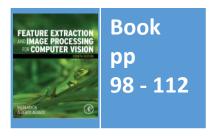
Lecture 5 Group Operators

COMP3204 & COMP6223 Computer Vision

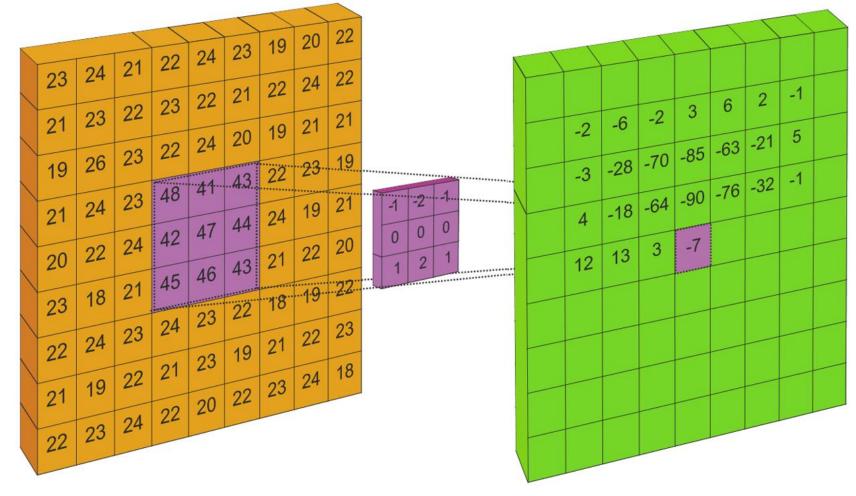
How do we combine points to make a new point in a new image?







Template convolution







Template convolution

100	100	200	200	200
100	100	200	200	200
100	100	200	200	200
200	200	400	400	400
300	300	400	400	400

0	0	0	0	0
0	400	400	0	0
0	400	400	0	0
0	400	400	0	0
0	0	0	0	0

 G_{y}

Result

0	0	0	0	0
0	400	400	0	0
0	640	806	800	0
0	894	894	800	0
0	0	0	0	0

0	0	0	0	0
0	0	0	0	0
0	500	700	800	0
0	800	800	800	0
0	0	0	0	0





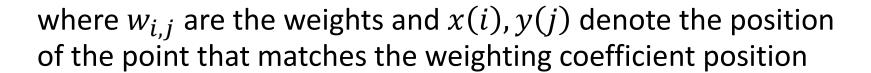


3×3 template and weighting coefficients

w ₀	w_I	w_2
W3	W4	W5
W6	w_7	W8

$$\mathbf{N}_{x,y} = \sum_{i \in \text{template } j \in \text{template}} w_{i,j} \times \mathbf{O}_{x(i),y(j)}$$





3×3 averaging operator

$$\mathbf{N}_{x,y} = \frac{1}{9} \sum_{i \in 3} \sum_{j \in 3} \mathbf{O}_{x(i),y(j)}$$

1/9	1/9	1/9
1/9	1/9	1/9
1/9	1/9	1/9

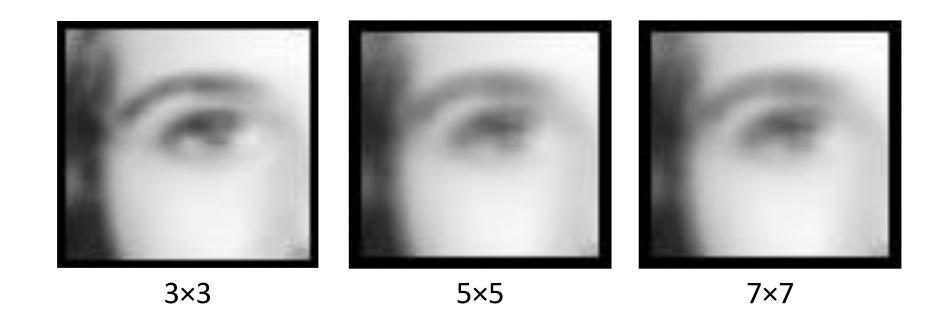








Illustrating the effect of window size





Template convolution via the Fourier transform

Allows for fast computation for template size ≥ 7×7

$$\mathbf{P} * \mathbf{T} = \mathfrak{I}^{-1} \left(\mathfrak{I}(\mathbf{P}) . \times \mathfrak{I}(\mathbf{T}) \right)$$

Template convolution *

Fourier transform of the picture, $\mathfrak{I}(\mathbf{P})$

Fourier transform of the template, $\Im(T)$

Point by point multiplication (.x).





Beware of clowns ... Oxford

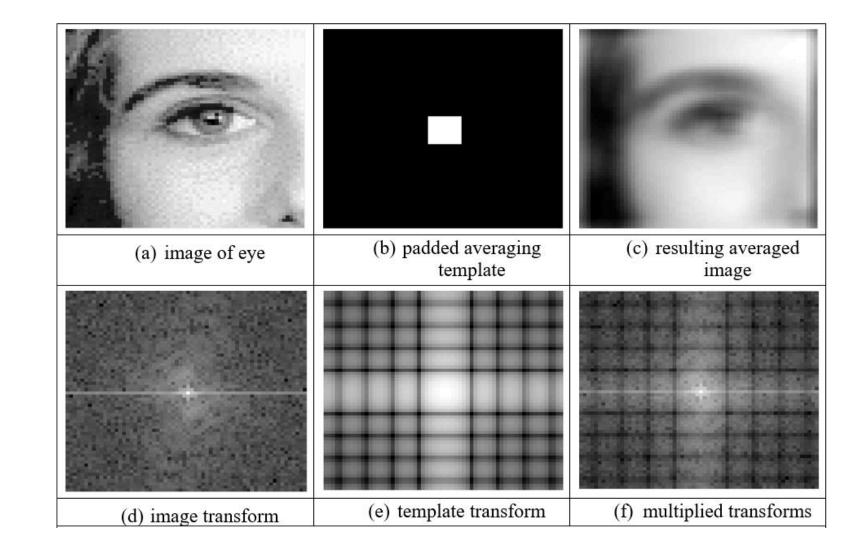
$$f(x,y) * h(x,y) \Leftrightarrow F(u,v)H(u,v)$$

Imperial

$$w(t) = u(t) * v(t) \Leftrightarrow W(f) = U(f)V(f)$$

it's point by point!!

Template Convolution via the Fourier Transform





2D Gaussian function

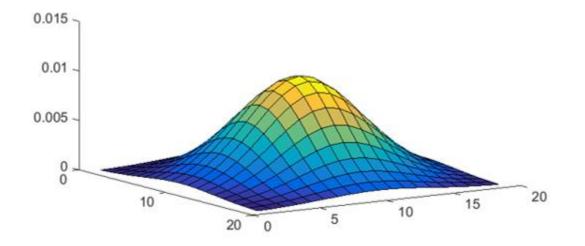
$$g(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{\frac{-(x^2+y^2)}{2\sigma^2}}$$

- Used to calculate template values
- Note compromise between variance σ^2 and window size
- Common choices 5×5, 1.0; 7×7, 1.2; 9×9, 1.4





2D Gaussian function and template

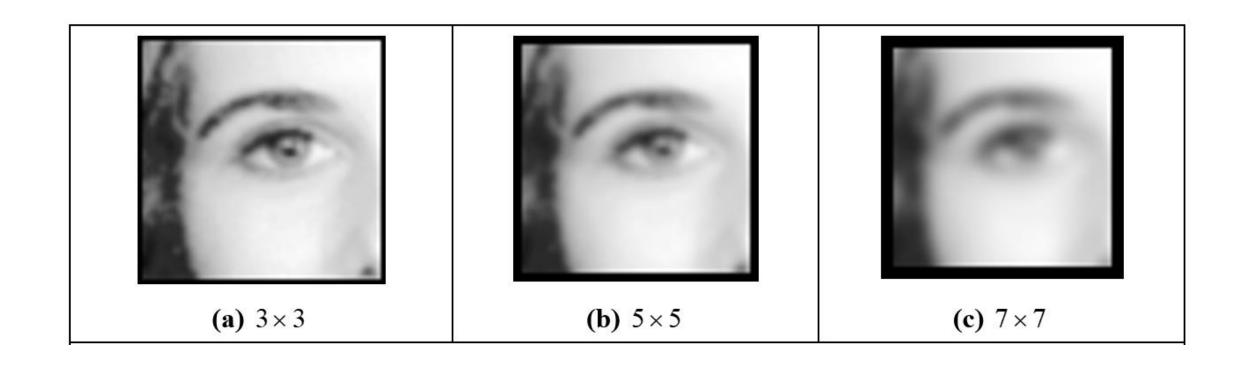


0.002	0.013	0.022	0.013	0. 002
0.013	0.060	0. 098	0.060	0.013
0.022	0. 098	0.162	0. 098	0.022
0.013	0. 060	0.098	0. 060	0.013
0. 002	0.013	0.022	0.013	0. 002





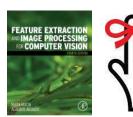
Applying Gaussian averaging





Finding the median from a 3×3 template

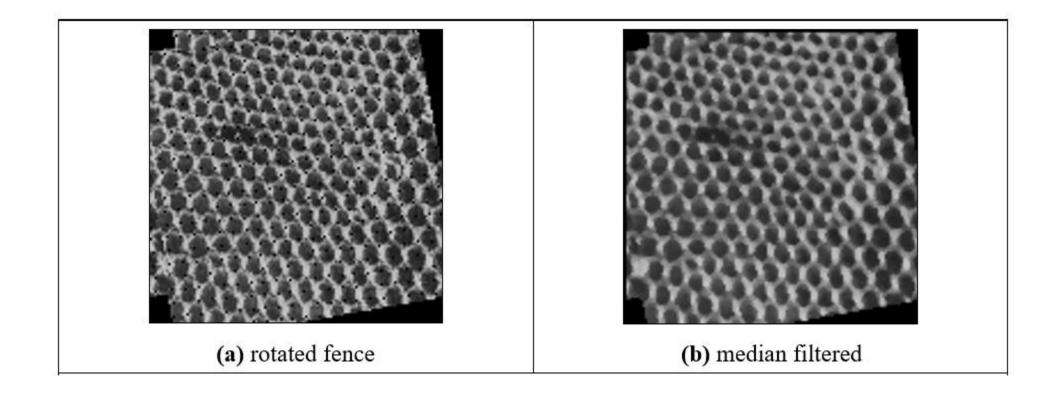
	2	8	7										
	4	0	6		2	4	3	8	0	5	7	6	7
	3	5	7										
((a) 3	×3 re	gion	(b) unsorted vector									
					0	2	3	4	5	6	7	7	8
				↑ median									
				(c) sorted vector, giving median									



Finding the median from a 3×3 template

Preserves edges

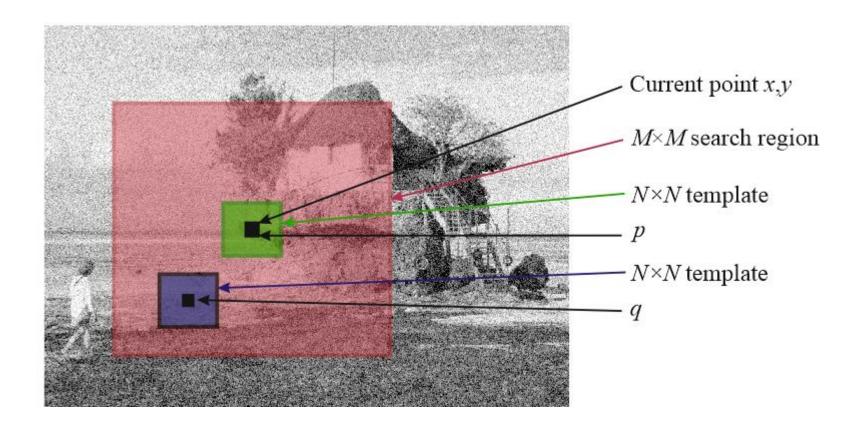
Removes salt and pepper noise





Newer stuff: non local means

Averaging which preserves regions



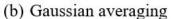


Applying non local means



(a) original image





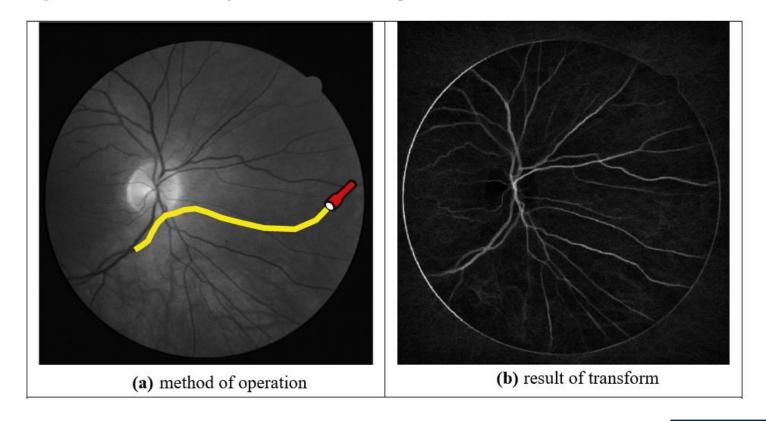


(c) nonlocal means



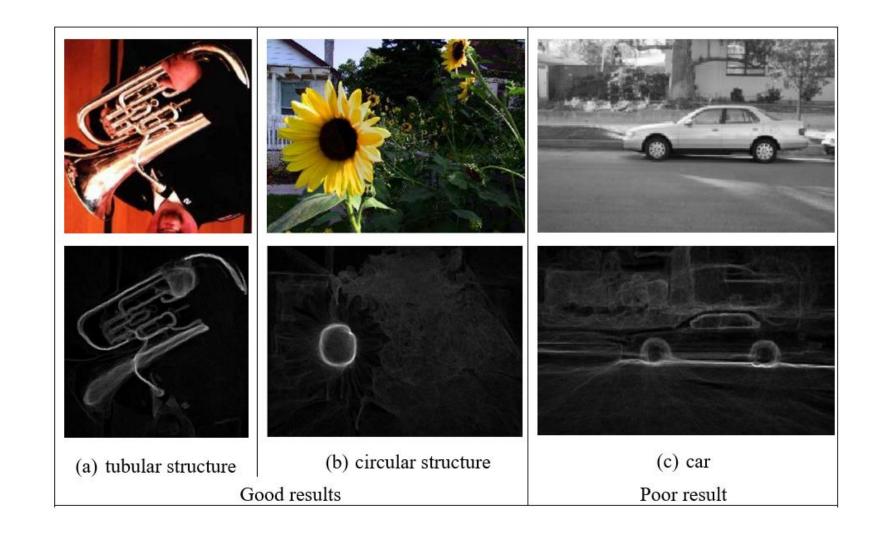
Even newer stuff: Image Ray Transform

Use analogy to light to find shapes, removing remainder

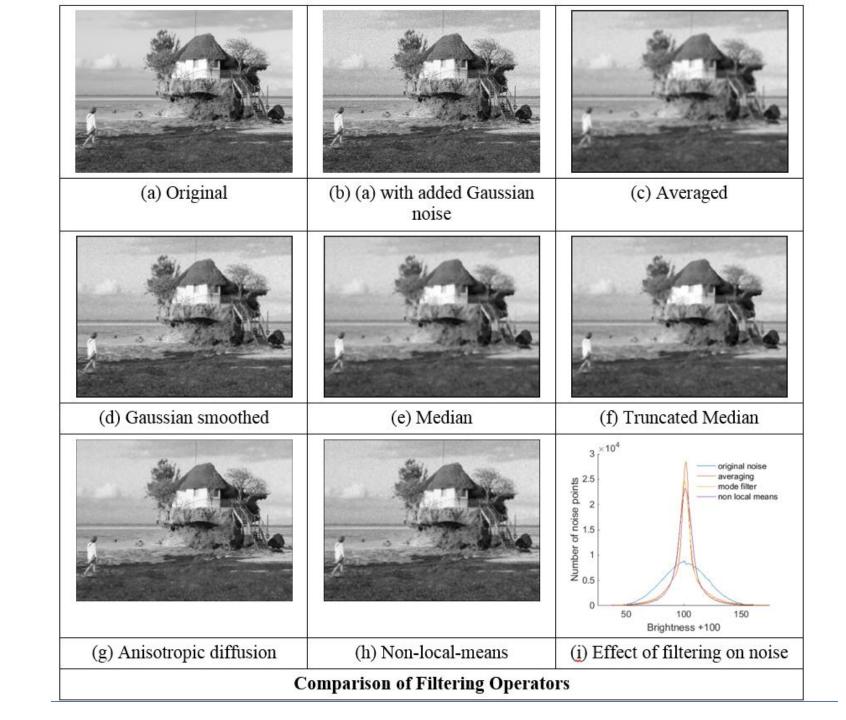




Applying Image Ray Transform







FEATURE EXTRACTION

AND IMAGE PROCESSING
FOR COMPUTER VISION