

Robotics Basics

Prof. Yunzhu Li
Spring 2024

CS598YL: Deep Learning for Robotic Manipulation
* Course materials adapted from Prof. Saurabh Gupta's ECE598SG at UIUC.

Logistics

- Presentation schedule is released.
- For the syllabus on the website, only papers with solid bullet points need to be presented. Papers with hollow bullet points are recommended but not required.
- After this week, the course format will be primarily student presentation/discussion, guest lectures, and project presentation.

Logistics

- The deadline for the slides for the first presentation is pushed back to tomorrow midnight (11:59 PM on 1/24/2024 Wednesday)
 - 01/30 (Tue) - Haozhe Si, Kulbir Singh Ahluwalia, Xin Xu
 - 02/01 (Thu) - Bryan Zhang, Vaibhav Dhanesh Raheja, Jose Cuaran

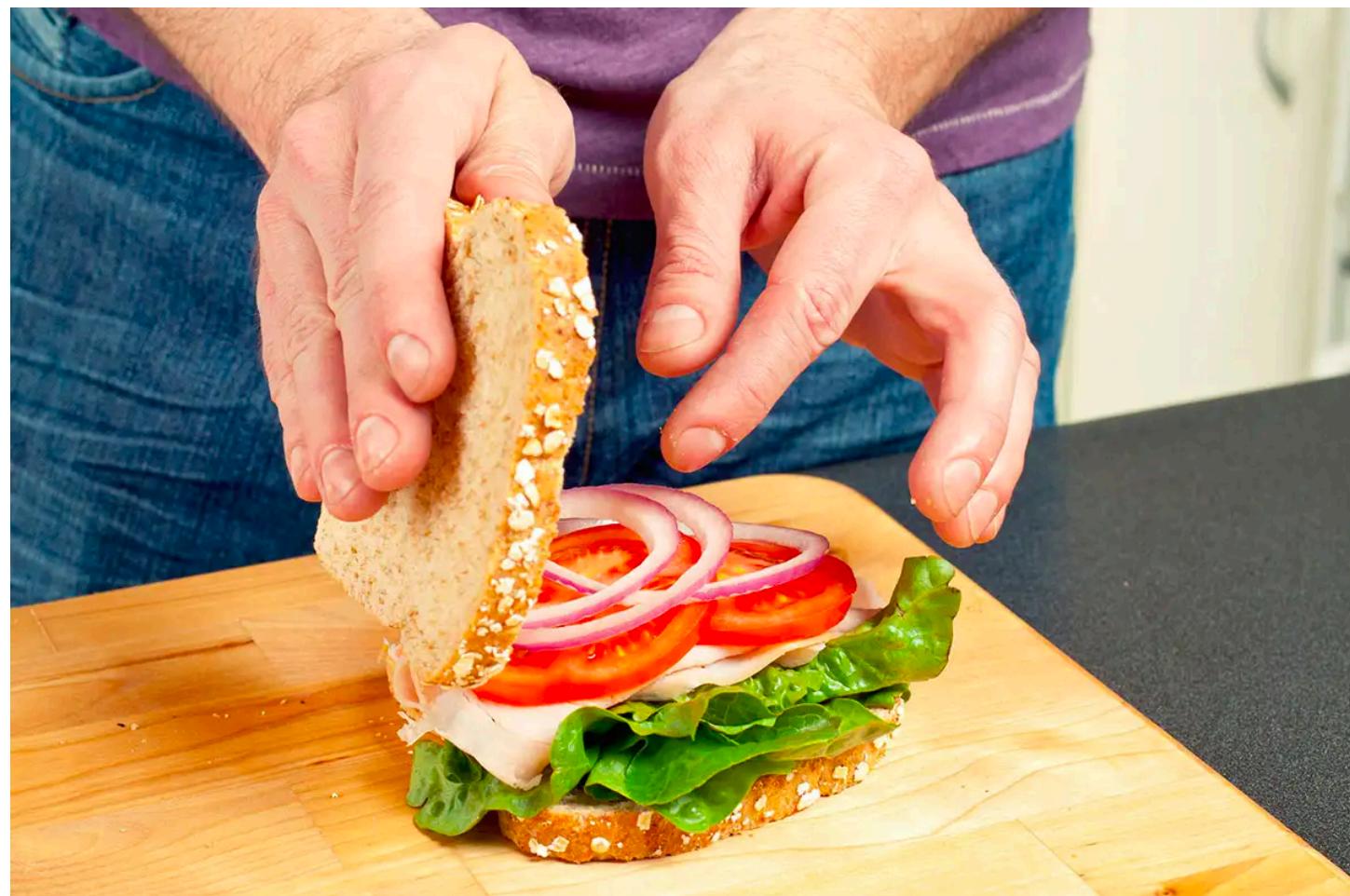
Logistics

- The feedback session for your presentation is on Thursday 1/25
 - 1:15-1:30 pm: Haozhe Si
 - 1:30-1:45 pm: Kulbir Singh Ahluwalia
 - 1:45-2:00 pm: Xin Xu
 - 2:00-2:15 pm: Bryan Zhang
 - 2:15-2:30 pm: Vaibhav Dhanesh Raheja
 - 2:30-2:45 pm: Jose Cuaran

Today's Agenda

- Robotic Tasks - Manipulation
- Terminology
- Observation and camera calibration
- How to move your robot?
 - Task space & configuration space
 - Forward kinematics and inverse kinematics
 - Path planning

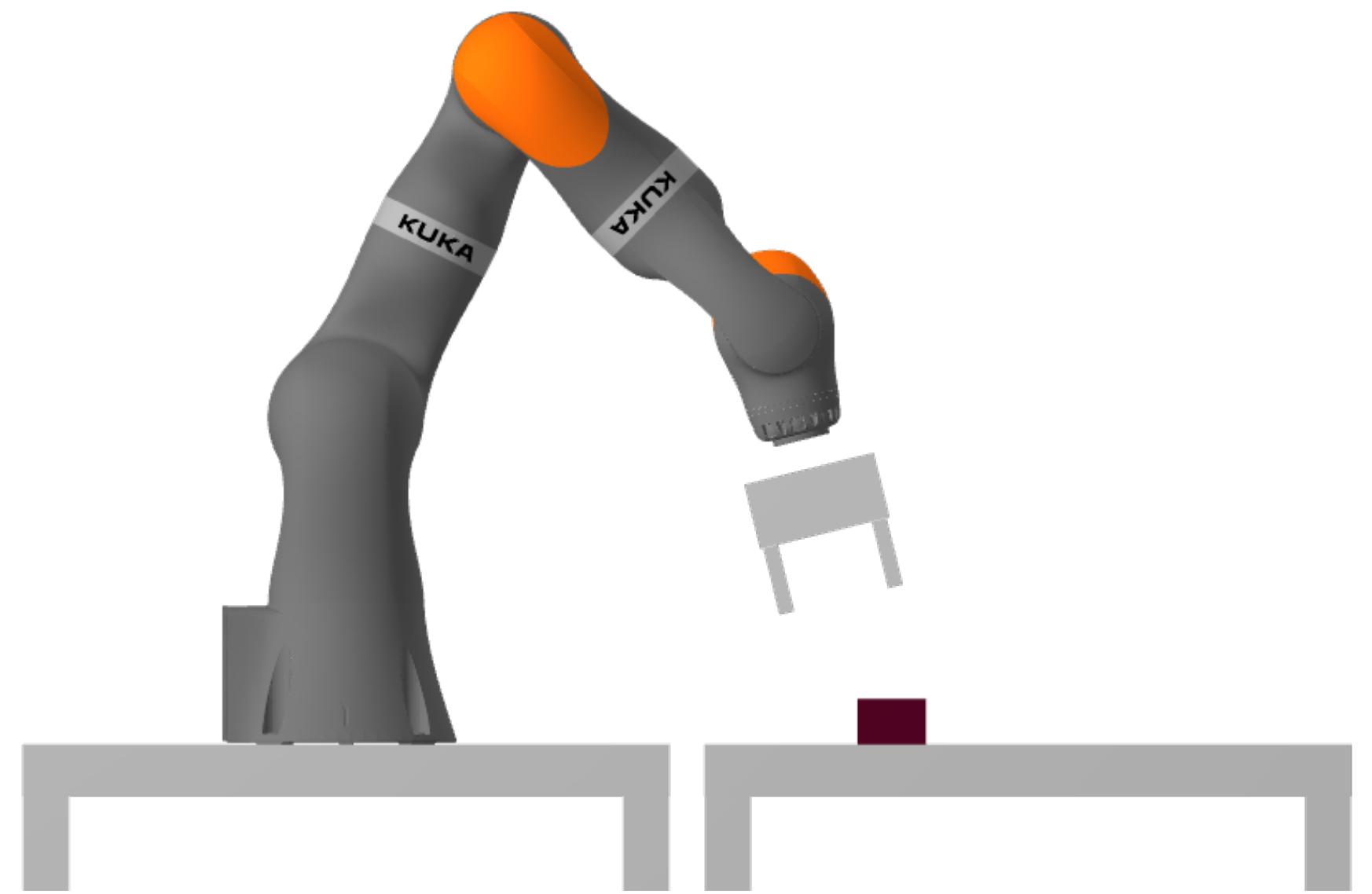
Robotic Tasks - Manipulation



Robotic Tasks - Manipulation

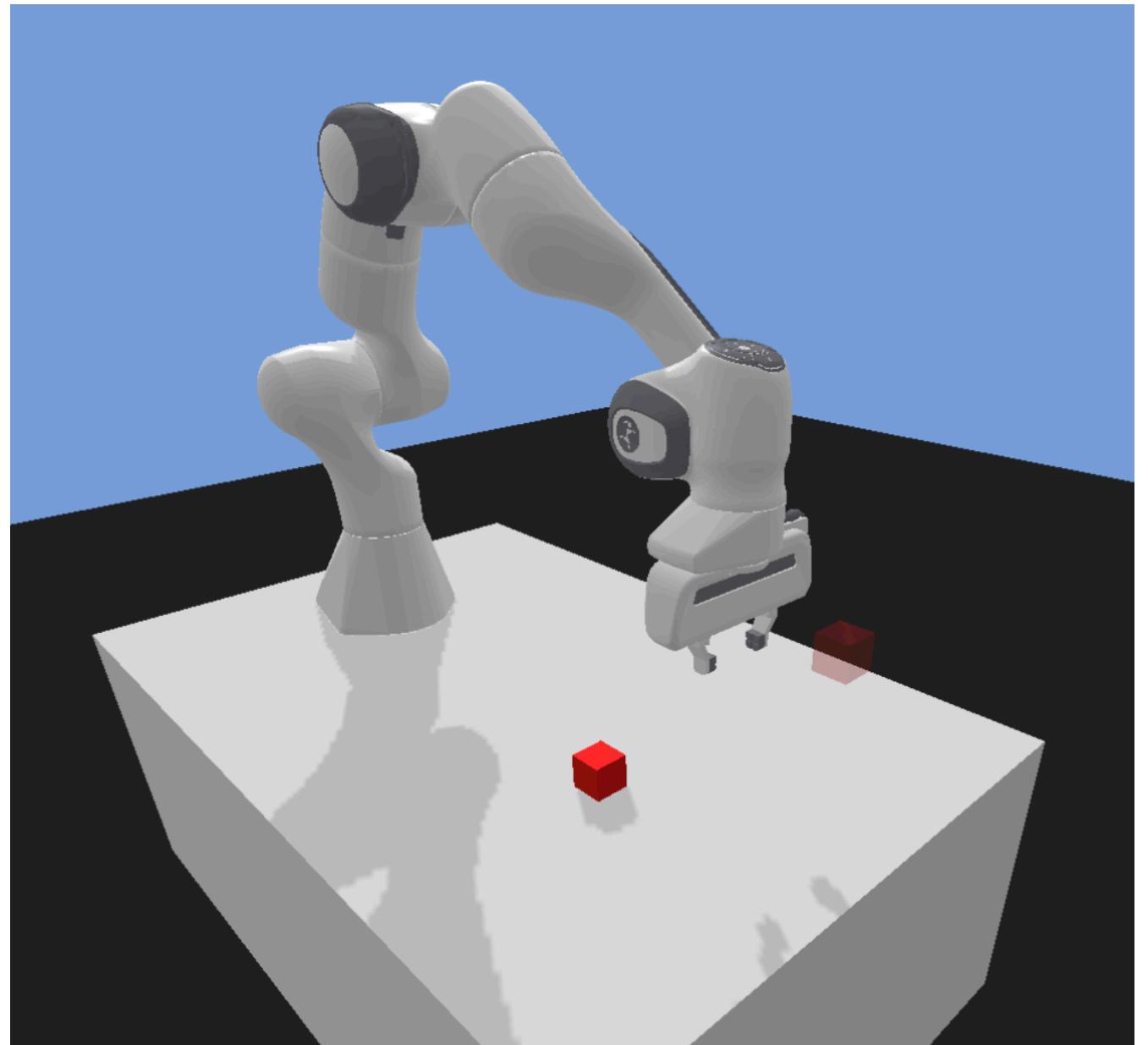
Robotic Tasks - Manipulation

- Task horizon



Robotic Tasks - Manipulation

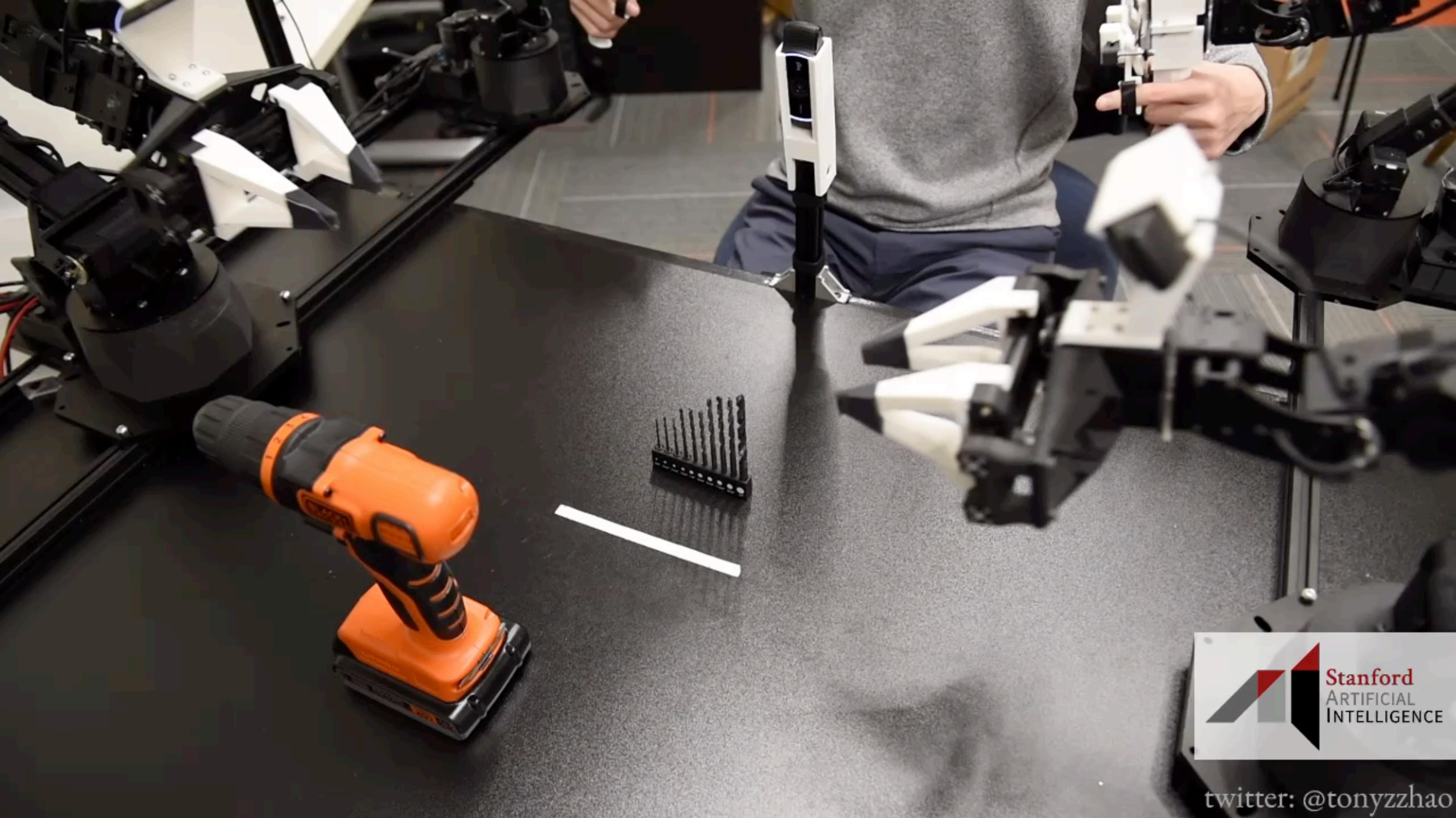
- Task horizon
- Number of objects involved
- Types of objects involved



Robotic Tasks - Manipulation

- Task horizon
- Number of objects involved
- Types of objects involved
- Your robot embodiment





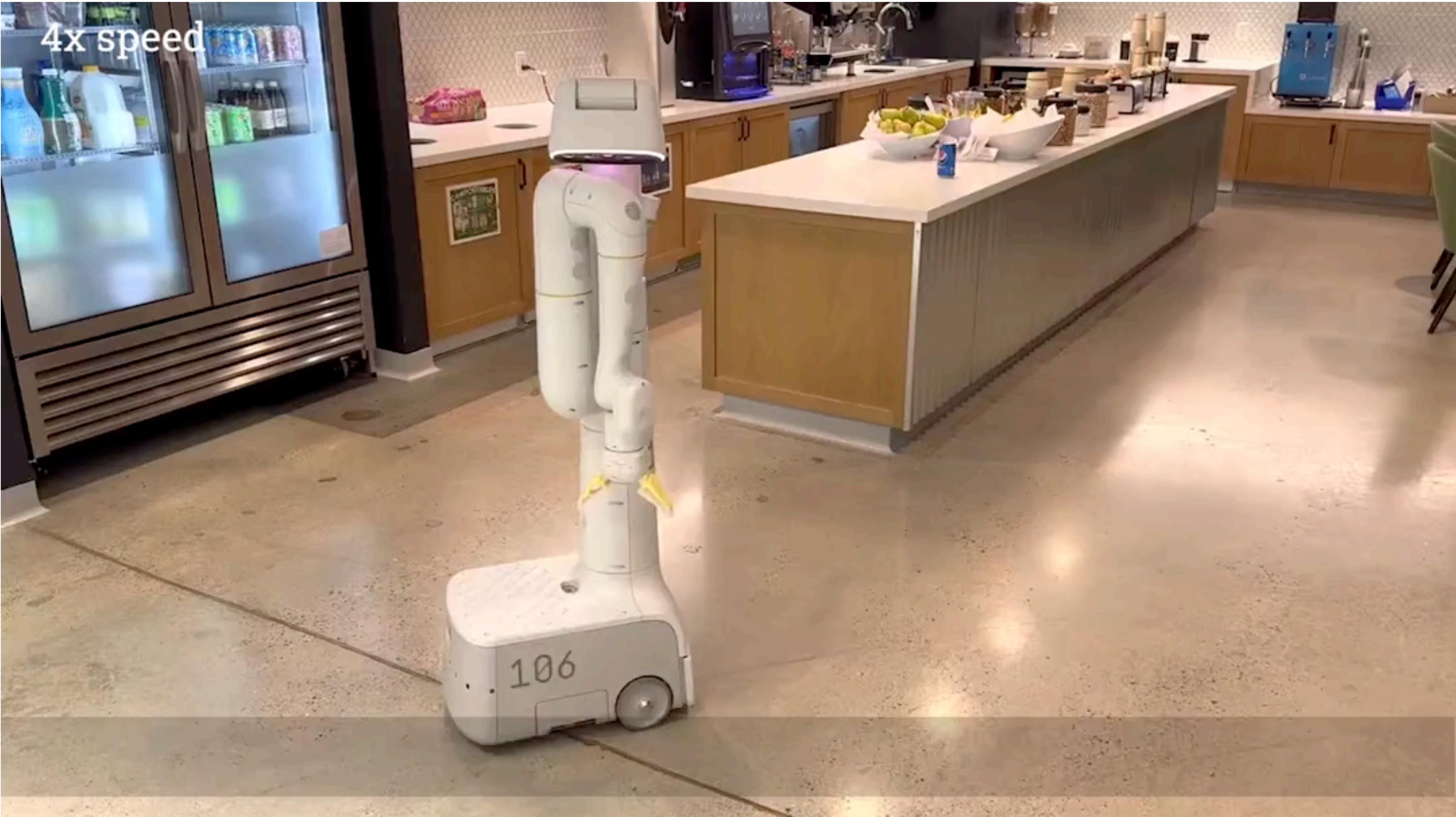
twitter: @tonyzzhao

The need for dexterous hands





The need for mobile manipulator



Robotic Tasks - Manipulation

- Task horizon
- Number of objects involved
- Types of objects involved
- Your robot embodiment



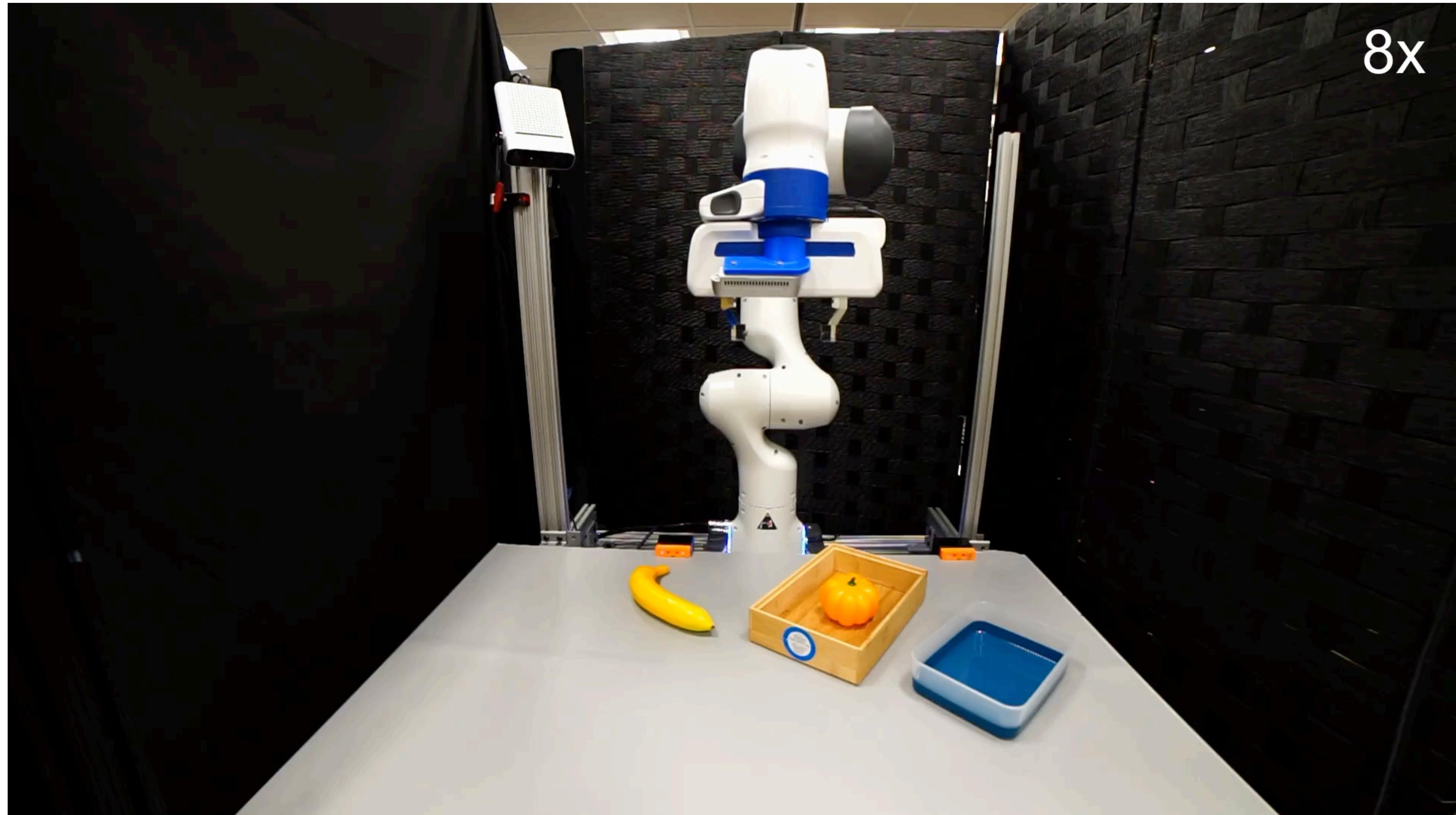
Robotic Tasks - Manipulation

- Task horizon
- Number of objects involved
- Types of objects involved
- Your robot embodiment
- Reliability and robustness

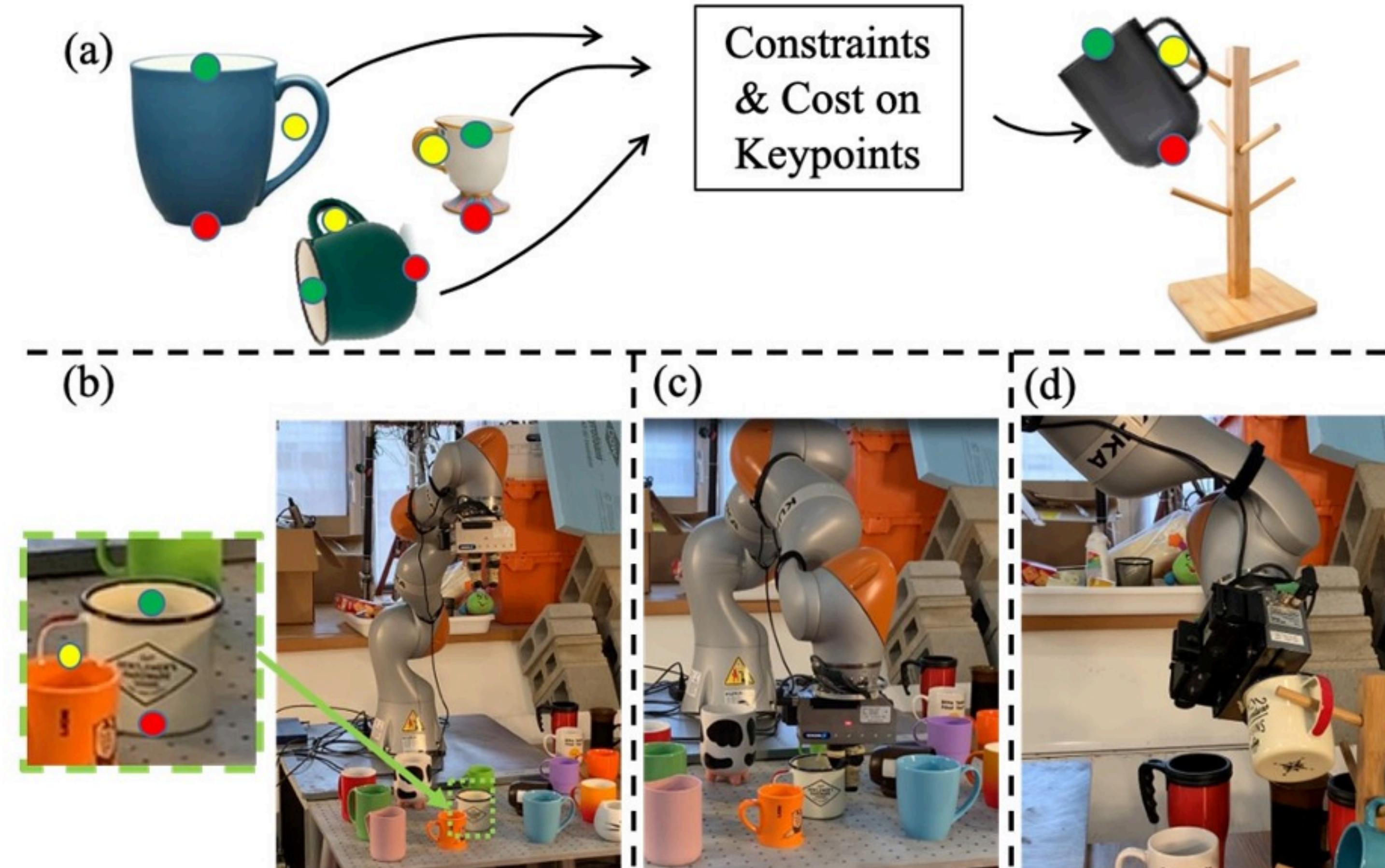


Robotic Tasks - Manipulation

- Task horizon
- Number of objects involved
- Types of objects involved
- Your robot embodiment
- Reliability and robustness



Robotic Tasks - Manipulation



Lucas Manuelli*, Wei Gao*, Peter Florence, Russ Tedrake

kPAM: KeyPoint Affordances for Category-Level Robotic Manipulation

1x speed



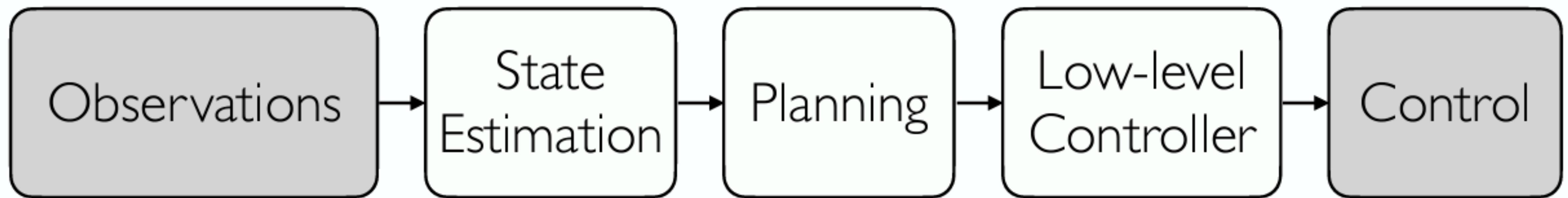


1x speed

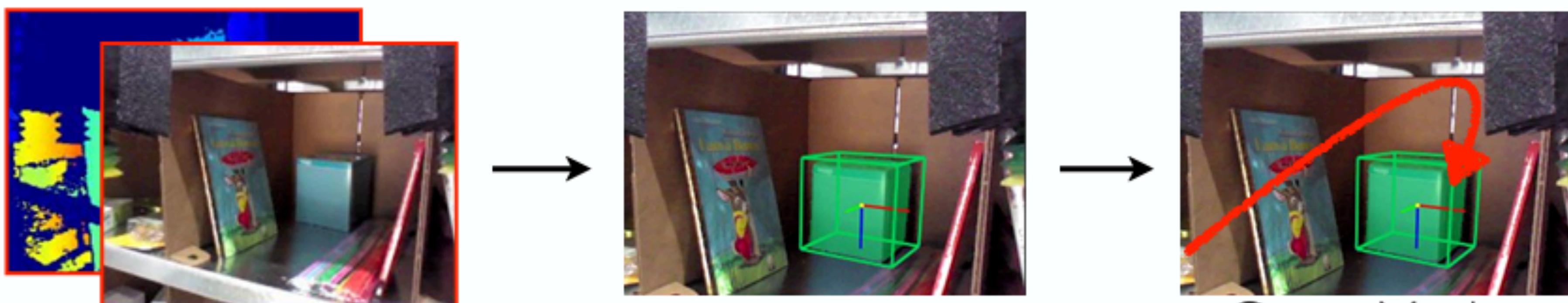




Typical Robotics Pipeline



Manipulation

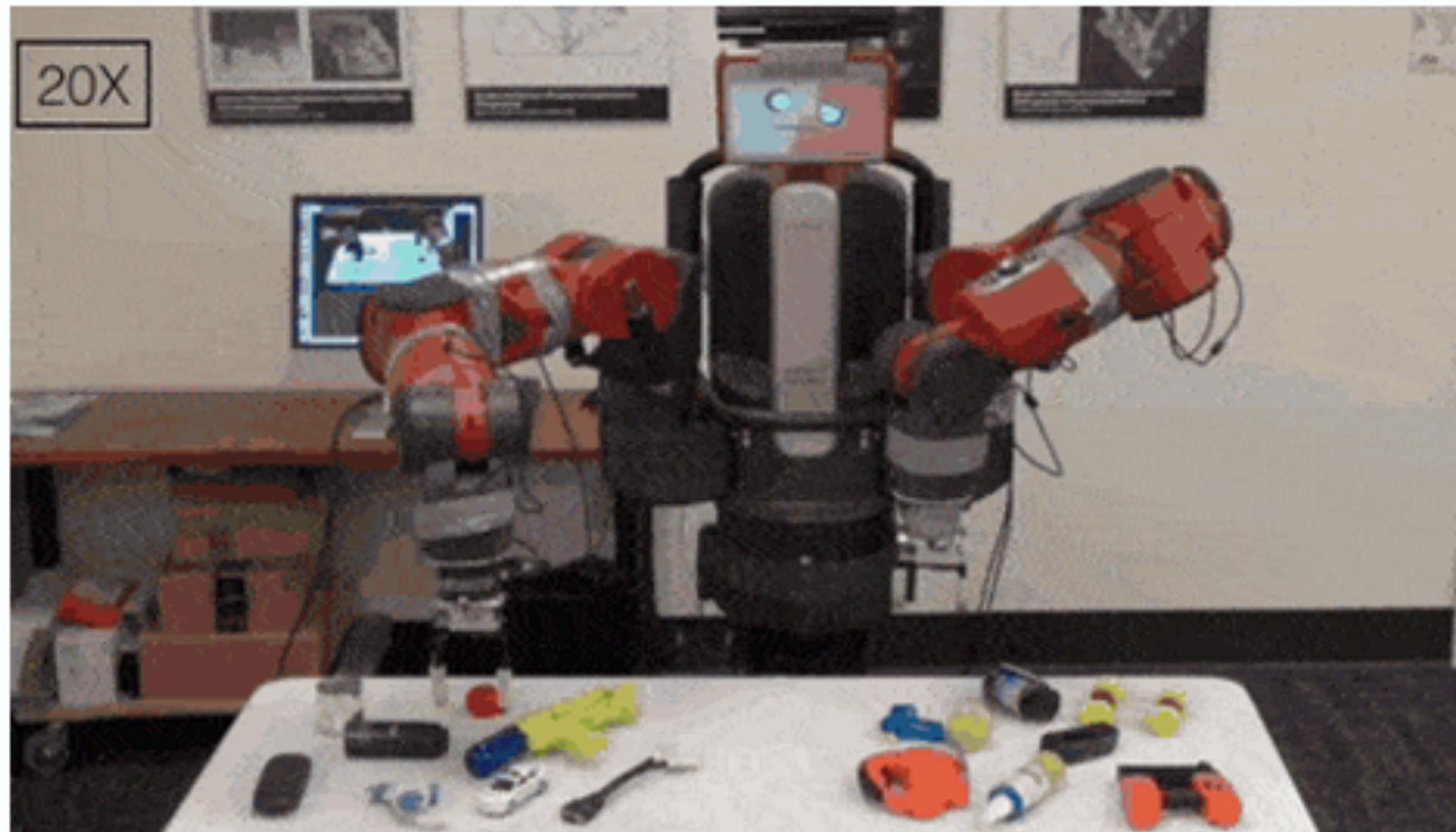


Observed Images

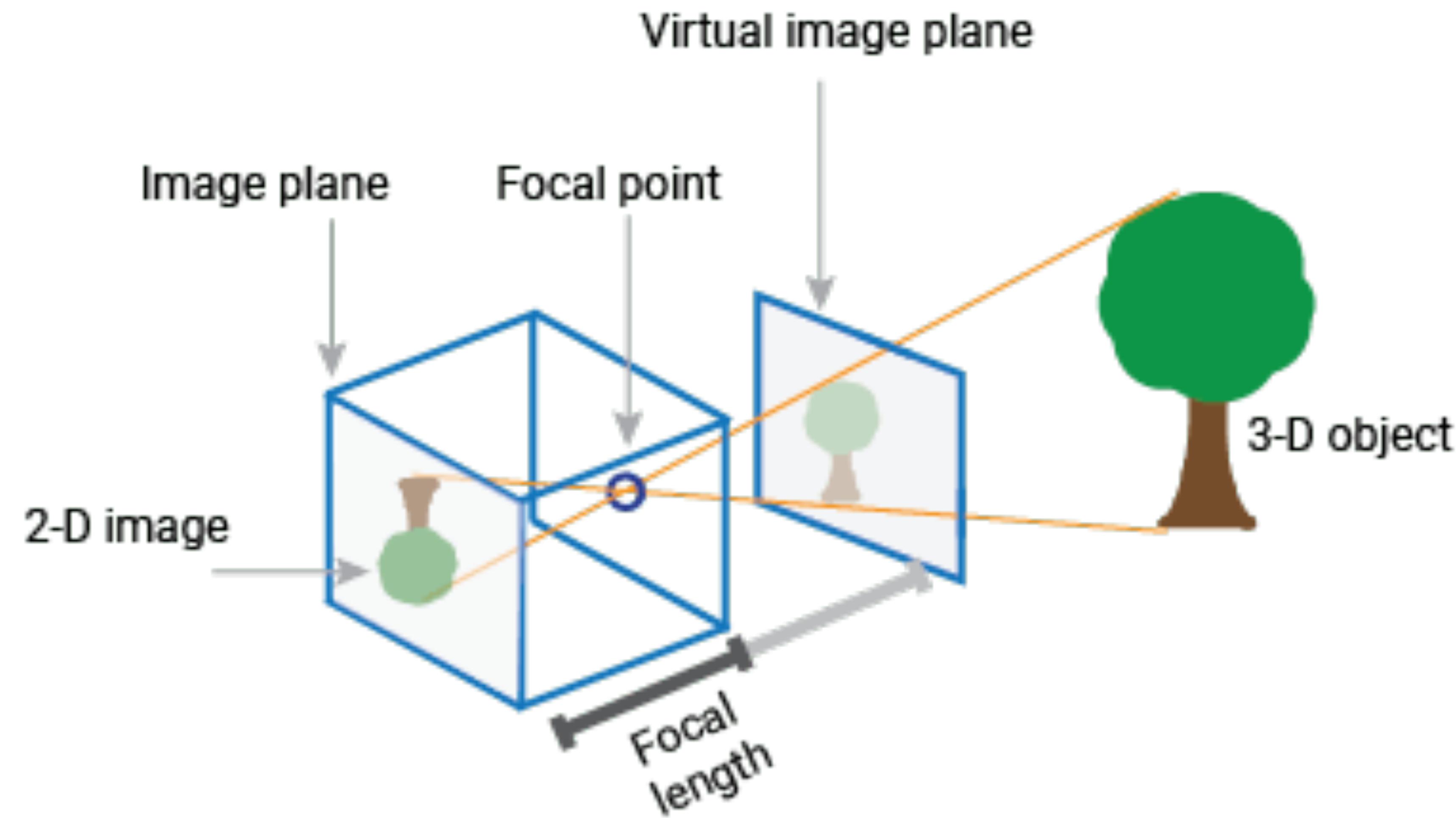
6DOF Pose

Grasp Motion
Planning

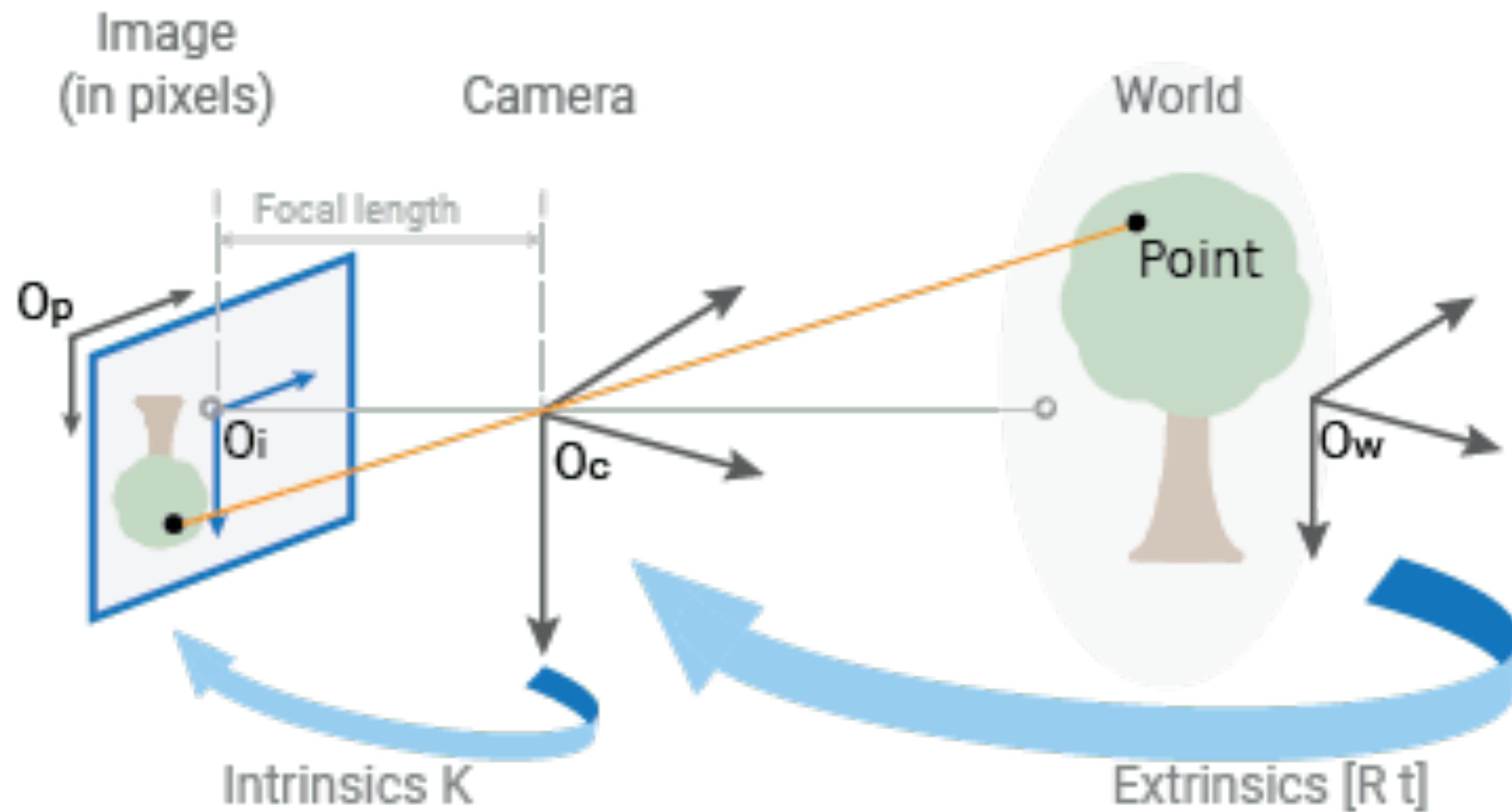
Camera Calibration



Camera Calibration



Camera Calibration



Camera Calibration



File **Panels** **Help****Interact** **Move Camera** **Select** **Focus Camera** **Measure** **2D Pose Estimate** **2D Nav Goal** **Publish Point**

Displays

- Global Options
 - Fixed Frame: world
 - Background Color: ■ 48; 48; 48
 - Frame Rate: 30
 - Default Light:
- Global Status: Ok
 - Fixed Frame: OK
- Grid
- DepthCloud
- DepthCloud
- DepthCloud
- DepthCloud DepthCloud
- TF



DepthCloud
Displays point clouds based on depth maps.
[More Information](#).

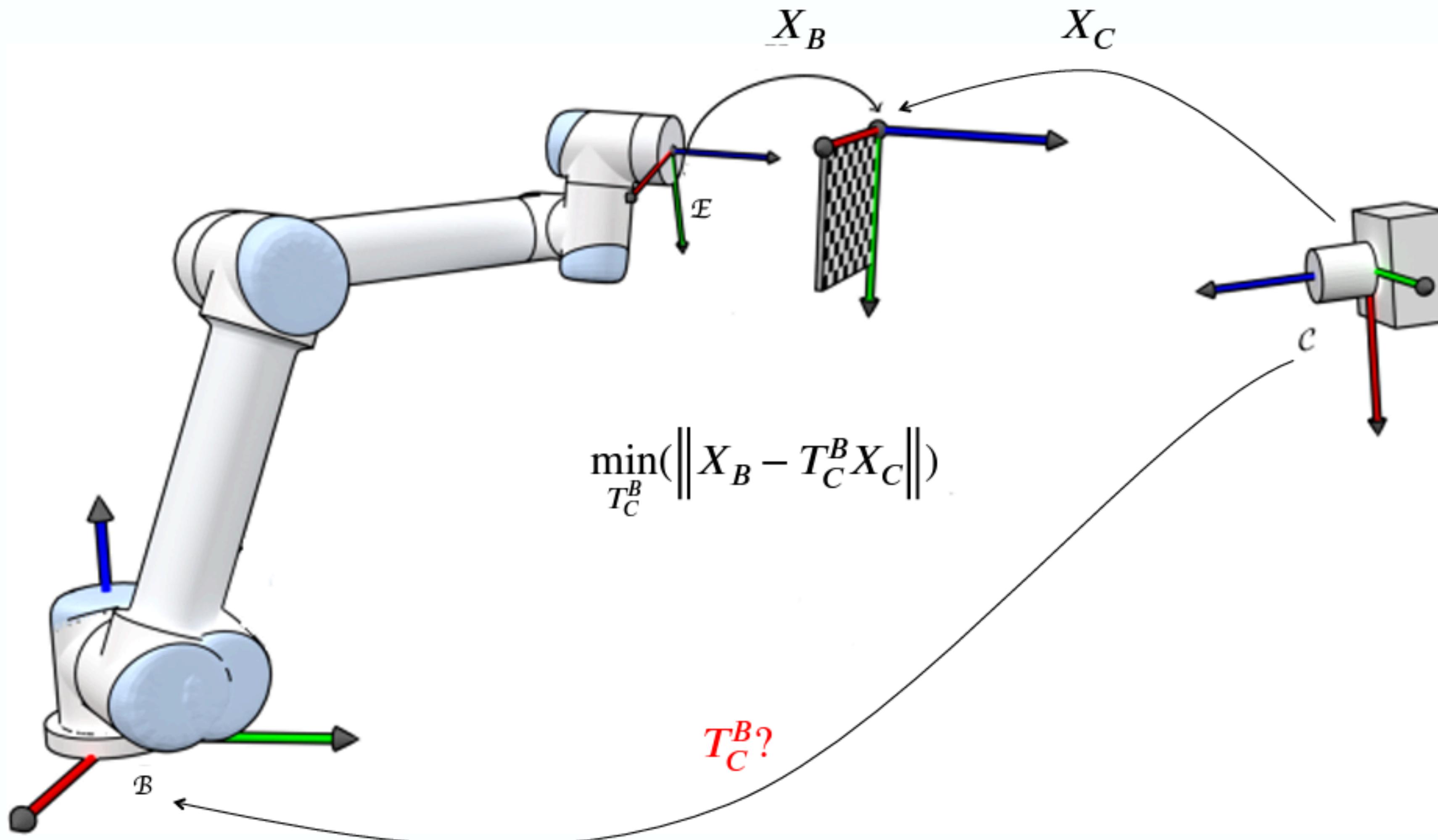
Add **Duplicate** **Remove** **Rename****Time**

ROS Time: 1625114777.37 ROS Elapsed: 3933.36 Wall Time: 1625114777.40 Wall Elapsed: 3933.36

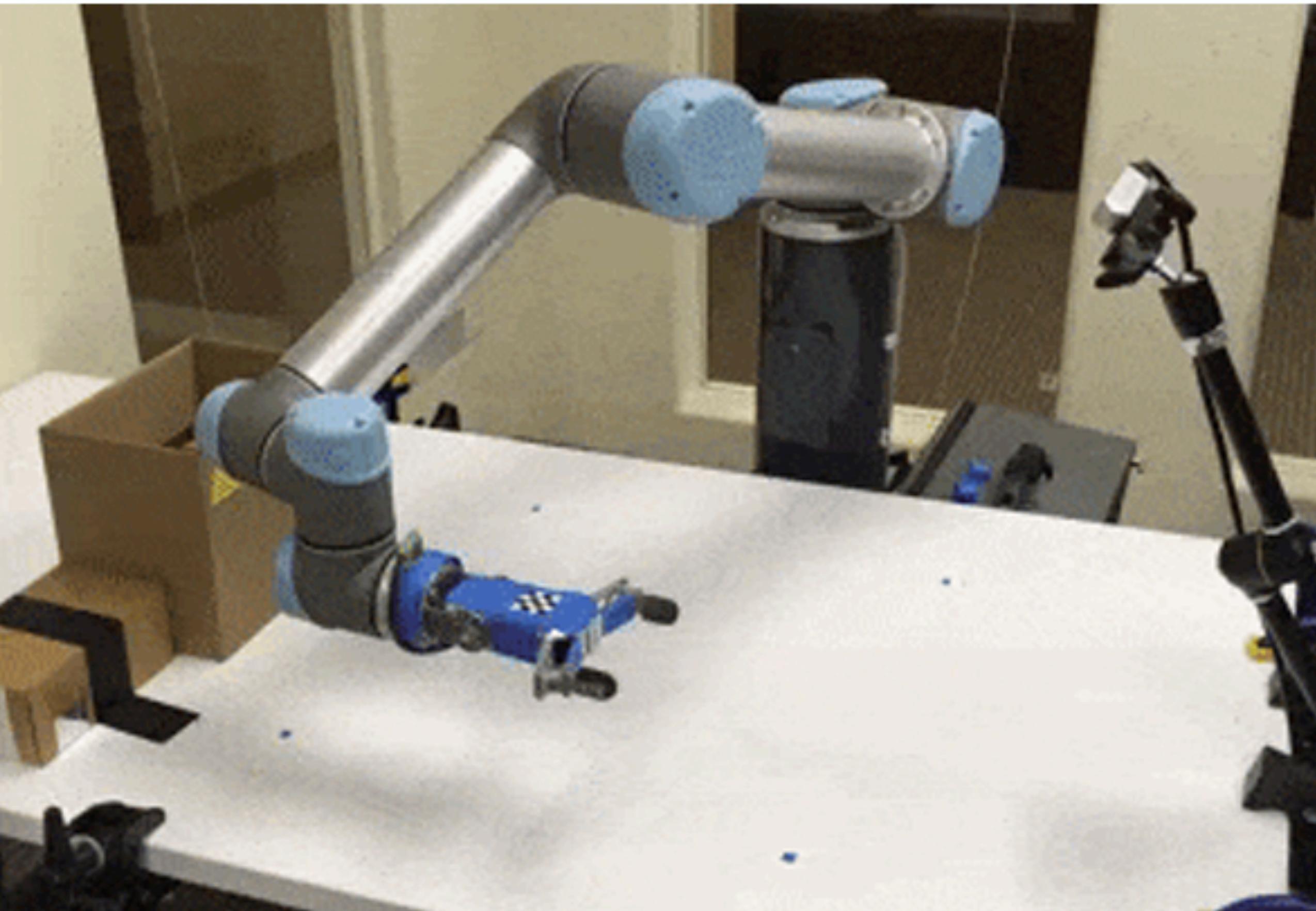
 Experimental**Reset**

31 fps

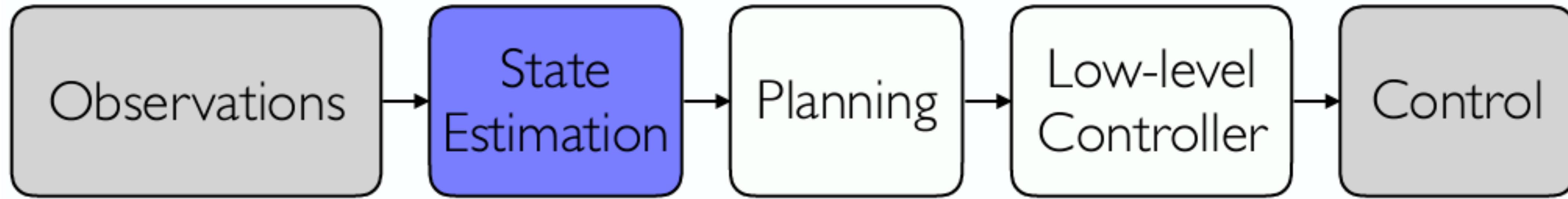
Camera Calibration



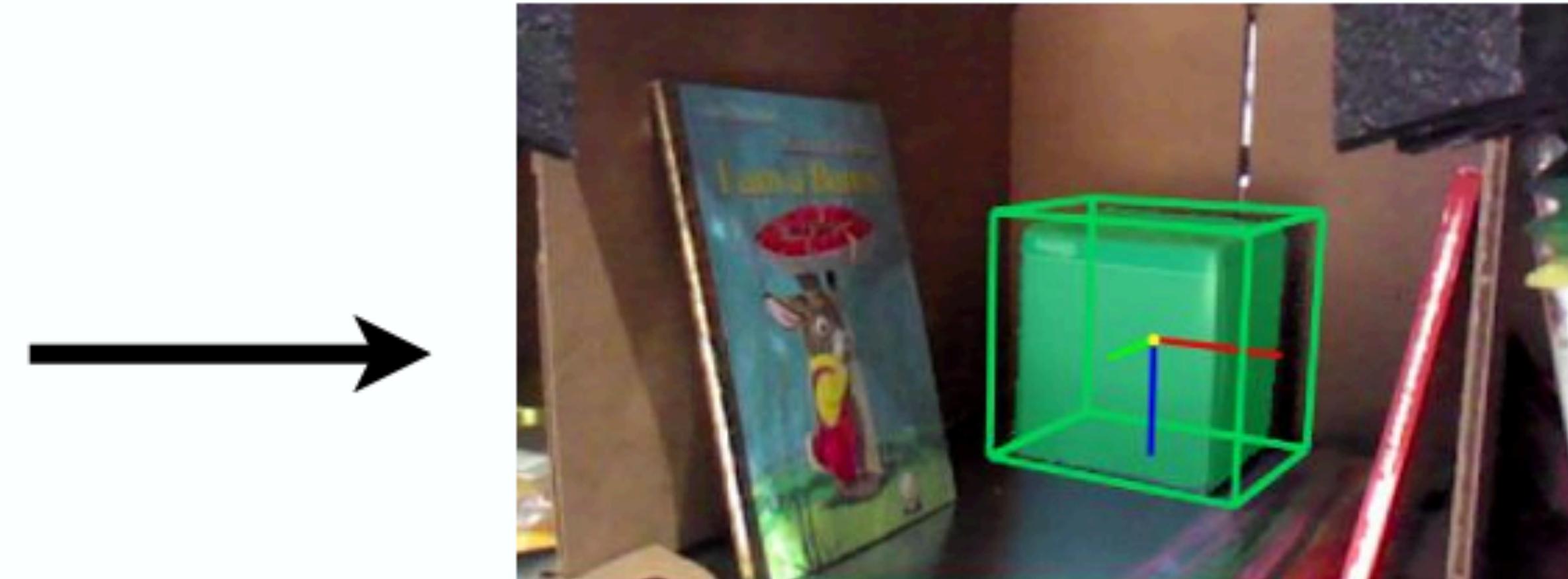
Camera Calibration



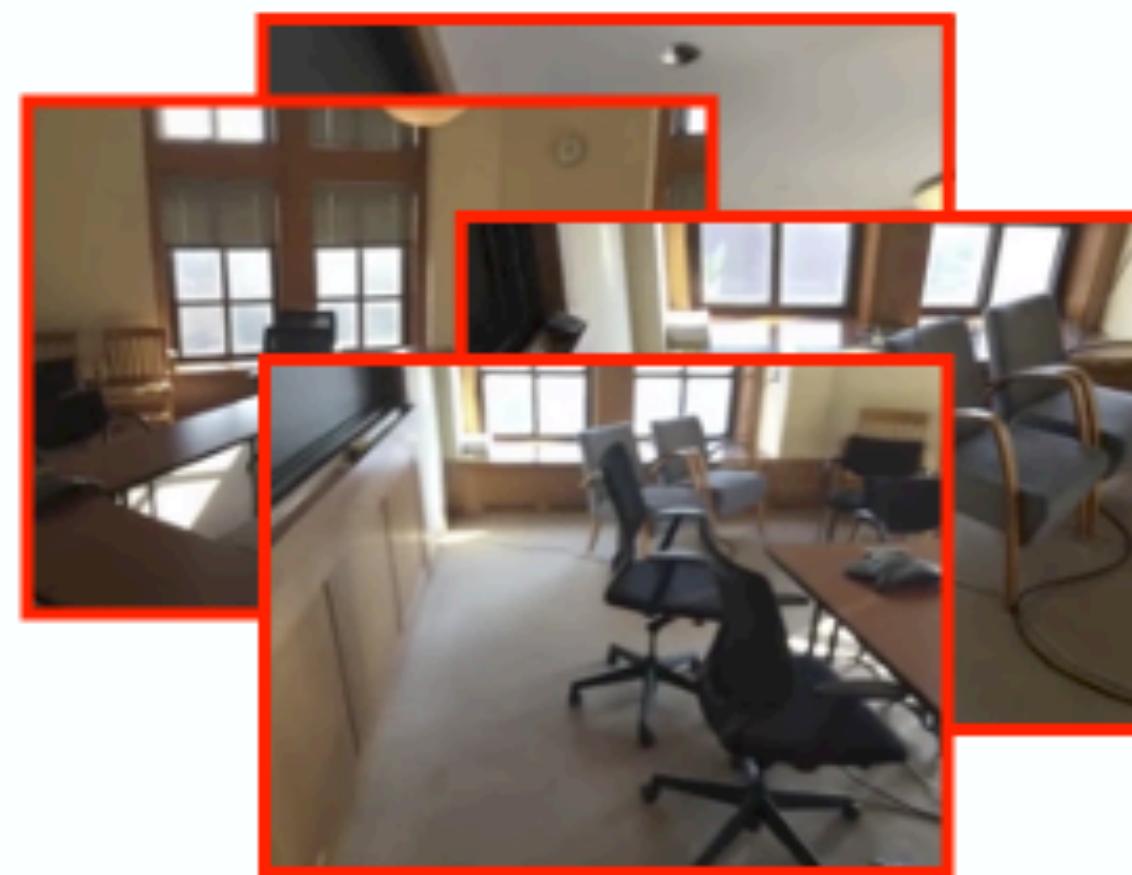
$$\min_{T_C^B} \sum_{i=1}^n \|X_B^i - T_C^B X_C^i\|$$



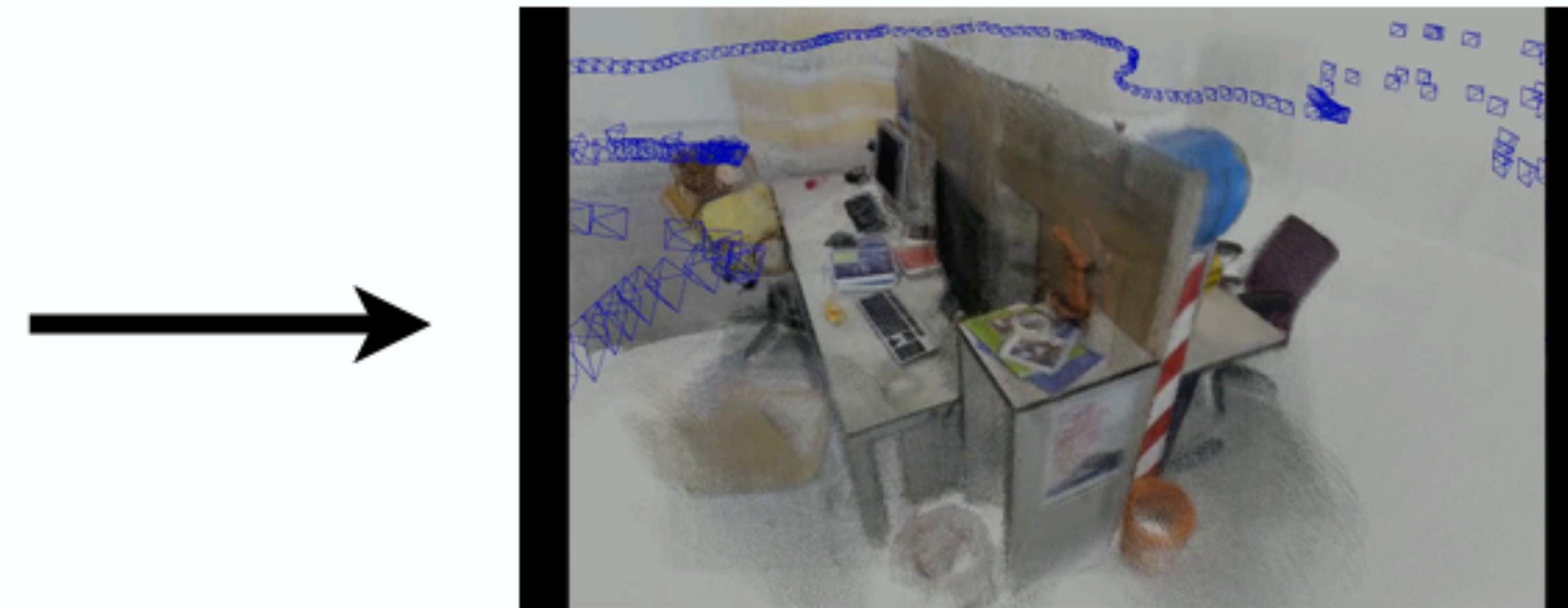
Observed Images



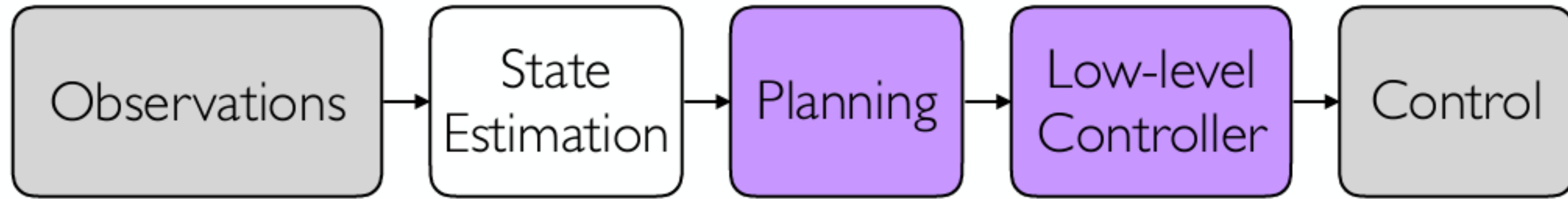
6DOF Pose



Observed Images



Geometric or Semantic Maps

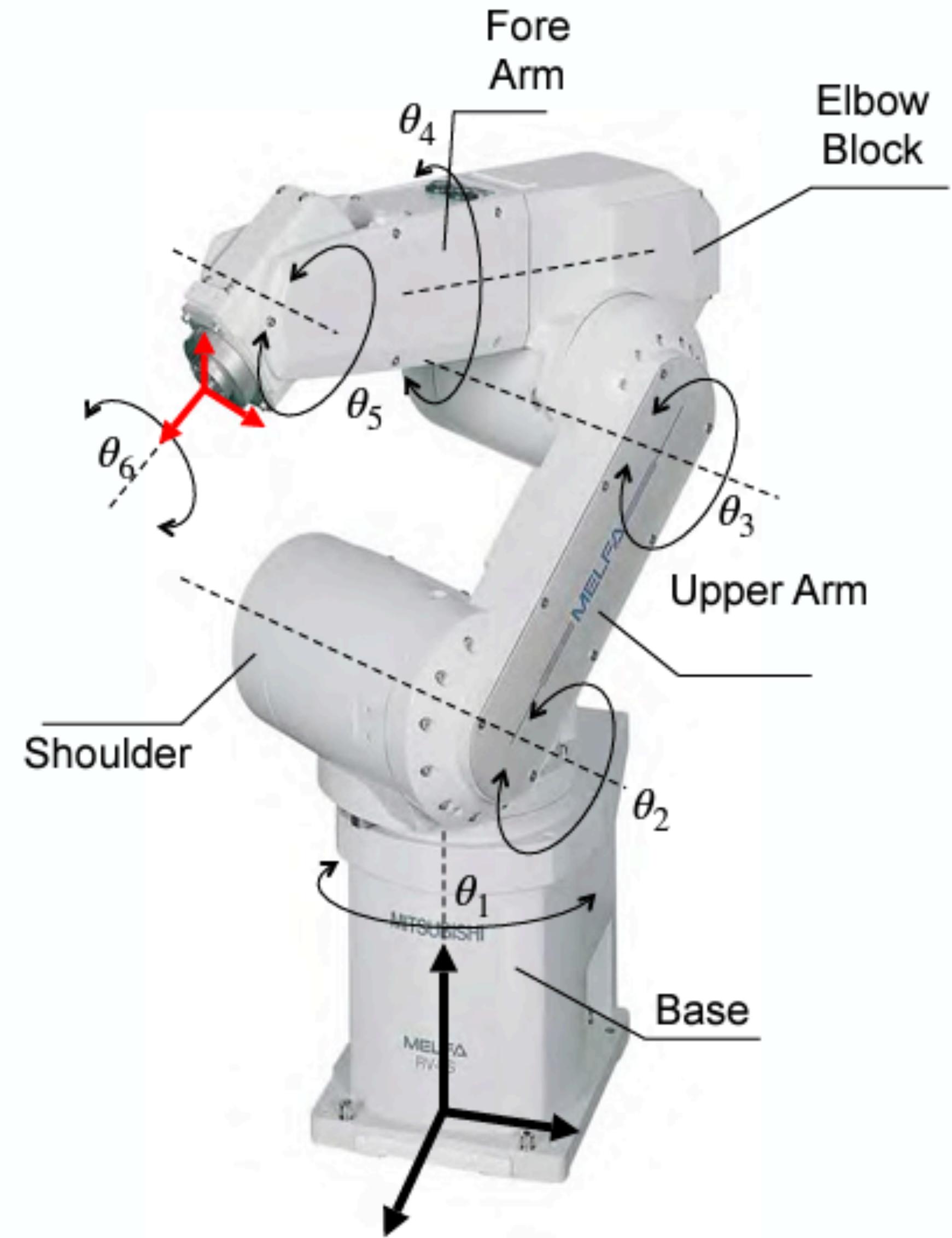


How to move a robot?



Terminology

- Link
- Joint
- End Effector
- Base
- Sensors

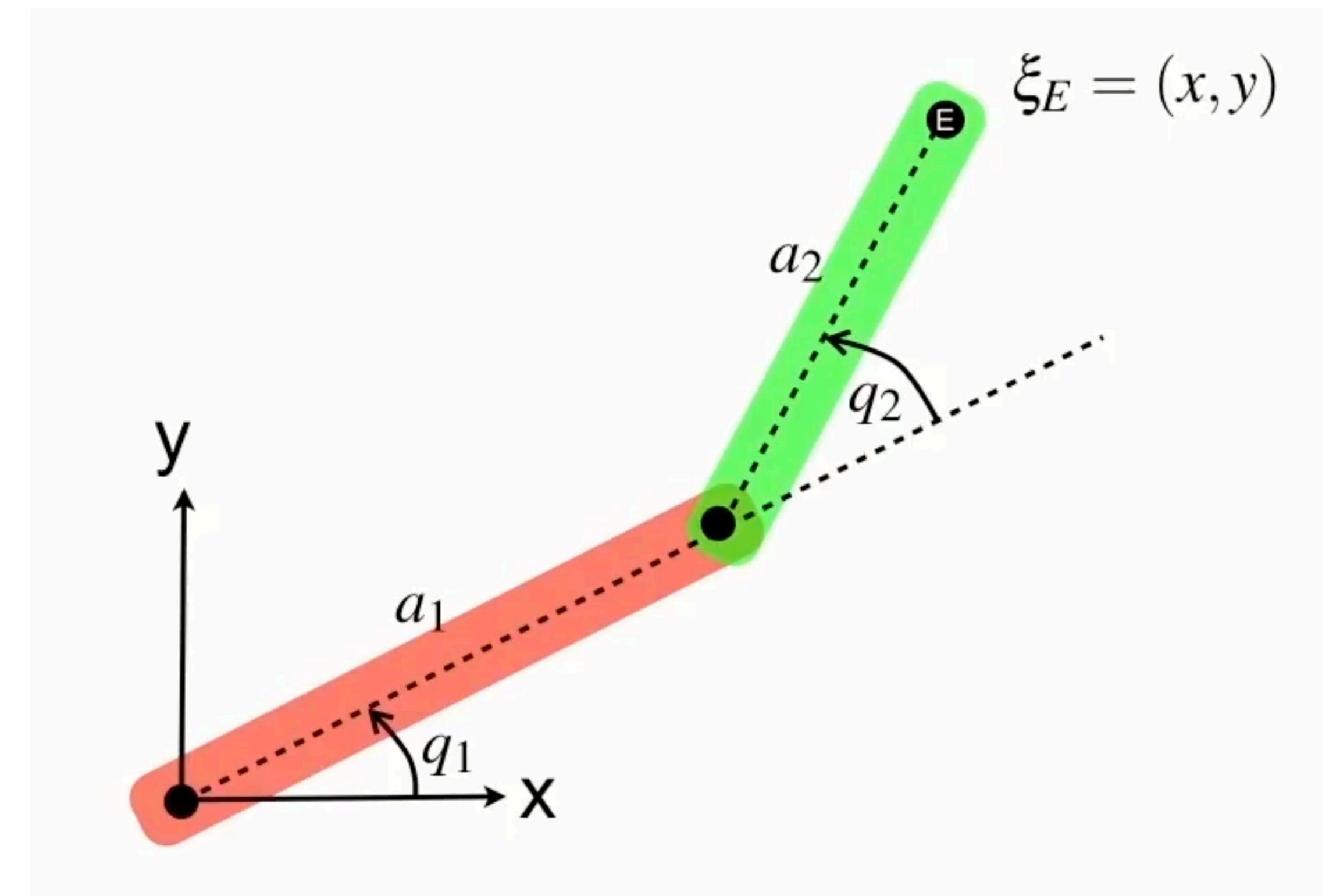


Spaces

- Work Space (or Task Space)
 - This refers to the physical space in which the robot operates. For a robotic arm, the work space might be the volume of space the end-effector (like a gripper or tool) can reach.
- Configuration Space (C-Space)
 - This is a representation of all possible configurations (or positions) of the robot. For robots with multiple joints, the C-space can have multiple dimensions, one for each degree of freedom.

Spaces

- Link
- Joint
- End Effector
- Base
- Work Space
- Configuration Space

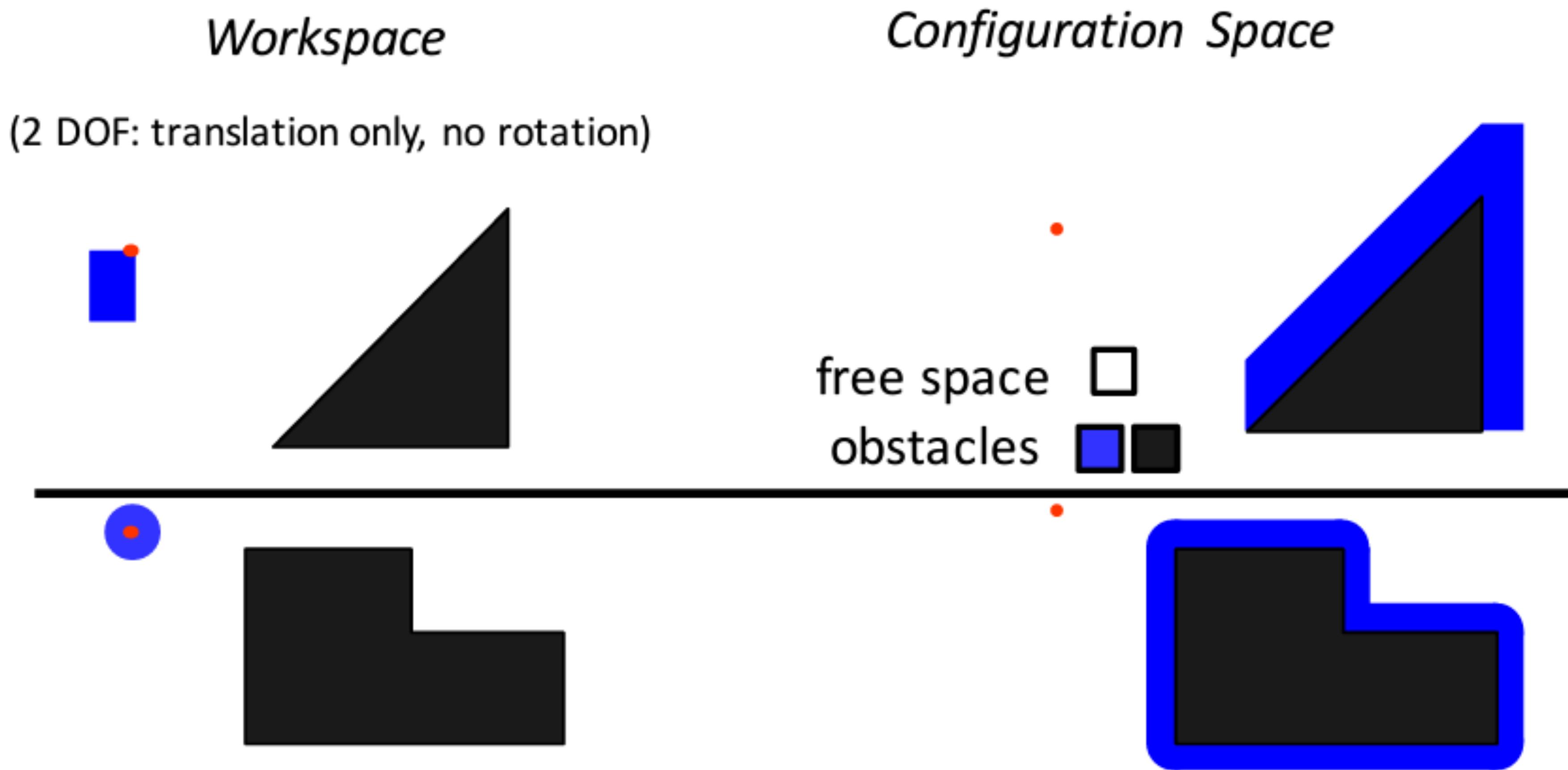


Spaces

- Link
- Joint
- End Effector
- Base
- Work Space
- Configuration Space

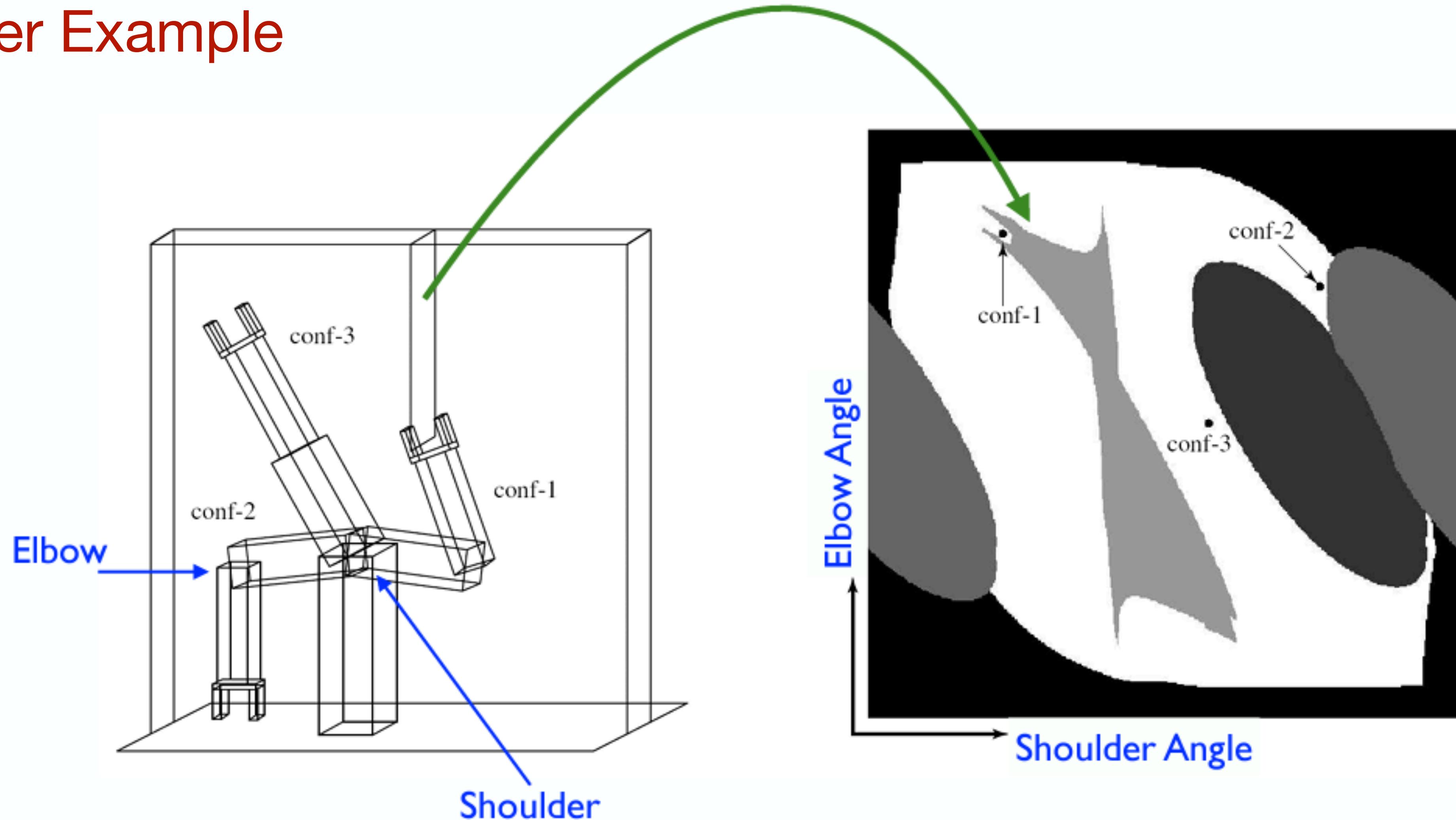


Work space obstacles → Configuration space obstacles



Configuration Space

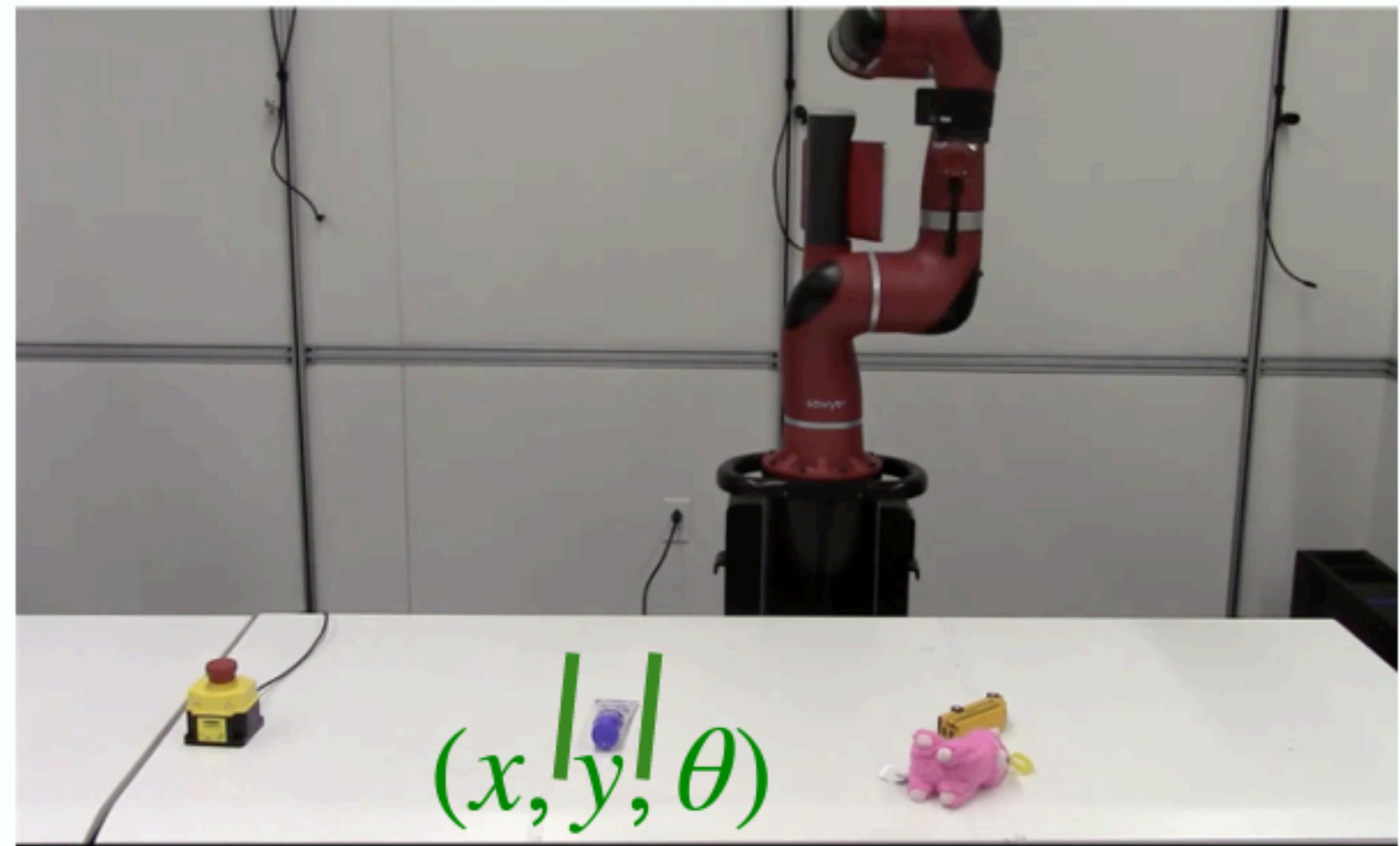
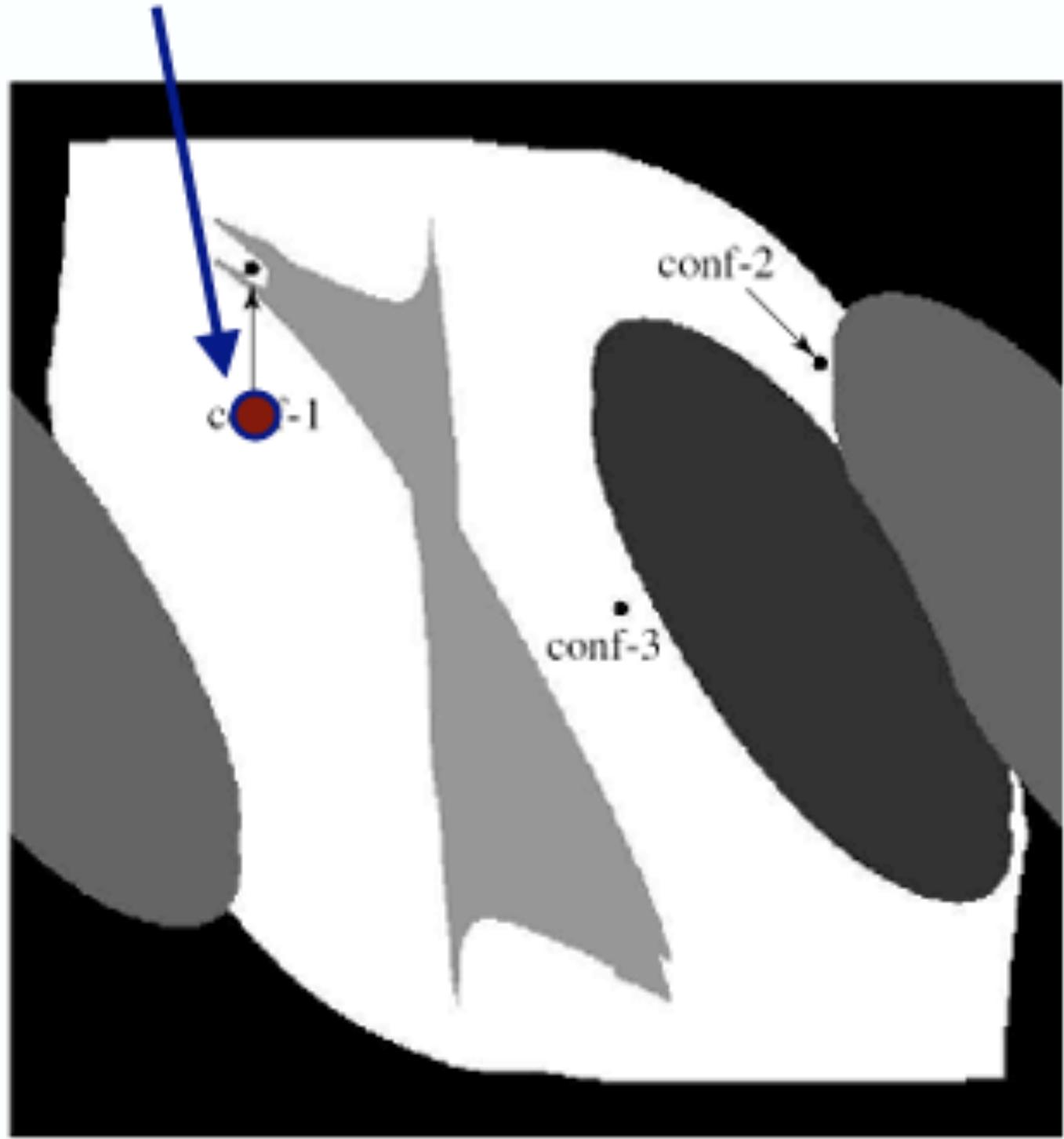
Another Example



How to move your robot?

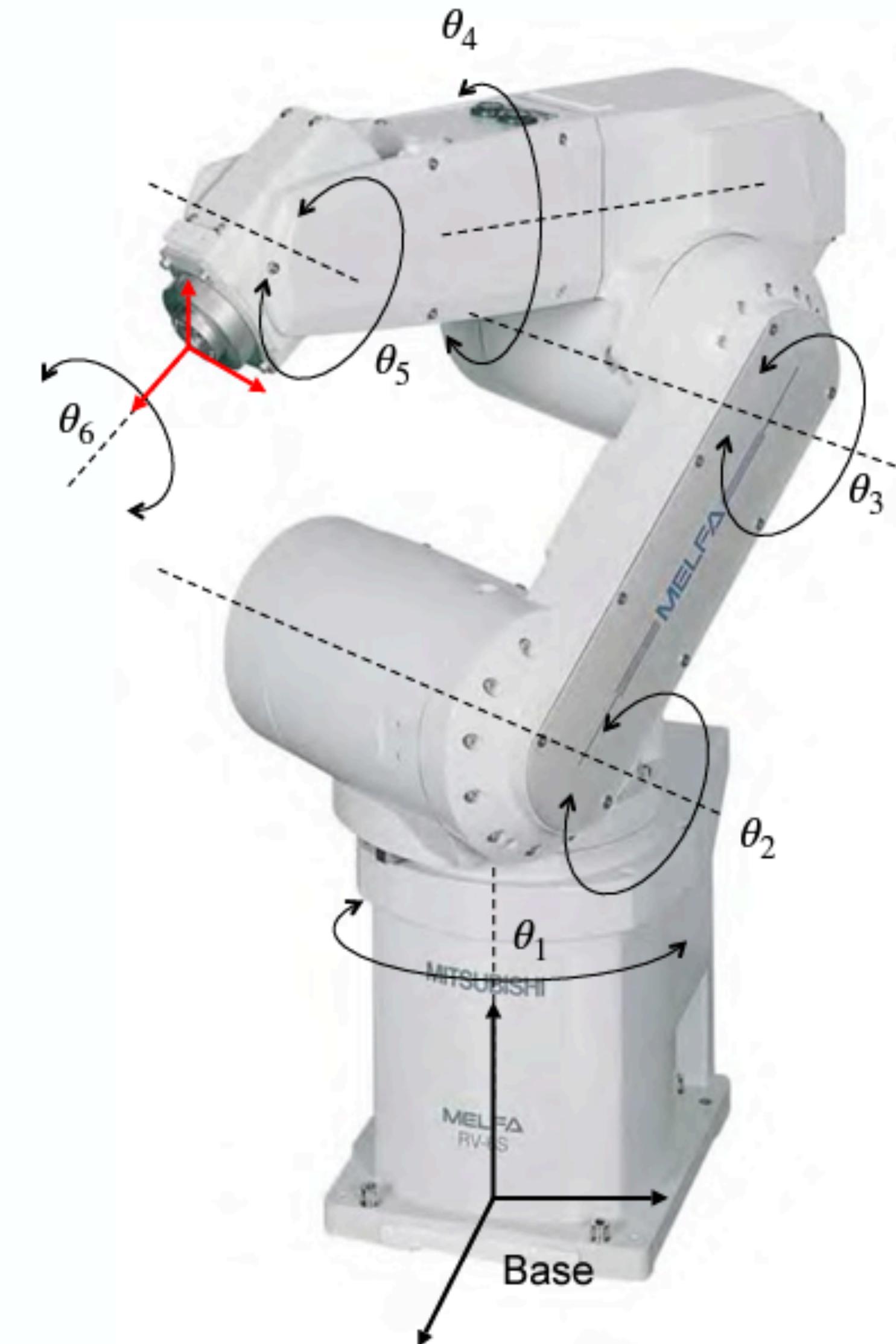
Task space to Configuration space

Initial
configuration



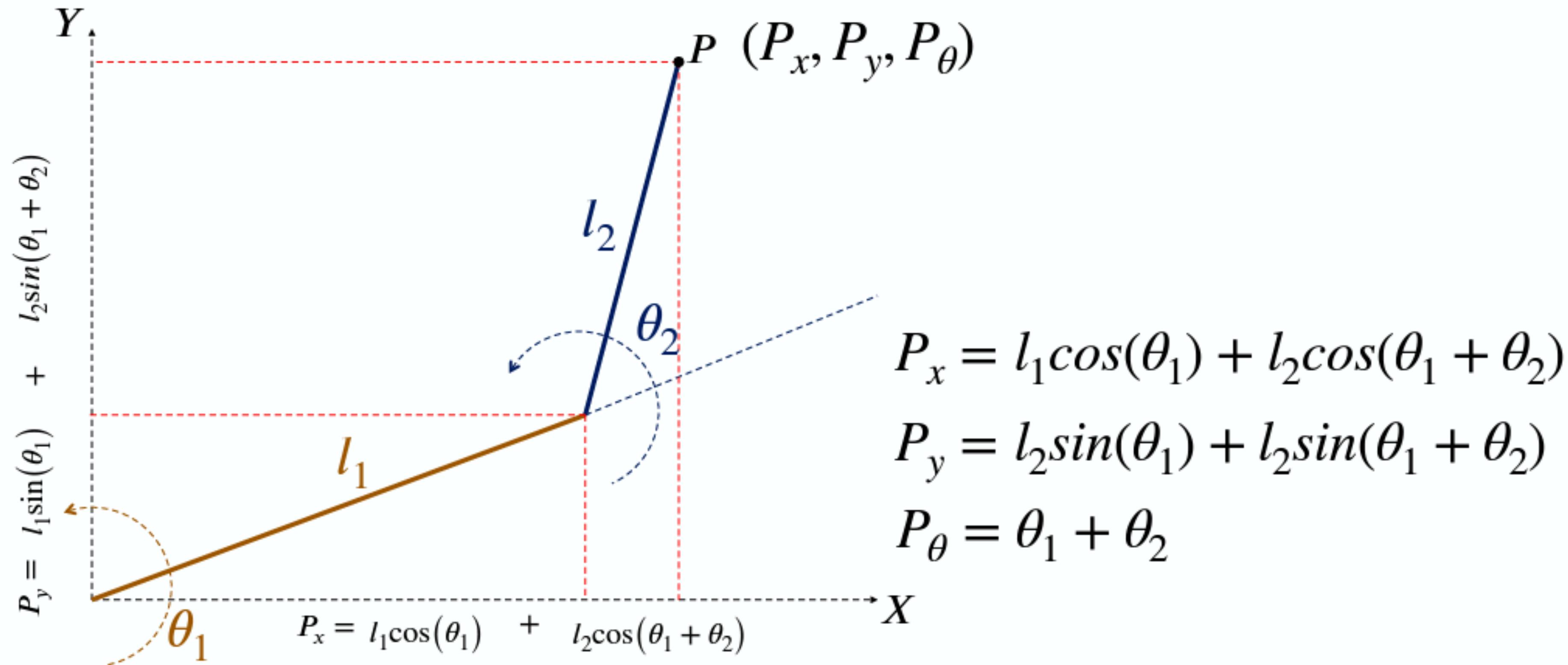
Configuration Space to Task Space

Forward Kinematics



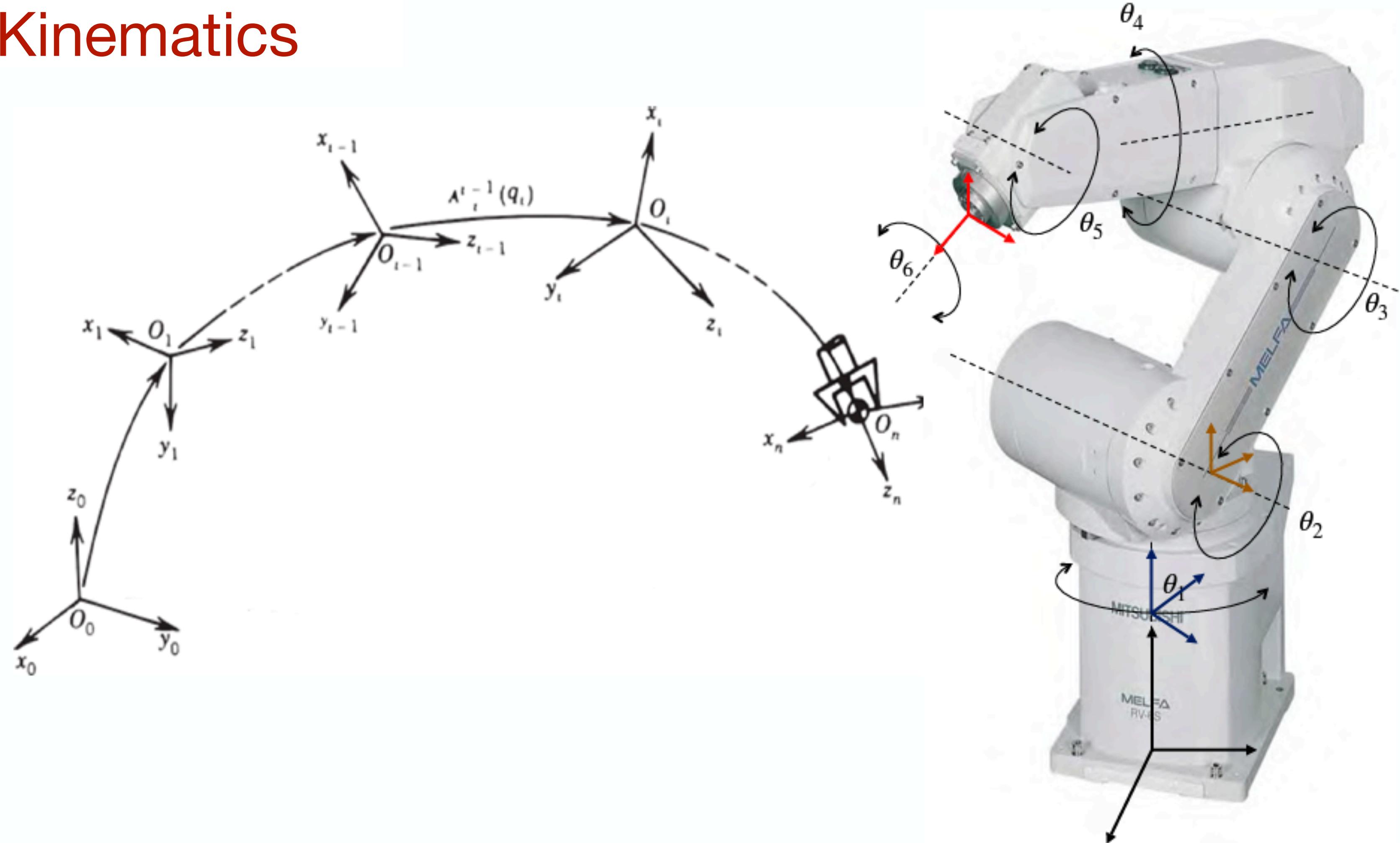
Configuration Space to Task Space

Forward Kinematics



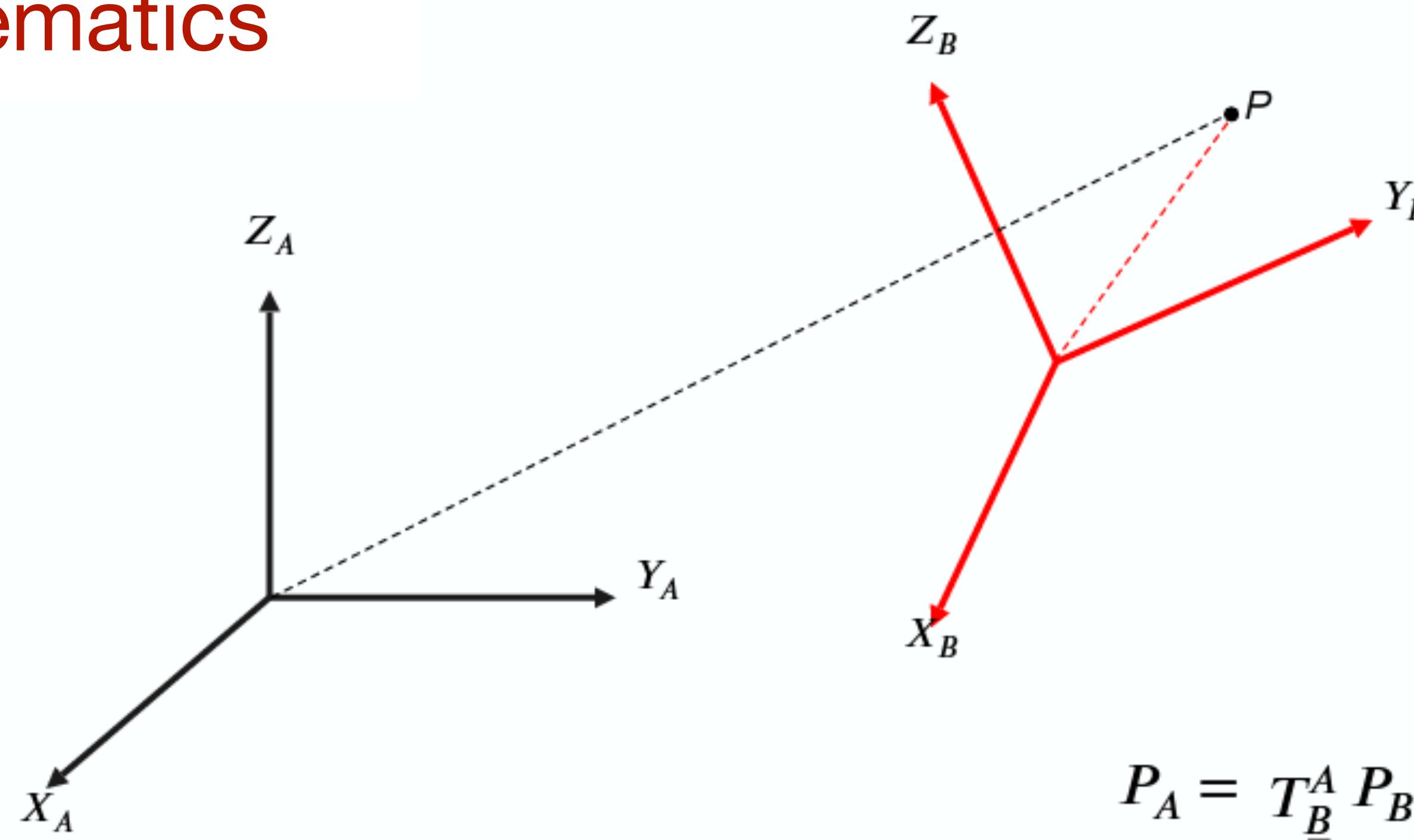
Configuration Space to Task Space

Forward Kinematics



Configuration Space to Task Space

Forward Kinematics

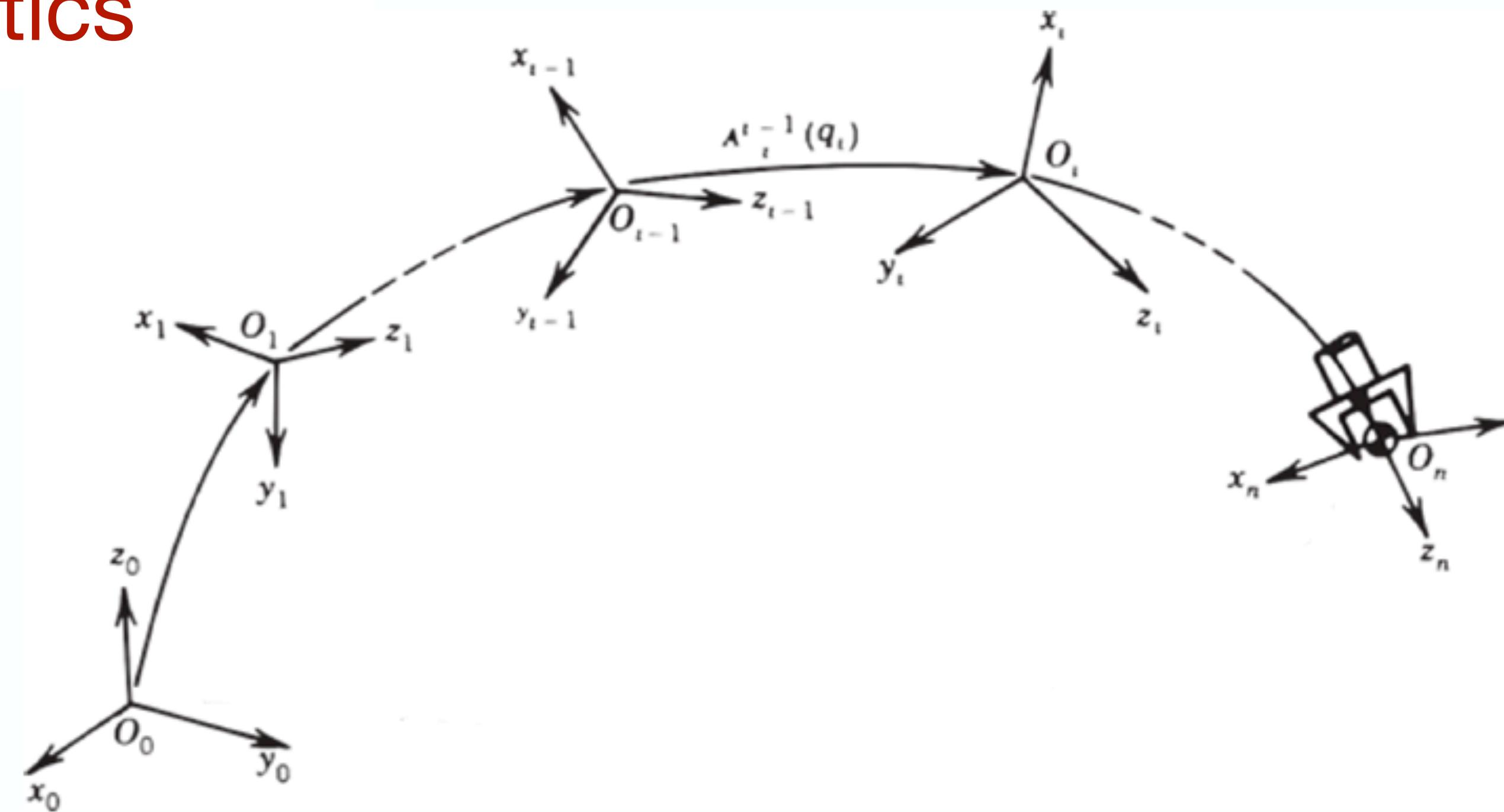


$$P_A = T_B^A P_B$$

$$T_B^A = \begin{bmatrix} r_{11} & r_{21} & r_{31} & \Delta x \\ r_{12} & r_{22} & r_{32} & \Delta y \\ r_{13} & r_{23} & r_{33} & \Delta z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

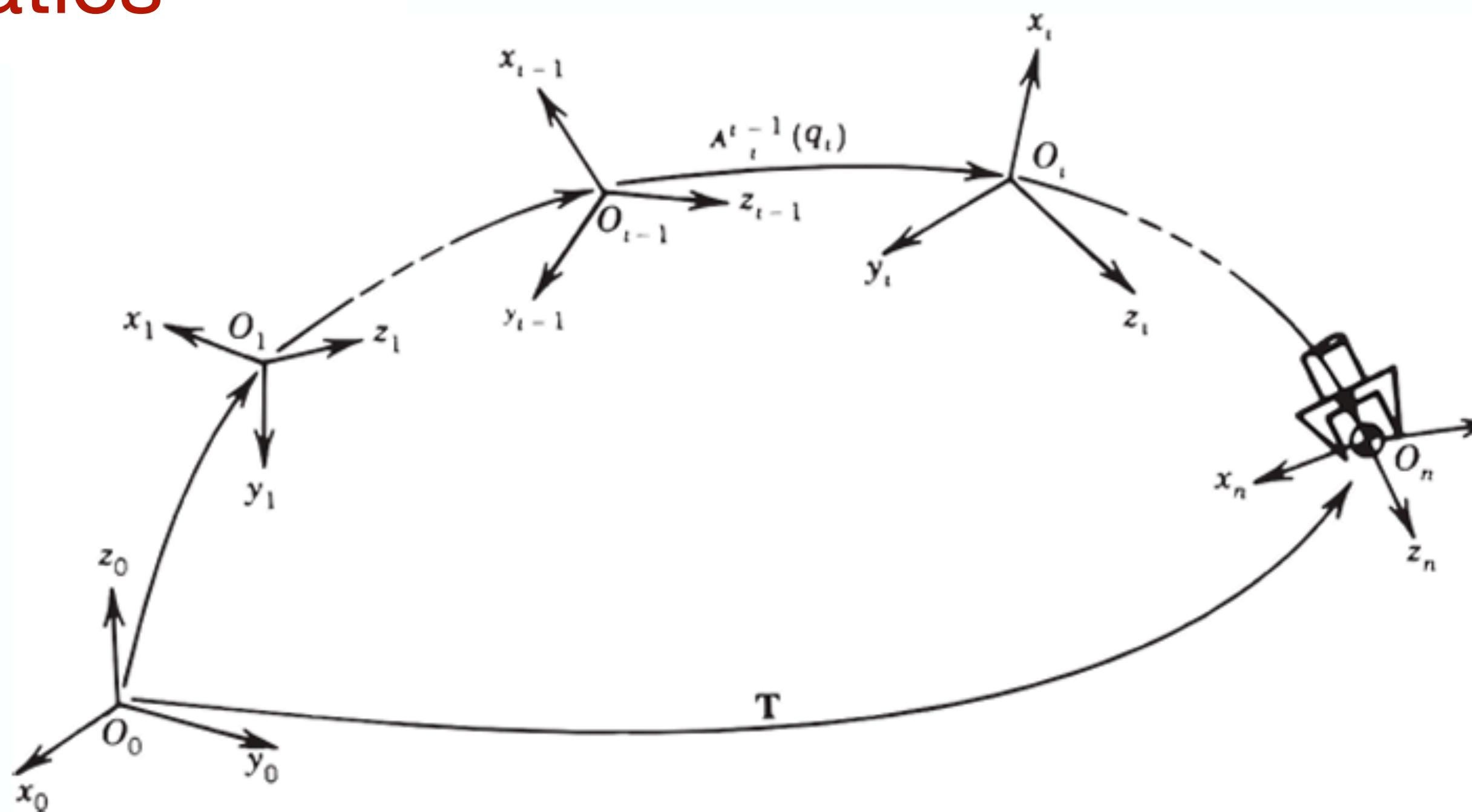
Configuration Space to Task Space

Forward Kinematics



Configuration Space to Task Space

Forward Kinematics



Maps configuration
space to work space

$$T = T_1^0(\theta_1) T_2^1(\theta_2) \dots T_{n-1}^{n-2}(\theta_{n-1}) T_n^{n-1}(\theta_n)$$

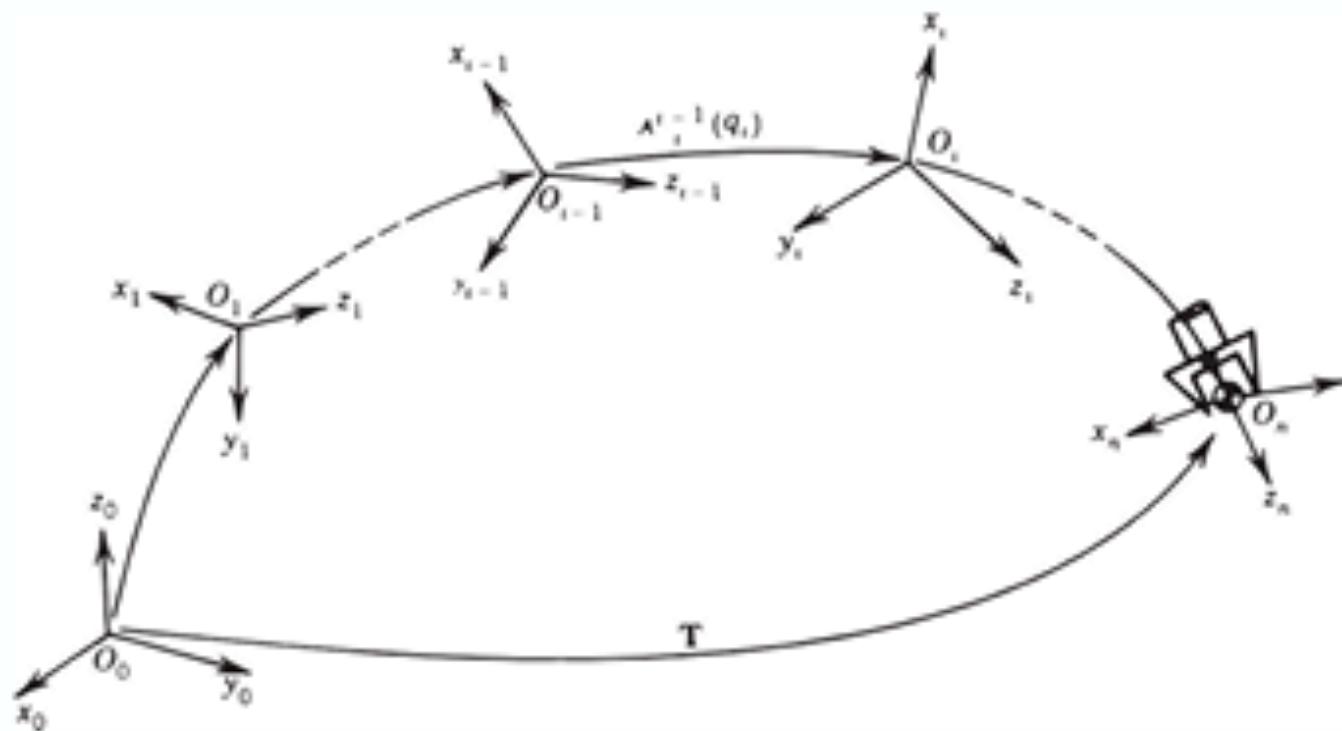
$$= \begin{bmatrix} r_{11} & r_{21} & r_{31} \\ r_{12} & r_{22} & r_{32} \\ r_{13} & r_{23} & r_{33} \end{bmatrix} \begin{bmatrix} \Delta x \\ \Delta y \\ \Delta z \end{bmatrix}$$

$$x = f(\theta) = f(\theta_1, \theta_2, \dots, \theta_{n-1}, \theta_n)$$

Configuration Space to Task Space

Inverse Kinematics

Numerical IK



$$x = f(\theta)$$

Solve for θ_d in:

$$x_d - f(\theta_d) = 0$$

Analytical IK

- Robot Specific
- Fast
- Characterize the solution space

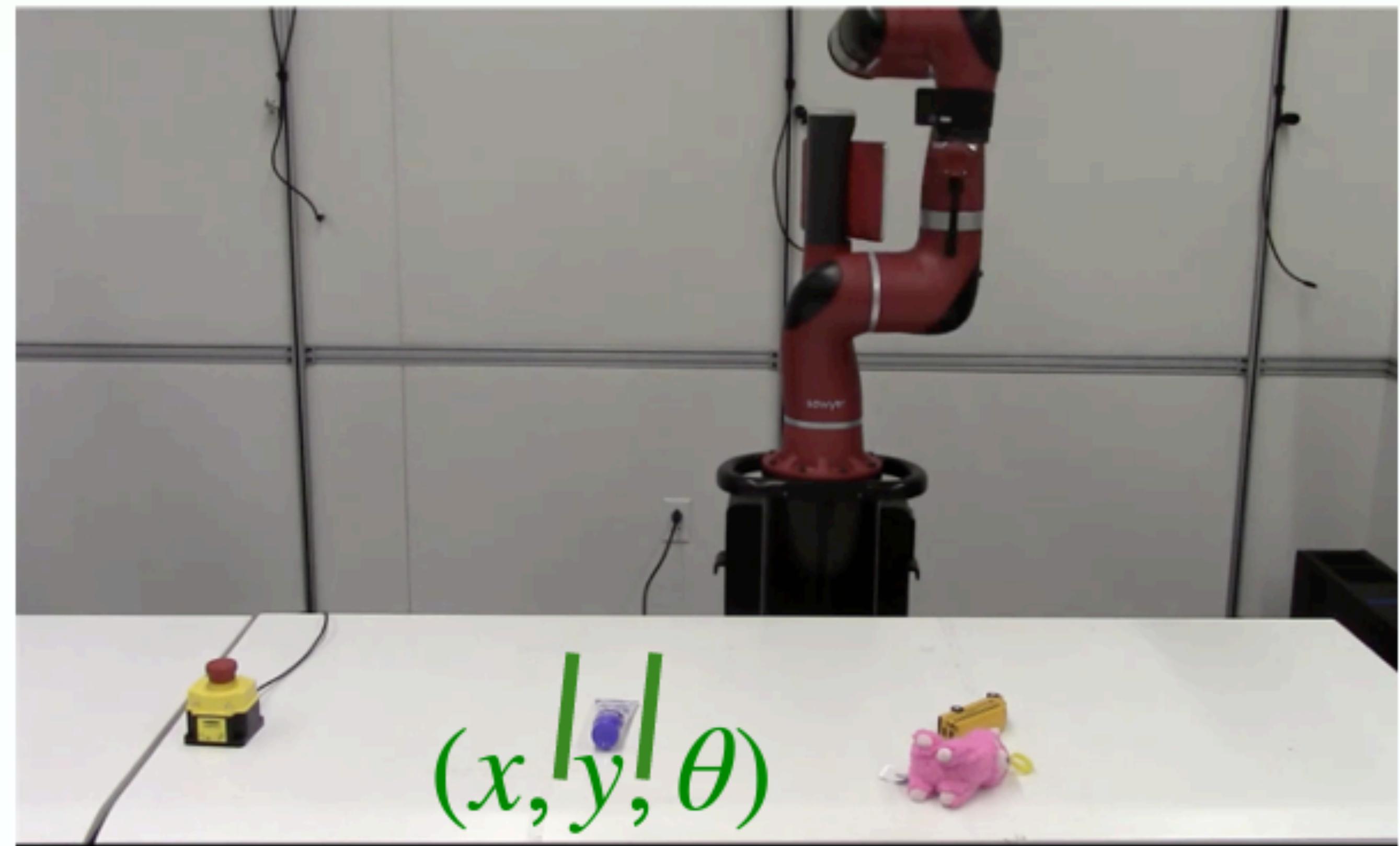
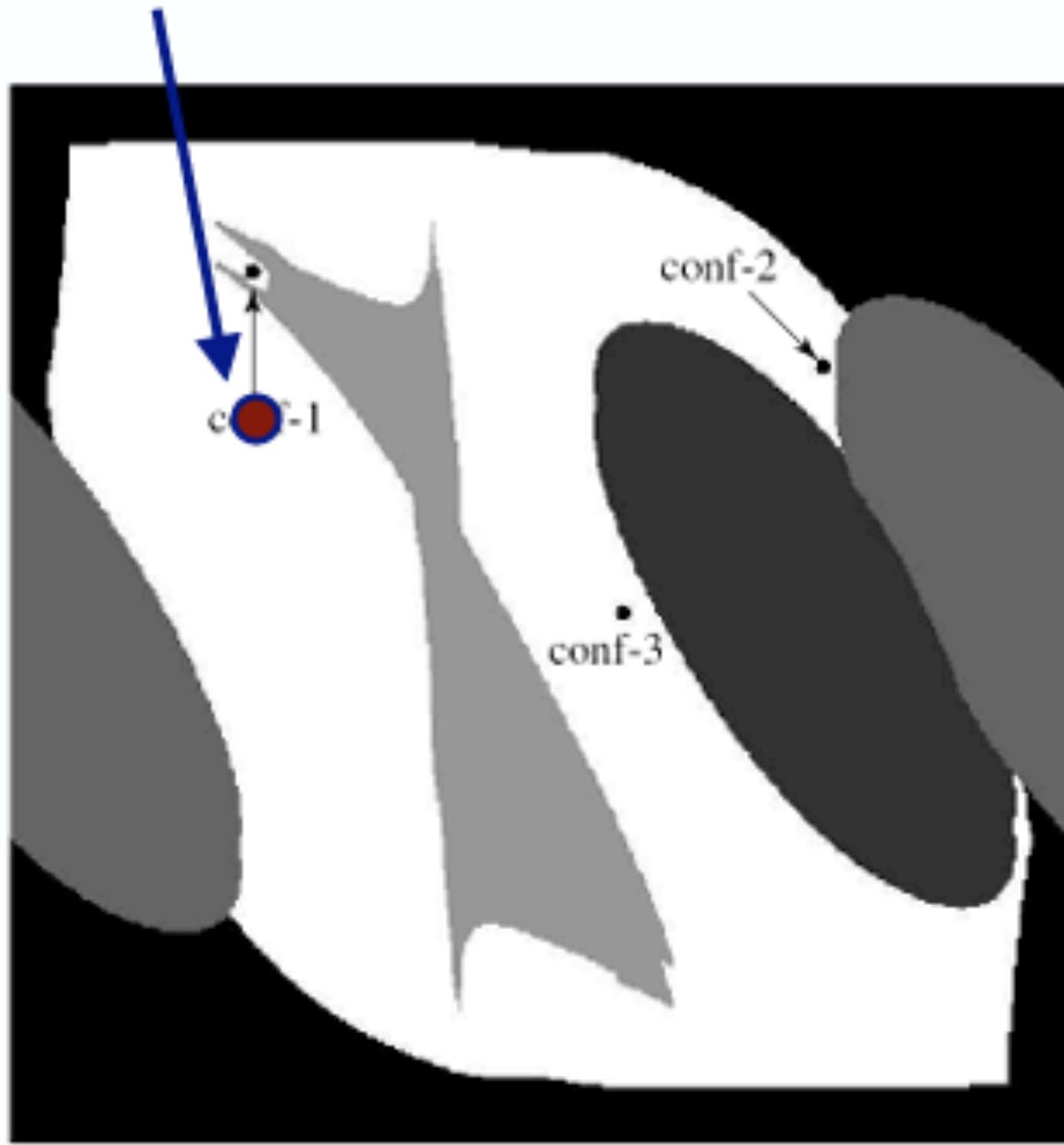
Maps configuration
space to work space

Find configuration(s) that map
to a given work space point

How to move your robot?

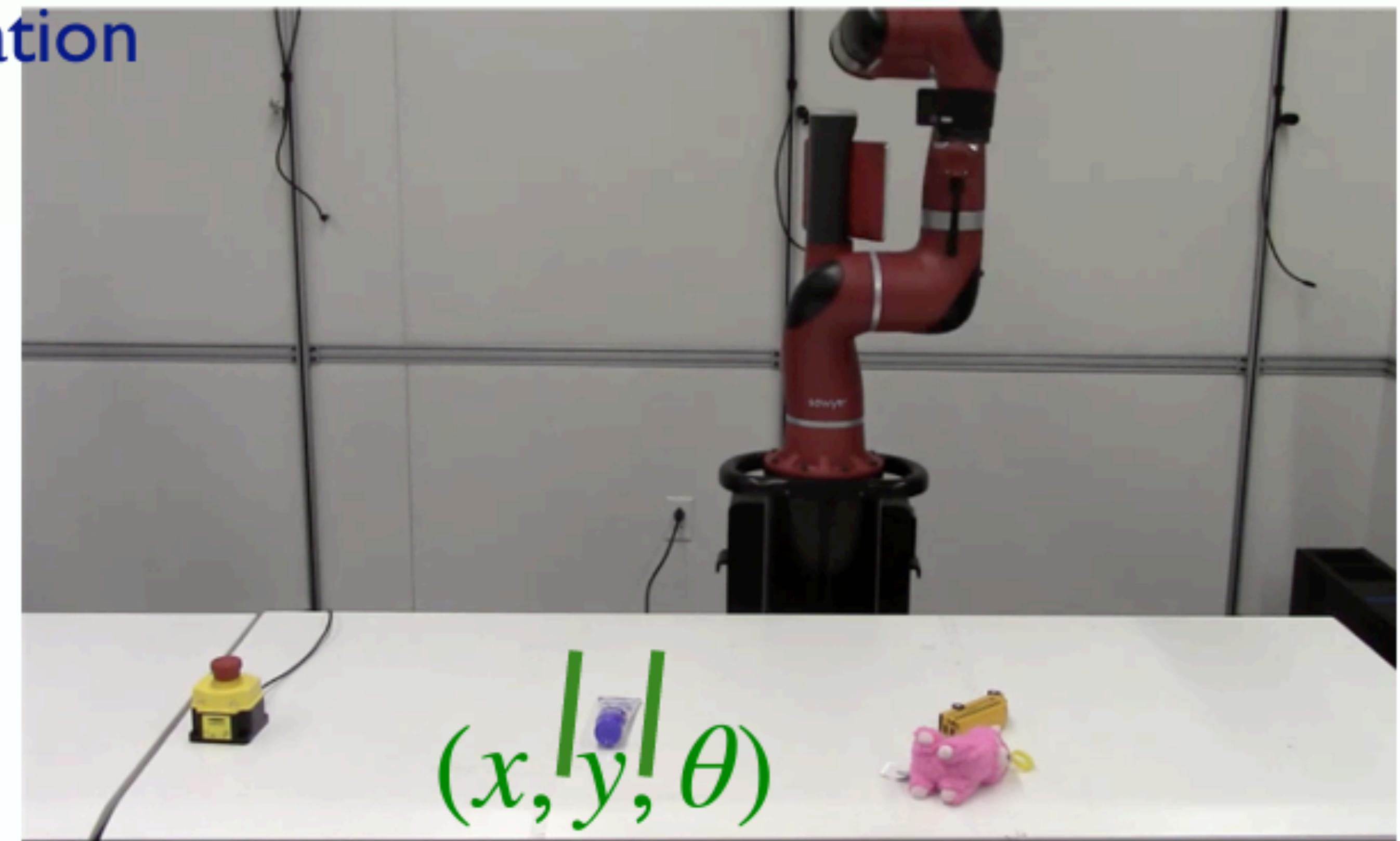
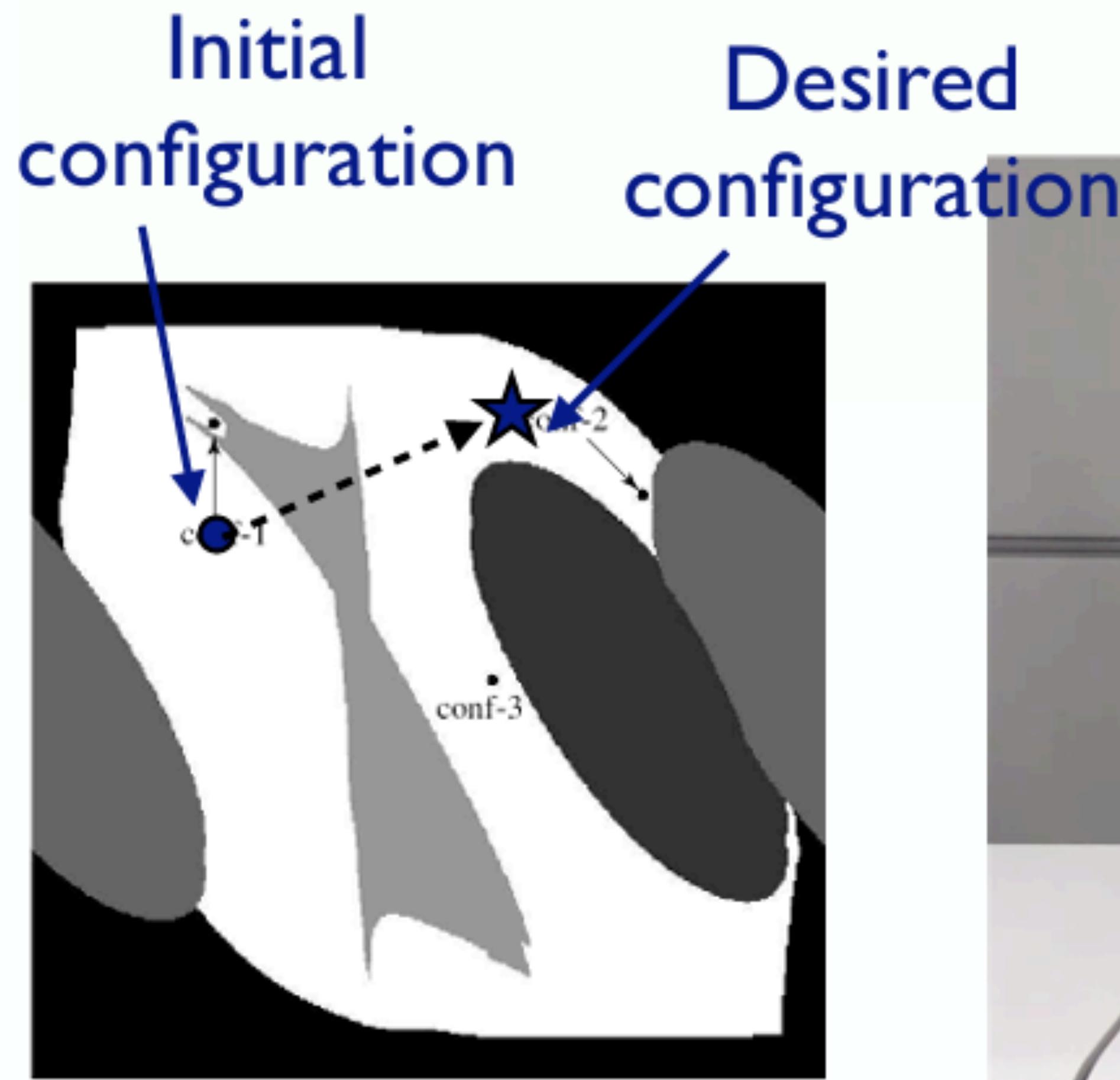
- Task space to Configuration space

Initial
configuration

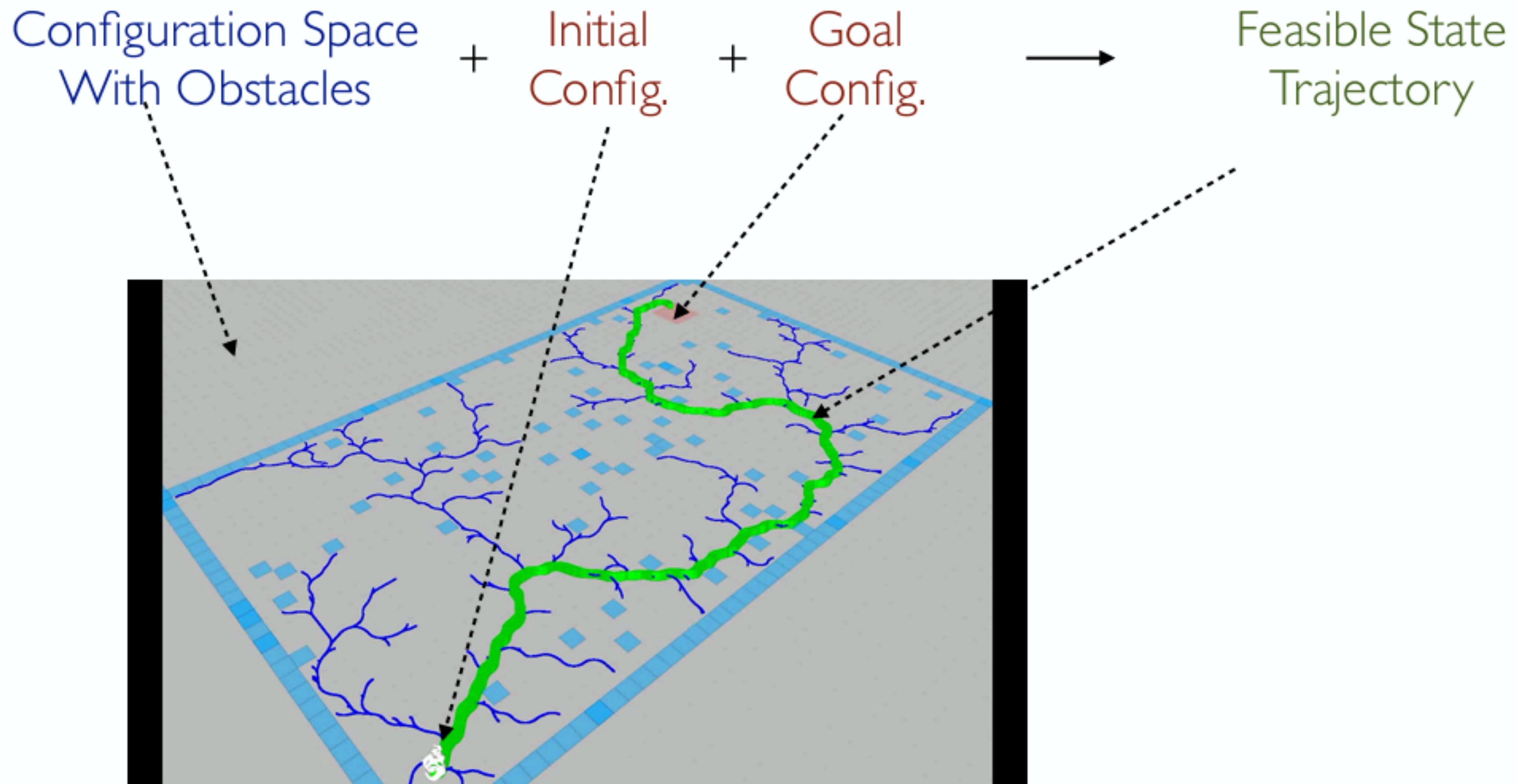


How to move your robot?

- Task space to Configuration space
- Configuration space trajectory



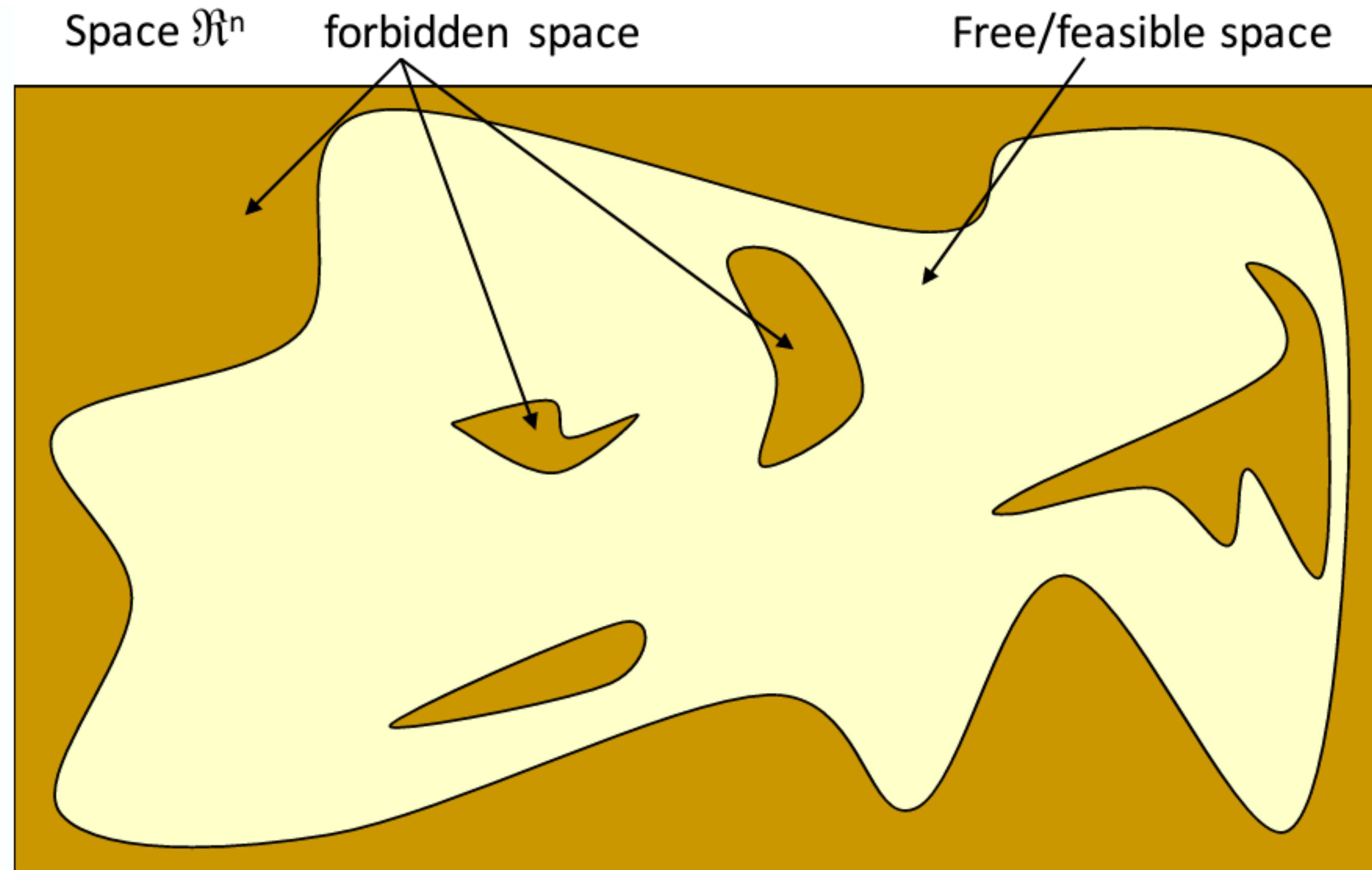
Path Planning



Path Planning

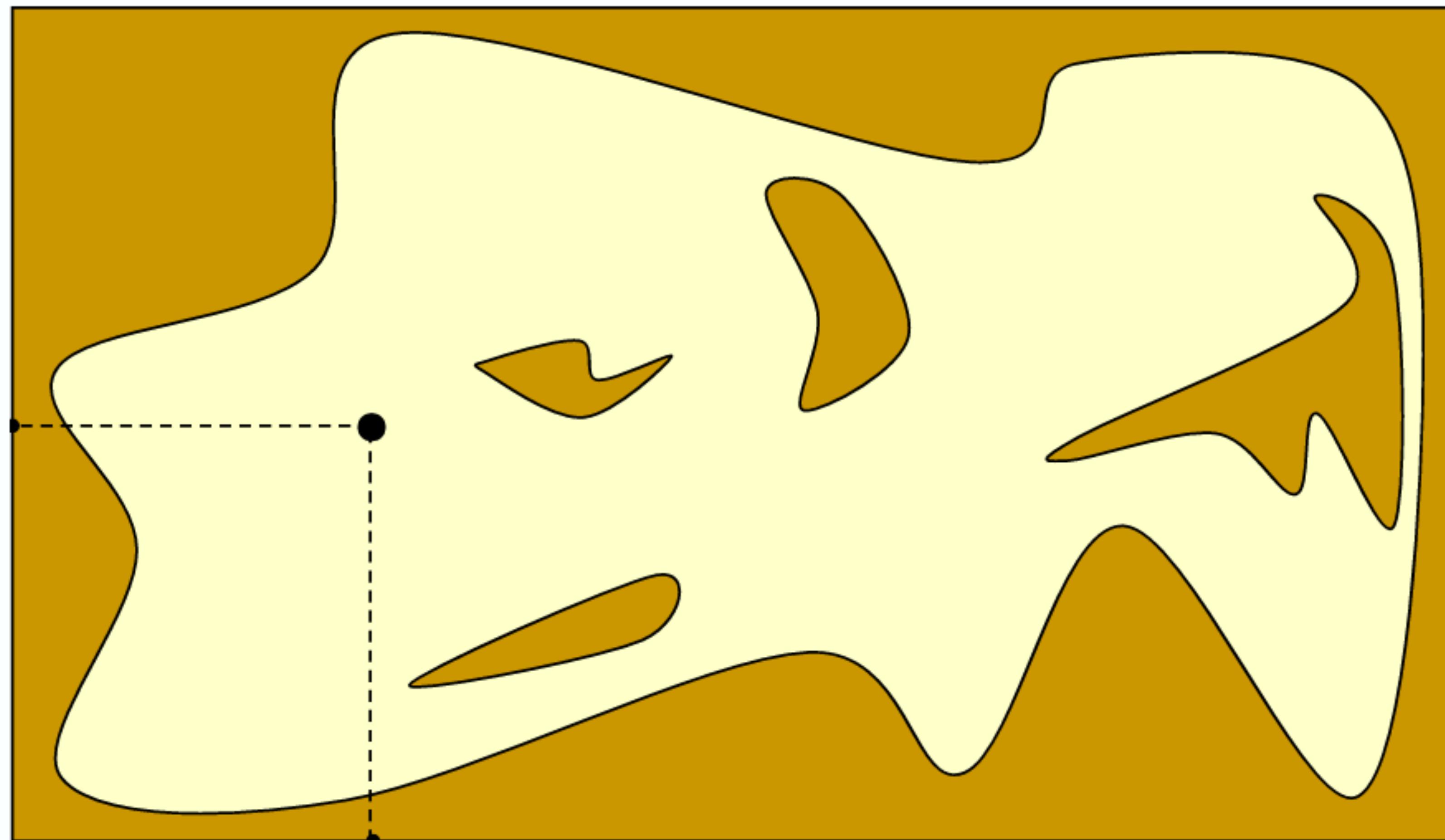
- Complete Methods
- Grid Methods
- Sampling Methods
- Potential Fields
- Trajectory Optimization

Probabilistic Roadmaps



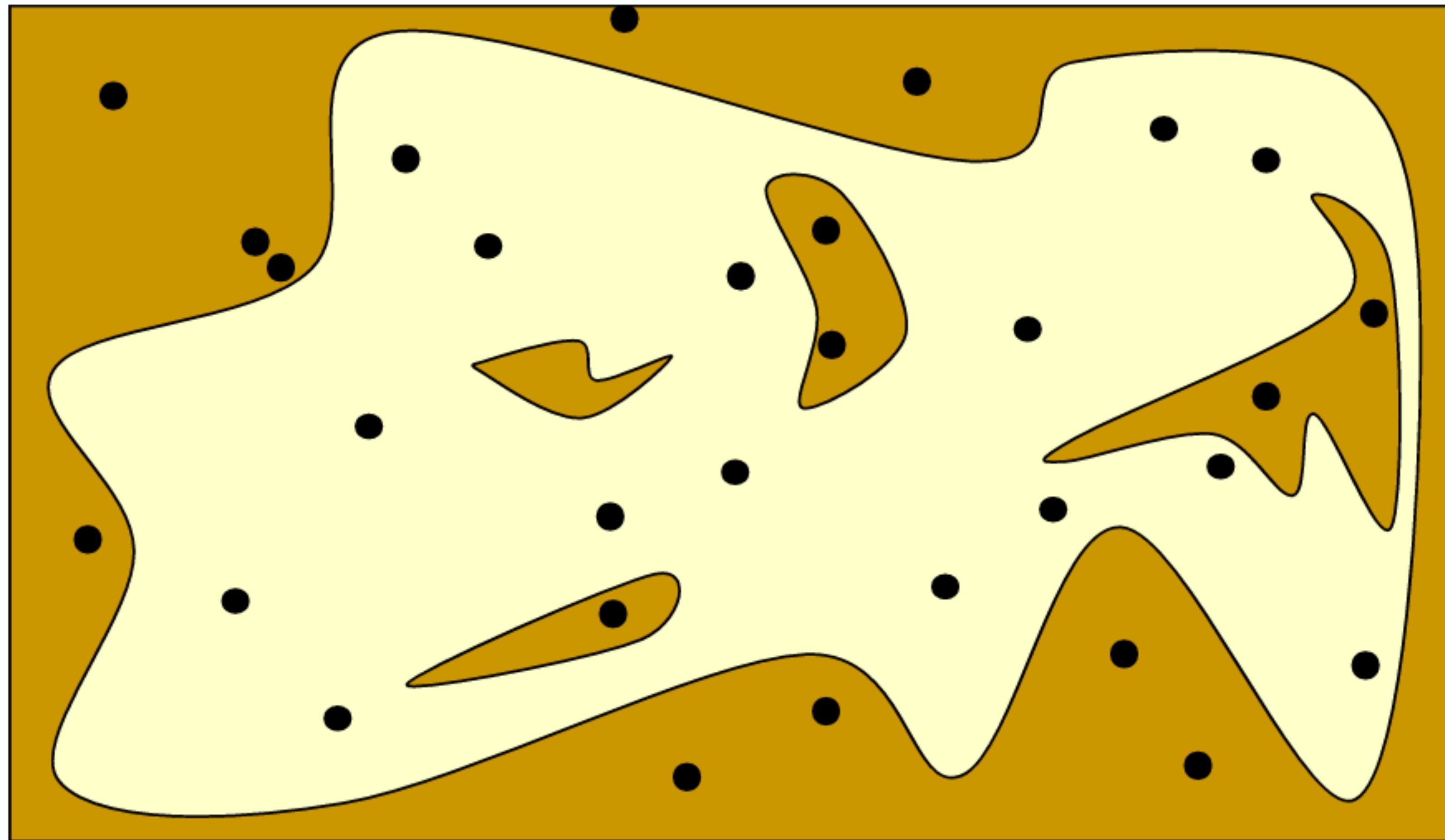
Probabilistic Roadmaps

Randomly Sample Configurations



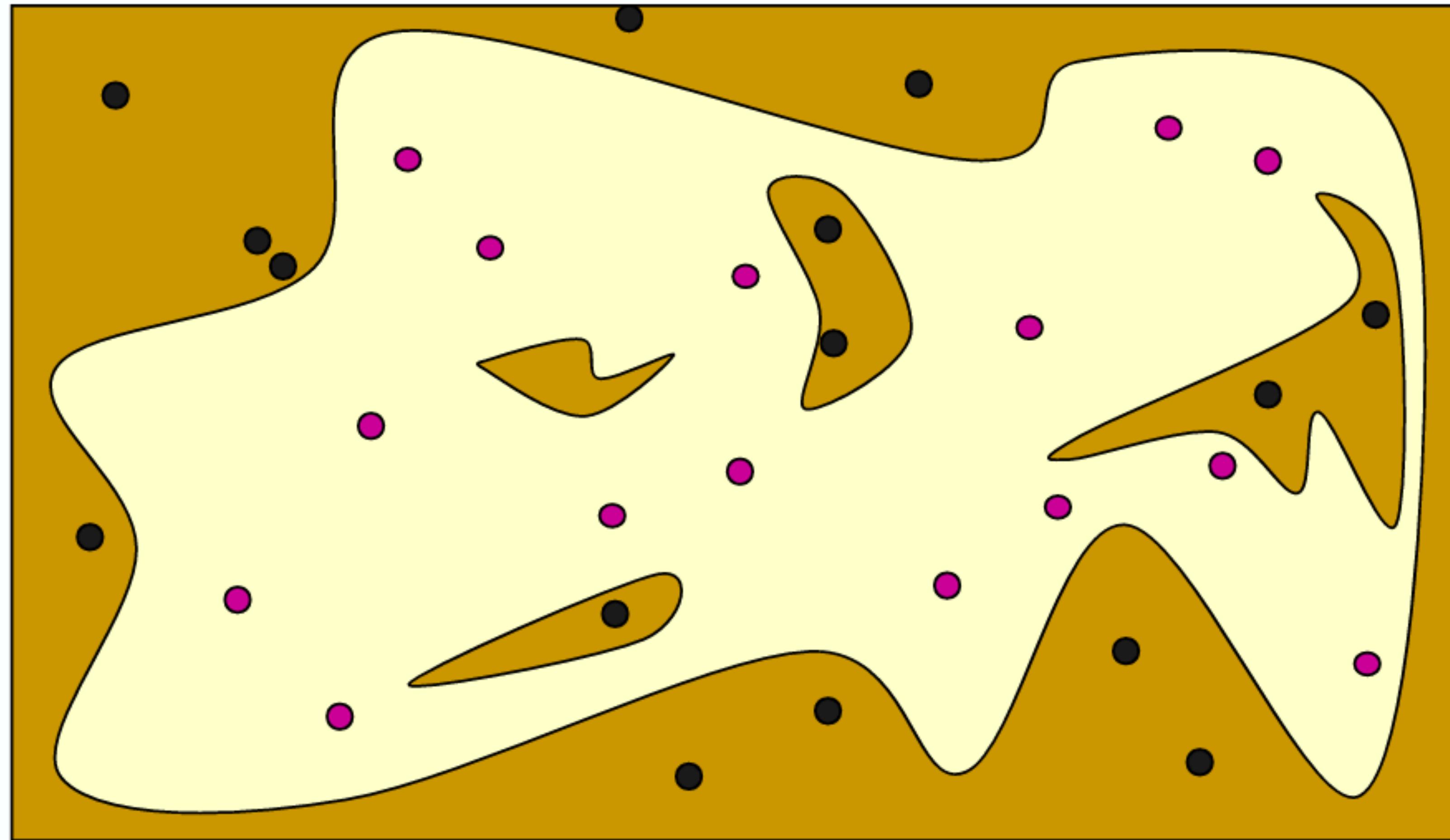
Probabilistic Roadmaps

Randomly Sample Configurations



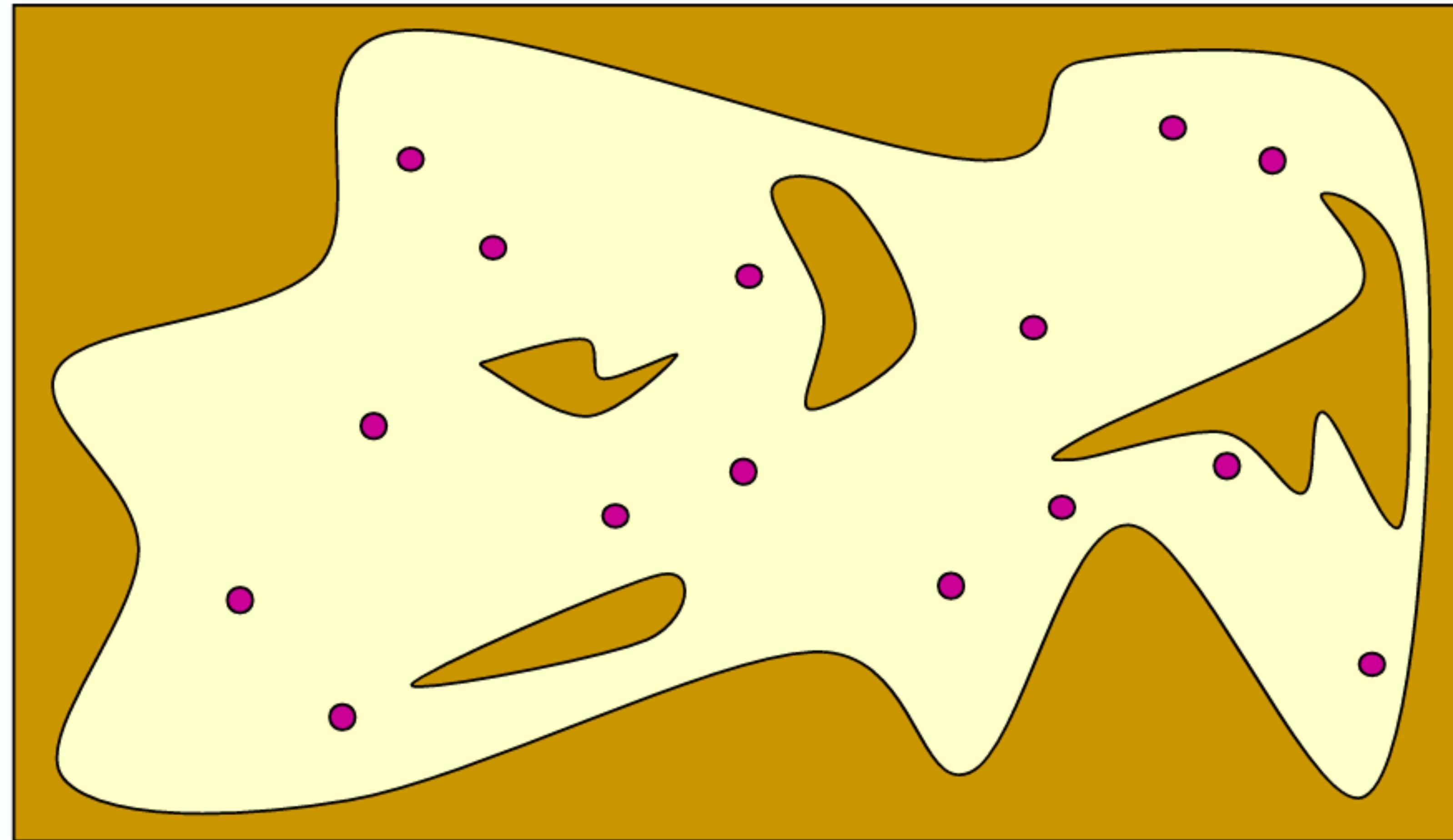
Probabilistic Roadmaps

Test Sampled Configurations for Collisions



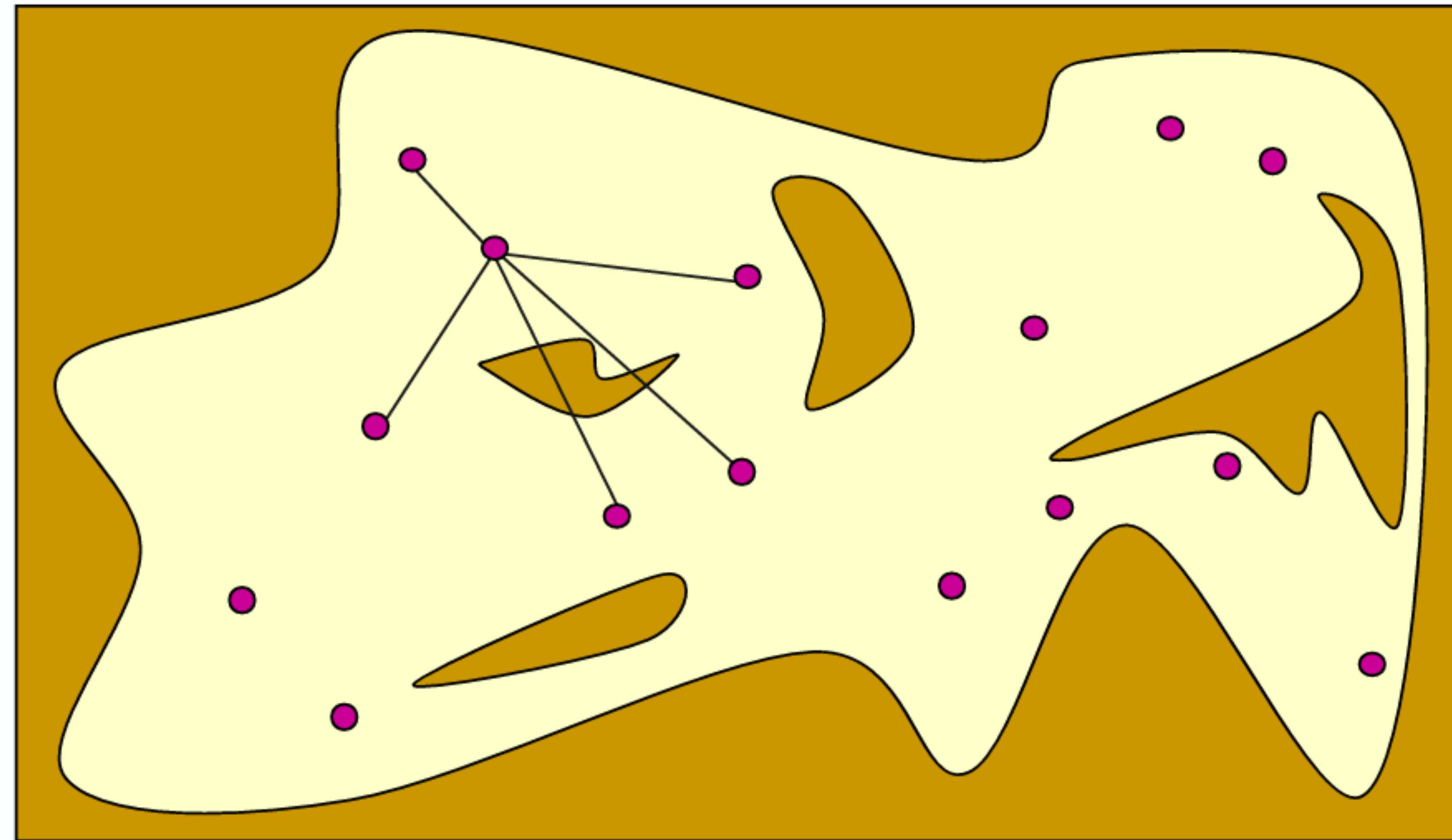
Probabilistic Roadmaps

The collision-free configurations are retained as milestones



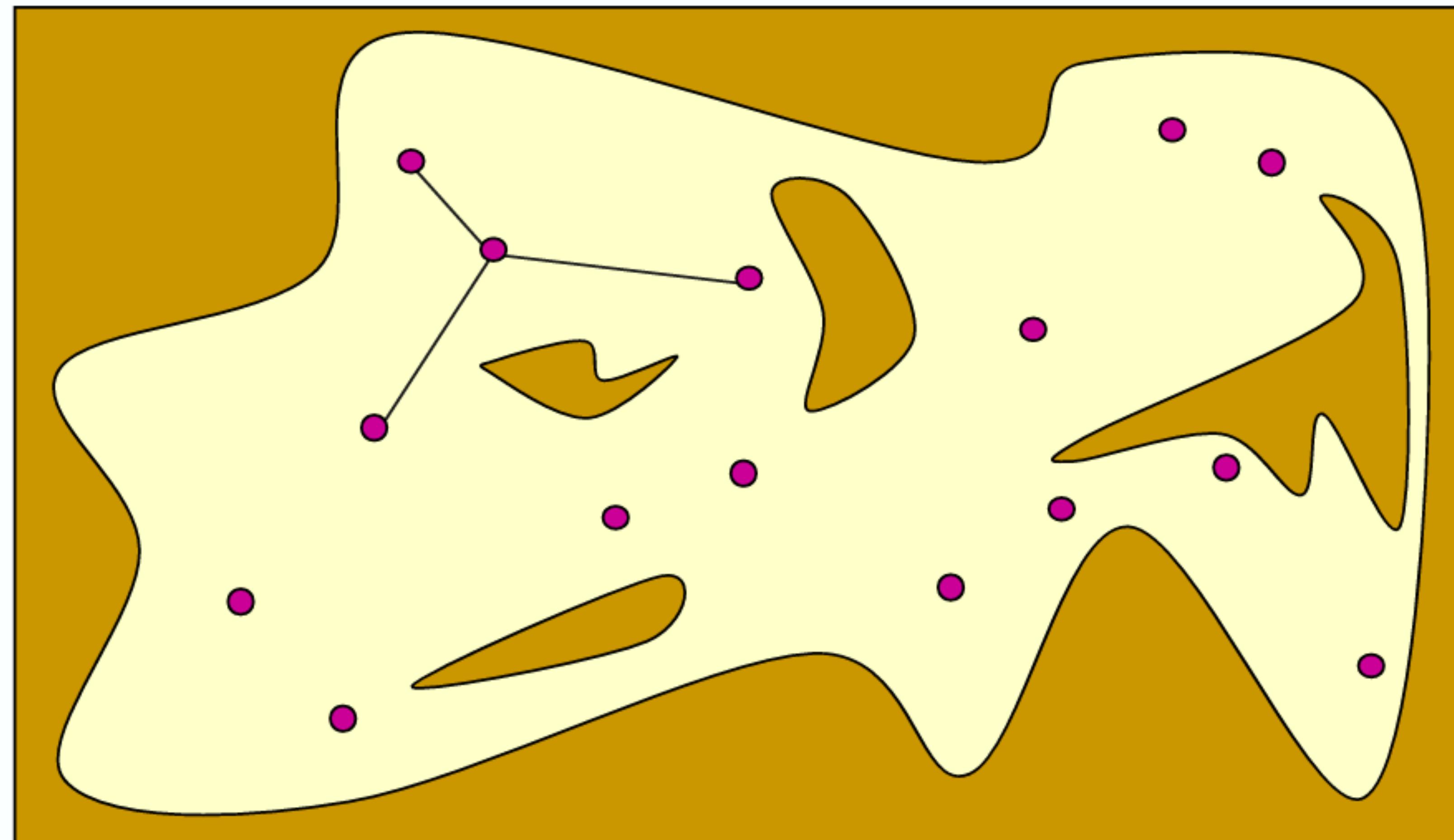
Probabilistic Roadmaps

Each milestone is linked by straight paths to its nearest neighbors



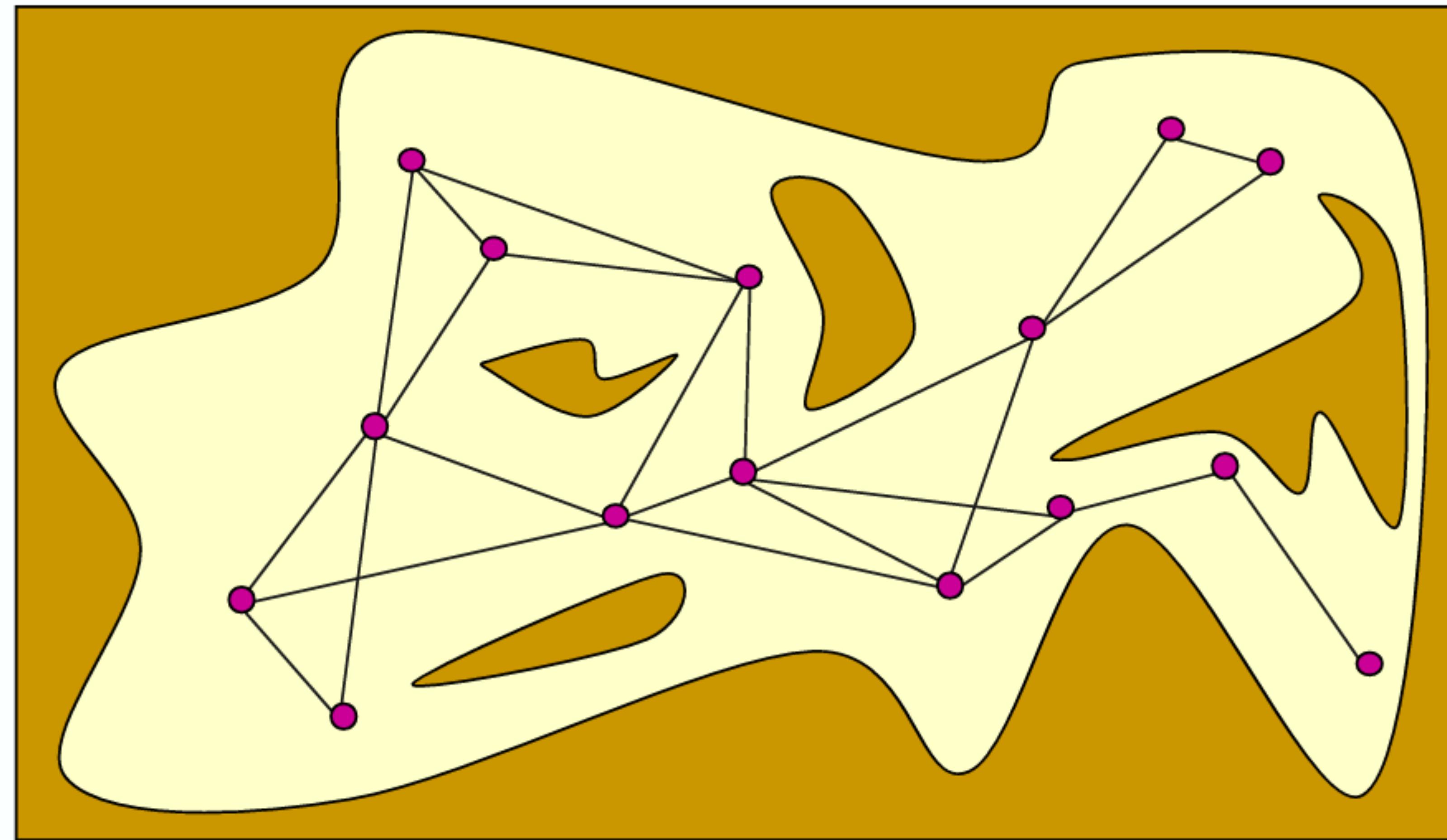
Probabilistic Roadmaps

Paths that undergo collisions are removed



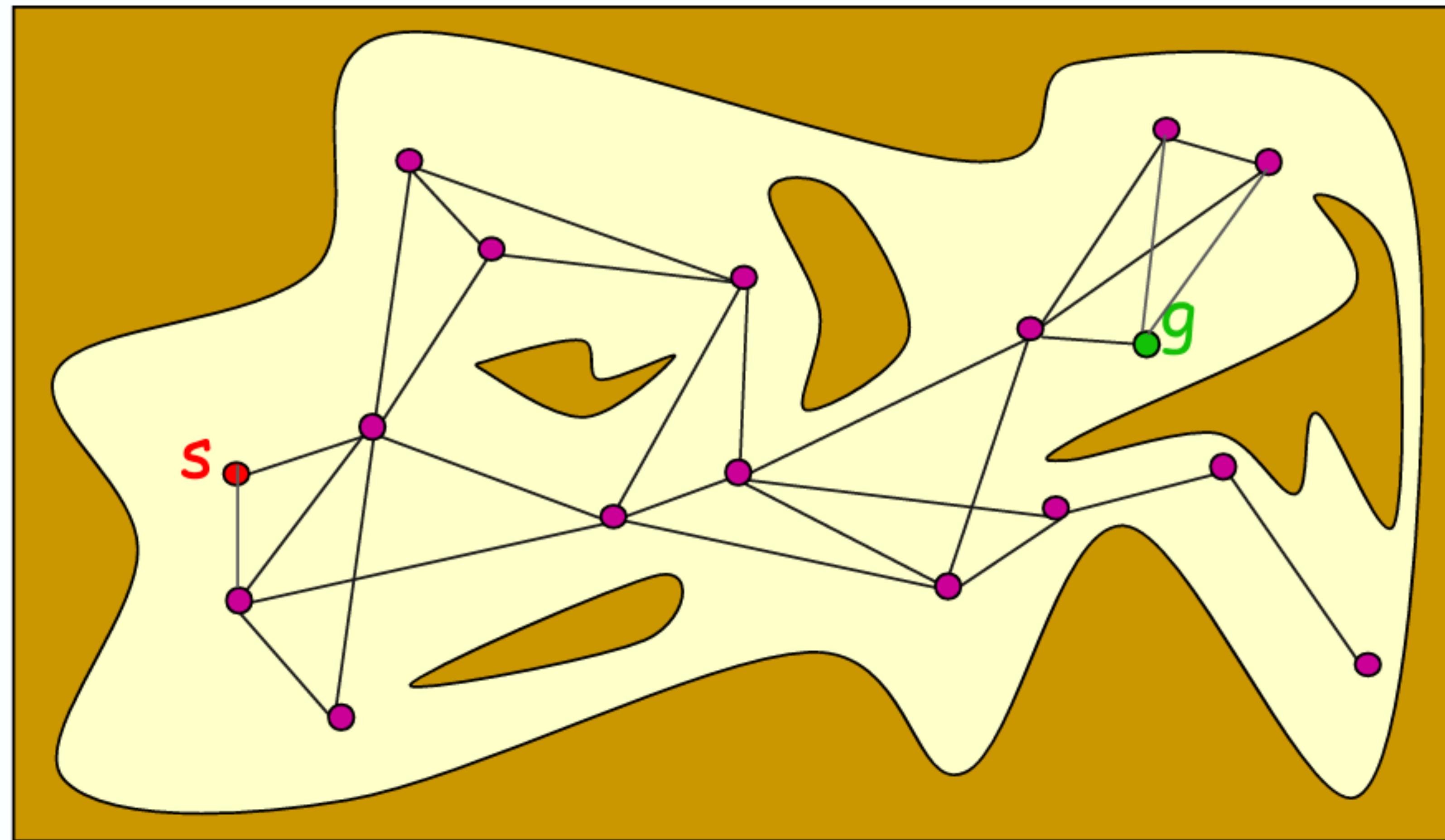
Probabilistic Roadmaps

The collision-free links are retained as local paths to form the PRM



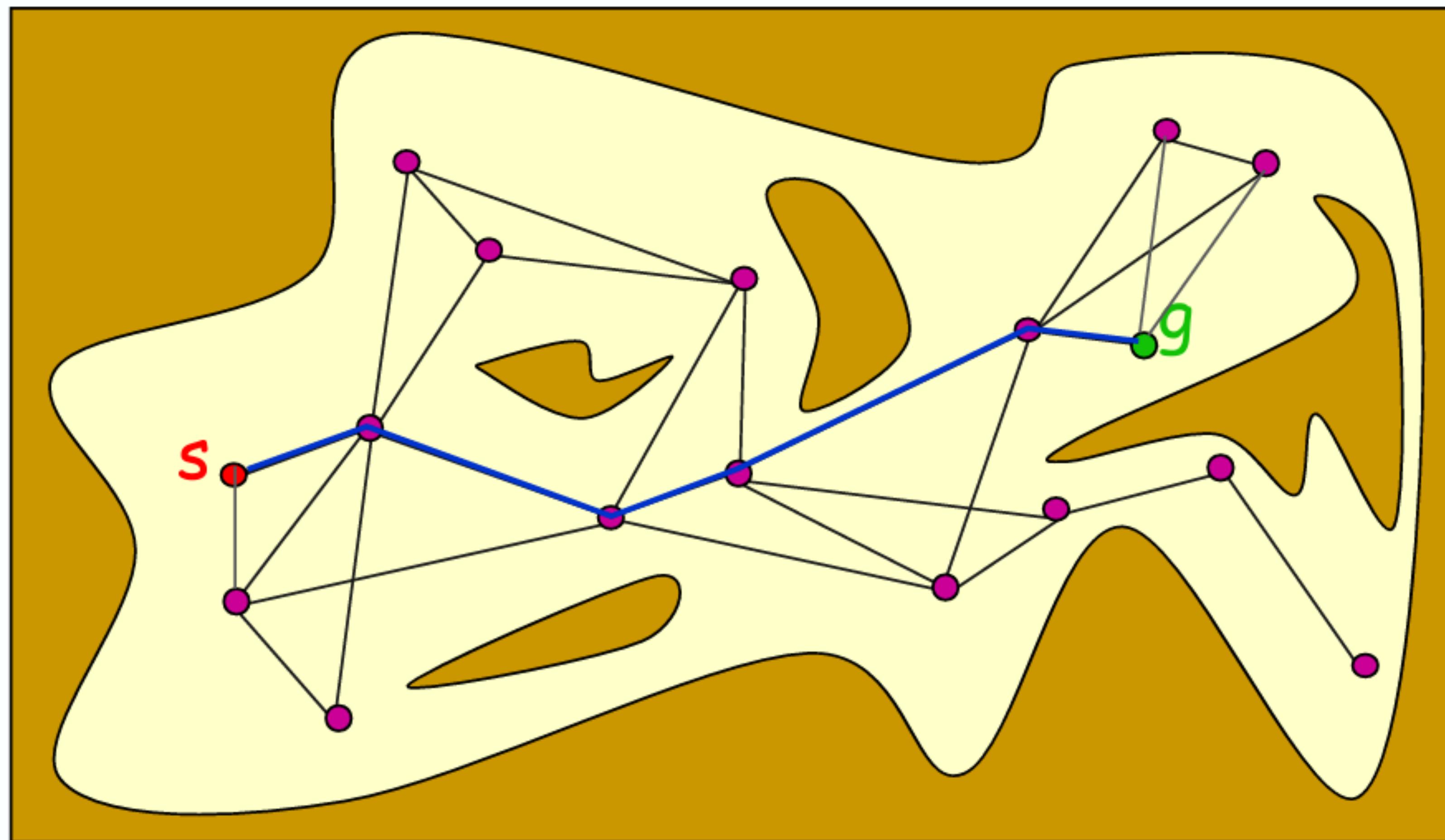
Probabilistic Roadmaps

The start and goal configurations are included as milestones



Probabilistic Roadmaps

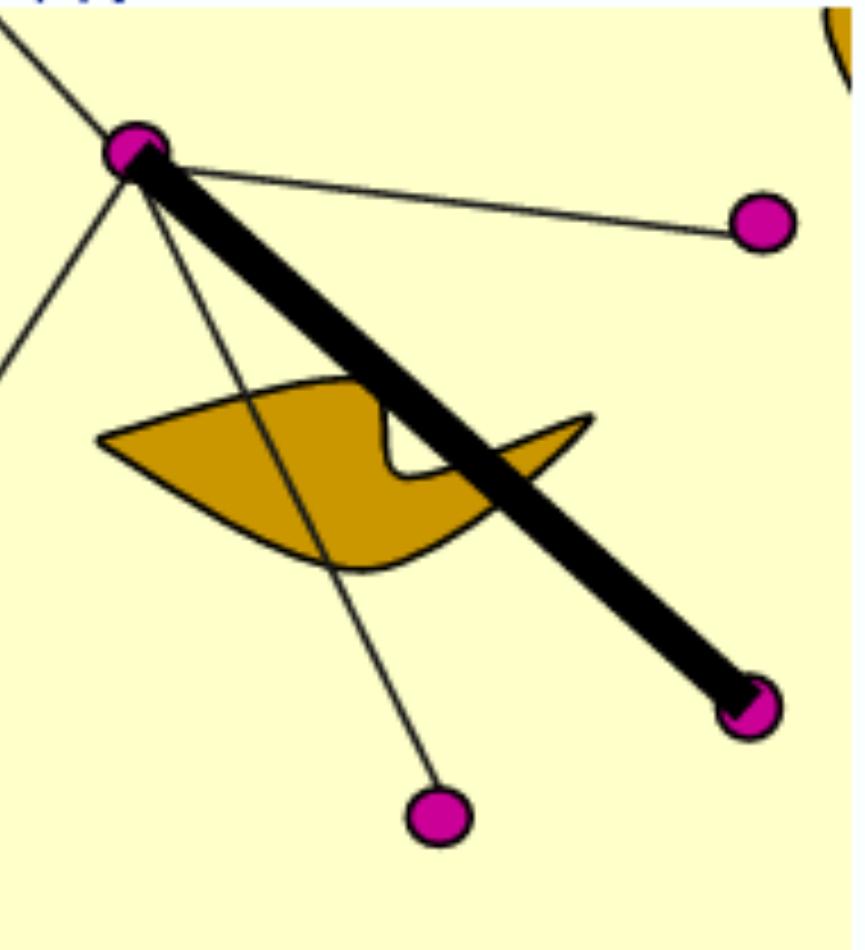
The PRM is searched for a path from s to g



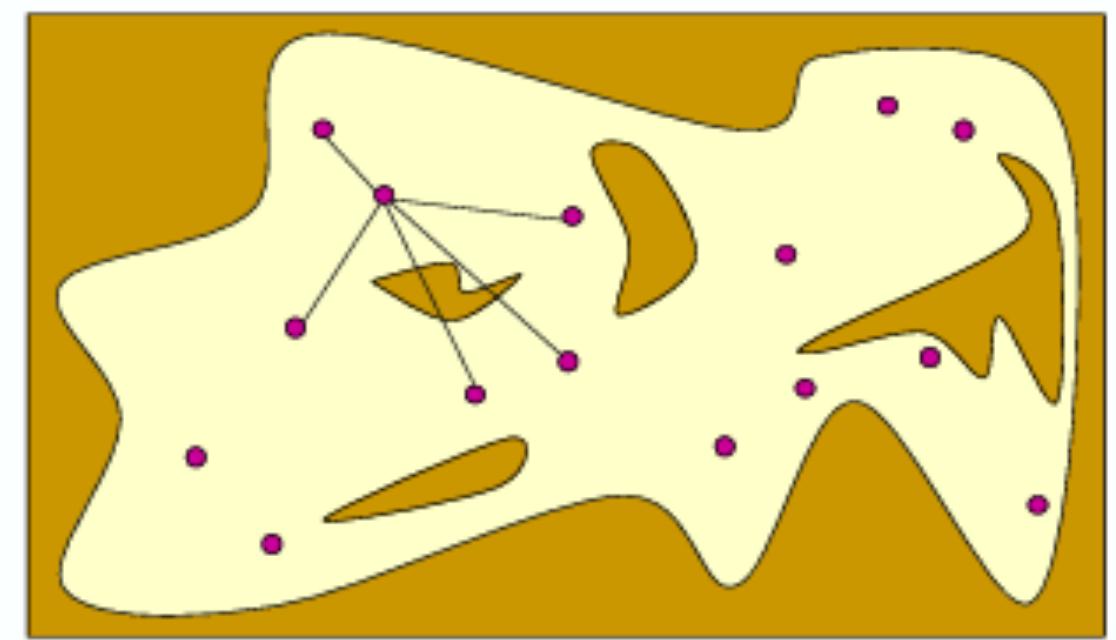
Probabilistic Roadmaps

Challenging to link milestones

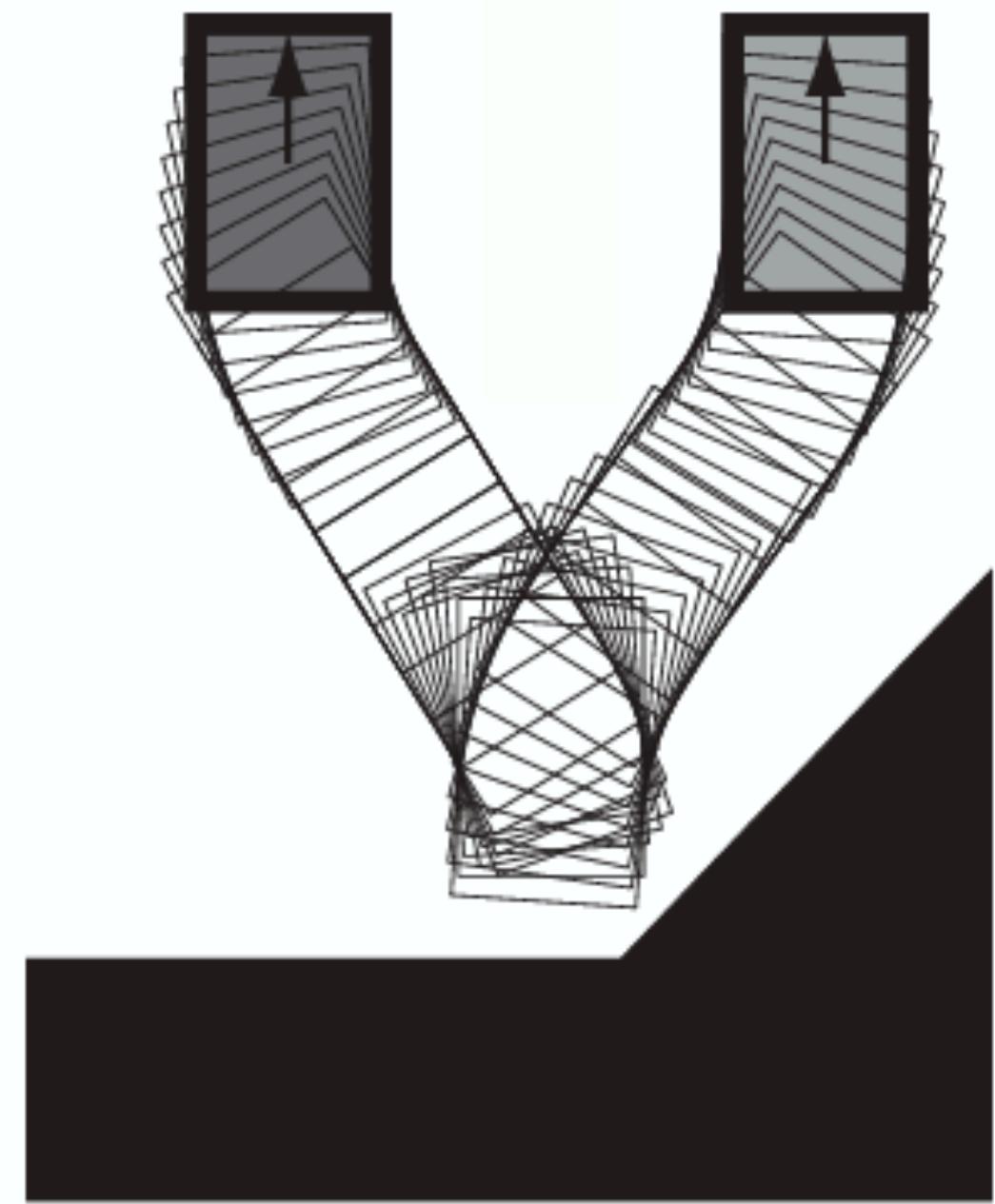
Collision checking can be slow.



All straight line paths may not be feasible, or a good measure of distance between states.

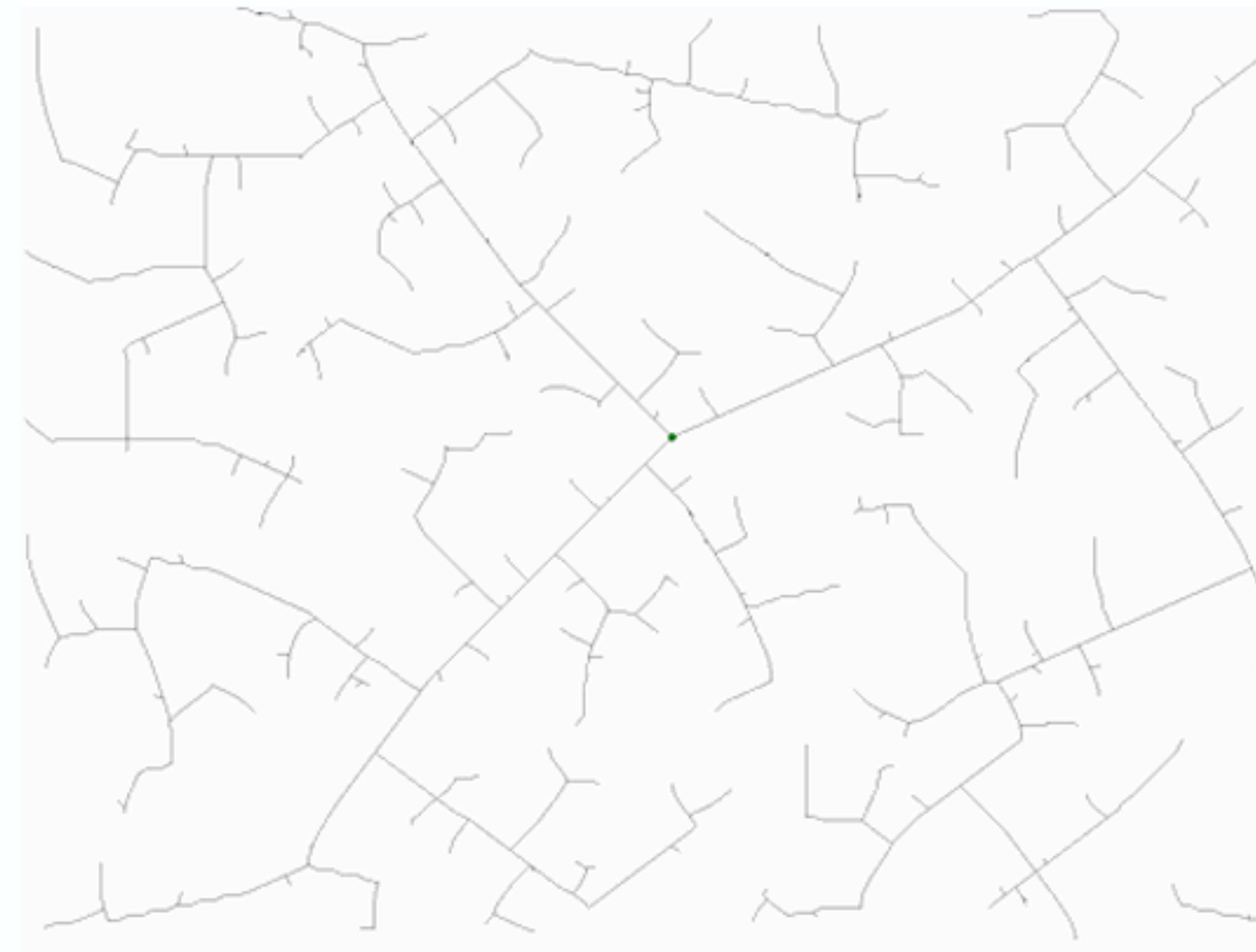


start goal



Rapidly Exploring Random Trees (RRTs)

- Kinodynamic planning
- Build up a tree through generating “next states” in the tree by executing random controls



Rapidly Exploring Random Trees (RRTs)

- Build up a tree through generating “next states” in the tree by executing random controls

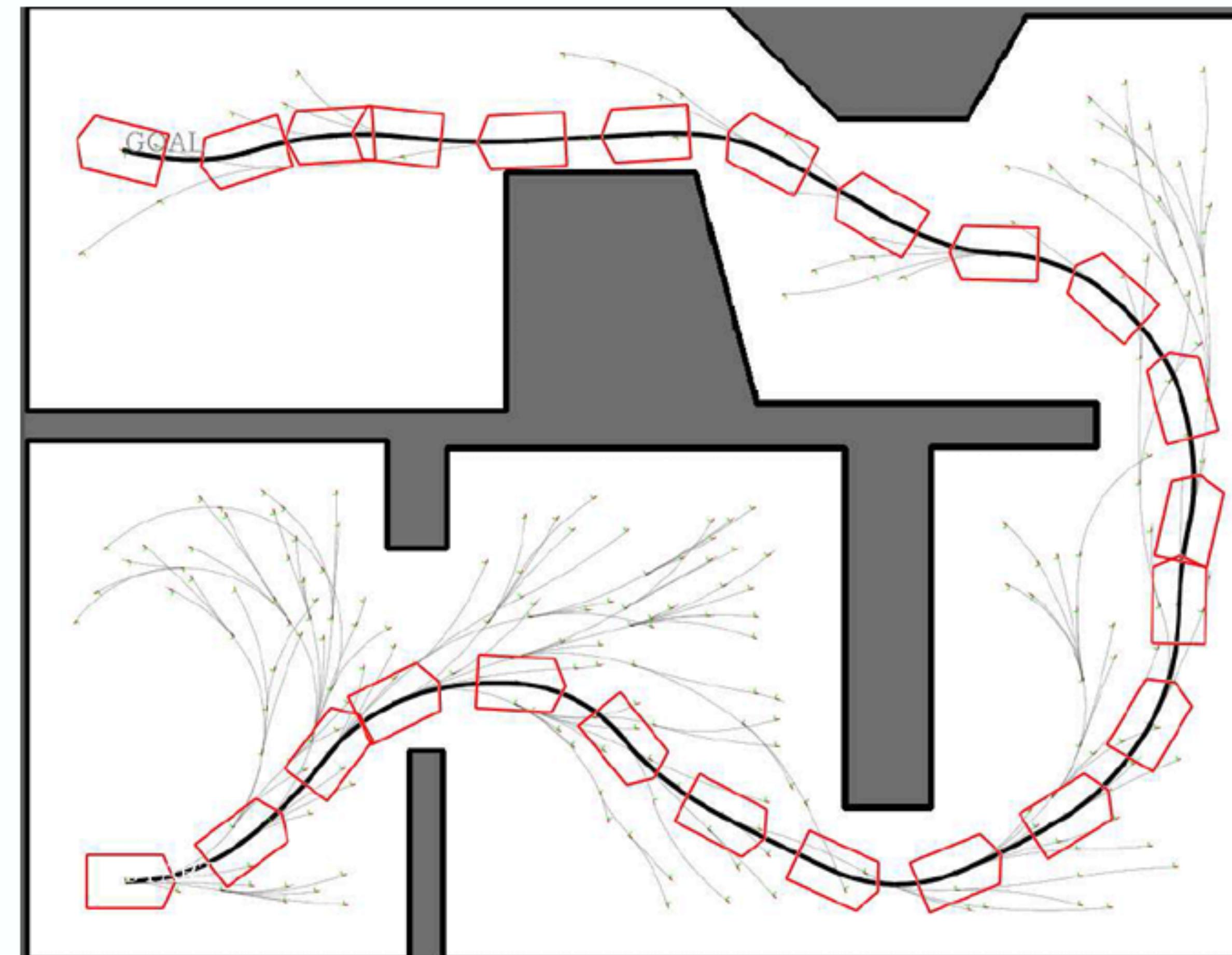
```
GENERATE_RRT( $x_{init}$ ,  $K$ ,  $\Delta t$ )
1    $\mathcal{T}.\text{init}(x_{init})$ ;
2   for  $k = 1$  to  $K$  do
3        $x_{rand} \leftarrow \text{RANDOM\_STATE}()$ ;
4        $x_{near} \leftarrow \text{NEAREST\_NEIGHBOR}(x_{rand}, \mathcal{T})$ ;
5        $u \leftarrow \text{SELECT\_INPUT}(x_{rand}, x_{near})$ ;
6        $x_{new} \leftarrow \text{NEW\_STATE}(x_{near}, u, \Delta t)$ ;
7        $\mathcal{T}.\text{add\_vertex}(x_{new})$ ;
8        $\mathcal{T}.\text{add\_edge}(x_{near}, x_{new}, u)$ ;
9   Return  $\mathcal{T}$ 
```

SELECT_INPUT(x_{rand} , x_{near})

- Two point boundary value problem
 - If too hard to solve, often just select best out of a set of control sequences.
This set could be random, or some well chosen set of primitives.

Rapidly Exploring Random Trees (RRTs)

- Build up a tree through generating “next states” in the tree by executing random controls



tree type

Random Tree RRT RRT*

obstacle type

narrow passage

number of nodes to add:

1 10 100 200 500

exploration bias

0.

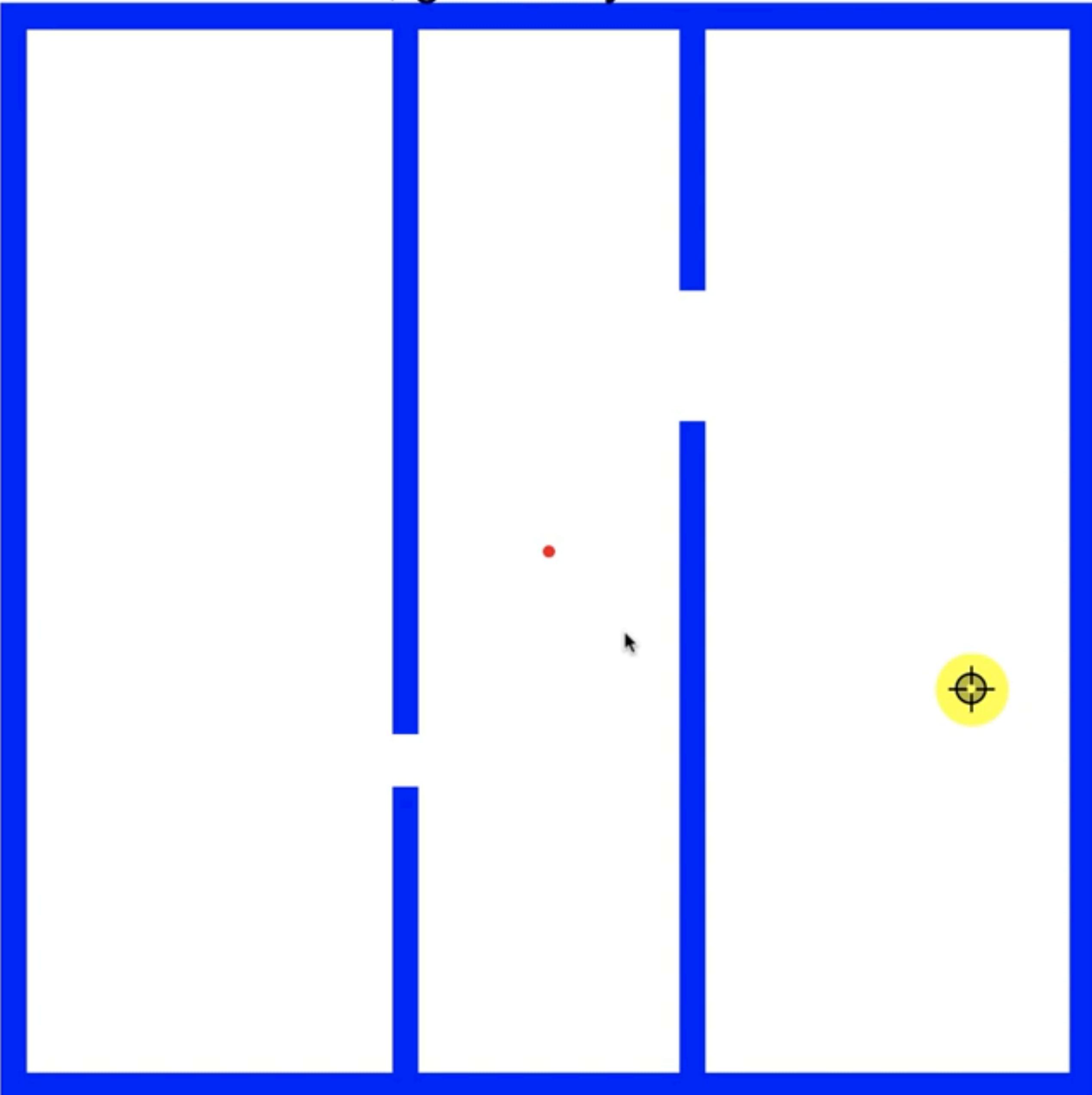
goal radius

1.4

code at
demonstrations.
[wolfram.com/
RapidlyExploring
RandomTree
RRTAndRRT/](http://wolfram.com/RapidlyExploringRandomTreeRRTAndRRT/)

by Aaron Becker
and Li Huang

1 node, goal not yet reached



tree type

Random Tree RRT RRT*

obstacle type

narrow passage

number of nodes to add:

1 10 100 200 500

exploration bias

0.

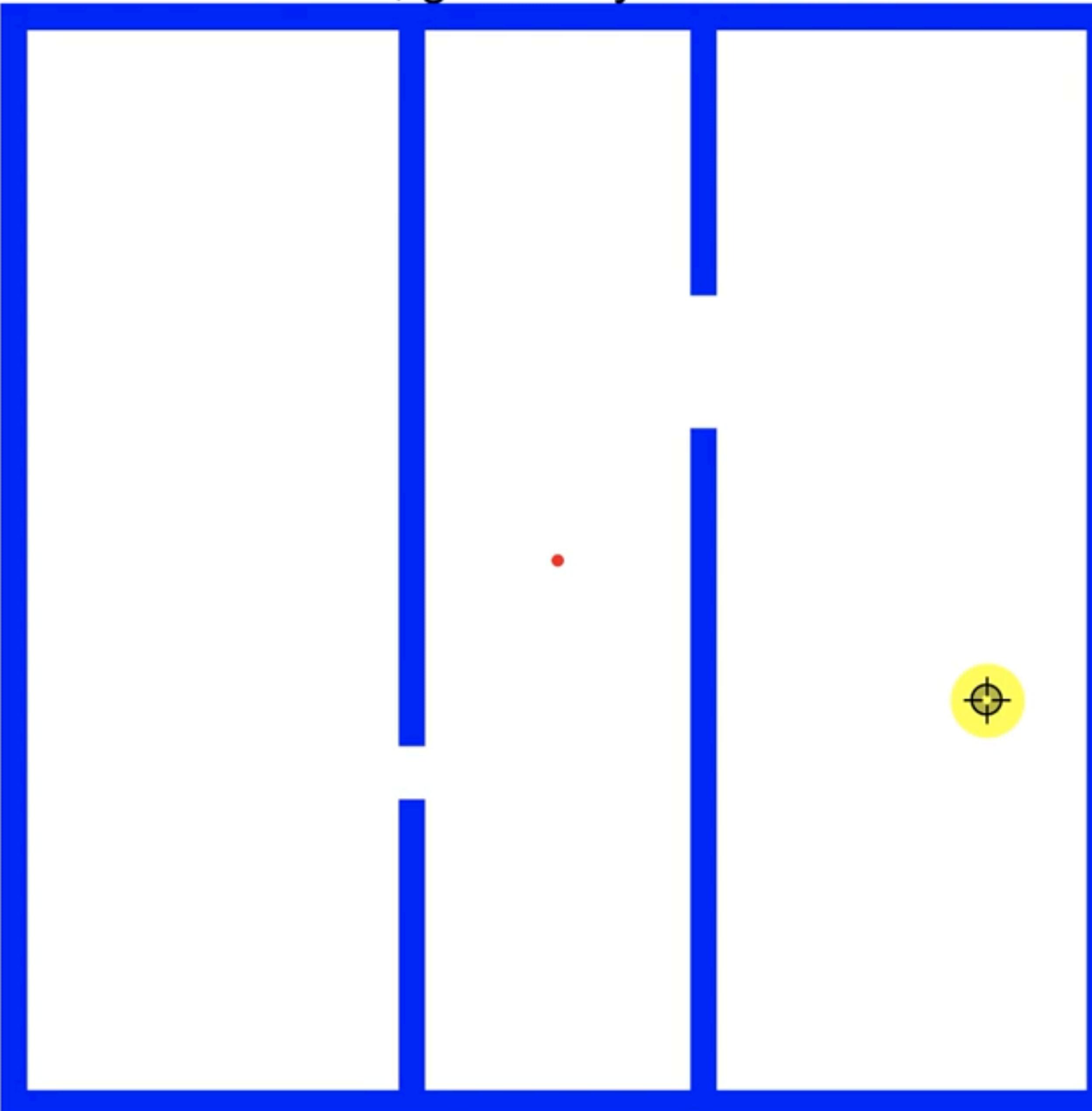
goal radius

1.4

```
Algorithm BuildRRT
  Input: Initial configuration  $q_{init}$ ,
         number of vertices in RRT  $K$ ,
         incremental distance  $\Delta q$ )
  Output: RRT graph  $G$ 

   $G.init(q_{init})$ 
  for  $k = 1$  to  $K$ 
     $q_{rand} \leftarrow RAND\_CONF()$ 
     $q_{near} \leftarrow NEAREST\_VERTEX(q_{rand}, G)$ 
     $q_{new} \leftarrow NEW\_CONF(q_{near}, q_{rand}, \Delta q)$ 
     $G.add\_vertex(q_{new})$ 
     $G.add\_edge(q_{near}, q_{new})$ 
  return  $G$ 
```

1 node, goal not yet reached



tree type

Random Tree RRT RRT*

obstacle type

narrow passage

number of nodes to add:

1 10 100 200 500

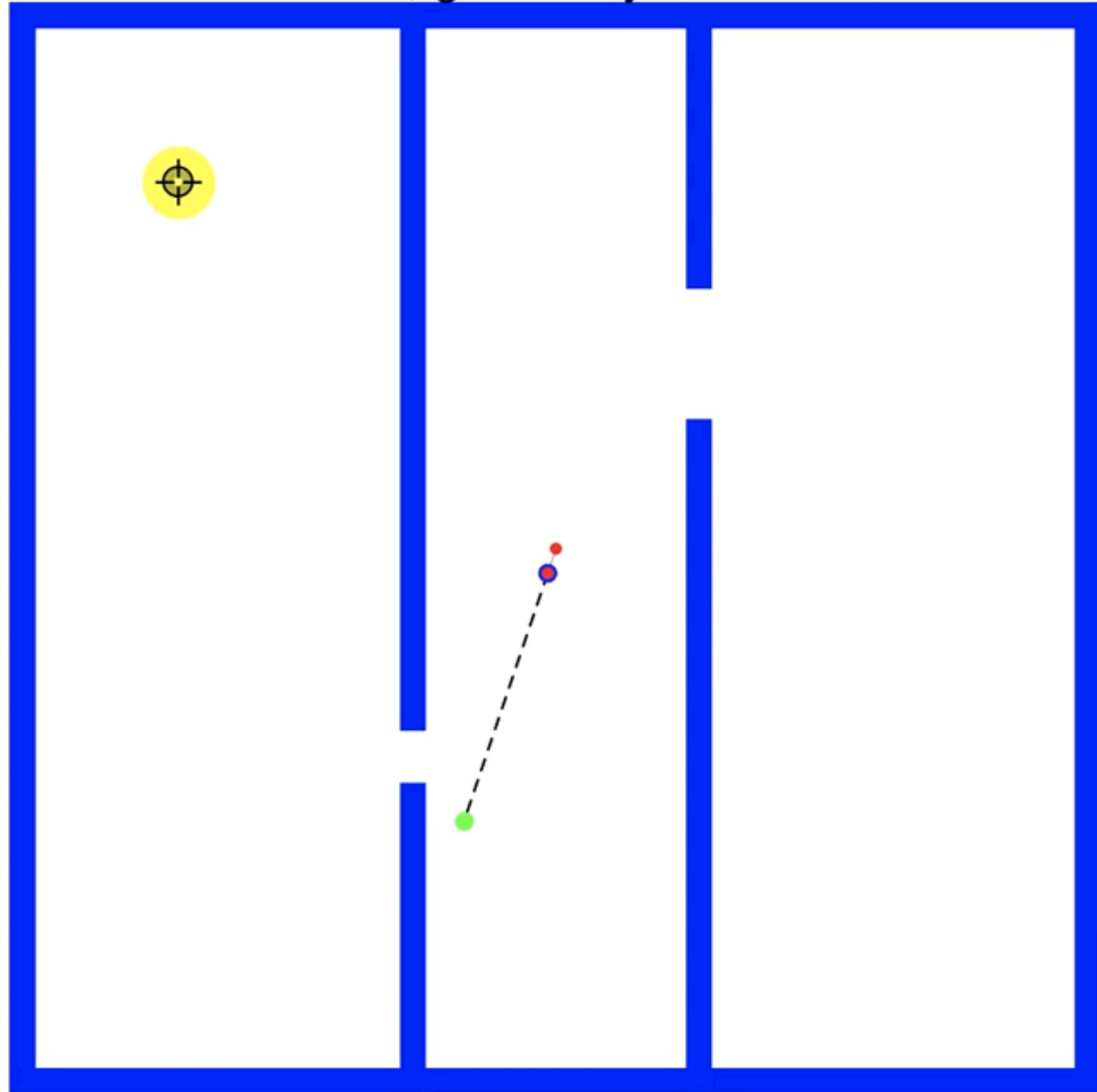
exploration bias

0.

goal radius

1.4

2 nodes, goal not yet reached



tree type

Random Tree RRT RRT*

obstacle type

none

number of nodes to add:

1 10 100 200 500

exploration bias

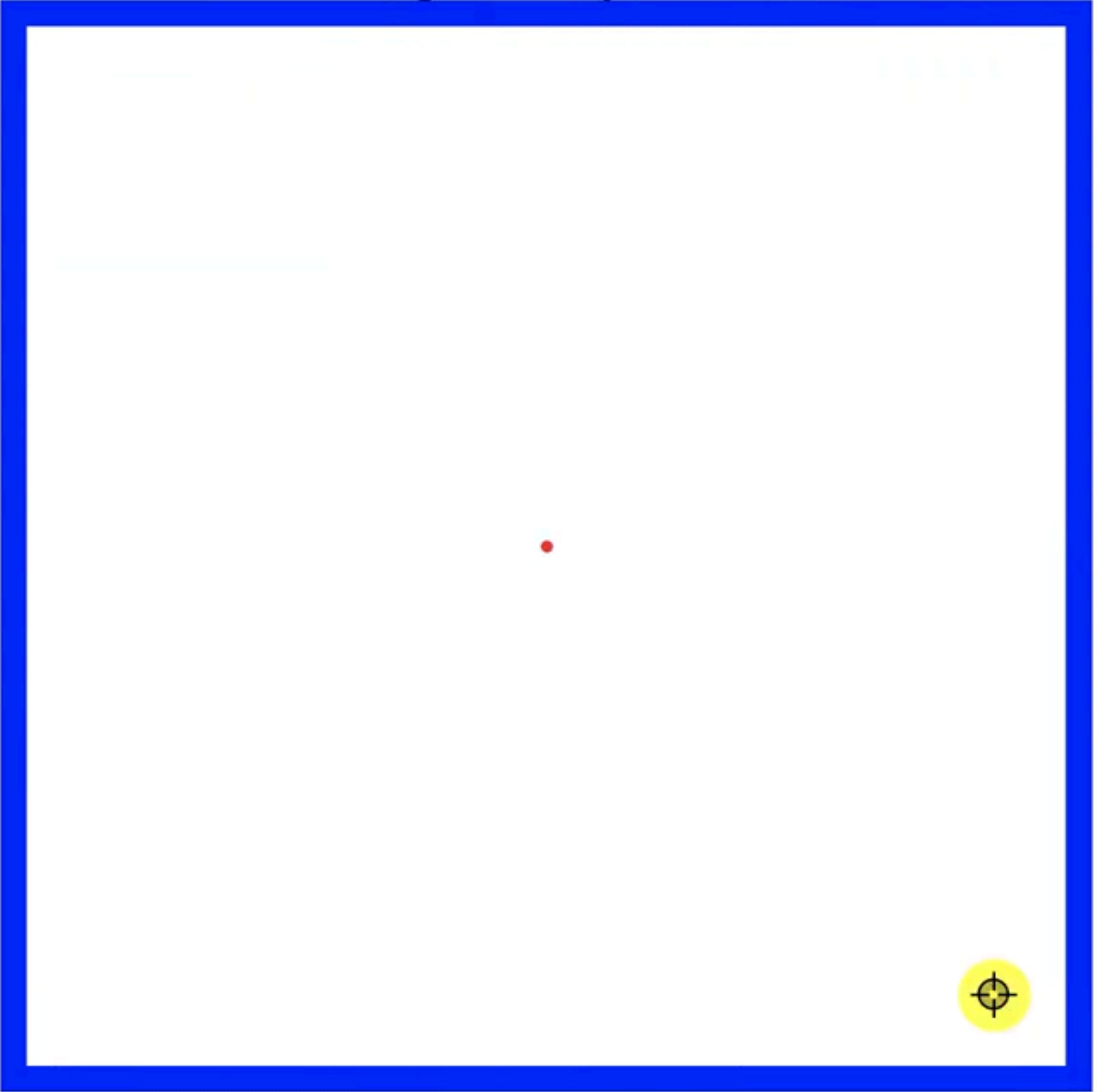
0.

goal radius

1.4

All three trees are *probabilistically complete*, meaning if a nonzero width path exists, the tree will eventually find the path.

1 node, goal not yet reached



tree type

Random Tree RRT RRT*

obstacle type

sparse

number of nodes to add:

1 10 100 200 500

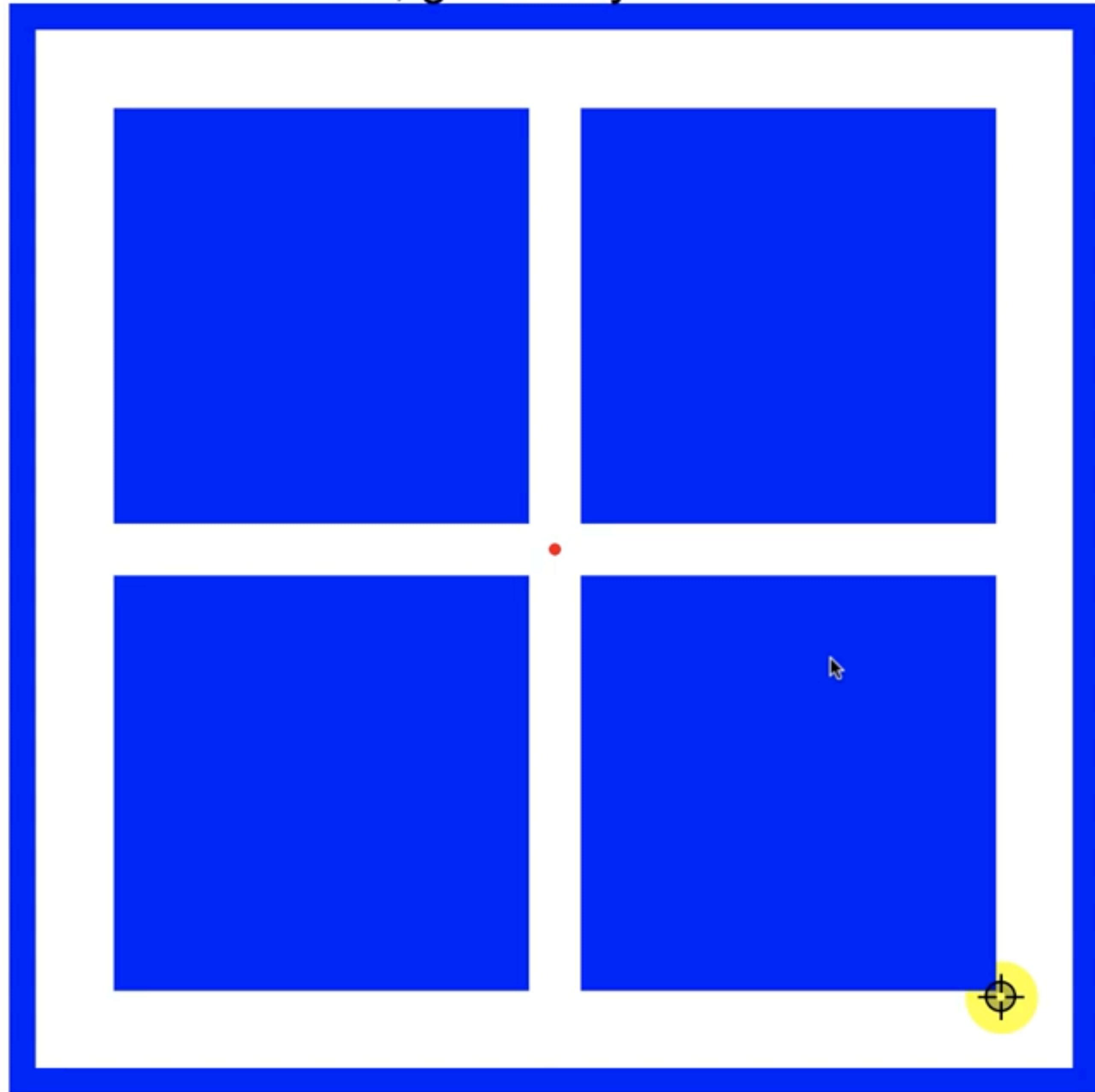
exploration bias

0.

goal radius

1.4

1 node, goal not yet reached



tree type

Random Tree RRT RRT*

obstacle type

concave

number of nodes to add:

1 10 100 200 500

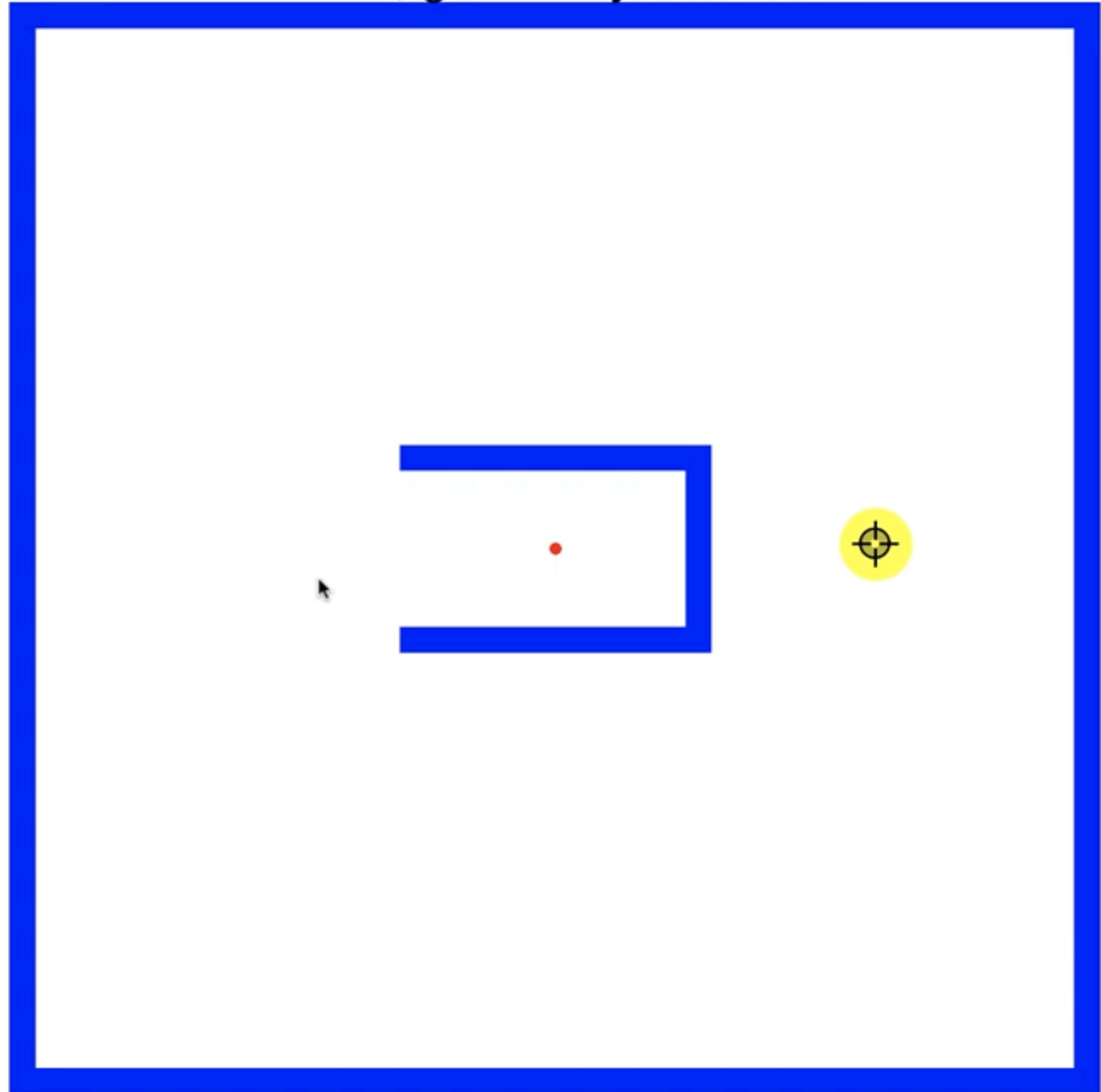
exploration bias

0.5

goal radius

1.4

1 node, goal not yet reached



Today's Agenda

- Robotic Tasks - Manipulation
- Terminology
- Observation and camera calibration
- How to move your robot?
 - Task space & configuration space
 - Forward kinematics and inverse kinematics
 - Path planning