

Sensitivity to starting point

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Multiple analyses of two catalogues using different initial values

The inlabru algorithm takes an initial guess on the mode of the parameters we are inverting for and iteratively updates this initial guess. There is the potential that there may be bad initial conditions such that they find different solutions and the runtime will differ depending upon how the solution converges.

In this notebook, we explore the robustness of the posteriors on two synthetic catalogues where the true parameters are known. Both catalogues contain 2000 days of data. One catalogue does not contain a large event and the second contains a M6.7 event on day 1000.

```
library(ETAS.inlabru)

library(tidyquant)
library(gridExtra)
library(grid)
library(lemon)
library(ggplot2)
library(ggpubr)
library(GGally)

library(inlabru)
library(INLA)
library(ETAS.inlabru)

# inla.setOption(pardiso.license=~"/sys/licences/pardiso.lic")

library(dplyr)

# Increase/decrease num.cores if you have more/fewer cores on your computer.
# future::multisession works on both Windows, MacOS, and Linux
num.cores <- 2
future::plan(future::multisession, workers = num.cores)
INLA::inla.setOption(num.threads = num.cores)
# To deactivate parallelism, run
# future::plan(future::sequential)
# INLA::inla.setOption(num.threads = 1)
```

Define the parameters for the synthetic catalogues and starting values for inversion

```
# Parameters we use to generate synthetics, which we will refer to as the 'true' parameters
mu <- 0.1
K <- 0.089
```

```

alpha <- 2.29
c <- 0.11
p <- 1.08

# Format the true ETAS parameters for code to generate the synthetics
theta_etas <- data.frame(mu = mu, K = K, alpha = alpha, c = c, p = p)

# A dataframe containing different starting values for the algorithm
startingValues <- data.frame(
  mu = c(5., mu),
  K = c(1., K),
  alpha = c(5., alpha),
  c = c(0.3, c),
  p = c(1.5, p)
)
nRealisations <- length(startingValues$mu)

# Temporal duration of the synthetic catalogue in days
modelledDuration <- 1000 # [days]

# The minimum magnitude that will be modelled
M0 <- 2.5

```

Generate new catalogues and save them

```

#####
#### Generate the first catalogue with no large events

samp.etas.list <- generate_temporal_ETAS_synthetic(
  theta = theta_etas,
  beta.p = log(10), M0 = M0, T1 = 0, T2 = modelledDuration, Ht = NULL
)

quiet.ETAS.cat <- bind_rows(samp.etas.list)
quiet.ETAS.cat <- quiet.ETAS.cat[order(quiet.ETAS.cat$ts), ]
# quiet.ETAS.cat <- na.omit(quiet.ETAS.cat)

```

```

#####
#### Generate the second catalogue with a M6.7 event on day 1000

Ht <- data.frame(ts = c(500), magnitudes = c(6.7)) # Impose a M6.7 event on day 1000

samp.etas.list <- generate_temporal_ETAS_synthetic(theta = theta_etas, beta.p = log(10), M0 = M0, T1 = 0, T2 = modelledDuration, Ht = Ht)

M6p7.ETAS.cat <- bind_rows(samp.etas.list)
M6p7.ETAS.cat <- M6p7.ETAS.cat[order(M6p7.ETAS.cat$ts), ]

```

In this vignette we use Rmd caching, but you can save the catalogues in files explicitly:

```

# save(M6p7.ETAS.cat, file="M6p7_ETAS_cat.Rda")
# save(quiet.ETAS.cat, file="quiet.ETAS_cat.Rda")

```

Present the catalogues

Load the catalogues

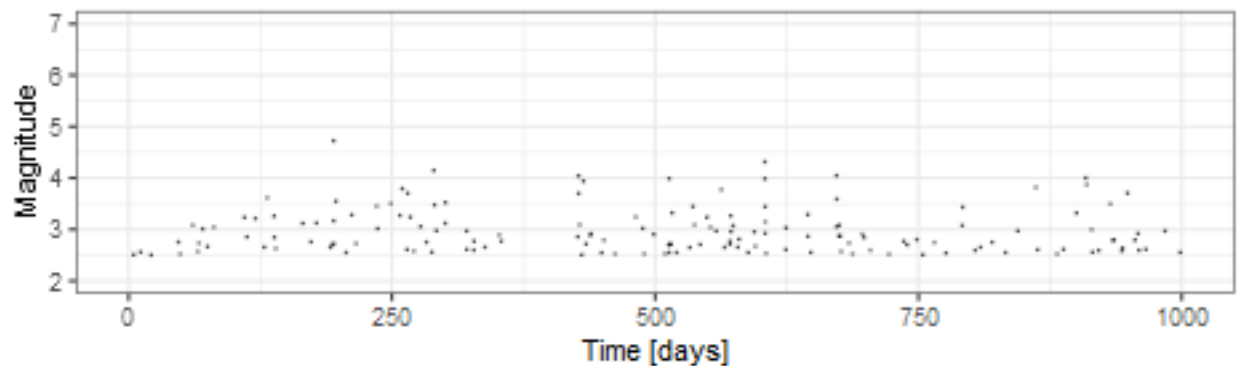
To read from saved object files:

```
# load("M6p7_ETAS_cat.Rda")  
# load("quiet.ETAS.cat.Rda")
```

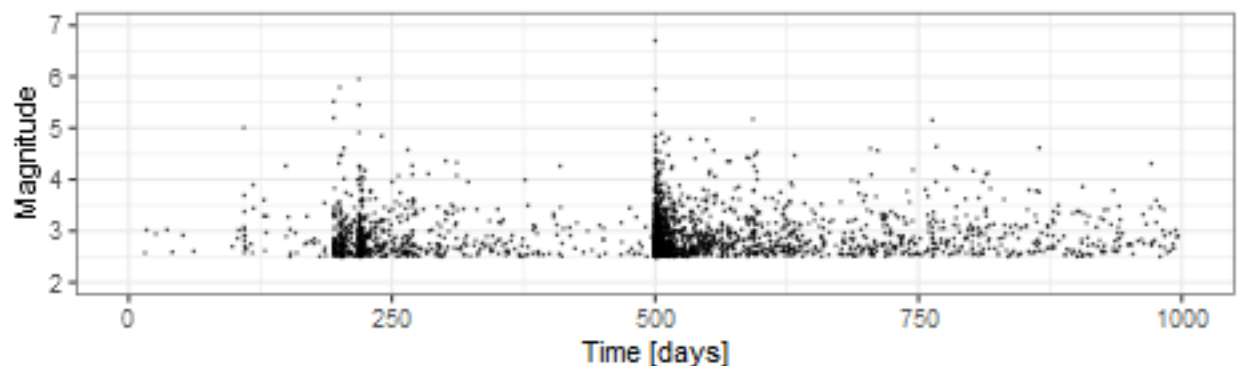
Plot properties of the catalogues

```
plots <- list()  
  
plots[[1]] <- ggplot() +  
  geom_point(data = quiet.ETAS.cat, aes(x = ts, y = magnitudes), size = 0.1, alpha = 0.5) +  
  xlim(0, modelledDuration) +  
  ggtitle(paste("A. Unseeded catalog, nEvents =", length(quiet.ETAS.cat$ts))) +  
  ylim(2, 7) +  
  xlab("Time [days]") +  
  ylab("Magnitude") +  
  theme_bw()  
  
plots[[2]] <- ggplot() +  
  geom_point(data = M6p7.ETAS.cat, aes(x = ts, y = magnitudes), size = 0.1, alpha = 0.5) +  
  xlim(0, modelledDuration) +  
  ggtitle(paste("B. Catalog seeded with M6.7 event on day 500, nEvents =", length(M6p7.ETAS.cat$ts))) +  
  ylim(2, 7) +  
  xlab("Time [days]") +  
  ylab("Magnitude") +  
  theme_bw()  
  
plt <- grid.arrange(plots[[1]], plots[[2]], ncol = 1, nrow = 2)
```

A. Unseeded catalog, nEvents = 157



B. Catalog seeded with M6.7 event on day 500, nEvents = 2602



```
# ggsave("initialConditionCats.png", plt)
# ggsave("initialConditionCats.pdf", plt)
```

Analyse the sensitivity to starting conditions

Analysis of quiet catalogue

```
list.output.quietScenario <- list()

for (i in seq_len(nRealisations)) {
  if (exists("list.input")) remove("list.input")

  # Load a set of parameters that we will need to tweak for this application
  fpath <- system.file("extdata", "user_input_synthetic_noCatalogue.txt", package = "ETAS.inlabru")
  list.input <- create_input_list_temporal_noCatalogue(fpath)

  #####
  # Tweak the variables loaded from the input file
  list.input$M0 <- M0
  list.input$time.int <- c(0, modelledDuration)
  list.input$T12 <- c(0, modelledDuration)

  # Change the starting location, measured on the ETAS scale
  list.input$mu.init <- startingValues$mu[i]
  list.input$alpha.init <- startingValues$alpha[i]
```

```

list.input$K.init <- startingValues$K[i]
list.input$c.init <- startingValues$c[i]
list.input$p.init <- startingValues$p[i]

link.f <- list(
  mu = \ (x) gamma_t(x, a_mu, b_mu),
  K = \ (x) loggaus_t(x, a_K, b_K),
  alpha = \ (x) unif_t(x, a_alpha, b_alpha),
  c_ = \ (x) unif_t(x, a_c, b_c),
  p = \ (x) unif_t(x, a_p, b_p)
)

# initial value - convert from ETAS scale to internal scale
list.input$th.init <- list(
  th.mu = inv_gamma_t(list.input$mu.init, list.input$a_mu, list.input$b_mu),
  th.K = inv_loggaus_t(list.input$K.init, list.input$a_K, list.input$b_K),
  th.alpha = inv_unif_t(list.input$alpha.init, list.input$a_alpha, list.input$b_alpha),
  th.c = inv_unif_t(list.input$c.init, list.input$a_c, list.input$b_c),
  th.p = inv_unif_t(list.input$p.init, list.input$a_p, list.input$b_p)
)

# Define options for inlabru
if (is.null(list.input$max_step)) {
  list.input$bru.opt.list <- list(
    bru_verbose = 0, # type of visual output
    bru_max_iter = list.input$max_iter, # maximum number of iterations
    # bru_method = list(max_step = 0.5),
    bru_initial = list.input$th.init
  ) # parameters initial values
} else {
  list.input$bru.opt.list <- list(
    bru_verbose = 0, # type of visual output
    bru_max_iter = list.input$max_iter, # maximum number of iterations
    bru_method = list(max_step = list.input$max_step),
    bru_initial = list.input$th.init
  ) # parameters initial values
}

## Add out catalogue to the input list
list.input$catalog <- data.frame(
  time_diff = quiet.ETAS.cat$ts,
  magnitudes = quiet.ETAS.cat$magnitudes
)

## Add the catalogue formatted for bru
list.input$catalog.bru <- data.frame(
  ts = quiet.ETAS.cat$ts,
  magnitudes = quiet.ETAS.cat$magnitudes,
  idx.p = seq_len(nrow(quiet.ETAS.cat))
)

## Input list is now formatted
#####

```

```

## Run the model according to the input list
ETAS.model.fit <- Temporal.ETAS.fit(list.input)

## Small bit of post processing
list.output.quietScenario[[i]] <- append(list.input, list(model.fit = ETAS.model.fit))
list.output.quietScenario[[i]]$runtime <- sum(list.output.quietScenario[[i]]$model.fit$bru_timings$Ti
list.output.quietScenario[[i]]$nEvents <- length(list.output.quietScenario[[i]]$catalog[, 1])
}

#> Start model fitting
#> Start creating grid...
#> Finished creating grid, time 0.5527861
#> Finish model fitting
#> Start model fitting
#> Start creating grid...
#> Finished creating grid, time 0.570051
#> Finish model fitting

```

Analysis of M6.7 catalogue

```

list.output.M6p7Scenario <- list()

for (i in seq_len(nRealisations)) {
  if (exists("list.input")) {
    remove(list.input)
  }

  # Load a set of parameters that we will need to tweak for this application
  fpath <- system.file("extdata", "user_input_synthetic_noCatalogue.txt", package = "ETAS.inlabru")
  list.input <- create_input_list_temporal_noCatalogue(fpath)

  #####
  # Tweak the variables loaded from the input file
  list.input$M0 <- M0
  list.input$time.int <- c(0, modelledDuration)
  list.input$T12 <- c(0, modelledDuration)

  # Change the starting location, measured on the ETAS scale
  list.input$mu.init <- startingValues$mu[i]
  list.input$alpha.init <- startingValues$alpha[i]
  list.input$K.init <- startingValues$K[i]
  list.input$c.init <- startingValues$c[i]
  list.input$p.init <- startingValues$p[i]

  link.f <- list(
    mu = \ (x) gamma_t(x, a_mu, b_mu),
    K = \ (x) loggaus_t(x, a_K, b_K),
    alpha = \ (x) unif_t(x, a_alpha, b_alpha),
    c_ = \ (x) unif_t(x, a_c, b_c),
    p = \ (x) unif_t(x, a_p, b_p)
  )

  # initial value - convert from ETAS scale to internal scale

```

```

list.input$th.init <- list(
  th.mu = inv_gamma_t(list.input$mu.init, list.input$a_mu, list.input$b_mu),
  th.K = inv_loggaus_t(list.input$K.init, list.input$a_K, list.input$b_K),
  th.alpha = inv_unif_t(list.input$alpha.init, list.input$a_alpha, list.input$b_alpha),
  th.c = inv_unif_t(list.input$c.init, list.input$a_c, list.input$b_c),
  th.p = inv_unif_t(list.input$p.init, list.input$a_p, list.input$b_p)
)

# Define options for inlabru
if (is.null(list.input$max_step)) {
  list.input$bru.opt.list <- list(
    bru_verbose = 4, # type of visual output
    bru_max_iter = list.input$max_iter, # maximum number of iterations
    # bru_method = list(max_step = 0.5),
    bru_initial = list.input$th.init
  ) # parameters initial values
} else {
  list.input$bru.opt.list <- list(
    bru_verbose = 4, # type of visual output
    bru_max_iter = list.input$max_iter, # maximum number of iterations
    bru_method = list(max_step = list.input$max_step),
    bru_initial = list.input$th.init
  ) # parameters initial values
}

## Add out catalogue to the input list
list.input$catalog <- data.frame(
  time_diff = M6p7.ETAS.cat$ts,
  magnitudes = M6p7.ETAS.cat$magnitudes
)

## Add the catalogue formatted for bru
list.input$catalog.bru <- data.frame(
  ts = M6p7.ETAS.cat$ts,
  magnitudes = M6p7.ETAS.cat$magnitudes,
  idx.p = seq_len(nrow(M6p7.ETAS.cat))
)

## Input list is now formatted
#####

## Run the model according to the input list
ETAS.model.fit <- Temporal.ETAS.fit(list.input)

## Small bit of post processing
list.output.M6p7Scenario[[i]] <- append(list.input, list(model.fit = ETAS.model.fit))
list.output.M6p7Scenario[[i]]$runtime <- sum(list.output.M6p7Scenario[[i]]$model.fit$bru_timings$Time)
list.output.M6p7Scenario[[i]]$nEvents <- length(list.output.M6p7Scenario[[i]]$catalog[, 1])
}

#> Start model fitting
#> Start creating grid...
#> Finished creating grid, time 8.939932
#> inla: Evaluate component inputs

```

```

#> iinla: Evaluate component linearisations
#> iinla: Evaluate component simplifications
#> iinla: Evaluate predictor linearisation
#> iinla: Construct inla stack
#> iinla: Model initialisation completed
#> iinla: Iteration 1 [max:100]
#> iinla: Step rescaling: 91.99%, Approx Optimisation (norm0 = 11080, norm1 = 517.1, norm01 = 11170)
#> iinla: |lin1-lin0| = 11170
#>      <eta-lin1,delta>/|delta| = -97.35
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 507.9
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Iteration 2 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 2433, norm1 = 445.5, norm01 = 2128)
#> iinla: Step rescaling: 126.9%, Approx Optimisation (norm0 = 1983, norm1 = 298.2, norm01 = 2128)
#> iinla: |lin1-lin0| = 2128
#>      <eta-lin1,delta>/|delta| = -161.1
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 251
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 2590% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 3 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 3248, norm1 = 4719, norm01 = 2367)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 1214, norm1 = 1698, norm01 = 2367)
#> iinla: Step rescaling: 69.19%, Approx Optimisation (norm0 = 1205, norm1 = 1213, norm01 = 2367)
#> iinla: |lin1-lin0| = 2367
#>      <eta-lin1,delta>/|delta| = -1188
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 246.9
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 1420% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 4 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 2432, norm1 = 643.6, norm01 = 1816)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 1595, norm1 = 243.5, norm01 = 1816)
#> iinla: Step rescaling: 115.2%, Approx Optimisation (norm0 = 1808, norm1 = 122.9, norm01 = 1816)
#> iinla: |lin1-lin0| = 1816
#>      <eta-lin1,delta>/|delta| = -12.4
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 122.3
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 1170% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 5 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 1141, norm1 = 424.5, norm01 = 716.5)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 709.4, norm1 = 7.12, norm01 = 716.5)
#> iinla: Step rescaling: 101%, Approx Optimisation (norm0 = 716.5, norm1 = 0.9076, norm01 = 716.5)
#> iinla: |lin1-lin0| = 716.5
#>      <eta-lin1,delta>/|delta| = -0.001566
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.9076
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 511% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 6 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 511.4, norm1 = 151.9, norm01 = 377.2)

```



```

#> iinla: Step rescaling: 100%, Overstep (norm0 = 342.3, norm1 = 45.71, norm01 = 377.2)
#> iinla: Step rescaling: 109.6%, Approx Optimisation (norm0 = 371.1, norm1 = 35.26, norm01 = 377.2)
#> iinla: |lin1-lin0| = 377.2
#>      <eta-lin1,delta>/|delta| = -7.763
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 34.39
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 276% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 7 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 554.9, norm1 = 211.8, norm01 = 343)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 343, norm1 = 0.2598, norm01 = 343)
#> iinla: Step rescaling: 100%, Approx Optimisation (norm0 = 343, norm1 = 0.2521, norm01 = 343)
#> iinla: |lin1-lin0| = 343
#>      <eta-lin1,delta>/|delta| = 0.0009766
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.2521
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 254% of SD, and line search is inactive [stop if: <10% and line se
#> iinla: Iteration 8 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 360, norm1 = 128.7, norm01 = 231.8)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 226.2, norm1 = 7.494, norm01 = 231.8)
#> iinla: Step rescaling: 102.5%, Approx Optimisation (norm0 = 231.6, norm1 = 5.163, norm01 = 231.8)
#> iinla: |lin1-lin0| = 231.8
#>      <eta-lin1,delta>/|delta| = -0.2431
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 5.157
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 174% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 9 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 319.7, norm1 = 117.4, norm01 = 202.4)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 199.5, norm1 = 3.889, norm01 = 202.4)
#> iinla: Step rescaling: 101.5%, Approx Optimisation (norm0 = 202.3, norm1 = 2.614, norm01 = 202.4)
#> iinla: |lin1-lin0| = 202.4
#>      <eta-lin1,delta>/|delta| = -0.07005
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 2.613
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 153% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 10 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 268.5, norm1 = 98.93, norm01 = 169.6)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 167.4, norm1 = 3.064, norm01 = 169.6)
#> iinla: Step rescaling: 101.4%, Approx Optimisation (norm0 = 169.6, norm1 = 2.099, norm01 = 169.6)
#> iinla: |lin1-lin0| = 169.6
#>      <eta-lin1,delta>/|delta| = -0.05353
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 2.098
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 128% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 11 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 232.4, norm1 = 86.15, norm01 = 146.3)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 144.7, norm1 = 2.24, norm01 = 146.3)
#> iinla: Step rescaling: 101.1%, Approx Optimisation (norm0 = 146.3, norm1 = 1.545, norm01 = 146.3)
#> iinla: |lin1-lin0| = 146.3

```

```

#>      <eta-lin1,delta>/|delta| = -0.03343
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 1.544
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 111% of SD, and line search is active [stop if: <10% and line se
#> iinla: Iteration 12 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 202.8, norm1 = 75.54, norm01 = 127.3)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 126.1, norm1 = 1.648, norm01 = 127.3)
#> iinla: Step rescaling: 101%, Approx Optimisation (norm0 = 127.3, norm1 = 1.143, norm01 = 127.3)
#> iinla: |lin1-lin0| = 127.3
#>      <eta-lin1,delta>/|delta| = -0.02093
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 1.142
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 96.9% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 13 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 178.4, norm1 = 66.73, norm01 = 111.7)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 110.8, norm1 = 1.22, norm01 = 111.7)
#> iinla: Step rescaling: 100.8%, Approx Optimisation (norm0 = 111.7, norm1 = 0.8487, norm01 = 111.7)
#> iinla: |lin1-lin0| = 111.7
#>      <eta-lin1,delta>/|delta| = -0.01312
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.8486
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 85.2% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 14 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 158, norm1 = 59.31, norm01 = 98.73)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 98.07, norm1 = 0.9089, norm01 = 98.73)
#> iinla: Step rescaling: 100.7%, Approx Optimisation (norm0 = 98.72, norm1 = 0.6343, norm01 = 98.73)
#> iinla: |lin1-lin0| = 98.73
#>      <eta-lin1,delta>/|delta| = -0.008269
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.6342
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 75.5% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 15 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 140.7, norm1 = 52.97, norm01 = 87.78)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 87.29, norm1 = 0.6826, norm01 = 87.78)
#> iinla: Step rescaling: 100.6%, Approx Optimisation (norm0 = 87.77, norm1 = 0.4773, norm01 = 87.78)
#> iinla: |lin1-lin0| = 87.78
#>      <eta-lin1,delta>/|delta| = -0.005255
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.4772
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 67.3% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 16 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 125.9, norm1 = 47.5, norm01 = 78.42)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 78.05, norm1 = 0.5166, norm01 = 78.42)
#> iinla: Step rescaling: 100.5%, Approx Optimisation (norm0 = 78.42, norm1 = 0.3616, norm01 = 78.42)
#> iinla: |lin1-lin0| = 78.42
#>      <eta-lin1,delta>/|delta| = -0.003371
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.3616
#> iinla: Evaluate component linearisations

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#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 60.2% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 17 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 113.1, norm1 = 42.74, norm01 = 70.35)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 70.07, norm1 = 0.3938, norm01 = 70.35)
#> iinla: Step rescaling: 100.4%, Approx Optimisation (norm0 = 70.35, norm1 = 0.2759, norm01 = 70.35)
#> iinla: |lin1-lin0| = 70.35
#>      <eta-lin1,delta>/|delta| = -0.002184
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.2759
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 54.1% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 18 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 101.9, norm1 = 38.57, norm01 = 63.32)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 63.1, norm1 = 0.3024, norm01 = 63.32)
#> iinla: Step rescaling: 100.3%, Approx Optimisation (norm0 = 63.32, norm1 = 0.2119, norm01 = 63.32)
#> iinla: |lin1-lin0| = 63.32
#>      <eta-lin1,delta>/|delta| = -0.001469
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.2119
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 48.8% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 19 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 92.04, norm1 = 34.89, norm01 = 57.16)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 56.99, norm1 = 0.2337, norm01 = 57.16)
#> iinla: Step rescaling: 100.3%, Approx Optimisation (norm0 = 57.15, norm1 = 0.1638, norm01 = 57.16)
#> iinla: |lin1-lin0| = 57.16
#>      <eta-lin1,delta>/|delta| = -0.001699
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.1638
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 44.1% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 20 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 83.34, norm1 = 31.62, norm01 = 51.72)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 51.58, norm1 = 0.1818, norm01 = 51.72)
#> iinla: Step rescaling: 100.3%, Approx Optimisation (norm0 = 51.72, norm1 = 0.1274, norm01 = 51.72)
#> iinla: |lin1-lin0| = 51.72
#>      <eta-lin1,delta>/|delta| = 0.0002508
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.1274
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 39.9% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 21 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 75.6, norm1 = 28.71, norm01 = 46.89)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 46.79, norm1 = 0.1422, norm01 = 46.89)
#> iinla: Step rescaling: 100.2%, Approx Optimisation (norm0 = 46.89, norm1 = 0.09965, norm01 = 46.89)
#> iinla: |lin1-lin0| = 46.89
#>      <eta-lin1,delta>/|delta| = -1.957e-05
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.09965
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 36.3% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 22 [max:100]

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#> iinla: Step rescaling: 162%, Expand (norm0 = 68.69, norm1 = 26.11, norm01 = 42.58)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 42.5, norm1 = 0.1119, norm01 = 42.58)
#> iinla: Step rescaling: 100.2%, Approx Optimisation (norm0 = 42.58, norm1 = 0.07837, norm01 = 42.58)
#> iinla: |lin1-lin0| = 42.58
#>      <eta-lin1,delta>/|delta| = -0.0002166
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.07837
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 33% of SD, and line search is active [stop if: <10% and line sea
#> iinla: Iteration 23 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 62.51, norm1 = 23.77, norm01 = 38.73)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 38.67, norm1 = 0.08851, norm01 = 38.73)
#> iinla: Step rescaling: 100.2%, Approx Optimisation (norm0 = 38.73, norm1 = 0.06196, norm01 = 38.73)
#> iinla: |lin1-lin0| = 38.73
#>      <eta-lin1,delta>/|delta| = -0.0003565
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.06196
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 30% of SD, and line search is active [stop if: <10% and line sea
#> iinla: Iteration 24 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 56.95, norm1 = 21.67, norm01 = 35.28)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 35.23, norm1 = 0.07034, norm01 = 35.28)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 35.28, norm1 = 0.04922, norm01 = 35.28)
#> iinla: |lin1-lin0| = 35.28
#>      <eta-lin1,delta>/|delta| = -0.0004523
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.04921
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 27.4% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 25 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 51.94, norm1 = 19.77, norm01 = 32.16)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 32.12, norm1 = 0.05616, norm01 = 32.16)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 32.16, norm1 = 0.03927, norm01 = 32.16)
#> iinla: |lin1-lin0| = 32.16
#>      <eta-lin1,delta>/|delta| = -0.0005143
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.03927
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 25% of SD, and line search is active [stop if: <10% and line sea
#> iinla: Iteration 26 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 47.41, norm1 = 18.06, norm01 = 29.35)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 29.32, norm1 = 0.04502, norm01 = 29.35)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 29.35, norm1 = 0.03147, norm01 = 29.35)
#> iinla: |lin1-lin0| = 29.35
#>      <eta-lin1,delta>/|delta| = -0.000551
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.03146
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 22.8% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 27 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 43.32, norm1 = 16.5, norm01 = 26.81)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 26.79, norm1 = 0.03624, norm01 = 26.81)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 26.81, norm1 = 0.02532, norm01 = 26.81)

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#> iinla: |lin1-lin0| = 26.81
#> <eta-lin1,delta>/|delta| = -0.0005686
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.02531
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 20.8% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 28 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 39.6, norm1 = 15.09, norm01 = 24.51)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 24.49, norm1 = 0.02928, norm01 = 24.51)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 24.51, norm1 = 0.02044, norm01 = 24.51)
#> iinla: |lin1-lin0| = 24.51
#> <eta-lin1,delta>/|delta| = 0.0004239
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.02044
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 19.1% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 29 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 36.23, norm1 = 13.81, norm01 = 22.42)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 22.4, norm1 = 0.02373, norm01 = 22.42)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 22.42, norm1 = 0.01656, norm01 = 22.42)
#> iinla: |lin1-lin0| = 22.42
#> <eta-lin1,delta>/|delta| = 0.0003459
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.01656
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 17.4% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 30 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 33.16, norm1 = 12.64, norm01 = 20.52)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 20.5, norm1 = 0.0193, norm01 = 20.52)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 20.52, norm1 = 0.01346, norm01 = 20.52)
#> iinla: |lin1-lin0| = 20.52
#> <eta-lin1,delta>/|delta| = 0.0002829
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.01346
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 16% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 31 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 30.37, norm1 = 11.58, norm01 = 18.79)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 18.78, norm1 = 0.01574, norm01 = 18.79)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 18.79, norm1 = 0.01097, norm01 = 18.79)
#> iinla: |lin1-lin0| = 18.79
#> <eta-lin1,delta>/|delta| = 0.0002319
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.01097
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 14.6% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 32 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 27.83, norm1 = 10.61, norm01 = 17.21)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 17.2, norm1 = 0.01287, norm01 = 17.21)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 17.21, norm1 = 0.008968, norm01 = 17.21)
#> iinla: |lin1-lin0| = 17.21
#> <eta-lin1,delta>/|delta| = 0.0001905
#> |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.008966

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#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 13.4% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 33 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 25.5, norm1 = 9.73, norm01 = 15.77)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 15.77, norm1 = 0.01055, norm01 = 15.77)
#> iinla: Step rescaling: 100%, Approx Optimisation (norm0 = 15.78, norm1 = 0.007349, norm01 = 15.77)
#> iinla: |lin1-lin0| = 15.77
#>      <eta-lin1,delta>/|delta| = 0.0001567
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.007347
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 12.3% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 34 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 23.38, norm1 = 8.922, norm01 = 14.46)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 14.46, norm1 = 0.00867, norm01 = 14.46)
#> iinla: Step rescaling: 100%, Approx Optimisation (norm0 = 14.46, norm1 = 0.006036, norm01 = 14.46)
#> iinla: |lin1-lin0| = 14.46
#>      <eta-lin1,delta>/|delta| = 0.0001292
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.006035
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 11.3% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 35 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 21.45, norm1 = 8.184, norm01 = 13.26)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 13.26, norm1 = 0.00714, norm01 = 13.26)
#> iinla: Step rescaling: 100%, Approx Optimisation (norm0 = 13.26, norm1 = 0.004969, norm01 = 13.26)
#> iinla: |lin1-lin0| = 13.26
#>      <eta-lin1,delta>/|delta| = 0.0001067
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.004968
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 10.3% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Iteration 36 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 19.68, norm1 = 7.509, norm01 = 12.17)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 12.16, norm1 = 0.005891, norm01 = 12.17)
#> iinla: Step rescaling: 100%, Approx Optimisation (norm0 = 12.17, norm1 = 0.004098, norm01 = 12.17)
#> iinla: |lin1-lin0| = 12.17
#>      <eta-lin1,delta>/|delta| = 8.832e-05
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.004097
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 9.49% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Convergence criterion met, running final INLA integration with known theta mode.
#> iinla: Iteration 37 [max:100]
#> Finish model fitting
#> Start model fitting
#> Start creating grid...
#> Finished creating grid, time 6.749804
#> iinla: Evaluate component inputs
#> iinla: Evaluate component linearisations
#> iinla: Evaluate component simplifications
#> iinla: Evaluate predictor linearisation

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#> iinla: Construct inla stack
#> iinla: Model initialisation completed
#> iinla: Iteration 1 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 247.2, norm1 = 89.3, norm01 = 157.9)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 154.7, norm1 = 3.516, norm01 = 157.9)
#> iinla: Step rescaling: 102.1%, Approx Optimisation (norm0 = 157.9, norm1 = 1.506, norm01 = 157.9)
#> iinla: |lin1-lin0| = 157.9
#>      <eta-lin1,delta>/|delta| = -0.0296
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 1.505
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Iteration 2 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 51.03, norm1 = 19.11, norm01 = 31.91)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 31.68, norm1 = 0.2481, norm01 = 31.91)
#> iinla: Step rescaling: 100.7%, Approx Optimisation (norm0 = 31.91, norm1 = 0.08549, norm01 = 31.91)
#> iinla: |lin1-lin0| = 31.91
#>      <eta-lin1,delta>/|delta| = -0.0004733
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.08548
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 25.5% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 3 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 36.77, norm1 = 13.93, norm01 = 22.84)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 22.77, norm1 = 0.09425, norm01 = 22.84)
#> iinla: Step rescaling: 100.3%, Approx Optimisation (norm0 = 22.84, norm1 = 0.06241, norm01 = 22.84)
#> iinla: |lin1-lin0| = 22.84
#>      <eta-lin1,delta>/|delta| = -0.0005424
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.06241
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 18.2% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 4 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 32.21, norm1 = 12.24, norm01 = 19.98)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 19.94, norm1 = 0.06288, norm01 = 19.98)
#> iinla: Step rescaling: 100.2%, Approx Optimisation (norm0 = 19.98, norm1 = 0.04654, norm01 = 19.98)
#> iinla: |lin1-lin0| = 19.98
#>      <eta-lin1,delta>/|delta| = -6.801e-05
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.04654
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 15.8% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 5 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 29.17, norm1 = 11.09, norm01 = 18.08)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 18.05, norm1 = 0.04646, norm01 = 18.08)
#> iinla: Step rescaling: 100.2%, Approx Optimisation (norm0 = 18.08, norm1 = 0.03488, norm01 = 18.08)
#> iinla: |lin1-lin0| = 18.08
#>      <eta-lin1,delta>/|delta| = -0.0001806
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.03488
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 14.3% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 6 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 26.62, norm1 = 10.13, norm01 = 16.49)

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#> iinla: Step rescaling: 100%, Overstep (norm0 = 16.47, norm1 = 0.0356, norm01 = 16.49)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 16.49, norm1 = 0.02671, norm01 = 16.49)
#> iinla: |lin1-lin0| = 16.49
#>      <eta-lin1,delta>/|delta| = -0.0002328
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.02671
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 13.1% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 7 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 24.36, norm1 = 9.274, norm01 = 15.08)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 15.07, norm1 = 0.02769, norm01 = 15.08)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 15.08, norm1 = 0.0207, norm01 = 15.08)
#> iinla: |lin1-lin0| = 15.08
#>      <eta-lin1,delta>/|delta| = -0.000263
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.0207
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 12% of SD, and line search is active [stop if: <10% and line sea
#> iinla: Iteration 8 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 22.31, norm1 = 8.499, norm01 = 13.81)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 13.8, norm1 = 0.0217, norm01 = 13.81)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 13.81, norm1 = 0.01615, norm01 = 13.81)
#> iinla: |lin1-lin0| = 13.81
#>      <eta-lin1,delta>/|delta| = -0.0002804
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.01615
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 10.9% of SD, and line search is active [stop if: <10% and line s
#> iinla: Iteration 9 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 20.45, norm1 = 7.794, norm01 = 12.66)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 12.65, norm1 = 0.01708, norm01 = 12.66)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 12.66, norm1 = 0.01266, norm01 = 12.66)
#> iinla: |lin1-lin0| = 12.66
#>      <eta-lin1,delta>/|delta| = 0.0002255
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.01266
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 10% of SD, and line search is inactive [stop if: <10% and line s
#> iinla: Iteration 10 [max:100]
#> iinla: Step rescaling: 162%, Expand (norm0 = 18.76, norm1 = 7.151, norm01 = 11.61)
#> iinla: Step rescaling: 100%, Overstep (norm0 = 11.6, norm1 = 0.01348, norm01 = 11.61)
#> iinla: Step rescaling: 100.1%, Approx Optimisation (norm0 = 11.61, norm1 = 0.009956, norm01 = 11.61)
#> iinla: |lin1-lin0| = 11.61
#>      <eta-lin1,delta>/|delta| = 0.0001812
#>      |eta-lin0 - delta <delta,eta-lin0>/<delta,delta>| = 0.009954
#> iinla: Evaluate component linearisations
#> iinla: Evaluate predictor linearisation
#> iinla: Max deviation from previous: 9.19% of SD, and line search is inactive [stop if: <10% and line
#> iinla: Convergence criterion met, running final INLA integration with known theta mode.
#> iinla: Iteration 11 [max:100]
#> Finish model fitting

```


Plot posteriors with corresponding starting values

```
plots <- list()

trueParas <- data.frame(value = c(mu, K, alpha, c, p), param = c("mu", "K", "alpha", "c", "p"))

post.list <- get_posterior_param(input.list = list.output.quietScenario[[1]])
post.df <- post.list[[1]]
post.df$id <- 1

for (i in 2:nRealisations) {
  post.list <- get_posterior_param(input.list = list.output.quietScenario[[i]])
  post.df.tmp <- post.list[[1]]
  post.df.tmp$id <- i

  post.df <- rbind(post.df, post.df.tmp)
}

plots[[1]] <- ggplot(post.df, aes(x = x, y = y, group = id, color = factor(id), lty = factor(id))) +
  geom_line() +
  # scale_x_discrete(guide = guide_axis(check.overlap = TRUE)) +
  facet_wrap(facets = vars(param), scales = "free", labeller = label_parsed, nrow = 1) +
  geom_vline(aes(xintercept = value),
    data = trueParas, color = "black", linetype = 2,
    label = "True value"
  ) +
  labs(color = "Initial ETAS Para. Set", linetype = "Initial ETAS Para. Set") +
  ggtitle(paste("A. Inversion of a 1000 day catalogue with no large events, nEvents =", length(quiet.E
  xlab("ETAS Posteriors") +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
  theme(legend.position = "hidden") +
  theme(plot.title = element_text(size = 12))
#> Warning in geom_vline(aes(xintercept = value), data = trueParas, color =
#> "black", : Ignoring unknown parameters: `label`

trueParas <- data.frame(value = c(mu, K, alpha, c, p), param = c("mu", "K", "alpha", "c", "p"))

post.list <- get_posterior_param(input.list = list.output.M6p7Scenario[[1]])
post.df <- post.list[[1]]
post.df$id <- 2

for (i in 2:nRealisations) {
  post.list <- get_posterior_param(input.list = list.output.M6p7Scenario[[i]])
  post.df.tmp <- post.list[[1]]
  post.df.tmp$id <- i

  post.df <- rbind(post.df, post.df.tmp)
}

plots[[2]] <- ggplot(post.df, aes(x = x, y = y, group = id, color = factor(id), lty = factor(id))) +
  geom_line() +
  # scale_x_discrete(guide = guide_axis(check.overlap = TRUE)) +
  facet_wrap(facets = vars(param), scales = "free", labeller = label_parsed, nrow = 1) +
```

```

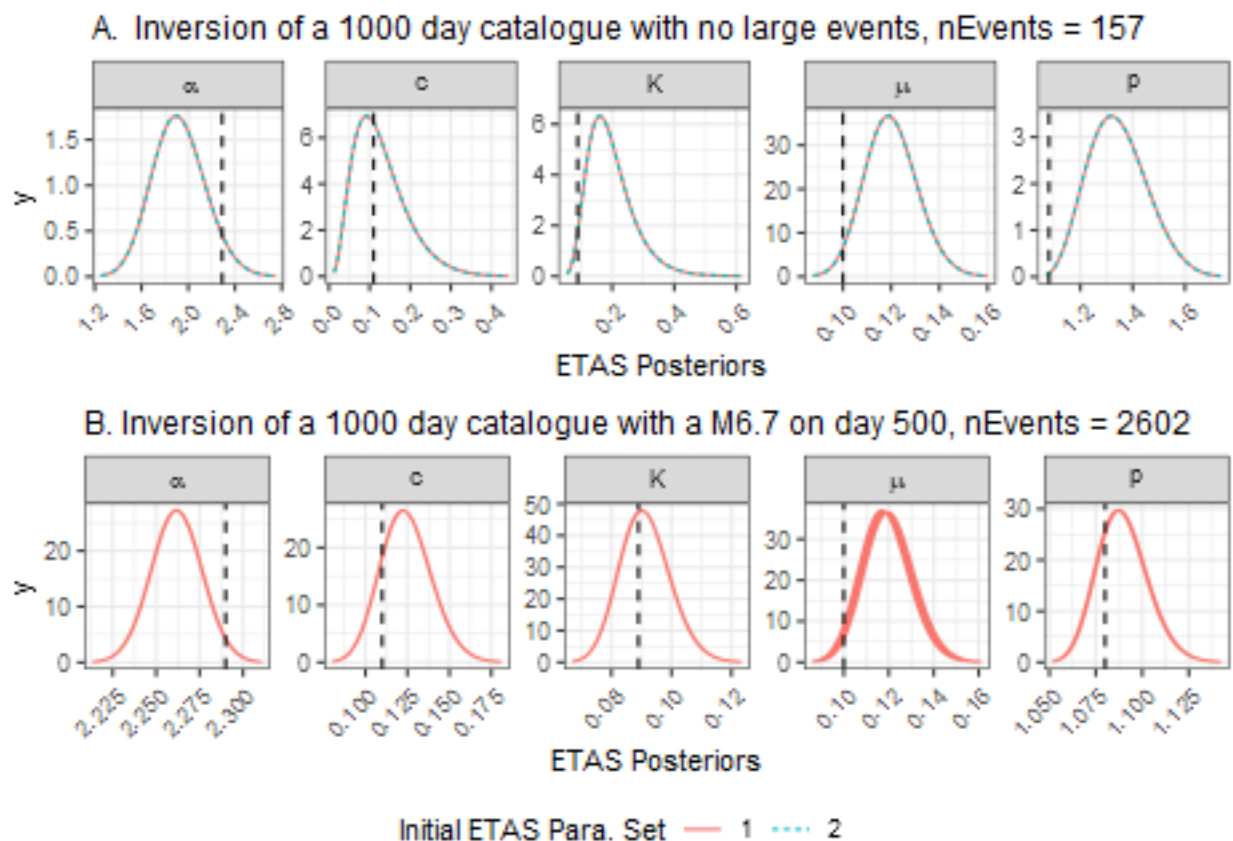
geom_vline(aes(xintercept = value),
  data = trueParas, color = "black", linetype = 2,
  label = "True value"
) +
labs(color = "Initial ETAS Para. Set", linetype = "Initial ETAS Para. Set") +
ggtitle(paste("B. Inversion of a 1000 day catalogue with a M6.7 on day 500, nEvents =", length(M6p7.E
xlab("ETAS Posteriors") +
theme_bw() +
theme(axis.text.x = element_text(angle = 45, hjust = 1)) +
theme(legend.position = "hidden") +
theme(plot.title = element_text(size = 12))
#> Warning in geom_vline(aes(xintercept = value), data = trueParas, color =
#> "black", : Ignoring unknown parameters: `label`

```

```

plt <- grid_arrange_shared_legend(plots[[1]], plots[[2]], ncol = 1, nrow = 2, position = "bottom")

```



```

plt
#> TableGrob (2 x 1) "arrange": 2 grobs
#> z      cells      name      grob
#> 1 1 (1-1,1-1) arrange gtable[arrange]
#> 2 2 (2-2,1-1) arrange gtable[guide-box]
# ggsave("initialCondition_posteriors.png", plt)
# ggsave("initialCondition_posteriors.pdf", plt)

```

Explore ETAS triggering function using posterior samples

```
plot_triggering <- list()
plot_triggering[[1]] <- triggering_fun_plot(list.output.quietScenario[[1]], magnitude = 4, n.samp = 100)
  ggtitle("C. M4 triggering function") +
  theme_bw() +
  ylim(0, 5.5) +
  theme(plot.title = element_text(size = 8))

plot_triggering[[2]] <- triggering_fun_plot(list.output.M6p7Scenario[[1]], magnitude = 4, n.samp = 100)
  ggtitle("D. M4 triggering function") +
  theme_bw() +
  ylim(0, 5.5) +
  theme(plot.title = element_text(size = 8))

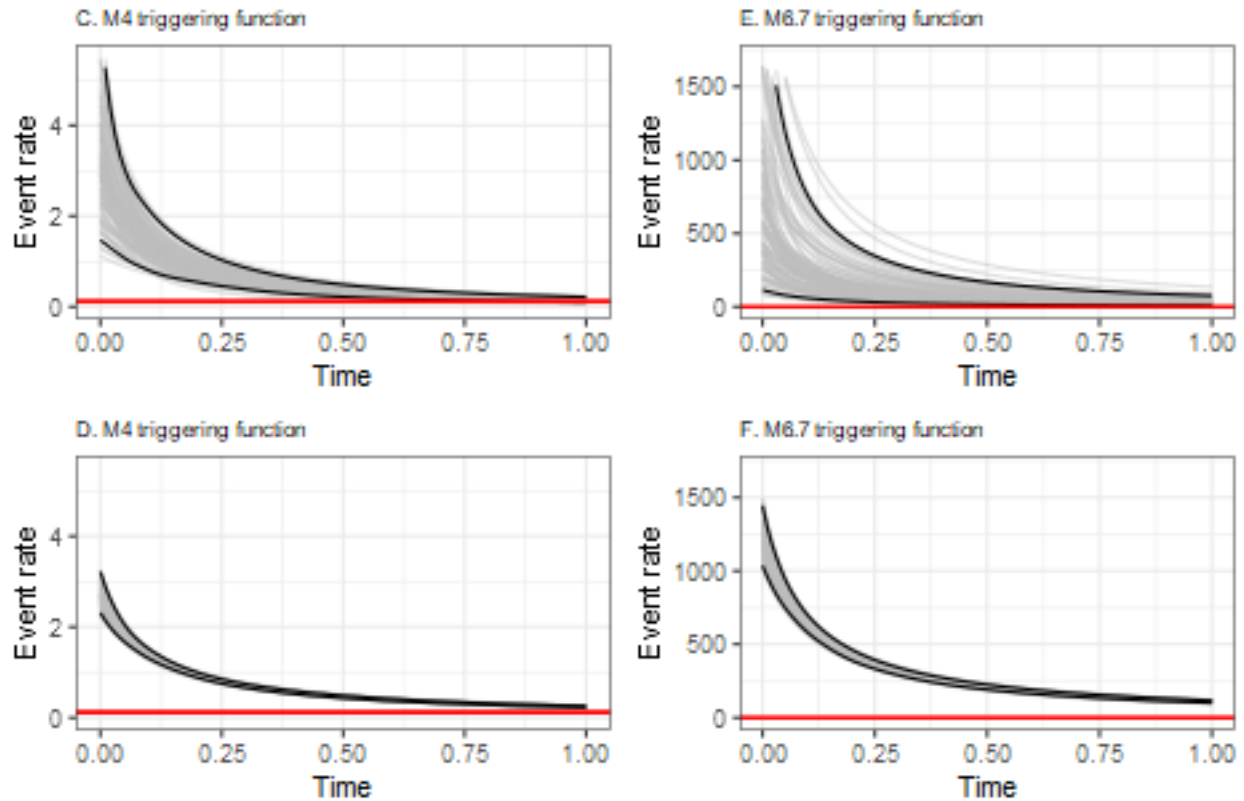
plot_triggering[[3]] <- triggering_fun_plot(list.output.quietScenario[[1]], magnitude = 6.7, n.samp = 100)
  ggtitle("E. M6.7 triggering function") +
  theme_bw() +
  ylim(0, 1700) +
  theme(plot.title = element_text(size = 8))

plot_triggering[[4]] <- triggering_fun_plot(list.output.M6p7Scenario[[1]], magnitude = 6.7, n.samp = 100)
  ggtitle("F. M6.7 triggering function") +
  theme_bw() +
  ylim(0, 1700) +
  theme(plot.title = element_text(size = 8))

plt <- grid.arrange(plot_triggering[[1]], plot_triggering[[3]], plot_triggering[[2]], plot_triggering[[4]])
  theme(plot.title = element_text(size = 8))

#> Warning: Removed 14 rows containing missing values (`geom_line()`).
#> Warning: Removed 1 row containing missing values (`geom_line()`).
#> Warning: Removed 26 rows containing missing values (`geom_line()`).
#> Warning: Removed 3 rows containing missing values (`geom_line()`).
```

Triggering function variability



```
plt
```

```
#> NULL
```

```
# ggsave("trigFuncVariability_runin.png", plt)
```

```
# ggsave("trigFuncVariability_runin.pdf", plt)
```

```
plot_omori <- list()
```

```
plot_omori[[1]] <- omori_plot_posterior(list.output.quietScenario[[1]], n.samp = 100) +  
  ggtitle("A. Omori decay") +  
  theme_bw() +  
  ylim(0, 1) +  
  theme(plot.title = element_text(size = 8))
```

```
plot_omori[[2]] <- omori_plot_posterior(list.output.M6p7Scenario[[1]], n.samp = 100) +  
  ggtitle("B. Omori decay") +  
  theme_bw() +  
  ylim(0, 1) +  
  theme(plot.title = element_text(size = 8))
```

```
plt <- grid.arrange(plot_omori[[1]], plot_triggering[[1]], plot_triggering[[3]], plot_omori[[2]], plot_
```

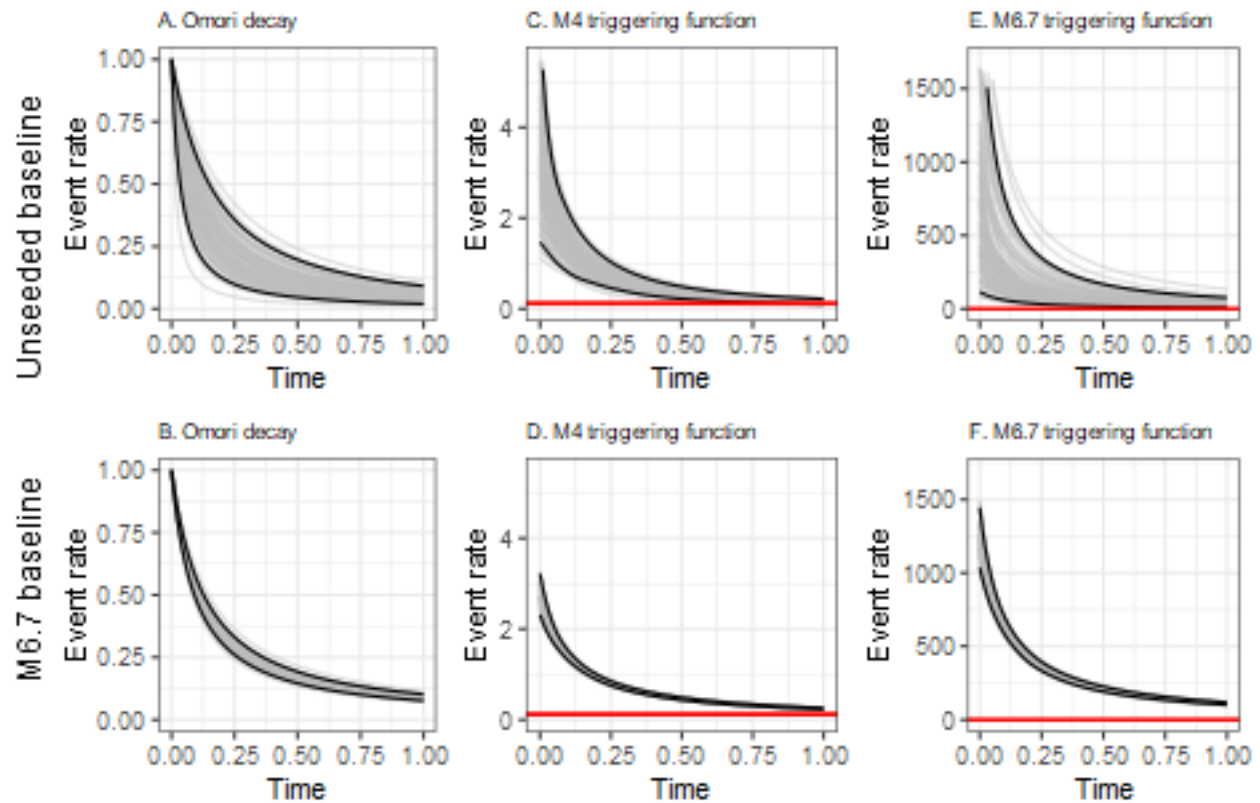
```
#> Warning: Removed 14 rows containing missing values (`geom_line()`).
```

```
#> Warning: Removed 1 row containing missing values (`geom_line()`).
```

```
#> Warning: Removed 26 rows containing missing values (`geom_line()`).
```

```
#> Warning: Removed 3 rows containing missing values (`geom_line()`).
```

Triggering function variability

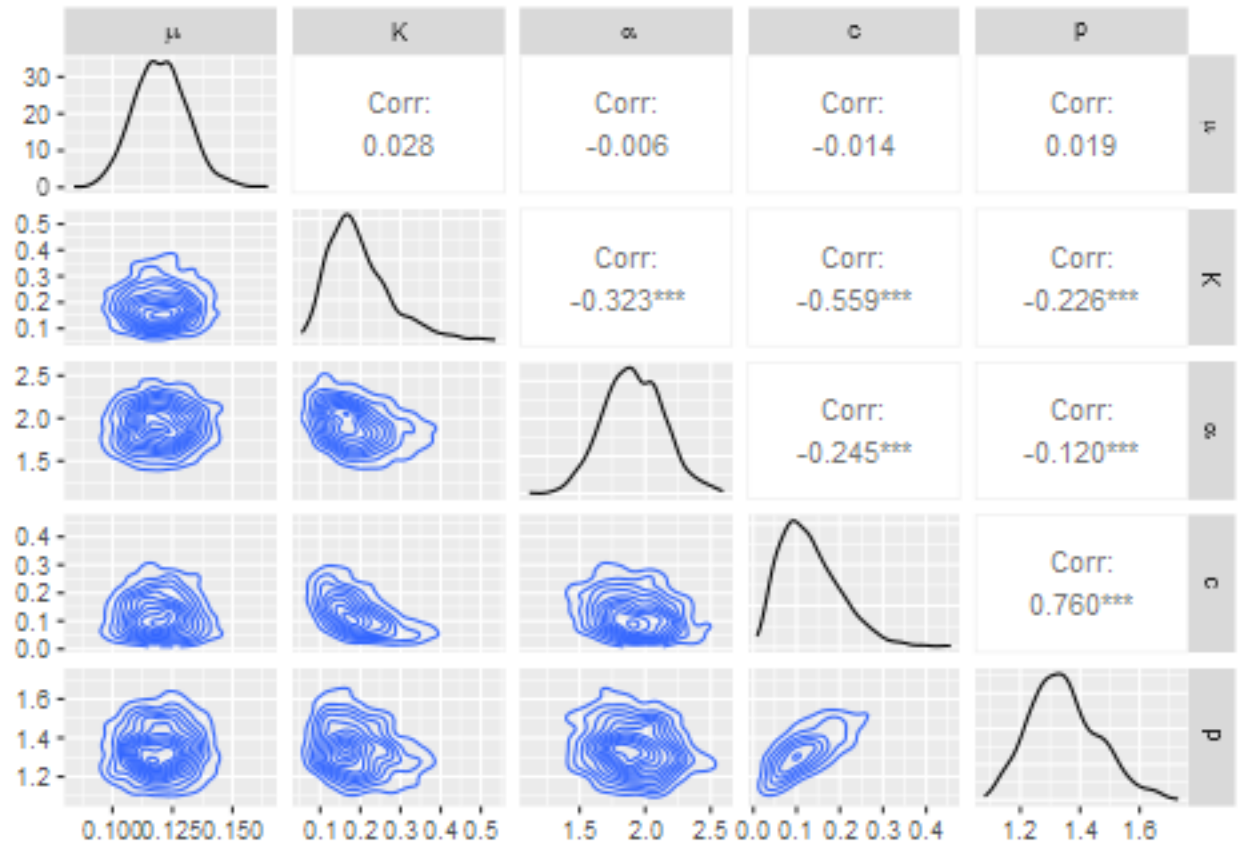


```
plt
#> TableGrob (3 x 4) "arrange": 8 grobs
#>   z     cells   name      grob
#> 1 1 (2-2,2-2) arrange gtable[layout]
#> 2 2 (2-2,3-3) arrange gtable[layout]
#> 3 3 (2-2,4-4) arrange gtable[layout]
#> 4 4 (3-3,2-2) arrange gtable[layout]
#> 5 5 (3-3,3-3) arrange gtable[layout]
#> 6 6 (3-3,4-4) arrange gtable[layout]
#> 7 7 (1-1,2-4) arrange text[GRID.text.1299]
#> 8 8 (1-3,1-1) arrange text[GRID.text.1300]

# ggsave("trigFuncVariability_runin.png", plt)
# ggsave("trigFuncVariability_runin.pdf", plt)
```

Plot the samples from the joint posteriors as pairs plots

```
post_pairs_plot(list.output.quietScenario[[1]], n.samp = 1000)$pair.plot
```

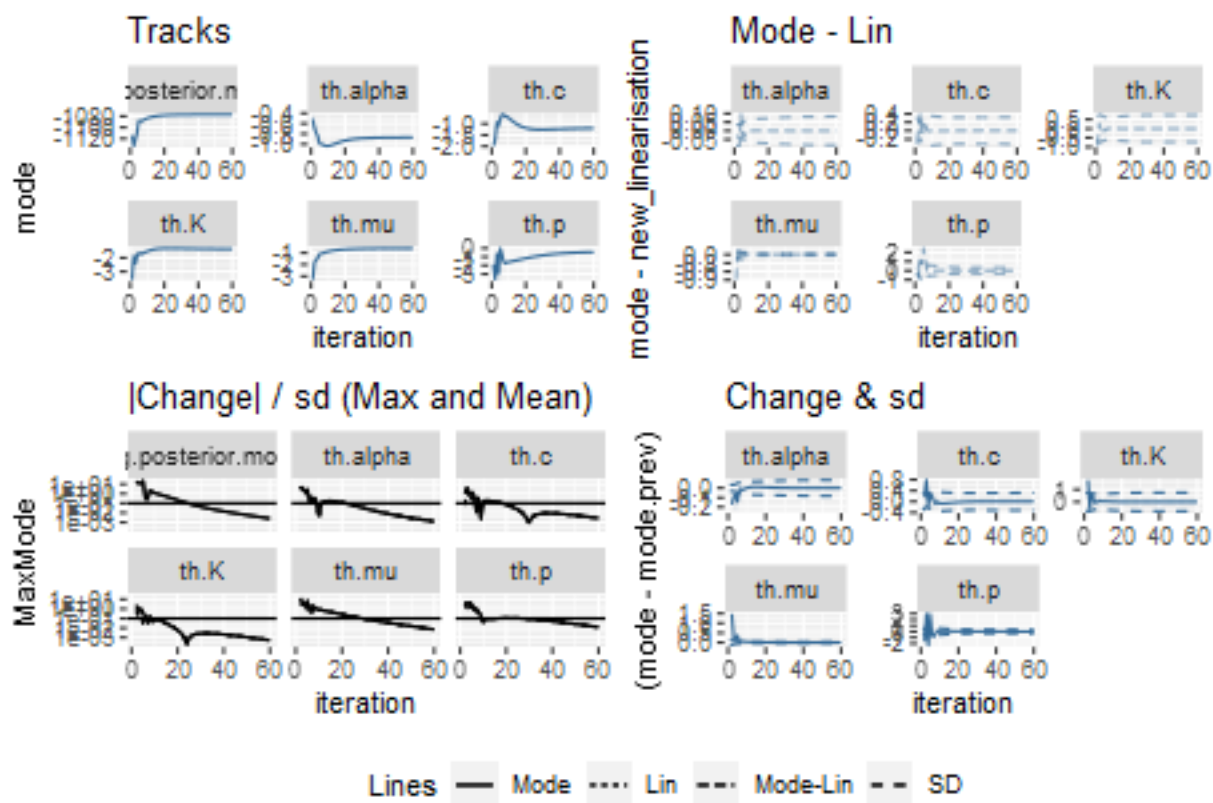


```
post_pairs_plot(list.output.M6p7Scenario[[1]], n.samp = 1000)$pair_plot
#> NULL
```

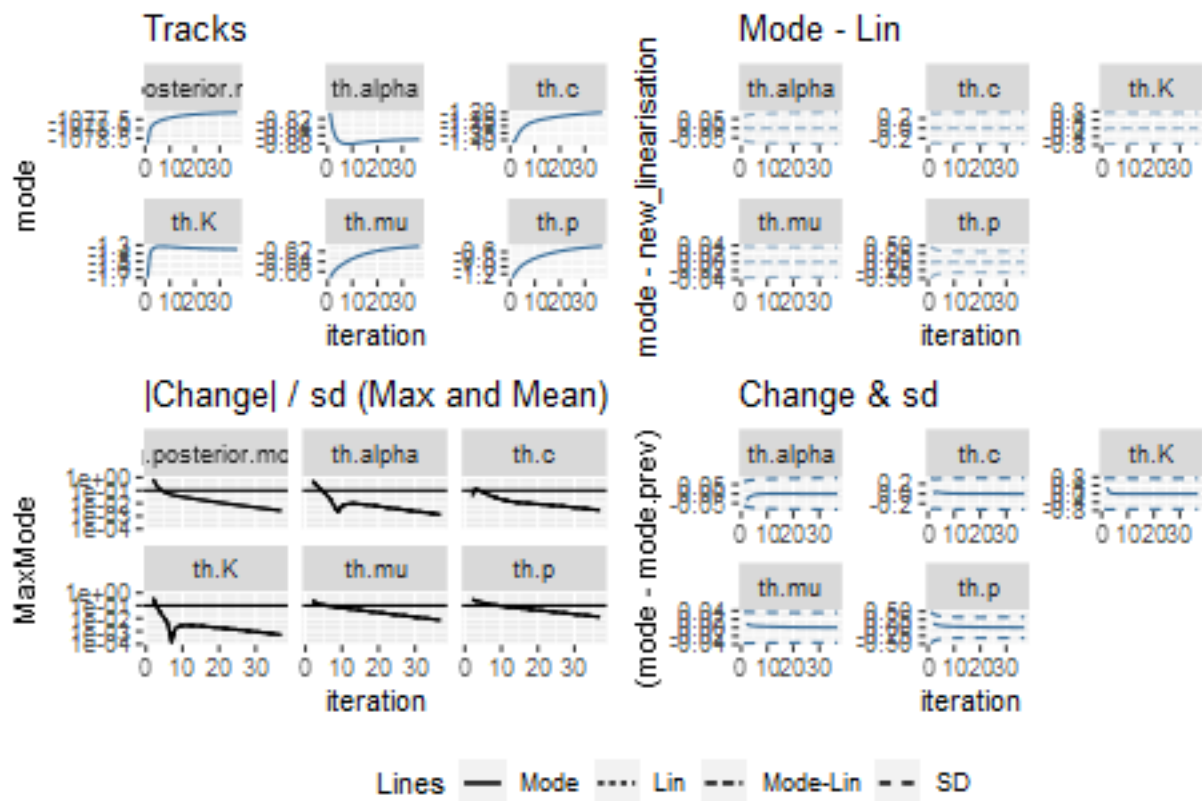
inlabru convergence diagnostics

We can also assess the convergence of the inlabru method itself, using the `bru_convergence_plot()` function. This can reveal if the starting values for the inlabru estimation are unreasonable, and better starting values for the nonlinear iterations might speed up the computations.

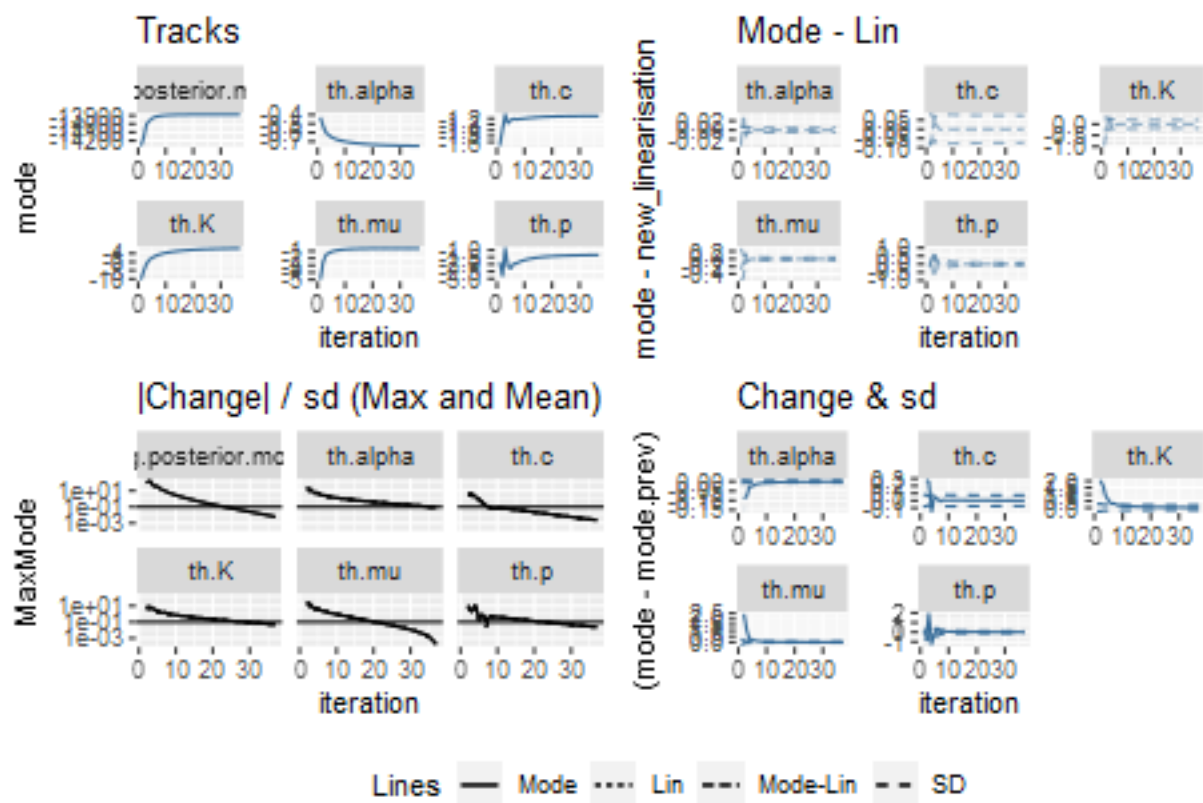
```
bru_convergence_plot(list.output.quietScenario[[1]]$model.fit)
```



```
bru_convergence_plot(list.output.quietScenario[[2]]$model.fit)
```



```
bru_convergence_plot(list.output.M6p7Scenario[[1]]$model.fit)
```

```
bru_convergence_plot(list.output.M6p7Scenario[[2]]$model.fit)
```

