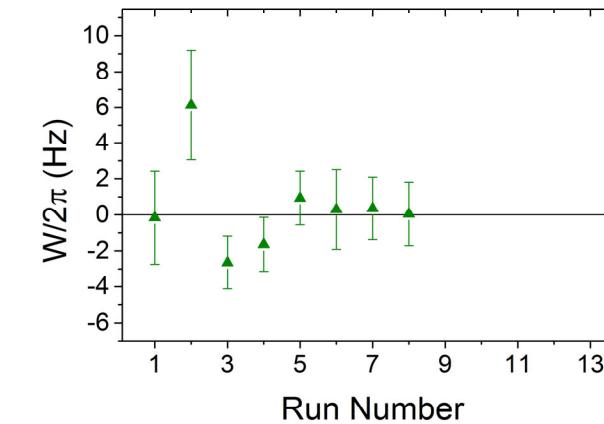
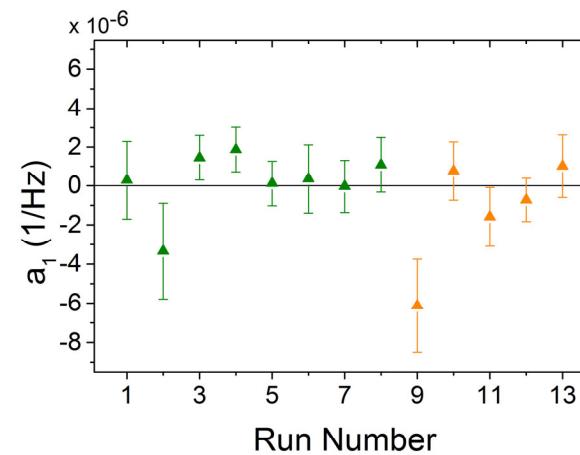
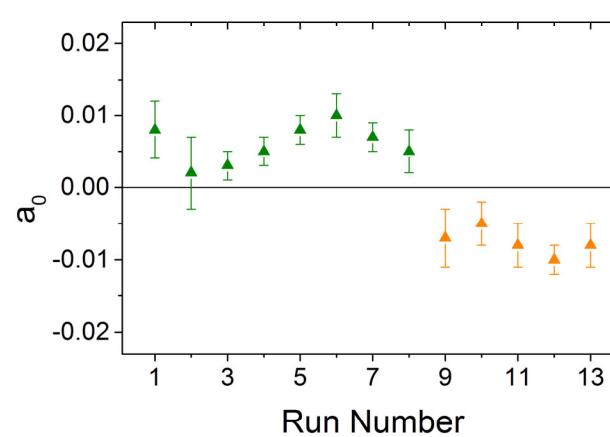


Weighted average $\rightarrow \frac{W}{2\pi} = 0.32 \pm 0.49_{\text{stat}} \text{ Hz}$
 $a_1 = (-1.27 \pm 4.02_{\text{stat}}) * 10^{-7} \text{ 1/Hz}$

- ^{138}BaF expected $W = 0$
- Measured with 3 different stray \mathcal{E} -fields
(all below 15 mV/cm)
- a_1 terms consistent with zero: no systematics

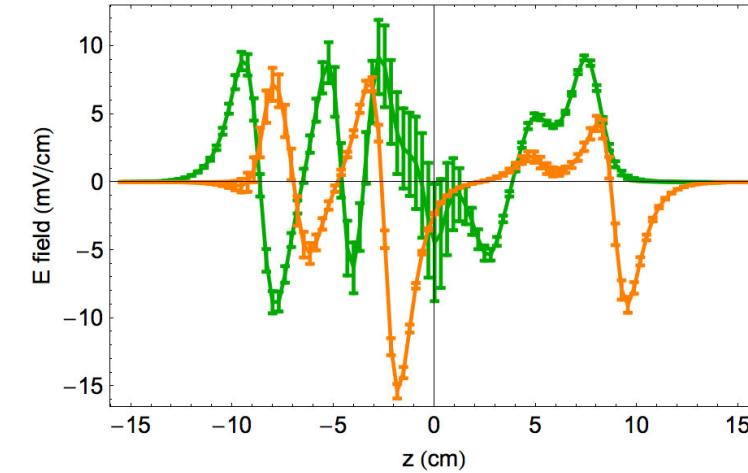


NSD-PV data with $^{138}\text{Ba}^{19}\text{F}$: 2nd crossing $W \rightarrow -W$



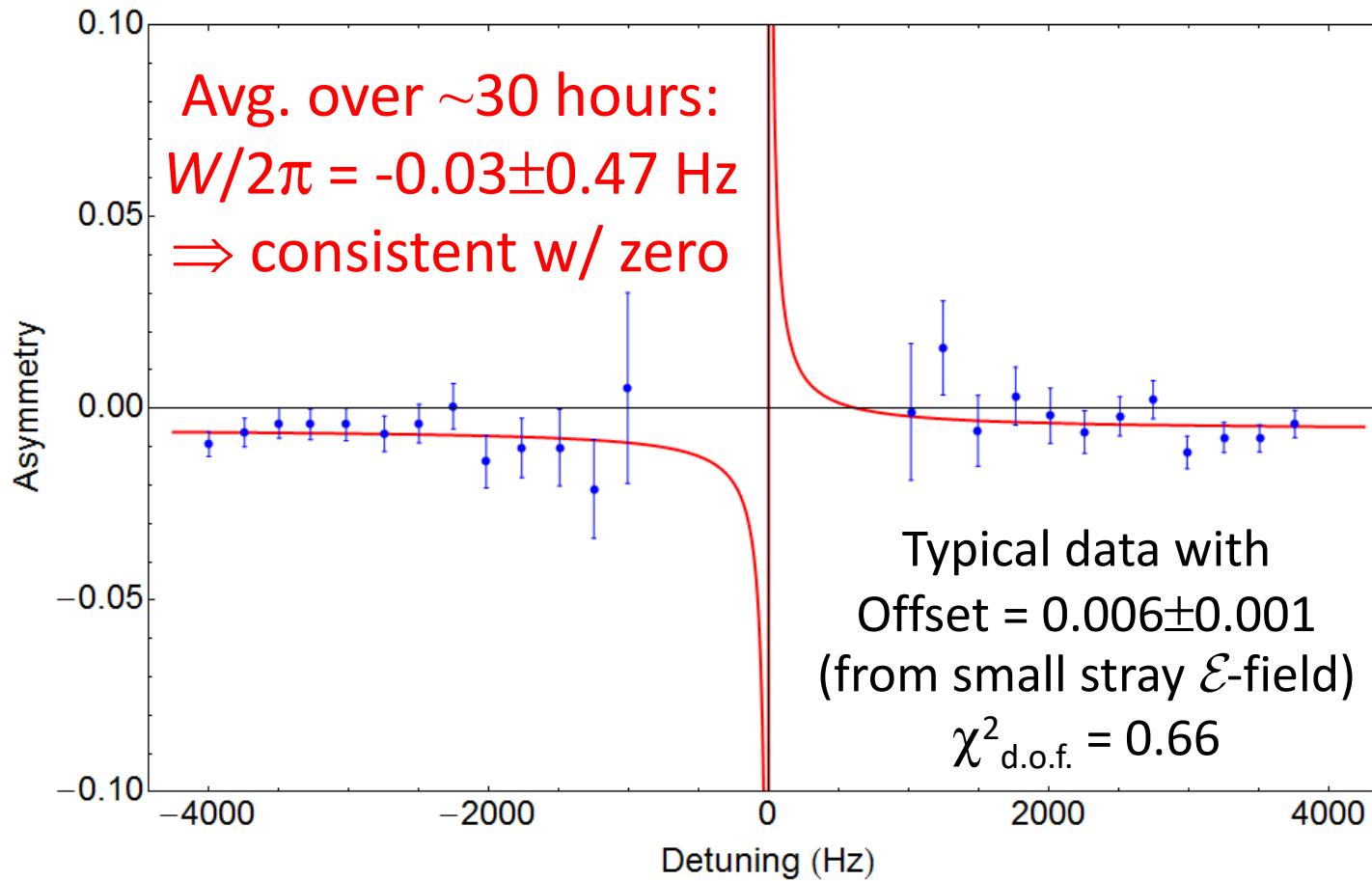
Weighted average $\rightarrow \frac{W}{2\pi} = 0.05 \pm 0.51_{\text{stat}} \text{ Hz}$
 $a_1 = (-1.69 \pm 3.98_{\text{stat}}) * 10^{-7} \text{ 1/Hz}$

- ^{138}BaF expected $W = 0$
- Measured with 2 different stray E-fields (all below 15mV/cm)
- No systematics $\rightarrow a_1$ terms consistent with zero



Recent PV data with $^{138}\text{Ba}^{19}\text{F}$

Proof of concept run (null signal expected for ^{19}F nucleus)



Statistical uncertainty $\delta W = 0.5 \text{ Hz}$ [\sim 30 hours data]

- \sim 60 \times more sensitive than best atomic experiment (Wieman, ^{133}Cs)
 - Sufficient to measure effect in many heavy nuclei & several light nuclei w/anticipated technical upgrades

Questions/requests for theorists

- Calculations with new HPV parameterization
- Calculate lightest nuclei (accessible via no-core shell model...?)
 - Quantitative uncertainties on calculations!
 - Could C_2 values be extracted reliably from light nuclei with existing HPV data & understanding?
- Is consistency check between isotopes in heavier nuclei useful?
 - special cases of particular interest?
(e.g. ^{19}F ... can it be calculated accurately?)
- Can anapole measurements (with known inputs) shed light on other related calculations e.g. Schiff moment, $0\nu\beta\beta$ decay, ...?
- Generally: modern theory perspective on anapole moments *URGENTLY* needed (>10 years since last nuclear theory paper)