

M2 AIC

TC2: Introduction to Optimization

Black-Box Optimization Benchmarking
with the COCO platform

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Multiobjective Optimizer adaptive IBEA (ϵ -indicator)

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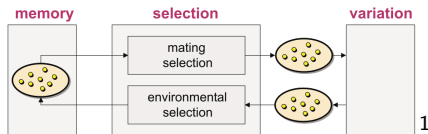
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 - CPU timing and results
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IBEA: Indicator-Based Evolutionary Algorithm

- optimization: find decision space vectors leading to objective space minima
- multiobjective: the objective space is multidimensional
- evolutionary: decision space candidates follows an natural selection-like evolution
- indicator-based: binary quality indicators to compare two Pareto set approximations

Successive steps of IBEA:

- ① Initialization
- ② Fitness assignment
- ③ Environmental selection
- ④ Termination
- ⑤ Mating selection
- ⑥ Variation



¹Illustration from:

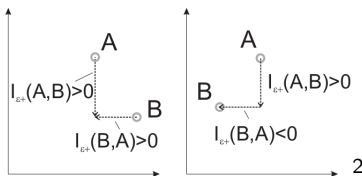
A Tutorial on Evolutionary Multiobjective Optimization - E. Zitzler,
M. Laumanns, and S. Bleuler

- Binary quality indicators:

$$I_{\epsilon^+}(A, B) = \min_{\epsilon} \{ \forall x^2 \in B \exists x^1 \in A : f_i(x^1) - \epsilon \leq f_i(x^2) \text{ for } i \in \{1, \dots, n\} \} \quad (1)$$

- Fitness values:

$$F(x^1) = \sum_{x^2 \in P \setminus \{x^1\}} -e^{-\frac{I(\{x^1\}, \{x^2\})}{ck}} \quad (2)$$



¹Illustration from:

Indicator-Based Selection in Multiobjective Search - E. Zitzler and S. Künzli

Recombination

For recombination, we use a Simulated Binary Crossover (SBX) operator. A uniform probability pick in $[0, 1]$ written u determines the parameter used in computing the features (decision space coordinates) of the children.

- if the uniform probability pick ≤ 0.5 :

$$\beta_q = (2u)^{\frac{1}{\mu+1}} \quad (3)$$

- else:

$$\beta_q = \left(\frac{1}{2(1-u)}\right)^{\frac{1}{\mu+1}} \quad (4)$$

Recombination

Thus, we can compute the children's coordinates:

- first child:

$$child0[j] = 0.5((1 + \beta_q)parent0[j] + (1 - \beta_q)parent1[j]) \quad (5)$$

- second child:

$$child1[j] = 0.5((1 - \beta_q)parent0[j] + (1 + \beta_q)parent1[j]) \quad (6)$$

Mating selection and mutation

Polynomial mutation operator:

The mutation operator modifies individuals by changing small parts in the associated vectors according to a given mutation rate.

- if the uniform probability pick ≤ 0.5 :

$$\sigma_L = (2u)^{\frac{1}{\mu+1}} - 1 \quad (7)$$

$$p_{mut}[j] = ind[j] + \sigma_L(ind[j] - Lo) \quad (8)$$

- else:

$$\sigma_R = (2(1 - u))^{\frac{1}{\mu+1}} \quad (9)$$

$$p_{mut}[j] = ind[j] + \sigma_R(Up - ind[j]) \quad (10)$$

Computer specifications and batch options

- Intel(R) Core(TM) i7-7500U CPU @ 2.70GHz
- Quad core CPU with 16GB RAM

Everything ran with a budget of 100

- Three batches for dimensions 2, 3, 5, 10, 20
- First batch running alone, and two others together
- One batch for dimensions 40

Options chosen to run the algorithm

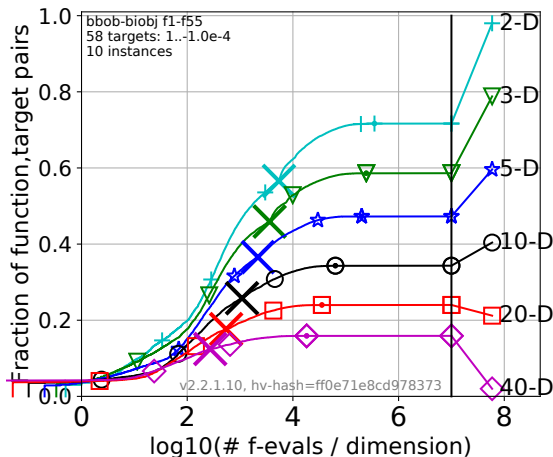
- Population size : 100
- Maximum number of generation : 100
- Scaling factor : 0.05
- Mutation rate : 0.01
- Recombination and mutation μ : 1
- Population initialization in range $(-5, 5)$

Dimension \ Batch	2	3	5
Batch 1 on 3	6.0e-04	6.3e-04	8.1e-04
Batch 2 and 3 on 3 run simultaneously	8.6e-04	8.6e-04	9.1e-04
	8.3e-04	8.4e-04	8.9e-04

Dimension \ Batch	10	20
Batch 1 on 3	8.3e-04	1.1e-03
Batch 2 and 3 on 3 run simultaneously	1.1e-03	1.3e-03
	1.0e-03	1.3e-03

Dimension \ Batch	40
Whole test suite	4.2e-03

Results

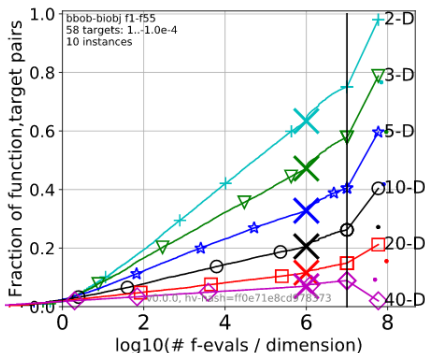


Results analysis

- Comparatively better in higher dimensions
- Results globally good for an EMOA
- More budget could have given better results
- A better initialization of population could lead to a sharper increase at the beginning

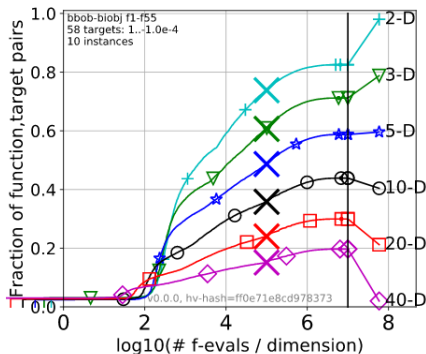
Random Search

- The introduce of Random Search:
- Its effect is directly proportional to its evaluations
- It doesn't work well when the dimension of input is too high



NSGA-II

- The introduce of NSGA-II:
- The gap between our algorithm and it



In our experiments, we majorly focused on the comparison with NSGA-II and Random search:

IBEA VS Random search: IBEA outperformed Random search, a relatively good Pareto set approximation was given by IBEA.

IBEA VS NSGA-II: IBEA performed worse than NSGA-II.

Choosing a representation of the problem addressed, an initial population, a method of selection, a crossover operator, mutation operator, the probabilities of crossover and mutation, and the insertion method creates a variant of MOEAs algorithms.

Non-exhaustive bibliography

- *Indicator-Based Selection in Multiobjective Search* - Zitzler, E. and Künzli, S.
- *A Tutorial on Evolutionary Multiobjective Optimization* - Zitzler, E. and Laumanns, M. and Bleuler, S.
- *Biobjective Performance Assessment with the COCO Platform* - Brockhoff, D. and Tušar, T. and Tušar, D. and Wagner, T. and Hansen, N. and Auger, A.