

$$\begin{aligned}
\overset{\text{posterior}}{p(x_k | Z_k)} &= \frac{p(x_k, Z_k)}{p(Z_k)} \\
&= \frac{p(x_k, z_k, Z_{k-1})}{p(z_k, Z_{k-1})} \\
&= \frac{p(z_k | x_k, Z_{k-1}) p(x_k, Z_{k-1})}{p(z_k | Z_{k-1}) p(Z_{k-1})} \\
&= \frac{p(z_k | x_k) p(x_k | Z_{k-1}) \cancel{p(Z_{k-1})}}{p(z_k | Z_{k-1}) \cancel{p(Z_{k-1})}} \\
&= \frac{\overset{\text{likelihood}}{p(z_k | x_k)} \overset{\text{prior (prediction)}}{p(x_k | Z_{k-1})}}{\int p(z_k | x_k) p(x_k | Z_{k-1}) dx_k}
\end{aligned}$$