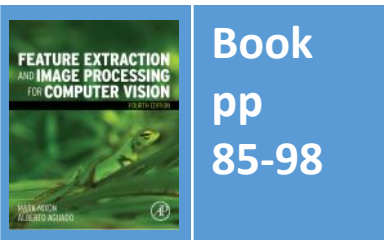


# Lecture 4 Point Operators

COMP3204 & COMP6223 Computer Vision

**How many different operators are there which operate on image points?**



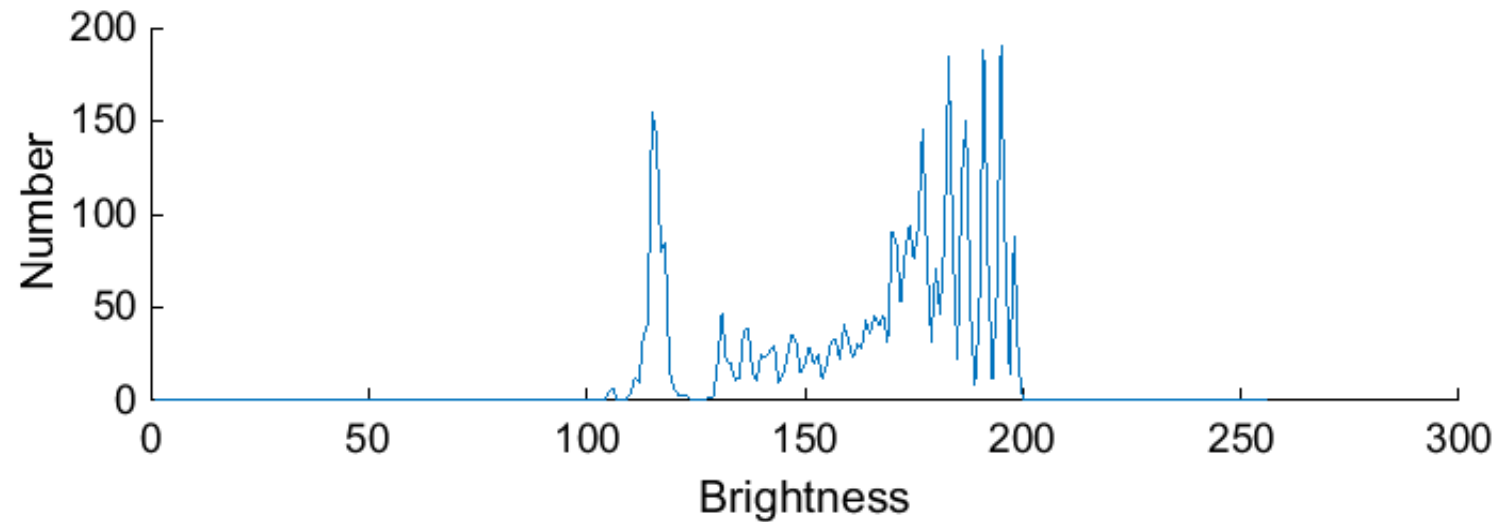
**Department of  
Electronics and  
Computer Science**

**UNIVERSITY OF  
Southampton**  
School of Electronics  
and Computer Science

# An image and its histogram



**(a)** image of an eye



**(b)** histogram of eye image



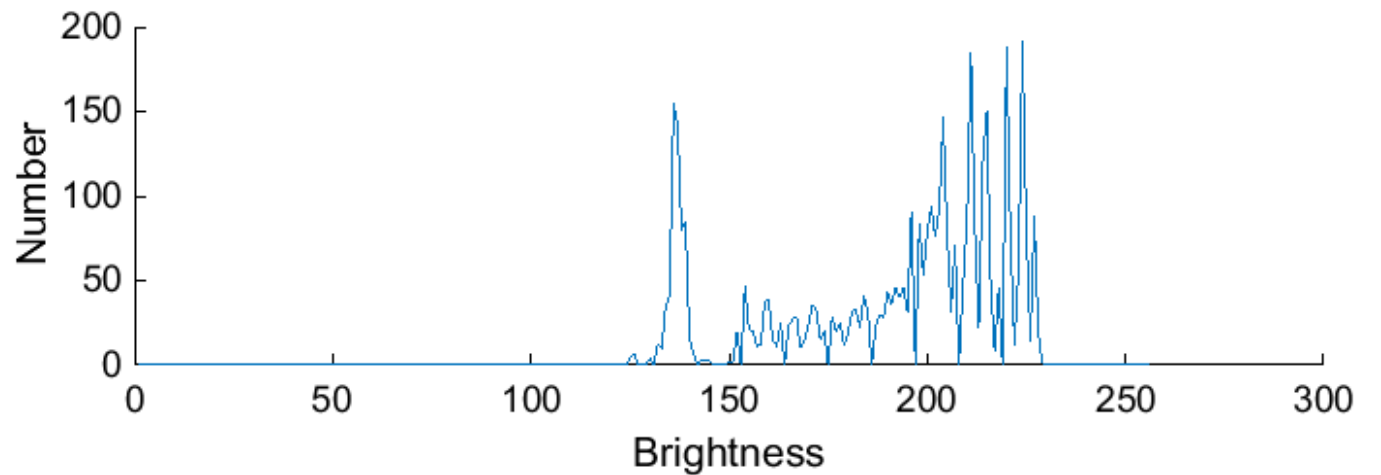
# Brightening an image

$$\mathbf{N}_{x,y} = k \times \mathbf{O}_{x,y} + l$$

new image **N**; old image **O**; gain  $k$ ; level  $l$ ; co-ordinates  $x,y$



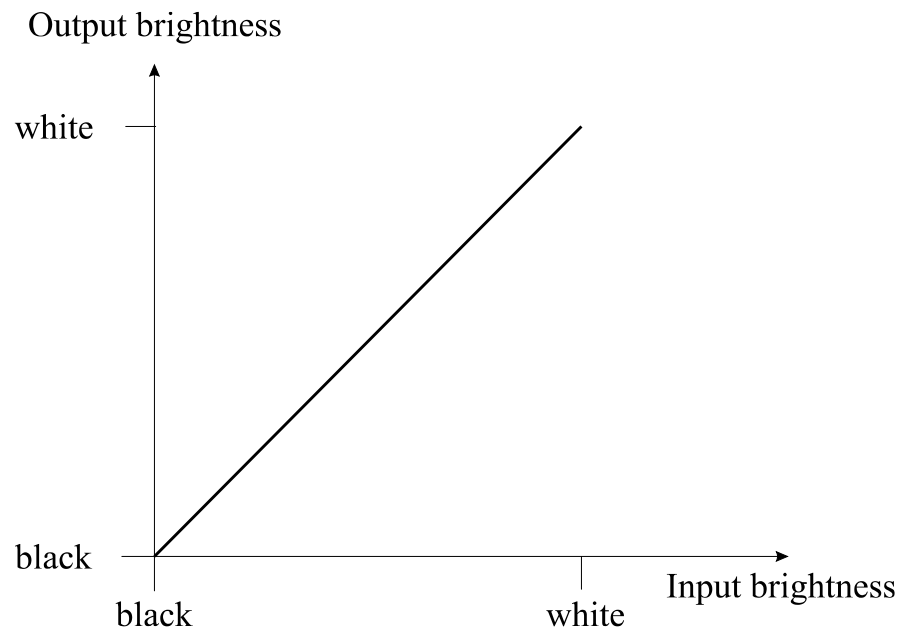
(a) image of brighter eye



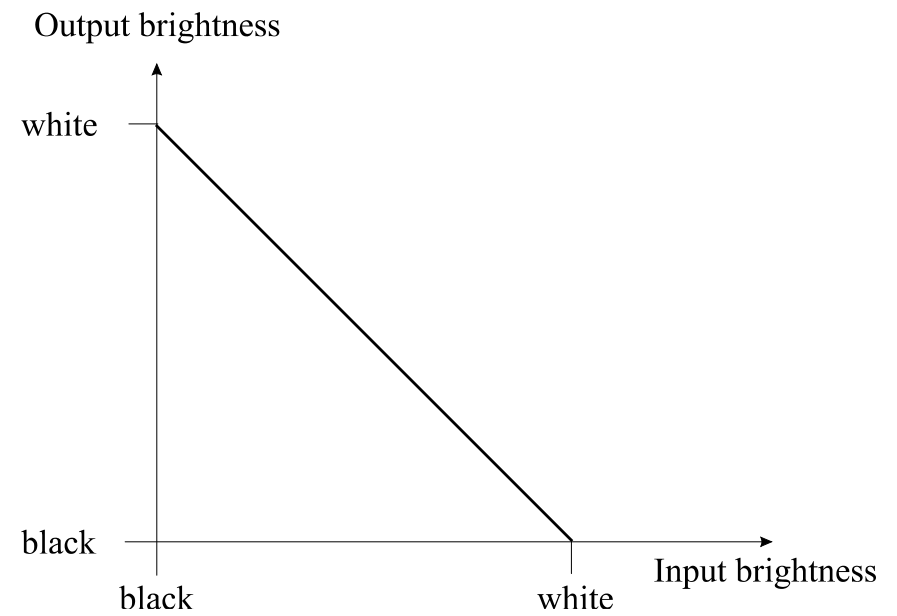
(b) histogram of brighter eye



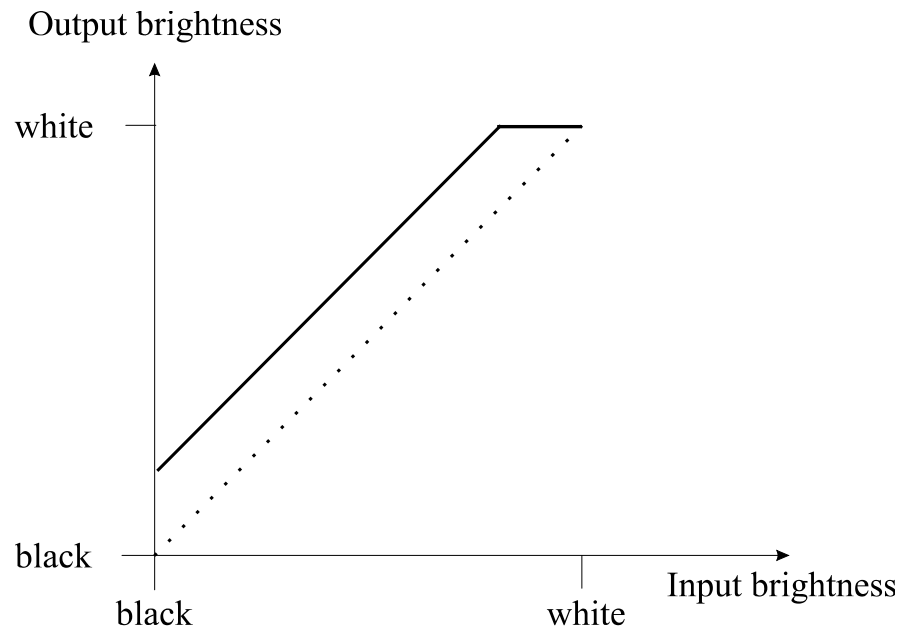
# Intensity mappings



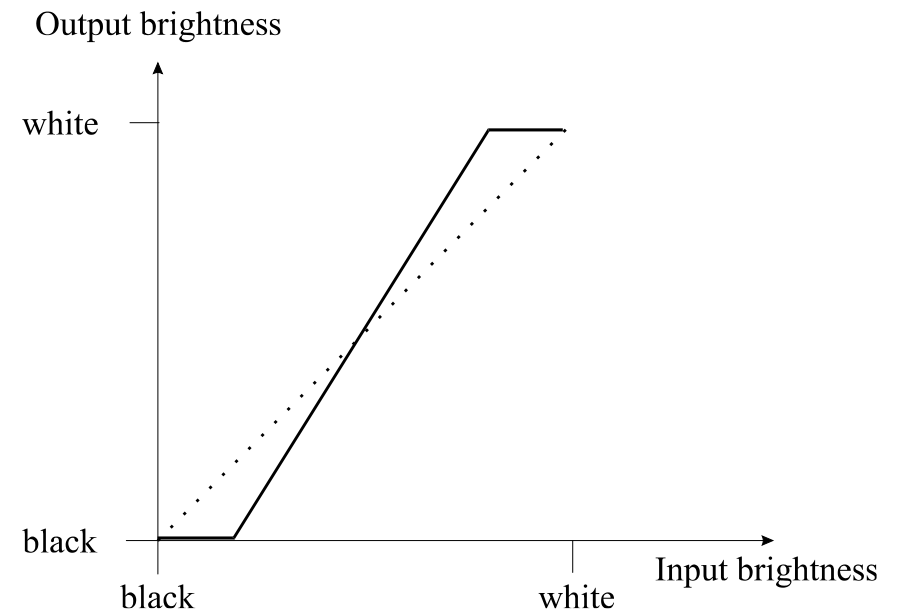
**(a) copy**



**(b) brightness inversion**



**(c) brightness addition**



**(d) brightness scaling by multiplication**



# Applying exponential and logarithmic point operators



**(a)** logarithmic compression



**(b)** exponential expansion

$$\mathbf{N}_{x,y} = \log(\mathbf{O}_{x,y})$$

$$\mathbf{N}_{x,y} = \exp(\mathbf{O}_{x,y})$$

# Intensity normalisation

$$\mathbf{N}_{x,y} = \frac{\mathbf{Nmax} - \mathbf{Nmin}}{\mathbf{Omax} - \mathbf{Omin}} \times (\mathbf{O}_{x,y} - \mathbf{Omin}) + \mathbf{Nmin} \quad \forall x, y \in 1, N$$

new image **N**; old image **O**; co-ordinates  $x,y$

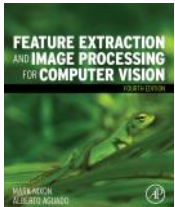
minimum input  **$N_{min}$**

maximum input  **$N_{max}$**

minimum output  **$O_{min}$**

maximum output  $O_{max}$

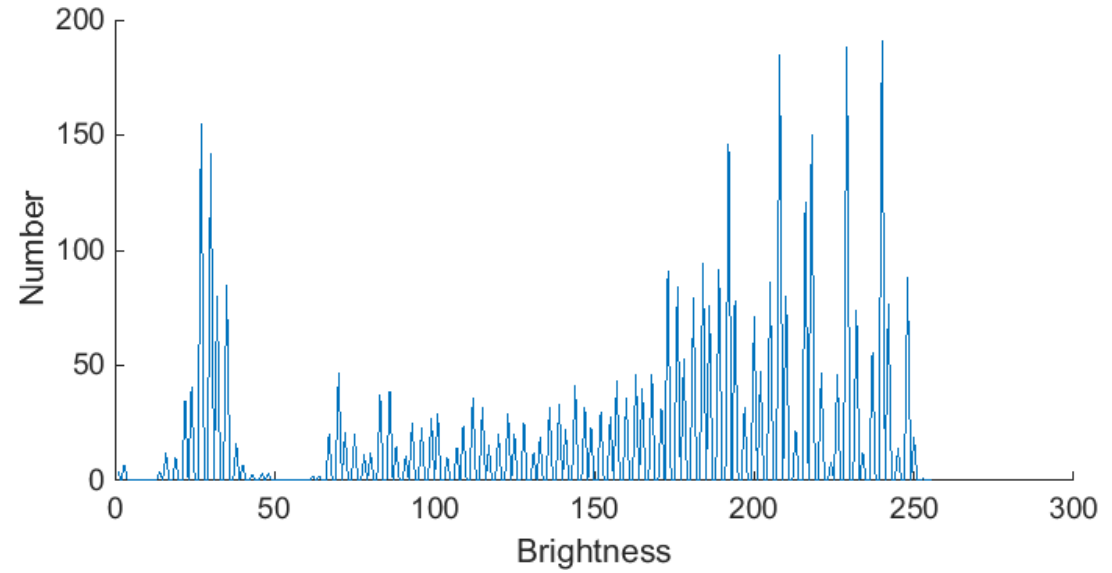
## Avoids need for parameter choice



# Intensity normalisation and histogram equalisation



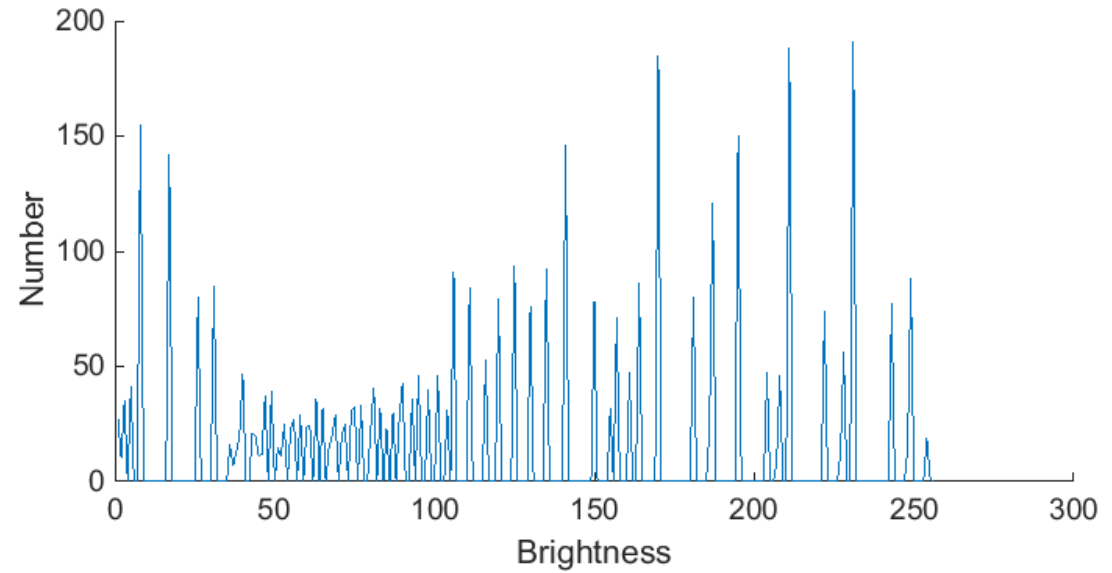
**(a)** intensity normalised eye



**(b)** histogram of intensity normalised eye



**(c)** histogram equalised eye



**(d)** histogram of histogram equalised eye



# Histogram Equalisation

$N^2$  points in the image; the sum of points per level is equal  $\sum_{l=0}^M \mathbf{O}(l) = \sum_{l=0}^M \mathbf{N}(l)$

cumulative histogram up to level  $p$  should be transformed to cover up to the level  $q$   $\sum_{l=0}^p \mathbf{O}(l) = \sum_{l=0}^q \mathbf{N}(l)$

number of points per level in the output picture  $\mathbf{N}(l) = \frac{N^2}{\mathbf{N}_{max} - \mathbf{N}_{min}}$

cumulative histogram of the output picture  $\sum_{l=0}^q \mathbf{N}(l) = q \times \frac{N^2}{\mathbf{N}_{max} - \mathbf{N}_{min}}$

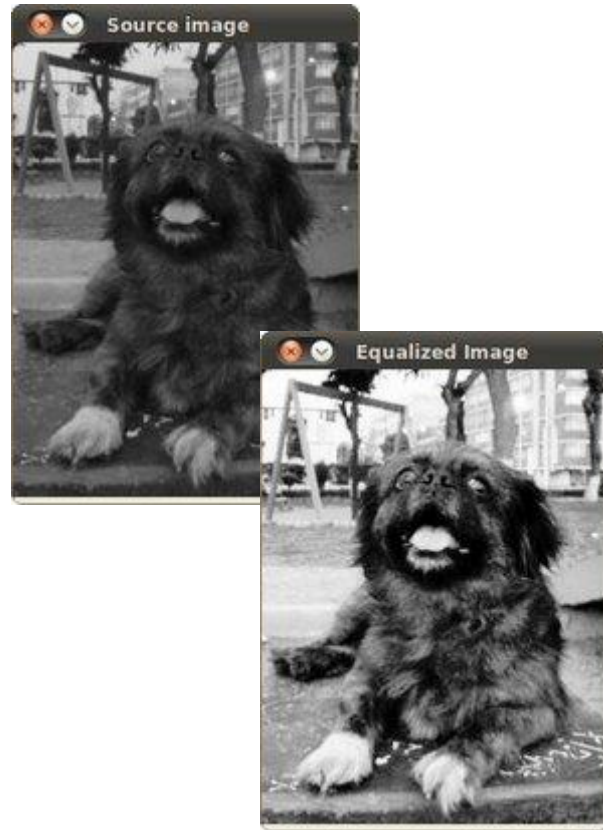
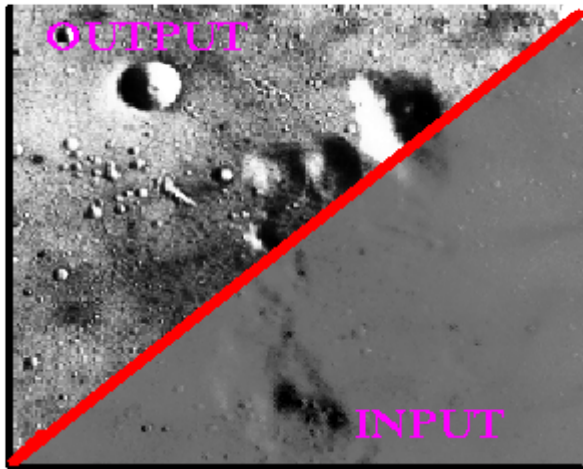
$$q = \frac{\mathbf{N}_{max} - \mathbf{N}_{min}}{N^2} \times \sum_{l=0}^p \mathbf{O}(l)$$

mapping for the output pixels at level  $q$





# Applying intensity normalisation and histogram equalisation



<http://homepages.inf.ed.ac.uk/rbf/HIPR2/histeq.htm>;

[http://docs.opencv.org/doc/tutorials/imgproc/histograms/histogram\\_equalization/histogram\\_equalization.html](http://docs.opencv.org/doc/tutorials/imgproc/histograms/histogram_equalization/histogram_equalization.html) ;

<http://www.softpedia.com/get/Multimedia/Video/Other-VIDEO-Tools/Easy-Histogram-Equalization.shtml>

# Thresholding an eye image

$$N_{x,y} = \begin{cases} 255 & \text{if } N_{x,y} > \text{threshold} \\ 0 & \text{otherwise} \end{cases}$$



# Thresholding an eye image: manual vs automatic

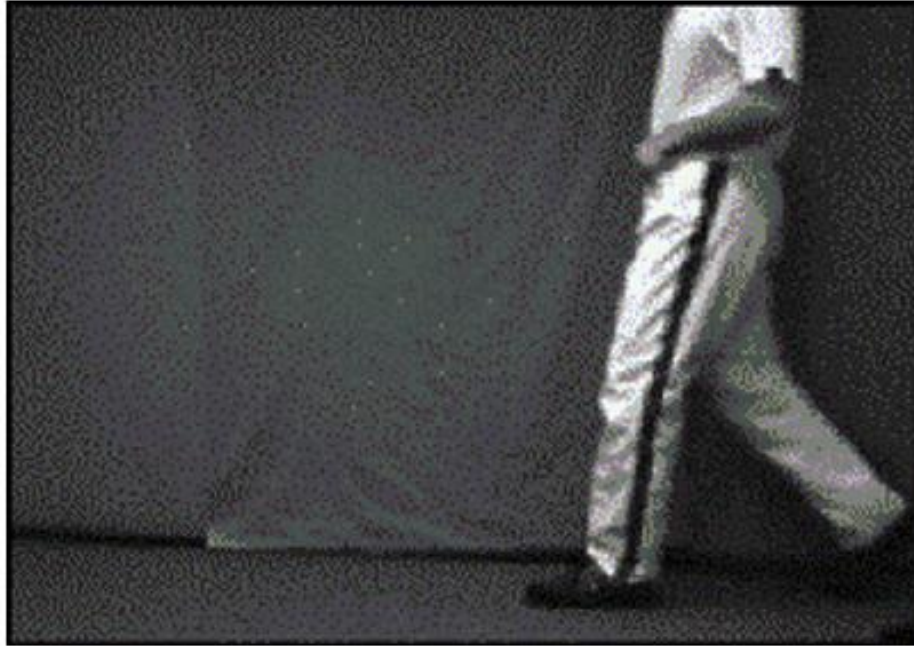


**(a)** thresholding at level 160



**(b)** thresholding by Otsu (level = 127)

# Thresholding an image of a walking subject



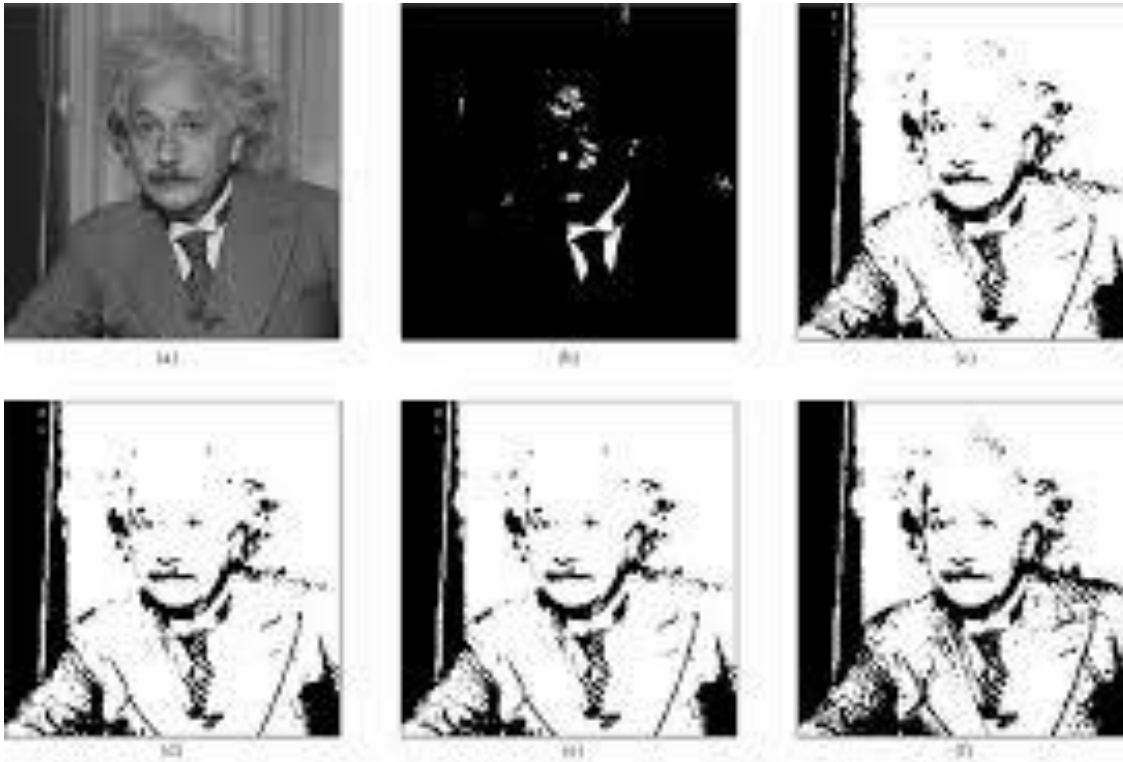
**(a)** walking subject



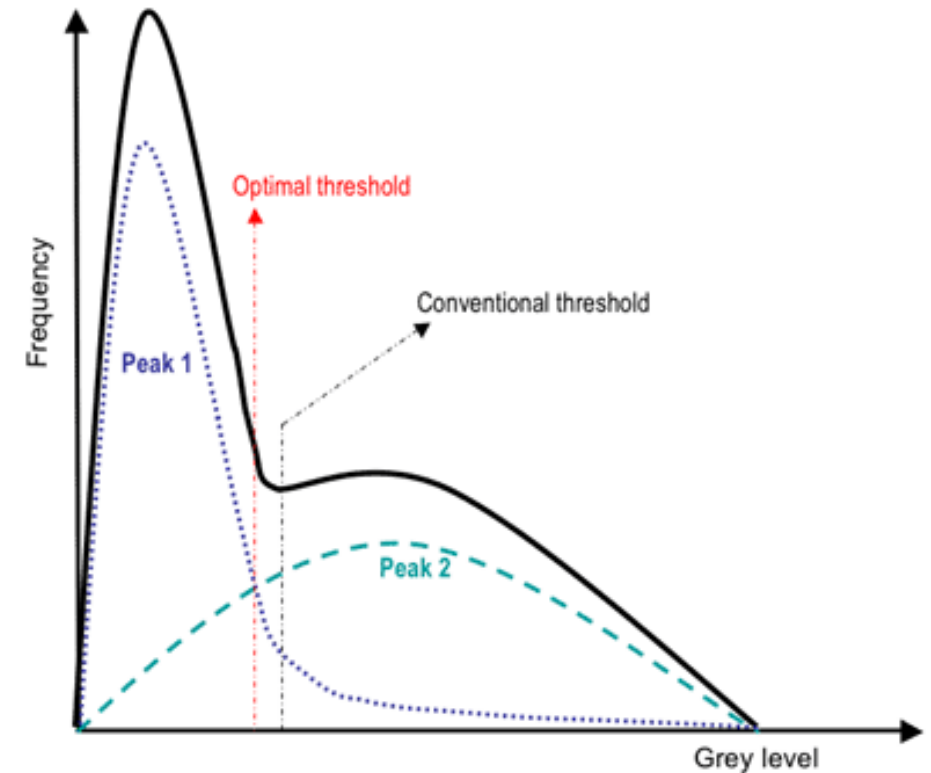
**(b)** automatic thresholding by Otsu

# Advanced thresholding

## Entropic thresholding (2010)



## Optimal thresholding



<http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1096546;>

<https://www.cs.auckland.ac.nz/courses/compsci773s1c/lectures/ImageProcessing-html/topic3.htm>