Earthquake Forecasting

Dissertation Project 2

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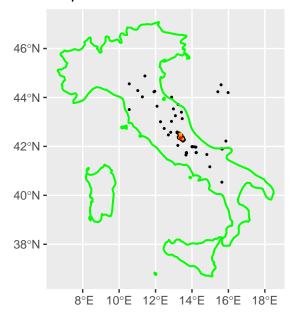
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```
require(ETAS.inlabru)
2 require(ggplot2)
3 require(dplyr)
4 require(magrittr)
5 require(tidyquant)
6 require(rnaturalearth)
7 require(terra)
8 require(sf)
  require(ggspatial)
   require(rnaturalearthdata)
   require(lubridate)
   # Increase/decrease num.cores if you have more/fewer cores on your computer.
14 # future::multisession works on both Windows, MacOS, and Linux
num.cores <- 8
16 future::plan(future::multisession, workers = num.cores)
   INLA::inla.setOption(num.threads = num.cores)
   # To deactivate parallelism, run
       future::plan(future::sequential)
       INLA::inla.setOption(num.threads = 1)
Copula transformation of the priors
1 # set copula transformations list
2 link.f <- list(</pre>
   mu = (x) gamma_t(x, 0.3, 0.6),
    K = (x) unif_t(x, 0, 10),
    alpha = (x) unif_t(x, 0, 10),
    c_= (x) unif_t(x, 0, 10),
```

```
p = (x) unif_t(x, 1, 10)
   # set inverse copula transformations list
10
   inv.link.f <- list(</pre>
    mu = \langle (x) inv_{gamma_t}(x, 0.3, 0.6),
    K = \langle (x) \text{ inv unif } t(x, 0, 10),
13
    alpha = (x) inv_unif_t(x, 0, 10),
    c_{-} = (x) inv_{unif_t}(x, 0, 10),
    p = (x) inv_unif_t(x, 1, 10)
  )
17
Italy
1 # transform time string in Date object
part 2    horus$time_date <- as.POSIXct(</pre>
    horus$time_string,
    format = "%Y-%m-%dT%H:%M:%OS",
    tz = "UTC"
  )
   # There may be some incorrectly registered data-times in the original data set,
  # that as.POSIXct() can't convert, depending on the system.
   # These should ideally be corrected, but for now, we just remove the rows that
10 # couldn't be converted.
   # horus <- na.omit(horus)</pre>
   # set up parameters for selection
   start.date <- as.POSIXct("2009-01-01T00:00:00",
                              format = "%Y-%m-%dT%H:%M:%OS")
15
   end.date <- as.POSIXct("2010-01-01T00:00:00", format = "%Y-%m-%dT%H:%M:%OS")
16
   min.longitude <- 10.5
17
18 max.longitude <- 16
   min.latitude <- 40.5
   max.latitude <- 45
   MO < -2.5
21
22
   # set up conditions for selection
   aquila.sel <- (horus$time_date >= start.date) &
24
     (horus$time_date < end.date) &</pre>
     (horus$lon >= min.longitude) &
26
     (horus$lon <= max.longitude) &
27
     (horus$lat >= min.latitude) &
```

```
(horus$lat <= max.latitude) &</pre>
29
     (horus$M >= M0)
30
31
   # select
   aquila <- horus[aquila.sel, ]
   italy.map <- ne_countries(country = 'Italy', returnclass = "sf",</pre>
                               scale = 'medium')
3
   aquila.sf <- st_as_sf(aquila,
                         coords = c("lon", "lat"),
                         crs = st_crs('EPSG:4326'))
6
   ggplot() +
     geom_sf(data = aquila.sf[aquila$M > 3,], size = 0.4) +
     geom_sf(data = italy.map, fill = alpha("lightgrey", 0), color = 'green',
              linewidth = 0.7) +
10
     geom_sf(data = aquila.sf[aquila$M > 5,], size = 0.5, color = 'orange') +
11
     geom_sf(data = aquila.sf[aquila$M > 6,], size = 0.6, color = 'red') +
12
     ggtitle("Map of event locations")
13
```

Map of event locations



```
ggplot(aquila, aes(time_date, M)) +
geom_point() +
theme_bw()
```

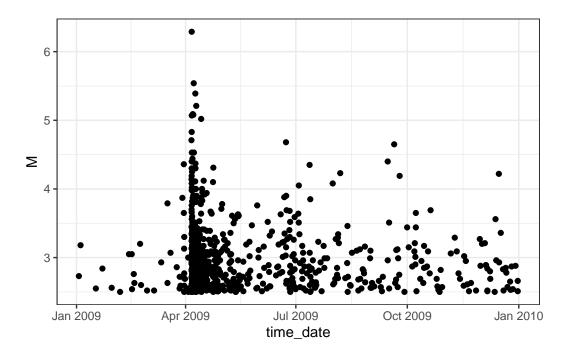


Figure 1: L'Aquila seismic sequence, times versus magnitudes

```
# set up data.frame for model fitting
aquila.bru <- data.frame(

ts = as.numeric(
    difftime(aquila$time_date, start.date, units = "days")
),
magnitudes = aquila$M,
idx.p = 1 : nrow(aquila)
)

# set up list of initial values
th.init <- list(
    th.mu = inv.link.f$mu(0.5),
    th.K = inv.link.f$K(0.1),
    th.alpha = inv.link.f$alpha(1),
    th.c = inv.link.f$c_(0.1),</pre>
```

```
th.p = inv.link.f$p(1.1)
8 )
1 # set starting and time of the time interval used for model fitting.
2 # In this case, we use the interval covered by the data.
3 T1 <- 0
4 T2 <- max(aquila.bru$ts) + 0.2 # Use <math>max(..., na.rm = TRUE) if there may
  # still be NAs here
1 # set up list of bru options
pru.opt.list <- list(</pre>
    bru_verbose = 3, # type of visual output
    bru_max_iter = 70, # maximum number of iterations
    # bru_method = list(max_step = 0.5),
    bru_initial = th.init # parameters' initial values
7
  )
  ETAS <- function(data = aquila.bru, m0 = M0, t1 = T1, t2 = T2,
                     ncore = num.cores, n.samp = 1000, max.batch = 1000,
2
                     mag = 4, n.breaks = 100, t.end.tri.post = 5,
                     t.end.tri.prior = 10, t.end.omori.post = 5,
                     t.end.omori.prior = 5){
       # maximum likelihood estimator for beta
       beta.p <- 1 / (mean(data$magnitudes) - m0)</pre>
       # fit the model
       model.fit <- Temporal.ETAS(</pre>
         total.data = data,
         MO = mO,
13
         T1 = t1,
14
         T2 = t2,
16
         link.functions = link.f,
         coef.t. = 1,
         delta.t. = 0.1,
         N.max. = 5,
         bru.opt = bru.opt.list
       )
21
22
       # create input list to explore model output
23
```

```
input_list <- list(</pre>
24
          model.fit = model.fit,
25
          link.functions = link.f
        )
        # get marginal posterior information
29
        post.list <- get_posterior_param(input.list = input_list)</pre>
30
31
        # plot marginal posteriors
32
        postplot <- post.list$post.plot</pre>
33
        # posterior sampling
        post.samp <- post_sampling(</pre>
36
          input.list = input_list,
37
          n.samp = n.samp,
38
          max.batch = max.batch,
39
          ncore = num.cores
        )
        # pair plot
        pair.plot <- post_pairs_plot(</pre>
44
          post.samp = post.samp,
45
          input.list = NULL,
46
          n.samp = NULL,
47
          max.batch = max.batch
        pairplot <- pair.plot$pair.plot</pre>
51
        # set additional elements of the list
52
        input_list$T12 <- c(t1, t2)
53
        input_list$MO <- mO</pre>
54
        input_list$catalog.bru <- data</pre>
        # posterior number of events
        N.post <- get_posterior_N(input.list = input_list)</pre>
        Npostplot <- N.post$post.plot</pre>
59
60
        # triggering function plots
61
        # posterior
62
        triplotpost <- triggering_fun_plot(</pre>
63
          input.list = input_list,
64
```

```
post.samp = post.samp,
          n.samp = NULL, magnitude = mag,
66
          t.end = t.end.tri.post, n.breaks = n.breaks
67
        )
68
69
        # prior
70
        triplotprior <- triggering_fun_plot_prior(input.list = input_list,</pre>
71
                                   magnitude = mag, n.samp = n.samp,
72
                                    t.end = t.end.tri.prior)
        # omori plots
75
        # posterior
76
        omoripost <- omori_plot_posterior(input.list = input_list,</pre>
77
                              post.samp = post.samp,
78
                              n.samp = NULL, t.end = t.end.omori.post)
79
        # prior
        omoriprior <- omori_plot_prior(input.list = input_list, n.samp = n.samp,</pre>
82
                          t.end = t.end.omori.prior)
83
84
        # returns the whole environment
        envir <- as.list(environment())</pre>
       return(tibble::lst(envir))
87
   etas <- ETAS()
Start creating grid...
Finished creating grid, time 3.307242
Synthetic catalogues generation
   set.seed(2)
   mult.synth.ETAS <- function(t1 = NULL, t2 = NULL, n.cat = 1,
                          ht = etas$envir$data[which.max(
                              etas$envir$data$magnitudes), ]){
4
        # inherits the environment of `etas`
        envir <- etas$envir</pre>
        # updates environments if specified by users
        envir$t1 <- ifelse(!is.null(t1), t1, envir$t1)</pre>
10
```

```
envir$t2 <- ifelse(!is.null(t2), t2, envir$t2)</pre>
11
12
        # generate catalogues as list of lists
13
        multi.synth.cat.list <- lapply(seq_len(n.cat), \(x)</pre>
        generate_temporal_ETAS_synthetic(
          theta = envir$post.samp[x, ], beta.p = envir$beta.p,
16
          MO = envir$mO, T1 = envir$t1,
17
          T2 = envir$t2, Ht = ht, ncore = envir$ncore))
18
19
        # store catalogues as list of data.frames
        multi.synth.cat.list.df <- lapply(multi.synth.cat.list,</pre>
                                             \(x) do.call(rbind, x))
22
        # set catalogue identifier
        multi.synth.cat.list.df <- lapply(seq_len(n.cat),</pre>
24
                                             \(x) cbind(
25
                                                 multi.synth.cat.list.df[[x]],
26
                                                   cat.idx = x))
27
        # merge catalogues in unique data.frame
        multi.synth.cat.df <- do.call(rbind, multi.synth.cat.list.df)</pre>
        # we need to bing the synthetics with the observed catalogue for plotting
        cat.df.for.plotting <- rbind(</pre>
32
          multi.synth.cat.df,
33
          cbind(envir$data[, c("ts", "magnitudes")],
            gen = NA, cat.idx = "observed"
          )
        )
        # plot them
39
        multi.synth.cat.plot <- ggplot(cat.df.for.plotting,</pre>
40
                                         aes(ts, magnitudes)) +
41
          geom_point(size = 0.5) +
42
          geom_point(
43
            data = ht, mapping = aes(ts, magnitudes), color = "red"
          facet_wrap(facets = ~cat.idx)
46
47
        # modelling
48
        multi.synth.etas <- ETAS(data = multi.synth.cat.df,</pre>
49
                                   t1 = envir$t1, t2 = envir$t2)
50
```

```
# returns the synthetic dataset with plots, as well as the modelling
52
       # results
53
       return(tibble::lst(cat.df.for.plotting, multi.synth.cat.plot,
54
                           multi.synth.etas))
55
56
   mult.synth.fit <- mult.synth.ETAS()</pre>
 Start creating grid...
Finished creating grid, time 1.788598
Forecasting
  ETAS.forecast <- function(){</pre>
       # inherits the environment of `etas`
       envir <- etas$envir</pre>
       # express 1 minute in days
       min.in.days <-1 / (24 * 60)
       # find time of the event with the greatest magnitude
       t.max.mag <- envir$data$ts[which.max(envir$data$magnitudes)]</pre>
       # set starting time of the forecasting period
10
       T1.fore <- t.max.mag + min.in.days</pre>
       # set forecast length
12
       fore.length <- 1
13
       # set end time of the forecasting period
14
       T2.fore <- T1.fore + fore.length
       # set known data
       Ht.fore <- envir$data[envir$data$ts < T1.fore, ]</pre>
       # produce forecast
19
       daily.fore <- Temporal.ETAS.forecast(</pre>
20
         post.samp = envir$post.samp, # ETAS parameters posterior samples
21
         n.cat = nrow(envir$post.samp), # number of synthetic catalogues
         beta.p = envir$beta.p, # magnitude distribution parameter
         MO = envir$mO, # cutoff magnitude
         T1 = T1.fore, # forecast starting time
         T2 = T2.fore, # forecast end time
         Ht = Ht.fore, # known events
         ncore = envir$ncore # number of cores
28
```

```
30
        # find number of events per catalogue
31
       N.fore <- vapply(</pre>
32
          seq_len(daily.fore$n.cat),
          \(x)  sum(daily.fore$fore.df$cat.idx == x), 0
        # find number of observed events in the forecasting period
       N.obs <- sum(envir$data$ts >= T1.fore & envir$data$ts <= T2.fore)</pre>
        # plot the distribution
       histfore <- ggplot() +</pre>
39
          geom_histogram(aes(x = N.fore, y = after_stat(density)),
40
                          binwidth = 1) +
41
          geom_vline(xintercept = N.obs) +
          xlim(100, 500)
       return(histfore)
46
   histfore <- ETAS.forecast()</pre>
   # save.image()
```