

Problem n.4

The file `power.txt` reports the measurements of the electric power consumption in one household collected every day for one year. Considering a functional data analysis approach, answer to the following questions.

- a) Perform a smoothing of the data using a Fourier basis. Choose the number of basis functions using a generalized cross-validation (GCV) criterion. Report the plot of the values of the GCV statistic as a function of the number of basis functions, the number of basis functions chosen, a plot of the basis system used and a plot of the smoothed data.
- b) Compute an approximation of the first derivative of the curve from the data and the first derivative of the smoothed curve obtained at point (a). Provide a plot to compare the two and comment on the result.
- c) Choose a number of basis functions that you deem appropriate to show the effect of oversmoothing. Report the number of basis functions chosen, provide a plot of the the smoothed data and comment the result.
- d) Choose a number of basis functions that you deem appropriate to show the effect of overfitting. Report the number of basis functions chosen, provide a plot of the the smoothed data and comment the result.

Upload your results here:

<https://forms.office.com/Pages/ResponsePage.aspx?id=K3EXCvNtXUKAjjCd8ope612LHtvIHvFEsEi2L6mhPg1URENHUdcyOUFUTV1SUUVKMUU4RUo2N09GVS4u>