CMPUT 272, Section B2, Second Midterm Examination W. w. Armstrong March 14, 2000

Your name:

Instr	r name:SID:	
you pr slightl exam i	at any time, even while leaving. Don't ask the instructor any questions about s are handed in. If you don't understand a question, make an assumption about rove convincingly there is a mistake in a question, you can also get full marks is open books, open notes.	ule exam until all
Total:	30 points. This is worth 15% of the mark in the course. Time: 45 minutes.	
Comple	ete the following proof in Mizar notation. Minor syntax problems will be ign	
envir	on syntax problems will be ign	ored.
EqualI	reserve A, B, C, x for THING; Def: for A, B holds Equal[A, B] iff (for x holds In[a]	
UnionD	Def: \rightarrow for A, B, C holds iff In[x, B]);	
~ ~ ~ ~ ~ 11	i la	11.
proof	Tot A, B st Equal[A, B] holds Union[A A	, , ,
1101	W TEL M M L - m	r AGES:
iff	(for what	N
2: Equ	(for x holds In[x,M] or In[x,M] iff In[x,N]) by Uni ual[M,N] iff (for x holds In[x,M] iff In[x,N]) by Eq wassume 3: Equal[M,N]; 4: (for x holds In[x,M] iff In[x,N])	OnDef.
ss: no		ualDef;
	s5: now let v be THING.	
	5: In[v.M] iff Tar	•
	thus In[y,M] or In[y,M] iff In[y,N] by 5;	
	6:	
	thus Union[M,M,N] by 1,6;	by s5;
	end;	
thus		
end;		by s3;
•		
thus		
		by s1;
CONTI	NUED ON OTHER SIDE	

CMPUT 272 (B ARMSTRONG, W MAR 00 MIDTERN

Question 2 (6 points) Make two Venn Diagrams of three sets A, B, C in general position inside a unof discourse E. Darken the following areas of the diagrams 1 and 2.	ıniverse

- 1. $(A \cap B \cap C) \cap (A^c \cup B^c \cup C^c) \text{ where the c-superscript means complementation in } E.$
- 2. $((A B) C) \cup ((B C) A)$

Question 3 (4 points) If P(x), Q(x), and R(x) are the indicator functions (or characteristic conditions in GT) of three sets A, B, C respectively, what is the indicator function of $(A \cup B) \cap (E - C)$, where E is the universe of discourse? You can use operations of set theory in defining the indicator function.

Question 4 (6 points)

- a. What exactly is the equivalence class of 16 modulo 7. Use set-builder notation. Let Rem(a,b) denote the smallest non-negative remainder when you divide a by b.
- b. In arithmetic modulo 5, what is [3] + [2] + [4] ? Ans: _____ (smallest non-negative representative please)
- c. In arithmetic modulo 5, what is [3] * [2] * [4] ? Ans: ______(smallest non-negative representative please)

Question 5 (4 points) Use a Venn Diagram to solve the following puzzle:

A history class with 19 people in it have some who are artists, some who are builders, and some who are contractors. These three groups don't overlap except for two people who are artists, builders, and contractors. There are three more artists than there are builders, and there is one fewer contractor than there are builders. How many people are in the class who are artists? Builders? Contractors?