

I. PREDICTION

1. state

2. state variance/covariance

II. UPDATE

3. state

4. state variance/covariance

prediction
measurement
update

single state

$$\begin{aligned}\mu_1 &= A \mu_{fused} + Bu \\ \sigma_1^2 &= A \sigma_{fused}^2 A + Q \\ &= A^2 \sigma_{fused}^2 + Q\end{aligned}$$

from previous time

$$\begin{aligned}\mu_{fused} &= \mu_1 + K(\mu_2 - C\mu_1) \\ &= \sigma_1^2 C (C\sigma_1^2 C + \sigma_2^2)^{-1} \\ &= \frac{C\sigma_1^2}{C^2\sigma_1^2 + \sigma_2^2}\end{aligned}$$

$$\sigma_{fused}^2 = (1 - KC)\sigma_1^2$$

multiple states

$$\begin{aligned}\hat{\mathbf{x}}_{k|k-1} &= A \hat{\mathbf{x}}_{k-1|k-1} + B\mathbf{u}_{k-1} \\ \mathbf{P}_{k|k-1} &= A \mathbf{P}_{k-1|k-1} A^T + \mathbf{Q}_k\end{aligned}$$

from previous time

$$\begin{aligned}\hat{\mathbf{x}}_{k|k} &= \hat{\mathbf{x}}_{k|k-1} + \mathbf{K}_k \left(\mathbf{y}_k - C\hat{\mathbf{x}}_{k|k-1} \right) \\ &= \mathbf{P}_{k|k-1} C^T \left(C\mathbf{P}_{k|k-1} C^T + \mathbf{R}_k \right)^{-1}\end{aligned}$$

innovation: measurement
innovation: covariance

$$\mathbf{P}_{k|k} = (\mathbf{I} - \mathbf{K}_k C) \mathbf{P}_{k|k-1}$$